

Mathematica 11.3 Integration Test Results

on the problems in the test-suite directory "3 Logarithms"

Test results for the 193 problems in "3.1.2 (d x)^m (a+b log(c x^n))^p.m"

Problem 54: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2}{x} dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^3}{3 b n}$$

Result (type 3, 46 leaves):

$$\frac{a^2 \operatorname{Log}[c x^n]}{n} + \frac{a b \operatorname{Log}[c x^n]^2}{n} + \frac{b^2 \operatorname{Log}[c x^n]^3}{3 n}$$

Problem 61: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3}{x} dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^4}{4 b n}$$

Result (type 3, 67 leaves):

$$\frac{a^3 \operatorname{Log}[c x^n]}{n} + \frac{3 a^2 b \operatorname{Log}[c x^n]^2}{2 n} + \frac{a b^2 \operatorname{Log}[c x^n]^3}{n} + \frac{b^3 \operatorname{Log}[c x^n]^4}{4 n}$$

Test results for the 456 problems in "3.1.4 (f x)^m (d+e x^r)^q (a+b log(c x^n))^p.m"

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{Log}[c x^n])}{(d + e x)^4} dx$$

Optimal (type 3, 79 leaves, 3 steps):

$$\frac{b d n}{6 e^3 (d + e x)^2} - \frac{2 b n}{3 e^3 (d + e x)} + \frac{x^3 (a + b \operatorname{Log}[c x^n])}{3 d (d + e x)^3} - \frac{b n \operatorname{Log}[d + e x]}{3 d e^3}$$

Result (type 3, 170 leaves):

$$-\frac{1}{6 d e^3 (d + e x)^3} \left(2 a d^3 + 3 b d^3 n + 6 a d^2 e x + 7 b d^2 e n x + 6 a d e^2 x^2 + 4 b d e^2 n x^2 - 2 b n (d + e x)^3 \operatorname{Log}[x] + \right. \\ \left. 2 b d (d^2 + 3 d e x + 3 e^2 x^2) \operatorname{Log}[c x^n] + 2 b d^3 n \operatorname{Log}[d + e x] + 6 b d^2 e n x \operatorname{Log}[d + e x] + 6 b d e^2 n x^2 \operatorname{Log}[d + e x] + 2 b e^3 n x^3 \operatorname{Log}[d + e x] \right)$$

Problem 64: Result more than twice size of optimal antiderivative.

$$\int \frac{x^6 (a + b \operatorname{Log}[c x^n])}{(d + e x)^7} dx$$

Optimal (type 4, 243 leaves, 8 steps):

$$-\frac{x^6 (a + b \operatorname{Log}[c x^n])}{6 e (d + e x)^6} - \frac{x^5 (6 a + b n + 6 b \operatorname{Log}[c x^n])}{30 e^2 (d + e x)^5} - \frac{x^2 (20 a + 19 b n + 20 b \operatorname{Log}[c x^n])}{40 e^5 (d + e x)^2} - \frac{x (20 a + 29 b n + 20 b \operatorname{Log}[c x^n])}{20 e^6 (d + e x)} - \\ \frac{x^4 (30 a + 11 b n + 30 b \operatorname{Log}[c x^n])}{120 e^3 (d + e x)^4} - \frac{x^3 (60 a + 37 b n + 60 b \operatorname{Log}[c x^n])}{180 e^4 (d + e x)^3} + \frac{(20 a + 49 b n + 20 b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x}{d}\right]}{20 e^7} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{e^7}$$

Result (type 4, 673 leaves):

$$\frac{1}{360 e^7 (d + e x)^6} \left(882 a d^6 + 812 b d^6 n + 4932 a d^5 e x + 4350 b d^5 e n x + 11250 a d^4 e^2 x^2 + 9399 b d^4 e^2 n x^2 + \right. \\
13200 a d^3 e^3 x^3 + 10262 b d^3 e^3 n x^3 + 8100 a d^2 e^4 x^4 + 5679 b d^2 e^4 n x^4 + 2160 a d e^5 x^5 + 1278 b d e^5 n x^5 + 882 b d^6 \operatorname{Log}[c x^n] + \\
4932 b d^5 e x \operatorname{Log}[c x^n] + 11250 b d^4 e^2 x^2 \operatorname{Log}[c x^n] + 13200 b d^3 e^3 x^3 \operatorname{Log}[c x^n] + 8100 b d^2 e^4 x^4 \operatorname{Log}[c x^n] + 2160 b d e^5 x^5 \operatorname{Log}[c x^n] + \\
360 a d^6 \operatorname{Log}[d + e x] + 882 b d^6 n \operatorname{Log}[d + e x] + 2160 a d^5 e x \operatorname{Log}[d + e x] + 5292 b d^5 e n x \operatorname{Log}[d + e x] + 5400 a d^4 e^2 x^2 \operatorname{Log}[d + e x] + \\
13230 b d^4 e^2 n x^2 \operatorname{Log}[d + e x] + 7200 a d^3 e^3 x^3 \operatorname{Log}[d + e x] + 17640 b d^3 e^3 n x^3 \operatorname{Log}[d + e x] + 5400 a d^2 e^4 x^4 \operatorname{Log}[d + e x] + \\
13230 b d^2 e^4 n x^4 \operatorname{Log}[d + e x] + 2160 a d e^5 x^5 \operatorname{Log}[d + e x] + 5292 b d e^5 n x^5 \operatorname{Log}[d + e x] + 360 a e^6 x^6 \operatorname{Log}[d + e x] + \\
882 b e^6 n x^6 \operatorname{Log}[d + e x] + 360 b d^6 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 2160 b d^5 e x \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 5400 b d^4 e^2 x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + \\
7200 b d^3 e^3 x^3 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 5400 b d^2 e^4 x^4 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 2160 b d e^5 x^5 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + \\
\left. 360 b e^6 x^6 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] - 18 b n (d + e x)^6 \operatorname{Log}[x] \left(49 + 20 \operatorname{Log}[d + e x] - 20 \operatorname{Log}\left[1 + \frac{e x}{d}\right]\right) + 360 b n (d + e x)^6 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right)$$

Problem 65: Result more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a + b \operatorname{Log}[c x^n])}{(d + e x)^7} dx$$

Optimal (type 3, 136 leaves, 3 steps):

$$-\frac{b d^4 n}{30 e^6 (d + e x)^5} + \frac{5 b d^3 n}{24 e^6 (d + e x)^4} - \frac{5 b d^2 n}{9 e^6 (d + e x)^3} + \frac{5 b d n}{6 e^6 (d + e x)^2} - \frac{5 b n}{6 e^6 (d + e x)} + \frac{x^6 (a + b \operatorname{Log}[c x^n])}{6 d (d + e x)^6} - \frac{b n \operatorname{Log}[d + e x]}{6 d e^6}$$

Result (type 3, 335 leaves):

$$-\frac{1}{360 d e^6 (d + e x)^6} \left(60 a d^6 + 137 b d^6 n + 360 a d^5 e x + 762 b d^5 e n x + 900 a d^4 e^2 x^2 + 1725 b d^4 e^2 n x^2 + 1200 a d^3 e^3 x^3 + 2000 b d^3 e^3 n x^3 + 900 a d^2 e^4 x^4 + 1200 b d^2 e^4 n x^4 + \right. \\
360 a d e^5 x^5 + 300 b d e^5 n x^5 - 60 b n (d + e x)^6 \operatorname{Log}[x] + 60 b d (d^5 + 6 d^4 e x + 15 d^3 e^2 x^2 + 20 d^2 e^3 x^3 + 15 d e^4 x^4 + 6 e^5 x^5) \operatorname{Log}[c x^n] + \\
60 b d^6 n \operatorname{Log}[d + e x] + 360 b d^5 e n x \operatorname{Log}[d + e x] + 900 b d^4 e^2 n x^2 \operatorname{Log}[d + e x] + 1200 b d^3 e^3 n x^3 \operatorname{Log}[d + e x] + \\
\left. 900 b d^2 e^4 n x^4 \operatorname{Log}[d + e x] + 360 b d e^5 n x^5 \operatorname{Log}[d + e x] + 60 b e^6 n x^6 \operatorname{Log}[d + e x] \right)$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{x}{c}\right]}{c - x} dx$$

Optimal (type 4, 10 leaves, 1 step):

$$\operatorname{PolyLog}\left[2, 1 - \frac{x}{c}\right]$$

Result (type 4, 27 leaves):

$$-\operatorname{Log}\left[\frac{x}{c}\right] \operatorname{Log}\left[1 - \frac{x}{c}\right] - \operatorname{PolyLog}\left[2, \frac{x}{c}\right]$$

Problem 115: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{Log}[c x^n])^2}{(d + e x)^4} dx$$

Optimal (type 4, 161 leaves, 5 steps):

$$\frac{b n x^2 (a + b \operatorname{Log}[c x^n])}{3 d e (d + e x)^2} + \frac{x^3 (a + b \operatorname{Log}[c x^n])^2}{3 d (d + e x)^3} + \frac{b n x (2 a + b n + 2 b \operatorname{Log}[c x^n])}{3 d e^2 (d + e x)} -$$

$$\frac{b n (2 a + 3 b n + 2 b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x}{d}\right]}{3 d e^3} - \frac{2 b^2 n^2 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{3 d e^3}$$

Result (type 4, 612 leaves):

$$-\frac{(a + b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))^2}{e^3 (d + e x)} + \frac{a^2 d + 2 a b d(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + b^2 d(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2}{e^3 (d + e x)^2} +$$

$$\frac{-a^2 d^2 - 2 a b d^2(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - b^2 d^2(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2}{3 e^3 (d + e x)^3} +$$

$$2 b n (a + b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) \left(\frac{\frac{x \operatorname{Log}[x]}{d + e x} - \frac{\operatorname{Log}[d + e x]}{e}}{d e^2} - \frac{e x (2 d + e x) \operatorname{Log}[x] - (d + e x)(-d + (d + e x) \operatorname{Log}[d + e x])}{d e^3 (d + e x)^2} + \right.$$

$$\left. \frac{2 e x (3 d^2 + 3 d e x + e^2 x^2) \operatorname{Log}[x] - (d + e x)(-d (3 d + 2 e x) + 2 (d + e x)^2 \operatorname{Log}[d + e x])}{6 d e^3 (d + e x)^3} \right) +$$

$$b^2 n^2 \left(\frac{\operatorname{Log}[x] (e x \operatorname{Log}[x] - 2 (d + e x) \operatorname{Log}\left[1 + \frac{e x}{d}\right]) - 2 (d + e x) \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{d e^3 (d + e x)} - \frac{1}{d e^3 (d + e x)^2} \right.$$

$$\left. \left(e x (2 d + e x) \operatorname{Log}[x]^2 + 2 (d + e x)^2 \operatorname{Log}\left[1 + \frac{e x}{d}\right] - 2 (d + e x) \operatorname{Log}[x] \left(e x + (d + e x) \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) - 2 (d + e x)^2 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right) + \right.$$

$$\frac{1}{3 d e^3 (d + e x)^3} \left(e x (3 d^2 + 3 d e x + e^2 x^2) \operatorname{Log}[x]^2 + (d + e x)^2 \left(e x + 3 (d + e x) \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) - \right.$$

$$\left. \left. (d + e x) \operatorname{Log}[x] \left(e x (4 d + 3 e x) + 2 (d + e x)^2 \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) - 2 (d + e x)^3 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right) \right)$$

Problem 116: Result more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{Log}[c x^n])^2}{(d + e x)^4} dx$$

Optimal (type 4, 210 leaves, 8 steps):

$$\frac{b^2 n^2}{3 d e^2 (d + e x)} - \frac{b n (a + b \operatorname{Log}[c x^n])}{3 e^2 (d + e x)^2} + \frac{b n (a + b \operatorname{Log}[c x^n])}{3 d e^2 (d + e x)} + \frac{(a + b \operatorname{Log}[c x^n])^2}{6 d^2 e^2} +$$

$$\frac{d (a + b \operatorname{Log}[c x^n])^2}{3 e^2 (d + e x)^3} - \frac{(a + b \operatorname{Log}[c x^n])^2}{2 e^2 (d + e x)^2} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x}{d}\right]}{3 d^2 e^2} - \frac{b^2 n^2 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{3 d^2 e^2}$$

Result (type 4, 441 leaves):

$$-\frac{1}{6 d^2 e^2 (d + e x)^3}$$

$$\left(a^2 d^3 + 3 a^2 d^2 e x - 2 a b d^2 e n x + 2 b^2 d^2 e n^2 x - 2 a b d e^2 n x^2 + 4 b^2 d e^2 n^2 x^2 + 2 b^2 e^3 n^2 x^3 + b^2 n^2 (d + e x)^3 \operatorname{Log}[x]^2 + 2 a b d^3 \operatorname{Log}[c x^n] + \right.$$

$$6 a b d^2 e x \operatorname{Log}[c x^n] - 2 b^2 d^2 e n x \operatorname{Log}[c x^n] - 2 b^2 d e^2 n x^2 \operatorname{Log}[c x^n] + b^2 d^3 \operatorname{Log}[c x^n]^2 + 3 b^2 d^2 e x \operatorname{Log}[c x^n]^2 + 2 a b d^3 n \operatorname{Log}[d + e x] +$$

$$6 a b d^2 e n x \operatorname{Log}[d + e x] + 6 a b d e^2 n x^2 \operatorname{Log}[d + e x] + 2 a b e^3 n x^3 \operatorname{Log}[d + e x] + 2 b^2 d^3 n \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] +$$

$$6 b^2 d^2 e n x \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 6 b^2 d e^2 n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] + 2 b^2 e^3 n x^3 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x] -$$

$$\left. 2 b n (d + e x)^3 \operatorname{Log}[x] \left(a + b \operatorname{Log}[c x^n] + b n \operatorname{Log}[d + e x] - b n \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) + 2 b^2 n^2 (d + e x)^3 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right)$$

Problem 121: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3}{x (d + e x)} dx$$

Optimal (type 4, 113 leaves, 4 steps):

$$-\frac{\operatorname{Log}\left[1 + \frac{d}{e x}\right] (a + b \operatorname{Log}[c x^n])^3}{d} + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{d}{e x}\right]}{d} + \frac{6 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{d}{e x}\right]}{d} + \frac{6 b^3 n^3 \operatorname{PolyLog}\left[4, -\frac{d}{e x}\right]}{d}$$

Result (type 4, 243 leaves):

$$\begin{aligned} & \frac{1}{4d} \left(4 \operatorname{Log}[x] \left(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n] \right)^3 - 4 \left(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n] \right)^3 \operatorname{Log}[d + e x] + \right. \\ & 6 b n \left(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n] \right)^2 \left(\operatorname{Log}[x]^2 - 2 \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e x}{d}\right] + \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]\right) \right) - \\ & 4 b^2 n^2 \left(-a + b n \operatorname{Log}[x] - b \operatorname{Log}[c x^n] \right) \left(\operatorname{Log}[x]^2 \left(\operatorname{Log}[x] - 3 \operatorname{Log}\left[1 + \frac{e x}{d}\right]\right) - 6 \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] + 6 \operatorname{PolyLog}\left[3, -\frac{e x}{d}\right] \right) + \\ & \left. b^3 n^3 \left(\operatorname{Log}[x]^4 - 4 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{e x}{d}\right] - 12 \operatorname{Log}[x]^2 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] + 24 \operatorname{Log}[x] \operatorname{PolyLog}\left[3, -\frac{e x}{d}\right] - 24 \operatorname{PolyLog}\left[4, -\frac{e x}{d}\right] \right) \right) \end{aligned}$$

Problem 134: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 211 leaves, 12 steps):

$$\begin{aligned} & -4 b n \sqrt{d+e x} + 4 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] + 2 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2 + 2 \sqrt{d+e x} (a+b \operatorname{Log}[c x^n]) - \\ & 2 \sqrt{d} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n]) - 4 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right] - 2 b \sqrt{d} n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right] \end{aligned}$$

Result (type 5, 177 leaves):

$$\begin{aligned} & \frac{1}{\sqrt{1+\frac{d}{e x}}} b n \sqrt{d+e x} \left(-4 \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{d}{e x}\right] + 2 \sqrt{1+\frac{d}{e x}} \operatorname{Log}[x] - \frac{2 \sqrt{d} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x]}{\sqrt{e} \sqrt{x}} \right) + \\ & 2 \sqrt{d+e x} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) - 2 \sqrt{d} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \end{aligned}$$

Problem 135: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{x^2} dx$$

Optimal (type 4, 221 leaves, 11 steps):

$$\begin{aligned}
& - \frac{b n \sqrt{d+e x}}{x} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]}{\sqrt{d}} + \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{\sqrt{d}} - \frac{\sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{x} \\
& \frac{e \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{\sqrt{d}} - \frac{2 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{\sqrt{d}} - \frac{b e n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{\sqrt{d}}
\end{aligned}$$

Result (type 5, 193 leaves):

$$\begin{aligned}
& \frac{1}{\sqrt{d} \sqrt{1+\frac{d}{e x}} x} \left(-2 b \sqrt{d} n \sqrt{d+e x} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{d}{e x}\right] - b \sqrt{e} n \sqrt{x} \sqrt{d+e x} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] (1+\operatorname{Log}[x]) - \right. \\
& \left. \sqrt{1+\frac{d}{e x}} \left(\sqrt{d} \sqrt{d+e x} (a+b n+b \operatorname{Log}[c x^n]) + e x \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n]) \right) \right)
\end{aligned}$$

Problem 136: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{x^3} dx$$

Optimal (type 4, 298 leaves, 16 steps):

$$\begin{aligned}
& - \frac{b n \sqrt{d+e x}}{4 x^2} - \frac{3 b e n \sqrt{d+e x}}{8 d x} - \frac{b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]}{8 d^{3/2}} - \frac{b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{4 d^{3/2}} - \frac{\sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{2 x^2} - \frac{e \sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{4 d x} + \\
& \frac{e^2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{4 d^{3/2}} + \frac{b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{2 d^{3/2}} + \frac{b e^2 n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{4 d^{3/2}}
\end{aligned}$$

Result (type 5, 208 leaves):

$$\frac{1}{36 d^{3/2} \sqrt{1 + \frac{d}{e x} x^2}} \left(-16 b d^{3/2} n \sqrt{d + e x} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{d}{e x}\right] + 9 e^2 \sqrt{1 + \frac{d}{e x} x^2} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) - 9 \sqrt{d + e x} \left(-b e^{3/2} n x^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x] + \sqrt{d} \sqrt{1 + \frac{d}{e x}} (2 d + e x) (a + b \operatorname{Log}[c x^n]) \right) \right)$$

Problem 141: Result unnecessarily involves higher level functions.

$$\int \frac{(d + e x)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 255 leaves, 18 steps):

$$-\frac{16}{3} b d n \sqrt{d + e x} - \frac{4}{9} b n (d + e x)^{3/2} + \frac{16}{3} b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] + 2 b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]^2 + 2 d \sqrt{d + e x} (a + b \operatorname{Log}[c x^n]) + \frac{2}{3} (d + e x)^{3/2} (a + b \operatorname{Log}[c x^n]) - 2 d^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n]) - 4 b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right] - 2 b d^{3/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right]$$

Result (type 5, 272 leaves):

$$\frac{1}{3 \sqrt{1 + \frac{e x}{d}}} b n \sqrt{d + e x} \left(-3 e x \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, -\frac{e x}{d}\right] + 2 \left(e x \sqrt{1 + \frac{e x}{d}} + d \left(-1 + \sqrt{1 + \frac{e x}{d}} \right) \right) \operatorname{Log}[x] \right) + \frac{1}{\sqrt{1 + \frac{d}{e x}}} b d n \sqrt{d + e x} \left(-4 \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{d}{e x}\right] + 2 \sqrt{1 + \frac{d}{e x}} \operatorname{Log}[x] - \frac{2 \sqrt{d} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x]}{\sqrt{e} \sqrt{x}} \right) + \frac{2}{3} \sqrt{d + e x} (4 d + e x) (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) - 2 d^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])$$

Problem 142: Result unnecessarily involves higher level functions.

$$\int \frac{(d + e x)^{3/2} (a + b \operatorname{Log}[c x^n])}{x^2} dx$$

Optimal (type 4, 259 leaves, 14 steps):

$$\begin{aligned} & -4 b e n \sqrt{d + e x} - \frac{b d n \sqrt{d + e x}}{x} + 3 b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] + 3 b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]^2 + \\ & 3 e \sqrt{d + e x} (a + b \operatorname{Log}[c x^n]) - \frac{(d + e x)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} - 3 \sqrt{d} e \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n]) - \\ & 6 b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right] - 3 b \sqrt{d} e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right] \end{aligned}$$

Result (type 5, 331 leaves):

$$\begin{aligned} & -\frac{1}{\sqrt{1 + \frac{d}{e x}} \sqrt{x}} 2 b \sqrt{e} n \sqrt{d + e x} \\ & \left(2 \sqrt{e} \sqrt{x} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{d}{e x}\right] - \sqrt{e} \sqrt{1 + \frac{d}{e x}} \sqrt{x} \operatorname{Log}[x] + \sqrt{d} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x] \right) - \frac{1}{\sqrt{1 + \frac{d}{e x}} x} \\ & b \sqrt{d} n \sqrt{d + e x} \left(2 \sqrt{d} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{d}{e x}\right] + \left(\sqrt{d} \sqrt{1 + \frac{d}{e x}} + \sqrt{e} \sqrt{x} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \right) (1 + \operatorname{Log}[x]) \right) - \\ & \frac{(d - 2 e x) \sqrt{d + e x} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{x} - 3 \sqrt{d} e \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \end{aligned}$$

Problem 143: Result unnecessarily involves higher level functions.

$$\int \frac{(d + e x)^{3/2} (a + b \operatorname{Log}[c x^n])}{x^3} dx$$

Optimal (type 4, 293 leaves, 16 steps):

$$\begin{aligned}
& - \frac{b d n \sqrt{d+e x}}{4 x^2} - \frac{11 b e n \sqrt{d+e x}}{8 x} - \frac{9 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]}{8 \sqrt{d}} + \frac{3 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{4 \sqrt{d}} \\
& - \frac{3 e \sqrt{d+e x} (a+b \operatorname{Log}[c x^n])}{4 x} - \frac{(d+e x)^{3/2} (a+b \operatorname{Log}[c x^n])}{2 x^2} - \frac{3 e^2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{4 \sqrt{d}} \\
& - \frac{3 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{2 \sqrt{d}} - \frac{3 b e^2 n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{4 \sqrt{d}}
\end{aligned}$$

Result (type 5, 270 leaves):

$$\begin{aligned}
& \frac{1}{36 \sqrt{d} \sqrt{1+\frac{d}{e x}} x^2} \left(-16 b d^{3/2} n \sqrt{d+e x} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{d}{e x}\right] - \right. \\
& \left. 9 \left(8 b \sqrt{d} e n x \sqrt{d+e x} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{d}{e x}\right] + b e^{3/2} n x^{3/2} \sqrt{d+e x} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] (4+3 \operatorname{Log}[x]) + \right. \right. \\
& \left. \left. \sqrt{1+\frac{d}{e x}} \left(3 e^2 x^2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n]) + \sqrt{d} \sqrt{d+e x} (2 a d+5 a e x+4 b e n x+b (2 d+5 e x) \operatorname{Log}[c x^n]) \right) \right) \right)
\end{aligned}$$

Problem 148: Result unnecessarily involves higher level functions.

$$\int \frac{a+b \operatorname{Log}[c x^n]}{x \sqrt{d+e x}} dx$$

Optimal (type 4, 152 leaves, 7 steps):

$$\frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{\sqrt{d}} - \frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{\sqrt{d}} - \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{\sqrt{d}} - \frac{2 b n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{\sqrt{d}}$$

Result (type 5, 132 leaves):

$$\frac{b n \sqrt{1+\frac{d}{e x}} \left(-4 \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{d}{e x}\right] - \frac{2 \sqrt{e} \sqrt{x} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x]}{\sqrt{d}} \right)}{\sqrt{d+e x}} - \frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b (-n \operatorname{Log}[x]+ \operatorname{Log}[c x^n]))}{\sqrt{d}}$$

Problem 149: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^2 \sqrt{d + e x}} dx$$

Optimal (type 4, 226 leaves, 11 steps):

$$\begin{aligned} & -\frac{b n \sqrt{d + e x}}{d x} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]}{d^{3/2}} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]^2}{d^{3/2}} - \frac{\sqrt{d + e x} (a + b \operatorname{Log}[c x^n])}{d x} + \\ & \frac{e \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{d^{3/2}} + \frac{2 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right]}{d^{3/2}} + \frac{b e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right]}{d^{3/2}} \end{aligned}$$

Result (type 5, 191 leaves):

$$\begin{aligned} & \frac{1}{9 d^{3/2} x \sqrt{d + e x}} \left(2 b d^{3/2} n \sqrt{1 + \frac{d}{e x}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{d}{e x}\right] + 9 b e^{3/2} n \sqrt{1 + \frac{d}{e x}} x^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] (1 + \operatorname{Log}[x]) - \right. \\ & \left. 9 \sqrt{d} (d + e x) (a + b n + b \operatorname{Log}[c x^n]) + 9 e x \sqrt{d + e x} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \right) \end{aligned}$$

Problem 150: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^3 \sqrt{d + e x}} dx$$

Optimal (type 4, 304 leaves, 16 steps):

$$\begin{aligned} & -\frac{b n \sqrt{d + e x}}{4 d x^2} + \frac{5 b e n \sqrt{d + e x}}{8 d^2 x} + \frac{7 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]}{8 d^{5/2}} + \frac{3 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right]^2}{4 d^{5/2}} - \frac{\sqrt{d + e x} (a + b \operatorname{Log}[c x^n])}{2 d x^2} + \frac{3 e \sqrt{d + e x} (a + b \operatorname{Log}[c x^n])}{4 d^2 x} \\ & \frac{3 e^2 \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{4 d^{5/2}} - \frac{3 b e^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right]}{2 d^{5/2}} - \frac{3 b e^2 n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x}}\right]}{4 d^{5/2}} \end{aligned}$$

Result (type 5, 206 leaves):

$$\frac{1}{100 d^{5/2} x^2 \sqrt{d+e x}} \left(-16 b d^{5/2} n \sqrt{1 + \frac{d}{e x}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{d}{e x}\right] - 25 \left(3 b e^{5/2} n \sqrt{1 + \frac{d}{e x}} x^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x] + \sqrt{d} (2 d^2 - d e x - 3 e^2 x^2) (a + b \operatorname{Log}[c x^n]) + 3 e^2 x^2 \sqrt{d+e x} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \right) \right)$$

Problem 155: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x)^{3/2}} dx$$

Optimal (type 4, 201 leaves, 11 steps):

$$\frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]}{d^{3/2}} + \frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{d^{3/2}} + \frac{2 (a + b \operatorname{Log}[c x^n])}{d \sqrt{d+e x}} - \frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{d^{3/2}} - \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x}}\right]}{d^{3/2}} - \frac{2 b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x}}\right]}{d^{3/2}}$$

Result (type 5, 185 leaves):

$$-\frac{1}{9 d^{3/2} e x \sqrt{d+e x}} 2 \left(2 b d^{3/2} n \sqrt{1 + \frac{d}{e x}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{d}{e x}\right] + 9 e x \left(b \sqrt{e} n \sqrt{1 + \frac{d}{e x}} \sqrt{x} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} \sqrt{x}}\right] \operatorname{Log}[x] - \sqrt{d} (a + b \operatorname{Log}[c x^n]) + \sqrt{d+e x} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \right) \right)$$

Problem 156: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^2 (d + e x)^{3/2}} dx$$

Optimal (type 4, 253 leaves, 15 steps):

$$\begin{aligned}
& - \frac{b n \sqrt{d+e x}}{d^2 x} - \frac{5 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]}{d^{5/2}} - \frac{3 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right]^2}{d^{5/2}} - \frac{3 e (a+b \operatorname{Log}[c x^n])}{d^2 \sqrt{d+e x}} - \frac{a+b \operatorname{Log}[c x^n]}{d x \sqrt{d+e x}} + \\
& \frac{3 e \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{d^{5/2}} + \frac{6 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{d^{5/2}} + \frac{3 b e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x}}\right]}{d^{5/2}}
\end{aligned}$$

Result (type 5, 186 leaves):

$$\begin{aligned}
& \frac{1}{25 d^{5/2} e x^2 \sqrt{d+e x}} \\
& \left(6 b d^{5/2} n \sqrt{1 + \frac{d}{e x}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{d}{e x}\right] - 5 \left(2 b d^{5/2} n \sqrt{1 + \frac{d}{e x}} \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, \frac{5}{2}, \frac{7}{2}, -\frac{d}{e x}\right] (1 + \operatorname{Log}[x]) + \right. \right. \\
& \left. \left. 5 e x \left(\sqrt{d} (d + 3 e x) - 3 e x \sqrt{d+e x} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x}}{\sqrt{d}}\right] \right) (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \right) \right)
\end{aligned}$$

Problem 210: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 (a + b \operatorname{Log}[c x^n])}{d + e x^2} dx$$

Optimal (type 4, 121 leaves, 6 steps):

$$\frac{b d n x^2}{4 e^2} - \frac{b n x^4}{16 e} - \frac{d x^2 (a + b \operatorname{Log}[c x^n])}{2 e^2} + \frac{x^4 (a + b \operatorname{Log}[c x^n])}{4 e} + \frac{d^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{2 e^3} + \frac{b d^2 n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{4 e^3}$$

Result (type 4, 226 leaves):

$$\begin{aligned}
& \frac{1}{16 e^3} \left(-8 a d e x^2 + 4 b d e n x^2 + 4 a e^2 x^4 - b e^2 n x^4 - 8 b d e x^2 \operatorname{Log}[c x^n] + \right. \\
& 4 b e^2 x^4 \operatorname{Log}[c x^n] + 8 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 a d^2 \operatorname{Log}[d + e x^2] - \\
& \left. 8 b d^2 n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + 8 b d^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 8 b d^2 n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 b d^2 n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)
\end{aligned}$$

Problem 211: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{Log}[c x^n])}{d + e x^2} dx$$

Optimal (type 4, 83 leaves, 5 steps):

$$-\frac{b n x^2}{4 e} + \frac{x^2 (a + b \operatorname{Log}[c x^n])}{2 e} - \frac{d (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{2 e^2} - \frac{b d n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{4 e^2}$$

Result (type 4, 174 leaves):

$$-\frac{1}{4 e^2} \left(-2 a e x^2 + b e n x^2 - 2 b e x^2 \operatorname{Log}[c x^n] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 a d \operatorname{Log}[d + e x^2] - \right. \\ \left. 2 b d n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + 2 b d \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 2 b d n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b d n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 212: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{Log}[c x^n])}{d + e x^2} dx$$

Optimal (type 4, 49 leaves, 2 steps):

$$\frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{2 e} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{4 e}$$

Result (type 4, 111 leaves):

$$\frac{1}{2 e} \left((a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}[d + e x^2] + b n \left(\operatorname{Log}[x] \left(\operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right) + \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right) \right)$$

Problem 213: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^2)} dx$$

Optimal (type 4, 49 leaves, 2 steps):

$$-\frac{\operatorname{Log}\left[1 + \frac{d}{e x^2}\right] (a + b \operatorname{Log}[c x^n])}{2 d} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{d}{e x^2}\right]}{4 d}$$

Result (type 4, 157 leaves):

$$-\frac{1}{2 d} \left(-2 a \operatorname{Log}[x] + b n \operatorname{Log}[x]^2 - 2 b \operatorname{Log}[x] \operatorname{Log}[c x^n] + b n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + b n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \right. \\ \left. a \operatorname{Log}[d + e x^2] - b n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + b \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 214: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^3 (d + e x^2)} dx$$

Optimal (type 4, 83 leaves, 4 steps):

$$-\frac{b n}{4 d x^2} - \frac{a + b \operatorname{Log}[c x^n]}{2 d x^2} + \frac{e \operatorname{Log}\left[1 + \frac{d}{e x^2}\right] (a + b \operatorname{Log}[c x^n])}{2 d^2} - \frac{b e n \operatorname{PolyLog}\left[2, -\frac{d}{e x^2}\right]}{4 d^2}$$

Result (type 4, 217 leaves):

$$-\frac{a - b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])}{2 d x^2} - \frac{e \operatorname{Log}[x] (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{d^2} + \frac{e (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) \operatorname{Log}[d + e x^2]}{2 d^2} + \\ b n \left(-\frac{e \operatorname{Log}[x]^2}{2 d^2} + \frac{-\frac{1}{4 x^2} - \frac{\operatorname{Log}[x]}{2 x^2}}{d} + \frac{e \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)}{2 d^2} + \frac{e \left(\operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)}{2 d^2} \right)$$

Problem 215: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^5 (d + e x^2)} dx$$

Optimal (type 4, 121 leaves, 6 steps):

$$-\frac{b n}{16 d x^4} + \frac{b e n}{4 d^2 x^2} - \frac{a + b \operatorname{Log}[c x^n]}{4 d x^4} + \frac{e (a + b \operatorname{Log}[c x^n])}{2 d^2 x^2} - \frac{e^2 \operatorname{Log}\left[1 + \frac{d}{e x^2}\right] (a + b \operatorname{Log}[c x^n])}{2 d^3} + \frac{b e^2 n \operatorname{PolyLog}\left[2, -\frac{d}{e x^2}\right]}{4 d^3}$$

Result (type 4, 276 leaves):

$$\frac{-a - b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])}{4 d x^4} + \frac{e(a + b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{2 d^2 x^2} + \frac{e^2 \operatorname{Log}[x](a + b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{d^3} -$$

$$\frac{e^2(a + b(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) \operatorname{Log}[d + e x^2]}{2 d^3} + b n \left(\frac{e^2 \operatorname{Log}[x]^2}{2 d^3} + \frac{-\frac{1}{16 x^4} - \frac{\operatorname{Log}[x]}{4 x^4}}{d} - \frac{e\left(-\frac{1}{4 x^2} - \frac{\operatorname{Log}[x]}{2 x^2}\right)}{d^2} - \right.$$

$$\left. \frac{e^2 \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{2 d^3} - \frac{e^2 \left(\operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{2 d^3} \right)$$

Problem 221: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^2} dx$$

Optimal (type 4, 129 leaves, 7 steps):

$$-\frac{b n x^2}{4 e^2} + \frac{x^2 (a + b \operatorname{Log}[c x^n])}{2 e^2} + \frac{d x^2 (a + b \operatorname{Log}[c x^n])}{2 e^2 (d + e x^2)} - \frac{b d n \operatorname{Log}[d + e x^2]}{4 e^3} - \frac{d (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{e^3} - \frac{b d n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{2 e^3}$$

Result (type 4, 426 leaves):

$$-\frac{1}{4 e^3 (d + e x^2)}$$

$$\left(2 a d^2 - 2 a d e x^2 + b d e n x^2 - 2 a e^2 x^4 + b e^2 n x^4 - 2 b d^2 n \operatorname{Log}[x] - 2 b d e n x^2 \operatorname{Log}[x] + 2 b d^2 \operatorname{Log}[c x^n] - 2 b d e x^2 \operatorname{Log}[c x^n] - 2 b e^2 x^4 \operatorname{Log}[c x^n] + \right.$$

$$4 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] +$$

$$4 a d^2 \operatorname{Log}[d + e x^2] + b d^2 n \operatorname{Log}[d + e x^2] + 4 a d e x^2 \operatorname{Log}[d + e x^2] + b d e n x^2 \operatorname{Log}[d + e x^2] - 4 b d^2 n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] -$$

$$4 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + 4 b d^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 4 b d e x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] +$$

$$\left. 4 b d n (d + e x^2) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b d n (d + e x^2) \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 222: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^2} dx$$

Optimal (type 4, 95 leaves, 6 steps):

$$-\frac{x^2 (a + b \operatorname{Log}[c x^n])}{2 e (d + e x^2)} + \frac{b n \operatorname{Log}[d + e x^2]}{4 e^2} + \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{2 e^2} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{4 e^2}$$

Result (type 4, 336 leaves):

$$\frac{1}{4 e^2 (d + e x^2)} \left(2 a d - 2 b d n \operatorname{Log}[x] - 2 b e n x^2 \operatorname{Log}[x] + 2 b d \operatorname{Log}[c x^n] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \right. \\ \left. 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 a d \operatorname{Log}[d + e x^2] + \right. \\ \left. b d n \operatorname{Log}[d + e x^2] + 2 a e x^2 \operatorname{Log}[d + e x^2] + b e n x^2 \operatorname{Log}[d + e x^2] - 2 b d n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] - 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + \right. \\ \left. 2 b d \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 2 b e x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 2 b n (d + e x^2) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b n (d + e x^2) \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 224: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^2)^2} dx$$

Optimal (type 4, 82 leaves, 3 steps):

$$\frac{a + b \operatorname{Log}[c x^n]}{2 d (d + e x^2)} - \frac{\operatorname{Log}\left[1 + \frac{d}{e x^2}\right] (2 a - b n + 2 b \operatorname{Log}[c x^n])}{4 d^2} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{d}{e x^2}\right]}{4 d^2}$$

Result (type 4, 401 leaves):

$$-\frac{1}{4 d^2 (d + e x^2)} \left(-2 a d - 4 a d \operatorname{Log}[x] + 2 b d n \operatorname{Log}[x] - 4 a e x^2 \operatorname{Log}[x] + 2 b e n x^2 \operatorname{Log}[x] + 2 b d n \operatorname{Log}[x]^2 + \right. \\ \left. 2 b e n x^2 \operatorname{Log}[x]^2 - 2 b d \operatorname{Log}[c x^n] - 4 b d \operatorname{Log}[x] \operatorname{Log}[c x^n] - 4 b e x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \right. \\ \left. 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b d n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 a d \operatorname{Log}[d + e x^2] - \right. \\ \left. b d n \operatorname{Log}[d + e x^2] + 2 a e x^2 \operatorname{Log}[d + e x^2] - b e n x^2 \operatorname{Log}[d + e x^2] - 2 b d n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] - 2 b e n x^2 \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + \right. \\ \left. 2 b d \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 2 b e x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 2 b n (d + e x^2) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 b n (d + e x^2) \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 225: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^3 (d + e x^2)^2} dx$$

Optimal (type 4, 126 leaves, 5 steps):

$$-\frac{bn}{2d^2x^2} + \frac{a + b \operatorname{Log}[c x^n]}{2dx^2(d + ex^2)} - \frac{4a - bn + 4b \operatorname{Log}[c x^n]}{4d^2x^2} + \frac{e \operatorname{Log}\left[1 + \frac{d}{ex^2}\right] (4a - bn + 4b \operatorname{Log}[c x^n])}{4d^3} - \frac{ben \operatorname{PolyLog}\left[2, -\frac{d}{ex^2}\right]}{2d^3}$$

Result (type 4, 337 leaves):

$$\begin{aligned} & -\frac{1}{4d^3} \left(\frac{2ad}{x^2} + \frac{bdn}{x^2} + \frac{2ade}{d + ex^2} + 8ae \operatorname{Log}[x] - 2ben \operatorname{Log}[x] - \frac{ib\sqrt{d}en \operatorname{Log}[x]}{-i\sqrt{d} + \sqrt{e}x} + \right. \\ & \frac{ib\sqrt{d}en \operatorname{Log}[x]}{i\sqrt{d} + \sqrt{e}x} - \frac{2bden \operatorname{Log}[x]}{d + ex^2} - 4ben \operatorname{Log}[x]^2 + \frac{2bd \operatorname{Log}[c x^n]}{x^2} + \frac{2bde \operatorname{Log}[c x^n]}{d + ex^2} + 8be \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\ & 4ben \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 4ben \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 4ae \operatorname{Log}[d + ex^2] + ben \operatorname{Log}[d + ex^2] + \\ & \left. 4ben \operatorname{Log}[x] \operatorname{Log}[d + ex^2] - 4be \operatorname{Log}[c x^n] \operatorname{Log}[d + ex^2] - 4ben \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] - 4ben \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] \right) \end{aligned}$$

Problem 227: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^2} dx$$

Optimal (type 4, 164 leaves, 14 steps):

$$\frac{bn \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]}{2\sqrt{d}e^{3/2}} - \frac{x(a + b \operatorname{Log}[c x^n])}{2e(d + ex^2)} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2\sqrt{d}e^{3/2}} - \frac{ibn \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right]}{4\sqrt{d}e^{3/2}} + \frac{ibn \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{4\sqrt{d}e^{3/2}}$$

Result (type 4, 391 leaves):

$$\begin{aligned}
& - \frac{x (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{2 e (d + e x^2)} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{2 \sqrt{d} e^{3/2}} + \\
& b n \left(\frac{\frac{\operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d} \sqrt{e}} + \frac{i \operatorname{Log}[x]}{\sqrt{d} \sqrt{e}} - \frac{\operatorname{Log}[x]}{\sqrt{e} (-i \sqrt{d} + \sqrt{e} x)} - \frac{i \operatorname{Log}[d + e x^2]}{2 \sqrt{d} \sqrt{e}}}{4 e} + \frac{\frac{\operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d} \sqrt{e}} - \frac{i \operatorname{Log}[x]}{\sqrt{d} \sqrt{e}} - \frac{\operatorname{Log}[x]}{\sqrt{e} (i \sqrt{d} + \sqrt{e} x)} + \frac{i \operatorname{Log}[d + e x^2]}{2 \sqrt{d} \sqrt{e}}}{4 e} - \right. \\
& \left. \frac{i \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{4 \sqrt{d} e^{3/2}} + \frac{i \left(\operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{4 \sqrt{d} e^{3/2}} \right)
\end{aligned}$$

Problem 228: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{(d + e x^2)^2} dx$$

Optimal (type 4, 164 leaves, 7 steps):

$$- \frac{b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{2 d^{3/2} \sqrt{e}} + \frac{x (a + b \operatorname{Log}[c x^n])}{2 d (d + e x^2)} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2 d^{3/2} \sqrt{e}} - \frac{i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{4 d^{3/2} \sqrt{e}} + \frac{i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{4 d^{3/2} \sqrt{e}}$$

Result (type 4, 391 leaves):

$$\frac{x (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{2 d (d + e x^2)} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] (a + b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]))}{2 d^{3/2} \sqrt{e}} +$$

$$b n \left(\frac{\frac{\operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}{\sqrt{d} \sqrt{e}} + \frac{i \operatorname{Log}[x]}{\sqrt{d} \sqrt{e}} - \frac{\operatorname{Log}[x]}{\sqrt{e} (-i \sqrt{d} + \sqrt{e} x)} - \frac{i \operatorname{Log}[d + e x^2]}{2 \sqrt{d} \sqrt{e}}}{4 d} - \frac{\frac{\operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}{\sqrt{d} \sqrt{e}} - \frac{i \operatorname{Log}[x]}{\sqrt{d} \sqrt{e}} - \frac{\operatorname{Log}[x]}{\sqrt{e} (i \sqrt{d} + \sqrt{e} x)} + \frac{i \operatorname{Log}[d + e x^2]}{2 \sqrt{d} \sqrt{e}}}{4 d} - \right.$$

$$\left. \frac{i \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{4 d^{3/2} \sqrt{e}} + \frac{i \left(\operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]\right)}{4 d^{3/2} \sqrt{e}} \right)$$

Problem 229: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^2 (d + e x^2)^2} dx$$

Optimal (type 4, 183 leaves, 8 steps):

$$-\frac{3 b n}{2 d^2 x} + \frac{a + b \operatorname{Log}[c x^n]}{2 d x (d + e x^2)} - \frac{3 a - b n + 3 b \operatorname{Log}[c x^n]}{2 d^2 x} -$$

$$\frac{\sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] (3 a - b n + 3 b \operatorname{Log}[c x^n])}{2 d^{5/2}} + \frac{3 i b \sqrt{e} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{4 d^{5/2}} - \frac{3 i b \sqrt{e} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{4 d^{5/2}}$$

Result (type 4, 398 leaves):

$$\frac{1}{4 d^{5/2}} \left(-\frac{4 a \sqrt{d}}{x} - \frac{4 b \sqrt{d} n}{x} - \frac{2 a \sqrt{d} e x}{d + e x^2} - 6 a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] + 2 b \sqrt{e} n \operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] + \frac{b \sqrt{d} \sqrt{e} n \operatorname{Log}[x]}{i \sqrt{d} - \sqrt{e} x} - \frac{b \sqrt{d} \sqrt{e} n \operatorname{Log}[x]}{i \sqrt{d} + \sqrt{e} x} + \right.$$

$$\frac{2 b \sqrt{d} e n x \operatorname{Log}[x]}{d + e x^2} + 6 b \sqrt{e} n \operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] \operatorname{Log}[x] - \frac{4 b \sqrt{d} \operatorname{Log}[c x^n]}{x} - \frac{2 b \sqrt{d} e x \operatorname{Log}[c x^n]}{d + e x^2} - 6 b \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] \operatorname{Log}[c x^n] -$$

$$\left. 3 i b \sqrt{e} n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 3 i b \sqrt{e} n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 3 i b \sqrt{e} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] - 3 i b \sqrt{e} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 231: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^3} dx$$

Optimal (type 4, 152 leaves, 10 steps):

$$\frac{b d n}{8 e^3 (d + e x^2)} + \frac{b n \operatorname{Log}[x]}{4 e^3} - \frac{d^2 (a + b \operatorname{Log}[c x^n])}{4 e^3 (d + e x^2)^2} - \frac{x^2 (a + b \operatorname{Log}[c x^n])}{e^2 (d + e x^2)} + \frac{3 b n \operatorname{Log}[d + e x^2]}{8 e^3} + \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x^2}{d}\right]}{2 e^3} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{e x^2}{d}\right]}{4 e^3}$$

Result (type 4, 553 leaves):

$$\frac{1}{8 e^3 (d + e x^2)^2} \left(6 a d^2 + b d^2 n + 8 a d e x^2 + b d e n x^2 - 6 b d^2 n \operatorname{Log}[x] - 12 b d e n x^2 \operatorname{Log}[x] - 6 b e^2 n x^4 \operatorname{Log}[x] + 6 b d^2 \operatorname{Log}[c x^n] + \right. \\ \left. 8 b d e x^2 \operatorname{Log}[c x^n] + 4 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b e^2 n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \right. \\ \left. 4 b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b e^2 n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 a d^2 \operatorname{Log}[d + e x^2] + \right. \\ \left. 3 b d^2 n \operatorname{Log}[d + e x^2] + 8 a d e x^2 \operatorname{Log}[d + e x^2] + 6 b d e n x^2 \operatorname{Log}[d + e x^2] + 4 a e^2 x^4 \operatorname{Log}[d + e x^2] + 3 b e^2 n x^4 \operatorname{Log}[d + e x^2] - \right. \\ \left. 4 b d^2 n \operatorname{Log}[x] \operatorname{Log}[d + e x^2] - 8 b d e n x^2 \operatorname{Log}[x] \operatorname{Log}[d + e x^2] - 4 b e^2 n x^4 \operatorname{Log}[x] \operatorname{Log}[d + e x^2] + 4 b d^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + \right. \\ \left. 8 b d e x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 4 b e^2 x^4 \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^2] + 4 b n (d + e x^2)^2 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 b n (d + e x^2)^2 \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 234: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^2)^3} dx$$

Optimal (type 4, 115 leaves, 4 steps):

$$\frac{a + b \operatorname{Log}[c x^n]}{4 d (d + e x^2)^2} - \frac{\operatorname{Log}\left[1 + \frac{d}{e x^2}\right] (4 a - 3 b n + 4 b \operatorname{Log}[c x^n])}{8 d^3} + \frac{4 a - b n + 4 b \operatorname{Log}[c x^n]}{8 d^2 (d + e x^2)} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{d}{e x^2}\right]}{4 d^3}$$

Result (type 4, 444 leaves):

$$\begin{aligned}
& -\frac{1}{16d^3} \left(\frac{bdn}{d-i\sqrt{d}\sqrt{ex}} + \frac{bdn}{d+i\sqrt{d}\sqrt{ex}} - \frac{4ad^2}{(d+ex^2)^2} - \frac{8ad}{d+ex^2} - 16a \operatorname{Log}[x] + 12bn \operatorname{Log}[x] - \frac{bdn \operatorname{Log}[x]}{(\sqrt{d}-i\sqrt{ex})^2} - \frac{bdn \operatorname{Log}[x]}{(\sqrt{d}+i\sqrt{ex})^2} + \right. \\
& \frac{5i b \sqrt{d} n \operatorname{Log}[x]}{-i\sqrt{d}+\sqrt{ex}} - \frac{5i b \sqrt{d} n \operatorname{Log}[x]}{i\sqrt{d}+\sqrt{ex}} + \frac{4bd^2 n \operatorname{Log}[x]}{(d+ex^2)^2} + \frac{8bdn \operatorname{Log}[x]}{d+ex^2} + 8bn \operatorname{Log}[x]^2 - \frac{4bd^2 \operatorname{Log}[cx^n]}{(d+ex^2)^2} - \frac{8bd \operatorname{Log}[cx^n]}{d+ex^2} - \\
& 16b \operatorname{Log}[x] \operatorname{Log}[cx^n] + 8bn \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{ex}}{\sqrt{d}}\right] + 8bn \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{ex}}{\sqrt{d}}\right] + 8a \operatorname{Log}[d+ex^2] - 6bn \operatorname{Log}[d+ex^2] - \\
& \left. 8bn \operatorname{Log}[x] \operatorname{Log}[d+ex^2] + 8b \operatorname{Log}[cx^n] \operatorname{Log}[d+ex^2] + 8bn \operatorname{PolyLog}\left[2, -\frac{i\sqrt{ex}}{\sqrt{d}}\right] + 8bn \operatorname{PolyLog}\left[2, \frac{i\sqrt{ex}}{\sqrt{d}}\right] \right)
\end{aligned}$$

Problem 235: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{a+b \operatorname{Log}[cx^n]}{x^3(d+ex^2)^3} dx$$

Optimal (type 4, 162 leaves, 6 steps):

$$\begin{aligned}
& -\frac{3bn}{4d^3x^2} + \frac{a+b \operatorname{Log}[cx^n]}{4dx^2(d+ex^2)^2} + \frac{6a-bn+6b \operatorname{Log}[cx^n]}{8d^2x^2(d+ex^2)} - \\
& \frac{12a-5bn+12b \operatorname{Log}[cx^n]}{8d^3x^2} + \frac{e \operatorname{Log}\left[1+\frac{d}{ex^2}\right] (12a-5bn+12b \operatorname{Log}[cx^n])}{8d^4} - \frac{3ben \operatorname{PolyLog}\left[2, -\frac{d}{ex^2}\right]}{4d^4}
\end{aligned}$$

Result (type 4, 468 leaves):

$$\begin{aligned}
& \frac{1}{16d^4} \left(24ben \operatorname{PolyLog}\left[2, -\frac{i\sqrt{ex}}{\sqrt{d}}\right] - \frac{1}{x^2(d+ex^2)^2} 2 \left(4ad^3+2bd^3n+18ad^2ex^2+3bd^2enx^2+12ade^2x^4+bde^2nx^4-12benx^2(d+ex^2)^2 \operatorname{Log}[x]^2 + \right. \right. \\
& 4bd^3 \operatorname{Log}[cx^n] + 18bd^2ex^2 \operatorname{Log}[cx^n] + 12bd^2ex^4 \operatorname{Log}[cx^n] - 12ad^2ex^2 \operatorname{Log}[d+ex^2] + 5bd^2enx^2 \operatorname{Log}[d+ex^2] - \\
& 24ade^2x^4 \operatorname{Log}[d+ex^2] + 10bde^2nx^4 \operatorname{Log}[d+ex^2] - 12ae^3x^6 \operatorname{Log}[d+ex^2] + 5be^3nx^6 \operatorname{Log}[d+ex^2] - \\
& 12bd^2ex^2 \operatorname{Log}[cx^n] \operatorname{Log}[d+ex^2] - 24bd^2ex^4 \operatorname{Log}[cx^n] \operatorname{Log}[d+ex^2] - 12be^3x^6 \operatorname{Log}[cx^n] \operatorname{Log}[d+ex^2] + \\
& \left. 2ex^2(d+ex^2)^2 \operatorname{Log}[x] \left(12a-5bn+12b \operatorname{Log}[cx^n] - 6bn \operatorname{Log}\left[1-\frac{i\sqrt{ex}}{\sqrt{d}}\right] - 6bn \operatorname{Log}\left[1+\frac{i\sqrt{ex}}{\sqrt{d}}\right] + 6bn \operatorname{Log}[d+ex^2] \right) - \right. \\
& \left. \left. 12benx^2(d+ex^2)^2 \operatorname{PolyLog}\left[2, \frac{i\sqrt{ex}}{\sqrt{d}}\right] \right) \right)
\end{aligned}$$

Problem 236: Result more than twice size of optimal antiderivative.

$$\int \frac{x^4 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^3} dx$$

Optimal (type 4, 211 leaves, 24 steps):

$$\begin{aligned} & -\frac{b n x}{8 e^2 (d + e x^2)} + \frac{b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{2 \sqrt{d} e^{5/2}} + \frac{d x (a + b \operatorname{Log}[c x^n])}{4 e^2 (d + e x^2)^2} - \frac{5 x (a + b \operatorname{Log}[c x^n])}{8 e^2 (d + e x^2)} + \\ & \frac{3 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{8 \sqrt{d} e^{5/2}} - \frac{3 i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 \sqrt{d} e^{5/2}} + \frac{3 i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 \sqrt{d} e^{5/2}} \end{aligned}$$

Result (type 4, 509 leaves):

$$\begin{aligned} & \frac{1}{16 e^{5/2}} \left(\frac{b n}{i \sqrt{d} - \sqrt{e} x} - \frac{b n}{i \sqrt{d} + \sqrt{e} x} + \frac{4 a d \sqrt{e} x}{(d + e x^2)^2} - \frac{10 a \sqrt{e} x}{d + e x^2} + \frac{6 a \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} + \frac{8 b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} - \right. \\ & \frac{i b \sqrt{d} n \operatorname{Log}[x]}{(\sqrt{d} - i \sqrt{e} x)^2} + \frac{i b \sqrt{d} n \operatorname{Log}[x]}{(\sqrt{d} + i \sqrt{e} x)^2} - \frac{5 b n \operatorname{Log}[x]}{-i \sqrt{d} + \sqrt{e} x} - \frac{5 b n \operatorname{Log}[x]}{i \sqrt{d} + \sqrt{e} x} - \frac{4 b d \sqrt{e} n x \operatorname{Log}[x]}{(d + e x^2)^2} + \frac{10 b \sqrt{e} n x \operatorname{Log}[x]}{d + e x^2} - \\ & \frac{6 b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x]}{\sqrt{d}} + \frac{4 b d \sqrt{e} x \operatorname{Log}[c x^n]}{(d + e x^2)^2} - \frac{10 b \sqrt{e} x \operatorname{Log}[c x^n]}{d + e x^2} + \frac{6 b \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n]}{\sqrt{d}} + \\ & \left. \frac{3 i b n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} - \frac{3 i b n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} - \frac{3 i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} + \frac{3 i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d}} \right) \end{aligned}$$

Problem 237: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^3} dx$$

Optimal (type 4, 187 leaves, 19 steps):

$$\frac{b n x}{8 d e (d + e x^2)} - \frac{x (a + b \operatorname{Log}[c x^n])}{4 e (d + e x^2)^2} + \frac{x (a + b \operatorname{Log}[c x^n])}{8 d e (d + e x^2)} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{8 d^{3/2} e^{3/2}} - \frac{i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{3/2} e^{3/2}} + \frac{i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{3/2} e^{3/2}}$$

Result (type 4, 589 leaves):

$$\frac{1}{16 d^{3/2} e^{3/2} (d + e x^2)^2}$$

$$\left(-2 a d^{3/2} \sqrt{e} x + 2 b d^{3/2} \sqrt{e} n x + 2 a \sqrt{d} e^{3/2} x^3 + 2 b \sqrt{d} e^{3/2} n x^3 + 2 a d^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 4 a d e x^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 2 a e^2 x^4 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] - \right.$$

$$2 b d^2 n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] - 4 b d e n x^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] - 2 b e^2 n x^4 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] - 2 b d^{3/2} \sqrt{e} x \operatorname{Log}[c x^n] +$$

$$2 b \sqrt{d} e^{3/2} x^3 \operatorname{Log}[c x^n] + 2 b d^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n] + 4 b d e x^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n] +$$

$$2 b e^2 x^4 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n] + i b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 i b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] +$$

$$i b e^2 n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] - i b d^2 n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] - 2 i b d e n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] -$$

$$\left. i b e^2 n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] - i b n (d + e x^2)^2 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + i b n (d + e x^2)^2 \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 238: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{(d + e x^2)^3} dx$$

Optimal (type 4, 210 leaves, 10 steps):

$$-\frac{b n x}{8 d^2 (d + e x^2)} - \frac{b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{2 d^{5/2} \sqrt{e}} + \frac{x (a + b \operatorname{Log}[c x^n])}{4 d (d + e x^2)^2} + \frac{3 x (a + b \operatorname{Log}[c x^n])}{8 d^2 (d + e x^2)} +$$

$$\frac{3 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{8 d^{5/2} \sqrt{e}} - \frac{3 i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{5/2} \sqrt{e}} + \frac{3 i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{5/2} \sqrt{e}}$$

Result (type 4, 533 leaves):

$$\frac{1}{16 d^{5/2}} \left(-\frac{b \sqrt{d} n}{-i \sqrt{d} \sqrt{e} + e x} - \frac{b \sqrt{d} n}{i \sqrt{d} \sqrt{e} + e x} + \frac{4 a d^{3/2} x}{(d + e x^2)^2} + \frac{6 a \sqrt{d} x}{d + e x^2} + \frac{6 a \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \right.$$

$$\frac{8 b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{i b d n \operatorname{Log}[x]}{\sqrt{e} (\sqrt{d} + i \sqrt{e} x)^2} + \frac{i b d n \operatorname{Log}[x]}{\sqrt{e} (i \sqrt{d} + \sqrt{e} x)^2} + \frac{3 b \sqrt{d} n \operatorname{Log}[x]}{-i \sqrt{d} \sqrt{e} + e x} + \frac{3 b \sqrt{d} n \operatorname{Log}[x]}{i \sqrt{d} \sqrt{e} + e x} - \frac{4 b d^{3/2} n x \operatorname{Log}[x]}{(d + e x^2)^2} -$$

$$\frac{6 b \sqrt{d} n x \operatorname{Log}[x]}{d + e x^2} - \frac{6 b n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x]}{\sqrt{e}} + \frac{4 b d^{3/2} x \operatorname{Log}[c x^n]}{(d + e x^2)^2} + \frac{6 b \sqrt{d} x \operatorname{Log}[c x^n]}{d + e x^2} + \frac{6 b \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n]}{\sqrt{e}} +$$

$$\left. \frac{3 i b n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{3 i b n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{3 i b n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{3 i b n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} \right)$$

Problem 239: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^2 (d + e x^2)^3} dx$$

Optimal (type 4, 219 leaves, 9 steps):

$$-\frac{15 b n}{8 d^3 x} + \frac{a + b \operatorname{Log}[c x^n]}{4 d x (d + e x^2)^2} + \frac{5 a - b n + 5 b \operatorname{Log}[c x^n]}{8 d^2 x (d + e x^2)} - \frac{15 a - 8 b n + 15 b \operatorname{Log}[c x^n]}{8 d^3 x} -$$

$$\frac{\sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (15 a - 8 b n + 15 b \operatorname{Log}[c x^n])}{8 d^{7/2}} + \frac{15 i b \sqrt{e} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{7/2}} - \frac{15 i b \sqrt{e} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{7/2}}$$

Result (type 4, 591 leaves):

$$\frac{1}{16 d^{7/2}} \left(-\frac{16 a \sqrt{d}}{x} - \frac{16 b \sqrt{d} n}{x} + \frac{b \sqrt{d} \sqrt{e} n}{i \sqrt{d} + \sqrt{e} x} + \frac{i b d \sqrt{e} n}{d + i \sqrt{d} \sqrt{e} x} - \frac{4 a d^{3/2} e x}{(d + e x^2)^2} - \frac{14 a \sqrt{d} e x}{d + e x^2} - \right.$$

$$30 a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 16 b \sqrt{e} n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + \frac{i b d \sqrt{e} n \operatorname{Log}[x]}{(\sqrt{d} - i \sqrt{e} x)^2} - \frac{i b d \sqrt{e} n \operatorname{Log}[x]}{(\sqrt{d} + i \sqrt{e} x)^2} - \frac{7 b \sqrt{d} \sqrt{e} n \operatorname{Log}[x]}{-i \sqrt{d} + \sqrt{e} x} -$$

$$\frac{7 b \sqrt{d} \sqrt{e} n \operatorname{Log}[x]}{i \sqrt{d} + \sqrt{e} x} + \frac{4 b d^{3/2} e n x \operatorname{Log}[x]}{(d + e x^2)^2} + \frac{14 b \sqrt{d} e n x \operatorname{Log}[x]}{d + e x^2} + 30 b \sqrt{e} n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] - \frac{16 b \sqrt{d} \operatorname{Log}[c x^n]}{x} -$$

$$\frac{4 b d^{3/2} e x \operatorname{Log}[c x^n]}{(d + e x^2)^2} - \frac{14 b \sqrt{d} e x \operatorname{Log}[c x^n]}{d + e x^2} - 30 b \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n] - 15 i b \sqrt{e} n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] +$$

$$\left. 15 i b \sqrt{e} n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 15 i b \sqrt{e} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] - 15 i b \sqrt{e} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 240: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^4 (d + e x^2)^3} dx$$

Optimal (type 4, 260 leaves, 11 steps):

$$-\frac{35 b n}{72 d^3 x^3} + \frac{35 b e n}{8 d^4 x} + \frac{a + b \operatorname{Log}[c x^n]}{4 d x^3 (d + e x^2)^2} + \frac{7 a - b n + 7 b \operatorname{Log}[c x^n]}{8 d^2 x^3 (d + e x^2)} - \frac{35 a - 12 b n + 35 b \operatorname{Log}[c x^n]}{24 d^3 x^3} + \frac{e (35 a - 12 b n + 35 b \operatorname{Log}[c x^n])}{8 d^4 x} +$$

$$\frac{e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (35 a - 12 b n + 35 b \operatorname{Log}[c x^n])}{8 d^{9/2}} - \frac{35 i b e^{3/2} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{9/2}} + \frac{35 i b e^{3/2} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{16 d^{9/2}}$$

Result (type 4, 645 leaves):

$$\frac{1}{144 d^{9/2}} \left(-\frac{48 a d^{3/2}}{x^3} - \frac{16 b d^{3/2} n}{x^3} + \frac{432 a \sqrt{d} e}{x} + \frac{432 b \sqrt{d} e n}{x} + \frac{9 i b d e^{3/2} n}{d - i \sqrt{d} \sqrt{e} x} - \frac{9 i b d e^{3/2} n}{d + i \sqrt{d} \sqrt{e} x} + \frac{36 a d^{3/2} e^2 x}{(d + e x^2)^2} + \frac{198 a \sqrt{d} e^2 x}{d + e x^2} + 630 a e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] - \right.$$

$$216 b e^{3/2} n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] - \frac{9 i b d e^{3/2} n \operatorname{Log}[x]}{(\sqrt{d} - i \sqrt{e} x)^2} + \frac{9 i b d e^{3/2} n \operatorname{Log}[x]}{(\sqrt{d} + i \sqrt{e} x)^2} + \frac{99 b \sqrt{d} e^{3/2} n \operatorname{Log}[x]}{-i \sqrt{d} + \sqrt{e} x} + \frac{99 b \sqrt{d} e^{3/2} n \operatorname{Log}[x]}{i \sqrt{d} + \sqrt{e} x} -$$

$$\frac{36 b d^{3/2} e^2 n x \operatorname{Log}[x]}{(d + e x^2)^2} - \frac{198 b \sqrt{d} e^2 n x \operatorname{Log}[x]}{d + e x^2} - 630 b e^{3/2} n \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] - \frac{48 b d^{3/2} \operatorname{Log}[c x^n]}{x^3} + \frac{432 b \sqrt{d} e \operatorname{Log}[c x^n]}{x} +$$

$$\frac{36 b d^{3/2} e^2 x \operatorname{Log}[c x^n]}{(d + e x^2)^2} + \frac{198 b \sqrt{d} e^2 x \operatorname{Log}[c x^n]}{d + e x^2} + 630 b e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c x^n] + 315 i b e^{3/2} n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] -$$

$$\left. 315 i b e^{3/2} n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] - 315 i b e^{3/2} n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 315 i b e^{3/2} n \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right)$$

Problem 242: Result more than twice size of optimal antiderivative.

$$\int \frac{x \operatorname{Log}\left[\frac{x^2}{c}\right]}{c - x^2} dx$$

Optimal (type 4, 16 leaves, 2 steps):

$$\frac{1}{2} \operatorname{PolyLog}\left[2, 1 - \frac{x^2}{c}\right]$$

Result (type 4, 37 leaves):

$$-\frac{1}{2} \operatorname{Log}\left[\frac{x^2}{c}\right] \operatorname{Log}\left[1 - \frac{x^2}{c}\right] - \frac{1}{2} \operatorname{PolyLog}\left[2, \frac{x^2}{c}\right]$$

Problem 247: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2}{(d + e x^2)^2} dx$$

Optimal (type 4, 509 leaves, 16 steps):

$$\frac{x (a + b \operatorname{Log}[c x^n])^2}{4 (-d)^{3/2} (\sqrt{-d} - \sqrt{e} x)} + \frac{x (a + b \operatorname{Log}[c x^n])^2}{4 (-d)^{3/2} (\sqrt{-d} + \sqrt{e} x)} + \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 - \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} -$$

$$\frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} - \frac{b^2 n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} +$$

$$\frac{b^2 n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}}$$

Result (type 4, 666 leaves):

$$\frac{1}{4 d^2}$$

$$\left(\frac{2 d x (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^2}{d + e x^2} + \frac{2 \sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^2}{\sqrt{e}} + \frac{1}{\sqrt{e} (d + e x^2)} 2 b \sqrt{d} n (-a + b n \operatorname{Log}[x] - b \operatorname{Log}[c x^n]) \right.$$

$$\left(2 d \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 2 e x^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] - 2 \sqrt{d} \sqrt{e} x \operatorname{Log}[x] - i d \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] - i e x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \right.$$

$$\left. i d \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + i e x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + i (d + e x^2) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] - i (d + e x^2) \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] \right) +$$

$$b^2 n^2 \left(\frac{x \operatorname{Log}[x]^2}{1 - \frac{i \sqrt{e} x}{\sqrt{d}}} + \frac{x \operatorname{Log}[x]^2}{1 + \frac{i \sqrt{e} x}{\sqrt{d}}} - \frac{2 i \sqrt{d} \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{i \sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{2 i \sqrt{d} \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \right.$$

$$\frac{i \sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{2 i \sqrt{d} (-1 + \operatorname{Log}[x]) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} +$$

$$\left. \frac{2 i \sqrt{d} (-1 + \operatorname{Log}[x]) \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{2 i \sqrt{d} \operatorname{PolyLog}\left[3, -\frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{2 i \sqrt{d} \operatorname{PolyLog}\left[3, \frac{i \sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} \right) \right)$$

Problem 248: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3}{(d + e x^2)^2} dx$$

Optimal (type 4, 711 leaves, 20 steps):

$$\begin{aligned}
& \frac{x (a + b \operatorname{Log}[c x^n])^3}{4 (-d)^{3/2} (\sqrt{-d} - \sqrt{e} x)} + \frac{x (a + b \operatorname{Log}[c x^n])^3}{4 (-d)^{3/2} (\sqrt{-d} + \sqrt{e} x)} + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} - \\
& \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 - \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} - \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} + \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} - \\
& \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} + \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \\
& \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{4 (-d)^{3/2} \sqrt{e}} + \frac{3 b^3 n^3 \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \\
& \frac{3 b^3 n^3 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} + \frac{3 b^3 n^3 \operatorname{PolyLog}\left[4, -\frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}} - \frac{3 b^3 n^3 \operatorname{PolyLog}\left[4, \frac{\sqrt{e} x}{\sqrt{-d}}\right]}{2 (-d)^{3/2} \sqrt{e}}
\end{aligned}$$

Result (type 4, 1104 leaves):

$$\begin{aligned}
& \frac{1}{4d^2} \\
& \left(\frac{2dx(a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n])^3}{d + ex^2} + \frac{2\sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] (a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n])^3}{\sqrt{e}} + \frac{1}{\sqrt{e}(d + ex^2)} 3b\sqrt{d}n(a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n])^2 \right. \\
& \left(-2d \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] - 2ex^2 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] + 2\sqrt{d}\sqrt{e}x \operatorname{Log}[x] + id \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] + ie x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - \right. \\
& \left. id \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - ie x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - i(d + ex^2) \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + i(d + ex^2) \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] \left. \right) + \\
& 3b^2n^2(a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n]) \left(\frac{x \operatorname{Log}[x]^2}{1 - \frac{i\sqrt{e}x}{\sqrt{d}}} + \frac{x \operatorname{Log}[x]^2}{1 + \frac{i\sqrt{e}x}{\sqrt{d}}} - \frac{2i\sqrt{d} \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{i\sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} + \right. \\
& \frac{2i\sqrt{d} \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{i\sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{2i\sqrt{d}(-1 + \operatorname{Log}[x]) \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} + \\
& \left. \frac{2i\sqrt{d}(-1 + \operatorname{Log}[x]) \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{2i\sqrt{d} \operatorname{PolyLog}\left[3, -\frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} - \frac{2i\sqrt{d} \operatorname{PolyLog}\left[3, \frac{i\sqrt{e}x}{\sqrt{d}}\right]}{\sqrt{e}} \right) + \\
& \frac{1}{\sqrt{e}} b^3n^3 \left(\frac{\sqrt{e}x \operatorname{Log}[x]^3}{1 - \frac{i\sqrt{e}x}{\sqrt{d}}} + \frac{\sqrt{e}x \operatorname{Log}[x]^3}{1 + \frac{i\sqrt{e}x}{\sqrt{d}}} - 3i\sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] + i\sqrt{d} \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] + \right. \\
& 3i\sqrt{d} \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - i\sqrt{d} \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 3i\sqrt{d}(-2 + \operatorname{Log}[x]) \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + \\
& 3i\sqrt{d}(-2 + \operatorname{Log}[x]) \operatorname{Log}[x] \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 6i\sqrt{d} \operatorname{PolyLog}\left[3, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 6i\sqrt{d} \operatorname{Log}[x] \operatorname{PolyLog}\left[3, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + \\
& \left. \left. 6i\sqrt{d} \operatorname{PolyLog}\left[3, \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 6i\sqrt{d} \operatorname{Log}[x] \operatorname{PolyLog}\left[3, \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 6i\sqrt{d} \operatorname{PolyLog}\left[4, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 6i\sqrt{d} \operatorname{PolyLog}\left[4, \frac{i\sqrt{e}x}{\sqrt{d}}\right] \right) \right)
\end{aligned}$$

Problem 254: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d + ex^2} (a + b \operatorname{Log}[cx^n])}{x} dx$$

Optimal (type 4, 220 leaves, 12 steps):

$$-b n \sqrt{d+e x^2} + b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] + \frac{1}{2} b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]^2 + \left(\sqrt{d+e x^2} - \sqrt{d} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]\right) (a + b \operatorname{Log}[c x^n]) -$$

$$b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^2}}\right] - \frac{1}{2} b \sqrt{d} n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^2}}\right]$$

Result (type 5, 203 leaves):

$$\frac{1}{\sqrt{1 + \frac{d}{e x^2}}} b n \sqrt{d+e x^2} \left(-\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{d}{e x^2}\right] + \sqrt{1 + \frac{d}{e x^2}} \operatorname{Log}[x] - \frac{\sqrt{d} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} x}\right] \operatorname{Log}[x]}{\sqrt{e} x} \right) +$$

$$\sqrt{d+e x^2} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) + \sqrt{d} \operatorname{Log}[x] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) - \sqrt{d} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}[d + \sqrt{d} \sqrt{d+e x^2}]$$

Problem 255: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d+e x^2} (a + b \operatorname{Log}[c x^n])}{x^3} dx$$

Optimal (type 4, 252 leaves, 14 steps):

$$-\frac{b n \sqrt{d+e x^2}}{4 x^2} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]}{4 \sqrt{d}} + \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]^2}{4 \sqrt{d}} - \frac{\sqrt{d+e x^2} (a + b \operatorname{Log}[c x^n])}{2 x^2} -$$

$$\frac{e \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2 \sqrt{d}} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^2}}\right]}{2 \sqrt{d}} - \frac{b e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^2}}\right]}{4 \sqrt{d}}$$

Result (type 5, 303 leaves):

$$\frac{1}{4 \sqrt{d} \sqrt{1 + \frac{d}{e x^2}} x^2} \left(-2 b \sqrt{d} n \sqrt{d + e x^2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{d}{e x^2}\right] - b \sqrt{e} n x \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} x}\right] (1 + 2 \operatorname{Log}[x]) + \right. \\ \left. \sqrt{1 + \frac{d}{e x^2}} \left(-2 a \sqrt{d} \sqrt{d + e x^2} - b \sqrt{d} n \sqrt{d + e x^2} - 2 b e n x^2 \operatorname{Log}[x]^2 - 2 a e x^2 \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}] + \right. \right. \\ \left. \left. 2 e x^2 \operatorname{Log}[x] \left(a + b \operatorname{Log}[c x^n] + b n \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}] \right) - 2 b \operatorname{Log}[c x^n] \left(\sqrt{d} \sqrt{d + e x^2} + e x^2 \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}] \right) \right) \right)$$

Problem 256: Result unnecessarily involves higher level functions.

$$\int x^4 \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n]) dx$$

Optimal (type 4, 469 leaves, 19 steps):

$$\frac{7 b d^2 n x \sqrt{d + e x^2}}{192 e^2} - \frac{5 b d n x^3 \sqrt{d + e x^2}}{288 e} - \frac{1}{36} b n x^5 \sqrt{d + e x^2} + \frac{5 b d^{5/2} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{192 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}} + \frac{b d^{5/2} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{32 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}} - \\ \frac{b d^{5/2} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1 - e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{16 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}} - \frac{d^2 x \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n])}{16 e^2} + \frac{d x^3 \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n])}{24 e} + \\ \frac{1}{6} x^5 \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n]) + \frac{d^{5/2} \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{16 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}} - \frac{b d^{5/2} n \sqrt{d + e x^2} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{32 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}}$$

Result (type 5, 276 leaves):

$$\frac{1}{1200 e^{5/2} \sqrt{1 + \frac{e x^2}{d}}} \left(-48 b e^{5/2} n x^5 \sqrt{d + e x^2} \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{e x^2}{d}\right] + \right. \\ \left. 75 b d^{5/2} n \sqrt{d + e x^2} \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \text{Log}[x] + 25 \sqrt{1 + \frac{e x^2}{d}} \left(a \sqrt{e} x \sqrt{d + e x^2} (-3 d^2 + 2 d e x^2 + 8 e^2 x^4) + \right. \right. \\ \left. \left. 3 d^3 (a - b n \text{Log}[x]) \text{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] + b \text{Log}[c x^n] \left(\sqrt{e} x \sqrt{d + e x^2} (-3 d^2 + 2 d e x^2 + 8 e^2 x^4) + 3 d^3 \text{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] \right) \right) \right)$$

Problem 257: Result unnecessarily involves higher level functions.

$$\int x^2 \sqrt{d + e x^2} (a + b \text{Log}[c x^n]) dx$$

Optimal (type 4, 409 leaves, 15 steps):

$$-\frac{3 b d n x \sqrt{d + e x^2}}{32 e} - \frac{1}{16} b n x^3 \sqrt{d + e x^2} - \frac{b d^{3/2} n \sqrt{d + e x^2} \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{32 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} - \frac{b d^{3/2} n \sqrt{d + e x^2} \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{16 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} + \\ \frac{b d^{3/2} n \sqrt{d + e x^2} \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \text{Log}\left[1 - e^{2 \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{8 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} + \frac{d x \sqrt{d + e x^2} (a + b \text{Log}[c x^n])}{8 e} + \frac{1}{4} x^3 \sqrt{d + e x^2} (a + b \text{Log}[c x^n]) - \\ \frac{d^{3/2} \sqrt{d + e x^2} \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \text{Log}[c x^n])}{8 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} + \frac{b d^{3/2} n \sqrt{d + e x^2} \text{PolyLog}\left[2, e^{2 \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{16 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}}$$

Result (type 5, 250 leaves):

$$\frac{1}{72 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} \left(-8 b e^{3/2} n x^3 \sqrt{d + e x^2} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{e x^2}{d}\right] - \right.$$

$$9 b d^{3/2} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] + 9 \sqrt{1 + \frac{e x^2}{d}} \left(a \sqrt{e} x \sqrt{d + e x^2} (d + 2 e x^2) + \right.$$

$$\left. \left. d^2 (-a + b n \operatorname{Log}[x]) \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] + b \operatorname{Log}[c x^n] \left(\sqrt{e} x \sqrt{d + e x^2} (d + 2 e x^2) - d^2 \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] \right) \right) \right)$$

Problem 258: Result unnecessarily involves higher level functions.

$$\int \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n]) dx$$

Optimal (type 4, 330 leaves, 11 steps):

$$-\frac{1}{4} b n x \sqrt{d + e x^2} + \frac{b d^{3/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{4 \sqrt{e} \sqrt{d + e x^2}} - \frac{b d n \operatorname{ArcTanh}\left[\frac{\sqrt{e} x}{\sqrt{d + e x^2}}\right]}{4 \sqrt{e}} - \frac{b d^{3/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1 - e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{2 \sqrt{e} \sqrt{d + e x^2}} +$$

$$\frac{1}{2} x \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n]) + \frac{d^{3/2} \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2 \sqrt{e} \sqrt{d + e x^2}} - \frac{b d^{3/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{4 \sqrt{e} \sqrt{d + e x^2}}$$

Result (type 5, 237 leaves):

$$\frac{1}{4 \sqrt{e} \sqrt{1 + \frac{e x^2}{d}}} \left(-2 b \sqrt{e} n x \sqrt{d + e x^2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{e x^2}{d}\right] + b \sqrt{d} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (-1 + 2 \operatorname{Log}[x]) + \sqrt{1 + \frac{e x^2}{d}} \right.$$

$$\left. \left(\sqrt{e} (2 a - b n) x \sqrt{d + e x^2} + 2 d (a - b n \operatorname{Log}[x]) \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] + 2 b \operatorname{Log}[c x^n] \left(\sqrt{e} x \sqrt{d + e x^2} + d \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] \right) \right) \right)$$

Problem 259: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n])}{x^2} dx$$

Optimal (type 4, 345 leaves, 11 steps):

$$\begin{aligned} & -\frac{b n \sqrt{d + e x^2}}{x} + \frac{b \sqrt{e} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{d} \sqrt{1 + \frac{e x^2}{d}}} + \frac{b \sqrt{e} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{2 \sqrt{d} \sqrt{1 + \frac{e x^2}{d}}} - \frac{b \sqrt{e} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1 - e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{\sqrt{d} \sqrt{1 + \frac{e x^2}{d}}} \\ & \frac{\sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n])}{x} + \frac{\sqrt{e} \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{\sqrt{d} \sqrt{1 + \frac{e x^2}{d}}} - \frac{b \sqrt{e} n \sqrt{d + e x^2} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{2 \sqrt{d} \sqrt{1 + \frac{e x^2}{d}}} \end{aligned}$$

Result (type 5, 183 leaves):

$$\begin{aligned} & \frac{1}{x \sqrt{1 + \frac{e x^2}{d}}} b n \sqrt{d + e x^2} \left(-\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{e x^2}{d}\right] - \sqrt{1 + \frac{e x^2}{d}} \operatorname{Log}[x] + \frac{\sqrt{e} x \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x]}{\sqrt{d}} \right) \\ & \frac{\sqrt{d + e x^2} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{x} + \sqrt{e} (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[ex + \sqrt{e} \sqrt{d + e x^2}\right] \end{aligned}$$

Problem 266: Result unnecessarily involves higher level functions.

$$\int \frac{(d + e x^2)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 260 leaves, 17 steps):

$$\begin{aligned}
& -\frac{4}{3} b d n \sqrt{d+e x^2} - \frac{1}{9} b n (d+e x^2)^{3/2} + \frac{4}{3} b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] + \\
& \frac{1}{2} b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]^2 + \frac{1}{3} \left(3 d \sqrt{d+e x^2} + (d+e x^2)^{3/2} - 3 d^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]\right) (a+b \operatorname{Log}[c x^n]) - \\
& b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right] - \frac{1}{2} b d^{3/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right]
\end{aligned}$$

Result (type 5, 315 leaves):

$$\begin{aligned}
& \frac{1}{12 \sqrt{1+\frac{e x^2}{d}}} b n \sqrt{d+e x^2} \left(-3 e x^2 \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, -\frac{e x^2}{d}\right] + 4 \left(e x^2 \sqrt{1+\frac{e x^2}{d}} + d \left(-1 + \sqrt{1+\frac{e x^2}{d}}\right)\right) \operatorname{Log}[x]\right) + \\
& \frac{1}{\sqrt{1+\frac{d}{e x^2}}} b d n \sqrt{d+e x^2} \left(-\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, -\frac{d}{e x^2}\right] + \sqrt{1+\frac{d}{e x^2}} \operatorname{Log}[x] - \frac{\sqrt{d} \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} x}\right] \operatorname{Log}[x]}{\sqrt{e} x}\right) + \\
& \frac{1}{3} \sqrt{d+e x^2} (4 d+e x^2) (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) + d^{3/2} \operatorname{Log}[x] (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) - \\
& d^{3/2} (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d + \sqrt{d} \sqrt{d+e x^2}\right]
\end{aligned}$$

Problem 267: Result unnecessarily involves higher level functions.

$$\int \frac{(d+e x^2)^{3/2} (a+b \operatorname{Log}[c x^n])}{x^3} dx$$

Optimal (type 4, 295 leaves, 18 steps):

$$\begin{aligned}
& -b e n \sqrt{d+e x^2} - \frac{b d n \sqrt{d+e x^2}}{4 x^2} + \frac{3}{4} b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] + \frac{3}{4} b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]^2 + \\
& \frac{3}{2} e \sqrt{d+e x^2} (a+b \operatorname{Log}[c x^n]) - \frac{(d+e x^2)^{3/2} (a+b \operatorname{Log}[c x^n])}{2 x^2} - \frac{3}{2} \sqrt{d} e \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n]) - \\
& \frac{3}{2} b \sqrt{d} e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right] - \frac{3}{4} b \sqrt{d} e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right]
\end{aligned}$$

Result (type 5, 349 leaves):

$$\frac{1}{\sqrt{1 + \frac{d}{e x^2}}}$$

$$b e n \sqrt{d + e x^2} \left(-\text{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2} \right\}, \left\{ \frac{1}{2}, \frac{1}{2} \right\}, -\frac{d}{e x^2} \right] + \sqrt{1 + \frac{d}{e x^2}} \text{Log}[x] - \frac{\sqrt{d} \text{ArcSinh} \left[\frac{\sqrt{d}}{\sqrt{e} x} \right] \text{Log}[x]}{\sqrt{e} x} \right) - \frac{1}{4 \sqrt{1 + \frac{d}{e x^2}} x^2}$$

$$b \sqrt{d} n \sqrt{d + e x^2} \left(2 \sqrt{d} \text{HypergeometricPFQ} \left[\left\{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2} \right\}, \left\{ \frac{3}{2}, \frac{3}{2} \right\}, -\frac{d}{e x^2} \right] + \left(\sqrt{d} \sqrt{1 + \frac{d}{e x^2}} + \sqrt{e} x \text{ArcSinh} \left[\frac{\sqrt{d}}{\sqrt{e} x} \right] \right) (1 + 2 \text{Log}[x]) \right) -$$

$$\frac{(d - 2 e x^2) \sqrt{d + e x^2} (a - b n \text{Log}[x] + b \text{Log}[c x^n])}{2 x^2} + \frac{3}{2} \sqrt{d} e \text{Log}[x] (a - b n \text{Log}[x] + b \text{Log}[c x^n]) -$$

$$\frac{3}{2} \sqrt{d} e (a - b n \text{Log}[x] + b \text{Log}[c x^n]) \text{Log}[d + \sqrt{d} \sqrt{d + e x^2}]$$

Problem 268: Result unnecessarily involves higher level functions.

$$\int x^2 (d + e x^2)^{3/2} (a + b \text{Log}[c x^n]) dx$$

Optimal (type 4, 464 leaves, 19 steps):

$$-\frac{11 b d^2 n x \sqrt{d + e x^2}}{192 e} - \frac{23}{288} b d n x^3 \sqrt{d + e x^2} - \frac{1}{36} b e n x^5 \sqrt{d + e x^2} - \frac{b d^{5/2} n \sqrt{d + e x^2} \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]}{192 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} - \frac{b d^{5/2} n \sqrt{d + e x^2} \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]^2}{32 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} +$$

$$\frac{b d^{5/2} n \sqrt{d + e x^2} \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \text{Log} \left[1 - e^{2 \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]} \right]}{16 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} + \frac{d^2 x \sqrt{d + e x^2} (a + b \text{Log}[c x^n])}{16 e} + \frac{1}{8} d x^3 \sqrt{d + e x^2} (a + b \text{Log}[c x^n]) +$$

$$\frac{1}{6} x^3 (d + e x^2)^{3/2} (a + b \text{Log}[c x^n]) - \frac{d^{5/2} \sqrt{d + e x^2} \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] (a + b \text{Log}[c x^n])}{16 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} + \frac{b d^{5/2} n \sqrt{d + e x^2} \text{PolyLog} \left[2, e^{2 \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]} \right]}{32 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}}$$

Result (type 5, 331 leaves):

$$\frac{1}{3600 e^{3/2} \sqrt{1 + \frac{e x^2}{d}}} \left(-400 b d e^{3/2} n x^3 \sqrt{d + e x^2} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{e x^2}{d}\right] - \right. \\ \left. 144 b e^{5/2} n x^5 \sqrt{d + e x^2} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{e x^2}{d}\right] - \right. \\ \left. 75 \left(3 b d^{5/2} n \sqrt{d + e x^2} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] + \sqrt{1 + \frac{e x^2}{d}} \left(-a \sqrt{e} x \sqrt{d + e x^2} (3 d^2 + 14 d e x^2 + 8 e^2 x^4) + \right. \right. \right. \\ \left. \left. \left. 3 d^3 (a - b n \operatorname{Log}[x]) \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] - b \operatorname{Log}[c x^n] \left(\sqrt{e} x \sqrt{d + e x^2} (3 d^2 + 14 d e x^2 + 8 e^2 x^4) - 3 d^3 \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] \right) \right) \right) \right) \right)$$

Problem 269: Result unnecessarily involves higher level functions.

$$\int (d + e x^2)^{3/2} (a + b \operatorname{Log}[c x^n]) dx$$

Optimal (type 4, 378 leaves, 16 steps):

$$-\frac{9}{32} b d n x \sqrt{d + e x^2} - \frac{1}{16} b n x (d + e x^2)^{3/2} + \frac{3 b d^{5/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{16 \sqrt{e} \sqrt{d + e x^2}} - \frac{9 b d^2 n \operatorname{ArcTanh}\left[\frac{\sqrt{e} x}{\sqrt{d + e x^2}}\right]}{32 \sqrt{e}} - \\ \frac{3 b d^{5/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1 - e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{8 \sqrt{e} \sqrt{d + e x^2}} + \frac{3}{8} d x \sqrt{d + e x^2} (a + b \operatorname{Log}[c x^n]) + \frac{1}{4} x (d + e x^2)^{3/2} (a + b \operatorname{Log}[c x^n]) + \\ \frac{3 d^{5/2} \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{8 \sqrt{e} \sqrt{d + e x^2}} - \frac{3 b d^{5/2} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{16 \sqrt{e} \sqrt{d + e x^2}}$$

Result (type 5, 314 leaves):

$$\frac{1}{72 \sqrt{e} \sqrt{1 + \frac{ex^2}{d}}} \left(-8 b e^{3/2} n x^3 \sqrt{d + ex^2} \operatorname{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, \frac{3}{2}, \frac{3}{2} \right\}, \left\{ \frac{5}{2}, \frac{5}{2} \right\}, -\frac{ex^2}{d} \right] + \right. \\ \left. 9 \left(-4 b d \sqrt{e} n x \sqrt{d + ex^2} \operatorname{HypergeometricPFQ} \left[\left\{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2} \right\}, \left\{ \frac{3}{2}, \frac{3}{2} \right\}, -\frac{ex^2}{d} \right] + \right. \right. \\ \left. b d^{3/2} n \sqrt{d + ex^2} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] (-2 + 3 \operatorname{Log}[x]) + \sqrt{1 + \frac{ex^2}{d}} \left(\sqrt{e} x \sqrt{d + ex^2} (5 a d - 2 b d n + 2 a e x^2) + \right. \right. \\ \left. \left. 3 d^2 (a - b n \operatorname{Log}[x]) \operatorname{Log}[e x + \sqrt{e} \sqrt{d + ex^2}] + b \operatorname{Log}[c x^n] \left(\sqrt{e} x \sqrt{d + ex^2} (5 d + 2 e x^2) + 3 d^2 \operatorname{Log}[e x + \sqrt{e} \sqrt{d + ex^2}] \right) \right) \right) \right)$$

Problem 270: Result unnecessarily involves higher level functions.

$$\int \frac{(d + ex^2)^{3/2} (a + b \operatorname{Log}[c x^n])}{x^2} dx$$

Optimal (type 4, 400 leaves, 14 steps):

$$-\frac{b d n \sqrt{d + ex^2}}{x} - \frac{1}{4} b e n x \sqrt{d + ex^2} + \frac{3 b \sqrt{d} \sqrt{e} n \sqrt{d + ex^2} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]}{4 \sqrt{1 + \frac{ex^2}{d}}} + \frac{3 b \sqrt{d} \sqrt{e} n \sqrt{d + ex^2} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]^2}{4 \sqrt{1 + \frac{ex^2}{d}}} - \\ \frac{3 b \sqrt{d} \sqrt{e} n \sqrt{d + ex^2} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \operatorname{Log} \left[1 - e^{2 \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]} \right]}{2 \sqrt{1 + \frac{ex^2}{d}}} + \frac{3}{2} e x \sqrt{d + ex^2} (a + b \operatorname{Log}[c x^n]) - \frac{(d + ex^2)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} + \\ \frac{3 \sqrt{d} \sqrt{e} \sqrt{d + ex^2} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] (a + b \operatorname{Log}[c x^n])}{2 \sqrt{1 + \frac{ex^2}{d}}} - \frac{3 b \sqrt{d} \sqrt{e} n \sqrt{d + ex^2} \operatorname{PolyLog} \left[2, e^{2 \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right]} \right]}{4 \sqrt{1 + \frac{ex^2}{d}}}$$

Result (type 5, 329 leaves):

$$\begin{aligned}
& - \frac{1}{x \sqrt{1 + \frac{ex^2}{d}}} b \sqrt{d} n \sqrt{d + ex^2} \left(\sqrt{d} \operatorname{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2} \right\}, \left\{ \frac{1}{2}, \frac{1}{2} \right\}, -\frac{ex^2}{d} \right] + \left(\sqrt{d} \sqrt{1 + \frac{ex^2}{d}} - \sqrt{e} x \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \right) \operatorname{Log}[x] \right) + \\
& \frac{1}{4 \sqrt{1 + \frac{ex^2}{d}}} \\
& b \sqrt{e} n \sqrt{d + ex^2} \left(-2 \sqrt{e} x \operatorname{HypergeometricPFQ} \left[\left\{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2} \right\}, \left\{ \frac{3}{2}, \frac{3}{2} \right\}, -\frac{ex^2}{d} \right] + \left(\sqrt{e} x \sqrt{1 + \frac{ex^2}{d}} + \sqrt{d} \operatorname{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \right) (-1 + 2 \operatorname{Log}[x]) \right) - \\
& \frac{(2d - ex^2) \sqrt{d + ex^2} (a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n])}{2x} + \frac{3}{2} d \sqrt{e} (a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n]) \operatorname{Log}[ex + \sqrt{e} \sqrt{d + ex^2}]
\end{aligned}$$

Problem 271: Result unnecessarily involves higher level functions.

$$\int \frac{(d + ex^2)^{3/2} (a + b \operatorname{Log}[cx^n])}{x^4} dx$$

Optimal (type 4, 400 leaves, 13 steps):

$$\begin{aligned}
& - \frac{4ben\sqrt{d+ex^2}}{3x} - \frac{bn(d+ex^2)^{3/2}}{9x^3} + \frac{4be^{3/2}n\sqrt{d+ex^2}\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]}{3\sqrt{d}\sqrt{1+\frac{ex^2}{d}}} + \frac{be^{3/2}n\sqrt{d+ex^2}\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]^2}{2\sqrt{d}\sqrt{1+\frac{ex^2}{d}}} - \\
& \frac{be^{3/2}n\sqrt{d+ex^2}\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]\operatorname{Log}\left[1 - e^{2\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]}\right]}{\sqrt{d}\sqrt{1+\frac{ex^2}{d}}} - \frac{e\sqrt{d+ex^2}(a+b\operatorname{Log}[cx^n])}{x} - \frac{(d+ex^2)^{3/2}(a+b\operatorname{Log}[cx^n])}{3x^3} + \\
& \frac{e^{3/2}\sqrt{d+ex^2}\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right](a+b\operatorname{Log}[cx^n])}{\sqrt{d}\sqrt{1+\frac{ex^2}{d}}} - \frac{be^{3/2}n\sqrt{d+ex^2}\operatorname{PolyLog}\left[2, e^{2\operatorname{ArcSinh}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right]}\right]}{2\sqrt{d}\sqrt{1+\frac{ex^2}{d}}}
\end{aligned}$$

Result (type 5, 269 leaves):

$$\frac{b d n \sqrt{d + e x^2} \left(-\text{Hypergeometric2F1} \left[-\frac{3}{2}, -\frac{3}{2}, -\frac{1}{2}, -\frac{e x^2}{d} \right] - 3 \left(1 + \frac{e x^2}{d} \right)^{3/2} \text{Log}[x] \right)}{9 x^3 \sqrt{1 + \frac{e x^2}{d}}} + \frac{1}{x \sqrt{1 + \frac{e x^2}{d}}}$$

$$b e n \sqrt{d + e x^2} \left(-\text{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2} \right\}, \left\{ \frac{1}{2}, \frac{1}{2} \right\}, -\frac{e x^2}{d} \right] - \sqrt{1 + \frac{e x^2}{d}} \text{Log}[x] + \frac{\sqrt{e} x \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \text{Log}[x]}{\sqrt{d}} \right) -$$

$$\frac{\sqrt{d + e x^2} (d + 4 e x^2) (a - b n \text{Log}[x] + b \text{Log}[c x^n])}{3 x^3} + e^{3/2} (a - b n \text{Log}[x] + b \text{Log}[c x^n]) \text{Log}[e x + \sqrt{e} \sqrt{d + e x^2}]$$

Problem 279: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \text{Log}[c x^n]}{x \sqrt{d + e x^2}} dx$$

Optimal (type 4, 166 leaves, 8 steps):

$$\frac{b n \text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right]^2}{2 \sqrt{d}} - \frac{\text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right] (a + b \text{Log}[c x^n])}{\sqrt{d}} - \frac{b n \text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right] \text{Log} \left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}} \right]}{\sqrt{d}} - \frac{b n \text{PolyLog} \left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}} \right]}{2 \sqrt{d}}$$

Result (type 5, 162 leaves):

$$\frac{b n \sqrt{1 + \frac{d}{e x^2}} \left(-\text{HypergeometricPFQ} \left[\left\{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2} \right\}, \left\{ \frac{3}{2}, \frac{3}{2} \right\}, -\frac{d}{e x^2} \right] - \frac{\sqrt{e} x \text{ArcSinh} \left[\frac{\sqrt{d}}{\sqrt{e} x} \right] \text{Log}[x]}{\sqrt{d}} \right)}{\sqrt{d + e x^2}} -$$

$$\frac{\text{Log}[x] (-a - b (-n \text{Log}[x] + \text{Log}[c x^n]))}{\sqrt{d}} + \frac{(-a - b (-n \text{Log}[x] + \text{Log}[c x^n])) \text{Log}[d + \sqrt{d} \sqrt{d + e x^2}]}{\sqrt{d}}$$

Problem 280: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \text{Log}[c x^n]}{x^3 \sqrt{d + e x^2}} dx$$

Optimal (type 4, 258 leaves, 14 steps):

$$\begin{aligned}
& - \frac{b n \sqrt{d+e x^2}}{4 d x^2} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]}{4 d^{3/2}} - \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right]^2}{4 d^{3/2}} - \frac{\sqrt{d+e x^2} (a+b \operatorname{Log}[c x^n])}{2 d x^2} + \\
& \frac{e \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{2 d^{3/2}} + \frac{b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right]}{2 d^{3/2}} + \frac{b e n \operatorname{PolyLog}\left[2, 1-\frac{2 \sqrt{d}}{\sqrt{d}-\sqrt{d+e x^2}}\right]}{4 d^{3/2}}
\end{aligned}$$

Result (type 5, 229 leaves):

$$\begin{aligned}
& \frac{1}{36 d^{3/2}} \left(\frac{1}{x^2 \sqrt{d+e x^2}} \right. \\
& b n \sqrt{1+\frac{d}{e x^2}} \left(2 d^{3/2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{d}{e x^2}\right] + 9 e x^2 \left(-\sqrt{d} \sqrt{1+\frac{d}{e x^2}} + \sqrt{e} x \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} x}\right] \right) (1+2 \operatorname{Log}[x]) \right) - \\
& \frac{18 \sqrt{d} \sqrt{d+e x^2} (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{x^2} - 18 e \operatorname{Log}[x] (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) + \\
& \left. 18 e (a-b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d+\sqrt{d} \sqrt{d+e x^2}\right] \right)
\end{aligned}$$

Problem 281: Result unnecessarily involves higher level functions.

$$\int \frac{x^2 (a+b \operatorname{Log}[c x^n])}{\sqrt{d+e x^2}} dx$$

Optimal (type 4, 359 leaves, 12 steps):

$$\begin{aligned}
& - \frac{b n x \sqrt{d+e x^2}}{4 e} - \frac{b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{4 e^{3/2} \sqrt{d+e x^2}} - \frac{b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{4 e^{3/2} \sqrt{d+e x^2}} + \frac{b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1-e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{2 e^{3/2} \sqrt{d+e x^2}} + \\
& \frac{x \sqrt{d+e x^2} (a+b \operatorname{Log}[c x^n])}{2 e} - \frac{d^{3/2} \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{2 e^{3/2} \sqrt{d+e x^2}} + \frac{b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{4 e^{3/2} \sqrt{d+e x^2}}
\end{aligned}$$

Result (type 5, 205 leaves):

$$\frac{1}{36 e^2} \left(\frac{1}{\sqrt{d + e x^2}} \right.$$

$$b n \sqrt{1 + \frac{e x^2}{d}} \left(2 e^2 x^3 \text{HypergeometricPFQ} \left[\left\{ \frac{3}{2}, \frac{3}{2}, \frac{3}{2} \right\}, \left\{ \frac{5}{2}, \frac{5}{2} \right\}, -\frac{e x^2}{d} \right] + 9 d \sqrt{e} \left(\sqrt{e} x \sqrt{1 + \frac{e x^2}{d}} - \sqrt{d} \text{ArcSinh} \left[\frac{\sqrt{e} x}{\sqrt{d}} \right] \right) (-1 + 2 \text{Log}[x]) \right) +$$

$$\left. 18 e x \sqrt{d + e x^2} (a - b n \text{Log}[x] + b \text{Log}[c x^n]) - 18 d \sqrt{e} (a - b n \text{Log}[x] + b \text{Log}[c x^n]) \text{Log}[e x + \sqrt{e} \sqrt{d + e x^2}] \right)$$

Problem 290: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \text{Log}[c x^n]}{x (d + e x^2)^{3/2}} dx$$

Optimal (type 4, 209 leaves, 11 steps):

$$\frac{b n \text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right]}{d^{3/2}} + \frac{b n \text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right]^2}{2 d^{3/2}} + \left(\frac{1}{d \sqrt{d + e x^2}} - \frac{\text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right]}{d^{3/2}} \right) (a + b \text{Log}[c x^n]) -$$

$$\frac{b n \text{ArcTanh} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d}} \right] \text{Log} \left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}} \right]}{d^{3/2}} - \frac{b n \text{PolyLog} \left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}} \right]}{2 d^{3/2}}$$

Result (type 5, 241 leaves):

$$\frac{1}{9 d^{3/2} e x^2 \sqrt{d + e x^2}} \left(-b d^{3/2} n \sqrt{1 + \frac{d}{e x^2}} \text{HypergeometricPFQ} \left[\left\{ \frac{3}{2}, \frac{3}{2}, \frac{3}{2} \right\}, \left\{ \frac{5}{2}, \frac{5}{2} \right\}, -\frac{d}{e x^2} \right] + \right.$$

$$9 e x^2 \left(-b \sqrt{e} n \sqrt{1 + \frac{d}{e x^2}} x \text{ArcSinh} \left[\frac{\sqrt{d}}{\sqrt{e} x} \right] \text{Log}[x] - b n \sqrt{d + e x^2} \text{Log}[x]^2 + \right.$$

$$\left. \left. \left. \sqrt{d + e x^2} \text{Log}[x] (a + b \text{Log}[c x^n] + b n \text{Log}[d + \sqrt{d} \sqrt{d + e x^2}]) + (a + b \text{Log}[c x^n]) (\sqrt{d} - \sqrt{d + e x^2} \text{Log}[d + \sqrt{d} \sqrt{d + e x^2}]) \right) \right) \right)$$

Problem 291: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^3 (d + e x^2)^{3/2}} dx$$

Optimal (type 4, 287 leaves, 12 steps):

$$\begin{aligned} & -\frac{b n \sqrt{d + e x^2}}{4 d^2 x^2} - \frac{5 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]}{4 d^{5/2}} - \frac{3 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]^2}{4 d^{5/2}} - \frac{3 e (a + b \operatorname{Log}[c x^n])}{2 d^2 \sqrt{d + e x^2}} - \frac{a + b \operatorname{Log}[c x^n]}{2 d x^2 \sqrt{d + e x^2}} + \\ & \frac{3 e \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2 d^{5/2}} + \frac{3 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{2 d^{5/2}} + \frac{3 b e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{4 d^{5/2}} \end{aligned}$$

Result (type 5, 218 leaves):

$$\begin{aligned} & \frac{1}{50 d^{5/2} e x^4 \sqrt{d + e x^2}} \\ & \left(3 b d^{5/2} n \sqrt{1 + \frac{d}{e x^2}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{d}{e x^2}\right] - 5 b d^{5/2} n \sqrt{1 + \frac{d}{e x^2}} \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, \frac{5}{2}, \frac{7}{2}, -\frac{d}{e x^2}\right] (1 + 2 \operatorname{Log}[x]) - \right. \\ & \left. 25 e x^2 (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \left(\sqrt{d} (d + 3 e x^2) + 3 e x^2 \sqrt{d + e x^2} \operatorname{Log}[x] - 3 e x^2 \sqrt{d + e x^2} \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}] \right) \right) \end{aligned}$$

Problem 292: Result unnecessarily involves higher level functions.

$$\int \frac{x^2 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^{3/2}} dx$$

Optimal (type 4, 328 leaves, 11 steps):

$$\begin{aligned} & \frac{b \sqrt{d} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{e^{3/2} \sqrt{d + e x^2}} + \frac{b \sqrt{d} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{2 e^{3/2} \sqrt{d + e x^2}} - \frac{b \sqrt{d} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[1 - e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{e^{3/2} \sqrt{d + e x^2}} - \\ & \frac{x (a + b \operatorname{Log}[c x^n])}{e \sqrt{d + e x^2}} + \frac{\sqrt{d} \sqrt{1 + \frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{e^{3/2} \sqrt{d + e x^2}} - \frac{b \sqrt{d} n \sqrt{1 + \frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}\right]}{2 e^{3/2} \sqrt{d + e x^2}} \end{aligned}$$

Result (type 5, 217 leaves):

$$\begin{aligned}
 & -\frac{1}{9 d e^{3/2} (d + e x^2)^{3/2}} b n \sqrt{1 + \frac{e x^2}{d}} \\
 & \left(e^{3/2} x^3 (d + e x^2) \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{e x^2}{d}\right] + 9 d^2 \sqrt{e} x \sqrt{1 + \frac{e x^2}{d}} \operatorname{Log}[x] - 9 d^{3/2} (d + e x^2) \operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[x] \right) - \\
 & \frac{x (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{e \sqrt{d + e x^2}} + \frac{(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}[e x + \sqrt{e} \sqrt{d + e x^2}]}{e^{3/2}}
 \end{aligned}$$

Problem 301: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^2)^{5/2}} dx$$

Optimal (type 4, 251 leaves, 15 steps):

$$\begin{aligned}
 & -\frac{b n}{3 d^2 \sqrt{d + e x^2}} + \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]}{3 d^{5/2}} + \frac{b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]^2}{2 d^{5/2}} + \\
 & \frac{1}{3} \left(\frac{1}{d (d + e x^2)^{3/2}} + \frac{3}{d^2 \sqrt{d + e x^2}} - \frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]}{d^{5/2}} \right) (a + b \operatorname{Log}[c x^n]) - \frac{b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{d^{5/2}} - \frac{b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{2 d^{5/2}}
 \end{aligned}$$

Result (type 5, 273 leaves):

$$\begin{aligned}
 & \frac{1}{75 d^{5/2} e^2 x^4 (d + e x^2)^{5/2}} b n \sqrt{1 + \frac{d}{e x^2}} \left(-3 d^{5/2} (d + e x^2)^2 \operatorname{HypergeometricPFQ}\left[\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{d}{e x^2}\right] + \right. \\
 & \left. 25 \sqrt{d} e^3 \sqrt{1 + \frac{d}{e x^2}} x^6 (4 d + 3 e x^2) \operatorname{Log}[x] - 75 e^{5/2} x^5 (d + e x^2)^2 \operatorname{ArcSinh}\left[\frac{\sqrt{d}}{\sqrt{e} x}\right] \operatorname{Log}[x] \right) + \\
 & \frac{(4 d + 3 e x^2) (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{3 d^2 (d + e x^2)^{3/2}} + \frac{\operatorname{Log}[x] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{d^{5/2}} - \frac{(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}]}{d^{5/2}}
 \end{aligned}$$

Problem 302: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x^3 (d + e x^2)^{5/2}} dx$$

Optimal (type 4, 337 leaves, 14 steps):

$$\begin{aligned} & \frac{b e n}{3 d^3 \sqrt{d + e x^2}} - \frac{b n \sqrt{d + e x^2}}{4 d^3 x^2} - \frac{31 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]}{12 d^{7/2}} - \frac{5 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right]^2}{4 d^{7/2}} - \frac{5 e (a + b \operatorname{Log}[c x^n])}{6 d^2 (d + e x^2)^{3/2}} - \frac{a + b \operatorname{Log}[c x^n]}{2 d x^2 (d + e x^2)^{3/2}} \\ & \frac{5 e (a + b \operatorname{Log}[c x^n])}{2 d^3 \sqrt{d + e x^2}} + \frac{5 e \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{2 d^{7/2}} + \frac{5 b e n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{2 d^{7/2}} + \frac{5 b e n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^2}}\right]}{4 d^{7/2}} \end{aligned}$$

Result (type 5, 227 leaves):

$$\begin{aligned} & \frac{1}{98 e^2 x^6 \sqrt{d + e x^2}} b n \sqrt{1 + \frac{d}{e x^2}} \left(5 \operatorname{HypergeometricPFQ}\left[\left\{\frac{7}{2}, \frac{7}{2}, \frac{7}{2}\right\}, \left\{\frac{9}{2}, \frac{9}{2}\right\}, -\frac{d}{e x^2}\right] - 7 \operatorname{Hypergeometric2F1}\left[\frac{5}{2}, \frac{7}{2}, \frac{9}{2}, -\frac{d}{e x^2}\right] (1 + 2 \operatorname{Log}[x]) \right) - \\ & \frac{(3 d^2 + 20 d e x^2 + 15 e^2 x^4) (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{6 d^3 x^2 (d + e x^2)^{3/2}} - \\ & \frac{5 e \operatorname{Log}[x] (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{2 d^{7/2}} + \frac{5 e (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}[d + \sqrt{d} \sqrt{d + e x^2}]}{2 d^{7/2}} \end{aligned}$$

Problem 303: Result unnecessarily involves higher level functions.

$$\int \frac{x^6 (a + b \operatorname{Log}[c x^n])}{(d + e x^2)^{5/2}} dx$$

Optimal (type 4, 443 leaves, 24 steps):

$$\frac{b d n x}{3 e^3 \sqrt{d+e x^2}} - \frac{b n x \sqrt{d+e x^2}}{4 e^3} - \frac{31 b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}{12 e^{7/2} \sqrt{d+e x^2}} - \frac{5 b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]^2}{4 e^{7/2} \sqrt{d+e x^2}} +$$

$$\frac{5 b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] \operatorname{Log}\left[1-e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}\right]}{2 e^{7/2} \sqrt{d+e x^2}} - \frac{x^5 (a+b \operatorname{Log}[c x^n])}{3 e (d+e x^2)^{3/2}} - \frac{5 x^3 (a+b \operatorname{Log}[c x^n])}{3 e^2 \sqrt{d+e x^2}} +$$

$$\frac{5 x \sqrt{d+e x^2} (a+b \operatorname{Log}[c x^n])}{2 e^3} - \frac{5 d^{3/2} \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{2 e^{7/2} \sqrt{d+e x^2}} + \frac{5 b d^{3/2} n \sqrt{1+\frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}\right]}{4 e^{7/2} \sqrt{d+e x^2}}$$

Result (type 5, 199 leaves):

$$\frac{1}{98 d^2 \sqrt{d+e x^2}} b n x^7 \sqrt{1+\frac{e x^2}{d}} \left(5 \operatorname{HypergeometricPFQ}\left[\left\{\frac{7}{2}, \frac{7}{2}, \frac{7}{2}\right\}, \left\{\frac{9}{2}, \frac{9}{2}\right\}, -\frac{e x^2}{d}\right] + 7 \operatorname{Hypergeometric2F1}\left[\frac{5}{2}, \frac{7}{2}, \frac{9}{2}, -\frac{e x^2}{d}\right] (-1+2 \operatorname{Log}[x]) \right) +$$

$$\frac{x (15 d^2 + 20 d e x^2 + 3 e^2 x^4) (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])}{6 e^3 (d+e x^2)^{3/2}} - \frac{5 d (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[e x + \sqrt{e} \sqrt{d+e x^2}\right]}{2 e^{7/2}}$$

Problem 304: Result unnecessarily involves higher level functions.

$$\int \frac{x^4 (a+b \operatorname{Log}[c x^n])}{(d+e x^2)^{5/2}} dx$$

Optimal (type 4, 383 leaves, 13 steps):

$$-\frac{b n x}{3 e^2 \sqrt{d+e x^2}} + \frac{4 b \sqrt{d} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}{3 e^{5/2} \sqrt{d+e x^2}} + \frac{b \sqrt{d} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]^2}{2 e^{5/2} \sqrt{d+e x^2}} -$$

$$\frac{b \sqrt{d} n \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] \operatorname{Log}\left[1-e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}\right]}{e^{5/2} \sqrt{d+e x^2}} - \frac{x^3 (a+b \operatorname{Log}[c x^n])}{3 e (d+e x^2)^{3/2}} - \frac{x (a+b \operatorname{Log}[c x^n])}{e^2 \sqrt{d+e x^2}} +$$

$$\frac{\sqrt{d} \sqrt{1+\frac{e x^2}{d}} \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right] (a+b \operatorname{Log}[c x^n])}{e^{5/2} \sqrt{d+e x^2}} - \frac{b \sqrt{d} n \sqrt{1+\frac{e x^2}{d}} \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e x}}{\sqrt{d}}\right]}\right]}{2 e^{5/2} \sqrt{d+e x^2}}$$

Result (type 5, 244 leaves):

$$\begin{aligned}
 & - \frac{1}{75 d^2 e^{5/2} (d + e x^2)^{5/2}} b n \sqrt{1 + \frac{e x^2}{d}} \left(3 e^{5/2} x^5 (d + e x^2)^2 \text{HypergeometricPFQ}\left[\left\{\frac{5}{2}, \frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\frac{e x^2}{d}\right] + \right. \\
 & \quad \left. 25 d^3 \sqrt{e} x (3 d + 4 e x^2) \sqrt{1 + \frac{e x^2}{d}} \text{Log}[x] - 75 d^{5/2} (d + e x^2)^2 \text{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \text{Log}[x] \right) - \\
 & \quad \frac{x (3 d + 4 e x^2) (a - b n \text{Log}[x] + b \text{Log}[c x^n])}{3 e^2 (d + e x^2)^{3/2}} + \frac{(a - b n \text{Log}[x] + b \text{Log}[c x^n]) \text{Log}[e x + \sqrt{e} \sqrt{d + e x^2}]}{e^{5/2}}
 \end{aligned}$$

Problem 312: Result unnecessarily involves higher level functions.

$$\int \frac{a + b \text{Log}[c x^n]}{x^3 \sqrt{d - e x} \sqrt{d + e x}} dx$$

Optimal (type 4, 489 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{b n (d^2 - e^2 x^2)}{4 d^2 x^2 \sqrt{d - e x} \sqrt{d + e x}} + \frac{b e^2 n \sqrt{1 - \frac{e^2 x^2}{d^2}} \text{ArcTanh}\left[\sqrt{1 - \frac{e^2 x^2}{d^2}}\right]}{4 d^2 \sqrt{d - e x} \sqrt{d + e x}} + \frac{b e^2 n \sqrt{1 - \frac{e^2 x^2}{d^2}} \text{ArcTanh}\left[\sqrt{1 - \frac{e^2 x^2}{d^2}}\right]^2}{4 d^2 \sqrt{d - e x} \sqrt{d + e x}} - \\
 & \quad \frac{(d^2 - e^2 x^2) (a + b \text{Log}[c x^n])}{2 d^2 x^2 \sqrt{d - e x} \sqrt{d + e x}} - \frac{e^2 \sqrt{1 - \frac{e^2 x^2}{d^2}} \text{ArcTanh}\left[\sqrt{1 - \frac{e^2 x^2}{d^2}}\right] (a + b \text{Log}[c x^n])}{2 d^2 \sqrt{d - e x} \sqrt{d + e x}} - \\
 & \quad \frac{b e^2 n \sqrt{1 - \frac{e^2 x^2}{d^2}} \text{ArcTanh}\left[\sqrt{1 - \frac{e^2 x^2}{d^2}}\right] \text{Log}\left[\frac{2}{1 - \sqrt{1 - \frac{e^2 x^2}{d^2}}}\right]}{2 d^2 \sqrt{d - e x} \sqrt{d + e x}} - \frac{b e^2 n \sqrt{1 - \frac{e^2 x^2}{d^2}} \text{PolyLog}\left[2, -\frac{1 + \sqrt{1 - \frac{e^2 x^2}{d^2}}}{1 - \sqrt{1 - \frac{e^2 x^2}{d^2}}}\right]}{4 d^2 \sqrt{d - e x} \sqrt{d + e x}}
 \end{aligned}$$

Result (type 5, 255 leaves):

$$\frac{1}{36 d^3} \left(\left(b n (-d^2 + e^2 x^2) \left(2 d^3 \text{HypergeometricPFQ} \left[\left\{ \frac{3}{2}, \frac{3}{2}, \frac{3}{2} \right\}, \left\{ \frac{5}{2}, \frac{5}{2} \right\}, \frac{d^2}{e^2 x^2} \right] + 9 e^2 x^2 \left(d \sqrt{1 - \frac{d^2}{e^2 x^2}} - e x \text{ArcSin} \left[\frac{d}{e x} \right] \right) (1 + 2 \text{Log}[x]) \right) \right) / \right. \\ \left. \left(e^2 \sqrt{1 - \frac{d^2}{e^2 x^2}} x^4 \sqrt{d - e x} \sqrt{d + e x} \right) - \frac{18 d \sqrt{d - e x} \sqrt{d + e x} (a - b n \text{Log}[x] + b \text{Log}[c x^n])}{x^2} + \right. \\ \left. 18 e^2 \text{Log}[x] (a - b n \text{Log}[x] + b \text{Log}[c x^n]) - 18 e^2 (a - b n \text{Log}[x] + b \text{Log}[c x^n]) \text{Log}[d + \sqrt{d - e x} \sqrt{d + e x}] \right)$$

Problem 348: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log} \left[\frac{a}{x} \right]}{a x - x^2} dx$$

Optimal (type 4, 14 leaves, 4 steps):

$$\frac{\text{PolyLog} \left[2, 1 - \frac{a}{x} \right]}{a}$$

Result (type 4, 61 leaves):

$$\frac{2 \text{Log} \left[\frac{a}{x} \right] (\text{Log}[x] - \text{Log}[-a + x]) + \text{Log}[x] \left(\text{Log}[x] - 2 \text{Log}[-a + x] + 2 \text{Log} \left[1 - \frac{x}{a} \right] \right) + 2 \text{PolyLog} \left[2, \frac{x}{a} \right]}{2 a}$$

Problem 349: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log} \left[\frac{a}{x^2} \right]}{a x - x^3} dx$$

Optimal (type 4, 17 leaves, 4 steps):

$$\frac{\text{PolyLog} \left[2, 1 - \frac{a}{x^2} \right]}{2 a}$$

Result (type 4, 104 leaves):

$$\frac{1}{2a} \left(2 \operatorname{Log} \left[\frac{a}{x^2} \right] \operatorname{Log}[x] + 2 \operatorname{Log}[x]^2 + 2 \operatorname{Log}[x] \operatorname{Log} \left[1 - \frac{x}{\sqrt{a}} \right] + 2 \operatorname{Log}[x] \operatorname{Log} \left[1 + \frac{x}{\sqrt{a}} \right] - \right. \\ \left. \operatorname{Log} \left[\frac{a}{x^2} \right] \operatorname{Log}[-a + x^2] - 2 \operatorname{Log}[x] \operatorname{Log}[-a + x^2] + 2 \operatorname{PolyLog} \left[2, -\frac{x}{\sqrt{a}} \right] + 2 \operatorname{PolyLog} \left[2, \frac{x}{\sqrt{a}} \right] \right)$$

Problem 350: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[a x^{1-n}]}{a x - x^n} dx$$

Optimal (type 4, 26 leaves, 3 steps):

$$-\frac{\operatorname{PolyLog} \left[2, 1 - a x^{1-n} \right]}{a (1-n)}$$

Result (type 4, 103 leaves):

$$\frac{1}{2a(-1+n)} \left((-1+n^2) \operatorname{Log}[x]^2 + 2 \operatorname{Log}[x] \left(n \operatorname{Log}[a x^{1-n}] + (-1+n) \left(\operatorname{Log} \left[1 - \frac{x^{-1+n}}{a} \right] - \operatorname{Log}[-a x + x^n] \right) \right) - 2 \operatorname{Log}[a x^{1-n}] \operatorname{Log}[-a x + x^n] + 2 \operatorname{PolyLog} \left[2, \frac{x^{-1+n}}{a} \right] \right)$$

Problem 363: Result more than twice size of optimal antiderivative.

$$\int \frac{(f x)^{-1+m} (a + b \operatorname{Log}[c x^n])^2}{d + e x^m} dx$$

Optimal (type 4, 129 leaves, 4 steps):

$$\frac{x^{1-m} (f x)^{-1+m} (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log} \left[1 + \frac{e x^m}{d} \right]}{e m} + \frac{2 b n x^{1-m} (f x)^{-1+m} (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog} \left[2, -\frac{e x^m}{d} \right]}{e m^2} - \frac{2 b^2 n^2 x^{1-m} (f x)^{-1+m} \operatorname{PolyLog} \left[3, -\frac{e x^m}{d} \right]}{e m^3}$$

Result (type 4, 502 leaves):

$$\frac{1}{3 e f m^3}$$

$$\begin{aligned} & x^{-m} (f x)^m \left(3 a^2 m^3 \operatorname{Log}[x] - 6 a b m^3 n \operatorname{Log}[x]^2 + 4 b^2 m^3 n^2 \operatorname{Log}[x]^3 + 6 a b m^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 6 b^2 m^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 3 b^2 m^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + \right. \\ & 3 b^2 m^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{d x^{-m}}{e}\right] + 3 a^2 m^2 \operatorname{Log}[d - d x^m] - 6 a b m^2 n \operatorname{Log}[x] \operatorname{Log}[d - d x^m] + 3 b^2 m^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[d - d x^m] + \\ & 6 a b m^2 \operatorname{Log}[c x^n] \operatorname{Log}[d - d x^m] - 6 b^2 m^2 n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d - d x^m] + 3 b^2 m^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d - d x^m] + \\ & 6 a b m^2 n \operatorname{Log}[x] \operatorname{Log}[d + e x^m] - 6 b^2 m^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[d + e x^m] - 6 a b m n \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[d + e x^m] + \\ & 6 b^2 m n^2 \operatorname{Log}[x] \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[d + e x^m] + 6 b^2 m^2 n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^m] - 6 b^2 m n \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[c x^n] \operatorname{Log}[d + e x^m] - \\ & \left. 6 b^2 m n^2 \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{d x^{-m}}{e}\right] - 6 b m n (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, 1 + \frac{e x^m}{d}\right] - 6 b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{d x^{-m}}{e}\right] \right) \end{aligned}$$

Problem 430: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2}{x (d + e x^r)} dx$$

Optimal (type 4, 94 leaves, 3 steps):

$$-\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{d x^{-r}}{e}\right]}{d r} + \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{d x^{-r}}{e}\right]}{d r^2} + \frac{2 b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{d x^{-r}}{e}\right]}{d r^3}$$

Result (type 4, 270 leaves):

$$\begin{aligned} & -\frac{1}{d r^3} \left(a^2 r^2 \operatorname{Log}[d - d x^r] - 2 a b r^2 (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) \operatorname{Log}[d - d x^r] + \right. \\ & b^2 r^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \operatorname{Log}[d - d x^r] - 2 a b n r \left(\frac{1}{2} r^2 \operatorname{Log}[x]^2 + \left(-r \operatorname{Log}[x] + \operatorname{Log}\left[-\frac{e x^r}{d}\right] \right) \operatorname{Log}[d + e x^r] + \operatorname{PolyLog}\left[2, 1 + \frac{e x^r}{d}\right] \right) + \\ & 2 b^2 n r (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) \left(\frac{1}{2} r^2 \operatorname{Log}[x]^2 + \left(-r \operatorname{Log}[x] + \operatorname{Log}\left[-\frac{e x^r}{d}\right] \right) \operatorname{Log}[d + e x^r] + \operatorname{PolyLog}\left[2, 1 + \frac{e x^r}{d}\right] \right) + \\ & \left. b^2 n^2 \left(r^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{d x^{-r}}{e}\right] - 2 r \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{d x^{-r}}{e}\right] - 2 \operatorname{PolyLog}\left[3, -\frac{d x^{-r}}{e}\right] \right) \right) \end{aligned}$$

Problem 431: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2}{x (d + e x^r)^2} dx$$

Optimal (type 4, 182 leaves, 7 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^2}{d r (d + e x^r)} + \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{d x^{-r}}{e}\right]}{d^2 r^2} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{d x^{-r}}{e}\right]}{d^2 r} -$$

$$\frac{2 b^2 n^2 \operatorname{PolyLog}\left[2, -\frac{d x^{-r}}{e}\right]}{d^2 r^3} + \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{d x^{-r}}{e}\right]}{d^2 r^2} + \frac{2 b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{d x^{-r}}{e}\right]}{d^2 r^3}$$

Result (type 4, 397 leaves):

$$\frac{1}{d^2 r^3} \left(\frac{d r^2 (a + b \operatorname{Log}[c x^n])^2}{d + e x^r} + 2 a b n r \operatorname{Log}[d - d x^r] - a^2 r^2 \operatorname{Log}[d - d x^r] + \right.$$

$$2 a b r^2 (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) \operatorname{Log}[d - d x^r] + 2 b^2 n r (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) \operatorname{Log}[d - d x^r] -$$

$$b^2 r^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \operatorname{Log}[d - d x^r] - 2 b^2 n^2 \left(\frac{1}{2} r^2 \operatorname{Log}[x]^2 + \left(-r \operatorname{Log}[x] + \operatorname{Log}\left[-\frac{e x^r}{d}\right] \right) \operatorname{Log}[d + e x^r] + \operatorname{PolyLog}\left[2, 1 + \frac{e x^r}{d}\right] \right) +$$

$$2 a b n r \left(\frac{1}{2} r^2 \operatorname{Log}[x]^2 + \left(-r \operatorname{Log}[x] + \operatorname{Log}\left[-\frac{e x^r}{d}\right] \right) \operatorname{Log}[d + e x^r] + \operatorname{PolyLog}\left[2, 1 + \frac{e x^r}{d}\right] \right) +$$

$$2 b^2 n r (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) \left(\frac{1}{2} r^2 \operatorname{Log}[x]^2 + \left(-r \operatorname{Log}[x] + \operatorname{Log}\left[-\frac{e x^r}{d}\right] \right) \operatorname{Log}[d + e x^r] + \operatorname{PolyLog}\left[2, 1 + \frac{e x^r}{d}\right] \right) -$$

$$b^2 n^2 \left(r^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{d x^{-r}}{e}\right] - 2 r \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{d x^{-r}}{e}\right] - 2 \operatorname{PolyLog}\left[3, -\frac{d x^{-r}}{e}\right] \right) \Bigg)$$

Problem 433: Unable to integrate problem.

$$\int \frac{(d + e x^r)^{5/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 327 leaves, 23 steps):

$$-\frac{92 b d^2 n \sqrt{d + e x^r}}{15 r^2} - \frac{32 b d n (d + e x^r)^{3/2}}{45 r^2} - \frac{4 b n (d + e x^r)^{5/2}}{25 r^2} + \frac{92 b d^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{15 r^2} + \frac{2 b d^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]^2}{r^2} +$$

$$\frac{2}{15} \left(\frac{15 d^2 \sqrt{d + e x^r}}{r} + \frac{5 d (d + e x^r)^{3/2}}{r} + \frac{3 (d + e x^r)^{5/2}}{r} - \frac{15 d^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{r} \right) (a + b \operatorname{Log}[c x^n]) -$$

$$\frac{4 b d^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2\sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2} - \frac{2 b d^{5/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2\sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2}$$

Result (type 8, 27 leaves):

$$\int \frac{(d + e x^r)^{5/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Problem 434: Unable to integrate problem.

$$\int \frac{(d + e x^r)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 284 leaves, 17 steps):

$$\begin{aligned} & -\frac{16 b d n \sqrt{d + e x^r}}{3 r^2} - \frac{4 b n (d + e x^r)^{3/2}}{9 r^2} + \frac{16 b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{3 r^2} + \\ & \frac{2 b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]^2}{r^2} + \frac{2}{3} \left(\frac{3 d \sqrt{d + e x^r}}{r} + \frac{(d + e x^r)^{3/2}}{r} - \frac{3 d^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{r} \right) (a + b \operatorname{Log}[c x^n]) - \\ & \frac{4 b d^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2} - \frac{2 b d^{3/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(d + e x^r)^{3/2} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Problem 435: Unable to integrate problem.

$$\int \frac{\sqrt{d + e x^r} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Optimal (type 4, 240 leaves, 12 steps):

$$\begin{aligned} & -\frac{4 b n \sqrt{d + e x^r}}{r^2} + \frac{4 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{r^2} + \frac{2 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]^2}{r^2} + \\ & 2 \left(\frac{\sqrt{d + e x^r}}{r} - \frac{\sqrt{d} \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{r} \right) (a + b \operatorname{Log}[c x^n]) - \frac{4 b \sqrt{d} n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2} - \frac{2 b \sqrt{d} n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{r^2} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\sqrt{d + e x^r} (a + b \operatorname{Log}[c x^n])}{x} dx$$

Problem 436: Unable to integrate problem.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x \sqrt{d + e x^r}} dx$$

Optimal (type 4, 174 leaves, 8 steps):

$$\frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right]^2}{\sqrt{d} r^2} - \frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{\sqrt{d} r} - \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^r}}\right]}{\sqrt{d} r^2} - \frac{2 b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^r}}\right]}{\sqrt{d} r^2}$$

Result (type 8, 27 leaves):

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x \sqrt{d + e x^r}} dx$$

Problem 437: Unable to integrate problem.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{3/2}} dx$$

Optimal (type 4, 225 leaves, 11 steps):

$$\frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right]}{d^{3/2} r^2} + \frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right]^2}{d^{3/2} r^2} + 2 \left(\frac{1}{d r \sqrt{d + e x^r}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right]}{d^{3/2} r} \right) (a + b \operatorname{Log}[c x^n]) - \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d+e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^r}}\right]}{d^{3/2} r^2} - \frac{2 b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d+e x^r}}\right]}{d^{3/2} r^2}$$

Result (type 8, 27 leaves):

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{3/2}} dx$$

Problem 438: Unable to integrate problem.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{5/2}} dx$$

Optimal (type 4, 271 leaves, 15 steps):

$$\begin{aligned} & - \frac{4 b n}{3 d^2 r^2 \sqrt{d + e x^r}} + \frac{16 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{3 d^{5/2} r^2} + \frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]^2}{d^{5/2} r^2} + \\ & \frac{2}{3} \left(\frac{1}{d r (d + e x^r)^{3/2}} + \frac{3}{d^2 r \sqrt{d + e x^r}} - \frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{d^{5/2} r} \right) (a + b \operatorname{Log}[c x^n]) - \\ & \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{d^{5/2} r^2} - \frac{2 b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{d^{5/2} r^2} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{5/2}} dx$$

Problem 439: Unable to integrate problem.

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{7/2}} dx$$

Optimal (type 4, 314 leaves, 20 steps):

$$\begin{aligned}
& - \frac{4 b n}{15 d^2 r^2 (d + e x^r)^{3/2}} - \frac{32 b n}{15 d^3 r^2 \sqrt{d + e x^r}} + \frac{92 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{15 d^{7/2} r^2} + \frac{2 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]^2}{d^{7/2} r^2} + \\
& \frac{2}{15} \left(\frac{3}{d r (d + e x^r)^{5/2}} + \frac{5}{d^2 r (d + e x^r)^{3/2}} + \frac{15}{d^3 r \sqrt{d + e x^r}} - \frac{15 \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right]}{d^{7/2} r} \right) (a + b \operatorname{Log}[c x^n]) - \\
& \frac{4 b n \operatorname{ArcTanh}\left[\frac{\sqrt{d + e x^r}}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{d^{7/2} r^2} - \frac{2 b n \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} - \sqrt{d + e x^r}}\right]}{d^{7/2} r^2}
\end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{a + b \operatorname{Log}[c x^n]}{x (d + e x^r)^{7/2}} dx$$

Problem 456: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x) (a + b \operatorname{Log}[c x^n])^3}{(d + e x)^3} dx$$

Optimal (type 4, 295 leaves, 11 steps):

$$\begin{aligned}
& - \frac{3 b (e f - d g) n x (a + b \operatorname{Log}[c x^n])^2}{2 d^2 e (d + e x)} + \frac{f^2 (a + b \operatorname{Log}[c x^n])^3}{2 d^2 (e f - d g)} - \frac{(f + g x)^2 (a + b \operatorname{Log}[c x^n])^3}{2 (e f - d g) (d + e x)^2} + \\
& \frac{3 b^2 (e f - d g) n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{e x}{d}\right]}{d^2 e^2} - \frac{3 b (e f + d g) n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{e x}{d}\right]}{2 d^2 e^2} + \\
& \frac{3 b^3 (e f - d g) n^3 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{d^2 e^2} - \frac{3 b^2 (e f + d g) n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]}{d^2 e^2} + \frac{3 b^3 (e f + d g) n^3 \operatorname{PolyLog}\left[3, -\frac{e x}{d}\right]}{d^2 e^2}
\end{aligned}$$

Result (type 4, 674 leaves):

$$\begin{aligned}
& - \frac{1}{2 d^2 e^2 (d+e x)^2} \left(-3 b (e f+d g) n (d+e x)^2 \operatorname{Log}[x] (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n])^2 + \right. \\
& 3 b d^2 n (d g+e (f+2 g x)) \operatorname{Log}[x] (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n])^2 - d^2 (-e f+d g) (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n])^3 + \\
& d (d+e x) (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n])^2 (2 a d g-3 b e f n+3 b d g n+2 b d g (-n \operatorname{Log}[x]+\operatorname{Log}[c x^n])) + \\
& 3 b (e f+d g) n (d+e x)^2 (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d+e x]+3 b^2 d g n^2 (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n]) \\
& \left. \left(-e^2 x^2 \operatorname{Log}[x]^2+2 (d+e x)^2 \operatorname{Log}\left[1+\frac{e x}{d}\right]+2 (d+e x) \operatorname{Log}[x] \left(-e x+(d+e x) \operatorname{Log}\left[1+\frac{e x}{d}\right]\right)+2 (d+e x)^2 \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right]\right) + \right. \\
& 3 b^2 e f n^2 (a-b n \operatorname{Log}[x]+b \operatorname{Log}[c x^n]) \left(-e x(2 d+e x) \operatorname{Log}[x]^2-2 (d+e x)^2 \operatorname{Log}\left[1+\frac{e x}{d}\right]+2 (d+e x) \operatorname{Log}[x] \left(e x+(d+e x) \operatorname{Log}\left[1+\frac{e x}{d}\right]\right) \right) + \\
& 2 (d+e x)^2 \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right]+b^3 e f n^3 \left(-e x(2 d+e x) \operatorname{Log}[x]^3+3 (d+e x) \operatorname{Log}[x]^2 \left(e x+(d+e x) \operatorname{Log}\left[1+\frac{e x}{d}\right]\right) - \right. \\
& 6 (d+e x)^2 \operatorname{Log}[x] \left(\operatorname{Log}\left[1+\frac{e x}{d}\right]-\operatorname{PolyLog}\left[2,-\frac{e x}{d}\right]\right)-6 (d+e x)^2 \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right]-6 (d+e x)^2 \operatorname{PolyLog}\left[3,-\frac{e x}{d}\right]\left. \right) + \\
& b^3 d g n^3 \left(\operatorname{Log}[x] \left(-e^2 x^2 \operatorname{Log}[x]^2+6 (d+e x)^2 \operatorname{Log}\left[1+\frac{e x}{d}\right]+3 (d+e x) \operatorname{Log}[x] \left(-e x+(d+e x) \operatorname{Log}\left[1+\frac{e x}{d}\right]\right) \right) \right) + \\
& \left. 6 (d+e x)^2 (1+\operatorname{Log}[x]) \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right]-6 (d+e x)^2 \operatorname{PolyLog}\left[3,-\frac{e x}{d}\right]\right)
\end{aligned}$$

Test results for the 249 problems in "3.1.5 u (a+b log(c x^n))^p.m"

Problem 22: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1+e x]}{x^2} dx$$

Optimal (type 4, 342 leaves, 14 steps):

$$\begin{aligned}
& 6 b^3 e n^3 \operatorname{Log}[x] - 6 b^2 e n^2 \operatorname{Log}\left[1+\frac{1}{e x}\right] (a+b \operatorname{Log}[c x^n]) - 3 b e n \operatorname{Log}\left[1+\frac{1}{e x}\right] (a+b \operatorname{Log}[c x^n])^2 - e \operatorname{Log}\left[1+\frac{1}{e x}\right] (a+b \operatorname{Log}[c x^n])^3 - \\
& 6 b^3 e n^3 \operatorname{Log}[1+e x] - \frac{6 b^3 n^3 \operatorname{Log}[1+e x]}{x} - \frac{6 b^2 n^2 (a+b \operatorname{Log}[c x^n]) \operatorname{Log}[1+e x]}{x} - \frac{3 b n (a+b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1+e x]}{x} - \\
& \frac{(a+b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1+e x]}{x} + 6 b^3 e n^3 \operatorname{PolyLog}\left[2,-\frac{1}{e x}\right] + 6 b^2 e n^2 (a+b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2,-\frac{1}{e x}\right] + \\
& 3 b e n (a+b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2,-\frac{1}{e x}\right] + 6 b^3 e n^3 \operatorname{PolyLog}\left[3,-\frac{1}{e x}\right] + 6 b^2 e n^2 (a+b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3,-\frac{1}{e x}\right] + 6 b^3 e n^3 \operatorname{PolyLog}\left[4,-\frac{1}{e x}\right]
\end{aligned}$$

Result (type 4, 770 leaves):

$$\begin{aligned}
& a^3 e \operatorname{Log}[x] + 3 a^2 b e n \operatorname{Log}[x] + 6 a b^2 e n^2 \operatorname{Log}[x] + 6 b^3 e n^3 \operatorname{Log}[x] - \frac{3}{2} a^2 b e n \operatorname{Log}[x]^2 - 3 a b^2 e n^2 \operatorname{Log}[x]^2 - 3 b^3 e n^3 \operatorname{Log}[x]^2 + a b^2 e n^2 \operatorname{Log}[x]^3 + \\
& b^3 e n^3 \operatorname{Log}[x]^3 - \frac{1}{4} b^3 e n^3 \operatorname{Log}[x]^4 + 3 a^2 b e \operatorname{Log}[x] \operatorname{Log}[c x^n] + 6 a b^2 e n \operatorname{Log}[x] \operatorname{Log}[c x^n] + 6 b^3 e n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 3 a b^2 e n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - \\
& 3 b^3 e n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + b^3 e n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] + 3 a b^2 e \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 3 b^3 e n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - \frac{3}{2} b^3 e n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 + \\
& b^3 e \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 - a^3 e \operatorname{Log}[1 + e x] - 3 a^2 b e n \operatorname{Log}[1 + e x] - 6 a b^2 e n^2 \operatorname{Log}[1 + e x] - 6 b^3 e n^3 \operatorname{Log}[1 + e x] - \frac{a^3 \operatorname{Log}[1 + e x]}{x} - \\
& \frac{3 a^2 b n \operatorname{Log}[1 + e x]}{x} - \frac{6 a b^2 n^2 \operatorname{Log}[1 + e x]}{x} - \frac{6 b^3 n^3 \operatorname{Log}[1 + e x]}{x} - 3 a^2 b e \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x] - 6 a b^2 e n \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x] - \\
& 6 b^3 e n^2 \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x] - \frac{3 a^2 b \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x]}{x} - \frac{6 a b^2 n \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x]}{x} - \frac{6 b^3 n^2 \operatorname{Log}[c x^n] \operatorname{Log}[1 + e x]}{x} - \\
& 3 a b^2 e \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + e x] - 3 b^3 e n \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + e x] - \frac{3 a b^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + e x]}{x} - \frac{3 b^3 n \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + e x]}{x} - \\
& b^3 e \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + e x] - \frac{b^3 \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + e x]}{x} - 3 b e n (a^2 + 2 a b n + 2 b^2 n^2 + 2 b (a + b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2) \operatorname{PolyLog}[2, -e x] + \\
& 6 b^2 e n^2 (a + b n + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, -e x] - 6 b^3 e n^3 \operatorname{PolyLog}[4, -e x]
\end{aligned}$$

Problem 23: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + e x]}{x^3} dx$$

Optimal (type 4, 470 leaves, 22 steps):

$$\begin{aligned}
& -\frac{45 b^3 e n^3}{8 x} - \frac{3}{8} b^3 e^2 n^3 \operatorname{Log}[x] - \frac{21 b^2 e n^2 (a + b \operatorname{Log}[c x^n])}{4 x} + \frac{3}{4} b^2 e^2 n^2 \operatorname{Log}\left[1 + \frac{1}{e x}\right] (a + b \operatorname{Log}[c x^n]) - \frac{9 b e n (a + b \operatorname{Log}[c x^n])^2}{4 x} + \\
& \frac{3}{4} b e^2 n \operatorname{Log}\left[1 + \frac{1}{e x}\right] (a + b \operatorname{Log}[c x^n])^2 - \frac{e (a + b \operatorname{Log}[c x^n])^3}{2 x} + \frac{1}{2} e^2 \operatorname{Log}\left[1 + \frac{1}{e x}\right] (a + b \operatorname{Log}[c x^n])^3 + \frac{3}{8} b^3 e^2 n^3 \operatorname{Log}[1 + e x] - \\
& \frac{3 b^3 n^3 \operatorname{Log}[1 + e x]}{8 x^2} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + e x]}{4 x^2} - \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + e x]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + e x]}{2 x^2} - \\
& \frac{3}{4} b^3 e^2 n^3 \operatorname{PolyLog}\left[2, -\frac{1}{e x}\right] - \frac{3}{2} b^2 e^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{1}{e x}\right] - \frac{3}{2} b e^2 n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{1}{e x}\right] - \\
& \frac{3}{2} b^3 e^2 n^3 \operatorname{PolyLog}\left[3, -\frac{1}{e x}\right] - 3 b^2 e^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{1}{e x}\right] - 3 b^3 e^2 n^3 \operatorname{PolyLog}\left[4, -\frac{1}{e x}\right]
\end{aligned}$$

Result (type 4, 1047 leaves):

$$\begin{aligned}
& -\frac{1}{8x^2} \left(4a^3 ex + 18a^2 benx + 42ab^2 en^2 x + 45b^3 en^3 x + 4a^3 e^2 x^2 \operatorname{Log}[x] + 6a^2 b e^2 n x^2 \operatorname{Log}[x] + 6ab^2 e^2 n^2 x^2 \operatorname{Log}[x] + 3b^3 e^2 n^3 x^2 \operatorname{Log}[x] - \right. \\
& 6a^2 b e^2 n x^2 \operatorname{Log}[x]^2 - 6ab^2 e^2 n^2 x^2 \operatorname{Log}[x]^2 - 3b^3 e^2 n^3 x^2 \operatorname{Log}[x]^2 + 4ab^2 e^2 n^2 x^2 \operatorname{Log}[x]^3 + 2b^3 e^2 n^3 x^2 \operatorname{Log}[x]^3 - b^3 e^2 n^3 x^2 \operatorname{Log}[x]^4 + \\
& 12a^2 b ex \operatorname{Log}[cx^n] + 36ab^2 enx \operatorname{Log}[cx^n] + 42b^3 en^2 x \operatorname{Log}[cx^n] + 12a^2 b e^2 x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] + 12ab^2 e^2 n x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] + \\
& 6b^3 e^2 n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] - 12ab^2 e^2 n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] - 6b^3 e^2 n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] + 4b^3 e^2 n^2 x^2 \operatorname{Log}[x]^3 \operatorname{Log}[cx^n] + \\
& 12ab^2 ex \operatorname{Log}[cx^n]^2 + 18b^3 enx \operatorname{Log}[cx^n]^2 + 12ab^2 e^2 x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 + 6b^3 e^2 n x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 - \\
& 6b^3 e^2 n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n]^2 + 4b^3 ex \operatorname{Log}[cx^n]^3 + 4b^3 e^2 x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^3 + 4a^3 \operatorname{Log}[1+ex] + 6a^2 bn \operatorname{Log}[1+ex] + \\
& 6ab^2 n^2 \operatorname{Log}[1+ex] + 3b^3 n^3 \operatorname{Log}[1+ex] - 4a^3 e^2 x^2 \operatorname{Log}[1+ex] - 6a^2 b e^2 n x^2 \operatorname{Log}[1+ex] - 6ab^2 e^2 n^2 x^2 \operatorname{Log}[1+ex] - \\
& 3b^3 e^2 n^3 x^2 \operatorname{Log}[1+ex] + 12a^2 b \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] + 12ab^2 n \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] + 6b^3 n^2 \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] - \\
& 12a^2 b e^2 x^2 \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] - 12ab^2 e^2 n x^2 \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] - 6b^3 e^2 n^2 x^2 \operatorname{Log}[cx^n] \operatorname{Log}[1+ex] + 12ab^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[1+ex] + \\
& 6b^3 n \operatorname{Log}[cx^n]^2 \operatorname{Log}[1+ex] - 12ab^2 e^2 x^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[1+ex] - 6b^3 e^2 n x^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[1+ex] + 4b^3 \operatorname{Log}[cx^n]^3 \operatorname{Log}[1+ex] - \\
& 4b^3 e^2 x^2 \operatorname{Log}[cx^n]^3 \operatorname{Log}[1+ex] - 6be^2 n x^2 (2a^2 + 2abn + b^2 n^2 + 2b(2a+bn) \operatorname{Log}[cx^n] + 2b^2 \operatorname{Log}[cx^n]^2) \operatorname{PolyLog}[2, -ex] + \\
& \left. 12b^2 e^2 n^2 x^2 (2a+bn + 2b \operatorname{Log}[cx^n]) \operatorname{PolyLog}[3, -ex] - 24b^3 e^2 n^3 x^2 \operatorname{PolyLog}[4, -ex] \right)
\end{aligned}$$

Problem 24: Result unnecessarily involves imaginary or complex numbers.

$$\int x^3 (a + b \operatorname{Log}[cx^n]) \operatorname{Log}\left[d \left(\frac{1}{d} + fx^2\right)\right] dx$$

Optimal (type 4, 180 leaves, 7 steps):

$$\begin{aligned}
& -\frac{3bnx^2}{16df} + \frac{1}{16}bnx^4 + \frac{x^2(a+b\operatorname{Log}[cx^n])}{4df} - \frac{1}{8}x^4(a+b\operatorname{Log}[cx^n]) + \frac{bn\operatorname{Log}[1+dfx^2]}{16d^2f^2} - \\
& \frac{1}{16}bnx^4\operatorname{Log}[1+dfx^2] - \frac{(a+b\operatorname{Log}[cx^n])\operatorname{Log}[1+dfx^2]}{4d^2f^2} + \frac{1}{4}x^4(a+b\operatorname{Log}[cx^n])\operatorname{Log}[1+dfx^2] - \frac{bn\operatorname{PolyLog}[2, -dfx^2]}{8d^2f^2}
\end{aligned}$$

Result (type 4, 356 leaves):

$$\begin{aligned}
& \frac{ax^2}{4df} - \frac{ax^4}{8} + \frac{1}{32}bx^4(n-4(-n\operatorname{Log}[x] + \operatorname{Log}[cx^n])) + \frac{bx^2(-n+4(-n\operatorname{Log}[x] + \operatorname{Log}[cx^n]))}{16df} - \frac{a\operatorname{Log}[1+dfx^2]}{4d^2f^2} + \frac{1}{4}ax^4\operatorname{Log}[1+dfx^2] + \\
& \frac{b(n-4(-n\operatorname{Log}[x] + \operatorname{Log}[cx^n]))\operatorname{Log}[1+dfx^2]}{16d^2f^2} + \frac{1}{16}bx^4(-n+4n\operatorname{Log}[x] + 4(-n\operatorname{Log}[x] + \operatorname{Log}[cx^n]))\operatorname{Log}[1+dfx^2] - \\
& \frac{1}{2}bdfn \left(-\frac{-\frac{x^2}{4} + \frac{1}{2}x^2\operatorname{Log}[x]}{d^2f^2} + \frac{-\frac{x^4}{16} + \frac{1}{4}x^4\operatorname{Log}[x]}{df} + \frac{\operatorname{Log}[x]\operatorname{Log}[1+i\sqrt{d}\sqrt{f}x] + \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x]}{2df} + \frac{\operatorname{Log}[x]\operatorname{Log}[1-i\sqrt{d}\sqrt{f}x] + \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x]}{2df} \right)
\end{aligned}$$

Problem 25: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right] dx$$

Optimal (type 4, 114 leaves, 8 steps):

$$\frac{1}{2} b n x^2 - \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n]) - \frac{b n (1 + d f x^2) \operatorname{Log}[1 + d f x^2]}{4 d f} + \frac{(1 + d f x^2) (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{2 d f} + \frac{b n \operatorname{PolyLog}[2, -d f x^2]}{4 d f}$$

Result (type 4, 286 leaves):

$$\begin{aligned} & -\frac{a x^2}{2} + \frac{1}{4} b x^2 (n - 2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) + \frac{a \operatorname{Log}[1 + d f x^2]}{2 d f} + \frac{1}{2} a x^2 \operatorname{Log}[1 + d f x^2] + \\ & \frac{b (-n + 2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) \operatorname{Log}[1 + d f x^2]}{4 d f} + \frac{1}{4} b x^2 (-n + 2 n \operatorname{Log}[x] + 2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])) \operatorname{Log}[1 + d f x^2] - \\ & b d f n \left(\frac{-\frac{x^2}{4} + \frac{1}{2} x^2 \operatorname{Log}[x]}{d f} - \frac{\frac{\operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x]}{2 d f} + \frac{\operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x]}{2 d f}}{d f} \right) \end{aligned}$$

Problem 26: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right]}{x} dx$$

Optimal (type 4, 39 leaves, 2 steps):

$$-\frac{1}{2} (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^2] + \frac{1}{4} b n \operatorname{PolyLog}[3, -d f x^2]$$

Result (type 4, 319 leaves):

$$\frac{1}{2} b \operatorname{Log}[x] \left(n \operatorname{Log}[x] + 2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \right) \operatorname{Log}[1 + d f x^2] - 2 b d f \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \\ \left(\frac{\operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x]}{2 d f} + \frac{\operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x]}{2 d f} \right) - \\ \frac{1}{2} a \operatorname{PolyLog}[2, -d f x^2] - b d f n \left(\frac{\frac{1}{2} \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x]}{d f} + \right. \\ \left. \frac{\frac{1}{2} \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x]}{d f} \right)$$

Problem 27: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right]}{x^3} dx$$

Optimal (type 4, 141 leaves, 9 steps):

$$\frac{1}{2} b d f n \operatorname{Log}[x] - \frac{1}{2} b d f n \operatorname{Log}[x]^2 + d f \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) - \frac{1}{4} b d f n \operatorname{Log}[1 + d f x^2] - \frac{b n \operatorname{Log}[1 + d f x^2]}{4 x^2} - \\ \frac{1}{2} d f (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2] - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{2 x^2} - \frac{1}{4} b d f n \operatorname{PolyLog}[2, -d f x^2]$$

Result (type 4, 252 leaves):

$$a d f \operatorname{Log}[x] + \frac{1}{2} b d f \operatorname{Log}[x] \left(n + 2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \right) - \frac{1}{2} a d f \operatorname{Log}[1 + d f x^2] - \frac{a \operatorname{Log}[1 + d f x^2]}{2 x^2} - \\ \frac{1}{4} b d f \left(n + 2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \right) \operatorname{Log}[1 + d f x^2] - \frac{b \left(n + 2 n \operatorname{Log}[x] + 2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \right) \operatorname{Log}[1 + d f x^2]}{4 x^2} + \\ b d f n \left(\frac{\operatorname{Log}[x]^2}{2} - d f \left(\frac{\operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x]}{2 d f} + \frac{\operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x]}{2 d f} \right) \right)$$

Problem 32: Result unnecessarily involves imaginary or complex numbers.

$$\int x^3 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right] dx$$

Optimal (type 4, 367 leaves, 13 steps):

$$\begin{aligned} & \frac{7 b^2 n^2 x^2}{32 d f} - \frac{3}{64} b^2 n^2 x^4 - \frac{3 b n x^2 (a + b \operatorname{Log}[c x^n])}{8 d f} + \frac{1}{8} b n x^4 (a + b \operatorname{Log}[c x^n]) + \frac{x^2 (a + b \operatorname{Log}[c x^n])^2}{4 d f} - \frac{1}{8} x^4 (a + b \operatorname{Log}[c x^n])^2 - \frac{b^2 n^2 \operatorname{Log}[1 + d f x^2]}{32 d^2 f^2} + \\ & \frac{1}{32} b^2 n^2 x^4 \operatorname{Log}[1 + d f x^2] + \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{8 d^2 f^2} - \frac{1}{8} b n x^4 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2] - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{4 d^2 f^2} + \\ & \frac{1}{4} x^4 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2] + \frac{b^2 n^2 \operatorname{PolyLog}[2, -d f x^2]}{16 d^2 f^2} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^2]}{4 d^2 f^2} + \frac{b^2 n^2 \operatorname{PolyLog}[3, -d f x^2]}{8 d^2 f^2} \end{aligned}$$

Result (type 4, 673 leaves):

$$\begin{aligned} & \frac{1}{64 d^2 f^2} \left(2 d f x^2 \left(8 a^2 - 4 a b n + b^2 n^2 + 4 b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 16 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 8 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \right) - \right. \\ & d^2 f^2 x^4 \left(8 a^2 - 4 a b n + b^2 n^2 + 4 b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 16 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 8 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \right) + \\ & 2 d^2 f^2 x^4 \left(8 a^2 - 4 a b n + b^2 n^2 - 4 b (-4 a + b n) \operatorname{Log}[c x^n] + 8 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{Log}[1 + d f x^2] - \\ & 2 \left(8 a^2 - 4 a b n + b^2 n^2 + 4 b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 16 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 8 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \right) \operatorname{Log}[1 + d f x^2] + \\ & b n (-4 a + b n + 4 b n \operatorname{Log}[x] - 4 b \operatorname{Log}[c x^n]) \left(4 d f x^2 - d^2 f^2 x^4 - 8 d f x^2 \operatorname{Log}[x] + 4 d^2 f^2 x^4 \operatorname{Log}[x] + \right. \\ & \left. 8 \operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + 8 \operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 8 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + 8 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] \right) - \\ & b^2 n^2 \left(-8 d f x^2 + d^2 f^2 x^4 + 16 d f x^2 \operatorname{Log}[x] - 4 d^2 f^2 x^4 \operatorname{Log}[x] - 16 d f x^2 \operatorname{Log}[x]^2 + 8 d^2 f^2 x^4 \operatorname{Log}[x]^2 + \right. \\ & \left. 16 \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + 16 \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 32 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \right. \\ & \left. 32 \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - 32 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 32 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] \right) \end{aligned}$$

Problem 33: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right] dx$$

Optimal (type 4, 241 leaves, 15 steps):

$$\begin{aligned} & -\frac{3}{4} b^2 n^2 x^2 + b n x^2 (a + b \operatorname{Log}[c x^n]) - \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n])^2 + \frac{b^2 n^2 (1 + d f x^2) \operatorname{Log}[1 + d f x^2]}{4 d f} - \frac{b n (1 + d f x^2) (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{2 d f} + \\ & \frac{(1 + d f x^2) (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{2 d f} - \frac{b^2 n^2 \operatorname{PolyLog}[2, -d f x^2]}{4 d f} + \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^2]}{2 d f} - \frac{b^2 n^2 \operatorname{PolyLog}[3, -d f x^2]}{4 d f} \end{aligned}$$

Result (type 4, 519 leaves):

$$\begin{aligned}
& \frac{1}{4df} \left(-dfx^2 \left(2a^2 - 2abn + b^2n^2 + 2b^2n \left(n \operatorname{Log}[x] - \operatorname{Log}[cx^n] \right) \right) + 4ab \left(-n \operatorname{Log}[x] + \operatorname{Log}[cx^n] \right) + 2b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[cx^n] \right)^2 \right) + \\
& dfx^2 \left(2a^2 - 2abn + b^2n^2 - 2b \left(-2a + bn \right) \operatorname{Log}[cx^n] + 2b^2 \operatorname{Log}[cx^n]^2 \right) \operatorname{Log}[1 + dfx^2] + \\
& \left(2a^2 - 2abn + b^2n^2 + 2b^2n \left(n \operatorname{Log}[x] - \operatorname{Log}[cx^n] \right) \right) + 4ab \left(-n \operatorname{Log}[x] + \operatorname{Log}[cx^n] \right) + 2b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[cx^n] \right)^2 \right) \operatorname{Log}[1 + dfx^2] + \\
& 2bn \left(2a - bn - 2bn \operatorname{Log}[x] + 2b \operatorname{Log}[cx^n] \right) \\
& \left(\frac{1}{2} dfx^2 - dfx^2 \operatorname{Log}[x] + \operatorname{Log}[x] \operatorname{Log}[1 - i\sqrt{d}\sqrt{f}x] + \operatorname{Log}[x] \operatorname{Log}[1 + i\sqrt{d}\sqrt{f}x] + \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x] + \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x] \right) - \\
& b^2n^2 \left(dfx^2 - 2dfx^2 \operatorname{Log}[x] + 2dfx^2 \operatorname{Log}[x]^2 - 2 \operatorname{Log}[x]^2 \operatorname{Log}[1 - i\sqrt{d}\sqrt{f}x] - 2 \operatorname{Log}[x]^2 \operatorname{Log}[1 + i\sqrt{d}\sqrt{f}x] - \right. \\
& \left. 4 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x] - 4 \operatorname{Log}[x] \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x] + 4 \operatorname{PolyLog}[3, -i\sqrt{d}\sqrt{f}x] + 4 \operatorname{PolyLog}[3, i\sqrt{d}\sqrt{f}x] \right)
\end{aligned}$$

Problem 34: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[cx^n])^2 \operatorname{Log}\left[d \left(\frac{1}{d} + fx^2\right)\right]}{x} dx$$

Optimal (type 4, 70 leaves, 3 steps):

$$-\frac{1}{2} (a + b \operatorname{Log}[cx^n])^2 \operatorname{PolyLog}[2, -dfx^2] + \frac{1}{2} bn (a + b \operatorname{Log}[cx^n]) \operatorname{PolyLog}[3, -dfx^2] - \frac{1}{4} b^2n^2 \operatorname{PolyLog}[4, -dfx^2]$$

Result (type 4, 484 leaves):

$$\begin{aligned}
& \frac{1}{3} \left(\operatorname{Log}[x] \left(b^2n^2 \operatorname{Log}[x]^2 - 3bn \operatorname{Log}[x] (a + b \operatorname{Log}[cx^n]) + 3(a + b \operatorname{Log}[cx^n])^2 \right) \operatorname{Log}[1 + dfx^2] - \right. \\
& 3(a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n])^2 \left(\operatorname{Log}[x] \left(\operatorname{Log}[1 - i\sqrt{d}\sqrt{f}x] + \operatorname{Log}[1 + i\sqrt{d}\sqrt{f}x] \right) + \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x] + \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x] \right) + \\
& 3bn \left(-a + bn \operatorname{Log}[x] - b \operatorname{Log}[cx^n] \right) \left(\operatorname{Log}[x]^2 \operatorname{Log}[1 - i\sqrt{d}\sqrt{f}x] + \operatorname{Log}[x]^2 \operatorname{Log}[1 + i\sqrt{d}\sqrt{f}x] + \right. \\
& \left. 2 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x] + 2 \operatorname{Log}[x] \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x] - 2 \operatorname{PolyLog}[3, -i\sqrt{d}\sqrt{f}x] - 2 \operatorname{PolyLog}[3, i\sqrt{d}\sqrt{f}x] \right) - \\
& b^2n^2 \left(\operatorname{Log}[x]^3 \operatorname{Log}[1 - i\sqrt{d}\sqrt{f}x] + \operatorname{Log}[x]^3 \operatorname{Log}[1 + i\sqrt{d}\sqrt{f}x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, -i\sqrt{d}\sqrt{f}x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, i\sqrt{d}\sqrt{f}x] - \right. \\
& \left. 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, -i\sqrt{d}\sqrt{f}x] - 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, i\sqrt{d}\sqrt{f}x] + 6 \operatorname{PolyLog}[4, -i\sqrt{d}\sqrt{f}x] + 6 \operatorname{PolyLog}[4, i\sqrt{d}\sqrt{f}x] \right)
\end{aligned}$$

Problem 35: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[cx^n])^2 \operatorname{Log}\left[d \left(\frac{1}{d} + fx^2\right)\right]}{x^3} dx$$

Optimal (type 4, 257 leaves, 11 steps):

$$\begin{aligned} & \frac{1}{2} b^2 d f n^2 \operatorname{Log}[x] - \frac{1}{2} b d f n \operatorname{Log}\left[1 + \frac{1}{d f x^2}\right] (a + b \operatorname{Log}[c x^n]) - \frac{1}{2} d f \operatorname{Log}\left[1 + \frac{1}{d f x^2}\right] (a + b \operatorname{Log}[c x^n])^2 - \\ & \frac{1}{4} b^2 d f n^2 \operatorname{Log}[1 + d f x^2] - \frac{b^2 n^2 \operatorname{Log}[1 + d f x^2]}{4 x^2} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{2 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{2 x^2} + \\ & \frac{1}{4} b^2 d f n^2 \operatorname{PolyLog}\left[2, -\frac{1}{d f x^2}\right] + \frac{1}{2} b d f n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{1}{d f x^2}\right] + \frac{1}{4} b^2 d f n^2 \operatorname{PolyLog}\left[3, -\frac{1}{d f x^2}\right] \end{aligned}$$

Result (type 4, 488 leaves):

$$\begin{aligned} & \frac{1}{4} \left(2 d f \operatorname{Log}[x] (2 a^2 + 2 a b n + b^2 n^2 + 4 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 2 b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 2 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2) - \right. \\ & \quad \left. \frac{(2 a^2 + 2 a b n + b^2 n^2 + 2 b (2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2) \operatorname{Log}[1 + d f x^2]}{x^2} - \right. \\ & \quad d f (2 a^2 + 2 a b n + b^2 n^2 + 4 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 2 b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 2 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2) \operatorname{Log}[1 + d f x^2] - \\ & \quad 2 b d f n (-2 a - b n + 2 b n \operatorname{Log}[x] - 2 b \operatorname{Log}[c x^n]) \\ & \quad \left. (\operatorname{Log}[x] (\operatorname{Log}[x] - \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x]) - \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x]) + \right. \\ & \quad \left. \frac{2}{3} b^2 d f n^2 (2 \operatorname{Log}[x]^3 - 3 \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - 3 \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] - 6 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \right. \\ & \quad \left. \left. 6 \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x]) \right) \right) \end{aligned}$$

Problem 40: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x^3 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right] dx$$

Optimal (type 4, 591 leaves, 22 steps):

$$\begin{aligned}
& - \frac{45 b^3 n^3 x^2}{128 d f} + \frac{3}{64} b^3 n^3 x^4 + \frac{21 b^2 n^2 x^2 (a + b \operatorname{Log}[c x^n])}{32 d f} - \frac{9}{64} b^2 n^2 x^4 (a + b \operatorname{Log}[c x^n]) - \frac{9 b n x^2 (a + b \operatorname{Log}[c x^n])^2}{16 d f} + \\
& \frac{3}{16} b n x^4 (a + b \operatorname{Log}[c x^n])^2 + \frac{x^2 (a + b \operatorname{Log}[c x^n])^3}{4 d f} - \frac{1}{8} x^4 (a + b \operatorname{Log}[c x^n])^3 + \frac{3 b^3 n^3 \operatorname{Log}[1 + d f x^2]}{128 d^2 f^2} - \frac{3}{128} b^3 n^3 x^4 \operatorname{Log}[1 + d f x^2] - \\
& \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{32 d^2 f^2} + \frac{3}{32} b^2 n^2 x^4 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2] + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{16 d^2 f^2} - \\
& \frac{3}{16} b n x^4 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2] - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + d f x^2]}{4 d^2 f^2} + \frac{1}{4} x^4 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + d f x^2] - \\
& \frac{3 b^3 n^3 \operatorname{PolyLog}[2, -d f x^2]}{64 d^2 f^2} + \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^2]}{16 d^2 f^2} - \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[2, -d f x^2]}{8 d^2 f^2} - \\
& \frac{3 b^3 n^3 \operatorname{PolyLog}[3, -d f x^2]}{32 d^2 f^2} + \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, -d f x^2]}{8 d^2 f^2} - \frac{3 b^3 n^3 \operatorname{PolyLog}[4, -d f x^2]}{16 d^2 f^2}
\end{aligned}$$

Result (type 4, 1250 leaves):

$$\begin{aligned}
& \frac{1}{256 d^2 f^2} \\
& \left(2 d f x^2 \left(32 a^3 - 24 a^2 b n + 12 a b^2 n^2 - 3 b^3 n^3 + 48 a b^2 n \left(n \operatorname{Log}[x] - \operatorname{Log}[c x^n] \right) + 96 a^2 b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 12 b^3 n^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) \right) + \right. \\
& \quad 96 a b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 - 24 b^3 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 32 b^3 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^3 \left. - \right. \\
& d^2 f^2 x^4 \left(32 a^3 - 24 a^2 b n + 12 a b^2 n^2 - 3 b^3 n^3 + 48 a b^2 n \left(n \operatorname{Log}[x] - \operatorname{Log}[c x^n] \right) + 96 a^2 b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + \right. \\
& \quad 12 b^3 n^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 96 a b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 - 24 b^3 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 32 b^3 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^3 \left. + 2 d^2 \right. \\
& \quad f^2 x^4 \left(32 a^3 - 24 a^2 b n + 12 a b^2 n^2 - 3 b^3 n^3 + 12 b \left(8 a^2 - 4 a b n + b^2 n^2 \right) \operatorname{Log}[c x^n] - 24 b^2 \left(-4 a + b n \right) \operatorname{Log}[c x^n]^2 + 32 b^3 \operatorname{Log}[c x^n]^3 \right) \operatorname{Log}[1 + d f x^2] - \\
& 2 \left(32 a^3 - 24 a^2 b n + 12 a b^2 n^2 - 3 b^3 n^3 + 48 a b^2 n \left(n \operatorname{Log}[x] - \operatorname{Log}[c x^n] \right) + 96 a^2 b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 12 b^3 n^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + \right. \\
& \quad 96 a b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 - 24 b^3 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 32 b^3 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^3 \left. \right) \operatorname{Log}[1 + d f x^2] - \\
& 24 b n \left(8 a^2 - 4 a b n + b^2 n^2 + 4 b^2 n \left(n \operatorname{Log}[x] - \operatorname{Log}[c x^n] \right) + 16 a b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 8 b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 \right) \\
& \left(\frac{1}{2} d f x^2 - \frac{1}{8} d^2 f^2 x^4 - d f x^2 \operatorname{Log}[x] + \frac{1}{2} d^2 f^2 x^4 \operatorname{Log}[x] + \operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \right. \\
& \quad \left. \operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] \right) + \\
& 3 b^2 n^2 \left(-4 a + b n + 4 b n \operatorname{Log}[x] - 4 b \operatorname{Log}[c x^n] \right) \left(-8 d f x^2 + d^2 f^2 x^4 + 16 d f x^2 \operatorname{Log}[x] - 4 d^2 f^2 x^4 \operatorname{Log}[x] - 16 d f x^2 \operatorname{Log}[x]^2 + \right. \\
& \quad 8 d^2 f^2 x^4 \operatorname{Log}[x]^2 + 16 \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + 16 \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 32 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \\
& \quad \left. 32 \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - 32 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 32 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] \right) + \\
& b^3 n^3 \left(d^2 f^2 x^4 \left(3 - 12 \operatorname{Log}[x] + 24 \operatorname{Log}[x]^2 - 32 \operatorname{Log}[x]^3 \right) + 16 d f x^2 \left(-3 + 6 \operatorname{Log}[x] - 6 \operatorname{Log}[x]^2 + 4 \operatorname{Log}[x]^3 \right) - \right. \\
& \quad 64 \left(\operatorname{Log}[x]^3 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x]^3 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - \right. \\
& \quad \left. \left. 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, -i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, i \sqrt{d} \sqrt{f} x] \right) \right) \left. \right)
\end{aligned}$$

Problem 41: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x \left(a + b \operatorname{Log}[c x^n] \right)^3 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2 \right) \right] dx$$

Optimal (type 4, 411 leaves, 24 steps):

$$\begin{aligned}
& \frac{3}{2} b^3 n^3 x^2 - \frac{9}{4} b^2 n^2 x^2 (a + b \operatorname{Log}[c x^n]) + \frac{3}{2} b n x^2 (a + b \operatorname{Log}[c x^n])^2 - \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n])^3 - \\
& \frac{3 b^3 n^3 (1 + d f x^2) \operatorname{Log}[1 + d f x^2]}{8 d f} + \frac{3 b^2 n^2 (1 + d f x^2) (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{4 d f} - \\
& \frac{3 b n (1 + d f x^2) (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{4 d f} + \frac{(1 + d f x^2) (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + d f x^2]}{2 d f} + \\
& \frac{3 b^3 n^3 \operatorname{PolyLog}[2, -d f x^2]}{8 d f} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^2]}{4 d f} + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[2, -d f x^2]}{4 d f} + \\
& \frac{3 b^3 n^3 \operatorname{PolyLog}[3, -d f x^2]}{8 d f} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, -d f x^2]}{4 d f} + \frac{3 b^3 n^3 \operatorname{PolyLog}[4, -d f x^2]}{8 d f}
\end{aligned}$$

Result (type 4, 990 leaves):

$$\begin{aligned}
& \frac{1}{8 d f} \\
& \left(-d f x^2 \left(4 a^3 - 6 a^2 b n + 6 a b^2 n^2 - 3 b^3 n^3 + 12 a b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 12 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 12 \right. \right. \\
& \quad \left. \left. a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - 6 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + 4 b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) + \right. \\
& d f x^2 \left(4 a^3 - 6 a^2 b n + 6 a b^2 n^2 - 3 b^3 n^3 + 6 b (2 a^2 - 2 a b n + b^2 n^2) \operatorname{Log}[c x^n] - 6 b^2 (-2 a + b n) \operatorname{Log}[c x^n]^2 + 4 b^3 \operatorname{Log}[c x^n]^3 \right) \operatorname{Log}[1 + d f x^2] + \\
& \left(4 a^3 - 6 a^2 b n + 6 a b^2 n^2 - 3 b^3 n^3 + 12 a b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 12 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + \right. \\
& \quad \left. 12 a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - 6 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + 4 b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) \operatorname{Log}[1 + d f x^2] + \\
& 6 b n \left(2 a^2 - 2 a b n + b^2 n^2 + 2 b^2 n (n \operatorname{Log}[x] - \operatorname{Log}[c x^n]) + 4 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 2 b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \right) \\
& \left(\frac{1}{2} d f x^2 - d f x^2 \operatorname{Log}[x] + \operatorname{Log}[x] \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x] \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] \right) + \\
& 3 b^2 n^2 (-2 a + b n + 2 b n \operatorname{Log}[x] - 2 b \operatorname{Log}[c x^n]) \left(d f x^2 - 2 d f x^2 \operatorname{Log}[x] + 2 d f x^2 \operatorname{Log}[x]^2 - 2 \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - \right. \\
& \quad \left. 2 \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] - 4 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - 4 \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] + \right. \\
& \quad \left. 4 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] + 4 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] \right) + b^3 n^3 \left(d f x^2 (3 - 6 \operatorname{Log}[x] + 6 \operatorname{Log}[x]^2 - 4 \operatorname{Log}[x]^3) + \right. \\
& \quad \left. 4 \left(\operatorname{Log}[x]^3 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x]^3 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - \right. \right. \\
& \quad \left. \left. 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, -i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, i \sqrt{d} \sqrt{f} x] \right) \right)
\end{aligned}$$

Problem 42: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right]}{x} dx$$

Optimal (type 4, 101 leaves, 4 steps):

$$-\frac{1}{2} (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}[2, -d f x^2] + \frac{3}{4} b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[3, -d f x^2] -$$

$$\frac{3}{4} b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[4, -d f x^2] + \frac{3}{8} b^3 n^3 \operatorname{PolyLog}[5, -d f x^2]$$

Result (type 4, 754 leaves):

$$\frac{1}{4} \left(-\operatorname{Log}[x] \left(b^3 n^3 \operatorname{Log}[x]^3 - 4 b^2 n^2 \operatorname{Log}[x]^2 (a + b \operatorname{Log}[c x^n]) + 6 b n \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n])^2 - 4 (a + b \operatorname{Log}[c x^n])^3 \right) \operatorname{Log}[1 + d f x^2] - \right.$$

$$4 (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^3 \left(\operatorname{Log}[x] \left(\operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] \right) + \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] \right) -$$

$$6 b n (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^2 \left(\operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 2 \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \right.$$

$$2 \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - 2 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 2 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] \left. \right) + 4 b^2 n^2 (-a + b n \operatorname{Log}[x] - b \operatorname{Log}[c x^n])$$

$$\left(\operatorname{Log}[x]^3 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x]^3 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + 3 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - \right.$$

$$6 \operatorname{Log}[x] \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 6 \operatorname{Log}[x] \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, -i \sqrt{d} \sqrt{f} x] + 6 \operatorname{PolyLog}[4, i \sqrt{d} \sqrt{f} x] \left. \right) -$$

$$b^3 n^3 \left(\operatorname{Log}[x]^4 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] + \operatorname{Log}[x]^4 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] + 4 \operatorname{Log}[x]^3 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] + \right.$$

$$4 \operatorname{Log}[x]^3 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] - 12 \operatorname{Log}[x]^2 \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] - 12 \operatorname{Log}[x]^2 \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] +$$

$$\left. 24 \operatorname{Log}[x] \operatorname{PolyLog}[4, -i \sqrt{d} \sqrt{f} x] + 24 \operatorname{Log}[x] \operatorname{PolyLog}[4, i \sqrt{d} \sqrt{f} x] - 24 \operatorname{PolyLog}[5, -i \sqrt{d} \sqrt{f} x] - 24 \operatorname{PolyLog}[5, i \sqrt{d} \sqrt{f} x] \right)$$

Problem 43: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^2\right)\right]}{x^3} dx$$

Optimal (type 4, 425 leaves, 15 steps):

$$\frac{3}{4} b^3 d f n^3 \operatorname{Log}[x] - \frac{3}{4} b^2 d f n^2 \operatorname{Log}\left[1 + \frac{1}{d f x^2}\right] (a + b \operatorname{Log}[c x^n]) - \frac{3}{4} b d f n \operatorname{Log}\left[1 + \frac{1}{d f x^2}\right] (a + b \operatorname{Log}[c x^n])^2 -$$

$$\frac{1}{2} d f \operatorname{Log}\left[1 + \frac{1}{d f x^2}\right] (a + b \operatorname{Log}[c x^n])^3 - \frac{3}{8} b^3 d f n^3 \operatorname{Log}[1 + d f x^2] - \frac{3 b^3 n^3 \operatorname{Log}[1 + d f x^2]}{8 x^2} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 + d f x^2]}{4 x^2} -$$

$$\frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[1 + d f x^2]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[1 + d f x^2]}{2 x^2} + \frac{3}{8} b^3 d f n^3 \operatorname{PolyLog}\left[2, -\frac{1}{d f x^2}\right] +$$

$$\frac{3}{4} b^2 d f n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{1}{d f x^2}\right] + \frac{3}{4} b d f n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{1}{d f x^2}\right] +$$

$$\frac{3}{8} b^3 d f n^3 \operatorname{PolyLog}\left[3, -\frac{1}{d f x^2}\right] + \frac{3}{4} b^2 d f n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{1}{d f x^2}\right] + \frac{3}{8} b^3 d f n^3 \operatorname{PolyLog}\left[4, -\frac{1}{d f x^2}\right]$$

Result (type 4, 940 leaves):

$$\begin{aligned}
& \frac{1}{8} \left(2 d f \operatorname{Log}[x] \left(4 a^3 + 6 a^2 b n + 6 a b^2 n^2 + 3 b^3 n^3 + 12 a^2 b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 12 a b^2 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + \right. \right. \\
& \quad \left. \left. 6 b^3 n^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 12 a b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 6 b^3 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 4 b^3 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^3 \right) - \frac{1}{x^2} \right. \\
& \quad \left(4 a^3 + 6 a^2 b n + 6 a b^2 n^2 + 3 b^3 n^3 + 6 b \left(2 a^2 + 2 a b n + b^2 n^2 \right) \operatorname{Log}[c x^n] + 6 b^2 \left(2 a + b n \right) \operatorname{Log}[c x^n]^2 + 4 b^3 \operatorname{Log}[c x^n]^3 \right) \operatorname{Log}[1 + d f x^2] - \\
& \quad d f \left(4 a^3 + 6 a^2 b n + 6 a b^2 n^2 + 3 b^3 n^3 + 12 a^2 b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 12 a b^2 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 6 b^3 n^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + \right. \\
& \quad \left. 12 a b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 6 b^3 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 + 4 b^3 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^3 \right) \operatorname{Log}[1 + d f x^2] + \\
& \quad 6 b d f n \left(2 a^2 + 2 a b n + b^2 n^2 + 4 a b \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 2 b^2 n \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right) + 2 b^2 \left(-n \operatorname{Log}[x] + \operatorname{Log}[c x^n] \right)^2 \right) \\
& \quad \left(\operatorname{Log}[x] \left(\operatorname{Log}[x] - \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] \right) - \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] \right) + \\
& \quad \left. 12 b^2 d f n^2 \left(2 a + b n - 2 b n \operatorname{Log}[x] + 2 b \operatorname{Log}[c x^n] \right) \left(\frac{\operatorname{Log}[x]^3}{3} - \frac{1}{2} \operatorname{Log}[x]^2 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - \frac{1}{2} \operatorname{Log}[x]^2 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] - \right. \right. \\
& \quad \left. \left. \operatorname{Log}[x] \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \operatorname{Log}[x] \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] + \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] \right) \right) + \\
& \quad 2 b^3 d f n^3 \left(\operatorname{Log}[x]^4 - 2 \operatorname{Log}[x]^3 \operatorname{Log}[1 - i \sqrt{d} \sqrt{f} x] - 2 \operatorname{Log}[x]^3 \operatorname{Log}[1 + i \sqrt{d} \sqrt{f} x] - 6 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, -i \sqrt{d} \sqrt{f} x] - \right. \\
& \quad \left. 6 \operatorname{Log}[x]^2 \operatorname{PolyLog}[2, i \sqrt{d} \sqrt{f} x] + 12 \operatorname{Log}[x] \operatorname{PolyLog}[3, -i \sqrt{d} \sqrt{f} x] + \right. \\
& \quad \left. \left. 12 \operatorname{Log}[x] \operatorname{PolyLog}[3, i \sqrt{d} \sqrt{f} x] - 12 \operatorname{PolyLog}[4, -i \sqrt{d} \sqrt{f} x] - 12 \operatorname{PolyLog}[4, i \sqrt{d} \sqrt{f} x] \right) \right) \left. \right)
\end{aligned}$$

Problem 63: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[d \left(\frac{1}{d} + f \sqrt{x}\right)\right] \left(a + b \operatorname{Log}[c x^n]\right)^3}{x^3} dx$$

Optimal (type 4, 849 leaves, 34 steps):

$$\begin{aligned}
& -\frac{175 b^3 d f n^3}{216 x^{3/2}} + \frac{45 b^3 d^2 f^2 n^3}{16 x} - \frac{255 b^3 d^3 f^3 n^3}{8 \sqrt{x}} + \frac{3}{8} b^3 d^4 f^4 n^3 \operatorname{Log}[1 + d f \sqrt{x}] - \frac{3 b^3 n^3 \operatorname{Log}[1 + d f \sqrt{x}]}{8 x^2} - \frac{3}{16} b^3 d^4 f^4 n^3 \operatorname{Log}[x] + \\
& \frac{3}{16} b^3 d^4 f^4 n^3 \operatorname{Log}[x]^2 - \frac{37 b^2 d f n^2 (a + b \operatorname{Log}[c x^n])}{36 x^{3/2}} + \frac{21 b^2 d^2 f^2 n^2 (a + b \operatorname{Log}[c x^n])}{8 x} - \frac{63 b^2 d^3 f^3 n^2 (a + b \operatorname{Log}[c x^n])}{4 \sqrt{x}} + \\
& \frac{3}{4} b^2 d^4 f^4 n^2 \operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n]) - \frac{3 b^2 n^2 \operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n])}{4 x^2} - \frac{3}{8} b^2 d^4 f^4 n^2 \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) - \\
& \frac{7 b d f n (a + b \operatorname{Log}[c x^n])^2}{12 x^{3/2}} + \frac{9 b d^2 f^2 n (a + b \operatorname{Log}[c x^n])^2}{8 x} - \frac{15 b d^3 f^3 n (a + b \operatorname{Log}[c x^n])^2}{4 \sqrt{x}} + \frac{3}{4} b d^4 f^4 n \operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n])^2 - \\
& \frac{3 b n \operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n])^2}{4 x^2} - \frac{1}{8} d^4 f^4 (a + b \operatorname{Log}[c x^n])^3 - \frac{d f (a + b \operatorname{Log}[c x^n])^3}{6 x^{3/2}} + \frac{d^2 f^2 (a + b \operatorname{Log}[c x^n])^3}{4 x} - \\
& \frac{d^3 f^3 (a + b \operatorname{Log}[c x^n])^3}{2 \sqrt{x}} + \frac{1}{2} d^4 f^4 \operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n])^3 - \frac{\operatorname{Log}[1 + d f \sqrt{x}] (a + b \operatorname{Log}[c x^n])^3}{2 x^2} - \frac{d^4 f^4 (a + b \operatorname{Log}[c x^n])^4}{16 b n} + \\
& \frac{3}{2} b^3 d^4 f^4 n^3 \operatorname{PolyLog}[2, -d f \sqrt{x}] + 3 b^2 d^4 f^4 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f \sqrt{x}] + 3 b d^4 f^4 n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[2, -d f \sqrt{x}] - \\
& 6 b^3 d^4 f^4 n^3 \operatorname{PolyLog}[3, -d f \sqrt{x}] - 12 b^2 d^4 f^4 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, -d f \sqrt{x}] + 24 b^3 d^4 f^4 n^3 \operatorname{PolyLog}[4, -d f \sqrt{x}]
\end{aligned}$$

Result (type 4, 2009 leaves):

$$\begin{aligned}
& -\frac{a^3 d f}{6 x^{3/2}} - \frac{7 a^2 b d f n}{12 x^{3/2}} - \frac{37 a b^2 d f n^2}{36 x^{3/2}} - \frac{175 b^3 d f n^3}{216 x^{3/2}} + \frac{a^3 d^2 f^2}{4 x} + \frac{9 a^2 b d^2 f^2 n}{8 x} + \frac{21 a b^2 d^2 f^2 n^2}{8 x} + \frac{45 b^3 d^2 f^2 n^3}{16 x} - \frac{a^3 d^3 f^3}{2 \sqrt{x}} - \frac{15 a^2 b d^3 f^3 n}{4 \sqrt{x}} - \\
& \frac{63 a b^2 d^3 f^3 n^2}{4 \sqrt{x}} - \frac{255 b^3 d^3 f^3 n^3}{8 \sqrt{x}} + \frac{1}{2} a^3 d^4 f^4 \operatorname{Log}[1 + d f \sqrt{x}] + \frac{3}{4} a^2 b d^4 f^4 n \operatorname{Log}[1 + d f \sqrt{x}] + \frac{3}{4} a b^2 d^4 f^4 n^2 \operatorname{Log}[1 + d f \sqrt{x}] + \\
& \frac{3}{8} b^3 d^4 f^4 n^3 \operatorname{Log}[1 + d f \sqrt{x}] - \frac{a^3 \operatorname{Log}[1 + d f \sqrt{x}]}{2 x^2} - \frac{3 a^2 b n \operatorname{Log}[1 + d f \sqrt{x}]}{4 x^2} - \frac{3 a b^2 n^2 \operatorname{Log}[1 + d f \sqrt{x}]}{4 x^2} - \frac{3 b^3 n^3 \operatorname{Log}[1 + d f \sqrt{x}]}{8 x^2} - \\
& \frac{1}{4} a^3 d^4 f^4 \operatorname{Log}[x] - \frac{3}{8} a^2 b d^4 f^4 n \operatorname{Log}[x] - \frac{3}{8} a b^2 d^4 f^4 n^2 \operatorname{Log}[x] - \frac{3}{16} b^3 d^4 f^4 n^3 \operatorname{Log}[x] + \frac{3}{8} a^2 b d^4 f^4 n \operatorname{Log}[x]^2 + \\
& \frac{3}{8} a b^2 d^4 f^4 n^2 \operatorname{Log}[x]^2 + \frac{3}{16} b^3 d^4 f^4 n^3 \operatorname{Log}[x]^2 - \frac{1}{4} a b^2 d^4 f^4 n^2 \operatorname{Log}[x]^3 - \frac{1}{8} b^3 d^4 f^4 n^3 \operatorname{Log}[x]^3 + \frac{1}{2} b^3 d^4 f^4 n^3 \operatorname{Log}\left[1 + \frac{1}{d f \sqrt{x}}\right] \operatorname{Log}[x]^3 - \\
& \frac{1}{2} b^3 d^4 f^4 n^3 \operatorname{Log}[1 + d f \sqrt{x}] \operatorname{Log}[x]^3 + \frac{1}{8} b^3 d^4 f^4 n^3 \operatorname{Log}[x]^4 - \frac{a^2 b d f \operatorname{Log}[c x^n]}{2 x^{3/2}} - \frac{7 a b^2 d f n \operatorname{Log}[c x^n]}{6 x^{3/2}} - \frac{37 b^3 d f n^2 \operatorname{Log}[c x^n]}{36 x^{3/2}} + \\
& \frac{3 a^2 b d^2 f^2 \operatorname{Log}[c x^n]}{4 x} + \frac{9 a b^2 d^2 f^2 n \operatorname{Log}[c x^n]}{4 x} + \frac{21 b^3 d^2 f^2 n^2 \operatorname{Log}[c x^n]}{8 x} - \frac{3 a^2 b d^3 f^3 \operatorname{Log}[c x^n]}{2 \sqrt{x}} - \frac{15 a b^2 d^3 f^3 n \operatorname{Log}[c x^n]}{2 \sqrt{x}} - \\
& \frac{63 b^3 d^3 f^3 n^2 \operatorname{Log}[c x^n]}{4 \sqrt{x}} + \frac{3}{2} a^2 b d^4 f^4 \operatorname{Log}[1 + d f \sqrt{x}] \operatorname{Log}[c x^n] + \frac{3}{2} a b^2 d^4 f^4 n \operatorname{Log}[1 + d f \sqrt{x}] \operatorname{Log}[c x^n] + \frac{3}{4} b^3 d^4 f^4 n^2 \operatorname{Log}[1 + d f \sqrt{x}] \operatorname{Log}[c x^n] -
\end{aligned}$$

$$\begin{aligned}
& \frac{3 a^2 b \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]}{2 x^2} - \frac{3 a b^2 n \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]}{2 x^2} - \frac{3 b^3 n^2 \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]}{4 x^2} - \frac{3}{4} a^2 b d^4 f^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\
& \frac{3}{4} a b^2 d^4 f^4 n \operatorname{Log}[x] \operatorname{Log}[c x^n] - \frac{3}{8} b^3 d^4 f^4 n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + \frac{3}{4} a b^2 d^4 f^4 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + \frac{3}{8} b^3 d^4 f^4 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - \\
& \frac{1}{4} b^3 d^4 f^4 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] - \frac{a b^2 d f \operatorname{Log}[c x^n]^2}{2 x^{3/2}} - \frac{7 b^3 d f n \operatorname{Log}[c x^n]^2}{12 x^{3/2}} + \frac{3 a b^2 d^2 f^2 \operatorname{Log}[c x^n]^2}{4 x} + \frac{9 b^3 d^2 f^2 n \operatorname{Log}[c x^n]^2}{8 x} - \\
& \frac{3 a b^2 d^3 f^3 \operatorname{Log}[c x^n]^2}{2 \sqrt{x}} - \frac{15 b^3 d^3 f^3 n \operatorname{Log}[c x^n]^2}{4 \sqrt{x}} + \frac{3}{2} a b^2 d^4 f^4 \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^2 + \frac{3}{4} b^3 d^4 f^4 n \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^2 - \\
& \frac{3 a b^2 \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^2}{2 x^2} - \frac{3 b^3 n \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^2}{4 x^2} - \frac{3}{4} a b^2 d^4 f^4 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - \frac{3}{8} b^3 d^4 f^4 n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + \\
& \frac{3}{8} b^3 d^4 f^4 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 - \frac{b^3 d f \operatorname{Log}[c x^n]^3}{6 x^{3/2}} + \frac{b^3 d^2 f^2 \operatorname{Log}[c x^n]^3}{4 x} - \frac{b^3 d^3 f^3 \operatorname{Log}[c x^n]^3}{2 \sqrt{x}} + \frac{1}{2} b^3 d^4 f^4 \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^3 - \\
& \frac{b^3 \operatorname{Log}[1+d f \sqrt{x}] \operatorname{Log}[c x^n]^3}{2 x^2} - \frac{1}{4} b^3 d^4 f^4 \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 - 3 b^3 d^4 f^4 n^3 \operatorname{Log}[x]^2 \operatorname{PolyLog}\left[2, -\frac{1}{d f \sqrt{x}}\right] + \\
& \frac{3}{2} b d^4 f^4 n \left(2 a^2 + 2 a b n + b^2 n^2 - 2 b^2 n^2 \operatorname{Log}[x]^2 + 2 b (2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2\right) \operatorname{PolyLog}\left[2, -d f \sqrt{x}\right] - \\
& 12 b^3 d^4 f^4 n^3 \operatorname{Log}[x] \operatorname{PolyLog}\left[3, -\frac{1}{d f \sqrt{x}}\right] - 12 a b^2 d^4 f^4 n^2 \operatorname{PolyLog}\left[3, -d f \sqrt{x}\right] - 6 b^3 d^4 f^4 n^3 \operatorname{PolyLog}\left[3, -d f \sqrt{x}\right] + \\
& 12 b^3 d^4 f^4 n^3 \operatorname{Log}[x] \operatorname{PolyLog}\left[3, -d f \sqrt{x}\right] - 12 b^3 d^4 f^4 n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -d f \sqrt{x}\right] - 24 b^3 d^4 f^4 n^3 \operatorname{PolyLog}\left[4, -\frac{1}{d f \sqrt{x}}\right]
\end{aligned}$$

Problem 64: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \operatorname{Log}[c x^n])^4 \operatorname{Log}\left[d\left(\frac{1}{d}+f x^m\right)\right]}{x} dx$$

Optimal (type 4, 137 leaves, 5 steps):

$$\begin{aligned}
& -\frac{(a+b \operatorname{Log}[c x^n])^4 \operatorname{PolyLog}\left[2, -d f x^m\right]}{m} + \frac{4 b n (a+b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[3, -d f x^m\right]}{m^2} - \\
& \frac{12 b^2 n^2 (a+b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[4, -d f x^m\right]}{m^3} + \frac{24 b^3 n^3 (a+b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[5, -d f x^m\right]}{m^4} - \frac{24 b^4 n^4 \operatorname{PolyLog}\left[6, -d f x^m\right]}{m^5}
\end{aligned}$$

Result (type 4, 1700 leaves):

$$\begin{aligned}
& -\frac{2}{3} a^3 b m n \operatorname{Log}[x]^3 + \frac{3}{2} a^2 b^2 m n^2 \operatorname{Log}[x]^4 - \frac{6}{5} a b^3 m n^3 \operatorname{Log}[x]^5 + \frac{1}{3} b^4 m n^4 \operatorname{Log}[x]^6 - 2 a^2 b^2 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] + 3 a b^3 m n^2 \operatorname{Log}[x]^4 \operatorname{Log}[c x^n] - \\
& \frac{6}{5} b^4 m n^3 \operatorname{Log}[x]^5 \operatorname{Log}[c x^n] - 2 a b^3 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^2 + \frac{3}{2} b^4 m n^2 \operatorname{Log}[x]^4 \operatorname{Log}[c x^n]^2 - \frac{2}{3} b^4 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^3 - \\
& 2 a^3 b n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + 4 a^2 b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - 3 a b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + \frac{4}{5} b^4 n^4 \operatorname{Log}[x]^5 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - \\
& 6 a^2 b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + 8 a b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - 3 b^4 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - \\
& 6 a b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + 4 b^4 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - 2 b^4 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^3 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + \\
& 2 a^3 b n \operatorname{Log}[x]^2 \operatorname{Log}[1 + d f x^m] - 4 a^2 b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[1 + d f x^m] + 3 a b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[1 + d f x^m] - \frac{4}{5} b^4 n^4 \operatorname{Log}[x]^5 \operatorname{Log}[1 + d f x^m] + \\
& \frac{a^4 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} - \frac{4 a^3 b n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \frac{6 a^2 b^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} - \\
& \frac{4 a b^3 n^3 \operatorname{Log}[x]^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \frac{b^4 n^4 \operatorname{Log}[x]^4 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + 6 a^2 b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] - \\
& 8 a b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] + 3 b^4 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] + \frac{4 a^3 b \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} - \\
& \frac{12 a^2 b^2 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} + \frac{12 a b^3 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} - \\
& \frac{4 b^4 n^3 \operatorname{Log}[x]^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} + 6 a b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m] - 4 b^4 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m] + \\
& \frac{6 a^2 b^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} - \frac{12 a b^3 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} + \\
& \frac{6 b^4 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} + 2 b^4 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + d f x^m] + \frac{4 a b^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + d f x^m]}{m} - \\
& \frac{4 b^4 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + d f x^m]}{m} + \frac{b^4 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^4 \operatorname{Log}[1 + d f x^m]}{m} + \frac{1}{m} \\
& b n \operatorname{Log}[x] \left(-b^3 n^3 \operatorname{Log}[x]^3 + 4 b^2 n^2 \operatorname{Log}[x]^2 (a + b \operatorname{Log}[c x^n]) - 6 b n \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n])^2 + 4 (a + b \operatorname{Log}[c x^n])^3 \right) \operatorname{PolyLog}\left[2, -\frac{x^{-m}}{d f}\right] + \\
& \frac{(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^4 \operatorname{PolyLog}\left[2, 1 + d f x^m\right]}{m} + \frac{4 a^3 b n \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \frac{12 a^2 b^2 n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \\
& \frac{12 a b^3 n \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \frac{4 b^4 n \operatorname{Log}[c x^n]^3 \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \frac{12 a^2 b^2 n^2 \operatorname{PolyLog}\left[4, -\frac{x^{-m}}{d f}\right]}{m^3} + \frac{24 a b^3 n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[4, -\frac{x^{-m}}{d f}\right]}{m^3} + \\
& \frac{12 b^4 n^2 \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}\left[4, -\frac{x^{-m}}{d f}\right]}{m^3} + \frac{24 a b^3 n^3 \operatorname{PolyLog}\left[5, -\frac{x^{-m}}{d f}\right]}{m^4} + \frac{24 b^4 n^3 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[5, -\frac{x^{-m}}{d f}\right]}{m^4} + \frac{24 b^4 n^4 \operatorname{PolyLog}\left[6, -\frac{x^{-m}}{d f}\right]}{m^5}
\end{aligned}$$

Problem 65: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^m\right)\right]}{x} dx$$

Optimal (type 4, 105 leaves, 4 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}[2, -d f x^m]}{m} + \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[3, -d f x^m]}{m^2} - \frac{6 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[4, -d f x^m]}{m^3} + \frac{6 b^3 n^3 \operatorname{PolyLog}[5, -d f x^m]}{m^4}$$

Result (type 4, 1035 leaves):

$$\begin{aligned} & -\frac{1}{2} a^2 b m n \operatorname{Log}[x]^3 + \frac{3}{4} a b^2 m n^2 \operatorname{Log}[x]^4 - \frac{3}{10} b^3 m n^3 \operatorname{Log}[x]^5 - a b^2 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] + \frac{3}{4} b^3 m n^2 \operatorname{Log}[x]^4 \operatorname{Log}[c x^n] - \\ & \frac{1}{2} b^3 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^2 - \frac{3}{2} a^2 b n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + 2 a b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - \frac{3}{4} b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - \\ & 3 a b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + 2 b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - \frac{3}{2} b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + \\ & \frac{3}{2} a^2 b n \operatorname{Log}[x]^2 \operatorname{Log}[1 + d f x^m] - 2 a b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[1 + d f x^m] + \frac{3}{4} b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[1 + d f x^m] + \frac{a^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} - \\ & \frac{3 a^2 b n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \frac{3 a b^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} - \frac{b^3 n^3 \operatorname{Log}[x]^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \\ & 3 a b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] - 2 b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] + \frac{3 a^2 b \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} - \\ & \frac{6 a b^2 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} + \frac{3 b^3 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} + \\ & \frac{3}{2} b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m] + \frac{3 a b^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} - \frac{3 b^3 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} + \\ & \frac{b^3 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^3 \operatorname{Log}[1 + d f x^m]}{m} + \frac{b n \operatorname{Log}[x] \left(b^2 n^2 \operatorname{Log}[x]^2 - 3 b n \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) + 3 (a + b \operatorname{Log}[c x^n])^2 \right) \operatorname{PolyLog}\left[2, -\frac{x^{-m}}{d f}\right]}{m} + \\ & \frac{(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}[2, 1 + d f x^m]}{m} + \frac{3 a^2 b n \operatorname{PolyLog}[3, -\frac{x^{-m}}{d f}]}{m^2} + \frac{6 a b^2 n \operatorname{Log}[c x^n] \operatorname{PolyLog}[3, -\frac{x^{-m}}{d f}]}{m^2} + \\ & \frac{3 b^3 n \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}[3, -\frac{x^{-m}}{d f}]}{m^2} + \frac{6 a b^2 n^2 \operatorname{PolyLog}[4, -\frac{x^{-m}}{d f}]}{m^3} + \frac{6 b^3 n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}[4, -\frac{x^{-m}}{d f}]}{m^3} + \frac{6 b^3 n^3 \operatorname{PolyLog}[5, -\frac{x^{-m}}{d f}]}{m^4} \end{aligned}$$

Problem 66: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[d \left(\frac{1}{d} + f x^m\right)\right]}{x} dx$$

Optimal (type 4, 73 leaves, 3 steps):

$$-\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[2, -d f x^m]}{m} + \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, -d f x^m]}{m^2} - \frac{2 b^2 n^2 \operatorname{PolyLog}[4, -d f x^m]}{m^3}$$

Result (type 4, 526 leaves):

$$\begin{aligned} & -\frac{1}{3} a b m n \operatorname{Log}[x]^3 + \frac{1}{4} b^2 m n^2 \operatorname{Log}[x]^4 - \frac{1}{3} b^2 m n \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] - a b n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + \\ & \frac{2}{3} b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] - b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{x^{-m}}{d f}\right] + a b n \operatorname{Log}[x]^2 \operatorname{Log}[1 + d f x^m] - \frac{2}{3} b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[1 + d f x^m] + \\ & \frac{a^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} - \frac{2 a b n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \frac{b^2 n^2 \operatorname{Log}[x]^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[1 + d f x^m]}{m} + \\ & b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m] + \frac{2 a b \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} - \frac{2 b^2 n \operatorname{Log}[x] \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n] \operatorname{Log}[1 + d f x^m]}{m} + \\ & \frac{b^2 \operatorname{Log}[-d f x^m] \operatorname{Log}[c x^n]^2 \operatorname{Log}[1 + d f x^m]}{m} + \frac{b n \operatorname{Log}[x] (-b n \operatorname{Log}[x] + 2 (a + b \operatorname{Log}[c x^n])) \operatorname{PolyLog}\left[2, -\frac{x^{-m}}{d f}\right]}{m} + \\ & \frac{(a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}[2, 1 + d f x^m]}{m} + \frac{2 a b n \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \frac{2 b^2 n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{d f}\right]}{m^2} + \frac{2 b^2 n^2 \operatorname{PolyLog}\left[4, -\frac{x^{-m}}{d f}\right]}{m^3} \end{aligned}$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[d \left(\frac{1}{d} + f x^m\right)\right]}{x} dx$$

Optimal (type 4, 40 leaves, 2 steps):

$$-\frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, -d f x^m]}{m} + \frac{b n \operatorname{PolyLog}[3, -d f x^m]}{m^2}$$

Result (type 4, 207 leaves):

$$\frac{1}{6m^2} \left(-bm^3n \operatorname{Log}[x]^3 - 3bm^2n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{x^{-m}}{df}\right] + 3bm^2n \operatorname{Log}[x]^2 \operatorname{Log}[1 + dfx^m] + \right. \\ \left. 6am \operatorname{Log}[-dfx^m] \operatorname{Log}[1 + dfx^m] - 6bmn \operatorname{Log}[x] \operatorname{Log}[-dfx^m] \operatorname{Log}[1 + dfx^m] + 6bm \operatorname{Log}[-dfx^m] \operatorname{Log}[cx^n] \operatorname{Log}[1 + dfx^m] + \right. \\ \left. 6bmn \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{x^{-m}}{df}\right] + 6m(a - bn \operatorname{Log}[x] + b \operatorname{Log}[cx^n]) \operatorname{PolyLog}\left[2, 1 + dfx^m\right] + 6bn \operatorname{PolyLog}\left[3, -\frac{x^{-m}}{df}\right] \right)$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[cx^n])^2 \operatorname{Log}[d(e + fx)^m]}{x} dx$$

Optimal (type 4, 131 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[cx^n])^3 \operatorname{Log}[d(e + fx)^m]}{3bn} - \frac{m(a + b \operatorname{Log}[cx^n])^3 \operatorname{Log}\left[1 + \frac{fx}{e}\right]}{3bn} - \\ m(a + b \operatorname{Log}[cx^n])^2 \operatorname{PolyLog}\left[2, -\frac{fx}{e}\right] + 2bmn(a + b \operatorname{Log}[cx^n]) \operatorname{PolyLog}\left[3, -\frac{fx}{e}\right] - 2b^2m^2 \operatorname{PolyLog}\left[4, -\frac{fx}{e}\right]$$

Result (type 4, 329 leaves):

$$a^2 \operatorname{Log}[x] \operatorname{Log}[d(e + fx)^m] - abn \operatorname{Log}[x]^2 \operatorname{Log}[d(e + fx)^m] + \frac{1}{3}b^2n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d(e + fx)^m] + 2ab \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}[d(e + fx)^m] - \\ b^2n \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] \operatorname{Log}[d(e + fx)^m] + b^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 \operatorname{Log}[d(e + fx)^m] - a^2m \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{fx}{e}\right] + abmn \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - \\ \frac{1}{3}b^2m^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 2abm \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}\left[1 + \frac{fx}{e}\right] + b^2mn \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] \operatorname{Log}\left[1 + \frac{fx}{e}\right] - b^2m \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - \\ m(a + b \operatorname{Log}[cx^n])^2 \operatorname{PolyLog}\left[2, -\frac{fx}{e}\right] + 2bmn(a + b \operatorname{Log}[cx^n]) \operatorname{PolyLog}\left[3, -\frac{fx}{e}\right] - 2b^2m^2 \operatorname{PolyLog}\left[4, -\frac{fx}{e}\right]$$

Problem 82: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[cx^n])^2 \operatorname{Log}[d(e + fx)^m]}{x^2} dx$$

Optimal (type 4, 248 leaves, 10 steps):

$$\frac{2 b^2 f m n^2 \operatorname{Log}[x]}{e} - \frac{2 b f m n \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])}{e} - \frac{f m \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^2}{e} - \frac{2 b^2 f m n^2 \operatorname{Log}[e + f x]}{e} -$$

$$\frac{2 b^2 n^2 \operatorname{Log}[d (e + f x)^m]}{x} - \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m]}{x} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{x} +$$

$$\frac{2 b^2 f m n^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e} + \frac{2 b f m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e} + \frac{2 b^2 f m n^2 \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{e}$$

Result (type 4, 600 leaves):

$$-\frac{1}{3 e x} \left(-3 a^2 f m x \operatorname{Log}[x] - 6 a b f m n x \operatorname{Log}[x] - 6 b^2 f m n^2 x \operatorname{Log}[x] + 3 a b f m n x \operatorname{Log}[x]^2 + 3 b^2 f m n^2 x \operatorname{Log}[x]^2 - b^2 f m n^2 x \operatorname{Log}[x]^3 - \right.$$

$$6 a b f m x \operatorname{Log}[x] \operatorname{Log}[c x^n] - 6 b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] + 3 b^2 f m n x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - 3 b^2 f m x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 +$$

$$3 a^2 f m x \operatorname{Log}[e + f x] + 6 a b f m n x \operatorname{Log}[e + f x] + 6 b^2 f m n^2 x \operatorname{Log}[e + f x] - 6 a b f m n x \operatorname{Log}[x] \operatorname{Log}[e + f x] -$$

$$6 b^2 f m n^2 x \operatorname{Log}[x] \operatorname{Log}[e + f x] + 3 b^2 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] + 6 a b f m x \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 6 b^2 f m n x \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] -$$

$$6 b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 3 b^2 f m x \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 3 a^2 e \operatorname{Log}[d (e + f x)^m] + 6 a b e n \operatorname{Log}[d (e + f x)^m] +$$

$$6 b^2 e n^2 \operatorname{Log}[d (e + f x)^m] + 6 a b e \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 6 b^2 e n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 3 b^2 e \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] +$$

$$6 a b f m n x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 6 b^2 f m n^2 x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 3 b^2 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] +$$

$$\left. 6 b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 6 b f m n x (a + b n + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] - 6 b^2 f m n^2 x \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] \right)$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{x^3} dx$$

Optimal (type 4, 344 leaves, 14 steps):

$$-\frac{7 b^2 f m n^2}{4 e x} - \frac{b^2 f^2 m n^2 \operatorname{Log}[x]}{4 e^2} - \frac{3 b f m n (a + b \operatorname{Log}[c x^n])}{2 e x} + \frac{b f^2 m n \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])}{2 e^2} - \frac{f m (a + b \operatorname{Log}[c x^n])^2}{2 e x} +$$

$$\frac{f^2 m \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^2}{2 e^2} + \frac{b^2 f^2 m n^2 \operatorname{Log}[e + f x]}{4 e^2} - \frac{b^2 n^2 \operatorname{Log}[d (e + f x)^m]}{4 x^2} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m]}{2 x^2} -$$

$$\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{2 x^2} - \frac{b^2 f^2 m n^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{2 e^2} - \frac{b f^2 m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e^2} - \frac{b^2 f^2 m n^2 \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{e^2}$$

Result (type 4, 796 leaves):

$$\begin{aligned}
& - \frac{1}{12 e^2 x^2} \left(6 a^2 e f m x + 18 a b e f m n x + 21 b^2 e f m n^2 x + 6 a^2 f^2 m x^2 \operatorname{Log}[x] + 6 a b f^2 m n x^2 \operatorname{Log}[x] + 3 b^2 f^2 m n^2 x^2 \operatorname{Log}[x] - 6 a b f^2 m n x^2 \operatorname{Log}[x]^2 - \right. \\
& 3 b^2 f^2 m n^2 x^2 \operatorname{Log}[x]^2 + 2 b^2 f^2 m n^2 x^2 \operatorname{Log}[x]^3 + 12 a b e f m x \operatorname{Log}[c x^n] + 18 b^2 e f m n x \operatorname{Log}[c x^n] + 12 a b f^2 m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 6 b^2 f^2 m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 6 b^2 f^2 m n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 6 b^2 e f m x \operatorname{Log}[c x^n]^2 + 6 b^2 f^2 m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - \\
& 6 a^2 f^2 m x^2 \operatorname{Log}[e + f x] - 6 a b f^2 m n x^2 \operatorname{Log}[e + f x] - 3 b^2 f^2 m n^2 x^2 \operatorname{Log}[e + f x] + 12 a b f^2 m n x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x] + \\
& 6 b^2 f^2 m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x] - 6 b^2 f^2 m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] - 12 a b f^2 m x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 6 b^2 f^2 m n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + \\
& 12 b^2 f^2 m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 6 b^2 f^2 m x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 6 a^2 e^2 \operatorname{Log}[d (e + f x)^m] + 6 a b e^2 n \operatorname{Log}[d (e + f x)^m] + \\
& 3 b^2 e^2 n^2 \operatorname{Log}[d (e + f x)^m] + 12 a b e^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 6 b^2 e^2 n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 6 b^2 e^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] - \\
& 12 a b f^2 m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b^2 f^2 m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 6 b^2 f^2 m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - \\
& \left. 12 b^2 f^2 m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b f^2 m n x^2 (2 a + b n + 2 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] + 12 b^2 f^2 m n^2 x^2 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] \right)
\end{aligned}$$

Problem 84: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{x^4} dx$$

Optimal (type 4, 420 leaves, 19 steps):

$$\begin{aligned}
& - \frac{19 b^2 f m n^2}{108 e x^2} + \frac{26 b^2 f^2 m n^2}{27 e^2 x} + \frac{2 b^2 f^3 m n^2 \operatorname{Log}[x]}{27 e^3} - \frac{5 b f m n (a + b \operatorname{Log}[c x^n])}{18 e x^2} + \frac{8 b f^2 m n (a + b \operatorname{Log}[c x^n])}{9 e^2 x} - \\
& \frac{2 b f^3 m n \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])}{9 e^3} - \frac{f m (a + b \operatorname{Log}[c x^n])^2}{6 e x^2} + \frac{f^2 m (a + b \operatorname{Log}[c x^n])^2}{3 e^2 x} - \frac{f^3 m \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^2}{3 e^3} - \\
& \frac{2 b^2 f^3 m n^2 \operatorname{Log}[e + f x]}{27 e^3} - \frac{2 b^2 n^2 \operatorname{Log}[d (e + f x)^m]}{27 x^3} - \frac{2 b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m]}{9 x^3} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{3 x^3} + \\
& \frac{2 b^2 f^3 m n^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{9 e^3} + \frac{2 b f^3 m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{3 e^3} + \frac{2 b^2 f^3 m n^2 \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{3 e^3}
\end{aligned}$$

Result (type 4, 909 leaves):

$$\begin{aligned}
& - \frac{1}{108 e^3 x^3} \left(18 a^2 e^2 f m x + 30 a b e^2 f m n x + 19 b^2 e^2 f m n^2 x - 36 a^2 e f^2 m x^2 - 96 a b e f^2 m n x^2 - 104 b^2 e f^2 m n^2 x^2 - 36 a^2 f^3 m x^3 \operatorname{Log}[x] - \right. \\
& 24 a b f^3 m n x^3 \operatorname{Log}[x] - 8 b^2 f^3 m n^2 x^3 \operatorname{Log}[x] + 36 a b f^3 m n x^3 \operatorname{Log}[x]^2 + 12 b^2 f^3 m n^2 x^3 \operatorname{Log}[x]^2 - 12 b^2 f^3 m n^2 x^3 \operatorname{Log}[x]^3 + 36 a b e^2 f m x \operatorname{Log}[c x^n] + \\
& 30 b^2 e^2 f m n x \operatorname{Log}[c x^n] - 72 a b e f^2 m x^2 \operatorname{Log}[c x^n] - 96 b^2 e f^2 m n x^2 \operatorname{Log}[c x^n] - 72 a b f^3 m x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 24 b^2 f^3 m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 36 b^2 f^3 m n x^3 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 18 b^2 e^2 f m x \operatorname{Log}[c x^n]^2 - 36 b^2 e f^2 m x^2 \operatorname{Log}[c x^n]^2 - 36 b^2 f^3 m x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 36 a^2 f^3 m x^3 \operatorname{Log}[e + f x] + \\
& 24 a b f^3 m n x^3 \operatorname{Log}[e + f x] + 8 b^2 f^3 m n^2 x^3 \operatorname{Log}[e + f x] - 72 a b f^3 m n x^3 \operatorname{Log}[x] \operatorname{Log}[e + f x] - 24 b^2 f^3 m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}[e + f x] + \\
& 36 b^2 f^3 m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] + 72 a b f^3 m x^3 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 24 b^2 f^3 m n x^3 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - \\
& 72 b^2 f^3 m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 36 b^2 f^3 m x^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 36 a^2 e^3 \operatorname{Log}[d (e + f x)^m] + 24 a b e^3 n \operatorname{Log}[d (e + f x)^m] + \\
& 8 b^2 e^3 n^2 \operatorname{Log}[d (e + f x)^m] + 72 a b e^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 24 b^2 e^3 n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 36 b^2 e^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] + \\
& 72 a b f^3 m n x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 24 b^2 f^3 m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 36 b^2 f^3 m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& \left. 72 b^2 f^3 m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 24 b f^3 m n x^3 (3 a + b n + 3 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] - 72 b^2 f^3 m n^2 x^3 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] \right)
\end{aligned}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m] dx$$

Optimal (type 4, 603 leaves, 34 steps):

$$\begin{aligned}
& \frac{21 a b^2 e m n^2 x}{4 f} - \frac{45 b^3 e m n^3 x}{8 f} + \frac{3}{4} b^3 m n^3 x^2 + \frac{21 b^3 e m n^2 x \operatorname{Log}[c x^n]}{4 f} - \frac{9}{8} b^2 m n^2 x^2 (a + b \operatorname{Log}[c x^n]) - \frac{9 b e m n x (a + b \operatorname{Log}[c x^n])^2}{4 f} + \\
& \frac{3}{4} b m n x^2 (a + b \operatorname{Log}[c x^n])^2 + \frac{e m x (a + b \operatorname{Log}[c x^n])^3}{2 f} - \frac{1}{4} m x^2 (a + b \operatorname{Log}[c x^n])^3 + \frac{3 b^3 e^2 m n^3 \operatorname{Log}[e + f x]}{8 f^2} - \frac{3}{8} b^3 n^3 x^2 \operatorname{Log}[d (e + f x)^m] + \\
& \frac{3}{4} b^2 n^2 x^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m] - \frac{3}{4} b n x^2 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m] + \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m] - \\
& \frac{3 b^2 e^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{4 f^2} + \frac{3 b e^2 m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{4 f^2} - \frac{e^2 m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{2 f^2} - \\
& \frac{3 b^3 e^2 m n^3 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{4 f^2} + \frac{3 b^2 e^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{2 f^2} - \frac{3 b e^2 m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{2 f^2} - \\
& \frac{3 b^3 e^2 m n^3 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right]}{2 f^2} + \frac{3 b^2 e^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right]}{f^2} - \frac{3 b^3 e^2 m n^3 \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right]}{f^2}
\end{aligned}$$

Result (type 4, 1431 leaves):

$\frac{1}{8 f^2}$

$$\begin{aligned}
& \left(4 a^3 e f m x - 18 a^2 b e f m n x + 42 a b^2 e f m n^2 x - 45 b^3 e f m n^3 x - 2 a^3 f^2 m x^2 + 6 a^2 b f^2 m n x^2 - 9 a b^2 f^2 m n^2 x^2 + 6 b^3 f^2 m n^3 x^2 + 12 a^2 b e f m x \operatorname{Log}[c x^n] - \right. \\
& 36 a b^2 e f m n x \operatorname{Log}[c x^n] + 42 b^3 e f m n^2 x \operatorname{Log}[c x^n] - 6 a^2 b f^2 m x^2 \operatorname{Log}[c x^n] + 12 a b^2 f^2 m n x^2 \operatorname{Log}[c x^n] - 9 b^3 f^2 m n^2 x^2 \operatorname{Log}[c x^n] + \\
& 12 a b^2 e f m x \operatorname{Log}[c x^n]^2 - 18 b^3 e f m n x \operatorname{Log}[c x^n]^2 - 6 a b^2 f^2 m x^2 \operatorname{Log}[c x^n]^2 + 6 b^3 f^2 m n x^2 \operatorname{Log}[c x^n]^2 + 4 b^3 e f m x \operatorname{Log}[c x^n]^3 - \\
& 2 b^3 f^2 m x^2 \operatorname{Log}[c x^n]^3 - 4 a^3 e^2 m \operatorname{Log}[e + f x] + 6 a^2 b e^2 m n \operatorname{Log}[e + f x] - 6 a b^2 e^2 m n^2 \operatorname{Log}[e + f x] + 3 b^3 e^2 m n^3 \operatorname{Log}[e + f x] + \\
& 12 a^2 b e^2 m n \operatorname{Log}[x] \operatorname{Log}[e + f x] - 12 a b^2 e^2 m n^2 \operatorname{Log}[x] \operatorname{Log}[e + f x] + 6 b^3 e^2 m n^3 \operatorname{Log}[x] \operatorname{Log}[e + f x] - \\
& 12 a b^2 e^2 m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] + 6 b^3 e^2 m n^3 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] + 4 b^3 e^2 m n^3 \operatorname{Log}[x]^3 \operatorname{Log}[e + f x] - 12 a^2 b e^2 m \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + \\
& 12 a b^2 e^2 m n \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 6 b^3 e^2 m n^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 24 a b^2 e^2 m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - \\
& 12 b^3 e^2 m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 12 b^3 e^2 m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 12 a b^2 e^2 m \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + \\
& 6 b^3 e^2 m n \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 12 b^3 e^2 m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] - 4 b^3 e^2 m \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x] + \\
& 4 a^3 f^2 x^2 \operatorname{Log}[d (e + f x)^m] - 6 a^2 b f^2 n x^2 \operatorname{Log}[d (e + f x)^m] + 6 a b^2 f^2 n^2 x^2 \operatorname{Log}[d (e + f x)^m] - 3 b^3 f^2 n^3 x^2 \operatorname{Log}[d (e + f x)^m] + \\
& 12 a^2 b f^2 x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] - 12 a b^2 f^2 n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 6 b^3 f^2 n^2 x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + \\
& 12 a b^2 f^2 x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] - 6 b^3 f^2 n x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] + 4 b^3 f^2 x^2 \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x)^m] - \\
& 12 a^2 b e^2 m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 12 a b^2 e^2 m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b^3 e^2 m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 12 a b^2 e^2 m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b^3 e^2 m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 4 b^3 e^2 m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - \\
& 24 a b^2 e^2 m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 12 b^3 e^2 m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 12 b^3 e^2 m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - \\
& 12 b^3 e^2 m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b e^2 m n \left(2 a^2 - 2 a b n + b^2 n^2 - 2 b (-2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] + \\
& 12 b^2 e^2 m n^2 \left(2 a - b n + 2 b \operatorname{Log}[c x^n] \right) \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] - 24 b^3 e^2 m n^3 \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] \Big)
\end{aligned}$$

Problem 86: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m] dx$$

Optimal (type 4, 473 leaves, 28 steps):

$$\begin{aligned}
& -12 a b^2 m n^2 x + 18 b^3 m n^3 x - 6 b^2 m n^2 (a - b n) x - 18 b^3 m n^2 x \operatorname{Log}[c x^n] + 6 b m n x (a + b \operatorname{Log}[c x^n])^2 - \\
& m x (a + b \operatorname{Log}[c x^n])^3 + \frac{6 b^2 e m n^2 (a - b n) \operatorname{Log}[e + f x]}{f} + 6 a b^2 n^2 x \operatorname{Log}[d (e + f x)^m] - 6 b^3 n^3 x \operatorname{Log}[d (e + f x)^m] + \\
& 6 b^3 n^2 x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] - 3 b n x (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m] + x (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m] + \\
& \frac{6 b^3 e m n^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{f} - \frac{3 b e m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{f} + \frac{e m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{f} + \\
& \frac{6 b^3 e m n^3 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{f} - \frac{6 b^2 e m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{f} + \frac{3 b e m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right]}{f} + \\
& \frac{6 b^3 e m n^3 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right]}{f} - \frac{6 b^2 e m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right]}{f} + \frac{6 b^3 e m n^3 \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right]}{f}
\end{aligned}$$

Result (type 4, 1122 leaves):

$$\begin{aligned}
& \frac{1}{f} \left(-a^3 f m x + 6 a^2 b f m n x - 18 a b^2 f m n^2 x + 24 b^3 f m n^3 x - 3 a^2 b f m x \operatorname{Log}[c x^n] + 12 a b^2 f m n x \operatorname{Log}[c x^n] - 18 b^3 f m n^2 x \operatorname{Log}[c x^n] - \right. \\
& 3 a b^2 f m x \operatorname{Log}[c x^n]^2 + 6 b^3 f m n x \operatorname{Log}[c x^n]^2 - b^3 f m x \operatorname{Log}[c x^n]^3 + a^3 e m \operatorname{Log}[e + f x] - 3 a^2 b e m n \operatorname{Log}[e + f x] + 6 a b^2 e m n^2 \operatorname{Log}[e + f x] - \\
& 6 b^3 e m n^3 \operatorname{Log}[e + f x] - 3 a^2 b e m n \operatorname{Log}[x] \operatorname{Log}[e + f x] + 6 a b^2 e m n^2 \operatorname{Log}[x] \operatorname{Log}[e + f x] - 6 b^3 e m n^3 \operatorname{Log}[x] \operatorname{Log}[e + f x] + \\
& 3 a b^2 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] - 3 b^3 e m n^3 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] - b^3 e m n^3 \operatorname{Log}[x]^3 \operatorname{Log}[e + f x] + 3 a^2 b e m \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - \\
& 6 a b^2 e m n \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 6 b^3 e m n^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 6 a b^2 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + \\
& 6 b^3 e m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 3 b^3 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 3 a b^2 e m \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] - \\
& 3 b^3 e m n \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] - 3 b^3 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + b^3 e m \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x] + a^3 f x \operatorname{Log}[d (e + f x)^m] - \\
& 3 a^2 b f n x \operatorname{Log}[d (e + f x)^m] + 6 a b^2 f n^2 x \operatorname{Log}[d (e + f x)^m] - 6 b^3 f n^3 x \operatorname{Log}[d (e + f x)^m] + 3 a^2 b f x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] - \\
& 6 a b^2 f n x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 6 b^3 f n^2 x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 3 a b^2 f x \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] - \\
& 3 b^3 f n x \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] + b^3 f x \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x)^m] + 3 a^2 b e m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 a b^2 e m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 6 b^3 e m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 3 a b^2 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 3 b^3 e m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + b^3 e m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 6 a b^2 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 6 b^3 e m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 3 b^3 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 3 b^3 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 3 b e m n (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] - \\
& \left. 6 b^2 e m n^2 (a - b n + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] + 6 b^3 e m n^3 \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] \right)
\end{aligned}$$

Problem 87: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m]}{x} dx$$

Optimal (type 4, 161 leaves, 6 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^4 \operatorname{Log}[d (e + f x)^m]}{4 b n} - \frac{m (a + b \operatorname{Log}[c x^n])^4 \operatorname{Log}\left[1 + \frac{f x}{e}\right]}{4 b n} - m (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] +$$

$$3 b m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] - 6 b^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] + 6 b^3 m n^3 \operatorname{PolyLog}\left[5, -\frac{f x}{e}\right]$$

Result (type 4, 602 leaves):

$$a^3 \operatorname{Log}[x] \operatorname{Log}[d (e + f x)^m] - \frac{3}{2} a^2 b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x)^m] + a b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d (e + f x)^m] -$$

$$\frac{1}{4} b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[d (e + f x)^m] + 3 a^2 b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] - 3 a b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] +$$

$$b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 3 a b^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] - \frac{3}{2} b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] +$$

$$b^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x)^m] - a^3 m \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \frac{3}{2} a^2 b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - a b^2 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right] +$$

$$\frac{1}{4} b^3 m n^3 \operatorname{Log}[x]^4 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 3 a^2 b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 3 a b^2 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] -$$

$$b^3 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 3 a b^2 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \frac{3}{2} b^3 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] -$$

$$b^3 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - m (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] + 3 b m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] -$$

$$6 a b^2 m n^2 \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] - 6 b^3 m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] + 6 b^3 m n^3 \operatorname{PolyLog}\left[5, -\frac{f x}{e}\right]$$

Problem 88: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m]}{x^2} dx$$

Optimal (type 4, 411 leaves, 14 steps):

$$\begin{aligned}
& \frac{6 b^3 f m n^3 \operatorname{Log}[x]}{e} - \frac{6 b^2 f m n^2 \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])}{e} - \frac{3 b f m n \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^2}{e} - \\
& \frac{f m \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^3}{e} - \frac{6 b^3 f m n^3 \operatorname{Log}[e + f x]}{e} - \frac{6 b^3 n^3 \operatorname{Log}[d (e + f x)^m]}{x} - \frac{6 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m]}{x} - \\
& \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{x} - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m]}{x} + \frac{6 b^3 f m n^3 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e} + \\
& \frac{6 b^2 f m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e} + \frac{3 b f m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{e} + \\
& \frac{6 b^3 f m n^3 \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{e} + \frac{6 b^2 f m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{e} + \frac{6 b^3 f m n^3 \operatorname{PolyLog}\left[4, -\frac{e}{f x}\right]}{e}
\end{aligned}$$

Result (type 4, 1347 leaves):

$$\begin{aligned}
& -\frac{1}{4 e x} \left(-4 a^3 f m x \operatorname{Log}[x] - 12 a^2 b f m n x \operatorname{Log}[x] - 24 a b^2 f m n^2 x \operatorname{Log}[x] - 24 b^3 f m n^3 x \operatorname{Log}[x] + 6 a^2 b f m n x \operatorname{Log}[x]^2 + 12 a b^2 f m n^2 x \operatorname{Log}[x]^2 + \right. \\
& 12 b^3 f m n^3 x \operatorname{Log}[x]^2 - 4 a b^2 f m n^2 x \operatorname{Log}[x]^3 - 4 b^3 f m n^3 x \operatorname{Log}[x]^3 + b^3 f m n^3 x \operatorname{Log}[x]^4 - 12 a^2 b f m x \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\
& 24 a b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] - 24 b^3 f m n^2 x \operatorname{Log}[x] \operatorname{Log}[c x^n] + 12 a b^2 f m n x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 12 b^3 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - \\
& 4 b^3 f m n^2 x \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] - 12 a b^2 f m x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - 12 b^3 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 6 b^3 f m n x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 - \\
& 4 b^3 f m x \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 + 4 a^3 f m x \operatorname{Log}[e + f x] + 12 a^2 b f m n x \operatorname{Log}[e + f x] + 24 a b^2 f m n^2 x \operatorname{Log}[e + f x] + 24 b^3 f m n^3 x \operatorname{Log}[e + f x] - \\
& 12 a^2 b f m n x \operatorname{Log}[x] \operatorname{Log}[e + f x] - 24 a b^2 f m n^2 x \operatorname{Log}[x] \operatorname{Log}[e + f x] - 24 b^3 f m n^3 x \operatorname{Log}[x] \operatorname{Log}[e + f x] + 12 a b^2 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] + \\
& 12 b^3 f m n^3 x \operatorname{Log}[x]^2 \operatorname{Log}[e + f x] - 4 b^3 f m n^3 x \operatorname{Log}[x]^3 \operatorname{Log}[e + f x] + 12 a^2 b f m x \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 24 a b^2 f m n x \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + \\
& 24 b^3 f m n^2 x \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 24 a b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] - 24 b^3 f m n^2 x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + \\
& 12 b^3 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x] + 12 a b^2 f m x \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 12 b^3 f m n x \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] - \\
& 12 b^3 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x] + 4 b^3 f m x \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x] + 4 a^3 e \operatorname{Log}[d (e + f x)^m] + 12 a^2 b e n \operatorname{Log}[d (e + f x)^m] + \\
& 24 a b^2 e n^2 \operatorname{Log}[d (e + f x)^m] + 24 b^3 e n^3 \operatorname{Log}[d (e + f x)^m] + 12 a^2 b e \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 24 a b^2 e n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + \\
& 24 b^3 e n^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x)^m] + 12 a b^2 e \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] + 12 b^3 e n \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x)^m] + \\
& 4 b^3 e \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x)^m] + 12 a^2 b f m n x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 24 a b^2 f m n^2 x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 24 b^3 f m n^3 x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 12 a b^2 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 12 b^3 f m n^3 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 4 b^3 f m n^3 x \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 24 a b^2 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 24 b^3 f m n^2 x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] - 12 b^3 f m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{f x}{e}\right] + \\
& 12 b^3 f m n x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{f x}{e}\right] + 12 b f m n x \left(a^2 + 2 a b n + 2 b^2 n^2 + 2 b (a + b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{f x}{e}\right] - \\
& \left. 24 b^2 f m n^2 x (a + b n + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x}{e}\right] + 24 b^3 f m n^3 x \operatorname{PolyLog}\left[4, -\frac{f x}{e}\right] \right)
\end{aligned}$$

Problem 89: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m]}{x^3} dx$$

Optimal (type 4, 555 leaves, 22 steps):

$$\begin{aligned} & - \frac{45 b^3 f m n^3}{8 e x} - \frac{3 b^3 f^2 m n^3 \operatorname{Log}[x]}{8 e^2} - \frac{21 b^2 f m n^2 (a + b \operatorname{Log}[c x^n])}{4 e x} + \frac{3 b^2 f^2 m n^2 \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])}{4 e^2} - \\ & \frac{9 b f m n (a + b \operatorname{Log}[c x^n])^2}{4 e x} + \frac{3 b f^2 m n \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^2}{4 e^2} - \frac{f m (a + b \operatorname{Log}[c x^n])^3}{2 e x} + \frac{f^2 m \operatorname{Log}\left[1 + \frac{e}{f x}\right] (a + b \operatorname{Log}[c x^n])^3}{2 e^2} + \\ & \frac{3 b^3 f^2 m n^3 \operatorname{Log}[e + f x]}{8 e^2} - \frac{3 b^3 n^3 \operatorname{Log}[d (e + f x)^m]}{8 x^2} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x)^m]}{4 x^2} - \\ & \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x)^m]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x)^m]}{2 x^2} - \frac{3 b^3 f^2 m n^3 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{4 e^2} - \\ & \frac{3 b^2 f^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{2 e^2} - \frac{3 b f^2 m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x}\right]}{2 e^2} - \\ & \frac{3 b^3 f^2 m n^3 \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{2 e^2} - \frac{3 b^2 f^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{e}{f x}\right]}{e^2} - \frac{3 b^3 f^2 m n^3 \operatorname{PolyLog}\left[4, -\frac{e}{f x}\right]}{e^2} \end{aligned}$$

Result (type 4, 1736 leaves):

$$\begin{aligned}
& -\frac{1}{8e^2x^2} \left(4a^3efmx + 18a^2befmnx + 42ab^2efmn^2x + 45b^3efmn^3x + 4a^3f^2mx^2 \operatorname{Log}[x] + 6a^2bf^2mnx^2 \operatorname{Log}[x] + \right. \\
& 6ab^2f^2mn^2x^2 \operatorname{Log}[x] + 3b^3f^2mn^3x^2 \operatorname{Log}[x] - 6a^2bf^2mnx^2 \operatorname{Log}[x]^2 - 6ab^2f^2mn^2x^2 \operatorname{Log}[x]^2 - 3b^3f^2mn^3x^2 \operatorname{Log}[x]^2 + \\
& 4ab^2f^2mn^2x^2 \operatorname{Log}[x]^3 + 2b^3f^2mn^3x^2 \operatorname{Log}[x]^3 - b^3f^2mn^3x^2 \operatorname{Log}[x]^4 + 12a^2befmx \operatorname{Log}[cx^n] + 36ab^2efmnx \operatorname{Log}[cx^n] + \\
& 42b^3efmn^2x \operatorname{Log}[cx^n] + 12a^2bf^2mx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] + 12ab^2f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] + 6b^3f^2mn^2x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] - \\
& 12ab^2f^2mnx^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] - 6b^3f^2mn^2x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] + 4b^3f^2mn^2x^2 \operatorname{Log}[x]^3 \operatorname{Log}[cx^n] + 12ab^2efmx \operatorname{Log}[cx^n]^2 + \\
& 18b^3efmnx \operatorname{Log}[cx^n]^2 + 12ab^2f^2mx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 + 6b^3f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 - 6b^3f^2mnx^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n]^2 + \\
& 4b^3efmx \operatorname{Log}[cx^n]^3 + 4b^3f^2mx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^3 - 4a^3f^2mx^2 \operatorname{Log}[e+fx] - 6a^2bf^2mnx^2 \operatorname{Log}[e+fx] - 6ab^2f^2mn^2x^2 \operatorname{Log}[e+fx] - \\
& 3b^3f^2mn^3x^2 \operatorname{Log}[e+fx] + 12a^2bf^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[e+fx] + 12ab^2f^2mn^2x^2 \operatorname{Log}[x] \operatorname{Log}[e+fx] + 6b^3f^2mn^3x^2 \operatorname{Log}[x] \operatorname{Log}[e+fx] - \\
& 12ab^2f^2mn^2x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e+fx] - 6b^3f^2mn^3x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e+fx] + 4b^3f^2mn^3x^2 \operatorname{Log}[x]^3 \operatorname{Log}[e+fx] - \\
& 12a^2bf^2mx^2 \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] - 12ab^2f^2mnx^2 \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] - 6b^3f^2mn^2x^2 \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] + \\
& 24ab^2f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] + 12b^3f^2mn^2x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] - 12b^3f^2mn^2x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] \operatorname{Log}[e+fx] - \\
& 12ab^2f^2mx^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[e+fx] - 6b^3f^2mnx^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[e+fx] + 12b^3f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 \operatorname{Log}[e+fx] - \\
& 4b^3f^2mx^2 \operatorname{Log}[cx^n]^3 \operatorname{Log}[e+fx] + 4a^3e^2 \operatorname{Log}[d(e+fx)^m] + 6a^2be^2n \operatorname{Log}[d(e+fx)^m] + 6ab^2e^2n^2 \operatorname{Log}[d(e+fx)^m] + \\
& 3b^3e^2n^3 \operatorname{Log}[d(e+fx)^m] + 12a^2be^2 \operatorname{Log}[cx^n] \operatorname{Log}[d(e+fx)^m] + 12ab^2e^2n \operatorname{Log}[cx^n] \operatorname{Log}[d(e+fx)^m] + 6b^3e^2n^2 \operatorname{Log}[cx^n] \operatorname{Log}[d(e+fx)^m] + \\
& 12ab^2e^2 \operatorname{Log}[cx^n]^2 \operatorname{Log}[d(e+fx)^m] + 6b^3e^2n \operatorname{Log}[cx^n]^2 \operatorname{Log}[d(e+fx)^m] + 4b^3e^2 \operatorname{Log}[cx^n]^3 \operatorname{Log}[d(e+fx)^m] - \\
& 12a^2bf^2mnx^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 12ab^2f^2mn^2x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 6b^3f^2mn^3x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{fx}{e}\right] + \\
& 12ab^2f^2mn^2x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{fx}{e}\right] + 6b^3f^2mn^3x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 4b^3f^2mn^3x^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - \\
& 24ab^2f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 12b^3f^2mn^2x^2 \operatorname{Log}[x] \operatorname{Log}[cx^n] \operatorname{Log}\left[1 + \frac{fx}{e}\right] + 12b^3f^2mn^2x^2 \operatorname{Log}[x]^2 \operatorname{Log}[cx^n] \operatorname{Log}\left[1 + \frac{fx}{e}\right] - \\
& 12b^3f^2mnx^2 \operatorname{Log}[x] \operatorname{Log}[cx^n]^2 \operatorname{Log}\left[1 + \frac{fx}{e}\right] - 6bf^2mnx^2 \left(2a^2 + 2abn + b^2n^2 + 2b(2a+bn) \operatorname{Log}[cx^n] + 2b^2 \operatorname{Log}[cx^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{fx}{e}\right] + \\
& \left. 12b^2f^2mn^2x^2 \left(2a+bn + 2b \operatorname{Log}[cx^n] \right) \operatorname{PolyLog}\left[3, -\frac{fx}{e}\right] - 24b^3f^2mn^3x^2 \operatorname{PolyLog}\left[4, -\frac{fx}{e}\right] \right)
\end{aligned}$$

Problem 90: Result unnecessarily involves imaginary or complex numbers.

$$\int x^3 (a + b \operatorname{Log}[cx^n]) \operatorname{Log}[d(e+fx^2)^m] dx$$

Optimal (type 4, 221 leaves, 9 steps):

$$\begin{aligned}
& -\frac{3bemnx^2}{16f} + \frac{1}{16} bmnx^4 + \frac{emx^2(a+b \operatorname{Log}[cx^n])}{4f} - \frac{1}{8} mx^4(a+b \operatorname{Log}[cx^n]) + \frac{be^2mn \operatorname{Log}[e+fx^2]}{16f^2} + \frac{be^2mn \operatorname{Log}\left[-\frac{fx^2}{e}\right] \operatorname{Log}[e+fx^2]}{8f^2} - \\
& \frac{e^2m(a+b \operatorname{Log}[cx^n]) \operatorname{Log}[e+fx^2]}{4f^2} - \frac{1}{16} bnx^4 \operatorname{Log}[d(e+fx^2)^m] + \frac{1}{4} x^4(a+b \operatorname{Log}[cx^n]) \operatorname{Log}[d(e+fx^2)^m] + \frac{be^2mn \operatorname{PolyLog}\left[2, 1 + \frac{fx^2}{e}\right]}{8f^2}
\end{aligned}$$

Result (type 4, 324 leaves):

$$\begin{aligned}
& -\frac{1}{16 f^2} \left(-4 a e f m x^2 + 3 b e f m n x^2 + 2 a f^2 m x^4 - b f^2 m n x^4 - 4 b e f m x^2 \operatorname{Log}[c x^n] + 2 b f^2 m x^4 \operatorname{Log}[c x^n] + \right. \\
& 4 b e^2 m n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 b e^2 m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 a e^2 m \operatorname{Log}[e + f x^2] - b e^2 m n \operatorname{Log}[e + f x^2] - \\
& 4 b e^2 m n \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 4 b e^2 m \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 4 a f^2 x^4 \operatorname{Log}[d (e + f x^2)^m] + b f^2 n x^4 \operatorname{Log}[d (e + f x^2)^m] - \\
& \left. 4 b f^2 x^4 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 4 b e^2 m n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 b e^2 m n \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 91: Result unnecessarily involves imaginary or complex numbers.

$$\int x (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m] dx$$

Optimal (type 4, 148 leaves, 9 steps):

$$\begin{aligned}
& \frac{1}{2} b m n x^2 - \frac{1}{2} m x^2 (a + b \operatorname{Log}[c x^n]) - \frac{b n (e + f x^2) \operatorname{Log}[d (e + f x^2)^m]}{4 f} - \\
& \frac{b e n \operatorname{Log}\left[-\frac{f x^2}{e}\right] \operatorname{Log}[d (e + f x^2)^m]}{4 f} + \frac{(e + f x^2) (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{2 f} - \frac{b e m n \operatorname{PolyLog}\left[2, 1 + \frac{f x^2}{e}\right]}{4 f}
\end{aligned}$$

Result (type 4, 263 leaves):

$$\begin{aligned}
& \frac{1}{4 f} \left(-2 a f m x^2 + 2 b f m n x^2 - 2 b f m x^2 \operatorname{Log}[c x^n] + 2 b e m n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 2 b e m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \right. \\
& 2 a e m \operatorname{Log}[e + f x^2] - b e m n \operatorname{Log}[e + f x^2] - 2 b e m n \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 2 b e m \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 2 a f x^2 \operatorname{Log}[d (e + f x^2)^m] - \\
& \left. b f n x^2 \operatorname{Log}[d (e + f x^2)^m] + 2 b f x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 2 b e m n \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 2 b e m n \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 92: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{x} dx$$

Optimal (type 4, 113 leaves, 4 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{2 b n} - \frac{m (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{2 b n} - \frac{1}{2} m (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right] + \frac{1}{4} b m n \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right]$$

Result (type 4, 307 leaves):

$$\begin{aligned} & \frac{1}{2} \left(b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2 b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \right. \\ & 2 b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 a \operatorname{Log}[x] \operatorname{Log}[d (e + f x^2)^m] - b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x^2)^m] + \\ & 2 b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 2 a m \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{f x^2}{e}\right] - 2 b m \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[2, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\ & \left. 2 b m \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[2, \frac{i\sqrt{f}x}{\sqrt{e}}\right] - a m \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right] + 2 b m n \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 b m n \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] \right) \end{aligned}$$

Problem 93: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{x^3} dx$$

Optimal (type 4, 195 leaves, 11 steps):

$$\begin{aligned} & \frac{b f m n \operatorname{Log}[x]}{2 e} - \frac{b f m n \operatorname{Log}[x]^2}{2 e} + \frac{f m \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n])}{e} - \frac{b f m n \operatorname{Log}[e + f x^2]}{4 e} + \frac{b f m n \operatorname{Log}\left[-\frac{f x^2}{e}\right] \operatorname{Log}[e + f x^2]}{4 e} - \\ & \frac{f m (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[e + f x^2]}{2 e} - \frac{b n \operatorname{Log}[d (e + f x^2)^m]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{2 x^2} + \frac{b f m n \operatorname{PolyLog}\left[2, 1 + \frac{f x^2}{e}\right]}{4 e} \end{aligned}$$

Result (type 4, 298 leaves):

$$\begin{aligned} & -\frac{1}{4 e x^2} \left(-4 a f m x^2 \operatorname{Log}[x] - 2 b f m n x^2 \operatorname{Log}[x] + 2 b f m n x^2 \operatorname{Log}[x]^2 - 4 b f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + \right. \\ & 2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 a f m x^2 \operatorname{Log}[e + f x^2] + b f m n x^2 \operatorname{Log}[e + f x^2] - \\ & 2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 2 b f m x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 2 a e \operatorname{Log}[d (e + f x^2)^m] + b e n \operatorname{Log}[d (e + f x^2)^m] + \\ & \left. 2 b e \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 2 b f m n x^2 \operatorname{PolyLog}\left[2, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 b f m n x^2 \operatorname{PolyLog}\left[2, \frac{i\sqrt{f}x}{\sqrt{e}}\right] \right) \end{aligned}$$

Problem 94: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{x^5} dx$$

Optimal (type 4, 248 leaves, 10 steps):

$$\begin{aligned}
& - \frac{3 b f m n}{16 e x^2} - \frac{b f^2 m n \operatorname{Log}[x]}{8 e^2} + \frac{b f^2 m n \operatorname{Log}[x]^2}{4 e^2} - \frac{f m (a + b \operatorname{Log}[c x^n])}{4 e x^2} - \frac{f^2 m \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n])}{2 e^2} + \\
& \frac{b f^2 m n \operatorname{Log}[e + f x^2]}{16 e^2} - \frac{b f^2 m n \operatorname{Log}\left[-\frac{f x^2}{e}\right] \operatorname{Log}[e + f x^2]}{8 e^2} + \frac{f^2 m (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[e + f x^2]}{4 e^2} - \\
& \frac{b n \operatorname{Log}[d (e + f x^2)^m]}{16 x^4} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{4 x^4} - \frac{b f^2 m n \operatorname{PolyLog}\left[2, 1 + \frac{f x^2}{e}\right]}{8 e^2}
\end{aligned}$$

Result (type 4, 363 leaves):

$$\begin{aligned}
& - \frac{1}{16 e^2 x^4} \left(4 a e f m x^2 + 3 b e f m n x^2 + 8 a f^2 m x^4 \operatorname{Log}[x] + 2 b f^2 m n x^4 \operatorname{Log}[x] - 4 b f^2 m n x^4 \operatorname{Log}[x]^2 + 4 b e f m x^2 \operatorname{Log}[c x^n] + \right. \\
& 8 b f^2 m x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 4 b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 4 b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 4 a f^2 m x^4 \operatorname{Log}[e + f x^2] - \\
& b f^2 m n x^4 \operatorname{Log}[e + f x^2] + 4 b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - 4 b f^2 m x^4 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 4 a e^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& \left. b e^2 n \operatorname{Log}[d (e + f x^2)^m] + 4 b e^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 4 b f^2 m n x^4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 4 b f^2 m n x^4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 100: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m] dx$$

Optimal (type 4, 310 leaves, 17 steps):

$$\begin{aligned}
& - \frac{3}{4} b^2 m n^2 x^2 + b m n x^2 (a + b \operatorname{Log}[c x^n]) - \frac{1}{2} m x^2 (a + b \operatorname{Log}[c x^n])^2 + \frac{b^2 e m n^2 \operatorname{Log}[e + f x^2]}{4 f} + \frac{1}{4} b^2 n^2 x^2 \operatorname{Log}[d (e + f x^2)^m] - \\
& \frac{1}{2} b n x^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m] + \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m] - \frac{b e m n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{2 f} + \\
& \frac{e m (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{2 f} - \frac{b^2 e m n^2 \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right]}{4 f} + \frac{b e m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right]}{2 f} - \frac{b^2 e m n^2 \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right]}{4 f}
\end{aligned}$$

Result (type 4, 814 leaves):

$$\begin{aligned}
& \frac{1}{4f} \\
& \left(-2a^2 f m x^2 + 4abf m n x^2 - 3b^2 f m n^2 x^2 - 4abf m x^2 \operatorname{Log}[c x^n] + 4b^2 f m n x^2 \operatorname{Log}[c x^n] - 2b^2 f m x^2 \operatorname{Log}[c x^n]^2 + 4abem n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \right. \\
& 2b^2 em n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2b^2 em n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 4b^2 em n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& 4abem n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2b^2 em n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2b^2 em n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& 4b^2 em n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2a^2 em \operatorname{Log}[e + f x^2] - 2abem n \operatorname{Log}[e + f x^2] + b^2 em n^2 \operatorname{Log}[e + f x^2] - \\
& 4abem n \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 2b^2 em n^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 2b^2 em n^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] + 4abem \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - \\
& 2b^2 em n \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 4b^2 em n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 2b^2 em \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + \\
& 2a^2 f x^2 \operatorname{Log}[d(e + f x^2)^m] - 2abf n x^2 \operatorname{Log}[d(e + f x^2)^m] + b^2 f n^2 x^2 \operatorname{Log}[d(e + f x^2)^m] + 4abf x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] - \\
& 2b^2 f n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] + 2b^2 f x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d(e + f x^2)^m] + 2bem n (2a - bn + 2b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& \left. 2bem n (2a - bn + 2b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 4b^2 em n^2 \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - 4b^2 em n^2 \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 101: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d(e + f x^2)^m]}{x} dx$$

Optimal (type 4, 147 leaves, 5 steps):

$$\begin{aligned}
& \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d(e + f x^2)^m]}{3bn} - \frac{m(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{3bn} - \\
& \frac{1}{2} m (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right] + \frac{1}{2} b m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right] - \frac{1}{4} b^2 m n^2 \operatorname{PolyLog}\left[4, -\frac{f x^2}{e}\right]
\end{aligned}$$

Result (type 4, 736 leaves):

$$\begin{aligned}
& -a^2 m \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + a b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \frac{1}{3} b^2 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2 a b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& b^2 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - b^2 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - a^2 m \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& a b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \frac{1}{3} b^2 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2 a b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& b^2 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - b^2 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + a^2 \operatorname{Log}[x] \operatorname{Log}[d(e + f x^2)^m] - \\
& a b n \operatorname{Log}[x]^2 \operatorname{Log}[d(e + f x^2)^m] + \frac{1}{3} b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d(e + f x^2)^m] + 2 a b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] - \\
& b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] + b^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[d(e + f x^2)^m] - m(a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& m(a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 a b m n \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 b^2 m n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& 2 a b m n \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 2 b^2 m n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2 b^2 m n^2 \operatorname{PolyLog}\left[4, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - 2 b^2 m n^2 \operatorname{PolyLog}\left[4, \frac{i\sqrt{f}x}{\sqrt{e}}\right]
\end{aligned}$$

Problem 102: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d(e + f x^2)^m]}{x^3} dx$$

Optimal (type 4, 276 leaves, 11 steps):

$$\begin{aligned}
& \frac{b^2 f m n^2 \operatorname{Log}[x]}{2 e} - \frac{b f m n \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])}{2 e} - \frac{f m \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])^2}{2 e} - \frac{b^2 f m n^2 \operatorname{Log}[e + f x^2]}{4 e} - \\
& \frac{b^2 n^2 \operatorname{Log}[d(e + f x^2)^m]}{4 x^2} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d(e + f x^2)^m]}{2 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d(e + f x^2)^m]}{2 x^2} + \\
& \frac{b^2 f m n^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{4 e} + \frac{b f m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{2 e} + \frac{b^2 f m n^2 \operatorname{PolyLog}\left[3, -\frac{e}{f x^2}\right]}{4 e}
\end{aligned}$$

Result (type 4, 946 leaves):

$$\begin{aligned}
& -\frac{1}{12 e x^2} \left(-12 a^2 f m x^2 \operatorname{Log}[x] - 12 a b f m n x^2 \operatorname{Log}[x] - 6 b^2 f m n^2 x^2 \operatorname{Log}[x] + 12 a b f m n x^2 \operatorname{Log}[x]^2 + 6 b^2 f m n^2 x^2 \operatorname{Log}[x]^2 - \right. \\
& \quad 4 b^2 f m n^2 x^2 \operatorname{Log}[x]^3 - 24 a b f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 12 b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + 12 b^2 f m n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - \\
& \quad 12 b^2 f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 12 a b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& \quad 6 b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 a b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& \quad 6 b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& \quad 6 a^2 f m x^2 \operatorname{Log}[e + f x^2] + 6 a b f m n x^2 \operatorname{Log}[e + f x^2] + 3 b^2 f m n^2 x^2 \operatorname{Log}[e + f x^2] - 12 a b f m n x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - \\
& \quad 6 b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 6 b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] + 12 a b f m x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + \\
& \quad 6 b^2 f m n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 12 b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 6 b^2 f m x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + \\
& \quad 6 a^2 e \operatorname{Log}[d (e + f x^2)^m] + 6 a b e n \operatorname{Log}[d (e + f x^2)^m] + 3 b^2 e n^2 \operatorname{Log}[d (e + f x^2)^m] + 12 a b e \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& \quad 6 b^2 e n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 6 b^2 e \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + 6 b f m n x^2 (2 a + b n + 2 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& \quad \left. 6 b f m n x^2 (2 a + b n + 2 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^2 f m n^2 x^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^2 f m n^2 x^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 103: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{x^5} dx$$

Optimal (type 4, 356 leaves, 15 steps):

$$\begin{aligned}
& -\frac{7 b^2 f m n^2}{32 e x^2} - \frac{b^2 f^2 m n^2 \operatorname{Log}[x]}{16 e^2} - \frac{3 b f m n (a + b \operatorname{Log}[c x^n])}{8 e x^2} + \frac{b f^2 m n \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])}{8 e^2} - \frac{f m (a + b \operatorname{Log}[c x^n])^2}{4 e x^2} + \\
& \frac{f^2 m \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])^2}{4 e^2} + \frac{b^2 f^2 m n^2 \operatorname{Log}[e + f x^2]}{32 e^2} - \frac{b^2 n^2 \operatorname{Log}[d (e + f x^2)^m]}{32 x^4} - \frac{b n (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{8 x^4} - \\
& \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{4 x^4} - \frac{b^2 f^2 m n^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{16 e^2} - \frac{b f^2 m n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{4 e^2} - \frac{b^2 f^2 m n^2 \operatorname{PolyLog}\left[3, -\frac{e}{f x^2}\right]}{8 e^2}
\end{aligned}$$

Result (type 4, 1111 leaves):

$$\begin{aligned}
& - \frac{1}{96 e^2 x^4} \\
& \left(24 a^2 e f m x^2 + 36 a b e f m n x^2 + 21 b^2 e f m n^2 x^2 + 48 a^2 f^2 m x^4 \operatorname{Log}[x] + 24 a b f^2 m n x^4 \operatorname{Log}[x] + 6 b^2 f^2 m n^2 x^4 \operatorname{Log}[x] - 48 a b f^2 m n x^4 \operatorname{Log}[x]^2 - \right. \\
& 12 b^2 f^2 m n^2 x^4 \operatorname{Log}[x]^2 + 16 b^2 f^2 m n^2 x^4 \operatorname{Log}[x]^3 + 48 a b e f m x^2 \operatorname{Log}[c x^n] + 36 b^2 e f m n x^2 \operatorname{Log}[c x^n] + 96 a b f^2 m x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 24 b^2 f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 48 b^2 f^2 m n x^4 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 24 b^2 e f m x^2 \operatorname{Log}[c x^n]^2 + 48 b^2 f^2 m x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - \\
& 48 a b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^2 f^2 m n^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 b^2 f^2 m n^2 x^4 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 48 b^2 f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 48 a b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^2 f^2 m n^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 24 b^2 f^2 m n^2 x^4 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 48 b^2 f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 24 a^2 f^2 m x^4 \operatorname{Log}[e + f x^2] - \\
& 12 a b f^2 m n x^4 \operatorname{Log}[e + f x^2] - 3 b^2 f^2 m n^2 x^4 \operatorname{Log}[e + f x^2] + 48 a b f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 12 b^2 f^2 m n^2 x^4 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - \\
& 24 b^2 f^2 m n^2 x^4 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] - 48 a b f^2 m x^4 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 12 b^2 f^2 m n x^4 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + \\
& 48 b^2 f^2 m n x^4 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 24 b^2 f^2 m x^4 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + 24 a^2 e^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& 12 a b e^2 n \operatorname{Log}[d (e + f x^2)^m] + 3 b^2 e^2 n^2 \operatorname{Log}[d (e + f x^2)^m] + 48 a b e^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 12 b^2 e^2 n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& 24 b^2 e^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 12 b f^2 m n x^4 (4 a + b n + 4 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& \left. 12 b f^2 m n x^4 (4 a + b n + 4 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 48 b^2 f^2 m n^2 x^4 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 48 b^2 f^2 m n^2 x^4 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 108: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] dx$$

Optimal (type 4, 514 leaves, 26 steps):

$$\begin{aligned}
& \frac{3}{2} b^3 m n^3 x^2 - \frac{9}{4} b^2 m n^2 x^2 (a + b \operatorname{Log}[c x^n]) + \frac{3}{2} b m n x^2 (a + b \operatorname{Log}[c x^n])^2 - \frac{1}{2} m x^2 (a + b \operatorname{Log}[c x^n])^3 - \\
& \frac{3 b^3 e m n^3 \operatorname{Log}[e + f x^2]}{8 f} - \frac{3}{8} b^3 n^3 x^2 \operatorname{Log}[d (e + f x^2)^m] + \frac{3}{4} b^2 n^2 x^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m] - \\
& \frac{3}{4} b n x^2 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m] + \frac{1}{2} x^2 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] + \frac{3 b^2 e m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{4 f} - \\
& \frac{3 b e m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{4 f} + \frac{e m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{2 f} + \frac{3 b^3 e m n^3 \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right]}{8 f} - \\
& \frac{3 b^2 e m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right]}{4 f} + \frac{3 b e m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right]}{4 f} + \\
& \frac{3 b^3 e m n^3 \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right]}{8 f} - \frac{3 b^2 e m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right]}{4 f} + \frac{3 b^3 e m n^3 \operatorname{PolyLog}\left[4, -\frac{f x^2}{e}\right]}{8 f}
\end{aligned}$$

Result (type 4, 1911 leaves):

$$\begin{aligned}
& \frac{1}{8 f} \left(-4 a^3 f m x^2 + 12 a^2 b f m n x^2 - 18 a b^2 f m n^2 x^2 + 12 b^3 f m n^3 x^2 - 12 a^2 b f m x^2 \operatorname{Log}[c x^n] + \right. \\
& 24 a b^2 f m n x^2 \operatorname{Log}[c x^n] - 18 b^3 f m n^2 x^2 \operatorname{Log}[c x^n] - 12 a b^2 f m x^2 \operatorname{Log}[c x^n]^2 + 12 b^3 f m n x^2 \operatorname{Log}[c x^n]^2 - 4 b^3 f m x^2 \operatorname{Log}[c x^n]^3 + \\
& 12 a^2 b e m n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 e m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 b^3 e m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 12 a b^2 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 b^3 e m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 b^3 e m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 24 a b^2 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 e m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 12 b^3 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 a^2 b e m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 e m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 b^3 e m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 b^3 e m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 4 b^3 e m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 a b^2 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 e m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 12 b^3 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 a^3 e m \operatorname{Log}[e + f x^2] - \\
& 6 a^2 b e m n \operatorname{Log}[e + f x^2] + 6 a b^2 e m n^2 \operatorname{Log}[e + f x^2] - 3 b^3 e m n^3 \operatorname{Log}[e + f x^2] - 12 a^2 b e m n \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + \\
& 12 a b^2 e m n^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - 6 b^3 e m n^3 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + 12 a b^2 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] - 6 b^3 e m n^3 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] \left. \right) -
\end{aligned}$$

$$\begin{aligned}
& 4 b^3 e m n^3 \operatorname{Log}[x]^3 \operatorname{Log}[e + f x^2] + 12 a^2 b e m \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 12 a b^2 e m n \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 6 b^3 e m n^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - \\
& 24 a b^2 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 12 b^3 e m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 12 b^3 e m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + \\
& 12 a b^2 e m \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] - 6 b^3 e m n \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] - 12 b^3 e m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + \\
& 4 b^3 e m \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x^2] + 4 a^3 f x^2 \operatorname{Log}[d (e + f x^2)^m] - 6 a^2 b f n x^2 \operatorname{Log}[d (e + f x^2)^m] + 6 a b^2 f n^2 x^2 \operatorname{Log}[d (e + f x^2)^m] - \\
& 3 b^3 f n^3 x^2 \operatorname{Log}[d (e + f x^2)^m] + 12 a^2 b f x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 12 a b^2 f n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& 6 b^3 f n^2 x^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 12 a b^2 f x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 6 b^3 f n x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& 4 b^3 f x^2 \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] + 6 b e m n \left(2 a^2 - 2 a b n + b^2 n^2 - 2 b (-2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 b e m n \left(2 a^2 - 2 a b n + b^2 n^2 - 2 b (-2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 a b^2 e m n^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 e m n^3 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 b^3 e m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 24 a b^2 e m n^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 e m n^3 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 b^3 e m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 b^3 e m n^3 \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 b^3 e m n^3 \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \Big)
\end{aligned}$$

Problem 109: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{x} dx$$

Optimal (type 4, 181 leaves, 6 steps):

$$\begin{aligned}
& \frac{(a + b \operatorname{Log}[c x^n])^4 \operatorname{Log}[d (e + f x^2)^m]}{4 b n} - \frac{m (a + b \operatorname{Log}[c x^n])^4 \operatorname{Log}\left[1 + \frac{f x^2}{e}\right]}{4 b n} - \frac{1}{2} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, -\frac{f x^2}{e}\right] + \\
& \frac{3}{4} b m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[3, -\frac{f x^2}{e}\right] - \frac{3}{4} b^2 m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[4, -\frac{f x^2}{e}\right] + \frac{3}{8} b^3 m n^3 \operatorname{PolyLog}\left[5, -\frac{f x^2}{e}\right]
\end{aligned}$$

Result (type 4, 1348 leaves):

$$\begin{aligned}
& -a^3 m \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \frac{3}{2} a^2 b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - a b^2 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& \frac{1}{4} b^3 m n^3 \operatorname{Log}[x]^4 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 3 a^2 b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 3 a b^2 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& b^3 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 3 a b^2 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \frac{3}{2} b^3 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& b^3 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}\left[1 - \frac{i\sqrt{f}x}{\sqrt{e}}\right] - a^3 m \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \frac{3}{2} a^2 b m n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - a b^2 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& \frac{1}{4} b^3 m n^3 \operatorname{Log}[x]^4 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 3 a^2 b m \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 3 a b^2 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& b^3 m n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 3 a b^2 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \frac{3}{2} b^3 m n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& b^3 m \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}\left[1 + \frac{i\sqrt{f}x}{\sqrt{e}}\right] + a^3 \operatorname{Log}[x] \operatorname{Log}[d(e + f x^2)^m] - \frac{3}{2} a^2 b n \operatorname{Log}[x]^2 \operatorname{Log}[d(e + f x^2)^m] + \\
& a b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d(e + f x^2)^m] - \frac{1}{4} b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[d(e + f x^2)^m] + 3 a^2 b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] - \\
& 3 a b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] + b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[d(e + f x^2)^m] + 3 a b^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[d(e + f x^2)^m] - \\
& \frac{3}{2} b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d(e + f x^2)^m] + b^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}[d(e + f x^2)^m] - m (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& m (a + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 3 a^2 b m n \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 6 a b^2 m n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& 3 b^3 m n \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}\left[3, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 3 a^2 b m n \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 6 a b^2 m n \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + \\
& 3 b^3 m n \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}\left[3, \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 6 a b^2 m n^2 \operatorname{PolyLog}\left[4, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - 6 b^3 m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[4, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] - \\
& 6 a b^2 m n^2 \operatorname{PolyLog}\left[4, \frac{i\sqrt{f}x}{\sqrt{e}}\right] - 6 b^3 m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[4, \frac{i\sqrt{f}x}{\sqrt{e}}\right] + 6 b^3 m n^3 \operatorname{PolyLog}\left[5, -\frac{i\sqrt{f}x}{\sqrt{e}}\right] + 6 b^3 m n^3 \operatorname{PolyLog}\left[5, \frac{i\sqrt{f}x}{\sqrt{e}}\right]
\end{aligned}$$

Problem 110: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d(e + f x^2)^m]}{x^3} dx$$

Optimal (type 4, 451 leaves, 15 steps):

$$\begin{aligned}
& \frac{3 b^3 f m n^3 \operatorname{Log}[x]}{4 e} - \frac{3 b^2 f m n^2 \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])}{4 e} - \frac{3 b f m n \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])^2}{4 e} \\
& - \frac{f m \operatorname{Log}\left[1 + \frac{e}{f x^2}\right] (a + b \operatorname{Log}[c x^n])^3}{2 e} - \frac{3 b^3 f m n^3 \operatorname{Log}[e + f x^2]}{8 e} - \frac{3 b^3 n^3 \operatorname{Log}[d (e + f x^2)^m]}{8 x^2} - \frac{3 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{4 x^2} \\
& - \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{2 x^2} + \frac{3 b^3 f m n^3 \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{8 e} \\
& + \frac{3 b^2 f m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{4 e} + \frac{3 b f m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{e}{f x^2}\right]}{4 e} \\
& + \frac{3 b^3 f m n^3 \operatorname{PolyLog}\left[3, -\frac{e}{f x^2}\right]}{8 e} + \frac{3 b^2 f m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{e}{f x^2}\right]}{4 e} + \frac{3 b^3 f m n^3 \operatorname{PolyLog}\left[4, -\frac{e}{f x^2}\right]}{8 e}
\end{aligned}$$

Result (type 4, 2248 leaves):

$$\begin{aligned}
& -\frac{1}{8 e x^2} \left(-8 a^3 f m x^2 \operatorname{Log}[x] - 12 a^2 b f m n x^2 \operatorname{Log}[x] - 12 a b^2 f m n^2 x^2 \operatorname{Log}[x] - 6 b^3 f m n^3 x^2 \operatorname{Log}[x] + 12 a^2 b f m n x^2 \operatorname{Log}[x]^2 + 12 a b^2 f m n^2 x^2 \operatorname{Log}[x]^2 + \right. \\
& 6 b^3 f m n^3 x^2 \operatorname{Log}[x]^2 - 8 a b^2 f m n^2 x^2 \operatorname{Log}[x]^3 - 4 b^3 f m n^3 x^2 \operatorname{Log}[x]^3 + 2 b^3 f m n^3 x^2 \operatorname{Log}[x]^4 - 24 a^2 b f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\
& 24 a b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] - 12 b^3 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] + 24 a b^2 f m n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 12 b^3 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - \\
& 8 b^3 f m n^2 x^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] - 24 a b^2 f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - 12 b^3 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 12 b^3 f m n x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 - \\
& 8 b^3 f m x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 + 12 a^2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 a b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 b^3 f m n^3 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 b^3 f m n^3 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 4 b^3 f m n^3 x^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 a b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 12 b^3 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 12 a^2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 12 a b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 b^3 f m n^3 x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 b^3 f m n^3 x^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 b^3 f m n^3 x^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 a b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 12 b^3 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] +
\end{aligned}$$

$$\begin{aligned}
& 12 b^3 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 4 a^3 f m x^2 \operatorname{Log}[e + f x^2] + 6 a^2 b f m n x^2 \operatorname{Log}[e + f x^2] + 6 a b^2 f m n^2 x^2 \operatorname{Log}[e + f x^2] + \\
& 3 b^3 f m n^3 x^2 \operatorname{Log}[e + f x^2] - 12 a^2 b f m n x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - 12 a b^2 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] - 6 b^3 f m n^3 x^2 \operatorname{Log}[x] \operatorname{Log}[e + f x^2] + \\
& 12 a b^2 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] + 6 b^3 f m n^3 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^2] - 4 b^3 f m n^3 x^2 \operatorname{Log}[x]^3 \operatorname{Log}[e + f x^2] + \\
& 12 a^2 b f m x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 12 a b^2 f m n x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 6 b^3 f m n^2 x^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - \\
& 24 a b^2 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] - 12 b^3 f m n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + 12 b^3 f m n^2 x^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^2] + \\
& 12 a b^2 f m x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + 6 b^3 f m n x^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] - 12 b^3 f m n x^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^2] + \\
& 4 b^3 f m x^2 \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x^2] + 4 a^3 e \operatorname{Log}[d (e + f x^2)^m] + 6 a^2 b e n \operatorname{Log}[d (e + f x^2)^m] + 6 a b^2 e n^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& 3 b^3 e n^3 \operatorname{Log}[d (e + f x^2)^m] + 12 a^2 b e \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 12 a b^2 e n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& 6 b^3 e n^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 12 a b^2 e \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + 6 b^3 e n \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& 4 b^3 e \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] + 6 b f m n x^2 \left(2 a^2 + 2 a b n + b^2 n^2 + 2 b (2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2\right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 b f m n x^2 \left(2 a^2 + 2 a b n + b^2 n^2 + 2 b (2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2\right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 a b^2 f m n^2 x^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 f m n^3 x^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 b^3 f m n^2 x^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 24 a b^2 f m n^2 x^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 f m n^3 x^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 24 b^3 f m n^2 x^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 b^3 f m n^3 x^2 \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 24 b^3 f m n^3 x^2 \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right]
\end{aligned}$$

Problem 111: Result more than twice size of optimal antiderivative.

$$\int x^2 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] dx$$

Optimal (type 4, 1092 leaves, 49 steps):

$$\begin{aligned}
& \frac{52 a b^2 e m n^2 x}{9 f} - \frac{160 b^3 e m n^3 x}{27 f} + \frac{16}{81} b^3 m n^3 x^3 + \frac{4 b^3 e^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right]}{27 f^{3/2}} + \frac{52 b^3 e m n^2 x \operatorname{Log}[c x^n]}{9 f} - \\
& \frac{4}{9} b^2 m n^2 x^3 (a + b \operatorname{Log}[c x^n]) - \frac{4 b^2 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] (a + b \operatorname{Log}[c x^n])}{9 f^{3/2}} - \frac{8 b e m n x (a + b \operatorname{Log}[c x^n])^2}{3 f} + \\
& \frac{4}{9} b m n x^3 (a + b \operatorname{Log}[c x^n])^2 + \frac{2 e m x (a + b \operatorname{Log}[c x^n])^3}{3 f} - \frac{2}{9} m x^3 (a + b \operatorname{Log}[c x^n])^3 + \frac{b (-e)^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} - \\
& \frac{(-e)^{3/2} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} - \frac{b (-e)^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} + \frac{(-e)^{3/2} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} - \\
& \frac{2}{27} b^3 n^3 x^3 \operatorname{Log}[d (e + f x^2)^m] + \frac{2}{9} b^2 n^2 x^3 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m] - \frac{1}{3} b n x^3 (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m] + \\
& \frac{1}{3} x^3 (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] - \frac{2 b^2 (-e)^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} + \\
& \frac{b (-e)^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}} + \frac{2 b^2 (-e)^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} - \\
& \frac{b (-e)^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}} + \frac{2 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right]}{9 f^{3/2}} - \frac{2 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right]}{9 f^{3/2}} + \\
& \frac{2 b^3 (-e)^{3/2} m n^3 \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} - \frac{2 b^2 (-e)^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}} - \frac{2 b^3 (-e)^{3/2} m n^3 \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 f^{3/2}} + \\
& \frac{2 b^2 (-e)^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}} + \frac{2 b^3 (-e)^{3/2} m n^3 \operatorname{PolyLog}\left[4, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}} - \frac{2 b^3 (-e)^{3/2} m n^3 \operatorname{PolyLog}\left[4, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{f^{3/2}}
\end{aligned}$$

Result (type 4, 2544 leaves):

$$\begin{aligned}
& \frac{1}{81 f^{3/2}} \left(54 a^3 e \sqrt{f} m x - 216 a^2 b e \sqrt{f} m n x + 468 a b^2 e \sqrt{f} m n^2 x - 480 b^3 e \sqrt{f} m n^3 x - 18 a^3 f^{3/2} m x^3 + 36 a^2 b f^{3/2} m n x^3 - 36 a b^2 f^{3/2} m n^2 x^3 + \right. \\
& 16 b^3 f^{3/2} m n^3 x^3 - 54 a^3 e^{3/2} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 54 a^2 b e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 36 a b^2 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 e^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + \\
& 162 a^2 b e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - 108 a b^2 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + 36 b^3 e^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - \\
& \left. 162 a b^2 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 + 54 b^3 e^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 + 54 b^3 e^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& 162 a^2 b e \sqrt{f} m x \operatorname{Log}[c x^n] - 432 a b^2 e \sqrt{f} m n x \operatorname{Log}[c x^n] + 468 b^3 e \sqrt{f} m n^2 x \operatorname{Log}[c x^n] - 54 a^2 b f^{3/2} m x^3 \operatorname{Log}[c x^n] + \\
& 72 a b^2 f^{3/2} m n x^3 \operatorname{Log}[c x^n] - 36 b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[c x^n] - 162 a^2 b e^{3/2} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + 108 a b^2 e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - \\
& 36 b^3 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + 324 a b^2 e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 108 b^3 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\
& 162 b^3 e^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 162 a b^2 e \sqrt{f} m x \operatorname{Log}[c x^n]^2 - 216 b^3 e \sqrt{f} m n x \operatorname{Log}[c x^n]^2 - 54 a b^2 f^{3/2} m x^3 \operatorname{Log}[c x^n]^2 + \\
& 36 b^3 f^{3/2} m n x^3 \operatorname{Log}[c x^n]^2 - 162 a b^2 e^{3/2} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 + 54 b^3 e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 + \\
& 162 b^3 e^{3/2} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 54 b^3 e \sqrt{f} m x \operatorname{Log}[c x^n]^3 - 18 b^3 f^{3/2} m x^3 \operatorname{Log}[c x^n]^3 - 54 b^3 e^{3/2} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^3 - \\
& 81 i a^2 b e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 54 i a b^2 e^{3/2} m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 18 i b^3 e^{3/2} m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 81 i a b^2 e^{3/2} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 27 i b^3 e^{3/2} m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 27 i b^3 e^{3/2} m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 162 i a b^2 e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 54 i b^3 e^{3/2} m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 81 i b^3 e^{3/2} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 81 i b^3 e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 81 i a^2 b e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 54 i a b^2 e^{3/2} m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 18 i b^3 e^{3/2} m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 81 i a b^2 e^{3/2} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 27 i b^3 e^{3/2} m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 27 i b^3 e^{3/2} m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 162 i a b^2 e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 54 i b^3 e^{3/2} m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 81 i b^3 e^{3/2} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 81 i b^3 e^{3/2} m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 27 a^3 f^{3/2} x^3 \operatorname{Log}[d (e + f x^2)^m] - 27 a^2 b f^{3/2} n x^3 \operatorname{Log}[d (e + f x^2)^m] + 18 a b^2 f^{3/2} n^2 x^3 \operatorname{Log}[d (e + f x^2)^m] - 6 b^3 f^{3/2} n^3 x^3 \operatorname{Log}[d (e + f x^2)^m] + \\
& 81 a^2 b f^{3/2} x^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 54 a b^2 f^{3/2} n x^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 18 b^3 f^{3/2} n^2 x^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& 81 a b^2 f^{3/2} x^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 27 b^3 f^{3/2} n x^3 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + 27 b^3 f^{3/2} x^3 \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] + \\
& 9 i b e^{3/2} m n \left(9 a^2 - 6 a b n + 2 b^2 n^2 - 6 b (-3 a + b n) \operatorname{Log}[c x^n] + 9 b^2 \operatorname{Log}[c x^n]^2\right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] -
\end{aligned}$$

$$\begin{aligned}
& 9 i b e^{3/2} m n \left(9 a^2 - 6 a b n + 2 b^2 n^2 - 6 b (-3 a + b n) \operatorname{Log}[c x^n] + 9 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 162 i a b^2 e^{3/2} m n^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 54 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 162 i b^3 e^{3/2} m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 162 i a b^2 e^{3/2} m n^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 54 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 162 i b^3 e^{3/2} m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 162 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 162 i b^3 e^{3/2} m n^3 \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \Big)
\end{aligned}$$

Problem 112: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] dx$$

Optimal (type 4, 977 leaves, 42 steps):

$$\begin{aligned}
& -24 a b^2 m n^2 x + 36 b^3 m n^3 x - 12 b^2 m n^2 (a - b n) x + \frac{12 b^2 \sqrt{e} m n^2 (a - b n) \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{f}} - \\
& 36 b^3 m n^2 x \operatorname{Log}[c x^n] + \frac{12 b^3 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]}{\sqrt{f}} + 12 b m n x (a + b \operatorname{Log}[c x^n])^2 - 2 m x (a + b \operatorname{Log}[c x^n])^3 + \\
& \frac{3 b \sqrt{-e} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{\sqrt{-e} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{3 b \sqrt{-e} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + \\
& \frac{\sqrt{-e} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + 6 a b^2 n^2 x \operatorname{Log}[d (e + f x^2)^m] - 6 b^3 n^3 x \operatorname{Log}[d (e + f x^2)^m] + 6 b^3 n^2 x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - \\
& 3 b n x (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m] + x (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m] - \frac{6 b^2 \sqrt{-e} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + \\
& \frac{3 b \sqrt{-e} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + \frac{6 b^2 \sqrt{-e} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \\
& \frac{3 b \sqrt{-e} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{f}} + \frac{6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{f}} + \\
& \frac{6 b^3 \sqrt{-e} m n^3 \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{6 b^2 \sqrt{-e} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{6 b^3 \sqrt{-e} m n^3 \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + \\
& \frac{6 b^2 \sqrt{-e} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} + \frac{6 b^3 \sqrt{-e} m n^3 \operatorname{PolyLog}\left[4, -\frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}} - \frac{6 b^3 \sqrt{-e} m n^3 \operatorname{PolyLog}\left[4, \frac{\sqrt{f} x}{\sqrt{-e}}\right]}{\sqrt{f}}
\end{aligned}$$

Result (type 4, 2302 leaves):

$$\begin{aligned}
& \frac{1}{\sqrt{f}} \left(-2 a^3 \sqrt{f} m x + 12 a^2 b \sqrt{f} m n x - 36 a b^2 \sqrt{f} m n^2 x + 48 b^3 \sqrt{f} m n^3 x + 2 a^3 \sqrt{e} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - \right. \\
& 6 a^2 b \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 12 a b^2 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 12 b^3 \sqrt{e} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 6 a^2 b \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + \\
& 12 a b^2 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - 12 b^3 \sqrt{e} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + 6 a b^2 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 - \\
& \left. 6 b^3 \sqrt{e} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 - 2 b^3 \sqrt{e} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^3 - 6 a^2 b \sqrt{f} m x \operatorname{Log}[c x^n] + 24 a b^2 \sqrt{f} m n x \operatorname{Log}[c x^n] - \right.
\end{aligned}$$

$$\begin{aligned}
& 36 b^3 \sqrt{f} m n^2 x \operatorname{Log}[c x^n] + 6 a^2 b \sqrt{e} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - 12 a b^2 \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + \\
& 12 b^3 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - 12 a b^2 \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] + 12 b^3 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 6 b^3 \sqrt{e} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - 6 a b^2 \sqrt{f} m x \operatorname{Log}[c x^n]^2 + 12 b^3 \sqrt{f} m n x \operatorname{Log}[c x^n]^2 + 6 a b^2 \sqrt{e} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 - \\
& 6 b^3 \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 - 6 b^3 \sqrt{e} m n \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - 2 b^3 \sqrt{f} m x \operatorname{Log}[c x^n]^3 + \\
& 2 b^3 \sqrt{e} m \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^3 + 3 i a^2 b \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i a b^2 \sqrt{e} m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i b^3 \sqrt{e} m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i a b^2 \sqrt{e} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 3 i b^3 \sqrt{e} m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& i b^3 \sqrt{e} m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i a b^2 \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{e} m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 3 i b^3 \sqrt{e} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 3 i b^3 \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 3 i a^2 b \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i a b^2 \sqrt{e} m n^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{e} m n^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i a b^2 \sqrt{e} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i b^3 \sqrt{e} m n^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - i b^3 \sqrt{e} m n^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 i a b^2 \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{e} m n^2 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i b^3 \sqrt{e} m n^2 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i b^3 \sqrt{e} m n \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& a^3 \sqrt{f} x \operatorname{Log}[d (e + f x^2)^m] - 3 a^2 b \sqrt{f} n x \operatorname{Log}[d (e + f x^2)^m] + 6 a b^2 \sqrt{f} n^2 x \operatorname{Log}[d (e + f x^2)^m] - 6 b^3 \sqrt{f} n^3 x \operatorname{Log}[d (e + f x^2)^m] + \\
& 3 a^2 b \sqrt{f} x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 6 a b^2 \sqrt{f} n x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + 6 b^3 \sqrt{f} n^2 x \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] + \\
& 3 a b^2 \sqrt{f} x \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 3 b^3 \sqrt{f} n x \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] + b^3 \sqrt{f} x \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] - \\
& 3 i b \sqrt{e} m n \left(a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i b \sqrt{e} m n \left(a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] +
\end{aligned}$$

$$\begin{aligned}
& 6 i a b^2 \sqrt{e} m n^2 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i b^3 \sqrt{e} m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i a b^2 \sqrt{e} m n^2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 i b^3 \sqrt{e} m n^2 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{e} m n^3 \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right]
\end{aligned}$$

Problem 113: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{x^2} dx$$

Optimal (type 4, 879 leaves, 26 steps):

$$\begin{aligned}
& \frac{12 b^3 \sqrt{f} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{e}} + \frac{12 b^2 \sqrt{f} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] (a + b \operatorname{Log}[c x^n])}{\sqrt{e}} + \frac{3 b \sqrt{f} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} + \\
& \frac{\sqrt{f} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \frac{3 b \sqrt{f} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \frac{\sqrt{f} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \\
& \frac{6 b^3 n^3 \operatorname{Log}[d (e + f x^2)^m]}{x} - \frac{6 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{x} - \frac{3 b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{x} - \\
& \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{x} - \frac{6 b^2 \sqrt{f} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \\
& \frac{3 b \sqrt{f} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} + \frac{6 b^2 \sqrt{f} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} + \\
& \frac{3 b \sqrt{f} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \frac{6 i b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{e}} + \frac{6 i b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{e}} + \\
& \frac{6 b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} + \frac{6 b^2 \sqrt{f} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \frac{6 b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \\
& \frac{6 b^2 \sqrt{f} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} - \frac{6 b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[4, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}} + \frac{6 b^3 \sqrt{f} m n^3 \operatorname{PolyLog}\left[4, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{\sqrt{-e}}
\end{aligned}$$

Result (type 4, 2166 leaves):

$$\begin{aligned}
& \frac{1}{\sqrt{e} x} \left(2 a^3 \sqrt{f} m x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 6 a^2 b \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 12 a b^2 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + 12 b^3 \sqrt{f} m n^3 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - \right. \\
& 6 a^2 b \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - 12 a b^2 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - 12 b^3 \sqrt{f} m n^3 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + \\
& 6 a b^2 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 + 6 b^3 \sqrt{f} m n^3 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 - 2 b^3 \sqrt{f} m n^3 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^3 + \\
& 6 a^2 b \sqrt{f} m x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + 12 a b^2 \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + 12 b^3 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - \\
& 12 a b^2 \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 12 b^3 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 6 b^3 \sqrt{f} m n^2 x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 6 a b^2 \sqrt{f} m x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 + 6 b^3 \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 - \\
& 6 b^3 \sqrt{f} m n x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + 2 b^3 \sqrt{f} m x \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^3 + 3 i a^2 b \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i a b^2 \sqrt{f} m n^2 x \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i a b^2 \sqrt{f} m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 3 i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i a b^2 \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i b^3 \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 3 i a^2 b \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 i a b^2 \sqrt{f} m n^2 x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 3 i a b^2 \sqrt{f} m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - i b^3 \sqrt{f} m n^3 x \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i a b^2 \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 3 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 3 i b^3 \sqrt{f} m n x \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - a^3 \sqrt{e} \operatorname{Log}[d (e + f x^2)^m] - 3 a^2 b \sqrt{e} n \operatorname{Log}[d (e + f x^2)^m] - 6 a b^2 \sqrt{e} n^2 \operatorname{Log}[d (e + f x^2)^m] -
\end{aligned}$$

$$\begin{aligned}
& 6 b^3 \sqrt{e} n^3 \operatorname{Log}[d (e + f x^2)^m] - 3 a^2 b \sqrt{e} \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 6 a b^2 \sqrt{e} n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - \\
& 6 b^3 \sqrt{e} n^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 3 a b^2 \sqrt{e} \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 3 b^3 \sqrt{e} n \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - \\
& b^3 \sqrt{e} \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] - 3 i b \sqrt{f} m n x \left(a^2 + 2 a b n + 2 b^2 n^2 + 2 b (a + b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 3 i b \sqrt{f} m n x \left(a^2 + 2 a b n + 2 b^2 n^2 + 2 b (a + b n) \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i a b^2 \sqrt{f} m n^2 x \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{f} m n^3 x \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 6 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i a b^2 \sqrt{f} m n^2 x \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{f} m n^3 x \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 6 i b^3 \sqrt{f} m n^2 x \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 \sqrt{f} m n^3 x \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 \sqrt{f} m n^3 x \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \Big)
\end{aligned}$$

Problem 114: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{x^4} dx$$

Optimal (type 4, 1007 leaves, 36 steps):

$$\begin{aligned}
& - \frac{160 b^3 f m n^3}{27 e x} - \frac{4 b^3 f^{3/2} m n^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right]}{27 e^{3/2}} - \frac{52 b^2 f m n^2 (a + b \operatorname{Log}[c x^n])}{9 e x} - \frac{4 b^2 f^{3/2} m n^2 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] (a + b \operatorname{Log}[c x^n])}{9 e^{3/2}} \\
& + \frac{8 b f m n (a + b \operatorname{Log}[c x^n])^2}{3 e x} - \frac{2 f m (a + b \operatorname{Log}[c x^n])^3}{3 e x} + \frac{b f^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} + \\
& - \frac{f^{3/2} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 - \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} - \frac{b f^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} - \frac{f^{3/2} m (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} \\
& - \frac{2 b^3 n^3 \operatorname{Log}[d (e + f x^2)^m]}{27 x^3} - \frac{2 b^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^2)^m]}{9 x^3} - \frac{b n (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^2)^m]}{3 x^3} \\
& - \frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^2)^m]}{3 x^3} - \frac{2 b^2 f^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} \\
& + \frac{b f^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}} + \frac{2 b^2 f^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} + \\
& + \frac{b f^{3/2} m n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}} + \frac{2 i b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right]}{9 e^{3/2}} - \frac{2 i b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right]}{9 e^{3/2}} + \\
& - \frac{2 b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} + \frac{2 b^2 f^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}} - \frac{2 b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{3 (-e)^{3/2}} \\
& - \frac{2 b^2 f^{3/2} m n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}} - \frac{2 b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[4, -\frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}} + \frac{2 b^3 f^{3/2} m n^3 \operatorname{PolyLog}\left[4, \frac{\sqrt{f} x}{\sqrt{e}}\right]}{(-e)^{3/2}}
\end{aligned}$$

Result (type 4, 2488 leaves):

$$\begin{aligned}
& \frac{1}{27 e^{3/2} x^3} \left(-18 a^3 \sqrt{e} f m x^2 - 72 a^2 b \sqrt{e} f m n x^2 - 156 a b^2 \sqrt{e} f m n^2 x^2 - 160 b^3 \sqrt{e} f m n^3 x^2 - \right. \\
& 18 a^3 f^{3/2} m x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 18 a^2 b f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 12 a b^2 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] - 4 b^3 f^{3/2} m n^3 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] + \\
& 54 a^2 b f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + 36 a b^2 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] + 12 b^3 f^{3/2} m n^3 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] - \\
& \left. 54 a b^2 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 - 18 b^3 f^{3/2} m n^3 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 + 18 b^3 f^{3/2} m n^3 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^3 - \right.
\end{aligned}$$

$$\begin{aligned}
& 54 a^2 b \sqrt{e} f m x^2 \operatorname{Log}[c x^n] - 144 a b^2 \sqrt{e} f m n x^2 \operatorname{Log}[c x^n] - 156 b^3 \sqrt{e} f m n^2 x^2 \operatorname{Log}[c x^n] - 54 a^2 b f^{3/2} m x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - \\
& 36 a b^2 f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] - 12 b^3 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n] + 108 a b^2 f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] + \\
& 36 b^3 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 54 b^3 f^{3/2} m n^2 x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] - 54 a b^2 \sqrt{e} f m x^2 \operatorname{Log}[c x^n]^2 - \\
& 72 b^3 \sqrt{e} f m n x^2 \operatorname{Log}[c x^n]^2 - 54 a b^2 f^{3/2} m x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 - 18 b^3 f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^2 + \\
& 54 b^3 f^{3/2} m n x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - 18 b^3 \sqrt{e} f m x^2 \operatorname{Log}[c x^n]^3 - 18 b^3 f^{3/2} m x^3 \operatorname{ArcTan}\left[\frac{\sqrt{f} x}{\sqrt{e}}\right] \operatorname{Log}[c x^n]^3 - \\
& 27 i a^2 b f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 18 i a b^2 f^{3/2} m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 6 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 27 i a b^2 f^{3/2} m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 9 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 9 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 54 i a b^2 f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 18 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 27 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 27 i b^3 f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 - \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 27 i a^2 b f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 18 i a b^2 f^{3/2} m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 6 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 27 i a b^2 f^{3/2} m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - 9 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 9 i b^3 f^{3/2} m n^3 x^3 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 54 i a b^2 f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 18 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 27 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 27 i b^3 f^{3/2} m n x^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 9 a^3 e^{3/2} \operatorname{Log}[d (e + f x^2)^m] - 9 a^2 b e^{3/2} n \operatorname{Log}[d (e + f x^2)^m] - 6 a b^2 e^{3/2} n^2 \operatorname{Log}[d (e + f x^2)^m] - 2 b^3 e^{3/2} n^3 \operatorname{Log}[d (e + f x^2)^m] - \\
& 27 a^2 b e^{3/2} \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 18 a b^2 e^{3/2} n \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - 6 b^3 e^{3/2} n^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^2)^m] - \\
& 27 a b^2 e^{3/2} \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 9 b^3 e^{3/2} n \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^2)^m] - 9 b^3 e^{3/2} \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^2)^m] + \\
& 3 i b f^{3/2} m n x^3 \left(9 a^2 + 6 a b n + 2 b^2 n^2 + 6 b (3 a + b n) \operatorname{Log}[c x^n] + 9 b^2 \operatorname{Log}[c x^n]^2\right) \operatorname{PolyLog}\left[2, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] -
\end{aligned}$$

$$\begin{aligned}
& 3 i b f^{3/2} m n x^3 \left(9 a^2 + 6 a b n + 2 b^2 n^2 + 6 b (3 a + b n) \operatorname{Log}[c x^n] + 9 b^2 \operatorname{Log}[c x^n]^2 \right) \operatorname{PolyLog}\left[2, \frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 54 i a b^2 f^{3/2} m n^2 x^3 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 18 i b^3 f^{3/2} m n^3 x^3 \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - \\
& 54 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] + 54 i a b^2 f^{3/2} m n^2 x^3 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 18 i b^3 f^{3/2} m n^3 x^3 \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + \\
& 54 i b^3 f^{3/2} m n^2 x^3 \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, \frac{i \sqrt{f} x}{\sqrt{e}}\right] + 54 i b^3 f^{3/2} m n^3 x^3 \operatorname{PolyLog}\left[4, -\frac{i \sqrt{f} x}{\sqrt{e}}\right] - 54 i b^3 f^{3/2} m n^3 x^3 \operatorname{PolyLog}\left[4, \frac{i \sqrt{f} x}{\sqrt{e}}\right] \Big)
\end{aligned}$$

Problem 125: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n])^2}{x} dx$$

Optimal (type 4, 145 leaves, 5 steps):

$$\frac{\operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n])^3}{3 b n} - \frac{\operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] (a + b \operatorname{Log}[c x^n])^3}{3 b n} - \\
2 (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right] + 8 b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right] - 16 b^2 n^2 \operatorname{PolyLog}\left[4, -\frac{f\sqrt{x}}{e}\right]$$

Result (type 4, 368 leaves):

$$\begin{aligned}
& a^2 \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x] - a^2 \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x] - a b n \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x]^2 + \\
& a b n \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x]^2 + \frac{1}{3} b^2 n^2 \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x]^3 - \frac{1}{3} b^2 n^2 \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x]^3 + \\
& 2 a b \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 2 a b \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - b^2 n \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + \\
& b^2 n \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + b^2 \operatorname{Log}[d(e + f\sqrt{x})] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - b^2 \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - \\
& 2 (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right] + 8 b n (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right] - 16 b^2 n^2 \operatorname{PolyLog}\left[4, -\frac{f\sqrt{x}}{e}\right]
\end{aligned}$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int x \operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n])^3 dx$$

Optimal (type 4, 907 leaves, 36 steps):

$$\begin{aligned} & -\frac{255 b^3 e^3 n^3 \sqrt{x}}{8 f^3} - \frac{9 a b^2 e^2 n^2 x}{4 f^2} + \frac{45 b^3 e^2 n^3 x}{16 f^2} - \frac{175 b^3 e n^3 x^{3/2}}{216 f} + \frac{3}{8} b^3 n^3 x^2 + \frac{3 b^3 e^4 n^3 \operatorname{Log}[e + f\sqrt{x}]}{8 f^4} - \frac{3}{8} b^3 n^3 x^2 \operatorname{Log}[d(e + f\sqrt{x})] + \\ & \frac{3 b^3 e^4 n^3 \operatorname{Log}[e + f\sqrt{x}] \operatorname{Log}\left[-\frac{f\sqrt{x}}{e}\right]}{2 f^4} - \frac{9 b^3 e^2 n^2 x \operatorname{Log}[c x^n]}{4 f^2} + \frac{63 b^2 e^3 n^2 \sqrt{x} (a + b \operatorname{Log}[c x^n])}{4 f^3} - \frac{3 b^2 e^2 n^2 x (a + b \operatorname{Log}[c x^n])}{8 f^2} + \\ & \frac{37 b^2 e n^2 x^{3/2} (a + b \operatorname{Log}[c x^n])}{36 f} - \frac{9}{16} b^2 n^2 x^2 (a + b \operatorname{Log}[c x^n]) - \frac{3 b^2 e^4 n^2 \operatorname{Log}[e + f\sqrt{x}] (a + b \operatorname{Log}[c x^n])}{4 f^4} + \\ & \frac{3}{4} b^2 n^2 x^2 \operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n]) - \frac{15 b e^3 n \sqrt{x} (a + b \operatorname{Log}[c x^n])^2}{4 f^3} + \frac{9 b e^2 n x (a + b \operatorname{Log}[c x^n])^2}{8 f^2} - \\ & \frac{7 b e n x^{3/2} (a + b \operatorname{Log}[c x^n])^2}{12 f} + \frac{3}{8} b n x^2 (a + b \operatorname{Log}[c x^n])^2 - \frac{3}{4} b n x^2 \operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n])^2 + \\ & \frac{3 b e^4 n \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] (a + b \operatorname{Log}[c x^n])^2}{4 f^4} + \frac{e^3 \sqrt{x} (a + b \operatorname{Log}[c x^n])^3}{2 f^3} - \frac{e^2 x (a + b \operatorname{Log}[c x^n])^3}{4 f^2} + \frac{e x^{3/2} (a + b \operatorname{Log}[c x^n])^3}{6 f} - \\ & \frac{1}{8} x^2 (a + b \operatorname{Log}[c x^n])^3 + \frac{1}{2} x^2 \operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[c x^n])^3 - \frac{e^4 \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] (a + b \operatorname{Log}[c x^n])^3}{2 f^4} + \\ & \frac{3 b^3 e^4 n^3 \operatorname{PolyLog}\left[2, 1 + \frac{f\sqrt{x}}{e}\right]}{2 f^4} + \frac{3 b^2 e^4 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right]}{f^4} - \frac{3 b e^4 n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right]}{f^4} - \\ & \frac{6 b^3 e^4 n^3 \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right]}{f^4} + \frac{12 b^2 e^4 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right]}{f^4} - \frac{24 b^3 e^4 n^3 \operatorname{PolyLog}\left[4, -\frac{f\sqrt{x}}{e}\right]}{f^4} \end{aligned}$$

Result (type 4, 1968 leaves):

$$\begin{aligned}
& \frac{1}{432 f^4} \left(216 a^3 e^3 f \sqrt{x} - 1620 a^2 b e^3 f n \sqrt{x} + 6804 a b^2 e^3 f n^2 \sqrt{x} - 13770 b^3 e^3 f n^3 \sqrt{x} - 108 a^3 e^2 f^2 x + 486 a^2 b e^2 f^2 n x - \right. \\
& 1134 a b^2 e^2 f^2 n^2 x + 1215 b^3 e^2 f^2 n^3 x + 72 a^3 e f^3 x^{3/2} - 252 a^2 b e f^3 n x^{3/2} + 444 a b^2 e f^3 n^2 x^{3/2} - 350 b^3 e f^3 n^3 x^{3/2} - 54 a^3 f^4 x^2 + \\
& 162 a^2 b f^4 n x^2 - 243 a b^2 f^4 n^2 x^2 + 162 b^3 f^4 n^3 x^2 - 216 a^3 e^4 \operatorname{Log}[e + f \sqrt{x}] + 324 a^2 b e^4 n \operatorname{Log}[e + f \sqrt{x}] - 324 a b^2 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] + \\
& 162 b^3 e^4 n^3 \operatorname{Log}[e + f \sqrt{x}] + 216 a^3 f^4 x^2 \operatorname{Log}[d(e + f \sqrt{x})] - 324 a^2 b f^4 n x^2 \operatorname{Log}[d(e + f \sqrt{x})] + 324 a b^2 f^4 n^2 x^2 \operatorname{Log}[d(e + f \sqrt{x})] - \\
& 162 b^3 f^4 n^3 x^2 \operatorname{Log}[d(e + f \sqrt{x})] + 648 a^2 b e^4 n \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] - 648 a b^2 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] + 324 b^3 e^4 n^3 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] - \\
& 648 a^2 b e^4 n \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] + 648 a b^2 e^4 n^2 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] - 324 b^3 e^4 n^3 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] - \\
& 648 a b^2 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x]^2 + 324 b^3 e^4 n^3 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x]^2 + 648 a b^2 e^4 n^2 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x]^2 - \\
& 324 b^3 e^4 n^3 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x]^2 + 216 b^3 e^4 n^3 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x]^3 - 216 b^3 e^4 n^3 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x]^3 + 648 a^2 b e^3 f \sqrt{x} \operatorname{Log}[c x^n] - \\
& 3240 a b^2 e^3 f n \sqrt{x} \operatorname{Log}[c x^n] + 6804 b^3 e^3 f n^2 \sqrt{x} \operatorname{Log}[c x^n] - 324 a^2 b e^2 f^2 x \operatorname{Log}[c x^n] + 972 a b^2 e^2 f^2 n x \operatorname{Log}[c x^n] - \\
& 1134 b^3 e^2 f^2 n^2 x \operatorname{Log}[c x^n] + 216 a^2 b e f^3 x^{3/2} \operatorname{Log}[c x^n] - 504 a b^2 e f^3 n x^{3/2} \operatorname{Log}[c x^n] + 444 b^3 e f^3 n^2 x^{3/2} \operatorname{Log}[c x^n] - 162 a^2 b f^4 x^2 \operatorname{Log}[c x^n] + \\
& 324 a b^2 f^4 n x^2 \operatorname{Log}[c x^n] - 243 b^3 f^4 n^2 x^2 \operatorname{Log}[c x^n] - 648 a^2 b e^4 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n] + 648 a b^2 e^4 n \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n] - \\
& 324 b^3 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n] + 648 a^2 b f^4 x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n] - 648 a b^2 f^4 n x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n] + \\
& 324 b^3 f^4 n^2 x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n] + 1296 a b^2 e^4 n \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 648 b^3 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] \operatorname{Log}[c x^n] - \\
& 1296 a b^2 e^4 n \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] + 648 b^3 e^4 n^2 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n] - 648 b^3 e^4 n^2 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + \\
& 648 b^3 e^4 n^2 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] + 648 a b^2 e^3 f \sqrt{x} \operatorname{Log}[c x^n]^2 - 1620 b^3 e^3 f n \sqrt{x} \operatorname{Log}[c x^n]^2 - 324 a b^2 e^2 f^2 x \operatorname{Log}[c x^n]^2 + \\
& 486 b^3 e^2 f^2 n x \operatorname{Log}[c x^n]^2 + 216 a b^2 e f^3 x^{3/2} \operatorname{Log}[c x^n]^2 - 252 b^3 e f^3 n x^{3/2} \operatorname{Log}[c x^n]^2 - 162 a b^2 f^4 x^2 \operatorname{Log}[c x^n]^2 + 162 b^3 f^4 n x^2 \operatorname{Log}[c x^n]^2 - \\
& 648 a b^2 e^4 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n]^2 + 324 b^3 e^4 n \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n]^2 + 648 a b^2 f^4 x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n]^2 - \\
& 324 b^3 f^4 n x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n]^2 + 648 b^3 e^4 n \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 - 648 b^3 e^4 n \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 + \\
& 216 b^3 e^3 f \sqrt{x} \operatorname{Log}[c x^n]^3 - 108 b^3 e^2 f^2 x \operatorname{Log}[c x^n]^3 + 72 b^3 e f^3 x^{3/2} \operatorname{Log}[c x^n]^3 - 54 b^3 f^4 x^2 \operatorname{Log}[c x^n]^3 - 216 b^3 e^4 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}[c x^n]^3 + \\
& 216 b^3 f^4 x^2 \operatorname{Log}[d(e + f \sqrt{x})] \operatorname{Log}[c x^n]^3 - 648 b e^4 n (2 a^2 - 2 a b n + b^2 n^2 - 2 b (-2 a + b n) \operatorname{Log}[c x^n] + 2 b^2 \operatorname{Log}[c x^n]^2) \operatorname{PolyLog}\left[2, -\frac{f \sqrt{x}}{e}\right] + \\
& 2592 b^2 e^4 n^2 (2 a - b n + 2 b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f \sqrt{x}}{e}\right] - 10368 b^3 e^4 n^3 \operatorname{PolyLog}\left[4, -\frac{f \sqrt{x}}{e}\right] \left. \right)
\end{aligned}$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Log}[d(e + f \sqrt{x})] (a + b \operatorname{Log}[c x^n])^3 dx$$

Optimal (type 4, 639 leaves, 30 steps):

$$\begin{aligned}
& -\frac{90 b^3 e n^3 \sqrt{x}}{f} - 6 a b^2 n^2 x + 12 b^3 n^3 x + \frac{6 b^3 e^2 n^3 \operatorname{Log}[e + f \sqrt{x}]}{f^2} - 6 b^3 n^3 x \operatorname{Log}[d(e + f \sqrt{x})] + \\
& \frac{12 b^3 e^2 n^3 \operatorname{Log}[e + f \sqrt{x}] \operatorname{Log}\left[-\frac{f \sqrt{x}}{e}\right]}{f^2} - 6 b^3 n^2 x \operatorname{Log}[c x^n] + \frac{42 b^2 e n^2 \sqrt{x} (a + b \operatorname{Log}[c x^n])}{f} - 3 b^2 n^2 x (a + b \operatorname{Log}[c x^n]) - \\
& \frac{6 b^2 e^2 n^2 \operatorname{Log}[e + f \sqrt{x}] (a + b \operatorname{Log}[c x^n])}{f^2} + 6 b^2 n^2 x \operatorname{Log}[d(e + f \sqrt{x})] (a + b \operatorname{Log}[c x^n]) - \frac{9 b e n \sqrt{x} (a + b \operatorname{Log}[c x^n])^2}{f} + \\
& 3 b n x (a + b \operatorname{Log}[c x^n])^2 - 3 b n x \operatorname{Log}[d(e + f \sqrt{x})] (a + b \operatorname{Log}[c x^n])^2 + \frac{3 b e^2 n \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] (a + b \operatorname{Log}[c x^n])^2}{f^2} + \\
& \frac{e \sqrt{x} (a + b \operatorname{Log}[c x^n])^3}{f} - \frac{1}{2} x (a + b \operatorname{Log}[c x^n])^3 + x \operatorname{Log}[d(e + f \sqrt{x})] (a + b \operatorname{Log}[c x^n])^3 - \frac{e^2 \operatorname{Log}\left[1 + \frac{f \sqrt{x}}{e}\right] (a + b \operatorname{Log}[c x^n])^3}{f^2} + \\
& \frac{12 b^3 e^2 n^3 \operatorname{PolyLog}\left[2, 1 + \frac{f \sqrt{x}}{e}\right]}{f^2} + \frac{12 b^2 e^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f \sqrt{x}}{e}\right]}{f^2} - \frac{6 b e^2 n (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f \sqrt{x}}{e}\right]}{f^2} - \\
& \frac{24 b^3 e^2 n^3 \operatorname{PolyLog}\left[3, -\frac{f \sqrt{x}}{e}\right]}{f^2} + \frac{24 b^2 e^2 n^2 (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f \sqrt{x}}{e}\right]}{f^2} - \frac{48 b^3 e^2 n^3 \operatorname{PolyLog}\left[4, -\frac{f \sqrt{x}}{e}\right]}{f^2}
\end{aligned}$$

Result (type 4, 1513 leaves):

$$\begin{aligned}
& \frac{1}{2} x \left(-a^3 + 3 a^2 b n - 6 a b^2 n^2 + 6 b^3 n^3 - 3 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 6 a b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - \right. \\
& \left. 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 3 a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + 3 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) + \\
& \frac{1}{f} e \sqrt{x} \left(a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 6 a b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + \right. \\
& \left. 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 3 a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - 3 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) - \\
& \frac{1}{f^2} e^2 \operatorname{Log}[e + f \sqrt{x}] \left(a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 6 a b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + \right. \\
& \left. 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 3 a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - 3 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) + \\
& x \operatorname{Log}[d(e + f \sqrt{x})] \left(a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 a^2 b n \operatorname{Log}[x] - 6 a b^2 n^2 \operatorname{Log}[x] + 6 b^3 n^3 \operatorname{Log}[x] + 3 a b^2 n^2 \operatorname{Log}[x]^2 - \right. \\
& \left. 3 b^3 n^3 \operatorname{Log}[x]^2 + b^3 n^3 \operatorname{Log}[x]^3 + 3 a^2 b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 6 a b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 6 b^3 n^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + \right. \\
& \left. 6 a b^2 n \operatorname{Log}[x] (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 6 b^3 n^2 \operatorname{Log}[x] (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + 3 b^3 n^2 \operatorname{Log}[x]^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + \right. \\
& \left. 3 a b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 - 3 b^3 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + 3 b^3 n \operatorname{Log}[x] (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 + b^3 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^3 \right) - \\
& 3 b f n \left(a^2 - 2 a b n + 2 b^2 n^2 + 2 a b (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) - 2 b^2 n (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n]) + b^2 (-n \operatorname{Log}[x] + \operatorname{Log}[c x^n])^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\left(-\frac{e\sqrt{x}}{f^2} + \frac{x}{2f} + \frac{e^2 \operatorname{Log}[e + f\sqrt{x}]}{f^3} \right) (-2 \operatorname{Log}[\sqrt{x}] + \operatorname{Log}[x]) + \right. \\
& \left. 2 \left(-\frac{e\sqrt{x}(-1 + \operatorname{Log}[\sqrt{x}])}{f^2} + \frac{-\frac{x}{4} + \frac{1}{2}x \operatorname{Log}[\sqrt{x}]}{f} + \frac{e^2 \left(\operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[\sqrt{x}] + \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right]\right)}{f^3} \right) \right) + \\
& 3b^2fn^2(-a + bn - b(-n \operatorname{Log}[x] + \operatorname{Log}[cx^n])) \left(\left(-\frac{e\sqrt{x}}{f^2} + \frac{x}{2f} + \frac{e^2 \operatorname{Log}[e + f\sqrt{x}]}{f^3} \right) (-2 \operatorname{Log}[\sqrt{x}] + \operatorname{Log}[x])^2 + \right. \\
& \left. 4(-2 \operatorname{Log}[\sqrt{x}] + \operatorname{Log}[x]) \left(-\frac{e\sqrt{x}(-1 + \operatorname{Log}[\sqrt{x}])}{f^2} + \frac{-\frac{x}{4} + \frac{1}{2}x \operatorname{Log}[\sqrt{x}]}{f} + \frac{e^2 \left(\operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[\sqrt{x}] + \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right]\right)}{f^3} \right) \right) + \\
& \frac{1}{f^3} 4 \left(-ef\sqrt{x} (2 - 2 \operatorname{Log}[\sqrt{x}] + \operatorname{Log}[\sqrt{x}]^2) + \frac{1}{4} f^2 x (1 - 2 \operatorname{Log}[\sqrt{x}] + 2 \operatorname{Log}[\sqrt{x}]^2) + \right. \\
& \left. e^2 \left(\operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \operatorname{Log}[\sqrt{x}]^2 + 2 \operatorname{Log}[\sqrt{x}] \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right] - 2 \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right] \right) \right) - \frac{1}{2(e + f\sqrt{x})} \\
& b^3fn^3 \left(1 + \frac{f\sqrt{x}}{e} \right) x^{3/2} \left(\frac{e \left(-2ef\sqrt{x} + f^2x + 2e^2 \operatorname{Log}\left[1 + \frac{f\sqrt{x}}{e}\right] \right) \operatorname{Log}[x]^3}{f^3x^{3/2}} - \frac{3e \operatorname{Log}[x]^2 \left(-4ef\sqrt{x} + f^2x - 4e^2 \operatorname{PolyLog}\left[2, -\frac{f\sqrt{x}}{e}\right] \right)}{f^3x^{3/2}} + \right. \\
& \left. \frac{6e \operatorname{Log}[x] \left(-8ef\sqrt{x} + f^2x - 8e^2 \operatorname{PolyLog}\left[3, -\frac{f\sqrt{x}}{e}\right] \right)}{f^3x^{3/2}} - \frac{6e \left(-16ef\sqrt{x} + f^2x - 16e^2 \operatorname{PolyLog}\left[4, -\frac{f\sqrt{x}}{e}\right] \right)}{f^3x^{3/2}} \right)
\end{aligned}$$

Problem 130: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[d(e + f\sqrt{x})] (a + b \operatorname{Log}[cx^n])^3}{x} dx$$

Optimal (type 4, 178 leaves, 6 steps):

$$\frac{\text{Log}[d(e + f\sqrt{x})] (a + b \text{Log}[c x^n])^4}{4 b n} - \frac{\text{Log}[1 + \frac{f\sqrt{x}}{e}] (a + b \text{Log}[c x^n])^4}{4 b n} - 2 (a + b \text{Log}[c x^n])^3 \text{PolyLog}[2, -\frac{f\sqrt{x}}{e}] +$$

$$12 b n (a + b \text{Log}[c x^n])^2 \text{PolyLog}[3, -\frac{f\sqrt{x}}{e}] - 48 b^2 n^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[4, -\frac{f\sqrt{x}}{e}] + 96 b^3 n^3 \text{PolyLog}[5, -\frac{f\sqrt{x}}{e}]$$

Result (type 4, 662 leaves):

$$\frac{1}{4} \left(4 a^3 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x] - 4 a^3 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x] - 6 a^2 b n \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^2 + 6 a^2 b n \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^2 +$$

$$4 a b^2 n^2 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^3 - 4 a b^2 n^2 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^3 - b^3 n^3 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^4 +$$

$$b^3 n^3 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^4 + 12 a^2 b \text{Log}[d(e + f\sqrt{x})] \text{Log}[x] \text{Log}[c x^n] - 12 a^2 b \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x] \text{Log}[c x^n] -$$

$$12 a b^2 n \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^2 \text{Log}[c x^n] + 12 a b^2 n \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^2 \text{Log}[c x^n] + 4 b^3 n^2 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^3 \text{Log}[c x^n] -$$

$$4 b^3 n^2 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^3 \text{Log}[c x^n] + 12 a b^2 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x] \text{Log}[c x^n]^2 - 12 a b^2 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x] \text{Log}[c x^n]^2 -$$

$$6 b^3 n \text{Log}[d(e + f\sqrt{x})] \text{Log}[x]^2 \text{Log}[c x^n]^2 + 6 b^3 n \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x]^2 \text{Log}[c x^n]^2 + 4 b^3 \text{Log}[d(e + f\sqrt{x})] \text{Log}[x] \text{Log}[c x^n]^3 -$$

$$4 b^3 \text{Log}[1 + \frac{f\sqrt{x}}{e}] \text{Log}[x] \text{Log}[c x^n]^3 - 8 (a + b \text{Log}[c x^n])^3 \text{PolyLog}[2, -\frac{f\sqrt{x}}{e}] + 48 b n (a + b \text{Log}[c x^n])^2 \text{PolyLog}[3, -\frac{f\sqrt{x}}{e}] -$$

$$192 a b^2 n^2 \text{PolyLog}[4, -\frac{f\sqrt{x}}{e}] - 192 b^3 n^2 \text{Log}[c x^n] \text{PolyLog}[4, -\frac{f\sqrt{x}}{e}] + 384 b^3 n^3 \text{PolyLog}[5, -\frac{f\sqrt{x}}{e}] \Big)$$

Problem 139: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \text{Log}[c x^n])^3 \text{Log}[d(e + f x^m)^r]}{x} dx$$

Optimal (type 4, 185 leaves, 6 steps):

$$\frac{(a + b \text{Log}[c x^n])^4 \text{Log}[d(e + f x^m)^r]}{4 b n} - \frac{r (a + b \text{Log}[c x^n])^4 \text{Log}[1 + \frac{f x^m}{e}]}{4 b n} - \frac{r (a + b \text{Log}[c x^n])^3 \text{PolyLog}[2, -\frac{f x^m}{e}]}{m} +$$

$$\frac{3 b n r (a + b \text{Log}[c x^n])^2 \text{PolyLog}[3, -\frac{f x^m}{e}]}{m^2} - \frac{6 b^2 n^2 r (a + b \text{Log}[c x^n]) \text{PolyLog}[4, -\frac{f x^m}{e}]}{m^3} + \frac{6 b^3 n^3 r \text{PolyLog}[5, -\frac{f x^m}{e}]}{m^4}$$

Result (type 4, 1395 leaves):

$$\begin{aligned}
& -\frac{1}{2} a^2 b m n r \operatorname{Log}[x]^3 + \frac{3}{4} a b^2 m n^2 r \operatorname{Log}[x]^4 - \frac{3}{10} b^3 m n^3 r \operatorname{Log}[x]^5 - a b^2 m n r \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] + \frac{3}{4} b^3 m n^2 r \operatorname{Log}[x]^4 \operatorname{Log}[c x^n] - \\
& \frac{1}{2} b^3 m n r \operatorname{Log}[x]^3 \operatorname{Log}[c x^n]^2 - \frac{3}{2} a^2 b n r \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] + 2 a b^2 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - \frac{3}{4} b^3 n^3 r \operatorname{Log}[x]^4 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - \\
& 3 a b^2 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] + 2 b^3 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - \frac{3}{2} b^3 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - \\
& a^3 r \operatorname{Log}[x] \operatorname{Log}[e + f x^m] + 3 a^2 b n r \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^m] - 3 a b^2 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}[e + f x^m] + b^3 n^3 r \operatorname{Log}[x]^4 \operatorname{Log}[e + f x^m] + \\
& \frac{a^3 r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - \frac{3 a^2 b n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} + \frac{3 a b^2 n^2 r \operatorname{Log}[x]^2 \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - \\
& \frac{b^3 n^3 r \operatorname{Log}[x]^3 \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - 3 a^2 b r \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + 6 a b^2 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] - \\
& 3 b^3 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + \frac{3 a^2 b r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} - \frac{6 a b^2 n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} + \\
& \frac{3 b^3 n^2 r \operatorname{Log}[x]^2 \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} - 3 a b^2 r \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m] + 3 b^3 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m] + \\
& \frac{3 a b^2 r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m]}{m} - \frac{3 b^3 n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m]}{m} - b^3 r \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x^m] + \\
& \frac{b^3 r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n]^3 \operatorname{Log}[e + f x^m]}{m} + a^3 \operatorname{Log}[x] \operatorname{Log}[d (e + f x^m)^r] - \frac{3}{2} a^2 b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x^m)^r] + a b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d (e + f x^m)^r] - \\
& \frac{1}{4} b^3 n^3 \operatorname{Log}[x]^4 \operatorname{Log}[d (e + f x^m)^r] + 3 a^2 b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] - 3 a b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] + \\
& b^3 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] + 3 a b^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^m)^r] - \frac{3}{2} b^3 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^m)^r] + \\
& b^3 \operatorname{Log}[x] \operatorname{Log}[c x^n]^3 \operatorname{Log}[d (e + f x^m)^r] + \frac{b n r \operatorname{Log}[x] \left(b^2 n^2 \operatorname{Log}[x]^2 - 3 b n \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) + 3 (a + b \operatorname{Log}[c x^n])^2 \right) \operatorname{PolyLog}\left[2, -\frac{e x^{-m}}{f}\right]}{m} + \\
& \frac{r (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^3 \operatorname{PolyLog}\left[2, 1 + \frac{f x^m}{e}\right]}{m} + \frac{3 a^2 b n r \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2} + \frac{6 a b^2 n r \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2} + \\
& \frac{3 b^3 n r \operatorname{Log}[c x^n]^2 \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2} + \frac{6 a b^2 n^2 r \operatorname{PolyLog}\left[4, -\frac{e x^{-m}}{f}\right]}{m^3} + \frac{6 b^3 n^2 r \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[4, -\frac{e x^{-m}}{f}\right]}{m^3} + \frac{6 b^3 n^3 r \operatorname{PolyLog}\left[5, -\frac{e x^{-m}}{f}\right]}{m^4}
\end{aligned}$$

Problem 140: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^m)^r]}{x} dx$$

Optimal (type 4, 150 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}[d (e + f x^m)^r]}{3 b n} - \frac{r (a + b \operatorname{Log}[c x^n])^3 \operatorname{Log}\left[1 + \frac{f x^m}{e}\right]}{3 b n} -$$

$$\frac{r (a + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, -\frac{f x^m}{e}\right]}{m} + \frac{2 b n r (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[3, -\frac{f x^m}{e}\right]}{m^2} - \frac{2 b^2 n^2 r \operatorname{PolyLog}\left[4, -\frac{f x^m}{e}\right]}{m^3}$$

Result (type 4, 741 leaves):

$$-\frac{1}{3} a b m n r \operatorname{Log}[x]^3 + \frac{1}{4} b^2 m n^2 r \operatorname{Log}[x]^4 - \frac{1}{3} b^2 m n r \operatorname{Log}[x]^3 \operatorname{Log}[c x^n] - a b n r \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] + \frac{2}{3} b^2 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] -$$

$$b^2 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - a^2 r \operatorname{Log}[x] \operatorname{Log}[e + f x^m] + 2 a b n r \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^m] - b^2 n^2 r \operatorname{Log}[x]^3 \operatorname{Log}[e + f x^m] +$$

$$\frac{a^2 r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - \frac{2 a b n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} + \frac{b^2 n^2 r \operatorname{Log}[x]^2 \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} -$$

$$2 a b r \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + 2 b^2 n r \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + \frac{2 a b r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} -$$

$$\frac{2 b^2 n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} - b^2 r \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m] + \frac{b^2 r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n]^2 \operatorname{Log}[e + f x^m]}{m} +$$

$$a^2 \operatorname{Log}[x] \operatorname{Log}[d (e + f x^m)^r] - a b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x^m)^r] + \frac{1}{3} b^2 n^2 \operatorname{Log}[x]^3 \operatorname{Log}[d (e + f x^m)^r] +$$

$$2 a b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] - b^2 n \operatorname{Log}[x]^2 \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] + b^2 \operatorname{Log}[x] \operatorname{Log}[c x^n]^2 \operatorname{Log}[d (e + f x^m)^r] +$$

$$\frac{b n r \operatorname{Log}[x] (-b n \operatorname{Log}[x] + 2 (a + b \operatorname{Log}[c x^n])) \operatorname{PolyLog}\left[2, -\frac{e x^{-m}}{f}\right]}{m} + \frac{r (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n])^2 \operatorname{PolyLog}\left[2, 1 + \frac{f x^m}{e}\right]}{m} +$$

$$\frac{2 a b n r \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2} + \frac{2 b^2 n r \operatorname{Log}[c x^n] \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2} + \frac{2 b^2 n^2 r \operatorname{PolyLog}\left[4, -\frac{e x^{-m}}{f}\right]}{m^3}$$

Problem 141: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^m)^r]}{x} dx$$

Optimal (type 4, 114 leaves, 4 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^m)^r]}{2 b n} - \frac{r (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x^m}{e}\right]}{2 b n} - \frac{r (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x^m}{e}\right]}{m} + \frac{b n r \operatorname{PolyLog}\left[3, -\frac{f x^m}{e}\right]}{m^2}$$

Result (type 4, 304 leaves):

$$\begin{aligned}
& -\frac{1}{6} b m n r \operatorname{Log}[x]^3 - \frac{1}{2} b n r \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - a r \operatorname{Log}[x] \operatorname{Log}[e + f x^m] + b n r \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^m] + \frac{a r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - \\
& \frac{b n r \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - b r \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + \frac{b r \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} + \\
& a \operatorname{Log}[x] \operatorname{Log}[d (e + f x^m)^r] - \frac{1}{2} b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x^m)^r] + b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^r] + \\
& \frac{b n r \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{e x^{-m}}{f}\right]}{m} + \frac{r (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, 1 + \frac{f x^m}{e}\right]}{m} + \frac{b n r \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2}
\end{aligned}$$

Problem 147: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[d (e + f x^m)^k]}{x} dx$$

Optimal (type 4, 114 leaves, 4 steps):

$$\frac{(a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}[d (e + f x^m)^k]}{2 b n} - \frac{k (a + b \operatorname{Log}[c x^n])^2 \operatorname{Log}\left[1 + \frac{f x^m}{e}\right]}{2 b n} - \frac{k (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, -\frac{f x^m}{e}\right]}{m} + \frac{b k n \operatorname{PolyLog}\left[3, -\frac{f x^m}{e}\right]}{m^2}$$

Result (type 4, 304 leaves):

$$\begin{aligned}
& -\frac{1}{6} b k m n \operatorname{Log}[x]^3 - \frac{1}{2} b k n \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{e x^{-m}}{f}\right] - a k \operatorname{Log}[x] \operatorname{Log}[e + f x^m] + b k n \operatorname{Log}[x]^2 \operatorname{Log}[e + f x^m] + \frac{a k \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - \\
& \frac{b k n \operatorname{Log}[x] \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[e + f x^m]}{m} - b k \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m] + \frac{b k \operatorname{Log}\left[-\frac{f x^m}{e}\right] \operatorname{Log}[c x^n] \operatorname{Log}[e + f x^m]}{m} + \\
& a \operatorname{Log}[x] \operatorname{Log}[d (e + f x^m)^k] - \frac{1}{2} b n \operatorname{Log}[x]^2 \operatorname{Log}[d (e + f x^m)^k] + b \operatorname{Log}[x] \operatorname{Log}[c x^n] \operatorname{Log}[d (e + f x^m)^k] + \\
& \frac{b k n \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{e x^{-m}}{f}\right]}{m} + \frac{k (a - b n \operatorname{Log}[x] + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}\left[2, 1 + \frac{f x^m}{e}\right]}{m} + \frac{b k n \operatorname{PolyLog}\left[3, -\frac{e x^{-m}}{f}\right]}{m^2}
\end{aligned}$$

Problem 166: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c x^n])^2 (d + e \operatorname{Log}[f x^r])}{x} dx$$

Optimal (type 3, 57 leaves, 4 steps):

$$-\frac{e r (a + b \operatorname{Log}[c x^n])^4}{12 b^2 n^2} + \frac{(a + b \operatorname{Log}[c x^n])^3 (d + e \operatorname{Log}[f x^r])}{3 b n}$$

Result (type 3, 129 leaves):

$$\frac{1}{12} \text{Log}[x] \left(-3 b^2 e n^2 r \text{Log}[x]^3 + 12 (a + b \text{Log}[c x^n])^2 (d + e \text{Log}[f x^r]) + \right. \\ \left. 4 b n \text{Log}[x]^2 (b d n + 2 a e r + 2 b e r \text{Log}[c x^n] + b e n \text{Log}[f x^r]) - 6 \text{Log}[x] (a + b \text{Log}[c x^n]) (2 b d n + a e r + b e r \text{Log}[c x^n] + 2 b e n \text{Log}[f x^r]) \right)$$

Problem 199: Unable to integrate problem.

$$\int \frac{(a + b \text{Log}[c x^n])^3 \text{PolyLog}[k, e x^q]}{x} dx$$

Optimal (type 4, 104 leaves, 4 steps):

$$\frac{(a + b \text{Log}[c x^n])^3 \text{PolyLog}[1 + k, e x^q]}{q} - \frac{3 b n (a + b \text{Log}[c x^n])^2 \text{PolyLog}[2 + k, e x^q]}{q^2} + \\ \frac{6 b^2 n^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[3 + k, e x^q]}{q^3} - \frac{6 b^3 n^3 \text{PolyLog}[4 + k, e x^q]}{q^4}$$

Result (type 8, 25 leaves):

$$\int \frac{(a + b \text{Log}[c x^n])^3 \text{PolyLog}[k, e x^q]}{x} dx$$

Problem 200: Unable to integrate problem.

$$\int \frac{(a + b \text{Log}[c x^n])^2 \text{PolyLog}[k, e x^q]}{x} dx$$

Optimal (type 4, 72 leaves, 3 steps):

$$\frac{(a + b \text{Log}[c x^n])^2 \text{PolyLog}[1 + k, e x^q]}{q} - \frac{2 b n (a + b \text{Log}[c x^n]) \text{PolyLog}[2 + k, e x^q]}{q^2} + \frac{2 b^2 n^2 \text{PolyLog}[3 + k, e x^q]}{q^3}$$

Result (type 8, 25 leaves):

$$\int \frac{(a + b \text{Log}[c x^n])^2 \text{PolyLog}[k, e x^q]}{x} dx$$

Problem 201: Unable to integrate problem.

$$\int \frac{(a + b \text{Log}[c x^n]) \text{PolyLog}[k, e x^q]}{x} dx$$

Optimal (type 4, 40 leaves, 2 steps):

$$\frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[1 + k, e x^q]}{q} - \frac{b n \operatorname{PolyLog}[2 + k, e x^q]}{q^2}$$

Result (type 8, 23 leaves):

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[k, e x^q]}{x} dx$$

Problem 205: Unable to integrate problem.

$$\int \frac{\operatorname{Log}[x] \operatorname{PolyLog}[n, a x]}{x} dx$$

Optimal (type 4, 20 leaves, 2 steps):

$$\operatorname{Log}[x] \operatorname{PolyLog}[1 + n, a x] - \operatorname{PolyLog}[2 + n, a x]$$

Result (type 8, 13 leaves):

$$\int \frac{\operatorname{Log}[x] \operatorname{PolyLog}[n, a x]}{x} dx$$

Problem 206: Unable to integrate problem.

$$\int \frac{\operatorname{Log}[x]^2 \operatorname{PolyLog}[n, a x]}{x} dx$$

Optimal (type 4, 33 leaves, 3 steps):

$$\operatorname{Log}[x]^2 \operatorname{PolyLog}[1 + n, a x] - 2 \operatorname{Log}[x] \operatorname{PolyLog}[2 + n, a x] + 2 \operatorname{PolyLog}[3 + n, a x]$$

Result (type 8, 15 leaves):

$$\int \frac{\operatorname{Log}[x]^2 \operatorname{PolyLog}[n, a x]}{x} dx$$

Problem 207: Unable to integrate problem.

$$\int \left(\frac{q \operatorname{PolyLog}[-1 + k, e x^q]}{b n x (a + b \operatorname{Log}[c x^n])} - \frac{\operatorname{PolyLog}[k, e x^q]}{x (a + b \operatorname{Log}[c x^n])^2} \right) dx$$

Optimal (type 4, 26 leaves, 2 steps):

$$\frac{\text{PolyLog}[k, e x^q]}{b n (a + b \text{Log}[c x^n])}$$

Result (type 8, 59 leaves):

$$\int \left(\frac{q \text{PolyLog}[-1 + k, e x^q]}{b n x (a + b \text{Log}[c x^n])} - \frac{\text{PolyLog}[k, e x^q]}{x (a + b \text{Log}[c x^n])^2} \right) dx$$

Problem 214: Unable to integrate problem.

$$\int x^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] dx$$

Optimal (type 4, 253 leaves, 15 steps):

$$\begin{aligned} & -\frac{2 b n x}{27 e^2} - \frac{b n x^2}{36 e} - \frac{4}{243} b n x^3 + \frac{x (a + b \text{Log}[c x^n])}{27 e^2} + \frac{x^2 (a + b \text{Log}[c x^n])}{54 e} + \frac{1}{81} x^3 (a + b \text{Log}[c x^n]) - \frac{b n \text{Log}[1 - e x]}{27 e^3} + \\ & \frac{1}{27} b n x^3 \text{Log}[1 - e x] + \frac{(a + b \text{Log}[c x^n]) \text{Log}[1 - e x]}{27 e^3} - \frac{1}{27} x^3 (a + b \text{Log}[c x^n]) \text{Log}[1 - e x] + \frac{b n \text{PolyLog}[2, e x]}{27 e^3} + \\ & \frac{2}{27} b n x^3 \text{PolyLog}[2, e x] - \frac{1}{9} x^3 (a + b \text{Log}[c x^n]) \text{PolyLog}[2, e x] - \frac{1}{9} b n x^3 \text{PolyLog}[3, e x] + \frac{1}{3} x^3 (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] \end{aligned}$$

Result (type 8, 21 leaves):

$$\int x^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] dx$$

Problem 215: Unable to integrate problem.

$$\int x (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] dx$$

Optimal (type 4, 221 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 b n x}{16 e} - \frac{1}{8} b n x^2 + \frac{x (a + b \text{Log}[c x^n])}{8 e} + \frac{1}{16} x^2 (a + b \text{Log}[c x^n]) - \frac{3 b n \text{Log}[1 - e x]}{16 e^2} + \frac{3}{16} b n x^2 \text{Log}[1 - e x] + \\ & \frac{(a + b \text{Log}[c x^n]) \text{Log}[1 - e x]}{8 e^2} - \frac{1}{8} x^2 (a + b \text{Log}[c x^n]) \text{Log}[1 - e x] + \frac{b n \text{PolyLog}[2, e x]}{8 e^2} + \frac{1}{4} b n x^2 \text{PolyLog}[2, e x] - \\ & \frac{1}{4} x^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[2, e x] - \frac{1}{4} b n x^2 \text{PolyLog}[3, e x] + \frac{1}{2} x^2 (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] \end{aligned}$$

Result (type 8, 19 leaves):

$$\int x (a + b \text{Log}[c x^n]) \text{PolyLog}[3, e x] dx$$

Problem 216: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x] dx$$

Optimal (type 4, 131 leaves, 14 steps):

$$-4 b n x + x (a + b \operatorname{Log}[c x^n]) - \frac{3 b n (1 - e x) \operatorname{Log}[1 - e x]}{e} + \frac{(1 - e x) (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 - e x]}{e} + \frac{b n \operatorname{PolyLog}[2, e x]}{e} + 2 b n x \operatorname{PolyLog}[2, e x] - x (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, e x] - b n x \operatorname{PolyLog}[3, e x] + x (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]$$

Result (type 8, 18 leaves):

$$\int (a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x] dx$$

Problem 217: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x} dx$$

Optimal (type 4, 26 leaves, 2 steps):

$$(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[4, e x] - b n \operatorname{PolyLog}[5, e x]$$

Result (type 8, 21 leaves):

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x} dx$$

Problem 218: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x^2} dx$$

Optimal (type 4, 174 leaves, 19 steps):

$$3 b e n \operatorname{Log}[x] - \frac{1}{2} b e n \operatorname{Log}[x]^2 + e \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) - 3 b e n \operatorname{Log}[1 - e x] + \frac{3 b n \operatorname{Log}[1 - e x]}{x} - e (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 - e x] + \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 - e x]}{x} - b e n \operatorname{PolyLog}[2, e x] - \frac{2 b n \operatorname{PolyLog}[2, e x]}{x} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, e x]}{x} - \frac{b n \operatorname{PolyLog}[3, e x]}{x} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x}$$

Result (type 8, 21 leaves):

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x^2} dx$$

Problem 219: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x^3} dx$$

Optimal (type 4, 238 leaves, 16 steps):

$$\begin{aligned} & -\frac{5 b e n}{16 x} + \frac{3}{16} b e^2 n \operatorname{Log}[x] - \frac{1}{16} b e^2 n \operatorname{Log}[x]^2 - \frac{e (a + b \operatorname{Log}[c x^n])}{8 x} + \frac{1}{8} e^2 \operatorname{Log}[x] (a + b \operatorname{Log}[c x^n]) - \frac{3}{16} b e^2 n \operatorname{Log}[1 - e x] + \\ & \frac{3 b n \operatorname{Log}[1 - e x]}{16 x^2} - \frac{1}{8} e^2 (a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 - e x] + \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{Log}[1 - e x]}{8 x^2} - \frac{1}{8} b e^2 n \operatorname{PolyLog}[2, e x] - \\ & \frac{b n \operatorname{PolyLog}[2, e x]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[2, e x]}{4 x^2} - \frac{b n \operatorname{PolyLog}[3, e x]}{4 x^2} - \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{2 x^2} \end{aligned}$$

Result (type 8, 21 leaves):

$$\int \frac{(a + b \operatorname{Log}[c x^n]) \operatorname{PolyLog}[3, e x]}{x^3} dx$$

Test results for the 314 problems in "3.2.1 (f+g x)^m (A+B log(e ((a+b x) over (c+d x))^n))^p.m"

Problem 10: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 396 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (b c - a d) g^4 n (a + b x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{10 b d} + \\
& \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{5 b} + \frac{B (b c - a d)^2 g^4 n (a + b x)^3 \left(4 A + B n + 4 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b d^2} - \\
& \frac{B (b c - a d)^3 g^4 n (a + b x)^2 \left(12 A + 7 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b d^3} + \frac{B (b c - a d)^4 g^4 n (a + b x) \left(12 A + 13 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b d^4} + \\
& \frac{B (b c - a d)^5 g^4 n \left(12 A + 25 B n + 12 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{30 b d^5} + \frac{2 B^2 (b c - a d)^5 g^4 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{5 b d^5}
\end{aligned}$$

Result (type 4, 3194 leaves):

$$\begin{aligned}
g^4 \left(- \frac{8 a^5 B^2 n^2}{5 b} + \frac{2 b^4 B^2 c^5 n^2}{5 d^5} - \frac{12 a b^3 B^2 c^4 n^2}{5 d^4} + \frac{6 a^2 b^2 B^2 c^3 n^2}{d^3} - \frac{8 a^3 b B^2 c^2 n^2}{d^2} + \frac{28 a^4 B^2 c n^2}{5 d} + a^4 A^2 x + \frac{8}{5} a^4 A B n x + \frac{2 A b^4 B c^4 n x}{5 d^4} - \frac{2 a A b^3 B c^3 n x}{d^3} + \right. \\
\frac{4 a^2 A b^2 B c^2 n x}{d^2} - \frac{4 a^3 A b B c n x}{d} + \frac{23}{30} a^4 B^2 n^2 x + \frac{13 b^4 B^2 c^4 n^2 x}{30 d^4} - \frac{59 a b^3 B^2 c^3 n^2 x}{30 d^3} + \frac{17 a^2 b^2 B^2 c^2 n^2 x}{5 d^2} - \frac{79 a^3 b B^2 c n^2 x}{30 d} + 2 a^3 A^2 b x^2 + \\
\frac{6}{5} a^3 A b B n x^2 - \frac{A b^4 B c^3 n x^2}{5 d^3} + \frac{a A b^3 B c^2 n x^2}{d^2} - \frac{2 a^2 A b^2 B c n x^2}{d} + \frac{13}{60} a^3 b B^2 n^2 x^2 - \frac{7 b^4 B^2 c^3 n^2 x^2}{60 d^3} + \frac{9 a b^3 B^2 c^2 n^2 x^2}{20 d^2} - \frac{11 a^2 b^2 B^2 c n^2 x^2}{20 d} + \\
2 a^2 A^2 b^2 x^3 + \frac{8}{15} a^2 A b^2 B n x^3 + \frac{2 A b^4 B c^2 n x^3}{15 d^2} - \frac{2 a A b^3 B c n x^3}{3 d} + \frac{1}{30} a^2 b^2 B^2 n^2 x^3 + \frac{b^4 B^2 c^2 n^2 x^3}{30 d^2} - \frac{a b^3 B^2 c n^2 x^3}{15 d} + a A^2 b^3 x^4 + \frac{1}{10} a A b^3 B n x^4 - \\
\frac{A b^4 B c n x^4}{10 d} + \frac{1}{5} A^2 b^4 x^5 + \frac{8 a^5 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{5 b} + \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{5 d^4} - \frac{2 a^2 b^2 B^2 c^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^3} + \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^2} - \\
\frac{4 a^4 B^2 c n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d} + \frac{a^5 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{5 b} - \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^3} + \\
\frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^2} - \frac{8 a^4 B^2 c n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{5 d} + \frac{b^4 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{5 d^5} - \frac{a b^3 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^4} + \frac{2 a^2 b^2 B^2 c^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^3} - \\
\frac{2 a^3 b B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^2} + \frac{a^4 B^2 c n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d} + \frac{2 a^5 A B n \operatorname{Log} [a + b x]}{5 b} - \frac{23 a^5 B^2 n^2 \operatorname{Log} [a + b x]}{30 b} + \frac{a^2 b^2 B^2 c^3 n^2 \operatorname{Log} [a + b x]}{5 d^3} - \\
\frac{13 a^3 b B^2 c^2 n^2 \operatorname{Log} [a + b x]}{15 d^2} + \frac{43 a^4 B^2 c n^2 \operatorname{Log} [a + b x]}{30 d} - \frac{2 a^5 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x]}{5 b} + \frac{2 a^5 B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x]}{5 b} - \\
\frac{2 a^5 B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right]}{5 b} + 2 a^4 A B x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \frac{8}{5} a^4 B^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \frac{2 b^4 B^2 c^4 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{5 d^4} - \\
\frac{2 a b^3 B^2 c^3 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{d^3} + \frac{4 a^2 b^2 B^2 c^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{d^2} - \frac{4 a^3 b B^2 c n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{d} + 4 a^3 A b B x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] +
\end{aligned}$$

$$\begin{aligned}
& \frac{6}{5} a^3 b B^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \frac{b^4 B^2 c^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{5 d^3} + \frac{a b^3 B^2 c^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{d^2} - \frac{2 a^2 b^2 B^2 c n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{d} + \\
& 4 a^2 A b^2 B x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \frac{8}{15} a^2 b^2 B^2 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \frac{2 b^4 B^2 c^2 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{15 d^2} - \frac{2 a b^3 B^2 c n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{3 d} + \\
& 2 a A b^3 B x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \frac{1}{10} a b^3 B^2 n x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \frac{b^4 B^2 c n x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{10 d} + \frac{2}{5} A b^4 B x^5 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& \frac{2 a^5 B^2 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{5 b} + a^4 B^2 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 2 a^3 b B^2 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 2 a^2 b^2 B^2 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& a b^3 B^2 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \frac{1}{5} b^4 B^2 x^5 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - \frac{2 A b^4 B c^5 n \operatorname{Log}[c+dx]}{5 d^5} + \frac{2 a A b^3 B c^4 n \operatorname{Log}[c+dx]}{d^4} - \\
& \frac{4 a^2 A b^2 B c^3 n \operatorname{Log}[c+dx]}{d^3} + \frac{4 a^3 A b B c^2 n \operatorname{Log}[c+dx]}{d^2} - \frac{2 a^4 A B c n \operatorname{Log}[c+dx]}{d} - \frac{13 b^4 B^2 c^5 n^2 \operatorname{Log}[c+dx]}{30 d^5} + \frac{53 a b^3 B^2 c^4 n^2 \operatorname{Log}[c+dx]}{30 d^4} - \\
& \frac{38 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}[c+dx]}{15 d^3} + \frac{6 a^3 b B^2 c^2 n^2 \operatorname{Log}[c+dx]}{5 d^2} + \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{5 d^5} - \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^4} + \\
& \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^3} - \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^2} + \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d} - \\
& \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{5 d^5} + \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^3} + \\
& \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^2} - \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d} - \frac{2 b^4 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx]}{5 d^5} + \\
& \frac{2 a b^3 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx]}{d^3} + \frac{4 a^3 b B^2 c^2 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx]}{d^2} - \\
& \frac{2 a^4 B^2 c n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx]}{d} - \frac{2 b^4 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^4} - \\
& \frac{4 a^2 b^2 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^3} + \frac{4 a^3 b B^2 c^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^2} - \frac{2 a^4 B^2 c n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d} - \\
& \frac{2 B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{5 d^5} - \frac{2 a^5 B^2 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{5 b}
\end{aligned}$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 335 leaves, 7 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g^3 n (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 b d} + \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{4 b} + \\ & \frac{B (b c - a d)^2 g^3 n (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{12 b d^2} - \frac{B (b c - a d)^3 g^3 n (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{12 b d^3} - \\ & \frac{B (b c - a d)^4 g^3 n \left(6 A + 11 B n + 6 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{12 b d^4} - \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{2 b d^4} \end{aligned}$$

Result (type 4, 2348 leaves):

$$\begin{aligned}
& \frac{1}{12 b d^4} g^3 \left(-6 b^4 B^2 c^4 n^2 + 30 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 54 a^3 b B^2 c d^3 n^2 - 18 a^4 B^2 d^4 n^2 + 12 a^3 A^2 b d^4 x - 6 A b^4 B c^3 d n x + 24 a A b^3 B c^2 d^2 n x - \right. \\
& 36 a^2 A b^2 B c d^3 n x + 18 a^3 A b B d^4 n x - 5 b^4 B^2 c^3 d n^2 x + 17 a b^3 B^2 c^2 d^2 n^2 x - 19 a^2 b^2 B^2 c d^3 n^2 x + 7 a^3 b B^2 d^4 n^2 x + 18 a^2 A^2 b^2 d^4 x^2 + \\
& 3 A b^4 B c^2 d^2 n x^2 - 12 a A b^3 B c d^3 n x^2 + 9 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + 12 a A^2 b^3 d^4 x^3 - \\
& 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 6 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 24 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 36 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 18 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 3 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 18 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 12 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^4 A B d^4 n \operatorname{Log}[a + b x] - 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] + 10 a^3 b B^2 c d^3 n^2 \operatorname{Log}[a + b x] - \\
& 7 a^4 B^2 d^4 n^2 \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 24 a^3 A b B d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 18 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 3 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 12 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 9 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a A b^3 B d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^4 B^2 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 12 a^3 b B^2 d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 6 A b^4 B c^4 n \operatorname{Log}[c + d x] - 24 a A b^3 B c^3 d n \operatorname{Log}[c + d x] + 36 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[c + d x] - 24 a^3 A b B c d^3 n \operatorname{Log}[c + d x] + \\
& 5 b^4 B^2 c^4 n^2 \operatorname{Log}[c + d x] - 14 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c + d x] + 9 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 24 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + \\
& 36 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 24 a^3 b B^2 c d^3 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& \left. 6 b B^2 c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 6 a^4 B^2 d^4 n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)
\end{aligned}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 274 leaves, 6 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g^2 n (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b d} + \\ & \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{3 b} + \frac{B (b c - a d)^2 g^2 n (a + b x) \left(2 A + B n + 2 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b d^2} + \\ & \frac{B (b c - a d)^3 g^2 n \left(2 A + 3 B n + 2 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{3 b d^3} + \frac{2 B^2 (b c - a d)^3 g^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned}
& g^2 \left(a^2 x \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + a b x^2 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + \\
& \frac{1}{3} b^2 x^3 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + 2 a^2 B n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right] + \frac{(b c - a d) (a d \text{Log} [a + b x] - b c \text{Log} [c + d x])}{b^2 c d - a b d^2} \right) + 2 b^2 B n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]}{6 b^3 d^3} \right) + \\
& 4 a b B n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{1}{2} (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \text{Log} [a + b x]}{b^2 (b c - a d)} - \frac{c^2 \text{Log} [c + d x]}{d^2 (b c - a d)} \right) \right) + \\
& a^2 B^2 n^2 \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{b d} \left(-a d \text{Log} \left[\frac{a}{b} + x \right]^2 - b c \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [a + b x] - 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [a + b x] + \right. \right. \\
& \quad 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - 2 a d \text{Log} [a + b x] \text{Log} \left[\frac{a + b x}{c + d x} \right] - 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [c + d x] + \\
& \quad \left. \left. 2 b c \text{Log} \left[\frac{a + b x}{c + d x} \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b c \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + 2 a b \\
& B^2 n^2 \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{2 b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + \right. \right. \\
& \quad b^2 c^2 \text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (a^2 d^2 \text{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \text{Log} [c + d x])) - \\
& \quad \left. \left. 2 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) + \\
& b^2 B^2 n^2 \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) - 2 a^3 d^3 \text{Log} \left[\frac{a}{b} + x \right]^2 + \right. \right. \\
& \quad 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^3 c^3 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (b c - a d) \\
& \quad \left(b x (2 a - b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \text{Log} [c + d x] \right) - \\
& \quad \left. \left. 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]) + \right. \right. \\
& \quad \left. \left. 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) \right)
\end{aligned}$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 196 leaves, 5 steps):

$$\frac{B (b c - a d) g n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b d} + \frac{g (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 b} - \frac{B (b c - a d)^2 g n \left(A + B n + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b d^2} - \frac{B^2 (b c - a d)^2 g n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2}$$

Result (type 4, 911 leaves):

$$g \left(-\frac{a^2 B^2 n^2}{b} - \frac{b B^2 c^2 n^2}{d^2} + \frac{2 a B^2 c n^2}{d} + a A^2 x + a A B n x - \frac{A b B c n x}{d} + \frac{1}{2} A^2 b x^2 + \frac{a^2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{b} - \frac{a B^2 c n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d} + \frac{a^2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2 b} + \frac{b B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^2} - \frac{a B^2 c n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d} - \frac{b B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{2 d^2} + \frac{a B^2 c n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d} + \frac{a^2 A B n \operatorname{Log} [a + b x]}{b} - \frac{a^2 B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x]}{b} + \frac{a^2 B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x]}{b} - \frac{a^2 B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right]}{b} + 2 a A B x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + a B^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - \frac{b B^2 c n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{d} + A b B x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + \frac{a^2 B^2 n \operatorname{Log} [a + b x] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]}{b} + a B^2 x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + \frac{1}{2} b B^2 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + \frac{A b B c^2 n \operatorname{Log} [c + d x]}{d^2} - \frac{2 a A B c n \operatorname{Log} [c + d x]}{d} - \frac{b B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x]}{d^2} + \frac{2 a B^2 c n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x]}{d} + \frac{b B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x]}{d^2} - \frac{2 a B^2 c n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x]}{d} + \frac{b B^2 c^2 n \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} [c + d x]}{d^2} - \frac{2 a B^2 c n \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log} [c + d x]}{d} + \frac{b B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right]}{d^2} - \frac{2 a B^2 c n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right]}{d} + \frac{B^2 c (b c - 2 a d) n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right]}{d^2} - \frac{a^2 B^2 n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right]}{b} \right)$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{ag + bgx} dx$$

Optimal (type 4, 138 leaves, 4 steps):

$$-\frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{2Bn \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{2B^2 n^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bg}$$

Result (type 4, 537 leaves):

$$\begin{aligned} & \frac{1}{3bg} \left(3 \operatorname{Log}[a+bx] \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + 3Bn \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right. \\ & \left. \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \operatorname{Log}[a+bx] \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) + \\ & B^2 n^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \operatorname{Log}[a+bx] \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + \right. \\ & \left. 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \right. \\ & \left. 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) - \\ & \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \end{aligned}$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ag + bgx)^2} dx$$

Optimal (type 3, 136 leaves, 3 steps):

$$-\frac{2B^2 n^2 (c+dx)}{(bc-ad)g^2(a+bx)} - \frac{2Bn(c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{(bc-ad)g^2(a+bx)} - \frac{(c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)g^2(a+bx)}$$

Result (type 3, 389 leaves):

$$\frac{1}{b(b c - a d) g^2 (a + b x)}$$

$$\left(-A^2 b c + a A^2 d - 2 A b B c n + 2 a A B d n - 2 b B^2 c n^2 + 2 a B^2 d n^2 + B^2 (-b c + a d) \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - a B^2 d n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - b B^2 d n^2 x \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - \right.$$

$$2 B d n (a + b x) \operatorname{Log}[a + b x] \left(A + B n + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + 2 a A B d n \operatorname{Log}[c + d x] + 2 a B^2 d n^2 \operatorname{Log}[c + d x] +$$

$$2 A b B d n x \operatorname{Log}[c + d x] + 2 b B^2 d n^2 x \operatorname{Log}[c + d x] - 2 a B^2 d n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \operatorname{Log}[c + d x] -$$

$$\left. 2 b B^2 d n^2 x \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \operatorname{Log}[c + d x] + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] (- (b c - a d) (A + B n) + B d n (a + b x) \operatorname{Log}[c + d x]) \right)$$

Problem 38: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 544 leaves, 19 steps):

$$\frac{13 B^2 (b c - a d)^4 g^4 n^2 x}{30 b^4} + \frac{7 B^2 (b c - a d)^3 g^4 n^2 (c + d x)^2}{60 b^3 d} + \frac{B^2 (b c - a d)^2 g^4 n^2 (c + d x)^3}{30 b^2 d} - \frac{2 B (b c - a d)^4 g^4 n (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{5 b^5}$$

$$\frac{B (b c - a d)^3 g^4 n (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{5 b^3 d} - \frac{2 B (b c - a d)^2 g^4 n (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{15 b^2 d}$$

$$\frac{B (b c - a d) g^4 n (c + d x)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{10 b d} + \frac{g^4 (c + d x)^5 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{5 d} + \frac{13 B^2 (b c - a d)^5 g^4 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]}{30 b^5 d} +$$

$$\frac{5 B^2 (b c - a d)^5 g^4 n^2 \operatorname{Log}[c + d x]}{6 b^5 d} + \frac{2 B (b c - a d)^5 g^4 n \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) \operatorname{Log}\left[1 - \frac{b(c + d x)}{d(a + b x)}\right]}{5 b^5 d} - \frac{2 B^2 (b c - a d)^5 g^4 n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{d(a + b x)}\right]}{5 b^5 d}$$

Result (type 4, 3163 leaves):

$$\frac{1}{60 b^5 d}$$

$$g^4 \left(-96 b^5 B^2 c^5 n^2 + 336 a b^4 B^2 c^4 d n^2 - 480 a^2 b^3 B^2 c^3 d^2 n^2 + 360 a^3 b^2 B^2 c^2 d^3 n^2 - 144 a^4 b B^2 c d^4 n^2 + 24 a^5 B^2 d^5 n^2 + 60 A^2 b^5 c^4 d x - 96 A b^5 B c^4 d n x + \right.$$

$$240 a A b^4 B c^3 d^2 n x - 240 a^2 A b^3 B c^2 d^3 n x + 120 a^3 A b^2 B c d^4 n x - 24 a^4 A b B d^5 n x + 46 b^5 B^2 c^4 d n^2 x - 158 a b^4 B^2 c^3 d^2 n^2 x + 204 a^2 b^3 B^2 c^2 d^3 n^2 x -$$

$$118 a^3 b^2 B^2 c d^4 n^2 x + 26 a^4 b B^2 d^5 n^2 x + 120 A^2 b^5 c^3 d^2 x^2 - 72 A b^5 B c^3 d^2 n x^2 + 120 a A b^4 B c^2 d^3 n x^2 - 60 a^2 A b^3 B c d^4 n x^2 + 12 a^3 A b^2 B d^5 n x^2 +$$

$$13 b^5 B^2 c^3 d^2 n^2 x^2 - 33 a b^4 B^2 c^2 d^3 n^2 x^2 + 27 a^2 b^3 B^2 c d^4 n^2 x^2 - 7 a^3 b^2 B^2 d^5 n^2 x^2 + 120 A^2 b^5 c^2 d^3 x^3 - 32 A b^5 B c^2 d^3 n x^3 + 40 a A b^4 B c d^4 n x^3 -$$

$$8 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 60 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 +$$

$$12 A^2 b^5 d^5 x^5 - 96 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] -$$

$$\begin{aligned}
& 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 60 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 120 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 120 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
& 60 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 96 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 240 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 120 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 24 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 12 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 120 a A b^4 B c^4 d n \operatorname{Log}[a + b x] - \\
& 240 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[a + b x] + 240 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[a + b x] - 120 a^4 A b B c d^4 n \operatorname{Log}[a + b x] + 24 a^5 A B d^5 n \operatorname{Log}[a + b x] + \\
& 72 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[a + b x] - 152 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[a + b x] + 106 a^4 b B^2 c d^4 n^2 \operatorname{Log}[a + b x] - 26 a^5 B^2 d^5 n^2 \operatorname{Log}[a + b x] - \\
& 120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 120 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 240 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 240 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 120 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 24 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 120 A b^5 B c^4 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 96 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 240 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 240 a^2 b^3 B^2 c^2 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 24 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 240 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 72 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 60 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 240 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 32 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 40 a b^4 B^2 c d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 8 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 120 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a b^4 B^2 c^4 d n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 240 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 240 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 120 a^4 b B^2 c d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a^5 B^2 d^5 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 60 b^5 B^2 c^4 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 120 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 120 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 60 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 24 A b^5 B c^5 n \operatorname{Log}[c + d x] - 46 b^5 B^2 c^5 n^2 \operatorname{Log}[c + d x] + \\
& 86 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c + d x] - 52 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c + d x] + 12 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c + d x] + 24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] -
\end{aligned}$$

$$24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 24 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 24 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] -$$

$$24 b^5 B^2 c^5 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 24 a B^2 d (5 b^4 c^4 - 10 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 5 a^3 b c d^3 + a^4 d^4) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 454 leaves, 15 steps):

$$\frac{5 B^2 (b c - a d)^3 g^3 n^2 x}{12 b^3} + \frac{B^2 (b c - a d)^2 g^3 n^2 (c + d x)^2}{12 b^2 d} - \frac{B (b c - a d)^3 g^3 n (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{2 b^4} -$$

$$\frac{B (b c - a d)^2 g^3 n (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{4 b^2 d} - \frac{B (b c - a d) g^3 n (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{6 b d} +$$

$$\frac{g^3 (c + d x)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{4 d} + \frac{5 B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]}{12 b^4 d} + \frac{11 B^2 (b c - a d)^4 g^3 n^2 \operatorname{Log}[c + d x]}{12 b^4 d} +$$

$$\frac{B (b c - a d)^4 g^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) \operatorname{Log}\left[1 - \frac{b(c + d x)}{d(a + b x)}\right]}{2 b^4 d} - \frac{B^2 (b c - a d)^4 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{d(a + b x)}\right]}{2 b^4 d}$$

Result (type 4, 2348 leaves):

$$\begin{aligned}
& \frac{1}{12 b^4 d} g^3 \left(-18 b^4 B^2 c^4 n^2 + 54 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 30 a^3 b B^2 c d^3 n^2 - 6 a^4 B^2 d^4 n^2 + 12 A^2 b^4 c^3 d x - 18 A b^4 B c^3 d n x + 36 a A b^3 B c^2 d^2 n x - \right. \\
& 24 a^2 A b^2 B c d^3 n x + 6 a^3 A b B d^4 n x + 7 b^4 B^2 c^3 d n^2 x - 19 a b^3 B^2 c^2 d^2 n^2 x + 17 a^2 b^2 B^2 c d^3 n^2 x - 5 a^3 b B^2 d^4 n^2 x + 18 A^2 b^4 c^2 d^2 x^2 - \\
& 9 A b^4 B c^2 d^2 n x^2 + 12 a A b^3 B c d^3 n x^2 - 3 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + 12 A^2 b^4 c d^3 x^3 - \\
& 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 18 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 18 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 24 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 24 a A b^3 B c^3 d n \operatorname{Log}[a + b x] - 36 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[a + b x] + 24 a^3 A b B c d^3 n \operatorname{Log}[a + b x] - 6 a^4 A B d^4 n \operatorname{Log}[a + b x] + \\
& 9 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] - 14 a^3 b B^2 c d^3 n^2 \operatorname{Log}[a + b x] + 5 a^4 B^2 d^4 n^2 \operatorname{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 A b^4 B c^3 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 18 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 24 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 9 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 3 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a b^3 B^2 c^3 d n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 24 a^3 b B^2 c d^3 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^4 B^2 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 b^4 B^2 c^3 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 18 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 A b^4 B c^4 n \operatorname{Log}[c + d x] - \\
& 7 b^4 B^2 c^4 n^2 \operatorname{Log}[c + d x] + 10 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c + d x] - 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& \left. 6 b^4 B^2 c^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 a B^2 d (-4 b^3 c^3 + 6 a b^2 c^2 d - 4 a^2 b c d^2 + a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)
\end{aligned}$$

Problem 40: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 361 leaves, 11 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^2 g^2 n^2 x}{3 b^2} - \frac{2 B (b c - a d)^2 g^2 n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b^3} - \frac{B (b c - a d) g^2 n (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b d} + \\ & \frac{g^2 (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{3 d} + \frac{B^2 (b c - a d)^3 g^2 n^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{3 b^3 d} + \frac{B^2 (b c - a d)^3 g^2 n^2 \operatorname{Log} [c + d x]}{b^3 d} + \\ & \frac{2 B (b c - a d)^3 g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{3 b^3 d} - \frac{2 B^2 (b c - a d)^3 g^2 n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{3 b^3 d} \end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned}
& g^2 \left(c^2 x \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + c d x^2 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + \\
& \frac{1}{3} d^2 x^3 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + 2 B c^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right] + \frac{(b c - a d) (a d \text{Log} [a + b x] - b c \text{Log} [c + d x])}{b^2 c d - a b d^2} \right) + 2 B d^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]}{6 b^3 d^3} \right) + \\
& 4 B c d n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{1}{2} (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \text{Log} [a + b x]}{b^2 (b c - a d)} - \frac{c^2 \text{Log} [c + d x]}{d^2 (b c - a d)} \right) \right) + \\
& B^2 c^2 n^2 \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{b d} \left(-a d \text{Log} \left[\frac{a}{b} + x \right]^2 - b c \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [a + b x] - 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [a + b x] + \right. \right. \\
& \quad 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - 2 a d \text{Log} [a + b x] \text{Log} \left[\frac{a + b x}{c + d x} \right] - 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [c + d x] + \\
& \quad \left. \left. 2 b c \text{Log} \left[\frac{a + b x}{c + d x} \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b c \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + 2 B^2 c \\
& d n^2 \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{2 b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + \right. \right. \\
& \quad b^2 c^2 \text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (a^2 d^2 \text{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \text{Log} [c + d x])) - \\
& \quad \left. \left. 2 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) \right) + \\
& B^2 d^2 n^2 \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) - 2 a^3 d^3 \text{Log} \left[\frac{a}{b} + x \right]^2 + \right. \right. \\
& \quad 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^3 c^3 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (b c - a d) \\
& \quad \left(b x (2 a - b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \text{Log} [c + d x] \right) - \\
& \quad \left. \left. 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]) + \right. \right. \\
& \quad \left. \left. 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int (c g + d g x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 220 leaves, 7 steps):

$$\frac{B (b c - a d) g n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b^2} + \frac{g (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 d} +$$

$$\frac{B^2 (b c - a d)^2 g n^2 \operatorname{Log}[c + d x]}{b^2 d} + \frac{B (b c - a d)^2 g n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 g n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d}$$

Result (type 4, 941 leaves):

$$\frac{1}{2 b^2 d} g \left(-2 b^2 B^2 c^2 n^2 + 4 a b B^2 c d n^2 - 2 a^2 B^2 d^2 n^2 + 2 A^2 b^2 c d x - 2 A b^2 B c d n x + 2 a A b B d^2 n x + A^2 b^2 d^2 x^2 - 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right.$$

$$2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] +$$

$$b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 4 a A b B c d n \operatorname{Log}[a + b x] - 2 a^2 A B d^2 n \operatorname{Log}[a + b x] - 4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] +$$

$$2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] -$$

$$4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 4 A b^2 B c d x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] -$$

$$2 b^2 B^2 c d n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 a b B^2 d^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 A b^2 B d^2 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 4 a b B^2 c d n \operatorname{Log}[a + b x] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] -$$

$$2 a^2 B^2 d^2 n \operatorname{Log}[a + b x] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 b^2 B^2 c d x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + b^2 B^2 d^2 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 - 2 A b^2 B c^2 n \operatorname{Log}[c + d x] +$$

$$2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log}[c + d x] -$$

$$\left. 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b^2 B^2 c^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a B^2 d (-2 b c + a d) n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right)$$

Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{c g + d g x} dx$$

Optimal (type 4, 137 leaves, 4 steps):

$$-\frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{d g}-\frac{2 B n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d g}+\frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d g}$$

Result (type 4, 537 leaves):

$$\begin{aligned} & \frac{1}{3 d g}\left(3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 \operatorname{Log}[c+d x]-3 B n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right. \\ & \quad \left.\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2+2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \operatorname{Log}[c+d x]-2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)\right)+ \\ & B^2 n^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^3+3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+3\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 \operatorname{Log}[c+d x]+ \right. \\ & \quad \left. 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \right. \\ & \quad \left. 3\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2-2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)\right)+ \\ & \quad \left. 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]-6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right) \end{aligned}$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(c g+d g x)^2} d x$$

Optimal (type 3, 163 leaves, 4 steps):

$$-\frac{2 A B n(a+b x)}{(b c-a d) g^2(c+d x)}+\frac{2 B^2 n^2(a+b x)}{(b c-a d) g^2(c+d x)}-\frac{2 B^2 n(a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d) g^2(c+d x)}+\frac{(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d) g^2(c+d x)}$$

Result (type 3, 391 leaves):

$$\frac{1}{d(-bc+ad)g^2(c+dx)} \left(A^2bc - aA^2d - 2ABbcn + 2aABdn + 2bB^2cn^2 - 2aB^2dn^2 + B^2(bc-ad) \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - bB^2cn^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 - bB^2dn^2x \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + \right. \\ \left. 2bBn(c+dx) \operatorname{Log}[a+bx] \left(-A+Bn - B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + Bn \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + 2ABbcn \operatorname{Log}[c+dx] - 2bB^2cn^2 \operatorname{Log}[c+dx] + \right. \\ \left. 2ABbdnx \operatorname{Log}[c+dx] - 2bB^2dn^2x \operatorname{Log}[c+dx] - 2bB^2cn^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \operatorname{Log}[c+dx] - \right. \\ \left. 2bB^2dn^2x \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \operatorname{Log}[c+dx] + 2B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left((bc-ad)(A-Bn) + bBn(c+dx) \operatorname{Log}[c+dx]\right) \right)$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int (f+gx)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 923 leaves, 15 steps):

$$\frac{B^2(bc-ad)^3g^3n^2x}{6b^3d^3} + \frac{B^2(bc-ad)^2g^2(4bdf-3bcg-adg)n^2x}{4b^3d^3} + \frac{B^2(bc-ad)^2g^3n^2(c+dx)^2}{12b^2d^4} - \frac{1}{2b^4d^3} \\ B(bc-ad)g(a^2d^2g^2-2abd g(2df-cg)+b^2(6d^2f^2-8cdfg+3c^2g^2))n(a+bx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right) - \\ \frac{B(bc-ad)g^2(4bdf-3bcg-adg)n(c+dx)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{4b^2d^4} - \frac{B(bc-ad)g^3n(c+dx)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{6b^4d^4} - \\ \frac{(bf-ag)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{4b^4g} + \frac{(f+gx)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{4g} - \frac{1}{2b^4d^4} \\ B(bc-ad)(2bdf-bcg-adg)(2abd^2fg-a^2d^2g^2-b^2(2d^2f^2-2cdfg+c^2g^2))n \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] + \\ \frac{B^2(bc-ad)^4g^3n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{6b^4d^4} + \frac{B^2(bc-ad)^3g^2(4bdf-3bcg-adg)n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{4b^4d^4} + \\ \frac{B^2(bc-ad)^4g^3n^2 \operatorname{Log}[c+dx]}{6b^4d^4} + \frac{B^2(bc-ad)^3g^2(4bdf-3bcg-adg)n^2 \operatorname{Log}[c+dx]}{4b^4d^4} + \\ \frac{B^2(bc-ad)^2g(a^2d^2g^2-2abd g(2df-cg)+b^2(6d^2f^2-8cdfg+3c^2g^2))n^2 \operatorname{Log}[c+dx]}{2b^4d^4} - \frac{1}{2b^4d^4} \\ B^2(bc-ad)(2bdf-bcg-adg)(2abd^2fg-a^2d^2g^2-b^2(2d^2f^2-2cdfg+c^2g^2))n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]$$

Result (type 4, 2541 leaves):

$$\begin{aligned}
& f^3 x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \frac{3}{2} f^2 g x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \\
& f g^2 x^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \frac{1}{4} g^3 x^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 - \\
& \frac{2 B f^3 n \left(-A - B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - b c \operatorname{Log} [c + d x] \right)}{b d} + \\
& \frac{1}{12} B g^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \\
& \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \frac{2 c x^3}{d} - \frac{6 a^4 \operatorname{Log} [a + b x]}{b^4} + 6 x^4 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + \frac{6 c^4 \operatorname{Log} [c + d x]}{d^4} \right) + \\
& B f g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + 2 x^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) - \\
& \frac{1}{b^2 d^2} 3 B f^2 g n \left(-A - B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-a^2 d^2 \operatorname{Log} [a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b c^2 \operatorname{Log} [c + d x] \right) \right) + \\
& \frac{1}{b d} B^2 f^3 n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \right. \\
& 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \\
& \left. 2 b c \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + \\
& \frac{1}{12} B^2 g^3 n^2 \left(3 x^4 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 + \frac{1}{b^4 d^4} \left(-6 b^4 c^4 + 6 a b^3 c^3 d + 6 a^3 b c d^3 - 6 a^4 d^4 - 5 b^4 c^3 d x + 5 a b^3 c^2 d^2 x + 5 a^2 b^2 c d^3 x - 5 a^3 b d^4 x + b^4 c^2 d^2 x^2 - \right. \right. \\
& 2 a b^3 c d^3 x^2 + a^2 b^2 d^4 x^2 - 6 a b^3 c^3 d \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] - 3 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 b^4 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right] - 6 a^3 b c d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - \\
& 3 b^4 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 3 a^2 b^2 c^2 d^2 \operatorname{Log} [a + b x] - 2 a^3 b c d^3 \operatorname{Log} [a + b x] + 5 a^4 d^4 \operatorname{Log} [a + b x] + 6 a^4 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] - \\
& 6 a^4 d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] + 6 a^4 d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - 6 b^4 c^3 d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + 6 a^3 b d^4 x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + \\
& 3 b^4 c^2 d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - 3 a^2 b^2 d^4 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - 2 b^4 c d^3 x^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + 2 a b^3 d^4 x^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - 6 a^4 d^4 \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + \\
& 5 b^4 c^4 \operatorname{Log} [c + d x] - 2 a b^3 c^3 d \operatorname{Log} [c + d x] - 3 a^2 b^2 c^2 d^2 \operatorname{Log} [c + d x] - 6 b^4 c^4 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] + 6 b^4 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + \\
& \left. 6 b^4 c^4 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \operatorname{Log} [c + d x] + 6 b^4 c^4 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 6 b^4 c^4 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 6 a^4 d^4 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + \\
& \frac{3}{2} B^2 f^2 g n^2 \left(x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(a^2 d^2 \operatorname{Log}[a+bx] - b(d(-bc+ad)x + bc^2 \operatorname{Log}[c+dx]) \right) - \\
& 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \Big) + \\
& 3 B^2 f g^2 n^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d(-bc+ad)(bc+ad)(a+bx) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
& 4 b(bc-ad)(bc+ad)(c+dx) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& \left. d^2(bc-ad) \left(bx(2a-bx) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a+bx] \right) + b^2(bc-ad) \left(dx(-2c+dx) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c+dx] \right) \right) - \\
& 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(b d(bc-ad)x(-2bc-2ad+bdx) - 2 a^3 d^3 \operatorname{Log}[a+bx] + 2 b^3 c^3 \operatorname{Log}[c+dx] \right) + \\
& 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \Big) \Big)
\end{aligned}$$

Problem 68: Result more than twice size of optimal antiderivative.

$$\int (f+gx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 565 leaves, 12 steps):

$$\begin{aligned}
& \frac{B^2 (bc-ad)^2 g^2 n^2 x}{3 b^2 d^2} - \frac{2 B (bc-ad) g (3 b d f - 2 b c g - a d g) n (a+bx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 b^3 d^2} - \\
& \frac{B (bc-ad) g^2 n (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 b d^3} - \frac{(bf-ag)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 b^3 g} + \frac{(f+gx)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 g} + \\
& \frac{1}{3 b^3 d^3} 2 B (bc-ad) \left(a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2) \right) n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)} \right] + \\
& \frac{B^2 (bc-ad)^3 g^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx} \right]}{3 b^3 d^3} + \frac{B^2 (bc-ad)^3 g^2 n^2 \operatorname{Log}[c+dx]}{3 b^3 d^3} + \frac{2 B^2 (bc-ad)^2 g (3 b d f - 2 b c g - a d g) n^2 \operatorname{Log}[c+dx]}{3 b^3 d^3} + \\
& \frac{2 B^2 (bc-ad) \left(a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2) \right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{3 b^3 d^3}
\end{aligned}$$

Result (type 4, 1534 leaves):

$$\begin{aligned}
& f^2 x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \\
& f g x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \frac{1}{3} g^2 x^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 - \\
& \frac{2 B f^2 n \left(-A - B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - b c \operatorname{Log} [c + d x] \right)}{b d} + \\
& \frac{1}{3} B g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + 2 x^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) - \\
& \frac{1}{b^2 d^2} 2 B f g n \left(-A - B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-a^2 d^2 \operatorname{Log} [a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b c^2 \operatorname{Log} [c + d x] \right) \right) + \\
& \frac{1}{b d} B^2 f^2 n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \right. \\
& \quad 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \\
& \quad \left. 2 b c \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + \\
& B^2 f g n^2 \left(x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + \right. \right. \\
& \quad b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x] \right) \right) - \\
& \quad \left. \left. 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) + \\
& B^2 g^2 n^2 \left(\frac{1}{3} x^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 2 a^3 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \right. \right. \\
& \quad 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^3 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
& \quad d^2 (b c - a d) \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \operatorname{Log} [a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \operatorname{Log} [c + d x] \right) - \\
& \quad \left. 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log} [a + b x] + 2 b^3 c^3 \operatorname{Log} [c + d x] \right) + \right. \\
& \quad \left. 4 b^3 c^3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 4 a^3 d^3 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 69: Result more than twice size of optimal antiderivative.

$$\int (f + g x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 290 leaves, 9 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b^2 d} - \frac{(b f - a g)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 b^2 g} + \\ & \frac{(f + g x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 g} + \frac{B (b c - a d) (2 b d f - b c g - a d g) n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b^2 d^2} + \\ & \frac{B^2 (b c - a d)^2 g n^2 \operatorname{Log} [c + d x]}{b^2 d^2} + \frac{B^2 (b c - a d) (2 b d f - b c g - a d g) n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^2 d^2} \end{aligned}$$

Result (type 4, 902 leaves):

$$\begin{aligned} & \frac{1}{2 b^2 d^2} \left(2 b^2 d^2 f x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + b^2 d^2 g x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \right. \\ & 4 b B d f n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] - b c \operatorname{Log} [c + d x] \right) - \\ & 2 B g n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b c^2 \operatorname{Log} [c + d x] \right) \right) + \\ & 2 b B^2 d f n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \right. \\ & 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \\ & \left. 2 b c \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + \\ & B^2 g n^2 \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\ & b^2 d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x] \right) \right) + \\ & \left. 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \end{aligned}$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\frac{(a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{b} + \frac{2B(bc-ad)n \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{bd} + \frac{2B^2(bc-ad)n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bd}$$

Result (type 4, 421 leaves):

$$\begin{aligned} & \frac{1}{bd} \left(A^2 b d x + a B^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a A B d n \operatorname{Log}[a+bx] - \right. \\ & 2 a B^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+bx] + 2 a B^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+bx] - 2 a B^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \\ & 2 A b B d x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 a B^2 d n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + b B^2 d x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 2 A b B c n \operatorname{Log}[c+dx] + \\ & 2 b B^2 c n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] - 2 b B^2 c n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - 2 b B^2 c n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - \\ & \left. 2 b B^2 c n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 b B^2 c n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 a B^2 d n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \end{aligned}$$

Problem 71: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{f+gx} dx$$

Optimal (type 4, 297 leaves, 9 steps):

$$\begin{aligned} & - \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{g} + \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{g} - \frac{2Bn \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{g} + \\ & \frac{2Bn \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{g} + \frac{2B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{g} - \frac{2B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{g} \end{aligned}$$

Result (type 4, 1441 leaves):

$$\begin{aligned}
& \frac{1}{g} \left(-B^2 n^2 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 + A^2 \operatorname{Log}[f+gx] - 2ABn \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[f+gx] + \right. \\
& B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log}[f+gx] + 2ABn \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] - 2B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] + \\
& B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log}[f+gx] + 2AB \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \operatorname{Log}[f+gx] - 2B^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \operatorname{Log}[f+gx] + \\
& 2B^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \operatorname{Log}[f+gx] + B^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 \operatorname{Log}[f+gx] + 2ABn \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 2B^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 2B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& B^2 n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 2B^2 n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& B^2 n^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - 2ABn \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + 2B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - \\
& B^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 2B^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - \\
& 2B^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + B^2 n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - \\
& 2B^2 n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + B^2 n^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)} \right] + \\
& 2Bn \left(A+B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + Bn \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(a+bx)}{-bf+ag} \right] - \\
& 2Bn \left(A+B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + Bn \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(c+dx)}{-df+cg} \right] - \\
& 2B^2 n^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right] + 2B^2 n^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + \\
& \left. 2B^2 n^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right] - 2B^2 n^2 \operatorname{PolyLog} \left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right)
\end{aligned}$$

Problem 72: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(f+gx)^2} dx$$

Optimal (type 4, 206 leaves, 4 steps):

$$\frac{(a+bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(bf-ag)(f+gx)} + \frac{2B(bc-ad)n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)} + \frac{2B^2(bc-ad)n^2 \operatorname{PolyLog} \left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)}$$

Result (type 4, 3524 leaves):

$$\frac{1}{g(-bf+ag)(-df+cg)(f+gx)} \left(\begin{aligned} & -A^2 b d f^2 + A^2 b c f g + a A^2 d f g - a A^2 c g^2 + 2 A b B d f^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 A b B c f g n \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 A b B d f g n x \operatorname{Log} \left[\frac{a}{b} + x \right] - \\ & 2 A b B c g^2 n x \operatorname{Log} \left[\frac{a}{b} + x \right] - b B^2 d f^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b B^2 c f g n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - b B^2 d f g n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b B^2 c g^2 n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\ & 2 A b B d f^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 a A B d f g n \operatorname{Log} \left[\frac{c}{d} + x \right] - 2 A b B d f g n x \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 a A B d g^2 n x \operatorname{Log} \left[\frac{c}{d} + x \right] + \\ & 2 b B^2 d f^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - 2 a B^2 d f g n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 b B^2 d f g n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - \\ & 2 a B^2 d g^2 n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - b B^2 d f^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + a B^2 d f g n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - b B^2 d f g n^2 x \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + a B^2 d g^2 n^2 x \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \\ & 2 A b B d f^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 A b B c f g \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 a A B d f g \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - 2 a A B c g^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + \\ & 2 b B^2 d f^2 n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - 2 b B^2 c f g n \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 b B^2 d f g n x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - \\ & 2 b B^2 c g^2 n x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - 2 b B^2 d f^2 n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 a B^2 d f g n \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - \\ & 2 b B^2 d f g n x \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 a B^2 d g^2 n x \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - b B^2 d f^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + \\ & b B^2 c f g \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + a B^2 d f g \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 - a B^2 c g^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 - 2 b B^2 c f g n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + \\ & 2 a B^2 d f g n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] - 2 b B^2 c g^2 n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + 2 a B^2 d g^2 n^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + \\ & b B^2 c f g n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - a B^2 d f g n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 + b B^2 c g^2 n^2 x \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - a B^2 d g^2 n^2 x \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - \\ & 2 b B^2 c f g n^2 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + 2 a B^2 d f g n^2 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] - \\ & 2 b B^2 c g^2 n^2 x \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + 2 a B^2 d g^2 n^2 x \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] - \\ & 2 b B^2 c f g n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + 2 a B^2 d f g n^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] - \end{aligned} \right)$$

$$\begin{aligned}
& 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
& b B^2 c f g n^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - a B^2 d f g n^2 \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 + b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - \\
& a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - 2 A b B d f^2 n \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2 A b B c f g n \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 A b B d f g n x \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 A b B c g^2 n x \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 b B^2 d f^2 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 b B^2 c f g n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 b B^2 d f g n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 b B^2 c g^2 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2 A b B d f^2 n \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - 2 a A B d f g n \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 A b B d f g n x \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 a A B d g^2 n x \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 a B^2 d f g n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 a B^2 d g^2 n^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 b B^2 d f^2 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 a B^2 d f g n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 b B^2 d f g n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 a B^2 d g^2 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 b B^2 d f^2 n^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 b B^2 c f g n^2 \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 b B^2 d f g n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] - \\
& 2 b B^2 c g^2 n^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 B^2 (bc-ad) g n^2 (f+gx) \operatorname{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] - \\
& 2 B^2 (bc-ad) g n^2 (f+gx) \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - 2 b B^2 c f g n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] + \\
& 2 a B^2 d f g n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - 2 b B^2 c g^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] + 2 a B^2 d g^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] \Big)
\end{aligned}$$

Problem 73: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(f+gx)^3} dx$$

Optimal (type 4, 389 leaves, 9 steps):

$$\begin{aligned} & \frac{B (bc - ad) g n (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{(bf - ag)^2 (df - cg) (f + gx)} + \frac{b^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2g (bf - ag)^2} - \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2g (f + gx)^2} + \\ & \frac{B^2 (bc - ad)^2 g n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{(bf - ag)^2 (df - cg)^2} + \frac{B (bc - ad) (2bdf - bcb - adg) n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{(df - cg)(a+bx)}{(bf - ag)(c+dx)} \right]}{(bf - ag)^2 (df - cg)^2} + \\ & \frac{B^2 (bc - ad) (2bdf - bcb - adg) n^2 \operatorname{PolyLog} \left[2, \frac{(df - cg)(a+bx)}{(bf - ag)(c+dx)} \right]}{(bf - ag)^2 (df - cg)^2} \end{aligned}$$

Result (type 4, 18311 leaves):

$$\begin{aligned} & - \frac{\left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{2g (f + gx)^2} + \\ & 2Bn \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \left(\frac{\frac{g \left(\frac{a+x}{b} \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} - \left(\frac{g^2 \left(\frac{a+x}{b} \right)^2}{\left(-f + \frac{ag}{b} \right)^4 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)^2} + \frac{2g \left(\frac{a+x}{b} \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right)} \right) \operatorname{Log} \left[\frac{a}{b} + x \right] - \frac{\operatorname{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) - \\ & \left(\frac{\frac{g \left(\frac{c+x}{d} \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} - \left(\frac{g^2 \left(\frac{c+x}{d} \right)^2}{\left(-f + \frac{cg}{d} \right)^4 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)^2} + \frac{2g \left(\frac{c+x}{d} \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right)} \right) \operatorname{Log} \left[\frac{c}{d} + x \right] - \frac{\operatorname{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) - \frac{-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right]}{2g (f + gx)^2} + \end{aligned}$$

$$\begin{aligned}
& B^2 n^2 \left(2 \left(\frac{\frac{g \left(\frac{a+x}{b}\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)} - \left(\frac{g^2 \left(\frac{a+x}{b}\right)^2}{\left(-f + \frac{ag}{b}\right)^4 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)^2} + \frac{2g \left(\frac{a+x}{b}\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)} \right) \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b}\right)^2} \right. \\
& \left. \frac{\frac{g \left(\frac{c+x}{d}\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} - \left(\frac{g^2 \left(\frac{c+x}{d}\right)^2}{\left(-f + \frac{cg}{d}\right)^4 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)^2} + \frac{2g \left(\frac{c+x}{d}\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d}\right)^2} \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) - \\
& \frac{\left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2}{2g(f+gx)^2} + \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{a+x}{b}\right)^2}{\left(-f + \frac{ag}{b}\right)^4 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)^2} + \frac{2g \left(\frac{a+x}{b}\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)} \right) \text{Log} \left[\frac{a}{b} + x \right]^2 + \right. \\
& \left. \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b}\right)^2} + \text{Log} \left[\frac{a}{b} + x \right] \left(\frac{g \left(\frac{a+x}{b}\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b}\right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b}\right)^2} \right) + \\
& \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c+x}{d}\right)^2}{\left(-f + \frac{cg}{d}\right)^4 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)^2} + \frac{2g \left(\frac{c+x}{d}\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} \right) \text{Log} \left[\frac{c}{d} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d}\right)^2} + \right. \\
& \left. \text{Log} \left[\frac{c}{d} + x \right] \left(\frac{g \left(\frac{c+x}{d}\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d}\right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d}\right)^2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{f^2} \left(\frac{1}{g} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right. \right. \\
& \left. \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) \right) + \\
& \frac{1}{2} \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \text{PolyLog} \left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] - \text{PolyLog} \left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] - \text{PolyLog} \left[3, \frac{c}{d} + x \right] + \text{PolyLog} \left[3, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& g^2 \left(\frac{1}{g} \left(\left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} - \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} - \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] - \right. \right. \\
& \left. \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} 2b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \right. \\
& \left. \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \right. \\
& \left. \left(-\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} + \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} + \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \frac{(-df+cg) \left(\frac{2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3} \right)}{d(f+gx)} \right) + \right. \\
& \left. \left. \frac{(-df+cg) \left(\frac{2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3} \right)}{d(f+gx)} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-df+cg) \times \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right) - \frac{c \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)}}{d(f+gx)^2} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \\
& \frac{1}{2} \left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right) - (bf-ag) \times \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right) - a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} + \right. \\
& \left. \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{2c(-bc+ad)x}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} \right) - b(-df+cg) \times \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)^2} + \right. \\
& \left. \frac{bc \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 + 2 \left(-\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \right. \\
& \left. \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \left(-\frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \right. \\
& \left. \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{dg \left(\frac{c}{d} + x \right)} (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \\
& \left(\left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) + \right. \\
& \left. \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right]
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{1}{d g \left(\frac{c}{d} + x \right)} 2 (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) + \right. \\
& \left(\frac{(b f - a g) \left(\frac{2 a b x}{(b f - a g)^2} + \frac{2 a^2 b (f + g x)}{(b f - a g)^3} \right)}{b (f + g x)} - \frac{(b f - a g) x \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)^2} - \frac{a \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \\
& \left. \frac{(-d f + c g) \left(\frac{2 c d x}{(-d f + c g)^2} - \frac{2 c^2 d (f + g x)}{(-d f + c g)^3} \right)}{d (f + g x)} - \frac{(-d f + c g) x \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)^2} + \frac{c \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \\
& \left. \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \\
& \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2} \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \right. \\
& \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
& \left(-\frac{2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2} + \right. \\
& \left. -\frac{b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) - b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g)^2 \left(\frac{c}{d} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} \right) + \\
& \left. \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2} \left(\frac{2 b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2}{d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2} \right) - \\
& \frac{2 b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
& \frac{2 b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
& \left. \frac{2 a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g)^2 \left(\frac{c}{d} + x \right)} \right) \\
& \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \frac{(b f - a g)^2 \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)^2 \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b^2 g^2 \left(\frac{a}{b} + x \right)^2} + \\
& \frac{2 (-d f + c g) \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{d g \left(\frac{c}{d} + x \right)} +
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \left(\frac{(b f - a g) \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \left(\frac{a b g \left(\frac{a+x}{b} \right) + b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} + \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right)}{b g \left(\frac{a}{b} + x \right) \left(1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right)} + \right. \\
& \frac{(b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a+x}{b} \right) - 2 a b \left(\frac{a+x}{b} \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \frac{a \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \\
& \left. \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x \right)} \right) + \frac{(-d f + c g)^2 \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right)^2 \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d^2 g^2 \left(\frac{c}{d} + x \right)^2} + \\
& \left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
& \left. \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) / \left(d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2 \right) + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \left(- \frac{(-d f + c g) \left(\frac{c d g \left(\frac{c+x}{d} \right) - d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} - \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right) \left(1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right)} - \frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c+x}{d} \right) - 2 c d \left(\frac{c+x}{d} \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} - \right. \\
& \left. \frac{c \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} + \frac{(-d f + c g) \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x \right)} \right) + \\
& \frac{b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c+x}{d} \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c+x}{d} \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2 \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c+x}{d} \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2} + \\
& \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} - \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) / \left(d (b f - a g) \left(\frac{c}{d} + x\right) \left(1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) - \\
& \frac{b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \frac{2 a c d \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x\right)} - \\
& \frac{b c \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x\right)} - \\
& \left. \frac{a b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g)^2 \left(\frac{c}{d} + x\right)} \right) + \\
& \frac{(b f - a g) \left(-\frac{2 a^2 b g \left(\frac{a}{b} + x\right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x\right)}{(b f - a g)^2} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x\right)} - \frac{a \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x\right)} - \\
& \frac{(b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x\right)} + \left(\frac{b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \frac{2 a c d \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x\right)} + \right. \\
& \left. \frac{b c \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x\right)} + \frac{a b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g)^2 \left(\frac{c}{d} + x\right)} \right) \\
& \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} - \\
& \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} + \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x\right)} +
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{b(-df+cg)\left(\frac{a}{b}+x\right)\left(-\frac{2c^2d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)}-\frac{2acd\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}\right)-\frac{bc\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)\left(\frac{c}{d}+x\right)}-\frac{bc\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)\left(\frac{c}{d}+x\right)} \right. \\
& \left. \frac{ab(-df+cg)\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)^2\left(\frac{c}{d}+x\right)} \right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] + \\
& \left(\frac{b(-df+cg)\left(\frac{a}{b}+x\right)\left(-\frac{2c^2d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)}-\frac{2acd\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}\right)-\frac{bc\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)\left(\frac{c}{d}+x\right)}-\frac{bc\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)\left(\frac{c}{d}+x\right)} \right. \\
& \left. \frac{ab(-df+cg)\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)}{d(bf-ag)^2\left(\frac{c}{d}+x\right)} \right) \left(\text{PolyLog}\left[2, \frac{c}{b}+\frac{x}{a}\right]-\text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) - \\
& \frac{b(-df+cg)\left(\frac{a}{b}+x\right)\left(-\frac{2c^2d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^3\left(\frac{a}{b}+x\right)}-\frac{2acd\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}\right)\text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]}{d(bf-ag)\left(\frac{c}{d}+x\right)} - \\
& \frac{bc\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)\text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]}{d(bf-ag)\left(\frac{c}{d}+x\right)} - \\
& \frac{ab(-df+cg)\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)\text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]}{d(bf-ag)^2\left(\frac{c}{d}+x\right)} \right) - \\
& \frac{1}{g^2} 2 \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag}+\frac{ab(f+gx)}{(bf-ag)^2}\right)\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{c}{d}+x\right]}{b(f+gx)} + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag}+\frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-df + cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) + \\
& \left(-\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \\
& \frac{1}{2} \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 + \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{2dg \left(\frac{c}{d} + x \right)} + \frac{1}{2dg \left(\frac{c}{d} + x \right)} (-df+cg) \\
& \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} \\
& b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} b(-df+cg) \\
& \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] \right) - \\
& \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf-ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf-ag} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x \right)} - \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 - \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)}
\end{aligned}$$

$$\begin{aligned}
& b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \text{Log} \left[\right. \\
& \left. 1 + \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf-ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf-ag} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x \right)} + \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} \\
& \left. b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right] - \\
& \left. \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} \right] + \\
& \frac{1}{g^3} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right) \\
& \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \\
& \frac{1}{2} \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b} + x\right)}{bf-ag}\right] + \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(\text{PolyLog}\left[2, \frac{c}{d} + x\right] - \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) - \\
& \left. \text{PolyLog}\left[3, -\frac{bg\left(\frac{a}{b} + x\right)}{bf-ag}\right] - \text{PolyLog}\left[3, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{c}{d} + x\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) + \\
4g & \left(\frac{1}{g} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right]}{b(f+gx)} + \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \right) \right. \\
& \left. \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \right) + \right. \\
& \left(-\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} - \frac{(-df+cg)\left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2}\right)}{d(f+gx)} \right) \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] + \\
& \frac{1}{2} \left(\frac{(bf-ag)\left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2}\right)}{b(f+gx)} + \frac{b(-df+cg)\left(\frac{a}{b} + x\right)\left(-\frac{(-bc+ad)x}{b(-df+cg)\left(\frac{a}{b} + x\right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2\left(\frac{a}{b} + x\right)}\right)}{(-bc+ad)(f+gx)} \right) \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right]^2 + \\
& \frac{(-df+cg)\left(-\frac{cdg\left(\frac{c}{d} + x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-df+cg}\right) \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right)}{2dg\left(\frac{c}{d} + x\right)} + \frac{1}{2dg\left(\frac{c}{d} + x\right)} (-df+cg) \\
& \left(-\frac{cdg\left(\frac{c}{d} + x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-df+cg} \right) \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \right) \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) - \frac{1}{d(bf-ag)\left(\frac{c}{d} + x\right)} \\
& b(-df+cg)\left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)^2\left(\frac{a}{b} + x\right)} + \frac{ad\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)} \right) \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c+x}{d} \right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d} \right)}{b(-df+cg) \left(\frac{a+x}{b} \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} \\
& \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \\
& \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& \frac{(bf-ag) \left(-\frac{abg \left(\frac{a+x}{b} \right)}{(bf-ag)^2} - \frac{b \left(\frac{a+x}{b} \right)}{bf-ag} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d} \right)}{b(-df+cg) \left(\frac{a+x}{b} \right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a+x}{b} \right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x \right)} \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c+x}{d} \right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-df+cg} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d} \right)}{b(-df+cg) \left(\frac{a+x}{b} \right)} \right] \right) \text{Log} \left[1 - \frac{dg \left(\frac{c+x}{d} \right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} \\
& b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \\
& \text{Log} \left[1 + \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a+x}{b} \right)}{(bf-ag)^2} - \frac{b \left(\frac{a+x}{b} \right)}{bf-ag} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a+x}{b} \right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x \right)} + \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c+x}{d} \right)}{b(-df+cg)^2 \left(\frac{a+x}{b} \right)} + \frac{ad \left(\frac{c+x}{d} \right)}{b(-df+cg) \left(\frac{a+x}{b} \right)} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a+x}{b} \right)}{bf-ag} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c+x}{d} \right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-df+cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c+x}{d} \right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x \right)} \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c+x}{d} \right)}{b(-df+cg)^2 \left(\frac{a+x}{b} \right)} + \frac{ad \left(\frac{c+x}{d} \right)}{b(-df+cg) \left(\frac{a+x}{b} \right)} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c+x}{d} \right)}{-df+cg} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)}
\end{aligned}$$

$$\begin{aligned}
& b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) - \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog}\left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \\
& \frac{1}{g^2} \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \frac{1}{2} \text{Log}\left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] \right) \right. \\
& \left. \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) + \text{Log}\left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) + \right. \\
& \left. \frac{1}{2} \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) + \right. \\
& \left. \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) \text{PolyLog}\left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag}\right] + \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) \right. \\
& \left. \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] + \text{Log}\left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) - \right. \\
& \left. \left. \left. \left. \left. \text{PolyLog}\left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag}\right] - \text{PolyLog}\left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)}\right] \right) \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 74: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(f+gx)^4} dx$$

Optimal (type 4, 747 leaves, 12 steps):

$$\begin{aligned}
& \frac{B^2 (bc - ad)^2 g^2 n^2 (c + dx)}{3 (bf - ag)^2 (df - cg)^3 (f + gx)} - \frac{B (bc - ad) g^2 n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 (bf - ag) (df - cg)^3 (f + gx)^2} + \\
& \frac{2B (bc - ad) g (3 bdf - b c g - 2 a d g) n (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 (bf - ag)^3 (df - cg)^2 (f + gx)} + \frac{b^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 g (bf - ag)^3} - \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 g (f + gx)^3} + \\
& \frac{B^2 (bc - ad)^3 g^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{3 (bf - ag)^3 (df - cg)^3} - \frac{B^2 (bc - ad)^3 g^2 n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{3 (bf - ag)^3 (df - cg)^3} + \frac{2 B^2 (bc - ad)^2 g (3 bdf - b c g - 2 a d g) n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{3 (bf - ag)^3 (df - cg)^3} + \frac{1}{3 (bf - ag)^3 (df - cg)^3} \\
& \frac{2B (bc - ad) (a^2 d^2 g^2 - a b d g (3 df - cg) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)} \right]}{3 (bf - ag)^3 (df - cg)^3} + \\
& \frac{2 B^2 (bc - ad) (a^2 d^2 g^2 - a b d g (3 df - cg) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) n^2 \operatorname{PolyLog} \left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)} \right]}{3 (bf - ag)^3 (df - cg)^3}
\end{aligned}$$

Result (type 4, 55 186 leaves): Display of huge result suppressed!

Problem 75: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(f + gx)^5} dx$$

Optimal (type 4, 1208 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^2 g^3 n^2 (c + dx)^2}{12 (bf - ag)^2 (df - cg)^4 (f + gx)^2} - \frac{B^2 (bc - ad)^3 g^3 n^2 (c + dx)}{6 (bf - ag)^3 (df - cg)^4 (f + gx)} + \frac{B^2 (bc - ad)^2 g^2 (4 bdf - b c g - 3 a d g) n^2 (c + dx)}{4 (bf - ag)^3 (df - cg)^4 (f + gx)} + \\
& \frac{B (bc - ad) g^3 n (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{6 (bf - ag) (df - cg)^4 (f + gx)^3} - \frac{B (bc - ad) g^2 (4 bdf - b c g - 3 a d g) n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{4 (bf - ag)^2 (df - cg)^4 (f + gx)^2} + \\
& \left(B (bc - ad) g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \right) / \\
& \left(2 (bf - ag)^4 (df - cg)^3 (f + gx) \right) + \frac{b^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{4 g (bf - ag)^4} - \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{4 g (f + gx)^4} - \frac{B^2 (bc - ad)^4 g^3 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{6 (bf - ag)^4 (df - cg)^4} + \\
& \frac{B^2 (bc - ad)^3 g^2 (4 bdf - b c g - 3 a d g) n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{4 (bf - ag)^4 (df - cg)^4} + \frac{B^2 (bc - ad)^4 g^3 n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{6 (bf - ag)^4 (df - cg)^4} - \frac{B^2 (bc - ad)^3 g^2 (4 bdf - b c g - 3 a d g) n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{4 (bf - ag)^4 (df - cg)^4} + \\
& \frac{B^2 (bc - ad)^2 g (3 a^2 d^2 g^2 - 2 a b d g (4 d f - c g) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) n^2 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{2 (bf - ag)^4 (df - cg)^4} - \frac{1}{2 (bf - ag)^4 (df - cg)^4} \\
& B (bc - ad) (2 bdf - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)} \right] - \\
& \frac{1}{2 (bf - ag)^4 (df - cg)^4} B^2 (bc - ad) (2 bdf - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) n^2 \operatorname{PolyLog} \left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)} \right]
\end{aligned}$$

Result (type 4, 142969 leaves): Display of huge result suppressed!

Problem 97: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^4 \left(A + B \operatorname{Log} \left[\frac{e(a + bx)}{c + dx} \right] \right)^2 dx$$

Optimal (type 4, 365 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) g^4 (a + bx)^4 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{10 b d} + \frac{g^4 (a + bx)^5 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{5 b} + \frac{B (bc - ad)^2 g^4 (a + bx)^3 \left(4 A + B + 4 B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{30 b d^2} \\
& \frac{B (bc - ad)^3 g^4 (a + bx)^2 \left(12 A + 7 B + 12 B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{60 b d^3} + \frac{B (bc - ad)^4 g^4 (a + bx) \left(12 A + 13 B + 12 B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{30 b d^4} + \\
& \frac{B (bc - ad)^5 g^4 \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(12 A + 25 B + 12 B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{30 b d^5} + \frac{2 B^2 (bc - ad)^5 g^4 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{5 b d^5}
\end{aligned}$$

Result (type 4, 2878 leaves):

$$\begin{aligned}
& g^4 \left(-\frac{8 a^5 B^2}{5 b} + \frac{2 b^4 B^2 c^5}{5 d^5} - \frac{12 a b^3 B^2 c^4}{5 d^4} + \frac{6 a^2 b^2 B^2 c^3}{d^3} - \frac{8 a^3 b B^2 c^2}{d^2} + \frac{28 a^4 B^2 c}{5 d} + a^4 A^2 x + \frac{8}{5} a^4 A B x + \frac{23}{30} a^4 B^2 x + \frac{2 A b^4 B c^4 x}{5 d^4} + \frac{13 b^4 B^2 c^4 x}{30 d^4} - \right. \\
& \frac{2 a A b^3 B c^3 x}{d^3} - \frac{59 a b^3 B^2 c^3 x}{30 d^3} + \frac{4 a^2 A b^2 B c^2 x}{d^2} + \frac{17 a^2 b^2 B^2 c^2 x}{5 d^2} - \frac{4 a^3 A b B c x}{d} - \frac{79 a^3 b B^2 c x}{30 d} + 2 a^3 A^2 b x^2 + \frac{6}{5} a^3 A b B x^2 + \\
& \frac{13}{60} a^3 b B^2 x^2 - \frac{A b^4 B c^3 x^2}{5 d^3} - \frac{7 b^4 B^2 c^3 x^2}{60 d^3} + \frac{a A b^3 B c^2 x^2}{d^2} + \frac{9 a b^3 B^2 c^2 x^2}{20 d^2} - \frac{2 a^2 A b^2 B c x^2}{d} - \frac{11 a^2 b^2 B^2 c x^2}{20 d} + 2 a^2 A^2 b^2 x^3 + \\
& \frac{8}{15} a^2 A b^2 B x^3 + \frac{1}{30} a^2 b^2 B^2 x^3 + \frac{2 A b^4 B c^2 x^3}{15 d^2} + \frac{b^4 B^2 c^2 x^3}{30 d^2} - \frac{2 a A b^3 B c x^3}{3 d} - \frac{a b^3 B^2 c x^3}{15 d} + a A^2 b^3 x^4 + \frac{1}{10} a A b^3 B x^4 - \frac{A b^4 B c x^4}{10 d} + \\
& \frac{1}{5} A^2 b^4 x^5 + \frac{8 a^5 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{5 b} + \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right]}{5 d^4} - \frac{2 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^2} - \frac{4 a^4 B^2 c \operatorname{Log}\left[\frac{a}{b} + x\right]}{d} + \\
& \frac{a^5 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{5 b} - \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2} - \frac{8 a^4 B^2 c \operatorname{Log}\left[\frac{c}{d} + x\right]}{5 d} + \\
& \frac{b^4 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{5 d^5} - \frac{a b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^4} + \frac{2 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} - \frac{2 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2} + \frac{a^4 B^2 c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d} + \\
& \frac{2 a^5 A B \operatorname{Log}[a + b x]}{5 b} - \frac{23 a^5 B^2 \operatorname{Log}[a + b x]}{30 b} + \frac{a^2 b^2 B^2 c^3 \operatorname{Log}[a + b x]}{5 d^3} - \frac{13 a^3 b B^2 c^2 \operatorname{Log}[a + b x]}{15 d^2} + \frac{43 a^4 B^2 c \operatorname{Log}[a + b x]}{30 d} - \\
& \frac{2 a^5 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x]}{5 b} + \frac{2 a^5 B^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x]}{5 b} - \frac{2 a^5 B^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{5 b} + 2 a^4 A B x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& \frac{8}{5} a^4 B^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{2 b^4 B^2 c^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 d^4} - \frac{2 a b^3 B^2 c^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3} + \frac{4 a^2 b^2 B^2 c^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^2} - \frac{4 a^3 b B^2 c x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d} + \\
& 4 a^3 A b B x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{6}{5} a^3 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \frac{b^4 B^2 c^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 d^3} + \frac{a b^3 B^2 c^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^2} - \frac{2 a^2 b^2 B^2 c x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d} + \\
& 4 a^2 A b^2 B x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{8}{15} a^2 b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{2 b^4 B^2 c^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{15 d^2} - \frac{2 a b^3 B^2 c x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{3 d} + \\
& 2 a A b^3 B x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \frac{1}{10} a b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \frac{b^4 B^2 c x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{10 d} + \frac{2}{5} A b^4 B x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& \frac{2 a^5 B^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{5 b} + a^4 B^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 2 a^3 b B^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 2 a^2 b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& a b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \frac{1}{5} b^4 B^2 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - \frac{2 A b^4 B c^5 \operatorname{Log}[c + d x]}{5 d^5} - \frac{13 b^4 B^2 c^5 \operatorname{Log}[c + d x]}{30 d^5} + \frac{2 a A b^3 B c^4 \operatorname{Log}[c + d x]}{d^4} + \\
& \frac{53 a b^3 B^2 c^4 \operatorname{Log}[c + d x]}{30 d^4} - \frac{4 a^2 A b^2 B c^3 \operatorname{Log}[c + d x]}{d^3} - \frac{38 a^2 b^2 B^2 c^3 \operatorname{Log}[c + d x]}{15 d^3} + \frac{4 a^3 A b B c^2 \operatorname{Log}[c + d x]}{d^2} + \frac{6 a^3 b B^2 c^2 \operatorname{Log}[c + d x]}{5 d^2} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2 a^4 A B c \operatorname{Log}[c+d x]}{d} + \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{5 d^5} - \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4} + \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3} - \\
& \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2} + \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{5 d^5} + \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4} - \\
& \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2} - \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{5 d^5} + \\
& \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^4} - \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d^2} - \\
& \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]}{d} - \frac{2 b^4 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{5 d^5} + \frac{2 a b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^4} - \\
& \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{4 a^3 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 a^4 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \\
& \frac{2 B^2 c\left(b^4 c^4-5 a b^3 c^3 d+10 a^2 b^2 B^2 c^2 d^2-10 a^3 b c d^3+5 a^4 d^4\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{5 d^5} - \frac{2 a^5 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{5 b}
\end{aligned}$$

Problem 98: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 dx$$

Optimal (type 4, 309 leaves, 7 steps):

$$\begin{aligned}
& - \frac{B(b c-a d) g^3(a+b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{6 b d} + \frac{g^3(a+b x)^4 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{4 b} + \\
& \frac{B(b c-a d)^2 g^3(a+b x)^2 \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{12 b d^2} - \frac{B(b c-a d)^3 g^3(a+b x) \left(6 A + 5 B + 6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{12 b d^3} - \\
& \frac{B(b c-a d)^4 g^3 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right] \left(6 A + 11 B + 6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{12 b d^4} - \frac{B^2(b c-a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{2 b d^4}
\end{aligned}$$

Result (type 4, 2110 leaves):

$$\begin{aligned}
& \frac{1}{12 b d^4} \\
& g^3 \left(-6 b^4 B^2 c^4 + 30 a b^3 B^2 c^3 d - 60 a^2 b^2 B^2 c^2 d^2 + 54 a^3 b B^2 c d^3 - 18 a^4 B^2 d^4 - 6 A b^4 B c^3 d x - 5 b^4 B^2 c^3 d x + 24 a A b^3 B c^2 d^2 x + 17 a b^3 B^2 c^2 d^2 x - 36 a^2 A \right. \\
& \left. b^2 B c d^3 x - 19 a^2 b^2 B^2 c d^3 x + 12 a^3 A^2 b d^4 x + 18 a^3 A b B d^4 x + 7 a^3 b B^2 d^4 x + 3 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 - 12 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& 18 a^2 A^2 b^2 d^4 x^2 + 9 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 - 2 A b^4 B c d^3 x^3 + 12 a A^2 b^3 d^4 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - 6 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 24 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 36 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 18 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 3 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 18 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] + 10 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] + 6 a^4 A B d^4 \operatorname{Log}[a + b x] - \\
& 7 a^4 B^2 d^4 \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 6 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 36 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a^3 A b B d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 18 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 3 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 9 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 a^4 B^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 6 A b^4 B c^4 \operatorname{Log}[c + d x] + 5 b^4 B^2 c^4 \operatorname{Log}[c + d x] - 24 a A b^3 B c^3 d \operatorname{Log}[c + d x] - 14 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] + \\
& 36 a^2 A b^2 B c^2 d^2 \operatorname{Log}[c + d x] + 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] - 24 a^3 A b B c d^3 \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + \\
& 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 6 b B^2 c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 6 a^4 B^2 d^4 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]
\end{aligned}$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 253 leaves, 6 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b d} + \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{3 b} + \frac{B (b c - a d)^2 g^2 (a + b x) \left(2 A + B + 2 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b d^2} + \\ & \frac{B (b c - a d)^3 g^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(2 A + 3 B + 2 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b d^3} + \frac{2 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1292 leaves):

$$\begin{aligned}
& g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + \frac{2 a^2 A B \left(a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] - b c \operatorname{Log}[c + d x]\right)}{b d} + \right. \\
& \left. \frac{1}{3} A b^2 B \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log}[a + b x]}{b^3} + 2 x^3 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] - \frac{2 c^3 \operatorname{Log}[c + d x]}{d^3} \right) + \right. \\
& \left. 2 a A B \left(a x - \frac{b c x}{d} - \frac{a^2 \operatorname{Log}[a + b x]}{b} + b x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + \frac{b c^2 \operatorname{Log}[c + d x]}{d^2} \right) + \right. \\
& \left. \frac{1}{b d} a^2 B^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
& \left. \left. 2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \right. \right. \\
& \left. \left. 2 b c \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \right. \\
& \left. \frac{1}{b d^2} a B^2 \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) - a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \right. \\
& \left. \left. b^2 d^2 x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 + 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x])\right) + \right. \right. \\
& \left. \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) + 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right) \right) + \right. \\
& \left. b^2 B^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \right. \\
& \left. \left. 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (b c - a d) \right. \right. \\
& \left. \left. \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x]\right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x]\right) - \right. \right. \\
& \left. \left. 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x]) + \right. \right. \\
& \left. \left. 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) + 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right) \right) \right) \right)
\end{aligned}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 180 leaves, 5 steps):

$$-\frac{B(b c - a d) g(a + b x) \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right)^2}{b d} + \frac{g(a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right)^2}{2 b} -$$

$$\frac{B(b c - a d)^2 g \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right)}{b d^2} - \frac{B^2(b c - a d)^2 g \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b d^2}$$

Result (type 4, 733 leaves):

$$g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + \frac{2 a A B \left(a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] - b c \operatorname{Log}[c + d x] \right)}{b d} + \right.$$

$$A B \left(a x - \frac{b c x}{d} - \frac{a^2 \operatorname{Log}[a + b x]}{b} + b x^2 \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] + \frac{b c^2 \operatorname{Log}[c + d x]}{d^2} \right) +$$

$$\frac{1}{b d} a B^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right.$$

$$2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] + b d x \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] -$$

$$2 b c \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \left. \right) +$$

$$\frac{1}{2} b B^2 \left(x^2 \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right]^2 - \frac{1}{b^2 d^2} \left(-2 d(-b c + a d)(a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b(b c - a d)(c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right.$$

$$b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b(d(-b c + a d)x + b c^2 \operatorname{Log}[c + d x]) \right) -$$

$$\left. \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) \right)$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 128 leaves, 4 steps):

$$-\frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right)^2 \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \frac{2 B \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)}}{c+d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b g} + \frac{2 B^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b g}$$

Result (type 4, 458 leaves):

$$\begin{aligned}
& \frac{1}{3 b g} \left(3 A^2 \operatorname{Log}[a + b x] + \right. \\
& 3 A B \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \operatorname{Log}[a + b x] \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) + \\
& B^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 3 \operatorname{Log}[a + b x] \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 + \right. \\
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) - \\
& \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right)
\end{aligned}$$

Problem 106: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{d(a + b x)}{b(c + d x)}\right]}{c f + d f x} dx$$

Optimal (type 4, 28 leaves, 1 step):

$$\frac{\operatorname{PolyLog}\left[2, \frac{b c - a d}{b(c + d x)}\right]}{d f}$$

Result (type 4, 130 leaves):

$$\begin{aligned}
& \frac{1}{2 d f} \left(-\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \right. \\
& \left. 2 \operatorname{Log}\left[\frac{d(a + b x)}{b(c + d x)}\right] \operatorname{Log}[c + d x] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)
\end{aligned}$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log}\left[\frac{e(a + b x)^2}{(c + d x)^2}\right] \right)^2 dx$$

Optimal (type 4, 377 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) g^4 (a + bx)^4 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{5bd} + \frac{g^4 (a + bx)^5 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{5b} + \frac{2B (bc - ad)^2 g^4 (a + bx)^3 \left(2A + B + 2B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{15bd^2} \\
& \frac{B (bc - ad)^3 g^4 (a + bx)^2 \left(6A + 7B + 6B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{15bd^3} + \frac{2B (bc - ad)^4 g^4 (a + bx) \left(6A + 13B + 6B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{15bd^4} + \\
& \frac{2B (bc - ad)^5 g^4 \left(6A + 25B + 6B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right]}{15bd^5} + \frac{8B^2 (bc - ad)^5 g^4 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{5bd^5}
\end{aligned}$$

Result (type 4, 2907 leaves):

$$\begin{aligned}
& \frac{1}{15bd^5} \\
& g^4 \left(24b^5 B^2 c^5 - 144ab^4 B^2 c^4 d + 360a^2 b^3 B^2 c^3 d^2 - 480a^3 b^2 B^2 c^2 d^3 + 336a^4 b B^2 c d^4 - 96a^5 B^2 d^5 + 12Ab^5 B c^4 dx + 26b^5 B^2 c^4 dx - 60aAb^4 B c^3 d^2 x - \right. \\
& 118ab^4 B^2 c^3 d^2 x + 120a^2 Ab^3 B c^2 d^3 x + 204a^2 b^3 B^2 c^2 d^3 x - 120a^3 Ab^2 B c d^4 x - 158a^3 b^2 B^2 c d^4 x + 15a^4 A^2 b d^5 x + 48a^4 Ab B d^5 x + \\
& 46a^4 b B^2 d^5 x - 6Ab^5 B c^3 d^2 x^2 - 7b^5 B^2 c^3 d^2 x^2 + 30aAb^4 B c^2 d^3 x^2 + 27a^4 b^2 B^2 c^2 d^3 x^2 - 60a^2 Ab^3 B c d^4 x^2 - 33a^2 b^3 B^2 c d^4 x^2 + \\
& 30a^3 A^2 b^2 d^5 x^2 + 36a^3 Ab^2 B d^5 x^2 + 13a^3 b^2 B^2 d^5 x^2 + 4Ab^5 B c^2 d^3 x^3 + 2b^5 B^2 c^2 d^3 x^3 - 20aAb^4 B c d^4 x^3 - 4ab^4 B^2 c d^4 x^3 + 30a^2 A^2 b^3 d^5 x^3 + \\
& 16a^2 Ab^3 B d^5 x^3 + 2a^2 b^3 B^2 d^5 x^3 - 3Ab^5 B c d^4 x^4 + 15aA^2 b^4 d^5 x^4 + 3aAb^4 B d^5 x^4 + 3A^2 b^5 d^5 x^5 + 24ab^4 B^2 c^4 d \operatorname{Log} \left[\frac{a}{b} + x \right] - \\
& 120a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 240a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] - 240a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] + 96a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] + 12a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\
& 24b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right] + 120ab^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right] - 240a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 240a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - 96a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\
& 12b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 60ab^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 120a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 120a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
& 60a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 12a^2 b^3 B^2 c^3 d^2 \operatorname{Log} [a + bx] - 52a^3 b^2 B^2 c^2 d^3 \operatorname{Log} [a + bx] + 86a^4 b B^2 c d^4 \operatorname{Log} [a + bx] + 12a^5 A B d^5 \operatorname{Log} [a + bx] - \\
& 46a^5 B^2 d^5 \operatorname{Log} [a + bx] - 24a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] + 24a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] - 24a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \\
& 12b^5 B^2 c^4 dx \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - 60ab^4 B^2 c^3 d^2 x \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 120a^2 b^3 B^2 c^2 d^3 x \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - 120a^3 b^2 B^2 c d^4 x \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + \\
& 30a^4 Ab B d^5 x \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 48a^4 b B^2 d^5 x \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - 6b^5 B^2 c^3 d^2 x^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 30ab^4 B^2 c^2 d^3 x^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - \\
& 60a^2 b^3 B^2 c d^4 x^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 60a^3 Ab^2 B d^5 x^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 36a^3 b^2 B^2 d^5 x^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 4b^5 B^2 c^2 d^3 x^3 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - \\
& 20ab^4 B^2 c d^4 x^3 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 60a^2 Ab^3 B d^5 x^3 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 16a^2 b^3 B^2 d^5 x^3 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] - 3b^5 B^2 c d^4 x^4 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] +
\end{aligned}$$

$$\begin{aligned}
& 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] + 3 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] + 6 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] + 12 a^5 B^2 d^5 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] + \\
& 15 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + 30 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + \\
& 3 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 - 12 A b^5 B c^5 \operatorname{Log}[c+dx] - 26 b^5 B^2 c^5 \operatorname{Log}[c+dx] + 60 a A b^4 B c^4 d \operatorname{Log}[c+dx] + \\
& 106 a b^4 B^2 c^4 d \operatorname{Log}[c+dx] - 120 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+dx] - 152 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+dx] + 120 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c+dx] + \\
& 72 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+dx] - 60 a^4 A b B c d^4 \operatorname{Log}[c+dx] + 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - \\
& 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 12 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx] + \\
& 60 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx] - 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx] + 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx] - \\
& 60 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 24 b B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 24 a^5 B^2 d^5 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 319 leaves, 7 steps):

$$\begin{aligned}
& - \frac{B (b c - a d) g^3 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{3 b d} + \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{4 b} + \\
& \frac{B (b c - a d)^2 g^3 (a + b x)^2 \left(3 A + 2 B + 3 B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{6 b d^2} - \frac{B (b c - a d)^3 g^3 (a + b x) \left(3 A + 5 B + 3 B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{3 b d^3} - \\
& \frac{B (b c - a d)^4 g^3 \left(3 A + 11 B + 3 B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{3 b d^4} - \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d^4}
\end{aligned}$$

Result (type 4, 2125 leaves):

$$\begin{aligned}
g^3 \left(\right. & \frac{6 a^4 B^2}{b} - \frac{2 b^3 B^2 c^4}{d^4} + \frac{10 a b^2 B^2 c^3}{d^3} - \frac{20 a^2 b B^2 c^2}{d^2} + \frac{18 a^3 B^2 c}{d} + a^3 A^2 x + 3 a^3 A B x + \frac{7}{3} a^3 B^2 x - \frac{A b^3 B c^3 x}{d^3} - \frac{5 b^3 B^2 c^3 x}{3 d^3} + \frac{4 a A b^2 B c^2 x}{d^2} + \\
& \frac{17 a b^2 B^2 c^2 x}{3 d^2} - \frac{6 a^2 A b B c x}{d} - \frac{19 a^2 b B^2 c x}{3 d} + \frac{3}{2} a^2 A^2 b x^2 + \frac{3}{2} a^2 A b B x^2 + \frac{1}{3} a^2 b B^2 x^2 + \frac{A b^3 B c^2 x^2}{2 d^2} + \frac{b^3 B^2 c^2 x^2}{3 d^2} - \frac{2 a A b^2 B c x^2}{d} - \\
& \frac{2 a b^2 B^2 c x^2}{3 d} + a A^2 b^2 x^3 + \frac{1}{3} a A b^2 B x^3 - \frac{A b^3 B c x^3}{3 d} + \frac{1}{4} A^2 b^3 x^4 + \frac{6 a^4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{b} - \frac{2 a b^2 B^2 c^3 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^3} + \frac{8 a^2 b B^2 c^2 \operatorname{Log} \left[\frac{a}{b} + x \right]}{d^2} - \\
& \frac{12 a^3 B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right]}{d} + \frac{a^4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b} + \frac{2 b^3 B^2 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{d^2} - \frac{6 a^3 B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]}{d} - \\
& \frac{b^3 B^2 c^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^4} + \frac{4 a b^2 B^2 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^3} - \frac{6 a^2 b B^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^2} + \frac{4 a^3 B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d} + \frac{a^4 A B \operatorname{Log} [a + b x]}{b} - \\
& \frac{7 a^4 B^2 \operatorname{Log} [a + b x]}{3 b} - \frac{a^2 b B^2 c^2 \operatorname{Log} [a + b x]}{d^2} + \frac{10 a^3 B^2 c \operatorname{Log} [a + b x]}{3 d} - \frac{2 a^4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x]}{b} + \frac{2 a^4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x]}{b} - \\
& \frac{2 a^4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right]}{b} + 2 a^3 A B x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + 3 a^3 B^2 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - \frac{b^3 B^2 c^3 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{d^3} + \\
& \frac{4 a b^2 B^2 c^2 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{d^2} - \frac{6 a^2 b B^2 c x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{d} + 3 a^2 A b B x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \\
& \frac{b^3 B^2 c^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{2 d^2} - \frac{2 a b^2 B^2 c x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{d} + 2 a A b^2 B x^3 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \frac{1}{3} a b^2 B^2 x^3 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - \frac{b^3 B^2 c x^3 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{3 d} + \\
& \left. \frac{1}{2} A b^3 B x^4 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \frac{a^4 B^2 \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]}{b} + a^3 B^2 x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 + \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + \frac{1}{4} b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]^2 + \frac{A b^3 B c^4 \operatorname{Log}[c+dx]}{d^4} + \frac{5 b^3 B^2 c^4 \operatorname{Log}[c+dx]}{3 d^4} - \frac{4 a A b^2 B c^3 \operatorname{Log}[c+dx]}{d^3} - \\
& \frac{14 a b^2 B^2 c^3 \operatorname{Log}[c+dx]}{3 d^3} + \frac{6 a^2 A b B c^2 \operatorname{Log}[c+dx]}{d^2} + \frac{3 a^2 b B^2 c^2 \operatorname{Log}[c+dx]}{d^2} - \frac{4 a^3 A B c \operatorname{Log}[c+dx]}{d} - \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^4} + \\
& \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^3} - \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d^2} + \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx]}{d} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^4} - \\
& \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d^2} - \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx]}{d} + \frac{b^3 B^2 c^4 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^4} - \\
& \frac{4 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^3} + \frac{6 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d^2} - \frac{4 a^3 B^2 c \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \operatorname{Log}[c+dx]}{d} + \\
& \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d^2} - \\
& \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{d} + \frac{2 B^2 c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^4} - \frac{2 a^4 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b} \Big)
\end{aligned}$$

Problem 130: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 255 leaves, 6 steps):

$$\begin{aligned}
& - \frac{2 B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)}{3 b d} + \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2}{3 b} + \frac{4 B (b c - a d)^2 g^2 (a + b x) \left(A + B + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)}{3 b d^2} + \\
& \frac{4 B (b c - a d)^3 g^2 \left(A + 3 B + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{3 b d^3} + \frac{8 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{3 b d^3}
\end{aligned}$$

Result (type 4, 1316 leaves):

$$\begin{aligned}
& g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + \frac{2 a^2 A B \left(2 a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] - 2 b c \operatorname{Log}[c + d x]\right)}{b d} + \right. \\
& \frac{2}{3} A b^2 B \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log}[a + b x]}{b^3} + x^3 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] - \frac{2 c^3 \operatorname{Log}[c + d x]}{d^3} \right) + \\
& 2 a A B \left(2 a x - \frac{2 b c x}{d} - \frac{2 a^2 \operatorname{Log}[a + b x]}{b} + b x^2 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] + \frac{2 b c^2 \operatorname{Log}[c + d x]}{d^2} \right) + \\
& \frac{1}{b d} a^2 B^2 \left(4 a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 8 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& 4 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]^2 + 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 4 b c \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 8 b c \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 8 a d \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \left. \right) + \frac{1}{b} \\
& a B^2 \left(b^2 x^2 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]^2 - \frac{1}{d^2} 4 \left(-2 d (-bc+ad) (a+bx) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b (bc-ad) (c+dx) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) + \right. \\
& b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b (d (-bc+ad) x + b c^2 \operatorname{Log}[c + d x]) \right) - \\
& 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \left. \right) + \\
& \frac{1}{3} b^2 B^2 \left(x^3 \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]^2 - \frac{1}{b^3 d^3} 2 \left(4 d (-bc+ad) (bc+ad) (a+bx) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
& 4 b (bc-ad) (bc+ad) (c+dx) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (bc-ad) \\
& \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (bc-ad) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - \\
& \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right] \right) \left(b d (bc-ad) x (-2 bc - 2 ad + b dx) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x] \right) + \\
& 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 131: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 dx$$

Optimal (type 4, 188 leaves, 5 steps):

$$-\frac{2 B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{b d} + \frac{g (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{2 b} -$$

$$\frac{2 B (b c - a d)^2 g \left(A + 2 B + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b d^2} - \frac{4 B^2 (b c - a d)^2 g \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2}$$

Result (type 4, 849 leaves):

$$g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + 2 a A B \left(\frac{2 (b c - a d) (a d \operatorname{Log} [a + b x] - b c \operatorname{Log} [c + d x])}{b^2 c d - a b d^2} + x \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right] \right) + \right.$$

$$2 A b B \left(- (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log} [a + b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log} [c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right] \right) +$$

$$a B^2 \left(x \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right]^2 - \frac{1}{b d} 4 \left(- a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] + \right.$$

$$2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] + 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] +$$

$$\left. b c \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \operatorname{Log} [c + d x] + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) +$$

$$b B^2 \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{a^2 e + 2 a b e x + b^2 e x^2}{(c + d x)^2} \right]^2 - \frac{1}{b^2 d^2} 2 \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \right.$$

$$2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 -$$

$$\left. \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) (a^2 d^2 \operatorname{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x])) \right) -$$

$$2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)$$

Problem 132: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{ag + b g x} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$-\frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2 \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{bg} + \frac{4B \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{bg} + \frac{8B^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{bg}$$

Result (type 4, 622 leaves):

$$\begin{aligned} & \frac{A^2 \operatorname{Log}[a+bx]}{bg} + \frac{1}{g} 2AB \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b} + \right. \\ & \left. \frac{\operatorname{Log}[a+bx] \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right)}{b} - \frac{2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} \right) + \\ & \frac{1}{g} B^2 \left(\frac{4 \operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3b} + \frac{\operatorname{Log}[a+bx] \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right)^2}{b} + 2 \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \right. \\ & \left. \operatorname{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right) \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b} - \frac{2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} \right) + \\ & \frac{8 \left(\frac{1}{2} \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] - \operatorname{PolyLog} \left[3, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} - \frac{1}{b} \\ & \left. 8 \left(\frac{1}{2} \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{bd \left(\frac{c+x}{d} \right)}{bc - ad} \right] \right) - \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, -\frac{d(a+bx)}{bc - ad} \right] + \operatorname{PolyLog} \left[3, -\frac{d(a+bx)}{bc - ad} \right] \right) \right) \end{aligned}$$

Problem 140: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Optimal (type 4, 91 leaves, 3 steps):

$$\frac{e^{\frac{A}{2B}} \sqrt{\frac{e (a+b x)^2}{(c+d x)^2}} (c+d x) \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{2B} \right]}{2B (b c - a d) g^2 (a+b x)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Problem 141: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Optimal (type 4, 149 leaves, 7 steps):

$$\frac{b e^{A/B} \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{B} \right]}{2B (b c - a d)^2 g^3} - \frac{d e^{\frac{A}{2B}} \sqrt{\frac{e (a+b x)^2}{(c+d x)^2}} (c+d x) \operatorname{ExpIntegralEi} \left[-\frac{A+B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right]}{2B} \right]}{2B (b c - a d)^2 g^3 (a+b x)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)} dx$$

Problem 145: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a+b x)^2}{(c+d x)^2} \right] \right)^2} dx$$

Optimal (type 4, 147 leaves, 4 steps):

$$-\frac{e^{\frac{A}{2B}} \sqrt{\frac{e^{(a+bx)^2}}{(c+dx)^2}} (c+dx) \operatorname{ExpIntegralEi}\left[-\frac{A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]}{2B}\right]}{4B^2 (bc-ad) g^2 (a+bx)} - \frac{c+dx}{2B (bc-ad) g^2 (a+bx) \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(ag+bx)^2 \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)^2} dx$$

Problem 146: Unable to integrate problem.

$$\int \frac{1}{(ag+bx)^3 \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)^2} dx$$

Optimal (type 4, 263 leaves, 9 steps):

$$-\frac{be^{A/B} \operatorname{ExpIntegralEi}\left[-\frac{A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]}{B}\right]}{2B^2 (bc-ad)^2 g^3} + \frac{de^{\frac{A}{2B}} \sqrt{\frac{e^{(a+bx)^2}}{(c+dx)^2}} (c+dx) \operatorname{ExpIntegralEi}\left[-\frac{A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]}{2B}\right]}{4B^2 (bc-ad)^2 g^3 (a+bx)} +$$

$$\frac{d(c+dx)}{2B (bc-ad)^2 g^3 (a+bx) \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)} - \frac{b(c+dx)^2}{2B (bc-ad)^2 g^3 (a+bx)^2 \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(ag+bx)^3 \left(A+B \operatorname{Log}\left[\frac{e^{(a+bx)^2}}{(c+dx)^2}\right]\right)^2} dx$$

Problem 156: Result more than twice size of optimal antiderivative.

$$\int (a+bx)^3 \left(A+B \operatorname{Log}\left[e^{(a+bx)^n} (c+dx)^{-n}\right]\right)^2 dx$$

Optimal (type 4, 322 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) n (a + bx)^3 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{6bd} + \frac{(a + bx)^4 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2}{4b} \\
& \frac{B (bc - ad)^2 n (a + bx)^2 (3A + Bn + 3B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{12bd^2} - \frac{B (bc - ad)^3 n (a + bx) (6A + 5Bn + 6B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{12bd^3} \\
& \frac{B (bc - ad)^4 n \operatorname{Log}\left[\frac{bc - ad}{b(c + dx)}\right] (6A + 11Bn + 6B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{12bd^4} - \frac{B^2 (bc - ad)^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{b(c + dx)}\right]}{2bd^4}
\end{aligned}$$

Result (type 4, 1709 leaves):

$$\begin{aligned}
& \frac{1}{12bd^4} \left(-24a^4ABd^4n + 6ab^3B^2c^3dn^2 - 24a^2b^2B^2c^2d^2n^2 + 36a^3bB^2cd^3n^2 - 24a^4B^2d^4n^2 + 12a^3A^2bd^4x - 6Ab^4Bc^3dnx + \right. \\
& 24aAb^3Bc^2d^2nx - 36a^2Ab^2Bcd^3nx + 18a^3AbBd^4nx - 5b^4B^2c^3d^2n^2x + 17ab^3B^2c^2d^2n^2x - 19a^2b^2B^2cd^3n^2x + 7a^3bB^2d^4n^2x + \\
& 18a^2A^2b^2d^4x^2 + 3Ab^4Bc^2d^2nx^2 - 12aAb^3Bcd^3nx^2 + 9a^2Ab^2Bd^4nx^2 + b^4B^2c^2d^2n^2x^2 - 2ab^3B^2cd^3n^2x^2 + a^2b^2B^2d^4n^2x^2 + \\
& 12aA^2b^3d^4x^3 - 2Ab^4Bcd^3nx^3 + 2aAb^3Bd^4nx^3 + 3A^2b^4d^4x^4 - 3a^4B^2d^4n^2 \operatorname{Log}[a + bx]^2 + 6Ab^4Bc^4n \operatorname{Log}[c + dx] - \\
& 24aAb^3Bc^3dn \operatorname{Log}[c + dx] + 36a^2Ab^2Bc^2d^2n \operatorname{Log}[c + dx] - 24a^3AbBcd^3n \operatorname{Log}[c + dx] + 11b^4B^2c^4n^2 \operatorname{Log}[c + dx] - \\
& 38ab^3B^2c^3dn^2 \operatorname{Log}[c + dx] + 45a^2b^2B^2c^2d^2n^2 \operatorname{Log}[c + dx] - 18a^3bB^2cd^3n^2 \operatorname{Log}[c + dx] - 24a^4B^2d^4n^2 \operatorname{Log}[c + dx] + \\
& 3b^4B^2c^4n^2 \operatorname{Log}[c + dx]^2 - 12ab^3B^2c^3dn^2 \operatorname{Log}[c + dx]^2 + 18a^2b^2B^2c^2d^2n^2 \operatorname{Log}[c + dx]^2 - 12a^3bB^2cd^3n^2 \operatorname{Log}[c + dx]^2 - \\
& 24a^4B^2d^4n \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 24a^3AbBd^4x \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - 6b^4B^2c^3dnx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + \\
& 24ab^3B^2c^2d^2nx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - 36a^2b^2B^2cd^3nx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 18a^3bB^2d^4nx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + \\
& 36a^2Ab^2Bd^4x^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 3b^4B^2c^2d^2nx^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - 12ab^3B^2cd^3nx^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + \\
& 9a^2b^2B^2d^4nx^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 24aAb^3Bd^4x^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - 2b^4B^2cd^3nx^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + \\
& 2ab^3B^2d^4nx^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 6Ab^4Bd^4x^4 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 6b^4B^2c^4n \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& 24ab^3B^2c^3dn \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 36a^2b^2B^2c^2d^2n \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& 24a^3bB^2cd^3n \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 12a^3bB^2d^4x \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + \\
& 18a^2b^2B^2d^4x^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + 12ab^3B^2d^4x^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + 3b^4B^2d^4x^4 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + \\
& Bn \operatorname{Log}[a + bx] \left(-6bBc (b^3c^3 - 4ab^2c^2d + 6a^2bcd^2 - 4a^3d^3) n \operatorname{Log}[c + dx] + 6B (bc - ad)^4 n \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + ad (-6b^3Bc^3n + \right. \\
& \left. 21ab^2Bc^2dn - 26a^2bBcd^2n + a^3d^3 (6A + 35Bn) + 6a^3Bd^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]) \right) + 6B^2 (bc - ad)^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \left. \right)
\end{aligned}$$

Problem 157: Result more than twice size of optimal antiderivative.

$$\int (a + bx)^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2 dx$$

Optimal (type 4, 263 leaves, 7 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) n (a + bx)^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{3bd} + \\
& \frac{(a + bx)^3 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2}{3b} + \frac{B (bc - ad)^2 n (a + bx) (2A + Bn + 2B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{3bd^2} + \\
& \frac{B (bc - ad)^3 n \operatorname{Log}\left[\frac{bc - ad}{b(c + dx)}\right] (2A + 3Bn + 2B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{3bd^3} + \frac{2B^2 (bc - ad)^3 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{b(c + dx)}\right]}{3bd^3}
\end{aligned}$$

Result (type 4, 1149 leaves):

$$\begin{aligned}
& \frac{1}{3bd^3} \left(-6a^3ABd^3n - 2ab^2B^2c^2dn^2 + 6a^2bB^2cd^2n^2 - 6a^3B^2d^3n^2 + 3a^2A^2bd^3x + 2Ab^3Bc^2dnx - 6aAb^2Bcd^2nx + 4a^2AbBd^3nx + \right. \\
& b^3B^2c^2dn^2x - 2ab^2B^2cd^2n^2x + a^2bB^2d^3n^2x + 3aA^2b^2d^3x^2 - Ab^3Bcd^2nx^2 + aAb^2Bd^3nx^2 + A^2b^3d^3x^3 - a^3B^2d^3n^2 \operatorname{Log}[a + bx]^2 - \\
& 2Ab^3Bc^3n \operatorname{Log}[c + dx] + 6aAb^2Bc^2dn \operatorname{Log}[c + dx] - 6a^2AbBcd^2n \operatorname{Log}[c + dx] - 3b^3B^2c^3n^2 \operatorname{Log}[c + dx] + 7ab^2B^2c^2dn^2 \operatorname{Log}[c + dx] - \\
& 4a^2bB^2cd^2n^2 \operatorname{Log}[c + dx] - 6a^3B^2d^3n^2 \operatorname{Log}[c + dx] - b^3B^2c^3n^2 \operatorname{Log}[c + dx]^2 + 3ab^2B^2c^2dn^2 \operatorname{Log}[c + dx]^2 - 3a^2bB^2cd^2n^2 \operatorname{Log}[c + dx]^2 - \\
& 6a^3B^2d^3n \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 6a^2AbBd^3x \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 2b^3B^2c^2dnx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& 6ab^2B^2cd^2nx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 4a^2bB^2d^3nx \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 6aAb^2Bd^3x^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& b^3B^2cd^2nx^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + ab^2B^2d^3nx^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 2Ab^3Bd^3x^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& 2b^3B^2c^3n \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 6ab^2B^2c^2dn \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] - \\
& 6a^2bB^2cd^2n \operatorname{Log}[c + dx] \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}] + 3a^2bB^2d^3x \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + 3ab^2B^2d^3x^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + \\
& b^3B^2d^3x^3 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]^2 + Bn \operatorname{Log}[a + bx] \left(2bBc (b^2c^2 - 3abcd + 3a^2d^2) n \operatorname{Log}[c + dx] - 2B (bc - ad)^3 n \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + \right. \\
& \left. ad (2b^2Bc^2n - 5abBcdn + a^2d^2 (2A + 9Bn) + 2a^2Bd^2 \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]) \right) - 2B^2 (bc - ad)^3 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \Big)
\end{aligned}$$

Problem 158: Result more than twice size of optimal antiderivative.

$$\int (a + bx) (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2 dx$$

Optimal (type 4, 195 leaves, 6 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) n (a + bx) (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{bd} + \frac{(a + bx)^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2}{2b} - \\
& \frac{B (bc - ad)^2 n \operatorname{Log}\left[\frac{bc - ad}{b(c + dx)}\right] (A + Bn + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{bd^2} - \frac{B^2 (bc - ad)^2 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{b(c + dx)}\right]}{bd^2}
\end{aligned}$$

Result (type 4, 656 leaves):

$$\begin{aligned}
& -\frac{2a^2ABn}{b} - \frac{2a^2B^2n^2}{b} + \frac{aB^2cn^2}{d} + aA^2x + aABnx - \frac{AbBcnx}{d} + \frac{1}{2}A^2bx^2 - \frac{a^2B^2n^2\text{Log}[a+bx]^2}{2b} + \frac{AbBc^2n\text{Log}[c+dx]}{d^2} - \\
& \frac{2aABcn\text{Log}[c+dx]}{d} - \frac{2a^2B^2n^2\text{Log}[c+dx]}{b} + \frac{bB^2c^2n^2\text{Log}[c+dx]}{d^2} - \frac{aB^2cn^2\text{Log}[c+dx]}{d} + \frac{bB^2c^2n^2\text{Log}[c+dx]^2}{2d^2} - \\
& \frac{aB^2cn^2\text{Log}[c+dx]^2}{d} - \frac{2a^2B^2n\text{Log}[e(a+bx)^n(c+dx)^{-n}]}{b} + 2aABx\text{Log}[e(a+bx)^n(c+dx)^{-n}] + aB^2nx\text{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& \frac{bB^2cnx\text{Log}[e(a+bx)^n(c+dx)^{-n}]}{d} + aABx^2\text{Log}[e(a+bx)^n(c+dx)^{-n}] + \frac{bB^2c^2n\text{Log}[c+dx]\text{Log}[e(a+bx)^n(c+dx)^{-n}]}{d^2} - \\
& \frac{2aB^2cn\text{Log}[c+dx]\text{Log}[e(a+bx)^n(c+dx)^{-n}]}{d} + aB^2x\text{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + \frac{1}{2}bB^2x^2\text{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + \frac{1}{bd^2}Bn\text{Log}[a+bx] \\
& \left(bBc(-bc+2ad)n\text{Log}[c+dx] + B(bc-ad)^2n\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + ad(-bBcn+ad(A+3Bn) + aBd\text{Log}[e(a+bx)^n(c+dx)^{-n}]) \right) + \\
& \frac{B^2(bc-ad)^2n^2\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{bd^2}
\end{aligned}$$

Problem 159: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B\text{Log}[e(a+bx)^n(c+dx)^{-n}])^2}{a+bx} dx$$

Optimal (type 4, 131 leaves, 5 steps):

$$-\frac{(A+B\text{Log}[e(a+bx)^n(c+dx)^{-n}])^2\text{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b} + \frac{2Bn(A+B\text{Log}[e(a+bx)^n(c+dx)^{-n}])\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b} + \frac{2B^2n^2\text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b}$$

Result (type 4, 443 leaves):

$$\begin{aligned}
& \frac{1}{3b} \left(B^2n^2\text{Log}[a+bx]^3 + 3Bn\text{Log}[a+bx]^2(A+B(-n\text{Log}[a+bx]+n\text{Log}[c+dx]+\text{Log}[e(a+bx)^n(c+dx)^{-n}]))) + 3\text{Log}[a+bx] \right. \\
& \left. (A+B(-n\text{Log}[a+bx]+n\text{Log}[c+dx]+\text{Log}[e(a+bx)^n(c+dx)^{-n}]))^2 - 6ABn \left(\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\
& 6B^2n(-n\text{Log}[a+bx]+n\text{Log}[c+dx]+\text{Log}[e(a+bx)^n(c+dx)^{-n}]) \left(\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) - \\
& 6B^2n^2 \left(\frac{1}{2}\text{Log}[a+bx]^2 \left(\text{Log}[c+dx] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - \text{Log}[a+bx] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 3B^2n^2 \left(\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx]^2 + 2\text{Log}[c+dx] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2\text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right)
\end{aligned}$$

Problem 164: Result more than twice size of optimal antiderivative.

$$\int (a + b x)^3 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3 dx$$

Optimal (type 4, 809 leaves, 27 steps):

$$\begin{aligned} & -\frac{B^3 (bc - ad)^3 n^3 x}{4 d^3} - \frac{B^3 (bc - ad)^4 n^3 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{4 b d^4} + \frac{3 B^3 (bc - ad)^4 n^3 \operatorname{Log}[c + d x]}{2 b d^4} - \frac{7 B^2 (bc - ad)^3 n^2 (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{4 b d^3} + \\ & \frac{b B^2 (bc - ad)^2 n^2 (c + d x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{4 d^4} - \frac{9 B^2 (bc - ad)^4 n^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{2 b d^4} - \\ & \frac{9 B (bc - ad)^3 n (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{4 b d^3} + \frac{9 b B (bc - ad)^2 n (c + d x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{8 d^4} - \\ & \frac{b^2 B (bc - ad) n (c + d x)^3 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{4 d^4} - \frac{3 B (bc - ad)^4 n \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{4 b d^4} + \\ & \frac{(a + b x)^4 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{4 b} + \frac{7 B^2 (bc - ad)^4 n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{4 b d^4} - \\ & \frac{9 B^3 (bc - ad)^4 n^3 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{2 b d^4} - \frac{3 B^2 (bc - ad)^4 n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{2 b d^4} - \\ & \frac{7 B^3 (bc - ad)^4 n^3 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{4 b d^4} + \frac{3 B^3 (bc - ad)^4 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{2 b d^4} \end{aligned}$$

Result (type 4, 6899 leaves):

$$\begin{aligned} & \frac{1}{8 b d^4} \left(12 a A b^3 B^2 c^3 d n^2 - 48 a^2 A b^2 B^2 c^2 d^2 n^2 + 60 a^3 A b B^2 c d^3 n^2 - 48 a^4 A B^2 d^4 n^2 - 12 b^4 B^3 c^4 n^3 + 58 a b^3 B^3 c^3 d n^3 - 100 a^2 b^2 B^3 c^2 d^2 n^3 + \right. \\ & 54 a^3 b B^3 c d^3 n^3 + 12 a^4 B^3 d^4 n^3 + 8 a^3 A^3 b d^4 x - 6 A^2 b^4 B c^3 d n x + 24 a A^2 b^3 B c^2 d^2 n x - 36 a^2 A^2 b^2 B c d^3 n x + 18 a^3 A^2 b B d^4 n x - \\ & 10 A b^4 B^2 c^3 d n^2 x + 34 a A b^3 B^2 c^2 d^2 n^2 x - 38 a^2 A b^2 B^2 c d^3 n^2 x + 14 a^3 A b B^2 d^4 n^2 x - 2 b^4 B^3 c^3 d n^3 x + 6 a b^3 B^3 c^2 d^2 n^3 x - \\ & 6 a^2 b^2 B^3 c d^3 n^3 x + 2 a^3 b B^3 d^4 n^3 x + 12 a^2 A^3 b^2 d^4 x^2 + 3 A^2 b^4 B c^2 d^2 n x^2 - 12 a A^2 b^3 B c d^3 n x^2 + 9 a^2 A^2 b^2 B d^4 n x^2 + 2 A b^4 B^2 c^2 d^2 n^2 x^2 - \\ & 4 a A b^3 B^2 c d^3 n^2 x^2 + 2 a^2 A b^2 B^2 d^4 n^2 x^2 + 8 a A^3 b^3 d^4 x^3 - 2 A^2 b^4 B c d^3 n x^3 + 2 a A^2 b^3 B d^4 n x^3 + 2 A^3 b^4 d^4 x^4 + 6 a^4 A^2 B d^4 n \operatorname{Log}[a + b x] - \\ & 12 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[a + b x] + 42 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] - 52 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[a + b x] + 22 a^4 A B^2 d^4 n^2 \operatorname{Log}[a + b x] - \\ & 22 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x] + 80 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x] - 94 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x] + 60 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x] - \\ & 6 a^4 A B^2 d^4 n^2 \operatorname{Log}[a + b x]^2 + 6 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x]^2 - 21 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x]^2 + 26 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x]^2 - \\ & 11 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x]^2 + 2 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x]^3 + 6 A^2 b^4 B c^4 n \operatorname{Log}[c + d x] - 24 a A^2 b^3 B c^3 d n \operatorname{Log}[c + d x] + \\ & 36 a^2 A^2 b^2 B c^2 d^2 n \operatorname{Log}[c + d x] - 24 a^3 A^2 b B c d^3 n \operatorname{Log}[c + d x] + 22 A b^4 B^2 c^4 n^2 \operatorname{Log}[c + d x] - 76 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[c + d x] + \\ & 90 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c + d x] - 36 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[c + d x] + 12 b^4 B^3 c^4 n^3 \operatorname{Log}[c + d x] - 26 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c + d x] - \\ & 8 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c + d x] + 46 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c + d x] - 48 a^4 B^3 d^4 n^3 \operatorname{Log}[c + d x] - 12 A b^4 B^2 c^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + \\ & 48 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 72 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 48 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + \\ & 12 a^4 A B^2 d^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 22 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 76 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - \end{aligned}$$

$$\begin{aligned}
& 90 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 36 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 6 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - \\
& 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] + 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - \\
& 12 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 12 a^4 A B^2 d^4 n^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] + 12 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] + \\
& 6 A b^4 B^2 c^4 n^2 \operatorname{Log}[c + d x]^2 - 24 A A b^3 B^2 c^3 d n^2 \operatorname{Log}[c + d x]^2 + 36 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c + d x]^2 - 24 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[c + d x]^2 + \\
& 11 b^4 B^3 c^4 n^3 \operatorname{Log}[c + d x]^2 - 38 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c + d x]^2 + 45 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c + d x]^2 - 18 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c + d x]^2 - \\
& 12 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 + 48 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 - 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 + \\
& 48 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 + 6 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 + 6 b^4 B^3 c^4 n^3 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 - \\
& 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 + 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 - 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 - \\
& 6 a^4 B^3 d^4 n^3 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 + 2 b^4 B^3 c^4 n^3 \operatorname{Log}[c + d x]^3 - 8 a b^3 B^3 c^3 d n^3 \operatorname{Log}[c + d x]^3 + 12 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[c + d x]^3 - \\
& 8 a^3 b B^3 c d^3 n^3 \operatorname{Log}[c + d x]^3 + 12 A b^4 B^2 c^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 48 a A b^3 B^2 c^3 d n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 72 a^2 A b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 48 a^3 A b B^2 c d^3 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 22 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 88 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 132 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 88 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 22 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 6 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 24 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 36 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 24 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 6 a^4 B^3 d^4 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 12 b^4 B^3 c^4 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 48 a b^3 B^3 c^3 d n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 48 a^3 b B^3 c d^3 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 12 a b^3 B^3 c^3 d n^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 48 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 60 a^3 b B^3 c d^3 n^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - \\
& 48 a^4 B^3 d^4 n^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 24 a^3 A^2 b B d^4 x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 12 A b^4 B^2 c^3 d n x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 48 a A b^3 B^2 c^2 d^2 n x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 72 a^2 A b^2 B^2 c d^3 n x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 36 a^3 A b B^2 d^4 n x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 10 b^4 B^3 c^3 d n^2 x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 34 a b^3 B^3 c^2 d^2 n^2 x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - \\
& 38 a^2 b^2 B^3 c d^3 n^2 x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 14 a^3 b B^3 d^4 n^2 x \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 36 a^2 A^2 b^2 B d^4 x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 6 A b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 24 A A b^3 B^2 c d^3 n x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 18 a^2 A b^2 B^2 d^4 n x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 2 b^4 B^3 c^2 d^2 n^2 x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 4 a b^3 B^3 c d^3 n^2 x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 2 a^2 b^2 B^3 d^4 n^2 x^2 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 24 a A^2 b^3 B d^4 x^3 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - 4 A b^4 B^2 c d^3 n x^3 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 4 a A b^3 B^2 d^4 n x^3 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + \\
& 6 A^2 b^4 B d^4 x^4 \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 12 a^4 A B^2 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - \\
& 12 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a + b x] \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 42 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] - \\
& 52 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] + 22 a^4 B^3 d^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[e(a + b x)^n (c + d x)^{-n}] -
\end{aligned}$$

$$\begin{aligned}
& 6 a^4 B^3 d^4 n^2 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 12 A b^4 B^2 c^4 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 48 a A b^3 B^2 c^3 d n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 72 a^2 A b^2 B^2 c^2 d^2 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 48 a^3 A b B^2 c d^3 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 22 b^4 B^3 c^4 n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 76 a b^3 B^3 c^3 d n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 90 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 36 a^3 b B^3 c d^3 n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 12 b^4 B^3 c^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + \\
& 48 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 72 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + \\
& 48 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 12 a^4 B^3 d^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 12 a^4 B^3 d^4 n^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 6 b^4 B^3 c^4 n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 24 a b^3 B^3 c^3 d n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 36 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 24 a^3 b B^3 c d^3 n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 12 b^4 B^3 c^4 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 48 a b^3 B^3 c^3 d n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + \\
& 72 a^2 b^2 B^3 c^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - \\
& 48 a^3 b B^3 c d^3 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 24 a^3 A b B^2 d^4 x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 6 b^4 B^3 c^3 d n x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 24 a b^3 B^3 c^2 d^2 n x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - 36 a^2 b^2 B^3 c d^3 n x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + \\
& 18 a^3 b B^3 d^4 n x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 36 a^2 A b^2 B^2 d^4 x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 3 b^4 B^3 c^2 d^2 n x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 12 a b^3 B^3 c d^3 n x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 9 a^2 b^2 B^3 d^4 n x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 24 a A b^3 B^2 d^4 x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 2 b^4 B^3 c d^3 n x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 2 a b^3 B^3 d^4 n x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 6 A b^4 B^2 d^4 x^4 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + \\
& 6 a^4 B^3 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 6 b^4 B^3 c^4 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 24 a b^3 B^3 c^3 d n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 36 a^2 b^2 B^3 c^2 d^2 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 24 a^3 b B^3 c d^3 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2 + 8 a^3 b B^3 d^4 x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + \\
& 12 a^2 b^2 B^3 d^4 x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + 8 a b^3 B^3 d^4 x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + 2 b^4 B^3 d^4 x^4 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + \\
& 2 B^2 n^2 (6 A b^4 c^4 - 24 a A b^3 c^3 d + 36 a^2 A b^2 c^2 d^2 - 24 a^3 A b c d^3 + 11 b^4 B c^4 n - 44 a b^3 B c^3 d n + 66 a^2 b^2 B c^2 d^2 n - 44 a^3 b B c d^3 n + 11 a^4 B d^4 n + \\
& 6 a^4 B d^4 n \operatorname{Log}[a + b x] + 6 b B c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) n \operatorname{Log}[c + d x] + 6 b^4 B c^4 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 24 a b^3 B c^3 d \operatorname{Log}\left[\right. \\
& \left. e (a + b x)^n (c + d x)^{-n}\right] + 36 a^2 b^2 B c^2 d^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 24 a^3 b B c d^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\
& 12 B^2 n^2 (a^4 B d^4 n \operatorname{Log}[a + b x] + b B c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) n \operatorname{Log}[c + d x] - a^4 d^4 (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])) \\
& \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 12 b^4 B^3 c^4 n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] + 48 a b^3 B^3 c^3 d n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - \\
& 72 a^2 b^2 B^3 c^2 d^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] + 48 a^3 b B^3 c d^3 n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 12 a^4 B^3 d^4 n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - \\
& 12 b^4 B^3 c^4 n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] + 48 a b^3 B^3 c^3 d n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] -
\end{aligned}$$

$$72 a^2 b^2 B^3 c^2 d^2 n^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 48 a^3 b B^3 c d^3 n^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 12 a^4 B^3 d^4 n^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]$$

Problem 165: Result more than twice size of optimal antiderivative.

$$\int (a+bx)^2 (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^3 dx$$

Optimal (type 4, 614 leaves, 17 steps):

$$\begin{aligned} & -\frac{B^3 (bc-ad)^3 n^3 \text{Log}[c+dx]}{bd^3} + \frac{B^2 (bc-ad)^2 n^2 (a+bx) (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{bd^2} + \\ & \frac{4B^2 (bc-ad)^3 n^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{bd^3} + \frac{2B (bc-ad)^2 n (a+bx) (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^2}{bd^2} - \\ & \frac{bB (bc-ad) n (c+dx)^2 (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^2}{2d^3} + \frac{B (bc-ad)^3 n \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^2}{bd^3} + \\ & \frac{(a+bx)^3 (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^3}{3b} - \frac{B^2 (bc-ad)^3 n^2 (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}]) \text{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{bd^3} + \\ & \frac{4B^3 (bc-ad)^3 n^3 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bd^3} + \frac{2B^2 (bc-ad)^3 n^2 (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}]) \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bd^3} + \\ & \frac{B^3 (bc-ad)^3 n^3 \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bd^3} - \frac{2B^3 (bc-ad)^3 n^3 \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{bd^3} \end{aligned}$$

Result (type 4, 4819 leaves):

$$\begin{aligned} & -\frac{6a^3 A B^2 n^2}{b} - \frac{2a A b B^2 c^2 n^2}{d^2} + \frac{4a^2 A B^2 c n^2}{d} + \frac{2a^3 B^3 n^3}{b} + \frac{2b^2 B^3 c^3 n^3}{d^3} - \frac{7a b B^3 c^2 n^3}{d^2} + \frac{5a^2 B^3 c n^3}{d} + a^2 A^3 x + 2a^2 A^2 B n x + \frac{A^2 b^2 B c^2 n x}{d^2} - \\ & \frac{3a A^2 b B c n x}{d} + a^2 A B^2 n^2 x + \frac{A b^2 B^2 c^2 n^2 x}{d^2} - \frac{2a A b B^2 c n^2 x}{d} + a A^3 b x^2 + \frac{1}{2} a A^2 b B n x^2 - \frac{A^2 b^2 B c n x^2}{2d} + \frac{1}{3} A^3 b^2 x^3 + \frac{a^3 A^2 B n \text{Log}[a+bx]}{b} + \\ & \frac{3a^3 A B^2 n^2 \text{Log}[a+bx]}{b} + \frac{2a A b B^2 c^2 n^2 \text{Log}[a+bx]}{d^2} - \frac{5a^2 A B^2 c n^2 \text{Log}[a+bx]}{d} + \frac{7a^3 B^3 n^3 \text{Log}[a+bx]}{b} + \frac{3a b B^3 c^2 n^3 \text{Log}[a+bx]}{d^2} - \\ & \frac{6a^2 B^3 c n^3 \text{Log}[a+bx]}{d} - \frac{a^3 A B^2 n^2 \text{Log}[a+bx]^2}{b} - \frac{3a^3 B^3 n^3 \text{Log}[a+bx]^2}{2b} - \frac{a b B^3 c^2 n^3 \text{Log}[a+bx]^2}{d^2} + \frac{5a^2 B^3 c n^3 \text{Log}[a+bx]^2}{2d} + \\ & \frac{a^3 B^3 n^3 \text{Log}[a+bx]^3}{3b} - \frac{A^2 b^2 B c^3 n \text{Log}[c+dx]}{d^3} + \frac{3a A^2 b B c^2 n \text{Log}[c+dx]}{d^2} - \frac{3a^2 A^2 B c n \text{Log}[c+dx]}{d} - \frac{3A b^2 B^2 c^3 n^2 \text{Log}[c+dx]}{d^3} + \\ & \frac{7a A b B^2 c^2 n^2 \text{Log}[c+dx]}{d^2} - \frac{4a^2 A B^2 c n^2 \text{Log}[c+dx]}{d} - \frac{6a^3 B^3 n^3 \text{Log}[c+dx]}{b} - \frac{b^2 B^3 c^3 n^3 \text{Log}[c+dx]}{d^3} + \frac{3a^2 B^3 c n^3 \text{Log}[c+dx]}{d} + \end{aligned}$$

$$\begin{aligned}
& \frac{2 a^3 A B^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{b} + \frac{2 A b^2 B^2 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \frac{6 a A b B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \\
& \frac{6 a^2 A B^2 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d} + \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^3} - \frac{7 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d^2} + \\
& \frac{4 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]}{d} - \frac{2 a^3 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{b} - \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^3} + \\
& \frac{3 a b B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d^2} - \frac{3 a^2 B^3 c n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}[c+d x]}{d} - \frac{2 a^3 A B^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} + \\
& \frac{2 a^3 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]}{b} - \frac{A b^2 B^2 c^3 n^2 \operatorname{Log}[c+d x]^2}{d^3} + \frac{3 a A b B^2 c^2 n^2 \operatorname{Log}[c+d x]^2}{d^2} - \frac{3 a^2 A B^2 c n^2 \operatorname{Log}[c+d x]^2}{d} - \\
& \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[c+d x]^2}{2 d^3} + \frac{7 a b B^3 c^2 n^3 \operatorname{Log}[c+d x]^2}{2 d^2} - \frac{2 a^2 B^3 c n^3 \operatorname{Log}[c+d x]^2}{d} + \frac{a^3 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{b} + \\
& \frac{2 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^3} - \frac{6 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x]^2}{d} - \\
& \frac{a^3 B^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{b} - \frac{b^2 B^3 c^3 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^3} + \frac{3 a b B^3 c^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d^2} - \\
& \frac{3 a^2 B^3 c n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2}{d} - \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[c+d x]^3}{3 d^3} + \frac{a b B^3 c^2 n^3 \operatorname{Log}[c+d x]^3}{d^2} - \frac{a^2 B^3 c n^3 \operatorname{Log}[c+d x]^3}{d} - \\
& \frac{2 A b^2 B^2 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{6 a A b B^2 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{6 a^2 A B^2 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \\
& \frac{3 a^3 B^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} - \frac{3 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{9 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
& \frac{9 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \frac{a^3 B^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} + \frac{b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \\
& \frac{3 a b B^3 c^2 n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} + \frac{3 a^2 B^3 c n^3 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{2 b^2 B^3 c^3 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
& \frac{6 a b B^3 c^2 n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{6 a^2 B^3 c n^3 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \frac{6 a^3 B^3 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} - \\
& \frac{2 a b B^3 c^2 n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{4 a^2 B^3 c n^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + 3 a^2 A^2 B x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] + \\
& \frac{4 a^2 A B^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{2 A b^2 B^2 c^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{6 a A b B^2 c n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
& \frac{a^2 B^3 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{b^2 B^3 c^2 n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{2 a b B^3 c n^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} +
\end{aligned}$$

$$\begin{aligned}
& 3 a A^2 b B x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right] + a A b B^2 n x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right] - \frac{A b^2 B^2 c n x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} + \\
& A^2 b^2 B x^3 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right] + \frac{2 a^3 A B^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{b} + \frac{3 a^3 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{b} + \\
& \frac{2 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} - \frac{5 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} - \\
& \frac{a^3 B^3 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{b} - \frac{2 A b^2 B^2 c^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^3} + \\
& \frac{6 a A b B^2 c^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} - \frac{6 a^2 A B^2 c n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} - \\
& \frac{3 b^2 B^3 c^3 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^3} + \frac{7 a b B^3 c^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} - \\
& \frac{4 a^2 B^3 c n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} + \frac{2 a^3 B^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{b} + \\
& \frac{2 b^2 B^3 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^3} - \frac{6 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} + \\
& \frac{6 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} - \frac{2 a^3 B^3 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{b} - \\
& \frac{b^2 B^3 c^3 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^3} + \frac{3 a b B^3 c^2 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} - \\
& \frac{3 a^2 B^3 c n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} - \frac{2 b^2 B^3 c^3 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^3} + \\
& \frac{6 a b B^3 c^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d^2} - \frac{6 a^2 B^3 c n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]}{d} + \\
& 3 a^2 A B^2 x \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2 + 2 a^2 B^3 n x \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2 + \frac{b^2 B^3 c^2 n x \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{d^2} - \\
& \frac{3 a b B^3 c n x \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{d} + 3 a A b B^2 x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2 + \frac{1}{2} a b B^3 n x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2 - \\
& \frac{b^2 B^3 c n x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{2 d} + A b^2 B^2 x^3 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2 + \frac{a^3 B^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{b} - \\
& \frac{b^2 B^3 c^3 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{d^3} + \frac{3 a b B^3 c^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{d^2} - \\
& \frac{3 a^2 B^3 c n \operatorname{Log}[c+d x] \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^2}{d} + a^2 B^3 x \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^3 + a b B^3 x^2 \operatorname{Log}\left[e (a+b x)^n (c+d x)^{-n}\right]^3 +
\end{aligned}$$

$$\frac{1}{3} b^2 B^3 x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 - \frac{1}{b d^3} B^2 n^2 (2 A b^3 c^3 - 6 a A b^2 c^2 d + 6 a^2 A b c d^2 + 3 b^3 B c^3 n - 9 a b^2 B c^2 d n + 9 a^2 b B c d^2 n - 3 a^3 B d^3 n - 2 a^3 B d^3 n \operatorname{Log}[a + b x] + 2 b B c (b^2 c^2 - 3 a b c d + 3 a^2 d^2) n \operatorname{Log}[c + d x] + 2 b^3 B c^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 6 a b^2 B c^2 d \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 6 a^2 b B c d^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - \frac{1}{b d^3} 2 B^2 n^2 (-a^3 B d^3 n \operatorname{Log}[a + b x] + b B c (b^2 c^2 - 3 a b c d + 3 a^2 d^2) n \operatorname{Log}[c + d x] + a^3 d^3 (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - \frac{2 a^3 B^3 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{b} + \frac{2 b^2 B^3 c^3 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^3} - \frac{6 a b B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d} - \frac{2 a^3 B^3 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b} + \frac{2 b^2 B^3 c^3 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d^3} - \frac{6 a b B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d^2} + \frac{6 a^2 B^3 c n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d}$$

Problem 166: Result more than twice size of optimal antiderivative.

$$\int (a + b x) (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])^3 dx$$

Optimal (type 4, 376 leaves, 11 steps):

$$\frac{3 B^2 (b c - a d)^2 n^2 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])}{b d^2} - \frac{3 B (b c - a d) n (a + b x) (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])^2}{2 b d} - \frac{3 B (b c - a d)^2 n \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])^2}{2 b d^2} + \frac{(a + b x)^2 (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])^3}{2 b} - \frac{3 B^3 (b c - a d)^2 n^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^2} - \frac{3 B^2 (b c - a d)^2 n^2 (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^2} + \frac{3 B^3 (b c - a d)^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{b d^2}$$

Result (type 4, 2998 leaves):

$$\frac{1}{2 b d^2} \left(-12 a^2 A B^2 d^2 n^2 - 6 b^2 B^3 c^2 n^3 + 6 a b B^3 c d n^3 + 6 a^2 B^3 d^2 n^3 + 2 a A^3 b d^2 x - 3 A^2 b^2 B c d n x + 3 a A^2 b B d^2 n x + A^3 b^2 d^2 x^2 + 3 a^2 A^2 B d^2 n \operatorname{Log}[a + b x] - 6 a A b B^2 c d n^2 \operatorname{Log}[a + b x] + 6 a^2 A B^2 d^2 n^2 \operatorname{Log}[a + b x] + 12 a^2 B^3 d^2 n^3 \operatorname{Log}[a + b x] - 3 a^2 A B^2 d^2 n^2 \operatorname{Log}[a + b x]^2 + 3 a b B^3 c d n^3 \operatorname{Log}[a + b x]^2 - 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a + b x]^2 + a^2 B^3 d^2 n^3 \operatorname{Log}[a + b x]^3 + 3 A^2 b^2 B c^2 n \operatorname{Log}[c + d x] - 6 a A^2 b B c d n \operatorname{Log}[c + d x] + 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[c + d x] - 6 a A b B^2 c d n^2 \operatorname{Log}[c + d x] - 12 a^2 B^3 d^2 n^3 \operatorname{Log}[c + d x] - 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 12 a A b B^2 c d n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 6 a^2 A B^2 d^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 6 a b B^3 c d n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 3 b^2 B^3 c^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 6 a b B^3 c d n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - \right)$$

$$\begin{aligned}
& 6 a^2 A B^2 d^2 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] + 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] + 3 A b^2 B^2 c^2 n^2 \operatorname{Log}[c+dx]^2 - \\
& 6 a A b B^2 c d n^2 \operatorname{Log}[c+dx]^2 + 3 b^2 B^3 c^2 n^3 \operatorname{Log}[c+dx]^2 - 3 a b B^3 c d n^3 \operatorname{Log}[c+dx]^2 - 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 + \\
& 12 a b B^3 c d n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 + 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 + 3 b^2 B^3 c^2 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 - \\
& 6 a b B^3 c d n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 - 3 a^2 B^3 d^2 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 + b^2 B^3 c^2 n^3 \operatorname{Log}[c+dx]^3 - \\
& 2 a b B^3 c d n^3 \operatorname{Log}[c+dx]^3 + 6 A b^2 B^2 c^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a A b B^2 c d n^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a b B^3 c d n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 6 a^2 B^3 d^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 3 b^2 B^3 c^2 n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 6 a b B^3 c d n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 3 a^2 B^3 d^2 n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 6 b^2 B^3 c^2 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a b B^3 c d n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 12 a^2 B^3 d^2 n^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 a A^2 b B d^2 x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - 6 A b^2 B^2 c d n x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + \\
& 6 a A b B^2 d^2 n x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 3 A^2 b^2 B d^2 x^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 a^2 A B^2 d^2 n \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6 a b B^3 c d n^2 \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 a^2 B^3 d^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 3 a^2 B^3 d^2 n^2 \operatorname{Log}[a+bx]^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 A b^2 B^2 c^2 n \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 12 a A b B^2 c d n \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 b^2 B^3 c^2 n^2 \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6 a b B^3 c d n^2 \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - 6 b^2 B^3 c^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + \\
& 12 a b B^3 c d n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 a^2 B^3 d^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6 a^2 B^3 d^2 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 3 b^2 B^3 c^2 n^2 \operatorname{Log}[c+dx]^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6 a b B^3 c d n^2 \operatorname{Log}[c+dx]^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 b^2 B^3 c^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 12 a b B^3 c d n^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6 a A b B^2 d^2 x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 - \\
& 3 b^2 B^3 c d n x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + 3 a b B^3 d^2 n x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + 3 A b^2 B^2 d^2 x^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + \\
& 3 a^2 B^3 d^2 n \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + 3 b^2 B^3 c^2 n \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 - \\
& 6 a b B^3 c d n \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + 2 a b B^3 d^2 x \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^3 + b^2 B^3 d^2 x^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^3 + \\
& 6 B^2 n^2 (A b^2 c^2 - 2 a A b c d + b^2 B c^2 n - 2 a b B c d n + a^2 B d^2 n + a^2 B d^2 n \operatorname{Log}[a+bx] + b B c (bc - 2 ad) n \operatorname{Log}[c+dx] + \\
& \quad b^2 B c^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - 2 a b B c d \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 6 B^2 n^2 (a^2 B d^2 n \operatorname{Log}[a+bx] + b B c (bc - 2 ad) n \operatorname{Log}[c+dx] - a^2 d^2 (A + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] -
\end{aligned}$$

$$6 b^2 B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 12 ab B^3 c d n^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 a^2 B^3 d^2 n^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] -$$

$$6 b^2 B^3 c^2 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 12 ab B^3 c d n^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 6 a^2 B^3 d^2 n^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]$$

Problem 167: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{a+bx} dx$$

Optimal (type 4, 186 leaves, 6 steps):

$$-\frac{(A + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^3 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b} + \frac{3 B n (A + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b} +$$

$$\frac{6 B^2 n^2 (A + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b} + \frac{6 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{b(c+dx)}{d(a+bx)}\right]}{b}$$

Result (type 4, 2513 leaves):

$$\frac{1}{4b} \left(4 A^3 \operatorname{Log}[a+bx] - 6 A^2 B n \operatorname{Log}[a+bx]^2 + 4 A B^2 n^2 \operatorname{Log}[a+bx]^3 - B^3 n^3 \operatorname{Log}[a+bx]^4 + \right.$$

$$B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^4 - 4 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] + 6 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^2 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^2 -$$

$$4 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^3 + B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^4 - 12 A B^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 +$$

$$12 B^3 n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}[c+dx]^2 + 12 A B^2 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 - 12 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 -$$

$$8 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^3 + 8 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^3 + 12 A^2 B n \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] -$$

$$12 A B^2 n^2 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 4 B^3 n^3 \operatorname{Log}[a+bx]^3 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 8 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^3 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] -$$

$$12 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^2 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 24 A B^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] -$$

$$24 B^3 n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 12 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] +$$

$$6 B^3 n^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]^2 + 12 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]^2 -$$

$$\begin{aligned}
& 18 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]^2 + 12 A^2 B \operatorname{Log}[a+bx] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] - \\
& 12 A B^2 n \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + 4 B^3 n^2 \operatorname{Log}[a+bx]^3 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] - \\
& 12 B^3 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + 12 B^3 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + \\
& 24 A B^2 n \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] - 12 B^3 n^2 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + \\
& 24 B^3 n^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + 12 A B^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]^2 - \\
& 6 B^3 n \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]^2 + 12 B^3 n \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]^2 + \\
& 4 B^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]^3 - 4 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^3 \operatorname{Log}\left[\frac{bc-ad}{bc+bdx}\right] + \\
& 12 B n \left(A^2 + B^2 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^2 + B^2 n^2 \operatorname{Log}[c+dx]^2 + 2 B^2 n^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \left(\operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] + \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2 A B \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] + \right. \\
& \quad \left. B^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]^2 + 2 B n \operatorname{Log}[c+dx] \left(A - B n \operatorname{Log}[a+bx] + B \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] \right) \right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 12 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right] + 12 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 24 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 12 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right]^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \\
& 24 A B^2 n^2 \operatorname{Log}[c+dx] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 24 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \\
& 12 B^3 n^3 \operatorname{Log}[c+dx]^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 24 B^3 n^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 24 B^3 n^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 24 B^3 n^2 \operatorname{Log}[c+dx] \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 24 A B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 24 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 24 B^3 n^2 \operatorname{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 24 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right] - \\
& 24 A B^2 n^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 24 B^3 n^3 \operatorname{Log}\left[-\frac{d(a+bx)}{b(c+dx)}\right] \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] -
\end{aligned}$$

$$24 B^3 n^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] - 24 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{d (a + b x)}{b (c + d x)}\right]$$

Problem 168: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(a + b x)^2} dx$$

Optimal (type 3, 184 leaves, 5 steps):

$$\frac{6 B^3 n^3 (c + d x)}{(b c - a d) (a + b x)} - \frac{6 B^2 n^2 (c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{(b c - a d) (a + b x)} - \frac{3 B n (c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(b c - a d) (a + b x)} - \frac{(c + d x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(b c - a d) (a + b x)}$$

Result (type 3, 524 leaves):

$$\frac{1}{b (b c - a d) (a + b x)} \left(-B^3 d n^3 (a + b x) \operatorname{Log}[a + b x]^3 + B^3 d n^3 (a + b x) \operatorname{Log}[c + d x]^3 + 3 B^2 d n^2 (a + b x) \operatorname{Log}[c + d x]^2 (A + B n + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) + 3 B^2 d n^2 (a + b x) \operatorname{Log}[a + b x]^2 (A + B n + B n \operatorname{Log}[c + d x] + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) + 3 B d n (a + b x) \operatorname{Log}[c + d x] (A^2 + 2 A B n + 2 B^2 n^2 + 2 B (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + B^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2) - (b c - a d) (A^3 + 3 A^2 B n + 6 A B^2 n^2 + 6 B^3 n^3 + 3 B (A^2 + 2 A B n + 2 B^2 n^2) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 3 B^2 (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + B^3 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^3) - 3 B d n (a + b x) \operatorname{Log}[a + b x] (A^2 + 2 A B n + 2 B^2 n^2 + B^2 n^2 \operatorname{Log}[c + d x]^2 + 2 B (A + B n) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + B^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 2 B n \operatorname{Log}[c + d x] (A + B n + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])) \right)$$

Problem 172: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])} dx$$

Optimal (type 4, 96 leaves, 4 steps):

$$\frac{e^{\frac{A}{B n}} (c + d x) (e (a + b x)^n (c + d x)^{-n})^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[-\frac{A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]}{B n}\right]}{B (b c - a d) g^2 n (a + b x)}$$

Result (type 8, 38 leaves):

$$\int \frac{1}{(a g + b g x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])} dx$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)^2 dx$$

Optimal (type 4, 503 leaves, 19 steps):

$$\begin{aligned} & \frac{13 B^2 (b c - a d)^4 g^4 x}{30 d^4} - \frac{7 B^2 (b c - a d)^3 g^4 (a + b x)^2}{60 b d^3} + \frac{B^2 (b c - a d)^2 g^4 (a + b x)^3}{30 b d^2} - \frac{5 B^2 (b c - a d)^5 g^4 \operatorname{Log}[a + b x]}{6 b d^5} - \\ & \frac{13 B^2 (b c - a d)^5 g^4 \operatorname{Log} \left[\frac{c + d x}{a + b x} \right]}{30 b d^5} + \frac{B (b c - a d)^3 g^4 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)}{5 b d^3} - \frac{2 B (b c - a d)^2 g^4 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)}{15 b d^2} + \\ & \frac{B (b c - a d) g^4 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)}{10 b d} - \frac{2 B (b c - a d)^4 g^4 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)}{5 d^5} + \\ & \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right)^2}{5 b} - \frac{2 B (b c - a d)^5 g^4 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)}{a + b x} \right] \right) \operatorname{Log} \left[1 - \frac{d (a + b x)}{b (c + d x)} \right]}{5 b d^5} + \frac{2 B^2 (b c - a d)^5 g^4 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{5 b d^5} \end{aligned}$$

Result (type 4, 2847 leaves):

$$\begin{aligned} & \frac{1}{60 b d^5} \\ & g^4 \left(24 b^5 B^2 c^5 - 144 a b^4 B^2 c^4 d + 360 a^2 b^3 B^2 c^3 d^2 - 480 a^3 b^2 B^2 c^2 d^3 + 336 a^4 b B^2 c d^4 - 96 a^5 B^2 d^5 - 24 A b^5 B c^4 d x + 26 b^5 B^2 c^4 d x + 120 a A b^4 B c^3 d^2 x - \right. \\ & 118 a b^4 B^2 c^3 d^2 x - 240 a^2 A b^3 B c^2 d^3 x + 204 a^2 b^3 B^2 c^2 d^3 x + 240 a^3 A b^2 B c d^4 x - 158 a^3 b^2 B^2 c d^4 x + 60 a^4 A^2 b d^5 x - 96 a^4 A b B d^5 x + \\ & 46 a^4 b B^2 d^5 x + 12 A b^5 B c^3 d^2 x^2 - 7 b^5 B^2 c^3 d^2 x^2 - 60 a A b^4 B c^2 d^3 x^2 + 27 a b^4 B^2 c^2 d^3 x^2 + 120 a^2 A b^3 B c d^4 x^2 - 33 a^2 b^3 B^2 c d^4 x^2 + \\ & 120 a^3 A^2 b^2 d^5 x^2 - 72 a^3 A b^2 B d^5 x^2 + 13 a^3 b^2 B^2 d^5 x^2 - 8 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 40 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + 120 a^2 A^2 b^3 d^5 x^3 - \\ & 32 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 6 A b^5 B c d^4 x^4 + 60 a A^2 b^4 d^5 x^4 - 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 + 24 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{a}{b} + x \right] - \\ & 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] - 240 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] + 96 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] + 12 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\ & 24 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right] + 120 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - 96 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\ & 12 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 60 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 60 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\ & 12 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + b x] - 52 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + b x] + 86 a^4 b B^2 c d^4 \operatorname{Log}[a + b x] - 24 a^5 A B d^5 \operatorname{Log}[a + b x] - 46 a^5 B^2 d^5 \operatorname{Log}[a + b x] - \\ & 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 24 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 24 A b^5 B c^5 \operatorname{Log}[c + d x] - \\ & 26 b^5 B^2 c^5 \operatorname{Log}[c + d x] - 120 a A b^4 B c^4 d \operatorname{Log}[c + d x] + 106 a b^4 B^2 c^4 d \operatorname{Log}[c + d x] + 240 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c + d x] - \end{aligned}$$

$$\begin{aligned}
& 152 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c + dx] - 240 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c + dx] + 72 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c + dx] + 120 a^4 A b B c d^4 \operatorname{Log}[c + dx] + \\
& 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] - 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] + 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] - \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] + 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] + \\
& 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - \\
& 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - \\
& 24 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 120 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 240 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 240 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + \\
& 120 a^4 A b B d^5 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 96 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 12 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 60 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + \\
& 120 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 240 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 72 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 8 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + \\
& 40 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 240 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 32 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + \\
& 120 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 24 a^5 B^2 d^5 \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + \\
& 24 b^5 B^2 c^5 \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - 120 a b^4 B^2 c^4 d \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] - \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 120 a^4 b B^2 c d^4 \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] + 60 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right]^2 + \\
& 120 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right]^2 + 120 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right]^2 + 60 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right]^2 - \\
& 24 b B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] - 24 a^5 B^2 d^5 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]
\end{aligned}$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^3 \left(A + B \operatorname{Log}\left[\frac{e(c + dx)}{a + bx}\right] \right)^2 dx$$

Optimal (type 4, 420 leaves, 15 steps):

$$\begin{aligned}
& - \frac{5 B^2 (b c - a d)^3 g^3 x}{12 d^3} + \frac{B^2 (b c - a d)^2 g^3 (a + b x)^2}{12 b d^2} + \frac{11 B^2 (b c - a d)^4 g^3 \operatorname{Log}[a + b x]}{12 b d^4} + \frac{5 B^2 (b c - a d)^4 g^3 \operatorname{Log}\left[\frac{c+d x}{a+b x}\right]}{12 b d^4} - \\
& \frac{B (b c - a d)^2 g^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)}{a+b x}\right]\right)}{4 b d^2} + \frac{B (b c - a d) g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)}{a+b x}\right]\right)}{6 b d} + \frac{B (b c - a d)^3 g^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (c+d x)}{a+b x}\right]\right)}{2 d^4} + \\
& \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)}{a+b x}\right]\right)^2}{4 b} + \frac{B (b c - a d)^4 g^3 \left(A + B \operatorname{Log}\left[\frac{e (c+d x)}{a+b x}\right]\right) \operatorname{Log}\left[1 - \frac{d (a+b x)}{b (c+d x)}\right]}{2 b d^4} - \frac{B^2 (b c - a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{2 b d^4}
\end{aligned}$$

Result (type 4, 2110 leaves):

$$\frac{1}{12 b d^4}$$

$$\begin{aligned}
& g^3 \left(-6 b^4 B^2 c^4 + 30 a b^3 B^2 c^3 d - 60 a^2 b^2 B^2 c^2 d^2 + 54 a^3 b B^2 c d^3 - 18 a^4 B^2 d^4 + 6 A b^4 B c^3 d x - 5 b^4 B^2 c^3 d x - 24 a A b^3 B c^2 d^2 x + 17 a b^3 B^2 c^2 d^2 x + 36 a^2 A \right. \\
& \quad b^2 B c d^3 x - 19 a^2 b^2 B^2 c d^3 x + 12 a^3 A^2 b d^4 x - 18 a^3 A b B d^4 x + 7 a^3 b B^2 d^4 x - 3 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + 12 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + \\
& \quad 18 a^2 A^2 b^2 d^4 x^2 - 9 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 2 A b^4 B c d^3 x^3 + 12 a A^2 b^3 d^4 x^3 - 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - 6 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& \quad 24 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 36 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 18 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 3 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& \quad 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& \quad 18 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] + 10 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] - 6 a^4 A B d^4 \operatorname{Log}[a + b x] - \\
& \quad 7 a^4 B^2 d^4 \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& \quad 6 A b^4 B c^4 \operatorname{Log}[c + d x] + 5 b^4 B^2 c^4 \operatorname{Log}[c + d x] + 24 a A b^3 B c^3 d \operatorname{Log}[c + d x] - 14 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] - 36 a^2 A b^2 B c^2 d^2 \operatorname{Log}[c + d x] + \\
& \quad 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] + 24 a^3 A b B c d^3 \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& \quad 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& \quad 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\
& \quad 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& \quad 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 6 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 24 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 36 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + \\
& \quad 24 a^3 A b B d^4 x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 18 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 3 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + \\
& \quad 36 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 9 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 24 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - \\
& \quad 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 6 a^4 B^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 6 b^4 B^2 c^4 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + \\
& \quad 24 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + 24 a^3 b B^2 c d^3 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] + \\
& \quad 12 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right]^2 + 18 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right]^2 + 12 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right]^2 + \\
& \quad \left. 6 b B^2 c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 6 a^4 B^2 d^4 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right)
\end{aligned}$$

Problem 184: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+d x)}}{a+b x} \right] \right)^2 dx$$

Optimal (type 4, 335 leaves, 11 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^2 g^2 x}{3 d^2} - \frac{B^2 (b c - a d)^3 g^2 \operatorname{Log}[a + b x]}{b d^3} - \frac{B^2 (b c - a d)^3 g^2 \operatorname{Log} \left[\frac{c+d x}{a+b x} \right]}{3 b d^3} + \\ & \frac{B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+d x)}}{a+b x} \right] \right)}{3 b d} - \frac{2 B (b c - a d)^2 g^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(c+d x)}}{a+b x} \right] \right)}{3 d^3} + \\ & \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(c+d x)}}{a+b x} \right] \right)^2}{3 b} - \frac{2 B (b c - a d)^3 g^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+d x)}}{a+b x} \right] \right) \operatorname{Log} \left[1 - \frac{d(a+b x)}{b(c+d x)} \right]}{3 b d^3} + \frac{2 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{b(c+d x)} \right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1398 leaves):

$$\begin{aligned}
& g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + 2 a^2 A B \left(\frac{(-b c + a d) (a d \operatorname{Log}[a + b x] - b c \operatorname{Log}[c + d x])}{b^2 c d - a b d^2} + x \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) + \right. \\
& 4 a A b B \left(-\frac{1}{2} (-b c + a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log}[a + b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log}[c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) + \\
& 2 A b^2 B \left(-\frac{(-b c + a d) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x])}{6 b^3 d^3 (b c - a d)} + \frac{1}{3} x^3 \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right] \right) + a^2 B^2 \\
& \left(x \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right]^2 - \frac{1}{b d (b c - a d)} (-b c + a d) \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \right. \\
& 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - 2 a d \\
& \left. \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (c + d x)}{a + b x}\right] + 2 b c \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e (c + d x)}{a + b x}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + 2 a \\
& b B^2 \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right]^2 + \frac{1}{2 b^2 d^2} \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - \right. \\
& b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 (a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x])) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (c + d x)}{a + b x}\right] \right) + \\
& \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) + \\
& b^2 B^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{c e + d e x}{a + b x}\right]^2 + \frac{1}{6 b^3 d^3} \left(-4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \right. \\
& 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (-b c + a d) \\
& \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (b c - a d) \left(d x (2 c - d x) + 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 c^2 \operatorname{Log}[c + d x] \right) + \\
& 2 (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x]) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (c + d x)}{a + b x}\right] \right) - \\
& \left. 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 185: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log}\left[\frac{e (c + d x)}{a + b x}\right] \right)^2 dx$$

Optimal (type 4, 202 leaves, 7 steps):

$$\frac{B^2 (bc - ad)^2 g \operatorname{Log}[a + bx]}{bd^2} + \frac{B (bc - ad) g (c + dx) \left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right)}{d^2} + \frac{g (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right)^2}{2b} +$$

$$\frac{B (bc - ad)^2 g \left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right) \operatorname{Log}\left[1 - \frac{d(a+bx)}{b(c+dx)}\right]}{bd^2} - \frac{B^2 (bc - ad)^2 g \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bd^2}$$

Result (type 4, 734 leaves):

$$\frac{1}{2bd^2} g \left(2aA^2bd^2x + A^2b^2d^2x^2 - 4aABd \left(ad \operatorname{Log}[a + bx] - b \left(c \operatorname{Log}[c + dx] + dx \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right) \right) \right) +$$

$$2AB \left(a^2d^2 \operatorname{Log}[a + bx] + b \left(-bc^2 \operatorname{Log}[c + dx] + dx \left(bc - ad + bdx \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right) \right) \right) +$$

$$2aB^2d \left(ad \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + bc \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2ad \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + 2ad \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - 2ad \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) +$$

$$2bc \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] - 2bc \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - 2bc \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2ad \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] +$$

$$2bc \operatorname{Log}[c + dx] \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] + bdx \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right]^2 - 2bc \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2ad \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) +$$

$$B^2 \left(2d(-bc+ad)(a+bx) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - a^2d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2b(bc-ad)(c+dx) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 +$$

$$b^2d^2x^2 \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right]^2 + 2(a^2d^2 \operatorname{Log}[a + bx] - b(d(-bc+ad)x + bc^2 \operatorname{Log}[c + dx])) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right) \right) +$$

$$2b^2c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + 2a^2d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right)$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right)^2}{ag + bgx} dx$$

Optimal (type 4, 128 leaves, 4 steps):

$$-\frac{\operatorname{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right)^2}{bg} - \frac{2B \left(A + B \operatorname{Log}\left[\frac{e^{-(c+dx)}}{a+bx}\right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bg} + \frac{2B^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bg}$$

Result (type 4, 454 leaves):

$$\begin{aligned} & \frac{1}{3 b g} \left(3 A^2 \operatorname{Log}[a + b x] - \right. \\ & 3 A B \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \operatorname{Log}[a + b x] \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) + \\ & B^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) \right) + \\ & 3 \operatorname{Log}[a + b x] \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] \right)^2 + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - \\ & 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(c + d x)}{a + b x}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) - \\ & \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \end{aligned}$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^4 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)^2 dx$$

Optimal (type 4, 515 leaves, 19 steps):

$$\begin{aligned} & \frac{26 B^2 (b c - a d)^4 g^4 x}{15 d^4} - \frac{7 B^2 (b c - a d)^3 g^4 (a + b x)^2}{15 b d^3} + \frac{2 B^2 (b c - a d)^2 g^4 (a + b x)^3}{15 b d^2} - \frac{10 B^2 (b c - a d)^5 g^4 \operatorname{Log}[a + b x]}{3 b d^5} - \\ & \frac{26 B^2 (b c - a d)^5 g^4 \operatorname{Log}\left[\frac{c + d x}{a + b x}\right]}{15 b d^5} + \frac{2 B (b c - a d)^3 g^4 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{5 b d^3} - \frac{4 B (b c - a d)^2 g^4 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{15 b d^2} + \\ & \frac{B (b c - a d) g^4 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{5 b d} - \frac{4 B (b c - a d)^4 g^4 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{5 d^5} + \\ & \frac{g^4 (a + b x)^5 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)^2}{5 b} - \frac{4 B (b c - a d)^5 g^4 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d(a + b x)}{b(c + d x)}\right]}{5 b d^5} + \frac{8 B^2 (b c - a d)^5 g^4 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{5 b d^5} \end{aligned}$$

Result (type 4, 2907 leaves):

$$\begin{aligned} & \frac{1}{15 b d^5} \\ & g^4 \left(24 b^5 B^2 c^5 - 144 a b^4 B^2 c^4 d + 360 a^2 b^3 B^2 c^3 d^2 - 480 a^3 b^2 B^2 c^2 d^3 + 336 a^4 b B^2 c d^4 - 96 a^5 B^2 d^5 - 12 A b^5 B c^4 d x + 26 b^5 B^2 c^4 d x + 60 a A b^4 B c^3 d^2 x - \right. \\ & \left. 118 a b^4 B^2 c^3 d^2 x - 120 a^2 A b^3 B c^2 d^3 x + 204 a^2 b^3 B^2 c^2 d^3 x + 120 a^3 A b^2 B c d^4 x - 158 a^3 b^2 B^2 c d^4 x + 15 a^4 A^2 b d^5 x - 48 a^4 A b B d^5 x + \right. \end{aligned}$$

$$\begin{aligned}
& 46 a^4 b B^2 d^5 x + 6 A b^5 B c^3 d^2 x^2 - 7 b^5 B^2 c^3 d^2 x^2 - 30 a A b^4 B c^2 d^3 x^2 + 27 a b^4 B^2 c^2 d^3 x^2 + 60 a^2 A b^3 B c d^4 x^2 - 33 a^2 b^3 B^2 c d^4 x^2 + \\
& 30 a^3 A^2 b^2 d^5 x^2 - 36 a^3 A b^2 B d^5 x^2 + 13 a^3 b^2 B^2 d^5 x^2 - 4 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 20 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + 30 a^2 A^2 b^3 d^5 x^3 - \\
& 16 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 3 A b^5 B c d^4 x^4 + 15 a A^2 b^4 d^5 x^4 - 3 a A b^4 B d^5 x^4 + 3 A^2 b^5 d^5 x^5 + 24 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
& 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] - 240 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 96 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
& 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 96 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 12 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 60 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 60 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 12 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + b x] - 52 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + b x] + 86 a^4 b B^2 c d^4 \operatorname{Log}[a + b x] - 12 a^5 A B d^5 \operatorname{Log}[a + b x] - 46 a^5 B^2 d^5 \operatorname{Log}[a + b x] - \\
& 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 24 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 12 A b^5 B c^5 \operatorname{Log}[c + d x] - \\
& 26 b^5 B^2 c^5 \operatorname{Log}[c + d x] - 60 a A b^4 B c^4 d \operatorname{Log}[c + d x] + 106 a b^4 B^2 c^4 d \operatorname{Log}[c + d x] + 120 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c + d x] - 152 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c + d x] - \\
& 120 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c + d x] + 72 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c + d x] + 60 a^4 A b B c d^4 \operatorname{Log}[c + d x] + 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 24 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 120 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 240 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 240 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 120 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 12 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + \\
& 60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 120 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 120 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + \\
& 30 a^4 A b B d^5 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 48 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 6 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 30 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + \\
& 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 36 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 4 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + \\
& 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 60 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 16 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 3 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + \\
& 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 3 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 6 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 12 a^5 B^2 d^5 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] +
\end{aligned}$$

$$\begin{aligned}
& 12 b^5 B^2 c^5 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - 60 a b^4 B^2 c^4 d \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 120 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] - \\
& 120 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 60 a^4 b B^2 c d^4 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] + 15 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right]^2 + \\
& 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right]^2 + 30 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right]^2 + 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right]^2 + 3 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right]^2 - \\
& 24 b B^2 c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 24 a^5 B^2 d^5 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]
\end{aligned}$$

Problem 211: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)^2 dx$$

Optimal (type 4, 422 leaves, 15 steps):

$$\begin{aligned}
& -\frac{5 B^2 (b c - a d)^3 g^3 x}{3 d^3} + \frac{B^2 (b c - a d)^2 g^3 (a + b x)^2}{3 b d^2} + \frac{11 B^2 (b c - a d)^4 g^3 \operatorname{Log}[a + b x]}{3 b d^4} + \frac{5 B^2 (b c - a d)^4 g^3 \operatorname{Log}\left[\frac{c + d x}{a + b x}\right]}{3 b d^4} - \\
& \frac{B (b c - a d)^2 g^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{2 b d^2} + \frac{B (b c - a d) g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{3 b d} + \frac{B (b c - a d)^3 g^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)}{d^4} + \\
& \frac{g^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right)^2}{4 b} + \frac{B (b c - a d)^4 g^3 \left(A + B \operatorname{Log}\left[\frac{e(c + d x)^2}{(a + b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d(a + b x)}{b(c + d x)}\right]}{b d^4} - \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{b d^4}
\end{aligned}$$

Result (type 4, 2127 leaves):

$$\begin{aligned}
& g^3 \left(-\frac{6 a^4 B^2}{b} - \frac{2 b^3 B^2 c^4}{d^4} + \frac{10 a b^2 B^2 c^3}{d^3} - \frac{20 a^2 b B^2 c^2}{d^2} + \frac{18 a^3 B^2 c}{d} + a^3 A^2 x - 3 a^3 A B x + \frac{7}{3} a^3 B^2 x + \frac{A b^3 B c^3 x}{d^3} - \frac{5 b^3 B^2 c^3 x}{3 d^3} - \frac{4 a A b^2 B c^2 x}{d^2} + \right. \\
& \frac{17 a b^2 B^2 c^2 x}{3 d^2} + \frac{6 a^2 A b B c x}{d} - \frac{19 a^2 b B^2 c x}{3 d} + \frac{3}{2} a^2 A^2 b x^2 - \frac{3}{2} a^2 A b B x^2 + \frac{1}{3} a^2 b B^2 x^2 - \frac{A b^3 B c^2 x^2}{2 d^2} + \frac{b^3 B^2 c^2 x^2}{3 d^2} + \frac{2 a A b^2 B c x^2}{d} - \frac{2 a b^2 B^2 c x^2}{3 d} \\
& \left. + a A^2 b^2 x^3 - \frac{1}{3} a A b^2 B x^3 + \frac{A b^3 B c x^3}{3 d} + \frac{1}{4} A^2 b^3 x^4 + \frac{6 a^4 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{b} - \frac{2 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^3} + \frac{8 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{d^2} - \frac{12 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b} + x\right]}{d} + \right. \\
& \left. \frac{a^4 B^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^3} + \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2} - \frac{6 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d} + x\right]}{d} - \frac{b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{4 a^2 b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^3} - \frac{6 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^2} + \frac{4 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d} - \frac{a^4 A B \operatorname{Log}[a+b x]}{b} - \frac{7 a^4 B^2 \operatorname{Log}[a+b x]}{3 b} - \frac{a^2 b B^2 c^2 \operatorname{Log}[a+b x]}{d^2} + \\
& \frac{10 a^3 B^2 c \operatorname{Log}[a+b x]}{3 d} - \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]}{b} + \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]}{b} - \frac{2 a^4 B^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]}{b} - \\
& \frac{A b^3 B c^4 \operatorname{Log}[c+d x]}{d^4} + \frac{5 b^3 B^2 c^4 \operatorname{Log}[c+d x]}{3 d^4} + \frac{4 a A b^2 B c^3 \operatorname{Log}[c+d x]}{d^3} - \frac{14 a b^2 B^2 c^3 \operatorname{Log}[c+d x]}{3 d^3} - \frac{6 a^2 A b B c^2 \operatorname{Log}[c+d x]}{d^2} + \\
& \frac{3 a^2 b B^2 c^2 \operatorname{Log}[c+d x]}{d^2} + \frac{4 a^3 A B c \operatorname{Log}[c+d x]}{d} - \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^4} + \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^3} - \\
& \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d^2} + \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]}{d} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^3} + \\
& \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d^2} - \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]}{d} + \frac{2 b^3 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^4} - \frac{8 a b^2 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
& \frac{12 a^2 b B^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{8 a^3 B^2 c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + 2 a^3 A B x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - 3 a^3 B^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \\
& \frac{b^3 B^2 c^3 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^3} - \frac{4 a b^2 B^2 c^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^2} + \frac{6 a^2 b B^2 c x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + 3 a^2 A b B x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
& \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \frac{b^3 B^2 c^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{2 d^2} + \frac{2 a b^2 B^2 c x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + 2 a A b^2 B x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \\
& \frac{1}{3} a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] + \frac{b^3 B^2 c x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{3 d} + \frac{1}{2} A b^3 B x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right] - \frac{a^4 B^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{b} - \\
& \frac{b^3 B^2 c^4 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^4} + \frac{4 a b^2 B^2 c^3 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^3} - \frac{6 a^2 b B^2 c^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d^2} + \\
& \frac{4 a^3 B^2 c \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]}{d} + a^3 B^2 x \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \frac{3}{2} a^2 b B^2 x^2 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + a b^2 B^2 x^3 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \\
& \left. \frac{1}{4} b^3 B^2 x^4 \operatorname{Log}\left[\frac{e(c+d x)^2}{(a+b x)^2}\right]^2 + \frac{2 B^2 c\left(b^3 c^3-4 a b^2 c^2 d+6 a^2 b c d^2-4 a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-2 a^4 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{d^4} - \frac{2 a^4 B^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b} \right)
\end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)^2 dx$$

Optimal (type 4, 343 leaves, 11 steps):

$$\begin{aligned} & \frac{4 B^2 (b c - a d)^2 g^2 x}{3 d^2} - \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}[a + b x]}{b d^3} - \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}\left[\frac{c + d x}{a + b x}\right]}{3 b d^3} + \\ & \frac{2 B (b c - a d) g^2 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right)}{3 b d} - \frac{4 B (b c - a d)^2 g^2 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right)}{3 d^3} + \\ & \frac{g^2 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right)^2}{3 b} - \frac{4 B (b c - a d)^3 g^2 \left(A + B \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right) \operatorname{Log}\left[1 - \frac{d (a + b x)}{b (c + d x)}\right]}{3 b d^3} + \frac{8 B^2 (b c - a d)^3 g^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{3 b d^3} \end{aligned}$$

Result (type 4, 1458 leaves):

$$\begin{aligned}
& g^2 \left(a^2 A^2 x + a A^2 b x^2 + \frac{1}{3} A^2 b^2 x^3 + 2 a^2 A B \left(\frac{2 (-b c + a d) (a d \operatorname{Log}[a + b x] - b c \operatorname{Log}[c + d x])}{b^2 c d - a b d^2} + x \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + \right. \\
& 4 a A b B \left(-(-b c + a d) \left(\frac{x}{b d} + \frac{a^2 \operatorname{Log}[a + b x]}{b^2 (b c - a d)} - \frac{c^2 \operatorname{Log}[c + d x]}{d^2 (b c - a d)} \right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + \\
& 2 A b^2 B \left(-\frac{(-b c + a d) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x])}{3 b^3 d^3 (b c - a d)} + \frac{1}{3} x^3 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right] \right) + \\
& a^2 B^2 \left(x \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right]^2 + \frac{1}{b d} 4 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \right. \\
& 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - \\
& \left. \left. a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] + b c \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) + \\
& 2 a b B^2 \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right]^2 + \frac{1}{b^2 d^2} 2 \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) - a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
& 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& \left. \left. (a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x])) \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right) \right) \right) + \\
& 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) + \\
& b^2 B^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{c^2 e + 2 c d e x + d^2 e x^2}{(a + b x)^2}\right]^2 + \frac{1}{3 b^3 d^3} 2 \left(-4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) + 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \right. \right. \\
& 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) + 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (-b c + a d) \\
& \left. \left. \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (b c - a d) \left(d x (2 c - d x) + 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 c^2 \operatorname{Log}[c + d x] \right) \right) \right) + \\
& (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x]) \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (c + d x)^2}{(a + b x)^2}\right] \right) - \\
& \left. \left. 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \right)
\end{aligned}$$

Problem 213: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)^2 dx$$

Optimal (type 4, 211 leaves, 7 steps):

$$\frac{4 B^2 (b c - a d)^2 g \operatorname{Log}[a + b x]}{b d^2} + \frac{2 B (b c - a d) g (c + d x) \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)}{d^2} + \frac{g (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)^2}{2 b} +$$

$$\frac{2 B (b c - a d)^2 g \left(A + B \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right) \operatorname{Log} \left[1 - \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2} - \frac{4 B^2 (b c - a d)^2 g \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d^2}$$

Result (type 4, 754 leaves):

$$g \left(a A^2 x + \frac{1}{2} A^2 b x^2 + \frac{2 a A B \left(-2 a d \operatorname{Log}[a + b x] + 2 b c \operatorname{Log}[c + d x] + b d x \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)}{b d} \right) +$$

$$A B \left(\frac{2 a^2 \operatorname{Log}[a + b x]}{b} + \frac{-2 b c^2 \operatorname{Log}[c + d x] + d x \left(2 b c - 2 a d + b d x \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right)}{d^2} \right) +$$

$$\frac{1}{b d} a B^2 \left(4 a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 8 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) +$$

$$8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 4 a d \operatorname{Log}[a + b x] \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] +$$

$$4 b c \operatorname{Log}[c + d x] \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] + b d x \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right]^2 - 8 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 8 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) +$$

$$b B^2 \left(\frac{1}{2} x^2 \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right]^2 + \frac{1}{b^2 d^2} 2 \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \right.$$

$$b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \left. \left(a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x]) \right) \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (c + d x)^2}{(a + b x)^2} \right] \right) \right) +$$

$$2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right)$$

Problem 214: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e^{-(c+dx)^2}}{(a+bx)^2} \right] \right)^2}{ag + b gx} dx$$

Optimal (type 4, 132 leaves, 4 steps):

$$\frac{\operatorname{Log} \left[-\frac{bc-ad}{d(a+bx)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{-(c+dx)^2}}{(a+bx)^2} \right] \right)^2}{bg} - \frac{4B \left(A + B \operatorname{Log} \left[\frac{e^{-(c+dx)^2}}{(a+bx)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{bg} + \frac{8B^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{bg}$$

Result (type 4, 624 leaves):

$$\begin{aligned} & \frac{A^2 \operatorname{Log}[a+bx]}{bg} + \frac{1}{g} 2AB \left(-\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b} + \right. \\ & \left. \frac{\operatorname{Log}[a+bx] \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 e x^2}{(a+bx)^2} \right] \right)}{b} + \frac{2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} \right) + \\ & \frac{1}{g} B^2 \left(\frac{4 \operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3b} + \frac{\operatorname{Log}[a+bx] \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 e x^2}{(a+bx)^2} \right] \right)^2}{b} + 2 \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \right. \right. \\ & \left. \left. \operatorname{Log} \left[\frac{c^2 e}{(a+bx)^2} + \frac{2cdex}{(a+bx)^2} + \frac{d^2 e x^2}{(a+bx)^2} \right] \right) \left(-\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b} + \frac{2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} \right) \right) + \\ & \frac{8 \left(\frac{1}{2} \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] - \operatorname{PolyLog} \left[3, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} - \frac{1}{b} \\ & \left. \left. 8 \left(\frac{1}{2} \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{bd \left(\frac{c+x}{d} \right)}{bc-ad} \right] \right) - \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, -\frac{d(a+bx)}{bc-ad} \right] + \operatorname{PolyLog} \left[3, -\frac{d(a+bx)}{bc-ad} \right] \right) \right) \right) \end{aligned}$$

Problem 222: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right] \right)} dx$$

Optimal (type 4, 91 leaves, 3 steps):

$$\frac{e^{-\frac{A}{2B}} (c + dx) \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right]}{2B} \right]}{2B (bc - ad) g^2 (a + bx) \sqrt{\frac{e^{(c+dx)^2}}{(a+bx)^2}}}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right] \right)} dx$$

Problem 223: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right] \right)} dx$$

Optimal (type 4, 151 leaves, 7 steps):

$$\frac{d e^{-\frac{A}{2B}} (c + dx) \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right]}{2B} \right]}{2B (bc - ad)^2 g^3 (a + bx) \sqrt{\frac{e^{(c+dx)^2}}{(a+bx)^2}}} - \frac{b e^{-\frac{A}{B}} \operatorname{ExpIntegralEi} \left[\frac{A+B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right]}{B} \right]}{2B (bc - ad)^2 e g^3}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right] \right)} dx$$

Problem 227: Unable to integrate problem.

$$\int \frac{1}{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(c+dx)^2}}{(a+bx)^2} \right] \right)^2} dx$$

Optimal (type 4, 147 leaves, 4 steps):

$$-\frac{e^{-\frac{A}{2B}} (c+dx) \operatorname{ExpIntegralEi}\left[\frac{A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]}{2B}\right]}{4B^2 (bc-ad) g^2 (a+bx) \sqrt{\frac{e^{(c+dx)^2}}{(a+bx)^2}}} + \frac{c+dx}{2B (bc-ad) g^2 (a+bx) \left(A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]\right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(ag+bgx)^2 \left(A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]\right)^2} dx$$

Problem 228: Unable to integrate problem.

$$\int \frac{1}{(ag+bgx)^3 \left(A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]\right)^2} dx$$

Optimal (type 4, 206 leaves, 10 steps):

$$\frac{d e^{-\frac{A}{2B}} (c+dx) \operatorname{ExpIntegralEi}\left[\frac{A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]}{2B}\right]}{4B^2 (bc-ad)^2 g^3 (a+bx) \sqrt{\frac{e^{(c+dx)^2}}{(a+bx)^2}}} - \frac{b e^{-\frac{A}{B}} \operatorname{ExpIntegralEi}\left[\frac{A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]}{B}\right]}{2B^2 (bc-ad)^2 e g^3} + \frac{c+dx}{2B (bc-ad) g^3 (a+bx)^2 \left(A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]\right)}$$

Result (type 8, 36 leaves):

$$\int \frac{1}{(ag+bgx)^3 \left(A+B \operatorname{Log}\left[\frac{e^{(c+dx)^2}}{(a+bx)^2}\right]\right)^2} dx$$

Problem 229: Unable to integrate problem.

$$\int \frac{1}{(ag+bgx)^2 \left(A+B \operatorname{Log}\left[e^{(a+bx)^n} (c+dx)^{-n}\right]\right)} dx$$

Optimal (type 4, 96 leaves, 4 steps):

$$\frac{e^{\frac{A}{Bn}} (c+dx) \left(e^{(a+bx)^n} (c+dx)^{-n}\right)^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[-\frac{A+B \operatorname{Log}\left[e^{(a+bx)^n} (c+dx)^{-n}\right]}{Bn}\right]}{B (bc-ad) g^2 n (a+bx)}$$

Result (type 8, 38 leaves):

$$\int \frac{1}{(a g + b g x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])} dx$$

Problem 240: Result more than twice size of optimal antiderivative.

$$\int (f + g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 874 leaves, 15 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^3 g^3 x}{6 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^2 (4 b d f - 3 b c g - a d g) x}{4 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^3 (c + d x)^2}{12 b^2 d^4} + \\ & \frac{B^2 (b c - a d)^4 g^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{6 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{4 b^4 d^4} - \frac{1}{2 b^4 d^3} \\ & B (b c - a d) g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) - \\ & \frac{B (b c - a d) g^2 (4 b d f - 3 b c g - a d g) (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{4 b^2 d^4} - \frac{B (b c - a d) g^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{6 b d^4} - \frac{1}{2 b^4 d^4} \\ & B (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) - \\ & \frac{(b f - a g)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{4 b^4 g} + \frac{(f + g x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{4 g} + \frac{B^2 (b c - a d)^4 g^3 \operatorname{Log} [c + d x]}{6 b^4 d^4} + \\ & \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} [c + d x]}{4 b^4 d^4} + \frac{B^2 (b c - a d)^2 g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) \operatorname{Log} [c + d x]}{2 b^4 d^4} - \\ & \frac{1}{2 b^4 d^4} B^2 (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right] \end{aligned}$$

Result (type 4, 2229 leaves):

$$\begin{aligned} & A^2 f^3 x + \frac{3}{2} A^2 f^2 g x^2 + A^2 f g^2 x^3 + \frac{1}{4} A^2 g^3 x^4 + \frac{2 A B f^3 (a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - b c \operatorname{Log} [c + d x])}{b d} + \\ & \frac{1}{12} A B g^3 \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \frac{2 c x^3}{d} - \frac{6 a^4 \operatorname{Log} [a + b x]}{b^4} + 6 x^4 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + \frac{6 c^4 \operatorname{Log} [c + d x]}{d^4} \right) + \\ & A B f g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + 2 x^3 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) + \end{aligned}$$

$$\begin{aligned}
& \frac{3 A B f^2 g \left(-a^2 d^2 \operatorname{Log}[a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + b c^2 \operatorname{Log}[c + d x] \right) \right)}{b^2 d^2} + \\
& \frac{1}{b d} B^2 f^3 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& \quad 2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + b d x \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& \quad \left. 2 b c \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
& \frac{1}{12} B^2 g^3 \left(3 x^4 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 + \frac{1}{b^4 d^4} \left(-6 b^4 c^4 + 6 a b^3 c^3 d + 6 a^3 b c d^3 - 6 a^4 d^4 - 5 b^4 c^3 d x + 5 a b^3 c^2 d^2 x + 5 a^2 b^2 c d^3 x - 5 a^3 b d^4 x + \right. \right. \\
& \quad b^4 c^2 d^2 x^2 - 2 a b^3 c d^3 x^2 + a^2 b^2 d^4 x^2 - 6 a b^3 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^4 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] - 3 a^4 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^4 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& \quad 6 a^3 b c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 b^4 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^2 b^2 c^2 d^2 \operatorname{Log}[a + b x] - 2 a^3 b c d^3 \operatorname{Log}[a + b x] + 5 a^4 d^4 \operatorname{Log}[a + b x] + \\
& \quad 6 a^4 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 6 a^4 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 6 a^4 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 6 b^4 c^3 d x \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + \\
& \quad 6 a^3 b d^4 x \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + 3 b^4 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] - 3 a^2 b^2 d^4 x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] - 2 b^4 c d^3 x^3 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + \\
& \quad 2 a b^3 d^4 x^3 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] - 6 a^4 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] + 5 b^4 c^4 \operatorname{Log}[c + d x] - 2 a b^3 c^3 d \operatorname{Log}[c + d x] - \\
& \quad 3 a^2 b^2 c^2 d^2 \operatorname{Log}[c + d x] - 6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 6 b^4 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 b^4 c^4 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \operatorname{Log}[c + d x] + \\
& \quad \left. \left. 6 b^4 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 6 b^4 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 a^4 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) + \\
& \frac{3}{2} B^2 f^2 g \left(x^2 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 - \frac{1}{b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \right. \\
& \quad \left. \left. b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x]) \right) - \right. \right. \\
& \quad \left. \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) + \\
& 3 B^2 f g^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
& \quad 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& \quad \left. \left. d^2 (b c - a d) \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - \right. \right.
\end{aligned}$$

$$2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]) +$$

$$4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right)$$

Problem 241: Result more than twice size of optimal antiderivative.

$$\int (f + g x)^2 \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 532 leaves, 12 steps):

$$\frac{B^2 (b c - a d)^2 g^2 x}{3 b^2 d^2} + \frac{B^2 (b c - a d)^3 g^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]}{3 b^3 d^3} -$$

$$\frac{2 B (b c - a d) g (3 b d f - 2 b c g - a d g) (a + b x) \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b^3 d^2} - \frac{B (b c - a d) g^2 (c + d x)^2 \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b d^3} +$$

$$\frac{1}{3 b^3 d^3} 2 B (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) \text{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) -$$

$$\frac{(b f - a g)^3 \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{3 b^3 g} + \frac{(f + g x)^3 \left(A + B \text{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{3 g} +$$

$$\frac{B^2 (b c - a d)^3 g^2 \text{Log} [c + d x]}{3 b^3 d^3} + \frac{2 B^2 (b c - a d)^2 g (3 b d f - 2 b c g - a d g) \text{Log} [c + d x]}{3 b^3 d^3} +$$

$$\frac{2 B^2 (b c - a d) (a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2)) \text{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{3 b^3 d^3}$$

Result (type 4, 1294 leaves):

$$\begin{aligned}
& A^2 f^2 x + A^2 f g x^2 + \frac{1}{3} A^2 g^2 x^3 + \frac{2 A B f^2 \left(a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - b c \operatorname{Log}[c + d x] \right)}{b d} + \\
& \frac{1}{3} A B g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log}[a + b x]}{b^3} + 2 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \frac{2 c^3 \operatorname{Log}[c + d x]}{d^3} \right) + \\
& \frac{2 A B f g \left(-a^2 d^2 \operatorname{Log}[a + b x] + b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + b c^2 \operatorname{Log}[c + d x] \right) \right)}{b^2 d^2} + \\
& \frac{1}{b d} B^2 f^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& \quad \left. 2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + b d x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \right. \\
& \quad \left. 2 b c \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
& B^2 f g \left(x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - \frac{1}{b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \right. \\
& \quad \left. \left. b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b \left(d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x] \right) \right) - \right. \\
& \quad \left. \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) + \\
& B^2 g^2 \left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
& \quad \left. \left. 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \right. \\
& \quad \left. \left. d^2 (b c - a d) \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - \right. \right. \\
& \quad \left. \left. 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \left(b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x] \right) + \right. \right. \\
& \quad \left. \left. 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right)
\end{aligned}$$

Problem 242: Result more than twice size of optimal antiderivative.

$$\int (f + g x) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 270 leaves, 9 steps):

$$\begin{aligned}
& - \frac{B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)}{b^2 d} + \\
& \frac{B (b c - a d) (2 b d f - b c g - a d g) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right) - (b f - a g)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2}{b^2 d^2} + \\
& \frac{(f + g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2}{2 g} + \frac{B^2 (b c - a d)^2 g \operatorname{Log} [c + d x]}{b^2 d^2} + \frac{B^2 (b c - a d) (2 b d f - b c g - a d g) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^2 d^2}
\end{aligned}$$

Result (type 4, 745 leaves):

$$\begin{aligned}
& \frac{1}{2 b^2 d^2} \left(2 A^2 b^2 d^2 f x + A^2 b^2 d^2 g x^2 + 4 A b B d f \left(a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] - b c \operatorname{Log} [c + d x] \right) - \right. \\
& \left. 2 A B g \left(a^2 d^2 \operatorname{Log} [a + b x] - b \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] + b c^2 \operatorname{Log} [c + d x] \right) \right) + \right. \\
& \left. 2 b B^2 d f \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \right. \right. \\
& \left. \left. 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] + b d x \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \right. \right. \\
& \left. \left. 2 b c \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) + \right. \\
& \left. B^2 g \left(2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \right. \\
& \left. \left. b^2 d^2 x^2 \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right) \left(a^2 d^2 \operatorname{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x]) \right) + \right. \right. \\
& \left. \left. 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) + 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 243: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2 dx$$

Optimal (type 4, 125 leaves, 6 steps):

$$\frac{2 B (b c - a d) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)}{b d} + \frac{(a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2}{b} + \frac{2 B^2 (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{b d}$$

Result (type 4, 338 leaves):

$$\begin{aligned} & \frac{1}{b d} \left(A^2 b d x + 2 A B \left(a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - b c \operatorname{Log}[c + d x] \right) + \right. \\ & B^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) + \\ & 2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + b d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\ & \left. 2 b c \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \end{aligned}$$

Problem 244: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2}{f + g x} dx$$

Optimal (type 4, 277 leaves, 9 steps):

$$\begin{aligned} & - \frac{\operatorname{Log}\left[\frac{b c - a d}{b(c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2}{g} + \frac{\left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 \operatorname{Log}\left[1 - \frac{(d f - c g)(a + b x)}{(b f - a g)(c + d x)}\right]}{g} - \frac{2 B \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{g} + \\ & \frac{2 B \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{(d f - c g)(a + b x)}{(b f - a g)(c + d x)}\right]}{g} + \frac{2 B^2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{b(c + d x)}\right]}{g} - \frac{2 B^2 \operatorname{PolyLog}\left[3, \frac{(d f - c g)(a + b x)}{(b f - a g)(c + d x)}\right]}{g} \end{aligned}$$

Result (type 4, 1348 leaves):

$$\begin{aligned}
& \frac{1}{g} \left(-B^2 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 + A^2 \operatorname{Log}[f+gx] - 2AB \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[f+gx] + \right. \\
& B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log}[f+gx] + 2AB \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] - 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] + B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log}[f+gx] + \\
& 2AB \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log}[f+gx] - 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log}[f+gx] + 2B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log}[f+gx] + \\
& B^2 \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right]^2 \operatorname{Log}[f+gx] + 2AB \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \\
& 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \\
& 2B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& 2AB \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - \\
& 2B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 2B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + \\
& B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 2B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + \\
& B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)} \right] + 2B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] + B \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(a+bx)}{-bf+ag} \right] - \\
& 2B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] + B \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(c+dx)}{-df+cg} \right] - 2B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right] + \\
& 2B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + 2B^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right] - 2B^2 \operatorname{PolyLog} \left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \Big)
\end{aligned}$$

Problem 245: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{(f+gx)^2} dx$$

Optimal (type 4, 196 leaves, 4 steps):

$$\frac{(a+bx) \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{(bf-ag)(f+gx)} + \frac{2B(bc-ad) \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)} + \frac{2B^2(bc-ad) \operatorname{PolyLog} \left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)}$$

Result (type 4, 3258 leaves):

$$\begin{aligned}
& \frac{1}{g(-bf+ag)(-df+cg)(f+gx)} \\
& \left(-A^2 b d f^2 + A^2 b c f g + a A^2 d f g - a A^2 c g^2 + 2 A b B d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] - 2 A b B c f g \operatorname{Log}\left[\frac{a}{b}+x\right] + 2 A b B d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] - 2 A b B c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] - \right. \\
& b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 A b B d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 a A B d f g \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
& 2 A b B d f g x \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 a A B d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - 2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] + \\
& 2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - b B^2 d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + a B^2 d f g \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - b B^2 d f g x \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \\
& a B^2 d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 A b B d f^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 A b B c f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 a A B d f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2 a A B c g^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2 b B^2 d f^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 a B^2 d f g \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 2 b B^2 d f g x \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + b B^2 c f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& a B^2 d f g \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - a B^2 c g^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 2 b B^2 c f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] + 2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] - \\
& 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] + 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] + b B^2 c f g \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 - a B^2 d f g \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 + \\
& b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 - a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right]^2 - 2 b B^2 c f g \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
& 2 a B^2 d f g \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] - 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
& 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] - 2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
& 2 a B^2 d f g \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] - 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + \\
& 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] + b B^2 c f g \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - a B^2 d f g \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 + \\
& b B^2 c g^2 x \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - a B^2 d g^2 x \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 - 2 A b B d f^2 \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \\
& 2 A b B c f g \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - 2 A b B d f g x \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2 A b B c g^2 x \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + 2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] -
\end{aligned}$$

$$\begin{aligned}
& 2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
& 2 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c f g \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
& 2 b B^2 c g^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-2 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
& 2 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+2 A b B d f^2 \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
& 2 a A B d f g \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 A b B d f g x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 a A B d g^2 x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 2 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 2 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 a B^2 d f g \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
& 2 a B^2 d g^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+2 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 2 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-2 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 2 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]-2 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]-2 b B^2 c f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+ \\
& 2 a B^2 d f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]-2 b B^2 c g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
\end{aligned}$$

Problem 246: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{(f+g x)^3} dx$$

Optimal (type 4, 369 leaves, 9 steps):

$$\begin{aligned}
& \frac{B(b c-a d) g(a+b x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{(b f-a g)^2(d f-c g)(f+g x)}+\frac{b^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 g(b f-a g)^2}-\frac{\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 g(f+g x)^2}+\frac{B^2(b c-a d)^2 g \operatorname{Log}\left[\frac{f+g x}{c+d x}\right]}{(b f-a g)^2(d f-c g)^2}+ \\
& \frac{B(b c-a d)\left(2 b d f-b c g-a d g\right)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{(b f-a g)^2(d f-c g)^2}+\frac{B^2(b c-a d)\left(2 b d f-b c g-a d g\right) \operatorname{PolyLog}\left[2, \frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{(b f-a g)^2(d f-c g)^2}
\end{aligned}$$

Result (type 4, 18235 leaves):

$$\begin{aligned}
 & -\frac{A^2}{2g(f+gx)^2} + 2AB \left(\frac{\frac{g\left(\frac{a}{b}+x\right)}{\left(-f+\frac{ag}{b}\right)^3 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)} - \left(\frac{g^2\left(\frac{a}{b}+x\right)^2}{\left(-f+\frac{ag}{b}\right)^4 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)^2} + \frac{2g\left(\frac{a}{b}+x\right)}{\left(-f+\frac{ag}{b}\right)^3 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)} \right) \text{Log}\left[\frac{a}{b}+x\right] - \frac{\text{Log}\left[1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right]}{\left(-f+\frac{ag}{b}\right)^2} \right. \\
 & \left. \frac{\frac{g\left(\frac{c}{d}+x\right)}{\left(-f+\frac{cg}{d}\right)^3 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)} - \left(\frac{g^2\left(\frac{c}{d}+x\right)^2}{\left(-f+\frac{cg}{d}\right)^4 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)^2} + \frac{2g\left(\frac{c}{d}+x\right)}{\left(-f+\frac{cg}{d}\right)^3 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)} \right) \text{Log}\left[\frac{c}{d}+x\right] - \frac{\text{Log}\left[1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right]}{\left(-f+\frac{cg}{d}\right)^2} \right. \\
 & \left. - \frac{\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]}{2g(f+gx)^2} \right) + \\
 & B^2 \left(2 \left(\frac{\frac{g\left(\frac{a}{b}+x\right)}{\left(-f+\frac{ag}{b}\right)^3 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)} - \left(\frac{g^2\left(\frac{a}{b}+x\right)^2}{\left(-f+\frac{ag}{b}\right)^4 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)^2} + \frac{2g\left(\frac{a}{b}+x\right)}{\left(-f+\frac{ag}{b}\right)^3 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)} \right) \text{Log}\left[\frac{a}{b}+x\right] - \frac{\text{Log}\left[1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right]}{\left(-f+\frac{ag}{b}\right)^2} \right. \\
 & \left. \frac{\frac{g\left(\frac{c}{d}+x\right)}{\left(-f+\frac{cg}{d}\right)^3 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)} - \left(\frac{g^2\left(\frac{c}{d}+x\right)^2}{\left(-f+\frac{cg}{d}\right)^4 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)^2} + \frac{2g\left(\frac{c}{d}+x\right)}{\left(-f+\frac{cg}{d}\right)^3 \left(1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right)} \right) \text{Log}\left[\frac{c}{d}+x\right] - \frac{\text{Log}\left[1-\frac{g\left(\frac{c}{d}+x\right)}{-f+\frac{cg}{d}}\right]}{\left(-f+\frac{cg}{d}\right)^2} \right. \\
 & \left. \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) - \right. \\
 & \left. \frac{\left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2g(f+gx)^2} + \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2\left(\frac{a}{b}+x\right)^2}{\left(-f+\frac{ag}{b}\right)^4 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)^2} + \frac{2g\left(\frac{a}{b}+x\right)}{\left(-f+\frac{ag}{b}\right)^3 \left(1-\frac{g\left(\frac{a}{b}+x\right)}{-f+\frac{ag}{b}}\right)} \right) \text{Log}\left[\frac{a}{b}+x\right]^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{\text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} + \text{Log}\left[\frac{a}{b} + x\right] \left(\frac{g\left(\frac{a}{b} + x\right)}{\left(-f + \frac{ag}{b}\right)^3 \left(1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right)} - \frac{\text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} - \frac{\text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{\left(-f + \frac{ag}{b}\right)^2} \right) + \\
& \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c}{d} + x\right)^2}{\left(-f + \frac{cg}{d}\right)^4 \left(1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)^2} + \frac{2g\left(\frac{c}{d} + x\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} \right) \text{Log}\left[\frac{c}{d} + x\right]^2 + \frac{\text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} + \right. \\
& \left. \text{Log}\left[\frac{c}{d} + x\right] \left(\frac{g\left(\frac{c}{d} + x\right)}{\left(-f + \frac{cg}{d}\right)^3 \left(1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right)} - \frac{\text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} - \frac{\text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{\left(-f + \frac{cg}{d}\right)^2} \right) - \right. \\
& \left. \frac{1}{f^2} \left(\frac{1}{g} 2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \frac{1}{2} \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \right) \right. \right. \\
& \left. \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right] \right) \right) + \\
& \left. \frac{1}{2} \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{bd\left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \right) + \\
& \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b} + x\right)}{bf-ag}\right] + \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(\text{PolyLog}\left[2, \frac{c}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) - \\
& \left. \text{PolyLog}\left[3, -\frac{bg\left(\frac{a}{b} + x\right)}{bf-ag}\right] - \text{PolyLog}\left[3, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right] - \text{PolyLog}\left[3, \frac{c}{\frac{a}{b} + x}\right] + \text{PolyLog}\left[3, -\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& g^2 \left(\frac{1}{g} \left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} - \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} - \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} \right) \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] - \\
& \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} 2b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \\
& \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \\
& \left(-\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} + \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} + \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \frac{(-df+cg) \left(\frac{2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3} \right)}{d(f+gx)} + \right. \\
& \left. \frac{(-df+cg)x \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)^2} - \frac{c \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \\
& \frac{1}{2} \left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} - \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} - \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \right. \\
& \left. \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{2c(-bc+ad)x}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} - \frac{b(-df+cg)x \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)^2} + \right. \\
& \left. \frac{bc \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 + 2 \left(-\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \right. \\
& \left. \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \left(-\frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{dg \left(\frac{c}{d} + x \right)} (-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \\
& \left(\left(\frac{(bf - ag) \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right)}{b(f + gx)} + \frac{(-df + cg) \left(-\frac{dx}{-df + cg} + \frac{cd(f + gx)}{(-df + cg)^2} \right)}{d(f + gx)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) \right) + \\
& \left. \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \\
& \left(\frac{1}{dg \left(\frac{c}{d} + x \right)} (-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(\frac{(bf - ag) \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right)}{b(f + gx)} + \frac{(-df + cg) \left(-\frac{dx}{-df + cg} + \frac{cd(f + gx)}{(-df + cg)^2} \right)}{d(f + gx)} \right) \right) + \\
& \left(\frac{(bf - ag) \left(\frac{2abx}{(bf - ag)^2} + \frac{2a^2b(f + gx)}{(bf - ag)^3} \right)}{b(f + gx)} - \frac{(bf - ag)x \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right)}{b(f + gx)^2} - \frac{a \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right)}{b(f + gx)} + \right. \\
& \left. \frac{(-df + cg) \left(\frac{2cdx}{(-df + cg)^2} - \frac{2c^2d(f + gx)}{(-df + cg)^3} \right)}{d(f + gx)} - \frac{(-df + cg)x \left(-\frac{dx}{-df + cg} + \frac{cd(f + gx)}{(-df + cg)^2} \right)}{d(f + gx)^2} + \frac{c \left(-\frac{dx}{-df + cg} + \frac{cd(f + gx)}{(-df + cg)^2} \right)}{d(f + gx)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \right. \\
& \left. \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) + \left(\frac{(-df + cg) \left(\frac{2c^2dg \left(\frac{c}{d} + x \right)}{(-df + cg)^3} - \frac{2cd \left(\frac{c}{d} + x \right)}{(-df + cg)^2} \right)}{dg \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg \left(\frac{c}{d} + x \right)} - \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg^2 \left(\frac{c}{d} + x \right)} \right) \\
& \left(\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \frac{1}{2} \left(\frac{(-df + cg) \left(\frac{2c^2dg \left(\frac{c}{d} + x \right)}{(-df + cg)^3} - \frac{2cd \left(\frac{c}{d} + x \right)}{(-df + cg)^2} \right)}{dg \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg \left(\frac{c}{d} + x \right)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg^2 \left(\frac{c}{d} + x \right)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) \left(\operatorname{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \operatorname{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \\
& \left(-\frac{2b(-df + cg)^2 \left(\frac{a}{b} + x \right) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d^2 g (bf - ag) \left(\frac{c}{d} + x \right)^2} + \right. \\
& \left(-\frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2 d (bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \right. \\
& \left. \frac{ab(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag)^2 \left(\frac{c}{d} + x \right)} \operatorname{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] + \left(\frac{(-df + cg) \left(\frac{2c^2 dg \left(\frac{c}{d} + x \right)}{(-df + cg)^3} - \frac{2cd \left(\frac{c}{d} + x \right)}{(-df + cg)^2} \right)}{dg \left(\frac{c}{d} + x \right)} + \right. \\
& \left. \frac{c \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg \left(\frac{c}{d} + x \right)} - \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right)}{dg^2 \left(\frac{c}{d} + x \right)} \right) \operatorname{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \left(-\operatorname{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \operatorname{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \frac{1}{2} \left(\frac{2b^2(-df + cg)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)^2}{d^2 (bf - ag)^2 \left(\frac{c}{d} + x \right)^2} - \right. \\
& \frac{2b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2 d (bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right) \operatorname{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \\
& \left. \frac{2bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \operatorname{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2ab(-df+cg)\left(\frac{a}{b}+x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)\text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right]}{d(bf-ag)^2\left(\frac{c}{d}+x\right)} \right) \\
& \left(\text{Log}\left[\frac{-bc+ad}{bd\left(\frac{a}{b}+x\right)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) + \frac{(bf-ag)^2\left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}-\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)^2\text{Log}\left[1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{b^2g^2\left(\frac{a}{b}+x\right)^2} + \\
& \frac{2(-df+cg)\left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}-\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right)\text{Log}\left[1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{dg\left(\frac{c}{d}+x\right)} + \\
& \left(\text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \left(\frac{(bf-ag)\left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}-\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)\left(\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}+\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)}{bg\left(\frac{a}{b}+x\right)\left(1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right)} + \right. \\
& \left. \frac{(bf-ag)\left(-\frac{2a^2bg\left(\frac{a}{b}+x\right)}{(bf-ag)^3}-\frac{2ab\left(\frac{a}{b}+x\right)}{(bf-ag)^2}\right)\text{Log}\left[1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{bg\left(\frac{a}{b}+x\right)} - \frac{a\left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}-\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)\text{Log}\left[1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{bg\left(\frac{a}{b}+x\right)} \right) \\
& \left. \frac{(bf-ag)\left(-\frac{abg\left(\frac{a}{b}+x\right)}{(bf-ag)^2}-\frac{b\left(\frac{a}{b}+x\right)}{bf-ag}\right)\text{Log}\left[1+\frac{bg\left(\frac{a}{b}+x\right)}{bf-ag}\right]}{bg^2\left(\frac{a}{b}+x\right)} \right) + \frac{(-df+cg)^2\left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2}+\frac{d\left(\frac{c}{d}+x\right)}{-df+cg}\right)^2\text{Log}\left[1-\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right]}{d^2g^2\left(\frac{c}{d}+x\right)^2} + \\
& \left(2b(-df+cg)^2\left(\frac{a}{b}+x\right)\left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2}+\frac{d\left(\frac{c}{d}+x\right)}{-df+cg}\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)^2\left(\frac{a}{b}+x\right)}+\frac{ad\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right) \right. \\
& \left. \text{Log}\left[1-\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right] \right) / \left(d^2g(bf-ag)\left(\frac{c}{d}+x\right)^2 \right) + \left(\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c}{d}+x\right)}{b(-df+cg)\left(\frac{a}{b}+x\right)}\right] \right) \\
& \left(\frac{(-df+cg)\left(\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2}-\frac{d\left(\frac{c}{d}+x\right)}{-df+cg}\right)\left(-\frac{cdg\left(\frac{c}{d}+x\right)}{(-df+cg)^2}+\frac{d\left(\frac{c}{d}+x\right)}{-df+cg}\right)}{dg\left(\frac{c}{d}+x\right)\left(1-\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right)} - \frac{(-df+cg)\left(\frac{2c^2dg\left(\frac{c}{d}+x\right)}{(-df+cg)^3}-\frac{2cd\left(\frac{c}{d}+x\right)}{(-df+cg)^2}\right)\text{Log}\left[1-\frac{dg\left(\frac{c}{d}+x\right)}{-df+cg}\right]}{dg\left(\frac{c}{d}+x\right)} \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& \frac{c \left(-\frac{c d g \left(\frac{c+x}{d} \right)}{(-d f+c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f+c g} \right) \operatorname{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f+c g} \right]}{d g \left(\frac{c}{d} + x \right)} + \frac{(-d f+c g) \left(-\frac{c d g \left(\frac{c+x}{d} \right)}{(-d f+c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f+c g} \right) \operatorname{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f+c g} \right]}{d g^2 \left(\frac{c}{d} + x \right)} \right\} + \\
& \frac{b^2 (-d f+c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right)^2 \operatorname{Log} \left[1 + \frac{d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right]}{d^2 (b f-a g)^2 \left(\frac{c}{d} + x \right)^2} + \\
& \operatorname{Log} \left[-\frac{d (b f-a g) \left(\frac{c}{d} + x \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right] \left(-\left(\left(b (-d f+c g) \left(\frac{a}{b} + x \right) \left(-\frac{c d (b f-a g) \left(\frac{c}{d} + x \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} - \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right) \right) \right. \right. \\
& \left. \left. \left(\frac{c d (b f-a g) \left(\frac{c}{d} + x \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) / \left(d (b f-a g) \left(\frac{c}{d} + x \right) \left(1 + \frac{d (b f-a g) \left(\frac{c}{d} + x \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right) \right) \right) - \\
& \frac{b (-d f+c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c+x}{d} \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} \right) \operatorname{Log} \left[1 + \frac{d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f-a g) \left(\frac{c}{d} + x \right)} - \\
& \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right) \operatorname{Log} \left[1 + \frac{d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f-a g) \left(\frac{c}{d} + x \right)} - \\
& \left. \frac{a b (-d f+c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right) \operatorname{Log} \left[1 + \frac{d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f-a g)^2 \left(\frac{c}{d} + x \right)} \right\} + \\
& \frac{(b f-a g) \left(-\frac{2 a^2 b g \left(\frac{a+x}{b} \right)}{(b f-a g)^3} - \frac{2 a b \left(\frac{a+x}{b} \right)}{(b f-a g)^2} \right) \operatorname{PolyLog} \left[2, -\frac{b g \left(\frac{a+x}{b} \right)}{b f-a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \frac{a \left(-\frac{a b g \left(\frac{a+x}{b} \right)}{(b f-a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f-a g} \right) \operatorname{PolyLog} \left[2, -\frac{b g \left(\frac{a+x}{b} \right)}{b f-a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \\
& \frac{(b f-a g) \left(-\frac{a b g \left(\frac{a+x}{b} \right)}{(b f-a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f-a g} \right) \operatorname{PolyLog} \left[2, -\frac{b g \left(\frac{a+x}{b} \right)}{b f-a g} \right]}{b g^2 \left(\frac{a}{b} + x \right)} + \left(\frac{b (-d f+c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f-a g) \left(\frac{c+x}{d} \right)}{b (-d f+c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c+x}{d} \right)}{b (-d f+c g)^2 \left(\frac{a}{b} + x \right)} \right)}{d (b f-a g) \left(\frac{c}{d} + x \right)} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag) \left(\frac{c}{d} + x \right)} + \frac{ab(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag)^2 \left(\frac{c}{d} + x \right)} \right) \\
& \text{PolyLog}\left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag}\right] - \frac{(-df+cg) \left(\frac{2c^2dg \left(\frac{c}{d} + x \right)}{(-df+cg)^3} - \frac{2cd \left(\frac{c}{d} + x \right)}{(-df+cg)^2} \right) \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right]}{dg \left(\frac{c}{d} + x \right)} - \\
& \frac{c \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right]}{dg \left(\frac{c}{d} + x \right)} + \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right]}{dg^2 \left(\frac{c}{d} + x \right)} + \\
& \left(-\frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag) \left(\frac{c}{d} + x \right)} \right) - \\
& \left. \frac{ab(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag)^2 \left(\frac{c}{d} + x \right)} \right) \text{PolyLog}\left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg}\right] + \\
& \left(-\frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag) \left(\frac{c}{d} + x \right)} - \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag) \left(\frac{c}{d} + x \right)} \right) - \\
& \left. \frac{ab(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf-ag)^2 \left(\frac{c}{d} + x \right)} \right) \left(\text{PolyLog}\left[2, \frac{c}{b} + x\right] - \text{PolyLog}\left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right) \text{PolyLog}\left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)}
\end{aligned}$$

$$\begin{aligned}
& \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x \right)} \\
& \frac{a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g)^2 \left(\frac{c}{d} + x \right)} \Bigg) - \\
& \frac{1}{g^2} 2 \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b (f + g x)} + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \right. \\
& \left. \left. \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \right. \\
& \left. \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \right. \\
& \left. \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right)}{(-b c + a d) (f + g x)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \right. \\
& \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right)}{2 d g \left(\frac{c}{d} + x \right)} + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \right. \\
& \left. \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \frac{1}{d (b f - a g) \left(\frac{c}{d} + x \right)} \right. \\
& \left. b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} b(-df + cg) \\
& \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{Log} \left[\frac{-bc + ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \right. \\
& \left. \text{Log} \left[-\frac{(-bc + ad)(f + gx)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) + \frac{(bf - ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf - ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf - ag} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{bg \left(\frac{a}{b} + x \right)} - \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 - \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} \\
& b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \text{Log} \left[\right. \\
& \left. 1 + \frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] + \frac{(bf - ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf - ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf - ag} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{bg \left(\frac{a}{b} + x \right)} + \\
& \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \\
& \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} \\
& b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} \right\} + \\
& \frac{1}{g^3} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right. \\
& \left. \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) \right. \\
& \left. \frac{1}{2} \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right. \\
& \left. \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[\right. \\
& \left. 2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \left. \left. \text{PolyLog} \left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] - \text{PolyLog} \left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] - \text{PolyLog} \left[3, \frac{c}{d} + x \right] + \text{PolyLog} \left[3, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right\} + \\
& 4g \left(\frac{1}{g} \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b(f+gx)} + \frac{1}{2} \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \right. \right. \\
& \left. \left. \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right) + \right. \\
& \left. \left(-\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \left(\frac{(bf - ag) \left(\frac{bx}{bf - ag} + \frac{ab(f+gx)}{(bf - ag)^2} \right)}{b(f + gx)} + \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc + ad)x}{b(-df + cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc + ad)(f + gx)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc + ad)(f + gx)} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]^2 + \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \left(\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right)}{2dg \left(\frac{c}{d} + x \right)} + \frac{1}{2dg \left(\frac{c}{d} + x \right)} (-df + cg) \\
& \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) \left(\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} \\
& b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \left(-\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} - \\
& \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \\
& \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{Log} \left[\frac{-bc + ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{(-bc + ad)(f + gx)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& \frac{(bf - ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf - ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf - ag} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{bg \left(\frac{a}{b} + x \right)} - \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 - \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} \\
& b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]
\end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[1 + \frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right] + \frac{(bf - ag)\left(-\frac{abg\left(\frac{a+x}{b}\right)}{(bf-ag)^2} - \frac{b\left(\frac{a+x}{b}\right)}{bf-ag}\right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a+x}{b}\right)}{bf-ag}\right]}{bg\left(\frac{a}{b} + x\right)} + \\
& \frac{b(-df + cg)\left(\frac{a}{b} + x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)^2\left(\frac{a+x}{b}\right)} + \frac{ad\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a+x}{b}\right)}\right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a+x}{b}\right)}{bf-ag}\right]}{d(bf - ag)\left(\frac{c}{d} + x\right)} - \\
& \frac{(-df + cg)\left(-\frac{cdg\left(\frac{c}{d} + x\right)}{(-df+cg)^2} + \frac{d\left(\frac{c}{d} + x\right)}{-df+cg}\right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right]}{dg\left(\frac{c}{d} + x\right)} - \\
& \frac{b(-df + cg)\left(\frac{a}{b} + x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)^2\left(\frac{a+x}{b}\right)} + \frac{ad\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a+x}{b}\right)}\right) \text{PolyLog}\left[2, \frac{dg\left(\frac{c}{d} + x\right)}{-df+cg}\right]}{d(bf - ag)\left(\frac{c}{d} + x\right)} - \frac{1}{d(bf - ag)\left(\frac{c}{d} + x\right)} \\
& \left. \frac{b(-df + cg)\left(\frac{a}{b} + x\right)\left(\frac{cd(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)^2\left(\frac{a}{b} + x\right)} + \frac{ad\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right) \left(\text{PolyLog}\left[2, \frac{c}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right]\right) - \right. \\
& \left. \frac{b(-df + cg)\left(\frac{a}{b} + x\right)\left(\frac{cd(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)^2\left(\frac{a+x}{b}\right)} + \frac{ad\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a+x}{b}\right)}\right) \text{PolyLog}\left[2, -\frac{d(bf-ag)\left(\frac{c}{d} + x\right)}{b(-df+cg)\left(\frac{a+x}{b}\right)}\right]}{d(bf - ag)\left(\frac{c}{d} + x\right)}\right] - \\
& \frac{1}{g^2} \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(f + gx)}{bf - ag}\right] + \frac{1}{2} \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df + cg}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df + cg}\right] \right) \right. \\
& \left. \left(\text{Log}\left[\frac{b(f + gx)}{bf - ag}\right] - \text{Log}\left[-\frac{d(f + gx)}{-df + cg}\right] \right) + \text{Log}\left[\frac{dg\left(\frac{c}{d} + x\right)}{-df + cg}\right] \text{Log}\left[-\frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b(f + gx)}{bf - ag}\right] + \text{Log}\left[-\frac{d(f + gx)}{-df + cg}\right] \right) + \right. \\
& \left. \frac{1}{2} \text{Log}\left[-\frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right]^2 \left(\text{Log}\left[\frac{-bc + ad}{bd\left(\frac{a}{b} + x\right)}\right] + \text{Log}\left[\frac{b(f + gx)}{bf - ag}\right] - \text{Log}\left[-\frac{(-bc + ad)(f + gx)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right] \right) + \right. \\
& \left. \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[-\frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right] \right) \text{PolyLog}\left[2, -\frac{bg\left(\frac{a}{b} + x\right)}{bf - ag}\right] + \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[-\frac{d(bf - ag)\left(\frac{c}{d} + x\right)}{b(-df + cg)\left(\frac{a}{b} + x\right)}\right] \right) \right)
\end{aligned}$$

$$\left. \begin{aligned} & \text{PolyLog}\left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] + \text{Log}\left[-\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \left(\text{PolyLog}\left[2, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] - \text{PolyLog}\left[2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \right) - \\ & \text{PolyLog}\left[3, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g}\right] - \text{PolyLog}\left[3, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g}\right] - \text{PolyLog}\left[3, \frac{\frac{c}{d} + x}{\frac{a}{b} + x}\right] + \text{PolyLog}\left[3, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)}\right] \end{aligned} \right)$$

Problem 247: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{(f+gx)^4} dx$$

Optimal (type 4, 714 leaves, 12 steps):

$$\begin{aligned} & \frac{B^2 (bc - ad)^2 g^2 (c + dx)}{3 (bf - ag)^2 (df - cg)^3 (f + gx)} + \frac{B^2 (bc - ad)^3 g^2 \text{Log}\left[\frac{a+bx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} - \frac{B (bc - ad) g^2 (c + dx)^2 \left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)}{3 (bf - ag) (df - cg)^3 (f + gx)^2} + \\ & \frac{2B (bc - ad) g (3 bdf - bcg - 2adg) (a + bx) \left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)}{3 (bf - ag)^3 (df - cg)^2 (f + gx)} + \frac{b^3 \left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{3 g (bf - ag)^3} - \frac{\left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{3 g (f + gx)^3} - \\ & \frac{B^2 (bc - ad)^3 g^2 \text{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} + \frac{2B^2 (bc - ad)^2 g (3 bdf - bcg - 2adg) \text{Log}\left[\frac{f+gx}{c+dx}\right]}{3 (bf - ag)^3 (df - cg)^3} + \frac{1}{3 (bf - ag)^3 (df - cg)^3} \\ & \frac{2B (bc - ad) (a^2 d^2 g^2 - abdg (3df - cg) + b^2 (3d^2 f^2 - 3cdfg + c^2 g^2)) \left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right) \text{Log}\left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right]}{3 (bf - ag)^3 (df - cg)^3} + \\ & \frac{2B^2 (bc - ad) (a^2 d^2 g^2 - abdg (3df - cg) + b^2 (3d^2 f^2 - 3cdfg + c^2 g^2)) \text{PolyLog}\left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right]}{3 (bf - ag)^3 (df - cg)^3} \end{aligned}$$

Result (type 4, 55110 leaves): Display of huge result suppressed!

Problem 248: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{(f+gx)^5} dx$$

Optimal (type 4, 1159 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^2 g^3 (c + dx)^2}{12 (bf - ag)^2 (df - cg)^4 (f + gx)^2} - \frac{B^2 (bc - ad)^3 g^3 (c + dx)}{6 (bf - ag)^3 (df - cg)^4 (f + gx)} + \\
& \frac{B^2 (bc - ad)^2 g^2 (4 bdf - b c g - 3 a d g) (c + dx)}{4 (bf - ag)^3 (df - cg)^4 (f + gx)} - \frac{B^2 (bc - ad)^4 g^3 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{6 (bf - ag)^4 (df - cg)^4} + \frac{B^2 (bc - ad)^3 g^2 (4 bdf - b c g - 3 a d g) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{4 (bf - ag)^4 (df - cg)^4} + \\
& \frac{B (bc - ad) g^3 (c + dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 (bf - ag) (df - cg)^4 (f + gx)^3} - \frac{B (bc - ad) g^2 (4 bdf - b c g - 3 a d g) (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{4 (bf - ag)^2 (df - cg)^4 (f + gx)^2} + \\
& \left(B (bc - ad) g (3 a^2 d^2 g^2 - 2 a b d g (4 df - cg) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) (a + bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \right) / \\
& \left(2 (bf - ag)^4 (df - cg)^3 (f + gx) \right) + \frac{b^4 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{4 g (bf - ag)^4} - \frac{\left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{4 g (f + gx)^4} + \\
& \frac{B^2 (bc - ad)^4 g^3 \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{6 (bf - ag)^4 (df - cg)^4} - \frac{B^2 (bc - ad)^3 g^2 (4 bdf - b c g - 3 a d g) \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{4 (bf - ag)^4 (df - cg)^4} + \\
& \frac{B^2 (bc - ad)^2 g (3 a^2 d^2 g^2 - 2 a b d g (4 df - cg) + b^2 (6 d^2 f^2 - 4 c d f g + c^2 g^2)) \operatorname{Log}\left[\frac{f+gx}{c+dx}\right]}{2 (bf - ag)^4 (df - cg)^4} - \frac{1}{2 (bf - ag)^4 (df - cg)^4} \\
& B (bc - ad) (2 bdf - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{Log}\left[1 - \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right] - \\
& \frac{1}{2 (bf - ag)^4 (df - cg)^4} B^2 (bc - ad) (2 bdf - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \operatorname{PolyLog}\left[2, \frac{(df - cg)(a + bx)}{(bf - ag)(c + dx)}\right]
\end{aligned}$$

Result (type 4, 142893 leaves): Display of huge result suppressed!

Problem 272: Result more than twice size of optimal antiderivative.

$$\int (f + gx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 869 leaves, 15 steps):

$$\begin{aligned}
& \frac{2 B^2 (b c - a d)^3 g^3 x}{3 b^3 d^3} + \frac{B^2 (b c - a d)^2 g^2 (4 b d f - 3 b c g - a d g) x}{b^3 d^3} + \frac{B^2 (b c - a d)^2 g^3 (c + d x)^2}{3 b^2 d^4} - \frac{1}{b^4 d^3} \\
& B (b c - a d) g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) - \\
& \frac{B (b c - a d) g^2 (4 b d f - 3 b c g - a d g) (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{2 b^2 d^4} - \frac{B (b c - a d) g^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{3 b^4 d^4} - \\
& \frac{(b f - a g)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{4 b^4 g} + \frac{(f + g x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{4 g} - \frac{1}{b^4 d^4} \\
& B (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] + \\
& \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{3 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{b^4 d^4} + \\
& \frac{2 B^2 (b c - a d)^4 g^3 \operatorname{Log} [c + d x]}{3 b^4 d^4} + \frac{B^2 (b c - a d)^3 g^2 (4 b d f - 3 b c g - a d g) \operatorname{Log} [c + d x]}{b^4 d^4} + \\
& \frac{2 B^2 (b c - a d)^2 g (a^2 d^2 g^2 - 2 a b d g (2 d f - c g) + b^2 (6 d^2 f^2 - 8 c d f g + 3 c^2 g^2)) \operatorname{Log} [c + d x]}{b^4 d^4} - \frac{1}{b^4 d^4} \\
& 2 B^2 (b c - a d) (2 b d f - b c g - a d g) (2 a b d^2 f g - a^2 d^2 g^2 - b^2 (2 d^2 f^2 - 2 c d f g + c^2 g^2)) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]
\end{aligned}$$

Result (type 4, 2279 leaves):

$$\begin{aligned}
& A^2 f^3 x + \frac{3}{2} A^2 f^2 g x^2 + A^2 f g^2 x^3 + \frac{1}{4} A^2 g^3 x^4 + \frac{2 A B f^3 (2 a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - 2 b c \operatorname{Log} [c + d x])}{b d} + \\
& \frac{1}{6} A B g^3 \left(\frac{6 a^3 x}{b^3} - \frac{6 c^3 x}{d^3} - \frac{3 a^2 x^2}{b^2} + \frac{3 c^2 x^2}{d^2} + \frac{2 a x^3}{b} - \frac{2 c x^3}{d} - \frac{6 a^4 \operatorname{Log} [a + b x]}{b^4} + 3 x^4 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + \frac{6 c^4 \operatorname{Log} [c + d x]}{d^4} \right) + \\
& 2 A B f g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log} [a + b x]}{b^3} + x^3 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - \frac{2 c^3 \operatorname{Log} [c + d x]}{d^3} \right) + \\
& \frac{3 A B f^2 g (-2 a^2 d^2 \operatorname{Log} [a + b x] + b (2 d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + 2 b c^2 \operatorname{Log} [c + d x])}{b^2 d^2} + \\
& \frac{1}{b d} B^2 f^3 \left(4 a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 8 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) +
\end{aligned}$$

$$\begin{aligned}
& 4 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + b d x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 8 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
& 4 b c \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] - 8 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 8 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 8 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \Big) + \\
& \frac{1}{12 b^4 d^4} B^2 g^3 \left(-24 b^4 c^4 + 24 a b^3 c^3 d + 24 a^3 b c d^3 - 24 a^4 d^4 - 20 b^4 c^3 d x + 20 a b^3 c^2 d^2 x + 20 a^2 b^2 c d^3 x - 20 a^3 b d^4 x + 4 b^4 c^2 d^2 x^2 - \right. \\
& 8 a b^3 c d^3 x^2 + 4 a^2 b^2 d^4 x^2 - 24 a b^3 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] + 24 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] - 12 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 24 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] - 24 a^3 b c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
& 12 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 12 a^2 b^2 c^2 d^2 \operatorname{Log}[a+b x] - 8 a^3 b c d^3 \operatorname{Log}[a+b x] + 20 a^4 d^4 \operatorname{Log}[a+b x] + 24 a^4 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - \\
& 24 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 24 a^4 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 12 b^4 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 12 a^3 b d^4 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + \\
& 6 b^4 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 6 a^2 b^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - 4 b^4 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 4 a b^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] - \\
& 12 a^4 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] + 3 b^4 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 + 20 b^4 c^4 \operatorname{Log}[c+d x] - 8 a b^3 c^3 d \operatorname{Log}[c+d x] - \\
& 12 a^2 b^2 c^2 d^2 \operatorname{Log}[c+d x] - 24 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 24 b^4 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 12 b^4 c^4 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}[c+d x] + \\
& 24 b^4 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 24 b^4 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 24 a^4 d^4 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \Big) + 3 B^2 f^2 g \\
& \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - \frac{1}{b^2 d^2} 2 \left(-2 d(-b c+a d)(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 b(b c-a d)(c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) \right) + \right. \\
& b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - \left(2 \operatorname{Log}\left[\frac{a}{b}+x\right] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \right) \left(a^2 d^2 \operatorname{Log}[a+b x] - b(d(-b c+a d)x + b c^2 \operatorname{Log}[c+d x]) \right) - \\
& 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \Big) \Big) + \\
& B^2 f g^2 \left(x^3 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right]^2 - \frac{1}{b^3 d^3} 2 \left(4 d(-b c+a d)(b c+a d)(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \right. \right. \\
& 4 b(b c-a d)(b c+a d)(c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \\
& \left. \left. d^2(b c-a d) \left(b x(2 a-b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right] - 2 a^2 \operatorname{Log}[a+b x] \right) + b^2(b c-a d) \left(d x(-2 c+d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 c^2 \operatorname{Log}[c+d x] \right) \right) - \right.
\end{aligned}$$

$$\left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right) (bd(bc-ad)x(-2bc-2ad+bdx) - 2a^3d^3 \operatorname{Log}[a+bx] + 2b^3c^3 \operatorname{Log}[c+dx]) + 4b^3c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + 4a^3d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right)$$

Problem 273: Result more than twice size of optimal antiderivative.

$$\int (f+gx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right] \right)^2 dx$$

Optimal (type 4, 542 leaves, 12 steps):

$$\frac{4B^2(bc-ad)^2g^2x}{3b^2d^2} - \frac{4B(bc-ad)g(3bdf-2bcg-adg)(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)}{3b^3d^2} - \frac{2B(bc-ad)g^2(c+dx)^2\left(A+B\operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)}{3bd^3} - \frac{(bf-ag)^3\left(A+B\operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{3b^3g} + \frac{(f+gx)^3\left(A+B\operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)^2}{3g} + \frac{1}{3b^3d^3}4B(bc-ad)\left(a^2d^2g^2-abdg(3df-cg)+b^2(3d^2f^2-3cdfg+c^2g^2)\right)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)^2}{(c+dx)^2}\right]\right)\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] + \frac{4B^2(bc-ad)^3g^2\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{3b^3d^3} + \frac{4B^2(bc-ad)^3g^2\operatorname{Log}[c+dx]}{3b^3d^3} + \frac{8B^2(bc-ad)^2g(3bdf-2bcg-adg)\operatorname{Log}[c+dx]}{3b^3d^3} + \frac{8B^2(bc-ad)\left(a^2d^2g^2-abdg(3df-cg)+b^2(3d^2f^2-3cdfg+c^2g^2)\right)\operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{3b^3d^3}$$

Result (type 4, 1323 leaves):

$$\begin{aligned}
& \frac{1}{3} \left(3 A^2 f^2 x + 3 A^2 f g x^2 + A^2 g^2 x^3 + \frac{6 A B f^2 \left(2 a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] - 2 b c \operatorname{Log}[c + d x] \right)}{b d} + \right. \\
& 2 A B g^2 \left(\frac{(b c - a d) x (2 b c + 2 a d - b d x)}{b^2 d^2} + \frac{2 a^3 \operatorname{Log}[a + b x]}{b^3} + x^3 \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] - \frac{2 c^3 \operatorname{Log}[c + d x]}{d^3} \right) + \\
& \left. \frac{6 A B f g \left(-2 a^2 d^2 \operatorname{Log}[a + b x] + b \left(2 d (-b c + a d) x + b d^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] + 2 b c^2 \operatorname{Log}[c + d x] \right) \right)}{b^2 d^2} + \right. \\
& \frac{1}{b d} 3 B^2 f^2 \left(4 a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 8 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 8 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \\
& 4 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] + b d x \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right]^2 + 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 4 b c \\
& \left. \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \operatorname{Log}[c + d x] - 8 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - 8 b c \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 8 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + 6 B^2 f g \\
& \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right]^2 - \frac{1}{b^2 d^2} 2 \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \right. \\
& \left. b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \right) (a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x])) - \right. \\
& \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - 2 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) + \\
& B^2 g^2 \left(x^3 \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right]^2 - \frac{1}{b^3 d^3} 2 \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
& 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 (b c - a d) \\
& \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - \\
& \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)^2}{(c + d x)^2}\right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x]) + \\
& \left. 4 b^3 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + 4 a^3 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \right)
\end{aligned}$$

Problem 274: Result more than twice size of optimal antiderivative.

$$\int (f + g x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 dx$$

Optimal (type 4, 281 leaves, 9 steps):

$$\begin{aligned} & - \frac{2 B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)}{b^2 d} - \frac{(b f - a g)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{2 b^2 g} + \\ & \frac{(f + g x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{2 g} + \frac{2 B (b c - a d) (2 b d f - b c g - a d g) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b^2 d^2} + \\ & \frac{4 B^2 (b c - a d)^2 g \operatorname{Log} [c + d x]}{b^2 d^2} + \frac{4 B^2 (b c - a d) (2 b d f - b c g - a d g) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^2 d^2} \end{aligned}$$

Result (type 4, 767 leaves):

$$\begin{aligned} & \frac{1}{2 b^2 d^2} \left(2 A^2 b^2 d^2 f x + A^2 b^2 d^2 g x^2 + 4 A b B d f \left(2 a d \operatorname{Log} [a + b x] + b d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] - 2 b c \operatorname{Log} [c + d x] \right) - \right. \\ & \left. 2 A B g \left(2 a^2 d^2 \operatorname{Log} [a + b x] - b \left(2 d (-b c + a d) x + b d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + 2 b c^2 \operatorname{Log} [c + d x] \right) \right) + \right. \\ & \left. 2 b B^2 d f \left(4 a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 8 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 8 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \right. \right. \\ & \left. \left. 4 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + b d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 + 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 8 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \right. \right. \\ & \left. \left. 4 b c \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \operatorname{Log} [c + d x] - 8 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 8 b c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 8 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + \right. \\ & \left. B^2 g \left(8 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 4 a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 8 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 4 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \right. \\ & \left. \left. b^2 d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 + 4 \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) (a^2 d^2 \operatorname{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x])) + \right. \right. \\ & \left. \left. 8 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 8 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) \end{aligned}$$

Problem 275: Result more than twice size of optimal antiderivative.

$$\int \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 dx$$

Optimal (type 4, 129 leaves, 6 steps):

$$\frac{(a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{b} + \frac{4 B (b c - a d) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b d} + \frac{8 B^2 (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b d}$$

Result (type 4, 385 leaves):

$$\begin{aligned} & \frac{1}{b d} \left(A^2 b d x + 4 a B^2 d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 4 a A B d \operatorname{Log} [a + b x] - 8 a B^2 d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 8 a B^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - \right. \\ & 8 a B^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 A b B d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + 4 a B^2 d \operatorname{Log} [a + b x] \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] + b B^2 d x \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right]^2 - \\ & 4 A b B c \operatorname{Log} [c + d x] + 8 b B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 8 b B^2 c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - 4 b B^2 c \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \operatorname{Log} [c + d x] - \\ & \left. 8 b B^2 c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 8 b B^2 c \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 8 a B^2 d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \end{aligned}$$

Problem 276: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2}{f + g x} dx$$

Optimal (type 4, 285 leaves, 9 steps):

$$\begin{aligned} & - \frac{\left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{g} + \frac{\left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right)^2 \operatorname{Log} \left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{g} - \frac{4 B \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{g} + \\ & \frac{4 B \left(A + B \operatorname{Log} \left[\frac{e (a + b x)^2}{(c + d x)^2} \right] \right) \operatorname{PolyLog} \left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{g} + \frac{8 B^2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{b (c + d x)} \right]}{g} - \frac{8 B^2 \operatorname{PolyLog} \left[3, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{g} \end{aligned}$$

Result (type 4, 1370 leaves):

$$\begin{aligned}
& \frac{1}{g} \left(-4 B^2 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 + A^2 \operatorname{Log}[f+gx] - 4 AB \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[f+gx] + \right. \\
& 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log}[f+gx] + 4 AB \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] - 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[f+gx] + \\
& 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log}[f+gx] + 2 AB \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \operatorname{Log}[f+gx] - 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \operatorname{Log}[f+gx] + \\
& 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \operatorname{Log}[f+gx] + B^2 \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right]^2 \operatorname{Log}[f+gx] + 4 AB \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 4 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& 4 B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + 8 B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \\
& 4 B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - 4 AB \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - \\
& 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 4 B^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 8 B^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + \\
& 4 B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] - 8 B^2 \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{Log} \left[\frac{d(f+gx)}{df-cg} \right] + \\
& 4 B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)} \right] + 4 B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 2 B \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(a+bx)}{-bf+ag} \right] - \\
& 4 B \left(A + B \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] + 2 B \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{g(c+dx)}{-df+cg} \right] - 8 B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right] + \\
& 8 B^2 \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + 8 B^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right] - 8 B^2 \operatorname{PolyLog} \left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] \Big)
\end{aligned}$$

Problem 277: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e(a+bx)^2}{(c+dx)^2} \right] \right)^2}{(f+gx)^2} dx$$

Optimal (type 4, 200 leaves, 4 steps):

$$\frac{(a+bx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{(bf-ag)(f+gx)} + \frac{4B(bc-ad) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \operatorname{Log} \left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)} + \frac{8B^2(bc-ad) \operatorname{PolyLog} \left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)} \right]}{(bf-ag)(df-cg)}$$

Result (type 4, 3314 leaves):

$$\frac{1}{g(-bf+ag)(-df+cg)(f+gx)}$$

$$\begin{aligned} & \left(-A^2 b d f^2 + A^2 b c f g + a A^2 d f g - a A^2 c g^2 + 4 A b B d f^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 4 A b B c f g \operatorname{Log} \left[\frac{a}{b} + x \right] + 4 A b B d f g x \operatorname{Log} \left[\frac{a}{b} + x \right] - \right. \\ & 4 A b B c g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] - 4 b B^2 d f^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b B^2 c f g \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 4 b B^2 d f g x \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 b B^2 c g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\ & 4 A b B d f^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 4 a A B d f g \operatorname{Log} \left[\frac{c}{d} + x \right] - 4 A b B d f g x \operatorname{Log} \left[\frac{c}{d} + x \right] + 4 a A B d g^2 x \operatorname{Log} \left[\frac{c}{d} + x \right] + 8 b B^2 d f^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - \\ & 8 a B^2 d f g \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] + 8 b B^2 d f g x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - 8 a B^2 d g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] - \\ & 4 b B^2 d f^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 4 a B^2 d f g \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 4 b B^2 d f g x \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 4 a B^2 d g^2 x \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 A b B d f^2 \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + \\ & 2 A b B c f g \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + 2 a A B d f g \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - 2 a A B c g^2 \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + 4 b B^2 d f^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - \\ & 4 b B^2 c f g \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + 4 b B^2 d f g x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - 4 b B^2 c g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - \\ & 4 b B^2 d f^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + 4 a B^2 d f g \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - 4 b B^2 d f g x \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] + \\ & 4 a B^2 d g^2 x \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] - b B^2 d f^2 \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]^2 + b B^2 c f g \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]^2 + a B^2 d f g \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]^2 - \\ & a B^2 c g^2 \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right]^2 - 8 b B^2 c f g \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + 8 a B^2 d f g \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] - \\ & 8 b B^2 c g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + 8 a B^2 d g^2 x \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right] + 4 b B^2 c f g \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - 4 a B^2 d f g \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 + \\ & 4 b B^2 c g^2 x \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - 4 a B^2 d g^2 x \operatorname{Log} \left[\frac{g(c+dx)}{-df+cg} \right]^2 - 8 b B^2 c f g \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + \\ & 8 a B^2 d f g \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] - 8 b B^2 c g^2 x \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)} \right] + \end{aligned}$$

$$\begin{aligned}
& 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]-8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
& 8 a B^2 d f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]-8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+ \\
& 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]+4 b B^2 c f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
& 4 a B^2 d f g \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2+4 b B^2 c g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2-4 a B^2 d g^2 x \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2- \\
& 4 A b B d f^2 \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 A b B c f g \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-4 A b B d f g x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 A b B c g^2 x \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
& 8 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+8 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
& 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-4 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 b B^2 c f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]- \\
& 4 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+4 b B^2 c g^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-8 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
& 8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]-8 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+ \\
& 4 A b B d f^2 \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-4 a A B d f g \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+4 A b B d f g x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-4 a A B d g^2 x \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
& 8 b B^2 d f^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 a B^2 d f g \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-8 b B^2 d f g x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 8 a B^2 d g^2 x \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+4 b B^2 d f^2 \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-4 a B^2 d f g \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 4 b B^2 d f g x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-4 a B^2 d g^2 x \operatorname{Log}\left[\frac{e(a+b x)^2}{(c+d x)^2}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 b B^2 d f^2 \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]- \\
& 8 b B^2 c f g \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+8 b B^2 d f g x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]-8 b B^2 c g^2 x \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]+ \\
& 8 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]-8 B^2(b c-a d) g(f+g x) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]-8 b B^2 c f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+ \\
& 8 a B^2 d f g \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]-8 b B^2 c g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+8 a B^2 d g^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
\end{aligned}$$

Problem 278: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{(f+gx)^3} dx$$

Optimal (type 4, 381 leaves, 9 steps):

$$\frac{2 B (b c - a d) g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{(b f - a g)^2 (d f - c g) (f + g x)} + \frac{b^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{2 g (b f - a g)^2} - \frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{2 g (f + g x)^2} + \frac{4 B^2 (b c - a d)^2 g \operatorname{Log} \left[\frac{f+g x}{c+dx} \right]}{(b f - a g)^2 (d f - c g)^2} +$$

$$\frac{2 B (b c - a d) (2 b d f - b c g - a d g) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \operatorname{Log} \left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{(b f - a g)^2 (d f - c g)^2} + \frac{4 B^2 (b c - a d) (2 b d f - b c g - a d g) \operatorname{PolyLog} \left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)} \right]}{(b f - a g)^2 (d f - c g)^2}$$

Result (type 4, 18290 leaves):

$$-\frac{A^2}{2 g (f + g x)^2} + 2 A B \left(\frac{\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} - \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{a g}{b} \right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)^2} + \frac{2 g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{a g}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right)} \right) \operatorname{Log} \left[\frac{a}{b} + x \right] - \frac{\operatorname{Log} \left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{a g}{b}} \right]}{\left(-f + \frac{a g}{b} \right)^2} \right. -$$

$$\frac{\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)} - \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{c g}{d} \right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)^2} + \frac{2 g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{c g}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right)} \right) \operatorname{Log} \left[\frac{c}{d} + x \right] - \frac{\operatorname{Log} \left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{c g}{d}} \right]}{\left(-f + \frac{c g}{d} \right)^2} \right. -$$

$$\left. \frac{-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2 a b e x}{(c+dx)^2} + \frac{b^2 e x^2}{(c+dx)^2} \right]}{2 g (f + g x)^2} \right) +$$

$$\begin{aligned}
& B^2 \left(2 \left(\frac{\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)}{\left(-f + \frac{ag}{b} \right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)^2} + \frac{2g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)} \right) \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) - \\
& \frac{\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)}{\left(-f + \frac{cg}{d} \right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)^2} + \frac{2g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) \\
& \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right) - \frac{\left(-2 \text{Log} \left[\frac{a}{b} + x \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a^2 e}{(c+dx)^2} + \frac{2abex}{(c+dx)^2} + \frac{b^2 ex^2}{(c+dx)^2} \right] \right)^2}{2g(f+gx)^2} + \\
& \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{a}{b} + x \right)^2}{\left(-f + \frac{ag}{b} \right)^4 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)^2} + \frac{2g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)} \right) \text{Log} \left[\frac{a}{b} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} + \right. \\
& \left. \text{Log} \left[\frac{a}{b} + x \right] \left(\frac{g \left(\frac{a}{b} + x \right)}{\left(-f + \frac{ag}{b} \right)^3 \left(1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{a}{b} + x \right)}{-f + \frac{ag}{b}} \right]}{\left(-f + \frac{ag}{b} \right)^2} \right) + \\
& \frac{1}{g} \left(-\frac{1}{2} \left(\frac{g^2 \left(\frac{c}{d} + x \right)^2}{\left(-f + \frac{cg}{d} \right)^4 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)^2} + \frac{2g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right]^2 + \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} + \right. \\
& \left. \text{Log} \left[\frac{c}{d} + x \right] \left(\frac{g \left(\frac{c}{d} + x \right)}{\left(-f + \frac{cg}{d} \right)^3 \left(1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right)} - \frac{\text{Log} \left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) - \frac{\text{PolyLog} \left[2, \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right]}{\left(-f + \frac{cg}{d} \right)^2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{f^2} 4 \left(\frac{1}{g} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right. \right. \\
& \left. \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \right. \\
& \left. \frac{1}{2} \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \right. \\
& \left. \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right. \\
& \left. \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \right. \\
& \left. \text{PolyLog} \left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] - \text{PolyLog} \left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] - \text{PolyLog} \left[3, \frac{c}{d} + x \right] + \text{PolyLog} \left[3, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& g^2 \left(\frac{1}{g} \left(\left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} - \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} - \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] - \right. \right. \\
& \left. \frac{1}{d(bf-ag) \left(\frac{c}{d} + x \right)} 2b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \right. \\
& \left. \left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \right. \\
& \left. \left(-\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right)}{b(f+gx)} + \frac{(bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)^2} + \frac{a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{(-df+cg) \left(\frac{2cdx}{(-df+cg)^2} - \frac{2c^2d(f+gx)}{(-df+cg)^3} \right) + \frac{(-df+cg)x \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right) - c \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)^2} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[\right. \\
& \left. - \frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \left(\frac{(bf-ag) \left(\frac{2abx}{(bf-ag)^2} + \frac{2a^2b(f+gx)}{(bf-ag)^3} \right) - (bf-ag)x \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right) - a \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} \right. \\
& \left. + \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{2c(-bc+ad)x}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} - \frac{2c^2(-bc+ad)(f+gx)}{b(-df+cg)^3 \left(\frac{a}{b} + x \right)} \right) - b(-df+cg)x \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right. \\
& \left. - \frac{bc \left(\frac{a}{b} + x \right) \left(-\frac{(-bc+ad)x}{b(-df+cg) \left(\frac{a}{b} + x \right)} + \frac{c(-bc+ad)(f+gx)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} \right)}{(-bc+ad)(f+gx)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 + 2 \left(-\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} \right. \\
& \left. - \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \left(-\frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right. \\
& \left. + \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{dg \left(\frac{c}{d} + x \right)} (-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \\
& \left(\left(\frac{(bf-ag) \left(\frac{bx}{bf-ag} + \frac{ab(f+gx)}{(bf-ag)^2} \right)}{b(f+gx)} + \frac{(-df+cg) \left(-\frac{dx}{-df+cg} + \frac{cd(f+gx)}{(-df+cg)^2} \right)}{d(f+gx)} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right. \\
& \left. + \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df+cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df+cg} \right) \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{dg \left(\frac{c}{d} + x \right)} \right) + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right]
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{1}{d g \left(\frac{c}{d} + x \right)} 2 (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) + \right. \\
& \left(\frac{(b f - a g) \left(\frac{2 a b x}{(b f - a g)^2} + \frac{2 a^2 b (f + g x)}{(b f - a g)^3} \right)}{b (f + g x)} - \frac{(b f - a g) x \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)^2} - \frac{a \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \\
& \left. \frac{(-d f + c g) \left(\frac{2 c d x}{(-d f + c g)^2} - \frac{2 c^2 d (f + g x)}{(-d f + c g)^3} \right)}{d (f + g x)} - \frac{(-d f + c g) x \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)^2} + \frac{c \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \\
& \left. \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \\
& \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2} \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} + \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \right. \\
& \left. \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\operatorname{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
& \left(\frac{2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2} + \right. \\
& \left. \frac{b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) - b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \frac{b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)}{d (b f - a g)^2 \left(\frac{c}{d} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \left(\frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} \right)}{d g \left(\frac{c}{d} + x \right)} \right) + \\
& \left. \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right)} - \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right)}{d g^2 \left(\frac{c}{d} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \\
& \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \frac{1}{2} \left(\frac{2 b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2}{d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2} \right) - \\
& \frac{2 b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x \right)} - \frac{2 a c d \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
& \frac{2 b c \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x \right)} - \\
& \frac{2 a b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d (b f - a g)^2 \left(\frac{c}{d} + x \right)} \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \right. \\
& \left. \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \frac{(b f - a g)^2 \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right)^2 \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b^2 g^2 \left(\frac{a}{b} + x \right)^2} + \\
& \frac{2 (-d f + c g) \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{d g \left(\frac{c}{d} + x \right)} +
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \left(\frac{(b f - a g) \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \left(\frac{a b g \left(\frac{a+x}{b} \right) + b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} + \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right)}{b g \left(\frac{a}{b} + x \right) \left(1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right)} + \right. \\
& \frac{(b f - a g) \left(- \frac{2 a^2 b g \left(\frac{a+x}{b} \right) - 2 a b \left(\frac{a+x}{b} \right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \frac{a \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \\
& \left. \frac{(b f - a g) \left(- \frac{a b g \left(\frac{a+x}{b} \right) - b \left(\frac{a+x}{b} \right)}{(b f - a g)^2} - \frac{b \left(\frac{a+x}{b} \right)}{b f - a g} \right) \text{Log} \left[1 + \frac{b g \left(\frac{a+x}{b} \right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x \right)} \right) + \frac{(-d f + c g)^2 \left(- \frac{c d g \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right)^2 \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d^2 g^2 \left(\frac{c}{d} + x \right)^2} + \\
& \left(2 b (-d f + c g)^2 \left(\frac{a}{b} + x \right) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right. \\
& \left. \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) / \left(d^2 g (b f - a g) \left(\frac{c}{d} + x \right)^2 \right) + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \left(- \frac{(-d f + c g) \left(\frac{c d g \left(\frac{c+x}{d} \right) - d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} - \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right)}{d g \left(\frac{c}{d} + x \right) \left(1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right)} - \frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c+x}{d} \right) - 2 c d \left(\frac{c+x}{d} \right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} - \right. \\
& \left. \frac{c \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} + \frac{(-d f + c g) \left(- \frac{c d g \left(\frac{c+x}{d} \right) + d \left(\frac{c+x}{d} \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c+x}{d} \right)}{-d f + c g} \right) \text{Log} \left[1 - \frac{d g \left(\frac{c+x}{d} \right)}{-d f + c g} \right]}{d g^2 \left(\frac{c}{d} + x \right)} \right) + \\
& \frac{b^2 (-d f + c g)^2 \left(\frac{a}{b} + x \right)^2 \left(\frac{c d (b f - a g) \left(\frac{c+x}{d} \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c+x}{d} \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right)^2 \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c+x}{d} \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]}{d^2 (b f - a g)^2 \left(\frac{c}{d} + x \right)^2} + \\
& \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(- \left(\left(b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} - \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \Bigg/ \left(d (b f - a g) \left(\frac{c}{d} + x\right) \left(1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \right) - \\
& \frac{b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \frac{2 a c d \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x\right)} - \\
& \frac{b c \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g) \left(\frac{c}{d} + x\right)} - \\
& \left. \frac{a b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[1 + \frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]}{d (b f - a g)^2 \left(\frac{c}{d} + x\right)} \right) + \\
& \frac{(b f - a g) \left(-\frac{2 a^2 b g \left(\frac{a}{b} + x\right)}{(b f - a g)^3} - \frac{2 a b \left(\frac{a}{b} + x\right)}{(b f - a g)^2} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x\right)} - \frac{a \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x\right)} - \\
& \frac{(b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x\right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x\right)}{b f - a g} \right) \text{PolyLog} \left[2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right]}{b g^2 \left(\frac{a}{b} + x\right)} + \left(\frac{b (-d f + c g) \left(\frac{a}{b} + x\right) \left(-\frac{2 c^2 d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^3 \left(\frac{a}{b} + x\right)} - \frac{2 a c d \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x\right)} + \right. \\
& \left. \frac{b c \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g) \left(\frac{c}{d} + x\right)} + \frac{a b (-d f + c g) \left(\frac{a}{b} + x\right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x\right)} + \frac{a d \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right)}{d (b f - a g)^2 \left(\frac{c}{d} + x\right)} \right) \text{PolyLog} \left[2, \right. \\
& \left. -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \frac{(-d f + c g) \left(\frac{2 c^2 d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^3} - \frac{2 c d \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} - \frac{c \left(-\frac{c d g \left(\frac{c}{d} + x\right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x\right)}{-d f + c g} \right) \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x\right)} +
\end{aligned}$$

$$\begin{aligned}
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{dg^2 \left(\frac{c}{d} + x \right)} + \left(-\frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} \right. \\
& \left. \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \frac{ab(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag)^2 \left(\frac{c}{d} + x \right)} \right) \text{PolyLog} \left[2, \right. \\
& \left. \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] + \left(-\frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag) \left(\frac{c}{d} + x \right)} \right. \\
& \left. \frac{ab(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right)}{d(bf - ag)^2 \left(\frac{c}{d} + x \right)} \right) \left(\text{PolyLog} \left[2, \frac{c}{b} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(-\frac{2c^2d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^3 \left(\frac{a}{b} + x \right)} - \frac{2acd \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \\
& \frac{bc \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \\
& \left. \frac{ab(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag)^2 \left(\frac{c}{d} + x \right)} \right) - \\
& \frac{1}{g^2} 2 \left(\frac{(bf - ag) \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b(f + gx)} + \frac{1}{2} \left(\frac{(bf - ag) \left(\frac{bx}{bf - ag} + \frac{ab(f + gx)}{(bf - ag)^2} \right)}{b(f + gx)} + \frac{(-df + cg) \left(-\frac{dx}{-df + cg} + \frac{cd(f + gx)}{(-df + cg)^2} \right)}{d(f + gx)} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \\
& \left(-\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(-\frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \frac{1}{2} \\
& \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{b (-d f + c g) \left(\frac{a}{b} + x \right) \left(-\frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right)}{(-b c + a d) (f + g x)} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \\
& \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right)}{2 d g \left(\frac{c}{d} + x \right)} + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \\
& \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \frac{1}{d (b f - a g) \left(\frac{c}{d} + x \right)} b \\
& (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) + \\
& \frac{1}{d g \left(\frac{c}{d} + x \right)} (-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[-\frac{d (f + g x)}{-d f + c g} \right] \right) - \\
& \frac{1}{d (b f - a g) \left(\frac{c}{d} + x \right)} b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \\
& \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(\text{Log} \left[\frac{-b c + a d}{b d \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[-\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& \frac{(b f - a g) \left(-\frac{a b g \left(\frac{a}{b} + x \right)}{(b f - a g)^2} - \frac{b \left(\frac{a}{b} + x \right)}{b f - a g} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 + \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right]}{b g \left(\frac{a}{b} + x \right)} - \\
& \frac{(-d f + c g) \left(-\frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{Log} \left[1 - \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right]}{d g \left(\frac{c}{d} + x \right)} - \frac{1}{d (b f - a g) \left(\frac{c}{d} + x \right)} b
\end{aligned}$$

$$\begin{aligned}
& (-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \\
& \text{Log} \left[1 + \frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] + \frac{(bf - ag) \left(-\frac{abg \left(\frac{a}{b} + x \right)}{(bf - ag)^2} - \frac{b \left(\frac{a}{b} + x \right)}{bf - ag} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{bg \left(\frac{a}{b} + x \right)} + \\
& \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \\
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c}{d} + x \right)}{(-df + cg)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-df + cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{dg \left(\frac{c}{d} + x \right)} - \\
& \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} - \frac{1}{d(bf - ag) \left(\frac{c}{d} + x \right)} b(-df + cg) \\
& \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \left. \frac{b(-df + cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf - ag) \left(\frac{c}{d} + x \right)} \right) + \\
& \frac{1}{g^3} 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) \left(\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \right. \right. \\
& \left. \left. \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] + \text{Log} \left[-\frac{d(f + gx)}{-df + cg} \right] \right) + \frac{1}{2} \right. \\
& \left. \text{Log} \left[-\frac{d(bf - ag) \left(\frac{c}{d} + x \right)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc + ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f + gx)}{bf - ag} \right] - \text{Log} \left[-\frac{(-bc + ad)(f + gx)}{b(-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \text{PolyLog} \left[2, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] + \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \right) - \text{PolyLog} \left[\right. \\
& \left. 3, - \frac{b g \left(\frac{a}{b} + x \right)}{b f - a g} \right] - \text{PolyLog} \left[3, \frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] - \text{PolyLog} \left[3, \frac{c}{d} + x \right] + \text{PolyLog} \left[3, - \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] \left. \right) + \\
4 g & \left(\frac{1}{g} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right]}{b (f + g x)} + \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \right. \right. \\
& \left. \left. \frac{(-d f + c g) \left(- \frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) + \right. \\
& \left(- \frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} - \frac{(-d f + c g) \left(- \frac{d x}{-d f + c g} + \frac{c d (f + g x)}{(-d f + c g)^2} \right)}{d (f + g x)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right] + \\
& \frac{1}{2} \left(\frac{(b f - a g) \left(\frac{b x}{b f - a g} + \frac{a b (f + g x)}{(b f - a g)^2} \right)}{b (f + g x)} + \frac{b (-d f + c g) \left(\frac{a}{b} + x \right) \left(- \frac{(-b c + a d) x}{b (-d f + c g) \left(\frac{a}{b} + x \right)} + \frac{c (-b c + a d) (f + g x)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} \right)}{(-b c + a d) (f + g x)} \right) \text{Log} \left[- \frac{d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right]^2 + \\
& \frac{(-d f + c g) \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[- \frac{d (f + g x)}{-d f + c g} \right] \right)}{2 d g \left(\frac{c}{d} + x \right)} + \frac{1}{2 d g \left(\frac{c}{d} + x \right)} (-d f + c g) \\
& \left(- \frac{c d g \left(\frac{c}{d} + x \right)}{(-d f + c g)^2} + \frac{d \left(\frac{c}{d} + x \right)}{-d f + c g} \right) \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \right) \left(\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] - \text{Log} \left[- \frac{d (f + g x)}{-d f + c g} \right] \right) - \frac{1}{d (b f - a g) \left(\frac{c}{d} + x \right)} \\
& b (-d f + c g) \left(\frac{a}{b} + x \right) \left(\frac{c d (b f - a g) \left(\frac{c}{d} + x \right)}{b (-d f + c g)^2 \left(\frac{a}{b} + x \right)} + \frac{a d \left(\frac{c}{d} + x \right)}{b (-d f + c g) \left(\frac{a}{b} + x \right)} \right) \text{Log} \left[\frac{d g \left(\frac{c}{d} + x \right)}{-d f + c g} \right] \left(-\text{Log} \left[\frac{b (f + g x)}{b f - a g} \right] + \text{Log} \left[- \frac{d (f + g x)}{-d f + c g} \right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{(-df + cg) \left(-\frac{cdg \left(\frac{c+x}{d}\right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-df+cg} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d}\right)}{b(-df+cg) \left(\frac{a+x}{b}\right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right)}{dg \left(\frac{c}{d} + x\right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x\right)} b(-df+cg) \\
& \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x\right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \right. \\
& \left. \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] \right) + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a+x}{b}\right)}{(bf-ag)^2} - \frac{b \left(\frac{a+x}{b}\right)}{bf-ag} \right) \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d}\right)}{b(-df+cg) \left(\frac{a+x}{b}\right)} \right] \right) \text{Log} \left[1 + \frac{bg \left(\frac{a+x}{b}\right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x\right)} - \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c+x}{d}\right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-df+cg} \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c+x}{d}\right)}{b(-df+cg) \left(\frac{a+x}{b}\right)} \right] \right) \text{Log} \left[1 - \frac{dg \left(\frac{c+x}{d}\right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x\right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x\right)} \\
& b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] \text{Log} \left[\right. \\
& \left. 1 + \frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] + \frac{(bf-ag) \left(-\frac{abg \left(\frac{a+x}{b}\right)}{(bf-ag)^2} - \frac{b \left(\frac{a+x}{b}\right)}{bf-ag} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a+x}{b}\right)}{bf-ag} \right]}{bg \left(\frac{a}{b} + x\right)} + \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c+x}{d}\right)}{b(-df+cg)^2 \left(\frac{a+x}{b}\right)} + \frac{ad \left(\frac{c+x}{d}\right)}{b(-df+cg) \left(\frac{a+x}{b}\right)} \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a+x}{b}\right)}{bf-ag} \right]}{d(bf-ag) \left(\frac{c}{d} + x\right)} - \\
& \frac{(-df+cg) \left(-\frac{cdg \left(\frac{c+x}{d}\right)}{(-df+cg)^2} + \frac{d \left(\frac{c+x}{d}\right)}{-df+cg} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c+x}{d}\right)}{-df+cg} \right]}{dg \left(\frac{c}{d} + x\right)} - \\
& \frac{b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c+x}{d}\right)}{b(-df+cg)^2 \left(\frac{a+x}{b}\right)} + \frac{ad \left(\frac{c+x}{d}\right)}{b(-df+cg) \left(\frac{a+x}{b}\right)} \right) \text{PolyLog} \left[2, \frac{dg \left(\frac{c+x}{d}\right)}{-df+cg} \right]}{d(bf-ag) \left(\frac{c}{d} + x\right)} - \frac{1}{d(bf-ag) \left(\frac{c}{d} + x\right)} \\
& b(-df+cg) \left(\frac{a}{b} + x\right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg)^2 \left(\frac{a}{b} + x\right)} + \frac{ad \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right) \left(\text{PolyLog} \left[2, \frac{c}{b} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x\right)}{b(-df+cg) \left(\frac{a}{b} + x\right)} \right] \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{b(-df+cg) \left(\frac{a}{b} + x \right) \left(\frac{cd(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg)^2 \left(\frac{a}{b} + x \right)} + \frac{ad \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right) \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]}{d(bf-ag) \left(\frac{c}{d} + x \right)} \right) - \\
& \frac{1}{g^2} \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \frac{1}{2} \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \left(-2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \right) \right. \\
& \left. \left(\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \text{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(-\text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] + \text{Log} \left[-\frac{d(f+gx)}{-df+cg} \right] \right) + \right. \\
& \left. \frac{1}{2} \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\text{Log} \left[\frac{-bc+ad}{bd \left(\frac{a}{b} + x \right)} \right] + \text{Log} \left[\frac{b(f+gx)}{bf-ag} \right] - \text{Log} \left[-\frac{(-bc+ad)(f+gx)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) + \right. \\
& \left. \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] + \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \text{PolyLog} \left[\right. \\
& \left. 2, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] + \text{Log} \left[-\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \left(\text{PolyLog} \left[2, \frac{c}{d} + x \right] - \text{PolyLog} \left[2, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) - \right. \\
& \left. \left. \left. \left. \left. \left. \text{PolyLog} \left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf-ag} \right] - \text{PolyLog} \left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df+cg} \right] - \text{PolyLog} \left[3, \frac{c}{d} + x \right] + \text{PolyLog} \left[3, -\frac{d(bf-ag) \left(\frac{c}{d} + x \right)}{b(-df+cg) \left(\frac{a}{b} + x \right)} \right] \right) \right) \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 279: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \text{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{(f+gx)^4} dx$$

Optimal (type 4, 724 leaves, 12 steps):

$$\begin{aligned}
& \frac{4 B^2 (b c - a d)^2 g^2 (c + d x)}{3 (b f - a g)^2 (d f - c g)^3 (f + g x)} - \frac{2 B (b c - a d) g^2 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right)}{3 (b f - a g) (d f - c g)^3 (f + g x)^2} + \\
& \frac{4 B (b c - a d) g (3 b d f - b c g - 2 a d g) (a + b x) \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right)}{3 (b f - a g)^3 (d f - c g)^2 (f + g x)} + \frac{b^3 \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right)^2}{3 g (b f - a g)^3} - \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right)^2}{3 g (f + g x)^3} + \\
& \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{3 (b f - a g)^3 (d f - c g)^3} - \frac{4 B^2 (b c - a d)^3 g^2 \operatorname{Log}\left[\frac{f+g x}{c+d x}\right]}{3 (b f - a g)^3 (d f - c g)^3} + \frac{8 B^2 (b c - a d)^2 g (3 b d f - b c g - 2 a d g) \operatorname{Log}\left[\frac{f+g x}{c+d x}\right]}{3 (b f - a g)^3 (d f - c g)^3} + \frac{1}{3 (b f - a g)^3 (d f - c g)^3} \\
& \frac{4 B (b c - a d) \left(a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2) \right) \left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right) \operatorname{Log}\left[1 - \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)}\right]}{3 (b f - a g)^3 (d f - c g)^3} + \\
& \frac{8 B^2 (b c - a d) \left(a^2 d^2 g^2 - a b d g (3 d f - c g) + b^2 (3 d^2 f^2 - 3 c d f g + c^2 g^2) \right) \operatorname{PolyLog}\left[2, \frac{(d f - c g) (a + b x)}{(b f - a g) (c + d x)}\right]}{3 (b f - a g)^3 (d f - c g)^3}
\end{aligned}$$

Result (type 4, 55 173 leaves): Display of huge result suppressed!

Problem 280: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[\frac{e^{(a+b x)^2}}{(c+d x)^2}\right]\right)^2}{(f + g x)^5} dx$$

Optimal (type 4, 1154 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^2 g^3 (c + dx)^2}{3 (bf - ag)^2 (df - cg)^4 (f + gx)^2} - \frac{2B^2 (bc - ad)^3 g^3 (c + dx)}{3 (bf - ag)^3 (df - cg)^4 (f + gx)} + \frac{B^2 (bc - ad)^2 g^2 (4bdf - bcg - 3adg) (c + dx)}{(bf - ag)^3 (df - cg)^4 (f + gx)} + \\
& \frac{B (bc - ad) g^3 (c + dx)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{3 (bf - ag) (df - cg)^4 (f + gx)^3} - \frac{B (bc - ad) g^2 (4bdf - bcg - 3adg) (c + dx)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)}{2 (bf - ag)^2 (df - cg)^4 (f + gx)^2} + \\
& \left(B (bc - ad) g (3a^2 d^2 g^2 - 2abd g (4df - cg) + b^2 (6d^2 f^2 - 4cdfg + c^2 g^2)) (a + bx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \right) / \\
& \left((bf - ag)^4 (df - cg)^3 (f + gx) \right) + \frac{b^4 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{4g (bf - ag)^4} - \frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right)^2}{4g (f + gx)^4} - \frac{2B^2 (bc - ad)^4 g^3 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{3 (bf - ag)^4 (df - cg)^4} + \\
& \frac{B^2 (bc - ad)^3 g^2 (4bdf - bcg - 3adg) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{(bf - ag)^4 (df - cg)^4} + \frac{2B^2 (bc - ad)^4 g^3 \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{3 (bf - ag)^4 (df - cg)^4} - \frac{B^2 (bc - ad)^3 g^2 (4bdf - bcg - 3adg) \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{(bf - ag)^4 (df - cg)^4} + \\
& \frac{2B^2 (bc - ad)^2 g (3a^2 d^2 g^2 - 2abd g (4df - cg) + b^2 (6d^2 f^2 - 4cdfg + c^2 g^2)) \operatorname{Log} \left[\frac{f+gx}{c+dx} \right]}{(bf - ag)^4 (df - cg)^4} - \frac{1}{(bf - ag)^4 (df - cg)^4} \\
& B (bc - ad) (2bdf - bcg - adg) (2abd^2 fg - a^2 d^2 g^2 - b^2 (2d^2 f^2 - 2cdfg + c^2 g^2)) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)^2}}{(c+dx)^2} \right] \right) \operatorname{Log} \left[1 - \frac{(df - cg) (a + bx)}{(bf - ag) (c + dx)} \right] - \\
& \frac{1}{(bf - ag)^4 (df - cg)^4} 2B^2 (bc - ad) (2bdf - bcg - adg) (2abd^2 fg - a^2 d^2 g^2 - b^2 (2d^2 f^2 - 2cdfg + c^2 g^2)) \operatorname{PolyLog} \left[2, \frac{(df - cg) (a + bx)}{(bf - ag) (c + dx)} \right]
\end{aligned}$$

Result (type 4, 142956 leaves): Display of huge result suppressed!

Problem 305: Result more than twice size of optimal antiderivative.

$$\int (A + B \operatorname{Log}[e^{(a+bx)^n} (c+dx)^{-n}])^2 dx$$

Optimal (type 4, 137 leaves, 6 steps):

$$\begin{aligned}
& \frac{2B (bc - ad) n \operatorname{Log} \left[\frac{bc - ad}{b(c + dx)} \right] (A + B \operatorname{Log}[e^{(a+bx)^n} (c + dx)^{-n}])}{bd} + \\
& \frac{(a + bx) (A + B \operatorname{Log}[e^{(a+bx)^n} (c + dx)^{-n}])^2}{b} + \frac{2B^2 (bc - ad) n^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{bd}
\end{aligned}$$

Result (type 4, 327 leaves):

$$\begin{aligned}
& -\frac{1}{bd} \left(2aABdn + 2aB^2dn^2 - A^2bdx + aB^2dn^2 \operatorname{Log}[a+bx]^2 + \right. \\
& 2aBc n \operatorname{Log}[c+dx] + 2aB^2dn^2 \operatorname{Log}[c+dx] + bB^2cn^2 \operatorname{Log}[c+dx]^2 + 2aB^2dn \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 2abBdx \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 2bB^2cn \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - bB^2dx \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 - \\
& \left. 2Bn \operatorname{Log}[a+bx] \left(bBcn \operatorname{Log}[c+dx] + B(-bc+ad)n \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + ad(A+Bn+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \right) \right) + \\
& 2B^2(bc-ad)n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]
\end{aligned}$$

Problem 306: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^2}{g+hx} dx$$

Optimal (type 4, 301 leaves, 10 steps):

$$\begin{aligned}
& -\frac{\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^2}{h} + \\
& \frac{(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^2 \operatorname{Log}\left[1 - \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} - \frac{2Bn(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{h} + \\
& \frac{2Bn(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} + \frac{2B^2n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{h} - \frac{2B^2n^2 \operatorname{PolyLog}\left[3, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h}
\end{aligned}$$

Result (type 4, 1082 leaves):

$$\begin{aligned}
& \frac{1}{h} \left((A + B (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]))^2 \operatorname{Log}[g + h x] + \right. \\
& 2 B n (A + B (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])) \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \operatorname{PolyLog}\left[2, \frac{h (a + b x)}{-b g + a h}\right] \right) - \\
& 2 A B n \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d (g + h x)}{d g - c h}\right] + \operatorname{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] \right) - \\
& 2 B^2 n (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d (g + h x)}{d g - c h}\right] + \operatorname{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] \right) + \\
& B^2 n^2 \left(\operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + 2 \operatorname{Log}[a + b x] \operatorname{PolyLog}\left[2, \frac{h (a + b x)}{-b g + a h}\right] - 2 \operatorname{PolyLog}\left[3, \frac{h (a + b x)}{-b g + a h}\right] \right) + \\
& B^2 n^2 \left(\operatorname{Log}[c + d x]^2 \operatorname{Log}\left[\frac{d (g + h x)}{d g - c h}\right] + 2 \operatorname{Log}[c + d x] \operatorname{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] - 2 \operatorname{PolyLog}\left[3, \frac{h (c + d x)}{-d g + c h}\right] \right) - \\
& 2 B^2 n^2 \left(\operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \frac{1}{2} \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \left(-2 \operatorname{Log}[a + b x] + \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right) \right. \\
& \left. \left(\operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \operatorname{Log}\left[\frac{d (g + h x)}{d g - c h}\right] \right) + \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \left(-\operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \operatorname{Log}\left[\frac{d (g + h x)}{d g - c h}\right] \right) + \right. \\
& \left. \frac{1}{2} \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right]^2 \left(\operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] + \operatorname{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \operatorname{Log}\left[\frac{(-b c + a d) (g + h x)}{(d g - c h) (a + b x)}\right] \right) \right. \\
& \left. \left(\operatorname{Log}[c + d x] - \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \right) \operatorname{PolyLog}\left[2, \frac{h (a + b x)}{-b g + a h}\right] + \left(\operatorname{Log}[a + b x] + \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \right) \operatorname{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] + \right. \\
& \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \left(\operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] - \operatorname{PolyLog}\left[2, \frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \right) - \\
& \left. \operatorname{PolyLog}\left[3, \frac{h (a + b x)}{-b g + a h}\right] - \operatorname{PolyLog}\left[3, \frac{h (c + d x)}{-d g + c h}\right] - \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right] + \operatorname{PolyLog}\left[3, \frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] \right) \Bigg)
\end{aligned}$$

Problem 307: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(g + h x)^2} dx$$

Optimal (type 4, 208 leaves, 5 steps):

$$\frac{(a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(b g - a h) (g + h x)} +$$

$$\frac{2 B (b c - a d) n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h) (d g - c h)} + \frac{2 B^2 (b c - a d) n^2 \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h) (d g - c h)}$$

Result (type 4, 3460 leaves):

$$\frac{1}{h (-b g + a h) (-d g + c h) (g + h x)}$$

$$\left(-A^2 b d g^2 + A^2 b c g h + a A^2 d g h - a A^2 c h^2 + 2 A b B d g^2 n \operatorname{Log}[a + b x] - 2 A b B c g h n \operatorname{Log}[a + b x] + 2 A b B d g h n x \operatorname{Log}[a + b x] - \right.$$

$$2 A b B c h^2 n x \operatorname{Log}[a + b x] - b B^2 d g^2 n^2 \operatorname{Log}[a + b x]^2 + b B^2 c g h n^2 \operatorname{Log}[a + b x]^2 - b B^2 d g h n^2 x \operatorname{Log}[a + b x]^2 +$$

$$b B^2 c h^2 n^2 x \operatorname{Log}[a + b x]^2 - 2 A b B d g^2 n \operatorname{Log}[c + d x] + 2 a A B d g h n \operatorname{Log}[c + d x] - 2 A b B d g h n x \operatorname{Log}[c + d x] +$$

$$2 a A B d h^2 n x \operatorname{Log}[c + d x] + 2 b B^2 d g^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 2 a B^2 d g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] +$$

$$2 b B^2 d g h n^2 x \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 2 a B^2 d h^2 n^2 x \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - b B^2 d g^2 n^2 \operatorname{Log}[c + d x]^2 +$$

$$a B^2 d g h n^2 \operatorname{Log}[c + d x]^2 - b B^2 d g h n^2 x \operatorname{Log}[c + d x]^2 + a B^2 d h^2 n^2 x \operatorname{Log}[c + d x]^2 - 2 b B^2 c g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] +$$

$$2 a B^2 d g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] - 2 b B^2 c h^2 n^2 x \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] + 2 a B^2 d h^2 n^2 x \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] +$$

$$b B^2 c g h n^2 \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 - a B^2 d g h n^2 \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 + b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 - a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right]^2 -$$

$$2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d g h n^2 \operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] -$$

$$2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] -$$

$$2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d g h n^2 \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] -$$

$$2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] + 2 a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right] +$$

$$b B^2 c g h n^2 \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right]^2 - a B^2 d g h n^2 \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right]^2 + b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right]^2 -$$

$$a B^2 d h^2 n^2 x \operatorname{Log}\left[\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}\right]^2 - 2 A b B d g^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 A b B c g h \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] +$$

$$2 a A B d g h \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] - 2 a A B c h^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 b B^2 d g^2 n \operatorname{Log}[a + b x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] -$$

$$2 b B^2 c g h n \operatorname{Log}[a + b x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 b B^2 d g h n x \operatorname{Log}[a + b x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] -$$

$$2 b B^2 c h^2 n x \operatorname{Log}[a + b x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] - 2 b B^2 d g^2 n \operatorname{Log}[c + d x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] +$$

$$\begin{aligned}
& 2 a B^2 d g h n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]-2 b B^2 d g h n x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]+ \\
& 2 a B^2 d h^2 n x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]-b B^2 d g^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+ \\
& b B^2 c g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2+a B^2 d g h \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2-a B^2 c h^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2- \\
& 2 A b B d g^2 n \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 A b B c g h n \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]-2 A b B d g h n x \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 A b B c h^2 n x \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+ \\
& 2 b B^2 d g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]-2 a B^2 d g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b B^2 d g h n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]- \\
& 2 a B^2 d h^2 n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]-2 b B^2 d g^2 n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]- \\
& 2 b B^2 d g h n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]- \\
& 2 b B^2 d g^2 n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b B^2 c g h n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]- \\
& 2 b B^2 d g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b B^2 c h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+ \\
& 2 A b B d g^2 n \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 a A B d g h n \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 A b B d g h n x \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 a A B d h^2 n x \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b B^2 d g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 a B^2 d g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 b B^2 d g h n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 a B^2 d h^2 n^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b B^2 d g^2 n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 b B^2 c g h n^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b B^2 d g h n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 b B^2 c h^2 n^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b B^2 d g^2 n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 a B^2 d g h n \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b B^2 d g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 a B^2 d h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 B^2(b c-a d) h n^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(a+b x)}{-b g+a h}\right]- \\
& 2 B^2(b c-a d) h n^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(c+d x)}{-d g+c h}\right]-2 b B^2 c g h n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+ \\
& 2 a B^2 d g h n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]-2 b B^2 c h^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 a B^2 d h^2 n^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
\end{aligned}$$

Problem 308: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(g + h x)^3} dx$$

Optimal (type 4, 393 leaves, 10 steps):

$$\begin{aligned} & \frac{B (b c - a d) h n (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{(b g - a h)^2 (d g - c h) (g + h x)} + \frac{b^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 h (b g - a h)^2} - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 h (g + h x)^2} + \\ & \frac{B^2 (b c - a d)^2 h n^2 \operatorname{Log}\left[\frac{g+h x}{c+d x}\right]}{(b g - a h)^2 (d g - c h)^2} + \frac{B (b c - a d) (2 b d g - b c h - a d h) n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} + \\ & \frac{B^2 (b c - a d) (2 b d g - b c h - a d h) n^2 \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} \end{aligned}$$

Result (type 4, 15422 leaves):

$$\begin{aligned} & - \frac{(A + B (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]))^2}{2 h (g + h x)^2} + \\ & \frac{1}{h} B n (A + B (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])) \\ & \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} - \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \operatorname{Log}[a + b x] - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) - \\ & \frac{A B n \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \operatorname{Log}[c + d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right)}{h} - \frac{1}{h} \\ & B^2 n (-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \\ & \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \operatorname{Log}[c + d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right) + \\ & \frac{1}{h} B^2 n^2 \left(-\frac{1}{2} \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \operatorname{Log}[a + b x]^2 + \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} + \right. \\ & \left. \operatorname{Log}[a + b x] \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) - \frac{b^2 \operatorname{PolyLog}\left[2, \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) + \end{aligned}$$

$$\begin{aligned}
& \frac{1}{h} B^2 n^2 \left(-\frac{1}{2} \left(\frac{d^2 h^2 (c+dx)^2}{(-dg+ch)^4 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)^2} + \frac{2d^2 h (c+dx)}{(-dg+ch)^3 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)} \right) \text{Log}[c+dx]^2 + \frac{d^2 \text{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} + \right. \\
& \left. \text{Log}[c+dx] \left(\frac{d^2 h (c+dx)}{(-dg+ch)^3 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)} - \frac{d^2 \text{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} \right) - \frac{d^2 \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} \right) - \\
& \frac{1}{g^2} B^2 n^2 \left(\frac{1}{h} 2 \left(\text{Log}[a+bx] \text{Log}[c+dx] \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \right) \right. \\
& \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \\
& \frac{1}{2} \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \text{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \text{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \text{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big) + \\
& h^2 \left(\frac{1}{h} \left(\left(\frac{(bg-ah) \left(\frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} - \frac{(bg-ah)x \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)^2} - \frac{a \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} \right) \text{Log}[a+bx] \text{Log}[c+dx] - \right. \\
& \frac{1}{(bg-ah)(c+dx)} 2(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \right. \\
& \left. \left. \frac{(-dg+ch)(a+bx) \left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right)}{(-bc+ad)(g+hx)} \right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \left(-\frac{(bg-ah) \left(\frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{(bg-ah)x\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)^2} + \frac{a\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} - \frac{(-dg+ch)\left(\frac{2cdx}{(-dg+ch)^2} - \frac{2c^2d(g+hx)}{(-dg+ch)^3}\right)}{d(g+hx)} + \frac{(-dg+ch)x\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)^2} \\
& \frac{c\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \left[\text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \frac{1}{2} \left(\frac{(bg-ah)\left(\frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3}\right)}{b(g+hx)} - \right. \right. \\
& \left. \frac{(bg-ah)x\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)^2} - \frac{a\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)(a+bx)\left(\frac{2c(-bc+a)d x}{(-dg+ch)^2(a+bx)} - \frac{2c^2(-bc+a)d(g+hx)}{(-dg+ch)^3(a+bx)}\right)}{(-bc+a d)(g+hx)} - \right. \\
& \left. \frac{(-dg+ch)x(a+bx)\left(-\frac{(-bc+a)d x}{(-dg+ch)(a+bx)} + \frac{c(-bc+a)d(g+hx)}{(-dg+ch)^2(a+bx)}\right)}{(-bc+a d)(g+hx)^2} + \frac{c(a+bx)\left(-\frac{(-bc+a)d x}{(-dg+ch)(a+bx)} + \frac{c(-bc+a)d(g+hx)}{(-dg+ch)^2(a+bx)}\right)}{(-bc+a d)(g+hx)} \right) \\
& \left. \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 + 2 \left(-\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} - \frac{(-dg+ch)\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \right) \right] \\
& \left(-\frac{(-dg+ch)(a+bx)\left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]}{(bg-ah)(c+dx)} + \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{h(c+dx)} \right) + \\
& \frac{1}{h(c+dx)}(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(\left(\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \right) \right. \\
& \left. \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) + \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(\text{Log}\left[\frac{h(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right)}{h(c+dx)} \right) + \\
& \frac{1}{2} \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(\frac{2(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \right)}{h(c+dx)} + \right. \\
& \left(\frac{(bg-ah)\left(\frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3}\right)}{b(g+hx)} - \frac{(bg-ah)x\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)^2} - \frac{a\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)\left(\frac{2cdx}{(-dg+ch)^2} - \frac{2c^2d(g+hx)}{(-dg+ch)^3}\right)}{d(g+hx)} - \right. \\
& \left. \frac{(-dg+ch)x\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)^2} + \frac{c\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \right) \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{(-dg + ch) \left(\frac{2c^2 h (c+dx)}{(-dg+ch)^3} - \frac{2c (c+dx)}{(-dg+ch)^2} \right)}{h (c+dx)} + \frac{c \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h (c+dx)} - \frac{(-dg + ch) \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2 (c+dx)} \right) \\
& \left(\text{Log} \left[\frac{b (g+hx)}{bg-ah} \right] - \text{Log} \left[-\frac{d (g+hx)}{-dg+ch} \right] \right) + \frac{1}{2} \left(\frac{(-dg + ch) \left(\frac{2c^2 h (c+dx)}{(-dg+ch)^3} - \frac{2c (c+dx)}{(-dg+ch)^2} \right)}{h (c+dx)} + \frac{c \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h (c+dx)} - \right. \\
& \left. \frac{(-dg + ch) \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2 (c+dx)} \right) \left(-2 \text{Log} [a + bx] + \text{Log} \left[\frac{h (c+dx)}{-dg+ch} \right] \right) \left(\text{Log} \left[\frac{b (g+hx)}{bg-ah} \right] - \text{Log} \left[-\frac{d (g+hx)}{-dg+ch} \right] \right) + \\
& \left(-\frac{2 (-dg + ch)^2 (a + bx) \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right)}{h (bg-ah) (c+dx)^2} + \right. \\
& \left(-\frac{(-dg + ch) (a + bx) \left(-\frac{2c^2 (bg-ah) (c+dx)}{(-dg+ch)^3 (a+bx)} - \frac{2ac (c+dx)}{(-dg+ch)^2 (a+bx)} \right)}{(bg-ah) (c+dx)} - \frac{c (a + bx) \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right)}{(bg-ah) (c+dx)} - \right. \\
& \left. \frac{a (-dg + ch) (a + bx) \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right)}{(bg-ah)^2 (c+dx)} \right) \text{Log} \left[\frac{h (c+dx)}{-dg+ch} \right] + \\
& \left(\frac{(-dg + ch) \left(\frac{2c^2 h (c+dx)}{(-dg+ch)^3} - \frac{2c (c+dx)}{(-dg+ch)^2} \right)}{h (c+dx)} + \frac{c \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h (c+dx)} - \frac{(-dg + ch) \left(-\frac{ch (c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2 (c+dx)} \right) \text{Log} \left[-\frac{(bg-ah) (c+dx)}{(-dg+ch) (a+bx)} \right] \Big) \\
& \left(-\text{Log} \left[\frac{b (g+hx)}{bg-ah} \right] + \text{Log} \left[-\frac{d (g+hx)}{-dg+ch} \right] \right) + \frac{1}{2} \left(\frac{2 (-dg + ch)^2 (a + bx)^2 \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right)^2}{(bg-ah)^2 (c+dx)^2} - \right. \\
& \frac{2 (-dg + ch) (a + bx) \left(-\frac{2c^2 (bg-ah) (c+dx)}{(-dg+ch)^3 (a+bx)} - \frac{2ac (c+dx)}{(-dg+ch)^2 (a+bx)} \right) \text{Log} \left[-\frac{(bg-ah) (c+dx)}{(-dg+ch) (a+bx)} \right]}{(bg-ah) (c+dx)} - \\
& \frac{2c (a + bx) \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right) \text{Log} \left[-\frac{(bg-ah) (c+dx)}{(-dg+ch) (a+bx)} \right]}{(bg-ah) (c+dx)} - \\
& \left. \frac{2a (-dg + ch) (a + bx) \left(\frac{c (bg-ah) (c+dx)}{(-dg+ch)^2 (a+bx)} + \frac{a (c+dx)}{(-dg+ch) (a+bx)} \right) \text{Log} \left[-\frac{(bg-ah) (c+dx)}{(-dg+ch) (a+bx)} \right]}{(bg-ah)^2 (c+dx)} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] + \text{Log} \left[\frac{b(g+hx)}{bg-ah} \right] - \text{Log} \left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)} \right] \right) + \frac{(bg-ah)^2 \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right)^2 \text{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)^2} + \\
& \frac{2(-dg+ch) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(c+dx)} + \left(\text{Log}[c+dx] - \text{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \right) \\
& \left(\frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\frac{ah(a+bx)}{(bg-ah)^2} + \frac{a+bx}{bg-ah} \right)}{h(a+bx) \left(1 + \frac{h(a+bx)}{bg-ah} \right)} + \frac{(bg-ah) \left(-\frac{2a^2h(a+bx)}{(bg-ah)^3} - \frac{2a(a+bx)}{(bg-ah)^2} \right) \text{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \right. \\
& \left. \frac{a \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \text{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \text{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)} \right) + \\
& \frac{(-dg+ch)^2 \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)^2 \text{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h^2(c+dx)^2} + \frac{1}{h(bg-ah)(c+dx)^2} 2(-dg+ch)^2(a+bx) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \\
& \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right] + \left(\text{Log}[a+bx] + \text{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \right) \\
& \left(-\frac{(-dg+ch) \left(\frac{ch(c+dx)}{(-dg+ch)^2} - \frac{c+dx}{-dg+ch} \right) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h(c+dx) \left(1 - \frac{h(c+dx)}{-dg+ch} \right)} - \frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right) \text{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} - \right. \\
& \left. \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} + \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h^2(c+dx)} \right) + \\
& \frac{(-dg+ch)^2(a+bx)^2 \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)^2 \text{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)^2(c+dx)^2} + \text{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \\
& \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} - \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx) \left(1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right)} - \right. \\
& \left. \frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \text{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)^2(c+dx)} + \\
& \frac{(bg-ah) \left(-\frac{2a^2h(a+bx)}{(bg-ah)^3} - \frac{2a(a+bx)}{(bg-ah)^2} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \frac{a \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \\
& \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)} + \left(\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} + \right. \\
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} + \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right] - \\
& \frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right) \operatorname{PolyLog} \left[2, \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} - \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{PolyLog} \left[2, \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} + \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{PolyLog} \left[2, \frac{h(c+dx)}{-dg+ch} \right]}{h^2(c+dx)} + \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} - \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \operatorname{PolyLog} \left[2, \frac{h(c+dx)}{-dg+ch} \right] + \\
& \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} - \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \left(\operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right] - \operatorname{PolyLog} \left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \right) - \\
& \frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \operatorname{PolyLog} \left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \\
& \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{PolyLog} \left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)^2(c+dx)} \right\} - \\
& \frac{1}{h^2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right) \text{Log}[a+bx] \text{Log}[c+dx]}{b(g+hx)} + \frac{1}{2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \right) \\
& \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) + \\
& \left(-\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} - \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{1}{2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch)(a+bx) \left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right)}{(-bc+ad)(g+hx)} \right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 + \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right)}{2h(c+dx)} + \frac{1}{2h(c+dx)} (-dg+ch) \\
& \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right)}{h(c+dx)} - \\
& \frac{1}{(bg-ah)(c+dx)} (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \\
& \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{1}{(bg-ah)(c+dx)}
\end{aligned}$$

$$\begin{aligned}
& (-dg + ch)(a + bx) \left(\frac{c(bg - ah)(c + dx)}{(-dg + ch)^2(a + bx)} + \frac{a(c + dx)}{(-dg + ch)(a + bx)} \right) \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \\
& \text{Log} \left[1 + \frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] + \frac{(bg - ah) \left(-\frac{ah(a + bx)}{(bg - ah)^2} - \frac{a + bx}{bg - ah} \right) \text{PolyLog} \left[2, -\frac{h(a + bx)}{bg - ah} \right]}{h(a + bx)} + \\
& \frac{(-dg + ch)(a + bx) \left(\frac{c(bg - ah)(c + dx)}{(-dg + ch)^2(a + bx)} + \frac{a(c + dx)}{(-dg + ch)(a + bx)} \right) \text{PolyLog} \left[2, -\frac{h(a + bx)}{bg - ah} \right]}{(bg - ah)(c + dx)} - \\
& \frac{(-dg + ch) \left(-\frac{ch(c + dx)}{(-dg + ch)^2} + \frac{c + dx}{-dg + ch} \right) \text{PolyLog} \left[2, \frac{h(c + dx)}{-dg + ch} \right]}{h(c + dx)} - \frac{(-dg + ch)(a + bx) \left(\frac{c(bg - ah)(c + dx)}{(-dg + ch)^2(a + bx)} + \frac{a(c + dx)}{(-dg + ch)(a + bx)} \right) \text{PolyLog} \left[2, \frac{h(c + dx)}{-dg + ch} \right]}{(bg - ah)(c + dx)} - \\
& \frac{1}{(bg - ah)(c + dx)} (-dg + ch)(a + bx) \left(\frac{c(bg - ah)(c + dx)}{(-dg + ch)^2(a + bx)} + \frac{a(c + dx)}{(-dg + ch)(a + bx)} \right) \left(\text{PolyLog} \left[2, \frac{b(c + dx)}{d(a + bx)} \right] - \text{PolyLog} \left[\right. \right. \\
& \left. \left. 2, -\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \right) - \frac{(-dg + ch)(a + bx) \left(\frac{c(bg - ah)(c + dx)}{(-dg + ch)^2(a + bx)} + \frac{a(c + dx)}{(-dg + ch)(a + bx)} \right) \text{PolyLog} \left[2, -\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right]}{(bg - ah)(c + dx)} \left. \right) + \\
& \frac{1}{h^3} 2 \left(\text{Log}[a + bx] \text{Log}[c + dx] \text{Log} \left[\frac{b(g + hx)}{bg - ah} \right] + \frac{1}{2} \text{Log} \left[\frac{h(c + dx)}{-dg + ch} \right] \left(-2 \text{Log}[a + bx] + \text{Log} \left[\frac{h(c + dx)}{-dg + ch} \right] \right) \right. \\
& \left. \left(\text{Log} \left[\frac{b(g + hx)}{bg - ah} \right] - \text{Log} \left[-\frac{d(g + hx)}{-dg + ch} \right] \right) + \text{Log} \left[\frac{h(c + dx)}{-dg + ch} \right] \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \left(-\text{Log} \left[\frac{b(g + hx)}{bg - ah} \right] + \text{Log} \left[-\frac{d(g + hx)}{-dg + ch} \right] \right) \right) + \\
& \frac{1}{2} \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right]^2 \left(\text{Log} \left[\frac{-bc + ad}{d(a + bx)} \right] + \text{Log} \left[\frac{b(g + hx)}{bg - ah} \right] - \text{Log} \left[-\frac{(-bc + ad)(g + hx)}{(-dg + ch)(a + bx)} \right] \right) + \\
& \left(\text{Log}[c + dx] - \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \right) \text{PolyLog} \left[2, -\frac{h(a + bx)}{bg - ah} \right] + \left(\text{Log}[a + bx] + \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \right) \\
& \text{PolyLog} \left[2, \frac{h(c + dx)}{-dg + ch} \right] + \text{Log} \left[-\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \left(\text{PolyLog} \left[2, \frac{b(c + dx)}{d(a + bx)} \right] - \text{PolyLog} \left[2, -\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \right) - \\
& \left. \left. \text{PolyLog} \left[3, -\frac{h(a + bx)}{bg - ah} \right] - \text{PolyLog} \left[3, \frac{h(c + dx)}{-dg + ch} \right] - \text{PolyLog} \left[3, \frac{b(c + dx)}{d(a + bx)} \right] + \text{PolyLog} \left[3, -\frac{(bg - ah)(c + dx)}{(-dg + ch)(a + bx)} \right] \right) \right) + \\
& 4h \left(\frac{1}{h} \left(\frac{(bg - ah) \left(\frac{bx}{bg - ah} + \frac{ab(g + hx)}{(bg - ah)^2} \right) \text{Log}[a + bx] \text{Log}[c + dx]}{b(g + hx)} + \frac{1}{2} \left(\frac{(bg - ah) \left(\frac{bx}{bg - ah} + \frac{ab(g + hx)}{(bg - ah)^2} \right)}{b(g + hx)} + \frac{(-dg + ch) \left(-\frac{dx}{-dg + ch} + \frac{cd(g + hx)}{(-dg + ch)^2} \right)}{d(g + hx)} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]\right) + \\
& \left(-\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} - \frac{(-dg+ch)\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)}\right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{1}{2} \left(\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)(a+bx)\left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)}\right)}{(-bc+ad)(g+hx)}\right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 + \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right)}{2h(c+dx)} + \frac{1}{2h(c+dx)} \\
& (-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]\right) \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right) - \\
& \frac{1}{(bg-ah)(c+dx)} (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \\
& \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right) + \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right)}{h(c+dx)} - \\
& \frac{1}{(bg-ah)(c+dx)} (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \\
& \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right]\right) + \\
& \frac{(bg-ah)\left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah}\right) \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \text{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \text{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \text{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{(bg-ah)\left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah}\right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{(bg-ah)(c+dx)} - \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} -
\end{aligned}$$

$$\begin{aligned}
& \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{(bg-ah)(c+dx)} - \frac{1}{(bg-ah)(c+dx)} \\
& \left((-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \right. \\
& \left. \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)(c+dx)} \right) - \\
& \frac{1}{h^2} \left(\text{Log}[a+bx] \text{Log}[c+dx] \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \right. \\
& \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) \right) + \\
& \frac{1}{2} \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \left. \left. \left. \text{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \text{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \text{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \right) \right)
\end{aligned}$$

Problem 309: Result more than twice size of optimal antiderivative.

$$\int (g+hx)^2 (A+B \text{Log}[e(a+bx)^n(c+dx)^{-n}])^3 dx$$

Optimal (type 4, 875 leaves, 19 steps):

$$\begin{aligned}
& - \frac{B^3 (bc - ad)^3 h^2 n^3 \operatorname{Log}[c + dx]}{b^3 d^3} + \frac{B^2 (bc - ad)^2 h^2 n^2 (a + bx) (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{b^3 d^2} - \\
& \frac{2 B^2 (bc - ad)^2 h (3bdg - 2bch - adh) n^2 \operatorname{Log}\left[\frac{bc - ad}{b(c + dx)}\right] (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])}{b^3 d^3} - \\
& \frac{B (bc - ad) h (3bdg - 2bch - adh) n (a + bx) (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2}{b^3 d^2} - \\
& \frac{B (bc - ad) h^2 n (c + dx)^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2}{2 b d^3} + \frac{1}{b^3 d^3} \\
& B (bc - ad) (a^2 d^2 h^2 - abdh (3dg - ch) + b^2 (3d^2 g^2 - 3cdgh + c^2 h^2)) n \operatorname{Log}\left[\frac{bc - ad}{b(c + dx)}\right] (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^2 - \\
& \frac{(bg - ah)^3 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^3}{3 b^3 h} + \frac{(g + hx)^3 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}])^3}{3 h} - \\
& \frac{B^2 (bc - ad)^3 h^2 n^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]) \operatorname{Log}\left[1 - \frac{b(c + dx)}{d(a + bx)}\right]}{b^3 d^3} - \frac{2 B^3 (bc - ad)^2 h (3bdg - 2bch - adh) n^3 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{b(c + dx)}\right]}{b^3 d^3} + \\
& \frac{1}{b^3 d^3} 2 B^2 (bc - ad) (a^2 d^2 h^2 - abdh (3dg - ch) + b^2 (3d^2 g^2 - 3cdgh + c^2 h^2)) n^2 (A + B \operatorname{Log}[e (a + bx)^n (c + dx)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{b(c + dx)}\right] + \\
& \frac{B^3 (bc - ad)^3 h^2 n^3 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{d(a + bx)}\right]}{b^3 d^3} - \frac{2 B^3 (bc - ad) (a^2 d^2 h^2 - abdh (3dg - ch) + b^2 (3d^2 g^2 - 3cdgh + c^2 h^2)) n^3 \operatorname{PolyLog}\left[3, \frac{d(a + bx)}{b(c + dx)}\right]}{b^3 d^3}
\end{aligned}$$

Result (type 4, 7328 leaves):

$$\begin{aligned}
& - \frac{6 a A B^2 g^2 n^2}{b} - \frac{6 A B^2 c g^2 n^2}{d} + \frac{12 a A B^2 c g h n^2}{b d} - \frac{2 a A B^2 c^2 h^2 n^2}{b d^2} - \frac{2 a^2 A B^2 c h^2 n^2}{b^2 d} + \frac{6 a B^3 g^2 n^3}{b} - \frac{6 a^2 B^3 g h n^3}{b^2} - \frac{6 B^3 c^2 g h n^3}{d^2} + \frac{6 a B^3 c g h n^3}{b d} + \\
& \frac{2 a^3 B^3 h^2 n^3}{b^3} + \frac{2 B^3 c^3 h^2 n^3}{d^3} - \frac{a B^3 c^2 h^2 n^3}{b d^2} - \frac{a^2 B^3 c h^2 n^3}{b^2 d} + A^3 g^2 x + \frac{3 a A^2 B g h n x}{b} - \frac{3 A^2 B c g h n x}{d} - \frac{a^2 A^2 B h^2 n x}{b^2} + \frac{A^2 B c^2 h^2 n x}{d^2} + \\
& \frac{a^2 A B^2 h^2 n^2 x}{b^2} + \frac{A B^2 c^2 h^2 n^2 x}{d^2} - \frac{2 a A B^2 c h^2 n^2 x}{b d} + A^3 g h x^2 + \frac{a A^2 B h^2 n x^2}{2 b} - \frac{A^2 B c h^2 n x^2}{2 d} + \frac{1}{3} A^3 h^2 x^3 + \frac{3 a A^2 B g^2 n \operatorname{Log}[a + bx]}{b} - \\
& \frac{3 a^3 A^2 B g h n \operatorname{Log}[a + bx]}{b^2} + \frac{a^3 A^2 B h^2 n \operatorname{Log}[a + bx]}{b^3} + \frac{6 a^2 A B^2 g h n^2 \operatorname{Log}[a + bx]}{b^2} - \frac{6 a A B^2 c g h n^2 \operatorname{Log}[a + bx]}{b d} - \frac{3 a^3 A B^2 h^2 n^2 \operatorname{Log}[a + bx]}{b^3} + \\
& \frac{2 a A B^2 c^2 h^2 n^2 \operatorname{Log}[a + bx]}{b d^2} + \frac{a^2 A B^2 c h^2 n^2 \operatorname{Log}[a + bx]}{b^2 d} + \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a + bx]}{b} + \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a + bx]}{d} - \frac{12 a B^3 c g h n^3 \operatorname{Log}[a + bx]}{b d} + \\
& \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a + bx]}{b^3} + \frac{3 a B^3 c^2 h^2 n^3 \operatorname{Log}[a + bx]}{b d^2} - \frac{3 a A B^2 g^2 n^2 \operatorname{Log}[a + bx]^2}{b} + \frac{3 a^2 A B^2 g h n^2 \operatorname{Log}[a + bx]^2}{b^2} - \frac{a^3 A B^2 h^2 n^2 \operatorname{Log}[a + bx]^2}{b^3} - \\
& \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a + bx]^2}{b^2} + \frac{3 a B^3 c g h n^3 \operatorname{Log}[a + bx]^2}{b d} + \frac{3 a^3 B^3 h^2 n^3 \operatorname{Log}[a + bx]^2}{2 b^3} - \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[a + bx]^2}{b d^2} - \frac{a^2 B^3 c h^2 n^3 \operatorname{Log}[a + bx]^2}{2 b^2 d} +
\end{aligned}$$

$$\begin{aligned}
& \frac{a B^3 g^2 n^3 \operatorname{Log}[a + b x]^3}{b} - \frac{a^2 B^3 g h n^3 \operatorname{Log}[a + b x]^3}{b^2} + \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x]^3}{3 b^3} - \frac{3 A^2 B c g^2 n \operatorname{Log}[c + d x]}{d} + \frac{3 A^2 B c^2 g h n \operatorname{Log}[c + d x]}{d^2} - \\
& \frac{A^2 B c^3 h^2 n \operatorname{Log}[c + d x]}{d^3} + \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[c + d x]}{d^2} - \frac{6 a A B^2 c g h n^2 \operatorname{Log}[c + d x]}{b d} - \frac{3 A B^2 c^3 h^2 n^2 \operatorname{Log}[c + d x]}{d^3} + \frac{a A B^2 c^2 h^2 n^2 \operatorname{Log}[c + d x]}{b d^2} + \\
& \frac{2 a^2 A B^2 c h^2 n^2 \operatorname{Log}[c + d x]}{b^2 d} - \frac{6 a B^3 g^2 n^3 \operatorname{Log}[c + d x]}{b} - \frac{6 B^3 c g^2 n^3 \operatorname{Log}[c + d x]}{d} + \frac{12 a B^3 c g h n^3 \operatorname{Log}[c + d x]}{b d} - \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[c + d x]}{d^3} - \\
& \frac{3 a^2 B^3 c h^2 n^3 \operatorname{Log}[c + d x]}{b^2 d} + \frac{6 a A B^2 g^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b} + \frac{6 A B^2 c g^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{d} - \frac{6 a^2 A B^2 g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b^2} - \\
& \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{d^2} + \frac{2 a^3 A B^2 h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b^3} + \frac{2 A B^2 c^3 h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{d^3} - \\
& \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{d^2} + \frac{6 a B^3 c g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b d} + \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{d^3} - \\
& \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b d^2} - \frac{2 a^2 B^3 c h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]}{b^2 d} - \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{b} - \\
& \frac{3 B^3 c g^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{d} + \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{b^2} + \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{d^2} - \\
& \frac{2 a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{b^3} - \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x]}{d^3} - \frac{6 a A B^2 g^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b} + \\
& \frac{6 a^2 A B^2 g h n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b^2} - \frac{2 a^3 A B^2 h^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b^3} + \frac{6 a B^3 g^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b} - \\
& \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b^2} + \frac{2 a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]}{b^3} - \frac{3 A B^2 c g^2 n^2 \operatorname{Log}[c + d x]^2}{d} + \\
& \frac{3 A B^2 c^2 g h n^2 \operatorname{Log}[c + d x]^2}{d^2} - \frac{A B^2 c^3 h^2 n^2 \operatorname{Log}[c + d x]^2}{d^3} + \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[c + d x]^2}{d^2} - \frac{3 a B^3 c g h n^3 \operatorname{Log}[c + d x]^2}{b d} - \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[c + d x]^2}{2 d^3} + \\
& \frac{a B^3 c^2 h^2 n^3 \operatorname{Log}[c + d x]^2}{2 b d^2} + \frac{a^2 B^3 c h^2 n^3 \operatorname{Log}[c + d x]^2}{b^2 d} + \frac{3 a B^3 g^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{b} + \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{d} - \\
& \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{b^2} - \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{d^2} + \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{b^3} + \\
& \frac{2 B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2}{d^3} - \frac{3 a B^3 g^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{b} - \frac{3 B^3 c g^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{d} + \\
& \frac{3 a^2 B^3 g h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{b^2} + \frac{3 B^3 c^2 g h n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{d^2} - \frac{a^3 B^3 h^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{b^3} - \\
& \frac{B^3 c^3 h^2 n^3 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c + d x]^2}{d^3} - \frac{B^3 c g^2 n^3 \operatorname{Log}[c + d x]^3}{d} + \frac{B^3 c^2 g h n^3 \operatorname{Log}[c + d x]^3}{d^2} - \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[c + d x]^3}{3 d^3} -
\end{aligned}$$

$$\begin{aligned}
& \frac{6 A B^2 c g^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \frac{6 A B^2 c^2 g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{2 A B^2 c^3 h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \\
& \frac{6 a^2 B^3 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2} + \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \frac{12 a B^3 c g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b d} - \\
& \frac{3 a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^3} - \frac{3 B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} + \frac{3 a B^3 c^2 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b d^2} + \\
& \frac{3 a^2 B^3 c h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2 d} + \frac{3 a B^3 g^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b} + \frac{3 B^3 c g^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} - \\
& \frac{3 a^2 B^3 g h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^2} - \frac{3 B^3 c^2 g h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} + \frac{a^3 B^3 h^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{b^3} + \\
& \frac{B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \frac{6 B^3 c g^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d} + \frac{6 B^3 c^2 g h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^2} - \\
& \frac{2 B^3 c^3 h^2 n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{d^3} - \frac{6 a B^3 g^2 n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b} - \frac{6 B^3 c g^2 n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{d} + \\
& \frac{12 a B^3 c g h n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b d} - \frac{2 a B^3 c^2 h^2 n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b d^2} - \frac{2 a^2 B^3 c h^2 n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2 d} + \\
& 3 A^2 B g^2 x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \frac{6 a A B^2 g h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b} - \frac{6 A B^2 c g h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{d} - \\
& \frac{2 a^2 A B^2 h^2 n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2} + \frac{2 A B^2 c^2 h^2 n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{d^2} + \frac{a^2 B^3 h^2 n^2 x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2} + \\
& \frac{B^3 c^2 h^2 n^2 x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{d^2} - \frac{2 a B^3 c h^2 n^2 x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b d} + 3 A^2 B g h x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& \frac{a A B^2 h^2 n x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b} - \frac{A B^2 c h^2 n x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{d} + A^2 B h^2 x^3 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& \frac{6 a A B^2 g^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b} - \frac{6 a^2 A B^2 g h n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2} + \\
& \frac{2 a^3 A B^2 h^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^3} + \frac{6 a^2 B^3 g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2} - \\
& \frac{6 a B^3 c g h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b d} - \frac{3 a^3 B^3 h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^3} + \\
& \frac{2 a B^3 c^2 h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b d^2} + \frac{a^2 B^3 c h^2 n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]}{b^2 d} -
\end{aligned}$$

$$\begin{aligned}
& \frac{3 a B^3 g^2 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \frac{3 a^2 B^3 g h n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} - \\
& \frac{a^3 B^3 h^2 n^2 \operatorname{Log}[a+b x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^3} - \frac{6 A B^2 c g^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
& \frac{6 A B^2 c^2 g h n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{2 A B^2 c^3 h^2 n \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
& \frac{6 B^3 c^2 g h n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{6 a B^3 c g h n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d} - \\
& \frac{3 B^3 c^3 h^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \frac{a B^3 c^2 h^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b d^2} + \\
& \frac{2 a^2 B^3 c h^2 n^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2 d} + \frac{6 a B^3 g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
& \frac{6 B^3 c g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} - \frac{6 a^2 B^3 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} - \\
& \frac{6 B^3 c^2 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} + \frac{2 a^3 B^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^3} + \\
& \frac{2 B^3 c^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} - \frac{6 a B^3 g^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b} + \\
& \frac{6 a^2 B^3 g h n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^2} - \frac{2 a^3 B^3 h^2 n^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{b^3} - \\
& \frac{3 B^3 c g^2 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \frac{3 B^3 c^2 g h n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \\
& \frac{B^3 c^3 h^2 n^2 \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} - \frac{6 B^3 c g^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d} + \\
& \frac{6 B^3 c^2 g h n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^2} - \frac{2 B^3 c^3 h^2 n^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]}{d^3} + \\
& 3 A B^2 g^2 x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \frac{3 a B^3 g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{b} - \frac{3 B^3 c g h n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d} - \\
& \frac{a^2 B^3 h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{b^2} + \frac{B^3 c^2 h^2 n x \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{d^2} + 3 A B^2 g h x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
& \frac{a B^3 h^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{2 b} - \frac{B^3 c h^2 n x^2 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{2 d} + A B^2 h^2 x^3 \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2 + \\
& \frac{3 a B^3 g^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{b} - \frac{3 a^2 B^3 g h n \operatorname{Log}[a+b x] \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]^2}{b^2} +
\end{aligned}$$

$$\begin{aligned}
& \frac{a^3 B^3 h^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2}{b^3} - \frac{3 B^3 c g^2 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2}{d} + \\
& \frac{3 B^3 c^2 g h n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2}{d^2} - \frac{B^3 c^3 h^2 n \operatorname{Log}[c + d x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^2}{d^3} + \\
& B^3 g^2 x \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + B^3 g h x^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 + \frac{1}{3} B^3 h^2 x^3 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]^3 - \\
& \frac{1}{b^3 d^3} B^2 n^2 (6 A b^3 c d^2 g^2 - 6 A b^3 c^2 d g h + 2 A b^3 c^3 h^2 - 6 b^3 B c^2 d g h n + 12 a b^2 B c d^2 g h n - 6 a^2 b B d^3 g h n + 3 b^3 B c^3 h^2 n - 3 a b^2 B c^2 d h^2 n - \\
& 3 a^2 b B c d^2 h^2 n + 3 a^3 B d^3 h^2 n - 2 a B d^3 (3 b^2 g^2 - 3 a b g h + a^2 h^2) n \operatorname{Log}[a + b x] + 2 b^3 B c (3 d^2 g^2 - 3 c d g h + c^2 h^2) n \operatorname{Log}[c + d x] + 6 b^3 B c d^2 g^2 \\
& \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] - 6 b^3 B c^2 d g h \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 2 b^3 B c^3 h^2 \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - \\
& \frac{1}{b^3 d^3} 2 B^2 n^2 (-a B d^3 (3 b^2 g^2 - 3 a b g h + a^2 h^2) n \operatorname{Log}[a + b x] + b^3 B c (3 d^2 g^2 - 3 c d g h + c^2 h^2) n \operatorname{Log}[c + d x] + \\
& a d^3 (3 b^2 g^2 - 3 a b g h + a^2 h^2) (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - \frac{6 a B^3 g^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{b} + \\
& \frac{6 B^3 c g^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d} + \frac{6 a^2 B^3 g h n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{b^2} - \frac{6 B^3 c^2 g h n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} - \frac{2 a^3 B^3 h^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{b^3} + \\
& \frac{2 B^3 c^3 h^2 n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^3} - \frac{6 a B^3 g^2 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b} + \frac{6 B^3 c g^2 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d} + \frac{6 a^2 B^3 g h n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b^2} - \\
& \frac{6 B^3 c^2 g h n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d^2} - \frac{2 a^3 B^3 h^2 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b^3} + \frac{2 B^3 c^3 h^2 n^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{d^3}
\end{aligned}$$

Problem 310: Result more than twice size of optimal antiderivative.

$$\int (g + h x) (A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right])^3 dx$$

Optimal (type 4, 466 leaves, 13 steps):

$$\begin{aligned}
& - \frac{3 B^2 (b c - a d)^2 h n^2 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])}{b^2 d^2} - \frac{3 B (b c - a d) h n (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 b^2 d} + \\
& \frac{3 B (b c - a d) (2 b d g - b c h - a d h) n \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 b^2 d^2} - \frac{(b g - a h)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 b^2 h} + \\
& \frac{(g + h x)^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 h} - \frac{3 B^3 (b c - a d)^2 h n^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^2 d^2} + \\
& \frac{3 B^2 (b c - a d) (2 b d g - b c h - a d h) n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^2 d^2} - \\
& \frac{3 B^3 (b c - a d) (2 b d g - b c h - a d h) n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{b^2 d^2}
\end{aligned}$$

Result (type 4, 3919 leaves):

$$\begin{aligned}
& \frac{1}{2 b^2 d^2} \left(-12 A b^2 B^2 c d g n^2 - 12 a A b B^2 d^2 g n^2 + 12 a A b B^2 c d h n^2 + 12 a b B^3 d^2 g n^3 - 6 b^2 B^3 c^2 h n^3 + 6 a b B^3 c d h n^3 - 6 a^2 B^3 d^2 h n^3 + 2 A^3 b^2 d^2 g x - \right. \\
& 3 A^2 b^2 B c d h n x + 3 a A^2 b B d^2 h n x + A^3 b^2 d^2 h x^2 + 6 a A^2 b B d^2 g n \operatorname{Log}[a + b x] - 3 a^2 A^2 B d^2 h n \operatorname{Log}[a + b x] - 6 a A b B^2 c d h n^2 \operatorname{Log}[a + b x] + \\
& 6 a^2 A B^2 d^2 h n^2 \operatorname{Log}[a + b x] + 12 b^2 B^3 c d g n^3 \operatorname{Log}[a + b x] + 12 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x] - 12 a b B^3 c d h n^3 \operatorname{Log}[a + b x] - \\
& 6 a A b B^2 d^2 g n^2 \operatorname{Log}[a + b x]^2 + 3 a^2 A B^2 d^2 h n^2 \operatorname{Log}[a + b x]^2 + 3 a b B^3 c d h n^3 \operatorname{Log}[a + b x]^2 - 3 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x]^2 + \\
& 2 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x]^3 - a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x]^3 - 6 A^2 b^2 B c d g n \operatorname{Log}[c + d x] + 3 A^2 b^2 B c^2 h n \operatorname{Log}[c + d x] + 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[c + d x] - \\
& 6 a A b B^2 c d h n^2 \operatorname{Log}[c + d x] - 12 b^2 B^3 c d g n^3 \operatorname{Log}[c + d x] - 12 a b B^3 d^2 g n^3 \operatorname{Log}[c + d x] + 12 a b B^3 c d h n^3 \operatorname{Log}[c + d x] + \\
& 12 A b^2 B^2 c d g n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 12 a A b B^2 d^2 g n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - \\
& 6 a^2 A B^2 d^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + 6 a b B^3 c d h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] - \\
& 6 b^2 B^3 c d g n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 12 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] + 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] + \\
& 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c + d x] - 12 a A b B^2 d^2 g n^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] + 6 a^2 A B^2 d^2 h n^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] + \\
& 12 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] - 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] - \\
& 6 A b^2 B^2 c d g n^2 \operatorname{Log}[c + d x]^2 + 3 A b^2 B^2 c^2 h n^2 \operatorname{Log}[c + d x]^2 + 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[c + d x]^2 - 3 a b B^3 c d h n^3 \operatorname{Log}[c + d x]^2 + \\
& 12 b^2 B^3 c d g n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 + 6 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 - 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 - \\
& 3 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x]^2 - 6 b^2 B^3 c d g n^3 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 - 6 a b B^3 d^2 g n^3 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 + \\
& 3 b^2 B^3 c^2 h n^3 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 + 3 a^2 B^3 d^2 h n^3 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x]^2 - 2 b^2 B^3 c d g n^3 \operatorname{Log}[c + d x]^3 + b^2 B^3 c^2 h n^3 \operatorname{Log}[c + d x]^3 - \\
& 12 A b^2 B^2 c d g n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 6 A b^2 B^2 c^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - \\
& 12 a b B^3 c d h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 6 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 6 b^2 B^3 c d g n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] +
\end{aligned}$$

$$\begin{aligned}
& 6 a b B^3 d^2 g n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 3 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 3 a^2 B^3 d^2 h n^3 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 12 b^2 B^3 c d g n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 6 b^2 B^3 c^2 h n^3 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& 12 b^2 B^3 c d g n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 12 a b B^3 d^2 g n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 12 a b B^3 c d h n^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 6 A^2 b^2 B d^2 g x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 6 A b^2 B^2 c d h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 6 a A b B^2 d^2 h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 3 A^2 b^2 B d^2 h x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 12 a A b B^2 d^2 g n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - \\
& 6 a^2 A B^2 d^2 h n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 6 a b B^3 c d h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 6 a^2 B^3 d^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 6 a b B^3 d^2 g n^2 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 3 a^2 B^3 d^2 h n^2 \operatorname{Log}[a + b x]^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 12 A b^2 B^2 c d g n \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 6 A b^2 B^2 c^2 h n \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 6 b^2 B^3 c^2 h n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - \\
& 6 a b B^3 c d h n^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 12 b^2 B^3 c d g n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 12 a b B^3 d^2 g n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 6 b^2 B^3 c^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - \\
& 6 a^2 B^3 d^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 12 a b B^3 d^2 g n^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 6 a^2 B^3 d^2 h n^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 6 b^2 B^3 c d g n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 3 b^2 B^3 c^2 h n^2 \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] - 12 b^2 B^3 c d g n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + \\
& 6 b^2 B^3 c^2 h n^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + 6 A b^2 B^2 d^2 g x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 3 b^2 B^3 c d h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 + 3 a b B^3 d^2 h n x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 + 3 A b^2 B^2 d^2 h x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 + \\
& 6 a b B^3 d^2 g n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 - 3 a^2 B^3 d^2 h n \operatorname{Log}[a + b x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 - \\
& 6 b^2 B^3 c d g n \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 + 3 b^2 B^3 c^2 h n \operatorname{Log}[c + d x] \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^2 + \\
& 2 b^2 B^3 d^2 g x \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^3 + b^2 B^3 d^2 h x^2 \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]^3 + \\
& 6 B^2 n^2 (-2 A b^2 c d g + A b^2 c^2 h + b^2 B c^2 h n - 2 a b B c d h n + a^2 B d^2 h n + a B d^2 (2 b g - a h) n \operatorname{Log}[a + b x] + b^2 B c (-2 d g + c h) n \operatorname{Log}[c + d x] - \\
& \quad 2 b^2 B c d g \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right] + b^2 B c^2 h \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\
& 6 B^2 n^2 (a B d^2 (2 b g - a h) n \operatorname{Log}[a + b x] + b^2 B c (-2 d g + c h) n \operatorname{Log}[c + d x] + a d^2 (-2 b g + a h) (A + B \operatorname{Log}\left[e(a + b x)^n (c + d x)^{-n}\right])) \\
& \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] + 12 b^2 B^3 c d g n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 12 a b B^3 d^2 g n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - \\
& 6 b^2 B^3 c^2 h n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] + 6 a^2 B^3 d^2 h n^3 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] + 12 b^2 B^3 c d g n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] - \\
& 12 a b B^3 d^2 g n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] - 6 b^2 B^3 c^2 h n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] + 6 a^2 B^3 d^2 h n^3 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right]
\end{aligned}$$

Problem 311: Result more than twice size of optimal antiderivative.

$$\int (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3 dx$$

Optimal (type 4, 203 leaves, 6 steps):

$$\frac{3 B (b c - a d) n \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{b d} + \frac{(a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{b} +$$

$$\frac{6 B^2 (b c - a d) n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b d} - \frac{6 B^3 (b c - a d) n^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{b d}$$

Result (type 4, 1465 leaves):

$$\begin{aligned}
& -\frac{1}{bd} \\
& \left(6AbB^2cn^2 + 6aAB^2dn^2 - 6aB^3dn^3 - A^3bdx - 3aA^2Bdn \operatorname{Log}[a+bx] - 6bB^3cn^3 \operatorname{Log}[a+bx] - 6aB^3dn^3 \operatorname{Log}[a+bx] + 3aAB^2dn^2 \operatorname{Log}[a+bx]^2 - \right. \\
& aB^3dn^3 \operatorname{Log}[a+bx]^3 + 3A^2bBcn \operatorname{Log}[c+dx] + 6bB^3cn^3 \operatorname{Log}[c+dx] + 6aB^3dn^3 \operatorname{Log}[c+dx] - 6AbB^2cn^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] - \\
& 6aAB^2dn^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] + 3bB^3cn^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}[c+dx] + 6aB^3dn^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}[c+dx] + \\
& 6aAB^2dn^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] - 6aB^3dn^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] + 3AbB^2cn^2 \operatorname{Log}[c+dx]^2 - \\
& 6bB^3cn^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 - 3aB^3dn^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx]^2 + 3bB^3cn^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 + \\
& 3aB^3dn^3 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 + bB^3cn^3 \operatorname{Log}[c+dx]^3 + 6AbB^2cn^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 3bB^3cn^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 3aB^3dn^3 \operatorname{Log}[a+bx]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 6bB^3cn^3 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 6bB^3cn^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6aB^3dn^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - 3A^2bBdx \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6aAB^2dn \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 3aB^3dn^2 \operatorname{Log}[a+bx]^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + \\
& 6AbB^2cn \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - 6bB^3cn^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 6aB^3dn^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6aB^3dn^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + \\
& 3bB^3cn^2 \operatorname{Log}[c+dx]^2 \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] + 6bB^3cn^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] - \\
& 3AbB^2dx \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 - 3aB^3dn \operatorname{Log}[a+bx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 + \\
& 3bB^3cn \operatorname{Log}[c+dx] \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^2 - bB^3dx \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]^3 + \\
& 6B^2n^2(-aBdn \operatorname{Log}[a+bx] + bc(A+Bn \operatorname{Log}[c+dx] + B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 6B^2n^2(-aBdn \operatorname{Log}[a+bx] + bBcn \operatorname{Log}[c+dx] + ad(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 6bB^3cn^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 6aB^3dn^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6bB^3cn^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 6aB^3dn^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \left. \right)
\end{aligned}$$

Problem 312: Unable to integrate problem.

$$\int \frac{(A+B \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])^3}{g+hx} dx$$

Optimal (type 4, 425 leaves, 12 steps):

$$\begin{aligned}
& - \frac{\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{h} + \\
& \frac{\left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3 \text{Log}\left[1-\frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} - \frac{3Bn \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{h} + \\
& \frac{3Bn \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^2 \text{PolyLog}\left[2, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} + \frac{6B^2n^2 \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right) \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{h} - \\
& \frac{6B^2n^2 \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right) \text{PolyLog}\left[3, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h} - \frac{6B^3n^3 \text{PolyLog}\left[4, \frac{d(a+bx)}{b(c+dx)}\right]}{h} + \frac{6B^3n^3 \text{PolyLog}\left[4, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{h}
\end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{\left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{g+hx} dx$$

Problem 313: Unable to integrate problem.

$$\int \frac{\left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{(g+hx)^2} dx$$

Optimal (type 4, 302 leaves, 6 steps):

$$\begin{aligned}
& \frac{(a+bx) \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{(bg-ah)(g+hx)} + \frac{3B(bc-ad)n \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^2 \text{Log}\left[1-\frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(dg-ch)} + \\
& \frac{6B^2(bc-ad)n^2 \left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right) \text{PolyLog}\left[2, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(dg-ch)} - \frac{6B^3(bc-ad)n^3 \text{PolyLog}\left[3, \frac{(dg-ch)(a+bx)}{(bg-ah)(c+dx)}\right]}{(bg-ah)(dg-ch)}
\end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{\left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{(g+hx)^2} dx$$

Problem 314: Unable to integrate problem.

$$\int \frac{\left(A+B \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right]\right)^3}{(g+hx)^3} dx$$

Optimal (type 4, 629 leaves, 13 steps):

$$\begin{aligned}
& \frac{3 B (b c - a d) h n (a + b x) (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{2 (b g - a h)^2 (d g - c h) (g + h x)} + \frac{b^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 h (b g - a h)^2} - \\
& \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{2 h (g + h x)^2} + \frac{3 B^2 (b c - a d)^2 h n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} + \\
& \frac{3 B (b c - a d) (2 b d g - b c h - a d h) n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{Log}\left[1 - \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{2 (b g - a h)^2 (d g - c h)^2} + \frac{3 B^3 (b c - a d)^2 h n^3 \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} + \\
& \frac{3 B^2 (b c - a d) (2 b d g - b c h - a d h) n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2} - \\
& \frac{3 B^3 (b c - a d) (2 b d g - b c h - a d h) n^3 \operatorname{PolyLog}\left[3, \frac{(d g - c h) (a + b x)}{(b g - a h) (c + d x)}\right]}{(b g - a h)^2 (d g - c h)^2}
\end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(g + h x)^3} dx$$

Test results for the 263 problems in "3.2.2 (f+g x)^m (h+i x)^q (A+B log(e ((a+b x) over (c+d x))^n))^p.m"

Problem 6: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) (A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right])}{(a g + b g x)^2} dx$$

Optimal (type 4, 142 leaves, 5 steps):

$$\frac{B i (c + d x)}{b g^2 (a + b x)} - \frac{i (c + d x) (A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right])}{b g^2 (a + b x)} - \frac{d i (A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g^2} + \frac{B d i \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g^2}$$

Result (type 4, 317 leaves):

$$\frac{1}{2 b^2 g^2} i \left(\frac{2 A (-b c + a d)}{a + b x} + 2 A d \operatorname{Log}[a + b x] + 2 b B c \left(\frac{d \operatorname{Log}\left[\frac{c}{d} + x\right]}{b c - a d} + \frac{d \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right]}{-b c + a d} - \frac{1 + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{a + b x} \right) + \right. \\ \left. B d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) + \right. \\ \left. \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c+d x]\right)\right)}{(b c - a d)(a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]\right) \right) \right)$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{a g + b g x} dx$$

Optimal (type 4, 276 leaves, 10 steps):

$$-\frac{B d (b c - a d) i^2 x}{2 b^2 g} - \frac{B (b c - a d)^2 i^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{2 b^3 g} + \frac{d (b c - a d) i^2 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{b^3 g} + \frac{i^2 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{2 b g} - \\ \frac{3 B (b c - a d)^2 i^2 \operatorname{Log}[c + d x]}{2 b^3 g} - \frac{(b c - a d)^2 i^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g} + \frac{B (b c - a d)^2 i^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g}$$

Result (type 4, 615 leaves):

$$\frac{1}{2 b^3 g} \\ i^2 \left(4 b^2 B c^2 - 6 a b B c d + 2 a^2 B d^2 + 4 A b^2 c d x - b^2 B c d x - 2 a A b d^2 x + a b B d^2 x + A b^2 d^2 x^2 + B (b c - a d)^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 a b B c \right. \\ \left. d \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 A b^2 c^2 \operatorname{Log}[a + b x] - 4 a A b c d \operatorname{Log}[a + b x] + 2 a^2 A d^2 \operatorname{Log}[a + b x] - a^2 B d^2 \operatorname{Log}[a + b x] + 2 b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \\ \left. 4 a b B c d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 2 a^2 B d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 B \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d (-2 b c + a d) + (b c - a d)^2 \operatorname{Log}[a + b x]\right) - \right. \\ \left. 2 b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 4 a b B c d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] - 2 a^2 B d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \\ \left. 4 b^2 B c d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 2 a b B d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + b^2 B d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 b^2 B c^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \right. \\ \left. 4 a b B c d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 a^2 B d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + b^2 B c^2 \operatorname{Log}[c + d x] - 2 B (b c - a d)^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right)$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 247 leaves, 8 steps):

$$\begin{aligned} & - \frac{B (b c - a d) i^2 (c + d x)}{b^2 g^2 (a + b x)} + \frac{d^2 i^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^3 g^2} - \frac{(b c - a d) i^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^2 g^2 (a + b x)} \\ & - \frac{B d (b c - a d) i^2 \operatorname{Log}[c + d x]}{b^3 g^2} - \frac{2 d (b c - a d) i^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^2} + \frac{2 B d (b c - a d) i^2 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^2} \end{aligned}$$

Result (type 4, 595 leaves):

$$\begin{aligned} & \frac{1}{b^3 g^2} i^2 \\ & \left(A b d^2 x - \frac{A (b c - a d)^2}{a + b x} + 2 A d (b c - a d) \operatorname{Log}[a + b x] - \frac{b^2 B c^2 \left(-d (a + b x) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + (b c - a d) \left(1 + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \right)}{(b c - a d) (a + b x)} + \right. \\ & b B c d \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \frac{2 a \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) + \right. \\ & \left. \frac{2 a \left((-b c + a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) - \\ & B d^2 \left(- (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \frac{a^2 \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{a + b x} + b \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \right. \\ & \left(b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) + \\ & \left. \frac{a^2 \left((-b c + a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 a \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) \end{aligned}$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 230 leaves, 7 steps):

$$\begin{aligned} & -\frac{B d i^2 (c + d x)}{b^2 g^3 (a + b x)} - \frac{B i^2 (c + d x)^2}{4 b g^3 (a + b x)^2} - \frac{d i^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^2 g^3 (a + b x)} \\ & - \frac{i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 b g^3 (a + b x)^2} - \frac{d^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} + \frac{B d^2 i^2 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} \end{aligned}$$

Result (type 4, 788 leaves):

$$\begin{aligned} & \frac{1}{4 b^3 g^3} \\ & i^2 \left(-\frac{2 A (b c - a d)^2}{(a + b x)^2} + \frac{8 A d (-b c + a d)}{a + b x} + 4 A d^2 \operatorname{Log} [a + b x] - \frac{1}{(b c - a d)^2 (a + b x)^2} b^2 B c^2 \left(b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + \right. \right. \\ & \quad \left. \left. 2 d^2 (a + b x)^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 2 d^2 (a + b x)^2 \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 b^2 c^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] - 4 a b c d \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + 2 a^2 d^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) - \\ & \quad \frac{1}{(b c - a d)^2 (a + b x)^2} 2 b B c d \left(3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - 2 d (-2 b c + a d) (a + b x)^2 \operatorname{Log} [a + b x] + \right. \\ & \quad \left. 2 (b c - a d)^2 (a + 2 b x) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] - 4 a^2 b c d \operatorname{Log} [c + d x] + 2 a^3 d^2 \operatorname{Log} [c + d x] - \right. \\ & \quad \left. 8 a b^2 c d x \operatorname{Log} [c + d x] + 4 a^2 b d^2 x \operatorname{Log} [c + d x] - 4 b^3 c d x^2 \operatorname{Log} [c + d x] + 2 a b^2 d^2 x^2 \operatorname{Log} [c + d x] \right) + \\ & B d^2 \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \frac{8 a \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{a + b x} - \frac{a^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{(a + b x)^2} + 2 \left(\frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log} [a + b x] \right) \right. \\ & \quad \left. \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) + \frac{8 a \left((-b c + a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x] \right) \right)}{(b c - a d) (a + b x)} + \right. \\ & \quad \left. \frac{2 a^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d (a+bx) (b c - a d + d (a+bx) \operatorname{Log} [a+bx] - d (a+bx) \operatorname{Log} [c+dx])}{(b c - a d)^2} \right)}{(a + b x)^2} - 4 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(a g + b g x)^4} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B i^2 (c + d x)^3}{9 (b c - a d) g^4 (a + b x)^3} - \frac{i^2 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 (b c - a d) g^4 (a + b x)^3}$$

Result (type 3, 186 leaves):

$$\frac{1}{9 b^3 g^4} i^2 \left(-\frac{(3 A + B) (b c - a d)^2}{(a + b x)^3} + \frac{3 (3 A + B) d (-b c + a d)}{(a + b x)^2} - \frac{3 (3 A + B) d^2}{a + b x} + \frac{3 B d^3 \operatorname{Log}[a + b x]}{-b c + a d} - \frac{3 B (a^2 d^2 + a b d (c + 3 d x) + b^2 (c^2 + 3 c d x + 3 d^2 x^2)) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right]}{(a + b x)^3} + \frac{3 B d^3 \operatorname{Log}[c + d x]}{b c - a d} \right)$$

Problem 24: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{a g + b g x} dx$$

Optimal (type 4, 356 leaves, 14 steps):

$$\begin{aligned} & -\frac{5 B d (b c - a d)^2 i^3 x}{6 b^3 g} - \frac{B (b c - a d) i^3 (c + d x)^2}{6 b^2 g} - \frac{5 B (b c - a d)^3 i^3 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{6 b^4 g} + \\ & \frac{d (b c - a d)^2 i^3 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^4 g} + \frac{(b c - a d) i^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 b^2 g} + \frac{i^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b g} - \\ & \frac{11 B (b c - a d)^3 i^3 \operatorname{Log}[c + d x]}{6 b^4 g} - \frac{(b c - a d)^3 i^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} + \frac{B (b c - a d)^3 i^3 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} \end{aligned}$$

Result (type 4, 1004 leaves):

$$\begin{aligned} & \frac{1}{6 b^4 g} i^3 \left(18 b^3 B c^3 - 36 a b^2 B c^2 d + 24 a^2 b B c d^2 - 6 a^3 B d^3 + 18 A b^3 c^2 d x - 7 b^3 B c^2 d x - 18 a A b^2 c d^2 x + 12 a b^2 B c d^2 x + 6 a^2 A b d^3 x - \right. \\ & 5 a^2 b B d^3 x + 9 A b^3 c d^2 x^2 - b^3 B c d^2 x^2 - 3 a A b^2 d^3 x^2 + a b^2 B d^3 x^2 + 2 A b^3 d^3 x^3 + 3 B (b c - a d)^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\ & 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 6 A b^3 c^3 \operatorname{Log}[a + b x] - 18 a A b^2 c^2 d \operatorname{Log}[a + b x] + 18 a^2 A b c d^2 \operatorname{Log}[a + b x] - \\ & 9 a^2 b B c d^2 \operatorname{Log}[a + b x] - 6 a^3 A d^3 \operatorname{Log}[a + b x] + 5 a^3 B d^3 \operatorname{Log}[a + b x] + 6 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\ & 18 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^3 B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 6 B \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d (3 b^2 c^2 - 3 a b c d + a^2 d^2) - (b c - a d)^3 \operatorname{Log}[a + b x] \right) - \\ & 6 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 18 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\ & 6 a^3 B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 b^3 B c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 a^2 b B d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 9 b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 3 a b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 b^3 B c^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a b^2 B c^2 d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 18 a^2 b B c d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\ & 6 a^3 B d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 7 b^3 B c^3 \operatorname{Log}[c + d x] - 3 a b^2 B c^2 d \operatorname{Log}[c + d x] - 6 B (b c - a d)^3 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \left. \right) \end{aligned}$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 373 leaves, 11 steps):

$$\begin{aligned} & -\frac{B d^2 (b c - a d) i^3 x}{2 b^3 g^2} - \frac{B (b c - a d)^2 i^3 (c + d x)}{b^3 g^2 (a + b x)} - \frac{B d (b c - a d)^2 i^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]}{2 b^4 g^2} + \frac{2 d^2 (b c - a d) i^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{b^4 g^2} - \\ & \frac{(b c - a d)^2 i^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{b^3 g^2 (a + b x)} + \frac{d i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{2 b^2 g^2} - \frac{5 B d (b c - a d)^2 i^3 \operatorname{Log}[c + d x]}{2 b^4 g^2} - \\ & \frac{3 d (b c - a d)^2 i^3 \left(A + B \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \operatorname{Log}\left[1 - \frac{b(c + d x)}{d(a + b x)}\right]}{b^4 g^2} + \frac{3 B d (b c - a d)^2 i^3 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{d(a + b x)}\right]}{b^4 g^2} \end{aligned}$$

Result (type 4, 967 leaves):

$$\begin{aligned}
& \frac{1}{2 b^4 g^2} i^3 \left(2 A b d^2 (3 b c - 2 a d) x + A b^2 d^3 x^2 - \frac{2 A (b c - a d)^3}{a + b x} + 6 A d (b c - a d)^2 \operatorname{Log}[a + b x] - \right. \\
& \left. \frac{2 b^3 B c^3 \left(-d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \right)}{(b c - a d) (a + b x)} + B d^3 \right. \\
& \left(4 a^2 - \frac{4 a b c}{d} + a b x - \frac{b^2 c x}{d} + \frac{2 a^3}{a + b x} + 3 a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{4 a b c \operatorname{Log}\left[\frac{c}{d} + x\right]}{d} - a^2 \operatorname{Log}[a + b x] + \frac{2 a^3 d \operatorname{Log}[a + b x]}{b c - a d} + 6 a^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \\
& 2 a^2 \operatorname{Log}\left[\frac{a}{b} + x\right] (2 + 3 \operatorname{Log}[a + b x]) - 6 a^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] - 4 a b x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + b^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
& \left. \frac{2 a^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{a + b x} + 6 a^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \frac{b^2 c^2 \operatorname{Log}[c + d x]}{d^2} + \frac{2 a^3 d \operatorname{Log}[c + d x]}{-b c + a d} - 6 a^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \\
& 3 b^2 B c^2 d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \right. \\
& \left. \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) - \\
& 6 b B c d^2 \left(- (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + a \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{a^2 (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a + b x} + b \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - \right. \\
& \left(b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \\
& \left. \frac{a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} - 2 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 26: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 345 leaves, 9 steps):

$$\begin{aligned}
& - \frac{2 B d (b c - a d) i^3 (c + d x)}{b^3 g^3 (a + b x)} - \frac{B (b c - a d) i^3 (c + d x)^2}{4 b^2 g^3 (a + b x)^2} + \frac{d^3 i^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{b^4 g^3} - \\
& \frac{2 d (b c - a d) i^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{2 b^2 g^3 (a + b x)^2} - \frac{B d^2 (b c - a d) i^3 \operatorname{Log}[c + d x]}{b^4 g^3} - \\
& \frac{3 d^2 (b c - a d) i^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^3} + \frac{3 B d^2 (b c - a d) i^3 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^3}
\end{aligned}$$

Result (type 4, 1170 leaves):

$$\begin{aligned}
& \frac{1}{4 b^4 g^3} i^3 \left(4 A b d^3 x - \frac{2 A (b c - a d)^3}{(a + b x)^2} - \frac{12 A d (b c - a d)^2}{a + b x} + 12 A d^2 (b c - a d) \operatorname{Log}[a + b x] - \right. \\
& \frac{1}{(b c - a d)^2 (a + b x)^2} b^2 B c^3 \left(b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\
& \left. 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 b^2 c^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 a b c d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a^2 d^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) - \\
& \frac{1}{(b c - a d)^2 (a + b x)^2} 3 b^2 B c^2 d \left(3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - 2 d (-2 b c + a d) (a + b x)^2 \operatorname{Log}[a + b x] + \right. \\
& 2 (b c - a d)^2 (a + 2 b x) \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 a^2 b c d \operatorname{Log}[c + d x] + 2 a^3 d^2 \operatorname{Log}[c + d x] - \\
& \left. 8 a b^2 c d x \operatorname{Log}[c + d x] + 4 a^2 b d^2 x \operatorname{Log}[c + d x] - 4 b^3 c d x^2 \operatorname{Log}[c + d x] + 2 a b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) + \\
& 3 b B c d^2 \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{8 a (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a + b x} - \frac{a^2 (1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right])}{(a + b x)^2} + 2 \left(\frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log}[a + b x] \right) \right. \\
& \left. \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) + \frac{8 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} + \right. \\
& \left. \frac{2 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a + b x) (b c - a d + d(a + b x) \operatorname{Log}[a + b x] - d(a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(a + b x)^2} - 4 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) - \\
& B d^3 \left(-4 (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 6 a \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{12 a^2 (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a + b x} - \frac{a^3 (1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right])}{(a + b x)^2} + 4 b \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \\
& 2 \left(-2 b x + \frac{a^2 (5 a + 6 b x)}{(a + b x)^2} + 6 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) + \\
& \frac{12 a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} + \\
& \left. \frac{2 a^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a + b x) (b c - a d + d(a + b x) \operatorname{Log}[a + b x] - d(a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(a + b x)^2} - 12 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 27: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(a g + b g x)^4} dx$$

Optimal (type 4, 310 leaves, 9 steps):

$$\begin{aligned} & - \frac{B d^2 i^3 (c + d x)}{b^3 g^4 (a + b x)} - \frac{B d i^3 (c + d x)^2}{4 b^2 g^4 (a + b x)^2} - \frac{B i^3 (c + d x)^3}{9 b g^4 (a + b x)^3} - \frac{d^2 i^3 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^3 g^4 (a + b x)} - \frac{d i^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 b^2 g^4 (a + b x)^2} \\ & - \frac{i^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b g^4 (a + b x)^3} - \frac{d^3 i^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g^4} + \frac{B d^3 i^3 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g^4} \end{aligned}$$

Result (type 4, 1407 leaves):

$$\begin{aligned} & \frac{1}{36 b^4 g^4} i^3 \left(- \frac{12 A (b c - a d)^3}{(a + b x)^3} - \frac{54 A d (b c - a d)^2}{(a + b x)^2} + \frac{108 A d^2 (-b c + a d)}{a + b x} + \right. \\ & 36 A d^3 \operatorname{Log}[a + b x] - \frac{1}{(b c - a d)^3 (a + b x)^3} 2 b^3 B c^3 \left(2 b^3 c^3 - 9 a b^2 c^2 d + 18 a^2 b c d^2 - 2 a^3 d^3 - 3 b^3 c^2 d x + 18 a b^2 c d^2 x + \right. \\ & 12 a^2 b d^3 x + 6 b^3 c d^2 x^2 + 21 a b^2 d^3 x^2 + 9 b^3 d^3 x^3 - 6 d^3 (a + b x)^3 \operatorname{Log} \left[\frac{c}{d} + x \right] + 6 d^3 (a + b x)^3 \operatorname{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] + \\ & \left. 6 b^3 c^3 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] - 18 a b^2 c^2 d \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + 18 a^2 b c d^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] - 6 a^3 d^3 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) + \\ & 3 b^2 B c^2 d \left(- \frac{9 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{(a + b x)^2} + \frac{4 a \left(1 + 3 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{(a + b x)^3} + \frac{6 (a + 3 b x) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(a + b x)^3} + \right. \\ & \left. 6 a \left(- \frac{2 \operatorname{Log} \left[\frac{c}{d} + x \right]}{(a + b x)^3} + \frac{d \left(\frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x] \right)}{(b c - a d)^3} \right) \right) + \\ & \left. \frac{18 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{(a + b x)^2} \right) - \\ & 6 b B c d^2 \left(\frac{18 \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{a + b x} - \frac{9 a \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{(a + b x)^2} + \frac{2 a^2 \left(1 + 3 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{(a + b x)^3} - \right. \end{aligned}$$

$$\begin{aligned}
& \frac{6 (a^2 + 3 a b x + 3 b^2 x^2) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)}{(a+bx)^3} + \frac{18 \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) (\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]) \right)}{(bc-ad)(a+bx)} + \\
& 3 a^2 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a+bx)^3} + \frac{d \left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2 d^2 \operatorname{Log}[a+bx] - 2 d^2 \operatorname{Log}[c+dx] \right)}{(bc-ad)^3} \right) + \\
& \frac{18 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{(a+bx)^2} \Bigg) + \\
& B d^3 \left(18 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{108 a (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a+bx} - \frac{27 a^2 (1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right])}{(a+bx)^2} + \frac{4 a^3 (1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right])}{(a+bx)^3} + \right. \\
& \left. 6 \left(\frac{a (11 a^2 + 27 a b x + 18 b^2 x^2)}{(a+bx)^3} + 6 \operatorname{Log}[a+bx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) + \right. \\
& \left. \frac{108 a \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) (\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]) \right)}{(bc-ad)(a+bx)} + \right. \\
& \left. 6 a^3 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a+bx)^3} + \frac{d \left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2 d^2 \operatorname{Log}[a+bx] - 2 d^2 \operatorname{Log}[c+dx] \right)}{(bc-ad)^3} \right) + \right. \\
& \left. \frac{54 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{(a+bx)^2} - 36 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \Bigg)
\end{aligned}$$

Problem 28: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)}{(a g + b g x)^5} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B i^3 (c+dx)^4}{16 (bc-ad) g^5 (a+bx)^4} - \frac{i^3 (c+dx)^4 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)}{4 (bc-ad) g^5 (a+bx)^4}$$

Result (type 3, 248 leaves):

$$\frac{1}{16 b^4 (b c - a d) g^5 (a + b x)^4} i^3 \left(- (4 A + B) (b c - a d)^4 + 4 (4 A + B) d (-b c + a d)^3 (a + b x) - \right. \\ \left. 6 (4 A + B) d^2 (b c - a d)^2 (a + b x)^2 + 4 (4 A + B) d^3 (-b c + a d) (a + b x)^3 - 4 B d^4 (a + b x)^4 \operatorname{Log}[a + b x] - \right. \\ \left. 4 B (b c - a d) \left((b c - a d)^3 + 4 d (b c - a d)^2 (a + b x) + 6 d^2 (b c - a d) (a + b x)^2 + 4 d^3 (a + b x)^3 \right) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 4 B d^4 (a + b x)^4 \operatorname{Log}[c + d x] \right)$$

Problem 31: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{c i + d i x} dx$$

Optimal (type 4, 252 leaves, 6 steps):

$$\frac{g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{3 d i} - \frac{(b c - a d) g^3 (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{6 d^2 i} + \frac{(b c - a d)^2 g^3 (a + b x) \left(6 A + 5 B + 6 B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{6 d^3 i} + \\ \frac{(b c - a d)^3 g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(6 A + 11 B + 6 B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{6 d^4 i} + \frac{B (b c - a d)^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i}$$

Result (type 4, 947 leaves):

$$\frac{1}{6 d^4 i} g^3 \left(6 b^3 B c^3 - 24 a b^2 B c^2 d + 36 a^2 b B c d^2 - 18 a^3 B d^3 + 6 A b^3 c^2 d x + 5 b^3 B c^2 d x - 18 a A b^2 c d^2 x - 12 a b^2 B c d^2 x + 18 a^2 A b d^3 x + \right. \\ \left. 7 a^2 b B d^3 x - 3 A b^3 c d^2 x^2 - b^3 B c d^2 x^2 + 9 a A b^2 d^3 x^2 + a b^2 B d^3 x^2 + 2 A b^3 d^3 x^3 - 6 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\ \left. 18 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 9 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 9 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^3 B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\ \left. 3 a^2 b B c d^2 \operatorname{Log}[a + b x] - 7 a^3 B d^3 \operatorname{Log}[a + b x] + 6 b^3 B c^2 d x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - 18 a b^2 B c d^2 x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \right. \\ \left. 18 a^2 b B d^3 x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - 3 b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 9 a b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 2 b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - \right. \\ \left. 6 A b^3 c^3 \operatorname{Log}[c + d x] - 5 b^3 B c^3 \operatorname{Log}[c + d x] + 18 a A b^2 c^2 d \operatorname{Log}[c + d x] + 9 a b^2 B c^2 d \operatorname{Log}[c + d x] - 18 a^2 A b c d^2 \operatorname{Log}[c + d x] + \right. \\ \left. 6 a^3 A d^3 \operatorname{Log}[c + d x] - 6 b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 18 a^2 b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \right. \\ \left. 6 a^3 B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^3 B c^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + 18 a b^2 B c^2 d \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - \right. \\ \left. 18 a^2 b B c d^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + 6 a^3 B d^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 6 B \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \\ \left. \left(-a d (b^2 c^2 - 3 a b c d + 3 a^2 d^2) - (b c - a d)^3 \operatorname{Log}[c + d x] + (b c - a d)^3 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 6 B (b c - a d)^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right)$$

Problem 32: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 198 leaves, 5 steps):

$$\frac{g^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 d i} - \frac{(b c - a d) g^2 (a + b x) \left(2 A + B + 2 B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 d^2 i} - \frac{(b c - a d)^2 g^2 \operatorname{Log} \left[\frac{b c - a d}{b (c+dx)} \right] \left(2 A + 3 B + 2 B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 d^3 i} - \frac{B (b c - a d)^2 g^2 \operatorname{PolyLog} \left[2, \frac{d (a+bx)}{b (c+dx)} \right]}{d^3 i}$$

Result (type 4, 575 leaves):

$$\begin{aligned} & \frac{1}{2 d^3 i} g^2 \left(-2 b^2 B c^2 + 6 a b B c d - 4 a^2 B d^2 - 2 A b^2 c d x - b^2 B c d x + 4 a A b d^2 x + a b B d^2 x + A b^2 d^2 x^2 + 2 b^2 B c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 4 a b B c d \operatorname{Log} \left[\frac{c}{d} + x \right] - \right. \\ & b^2 B c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 a b B c d \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - a^2 B d^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - a^2 B d^2 \operatorname{Log} [a + b x] - 2 b^2 B c d x \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + \\ & 4 a b B d^2 x \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + b^2 B d^2 x^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + 2 A b^2 c^2 \operatorname{Log} [c + d x] + b^2 B c^2 \operatorname{Log} [c + d x] - 4 a A b c d \operatorname{Log} [c + d x] + \\ & 2 a^2 A d^2 \operatorname{Log} [c + d x] + 2 b^2 B c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] - 4 a b B c d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + 2 a^2 B d^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + \\ & 2 b^2 B c^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \operatorname{Log} [c + d x] - 4 a b B c d \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \operatorname{Log} [c + d x] + 2 a^2 B d^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \operatorname{Log} [c + d x] - \\ & \left. 2 B \operatorname{Log} \left[\frac{a}{b} + x \right] \left(a d (b c - 2 a d) + (b c - a d)^2 \operatorname{Log} [c + d x] - (b c - a d)^2 \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + 2 B (b c - a d)^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \end{aligned}$$

Problem 33: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 125 leaves, 4 steps):

$$\frac{g (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{d i} + \frac{(b c - a d) g \operatorname{Log} \left[\frac{b c - a d}{b (c+dx)} \right] \left(A + B + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{d^2 i} + \frac{B (b c - a d) g \operatorname{PolyLog} \left[2, \frac{d (a+bx)}{b (c+dx)} \right]}{d^2 i}$$

Result (type 4, 291 leaves):

$$\begin{aligned} & \frac{1}{2 d^2 i} g \left(2 b B c - 2 a B d + 2 A b d x - 2 b B c \operatorname{Log}\left[\frac{c}{d} + x\right] + b B c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \right. \\ & \quad a B d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b B d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 2 A b c \operatorname{Log}[c+d x] + 2 a A d \operatorname{Log}[c+d x] - 2 b B c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] + \\ & \quad 2 a B d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - 2 b B c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 2 a B d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\ & \quad \left. 2 B \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d + (b c - a d) \operatorname{Log}[c+d x] + (-b c + a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (-2 b B c + 2 a B d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \end{aligned}$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 341 leaves, 9 steps):

$$\begin{aligned} & \frac{3 B (b c - a d)^2 g^3 (a + b x)}{d^3 i^2 (c + d x)} - \frac{(6 A + 5 B) (b c - a d)^2 g^3 (a + b x)}{2 d^3 i^2 (c + d x)} - \frac{3 B (b c - a d)^2 g^3 (a + b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3 i^2 (c + d x)} + \\ & \frac{g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d i^2 (c + d x)} - \frac{(b c - a d) g^3 (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^2 i^2 (c + d x)} - \\ & \frac{b (b c - a d)^2 g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(6 A + 5 B + 6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^4 i^2} - \frac{3 b B (b c - a d)^2 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b (c + d x)}\right]}{d^4 i^2} \end{aligned}$$

Result (type 4, 956 leaves):

$$\begin{aligned}
& \frac{1}{2 d^4 i^2} g^3 \left(-2 A b^2 d (2 b c - 3 a d) x + A b^3 d^2 x^2 + \frac{2 A (b c - a d)^3}{c + d x} + 6 A b (b c - a d)^2 \operatorname{Log}[c + d x] + \frac{1}{(b c - a d)(c + d x)} \right. \\
& 2 a^3 B d^3 \left(b c - a d + b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] + (-b c + a d) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - b c \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - b d x \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \\
& 3 a^2 b B d^2 \left(-\operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 \left(-\frac{c}{c + d x} + \frac{b c \operatorname{Log}[a + b x]}{-b c + a d} + \frac{b c \operatorname{Log}[c + d x]}{b c - a d} - \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \right. \right. \\
& \left. \left. \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \left(\frac{c}{c + d x} + \operatorname{Log}[c + d x] \right) + \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& b^3 B \left(-4 c^2 + \frac{4 a c d}{b} - c d x + \frac{a d^2 x}{b} - \frac{2 c^3}{c + d x} + 4 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \frac{a^2 d^2 \operatorname{Log}[a + b x]}{b^2} + \frac{2 b c^3 \operatorname{Log}[a + b x]}{-b c + a d} - \right. \\
& 4 c d x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + d^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \frac{2 c^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{c + d x} + c^2 \operatorname{Log}[c + d x] + \frac{2 b c^3 \operatorname{Log}[c + d x]}{b c - a d} + 6 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\
& \left. 6 c^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - \frac{2 c \operatorname{Log}\left[\frac{a}{b} + x\right] \left(2 a d + 3 b c \operatorname{Log}[c + d x] - 3 b c \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right)}{b} + 6 c^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& 6 a b^2 B d \left(d \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \frac{c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{c + d x} + \right. \\
& c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{b c - a d} \right) + \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left(d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x] \right) - \\
& \left. 2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 40: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 260 leaves, 8 steps):

$$\begin{aligned}
& - \frac{2B(bc-ad)g^2(a+bx)}{d^2i^2(c+dx)} + \frac{(2A+B)(bc-ad)g^2(a+bx)}{d^2i^2(c+dx)} + \frac{2B(bc-ad)g^2(a+bx)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]}{d^2i^2(c+dx)} + \\
& \frac{g^2(a+bx)^2\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{di^2(c+dx)} + \frac{b(bc-ad)g^2\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(2A+B+2B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{d^3i^2} + \frac{2bB(bc-ad)g^2\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3i^2}
\end{aligned}$$

Result (type 4, 588 leaves):

$$\begin{aligned}
& \frac{1}{d^3i^2}g^2\left(Ab^2dx - \frac{A(bc-ad)^2}{c+dx} + 2Ab(-bc+ad)\text{Log}[c+dx] + \frac{1}{(bc-ad)(c+dx)}\right. \\
& a^2Bd^2\left(bc-ad+b(c+dx)\text{Log}\left[\frac{a}{b}+x\right] + (-bc+ad)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right] - bc\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - bdx\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) + \\
& abBd\left(-\text{Log}\left[\frac{c}{d}+x\right]^2 + 2\text{Log}\left[\frac{c}{d}+x\right]\text{Log}[c+dx] + 2\left(-\frac{c}{c+dx} + \frac{bc\text{Log}[a+bx]}{-bc+ad} + \frac{bc\text{Log}[c+dx]}{bc-ad} - \text{Log}\left[\frac{a}{b}+x\right]\text{Log}[c+dx] + \right. \right. \\
& \left. \left. \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\left(\frac{c}{c+dx} + \text{Log}[c+dx]\right) + \text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) + 2\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) + \\
& b^2B\left(d\left(\frac{a}{b}+x\right)\left(-1 + \text{Log}\left[\frac{a}{b}+x\right]\right) - (c+dx)\left(-1 + \text{Log}\left[\frac{c}{d}+x\right]\right) + c\text{Log}\left[\frac{c}{d}+x\right]^2 + \frac{c^2\left(1 + \text{Log}\left[\frac{c}{d}+x\right]\right)}{c+dx} + \right. \\
& \left. c^2\left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{c+dx} + \frac{b\left(\text{Log}[a+bx] - \text{Log}[c+dx]\right)}{bc-ad}\right) + \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)\left(dx - \frac{c^2}{c+dx} - 2c\text{Log}[c+dx]\right) - \\
& \left. 2c\left(\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)\right)
\end{aligned}$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag+bgx)\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{(ci+di)^2} dx$$

Optimal (type 4, 160 leaves, 7 steps):

$$\begin{aligned}
& - \frac{Ag(a+bx)}{di^2(c+dx)} + \frac{Bg(a+bx)}{di^2(c+dx)} - \frac{Bg(a+bx)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]}{di^2(c+dx)} - \frac{bg\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{d^2i^2} - \frac{bBg\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^2i^2}
\end{aligned}$$

Result (type 4, 333 leaves):

$$\frac{1}{2 d^2 i^2} g \left(\frac{2 A (b c - a d)}{c + d x} + 2 A b \operatorname{Log}[c + d x] + \frac{1}{(b c - a d) (c + d x)} \right. \\ \left. 2 a B d \left(b c - a d + b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] + (-b c + a d) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - b c \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - b d x \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \right. \\ \left. b B \left(-\operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 \left(-\frac{c}{c + d x} + \frac{b c \operatorname{Log}[a + b x]}{-b c + a d} + \frac{b c \operatorname{Log}[c + d x]}{b c - a d} - \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \right. \right. \right. \\ \left. \left. \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \left(\frac{c}{c + d x} + \operatorname{Log}[c + d x] \right) + \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right)$$

Problem 47: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 361 leaves, 9 steps):

$$-\frac{3 B (b c - a d) g^3 (a + b x)^2}{4 d^2 i^3 (c + d x)^2} - \frac{3 b B (b c - a d) g^3 (a + b x)}{d^3 i^3 (c + d x)} + \frac{b (3 A + B) (b c - a d) g^3 (a + b x)}{d^3 i^3 (c + d x)} + \\ \frac{3 b B (b c - a d) g^3 (a + b x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{d^3 i^3 (c + d x)} + \frac{g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{d i^3 (c + d x)^2} + \frac{(b c - a d) g^3 (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{2 d^2 i^3 (c + d x)^2} + \\ \frac{b^2 (b c - a d) g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{d^4 i^3} + \frac{3 b^2 B (b c - a d) g^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i^3}$$

Result (type 4, 1161 leaves):

$$\begin{aligned}
& \frac{1}{4 d^4 i^3} \\
& g^3 \left(4 A b^3 d x + \frac{2 A (b c - a d)^3}{(c + d x)^2} - \frac{12 A b (b c - a d)^2}{c + d x} + 12 A b^2 (-b c + a d) \operatorname{Log}[c + d x] - \frac{1}{(b c - a d)^2 (c + d x)^2} \right. \\
& \quad \left. 3 a^2 b B d^2 \left(-b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - \right. \right. \\
& \quad \left. \left. 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - 2 b (b c - 2 a d) (c + d x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d)^2 (c + 2 d x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 2 b^2 c^3 \operatorname{Log}[c + d x] - \right. \right. \\
& \quad \left. \left. 4 a b c^2 d \operatorname{Log}[c + d x] + 4 b^2 c^2 d x \operatorname{Log}[c + d x] - 8 a b c d^2 x \operatorname{Log}[c + d x] + 2 b^2 c d^2 x^2 \operatorname{Log}[c + d x] - 4 a b d^3 x^2 \operatorname{Log}[c + d x] \right) - \right. \\
& \quad \left. \frac{1}{(b c - a d)^2 (c + d x)^2} a^3 B d^3 \left(-b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c + d x)^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \right. \right. \\
& \quad \left. \left. 2 (b c - a d)^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 2 b^2 c^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 4 b^2 c d x \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b^2 d^2 x^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \right. \\
& \quad \left. 3 a b^2 B d \left(-2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \frac{8 c (1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{c + d x} + \frac{c^2 (1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right])}{(c + d x)^2} + 8 c \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])}{-b c + a d} \right) \right) + \right. \\
& \quad \left. 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left(\frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \operatorname{Log}[c + d x] \right) + \right. \\
& \quad \left. \frac{2 c^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c + d x) (b c - a d + b (c + d x) \operatorname{Log}[a + b x] - b (c + d x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(c + d x)^2} + 4 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) - \\
& b^3 B \left(-4 d \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 4 (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 6 c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \frac{12 c^2 (1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{c + d x} + \right. \\
& \quad \left. \frac{c^3 (1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right])}{(c + d x)^2} - 12 c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])}{b c - a d} \right) \right) + \\
& \quad \left. 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left(-2 d x + \frac{c^2 (5 c + 6 d x)}{(c + d x)^2} + 6 c \operatorname{Log}[c + d x] \right) + \right. \\
& \quad \left. \frac{2 c^3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c + d x) (b c - a d + b (c + d x) \operatorname{Log}[a + b x] - b (c + d x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(c + d x)^2} + 12 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 48: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 251 leaves, 8 steps):

$$\frac{B g^2 (a + b x)^2}{4 d i^3 (c + d x)^2} - \frac{A b g^2 (a + b x)}{d^2 i^3 (c + d x)} + \frac{b B g^2 (a + b x)}{d^2 i^3 (c + d x)} - \frac{b B g^2 (a + b x) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right]}{d^2 i^3 (c + d x)} -$$

$$\frac{g^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 d i^3 (c + d x)^2} - \frac{b^2 g^2 \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{d^3 i^3} - \frac{b^2 B g^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i^3}$$

Result (type 4, 790 leaves):

$$\frac{1}{4 d^3 i^3} g^2 \left(-\frac{2 A (b c - a d)^2}{(c + d x)^2} + \frac{8 A b (b c - a d)}{c + d x} + 4 A b^2 \operatorname{Log}[c + d x] - \frac{1}{(b c - a d)^2 (c + d x)^2} 2 a b B d \left(-b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - \right. \right.$$

$$4 a^2 d^3 x - 2 b (b c - 2 a d) (c + d x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d)^2 (c + 2 d x) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + 2 b^2 c^3 \operatorname{Log}[c + d x] -$$

$$\left. 4 a b c^2 d \operatorname{Log}[c + d x] + 4 b^2 c^2 d x \operatorname{Log}[c + d x] - 8 a b c d^2 x \operatorname{Log}[c + d x] + 2 b^2 c d^2 x^2 \operatorname{Log}[c + d x] - 4 a b d^3 x^2 \operatorname{Log}[c + d x] \right) -$$

$$\frac{1}{(b c - a d)^2 (c + d x)^2} a^2 B d^2 \left(-b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c + d x)^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right.$$

$$\left. 2 (b c - a d)^2 \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + 2 b^2 c^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 4 b^2 c d x \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 b^2 d^2 x^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) +$$

$$b^2 B \left(-2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \frac{8 c \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{c + d x} + \frac{c^2 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{(c + d x)^2} + 8 c \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]}{c + d x} + \frac{b \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{-b c + a d} \right) \right) +$$

$$2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c + d x] \right) +$$

$$\left. \frac{2 c^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{(c + d x)^2} + 4 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right)$$

Problem 55: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 (c i + d i x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 539 leaves, 11 steps):

$$\begin{aligned} & \frac{3 B^2 (b c - a d)^4 g^3 i x}{10 b d^3} - \frac{3 B^2 (b c - a d)^3 g^3 i (c + d x)^2}{20 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i (c + d x)^3}{30 d^4} - \frac{B (b c - a d)^2 g^3 i (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{30 b^2 d} \\ & \frac{B (b c - a d) g^3 i (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{10 b^2} + \frac{(b c - a d) g^3 i (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{20 b^2} + \frac{g^3 i (a + b x)^4 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{5 b} \\ & \frac{B (b c - a d)^3 g^3 i (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^2 d^2} - \frac{B (b c - a d)^4 g^3 i (a + b x) \left(6 A + 5 B + 6 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^2 d^3} \\ & \frac{B (b c - a d)^5 g^3 i \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(6 A + 11 B + 6 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^2 d^4} - \frac{B^2 (b c - a d)^5 g^3 i \operatorname{Log} [c + d x]}{10 b^2 d^4} - \frac{B^2 (b c - a d)^5 g^3 i \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{10 b^2 d^4} \end{aligned}$$

Result (type 4, 3093 leaves):

$$\begin{aligned} & \frac{1}{60 b^2 d^4} g^3 i \left(-6 b^5 B^2 c^5 + 36 a b^4 B^2 c^4 d - 90 a^2 b^3 B^2 c^3 d^2 + 90 a^3 b^2 B^2 c^2 d^3 - 24 a^4 b B^2 c d^4 - 6 a^5 B^2 d^5 - 6 A b^5 B c^4 d x + b^5 B^2 c^4 d x + 30 a A b^4 B c^3 d^2 x - \right. \\ & 8 a b^4 B^2 c^3 d^2 x - 60 a^2 A b^3 B c^2 d^3 x + 24 a^2 b^3 B^2 c^2 d^3 x + 60 a^3 A^2 b^2 c d^4 x + 30 a^3 A b^2 B c d^4 x - 28 a^3 b^2 B^2 c d^4 x + 6 a^4 A b B d^5 x + 11 a^4 b B^2 d^5 x + \\ & 3 A b^5 B c^3 d^2 x^2 - 2 b^5 B^2 c^3 d^2 x^2 - 15 a A b^4 B c^2 d^3 x^2 + 12 a b^4 B^2 c^2 d^3 x^2 + 90 a^2 A^2 b^3 c d^4 x^2 - 15 a^2 A b^3 B c d^4 x^2 - 18 a^2 b^3 B^2 c d^4 x^2 + \\ & 30 a^3 A^2 b^2 d^5 x^2 + 27 a^3 A b^2 B d^5 x^2 + 8 a^3 b^2 B^2 d^5 x^2 - 2 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 60 a A^2 b^4 c d^4 x^3 - 20 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\ & 60 a^2 A^2 b^3 d^5 x^3 + 22 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 15 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + 45 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 - \\ & 6 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{a}{b} + x \right] + 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 30 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\ & 15 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 3 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right] - 30 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \\ & 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right] - 6 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] - 3 b^5 B^2 c^5 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 15 a b^4 B^2 c^4 d \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\ & 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 3 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} [a + b x] + 13 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} [a + b x] + 30 a^4 A b B c d^4 \operatorname{Log} [a + b x] + a^4 b B^2 c d^4 \operatorname{Log} [a + b x] - \\ & 6 a^5 A B d^5 \operatorname{Log} [a + b x] - 11 a^5 B^2 d^5 \operatorname{Log} [a + b x] - 30 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 6 a^5 B^2 d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \\ & 30 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 6 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 30 a^4 b B^2 c d^4 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \\ & 6 a^5 B^2 d^5 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - 6 b^5 B^2 c^4 d x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + 30 a b^4 B^2 c^3 d^2 x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + \\ & 120 a^3 A b^2 B c d^4 x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + 30 a^3 b^2 B^2 c d^4 x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + 6 a^4 b B^2 d^5 x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + 3 b^5 B^2 c^3 d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - \end{aligned}$$

$$\begin{aligned}
& 15 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 180 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 15 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 27 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 22 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 30 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 90 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 30 a^4 b B^2 c d^4 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 6 a^5 B^2 d^5 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 90 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 60 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 15 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 45 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 6 A b^5 B c^5 \operatorname{Log}[c+dx] - b^5 B^2 c^5 \operatorname{Log}[c+dx] - 30 a A b^4 B c^4 d \operatorname{Log}[c+dx] + 11 a b^4 B^2 c^4 d \operatorname{Log}[c+dx] + 60 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+dx] - \\
& 37 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+dx] - 60 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c+dx] + 27 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+dx] - 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + \\
& 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 6 b^2 B^2 c^2 (b^3 c^3 - 5 a b^2 c^2 d + 10 a^2 b c d^2 - 10 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 a^4 B^2 d^4 (-5 b c + a d) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 56: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^2 (ci + dix) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 450 leaves, 10 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^3 g^2 i x}{3 b d^2} + \frac{B^2 (bc - ad)^2 g^2 i (c + dx)^2}{12 d^3} - \frac{B (bc - ad)^2 g^2 i (a + bx)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{12 b^2 d} \\
& - \frac{B (bc - ad) g^2 i (a + bx)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{6 b^2} + \frac{(bc - ad) g^2 i (a + bx)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{12 b^2} + \\
& \frac{g^2 i (a + bx)^3 (c + dx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{4 b} + \frac{B (bc - ad)^3 g^2 i (a + bx) \left(2A + B + 2B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{12 b^2 d^2} + \\
& \frac{B (bc - ad)^4 g^2 i \operatorname{Log} \left[\frac{bc - ad}{b(c+dx)} \right] \left(2A + 3B + 2B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{12 b^2 d^3} + \frac{B^2 (bc - ad)^4 g^2 i \operatorname{Log} [c + dx]}{6 b^2 d^3} + \frac{B^2 (bc - ad)^4 g^2 i \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{6 b^2 d^3}
\end{aligned}$$

Result (type 4, 2270 leaves):

$$\begin{aligned}
& \frac{1}{12 b^2 d^3} g^2 i \left(2 b^4 B^2 c^4 - 10 a b^3 B^2 c^3 d + 12 a^2 b^2 B^2 c^2 d^2 - 2 a^3 b B^2 c d^3 - 2 a^4 B^2 d^4 + 2 A b^4 B c^3 d x - b^4 B^2 c^3 d x - 8 a A b^3 B c^2 d^2 x + \right. \\
& 5 a b^3 B^2 c^2 d^2 x + 12 a^2 A^2 b^2 c d^3 x + 4 a^2 A b^2 B c d^3 x - 7 a^2 b^2 B^2 c d^3 x + 2 a^3 A b B d^4 x + 3 a^3 b B^2 d^4 x - A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + \\
& 12 a A^2 b^3 c d^3 x^2 - 4 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + 6 a^2 A^2 b^2 d^4 x^2 + 5 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 4 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 x^3 + \\
& 8 a A^2 b^3 d^4 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 + 2 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 8 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 4 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 4 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 4 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 4 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] + 8 a^3 A b B c d^3 \operatorname{Log}[a + b x] + 2 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] - 2 a^4 A B d^4 \operatorname{Log}[a + b x] - 3 a^4 B^2 d^4 \operatorname{Log}[a + b x] - \\
& 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 2 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 8 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a^2 A b^2 B c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 2 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 5 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 8 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 16 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 8 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 2 a^4 B^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 6 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 4 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 8 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 - \\
& 2 A b^4 B c^4 \operatorname{Log}[c + d x] + b^4 B^2 c^4 \operatorname{Log}[c + d x] + 8 a A b^3 B c^3 d \operatorname{Log}[c + d x] - 6 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] - 12 a^2 A b^2 B c^2 d^2 \operatorname{Log}[c + d x] + \\
& 5 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] + 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - \\
& 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& \left. 2 b^2 B^2 c^2 (b^2 c^2 - 4 a b c d + 6 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 a^3 B^2 d^3 (-4 b c + a d) \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right)
\end{aligned}$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) (c i + d i x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2 dx$$

Optimal (type 4, 343 leaves, 9 steps):

$$\begin{aligned} & \frac{B^2 (bc - ad)^2 g i x}{3 b d} - \frac{B (bc - ad)^2 g i (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b^2 d} - \frac{B (bc - ad) g i (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b^2} + \\ & \frac{(bc - ad) g i (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{6 b^2} + \frac{g i (a + b x)^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{3 b} - \\ & \frac{B (bc - ad)^3 g i \operatorname{Log} \left[\frac{bc - ad}{b(c+dx)} \right] \left(A + B + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b^2 d^2} - \frac{B^2 (bc - ad)^3 g i \operatorname{Log} [c + d x]}{3 b^2 d^2} - \frac{B^2 (bc - ad)^3 g i \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{3 b^2 d^2} \end{aligned}$$

Result (type 4, 1443 leaves):

$$\frac{1}{6 b^2 d^2}$$

$$\begin{aligned} & \text{g i} \left(-2 b^3 B^2 c^3 + 2 a b^2 B^2 c^2 d + 2 a^2 b B^2 c d^2 - 2 a^3 B^2 d^3 - 2 A b^3 B c^2 d x + 2 b^3 B^2 c^2 d x + 6 a A^2 b^2 c d^2 x - 4 a b^2 B^2 c d^2 x + 2 a^2 A b B d^3 x + 2 a^2 b B^2 d^3 x + \right. \\ & 3 A^2 b^3 c d^2 x^2 - 2 A b^3 B c d^2 x^2 + 3 a A^2 b^2 d^3 x^2 + 2 a A b^2 B d^3 x^2 + 2 A^2 b^3 d^3 x^3 - 2 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right] + 2 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] + \\ & 3 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right] - 2 a^2 b B^2 c d^2 \text{Log}\left[\frac{c}{d} + x\right] - b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\ & 3 a b^2 B^2 c^2 d \text{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^2 A b B c d^2 \text{Log}[a + b x] + 2 a^2 b B^2 c d^2 \text{Log}[a + b x] - 2 a^3 A B d^3 \text{Log}[a + b x] - 2 a^3 B^2 d^3 \text{Log}[a + b x] - \\ & 6 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 2 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 6 a^2 b B^2 c d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 2 a^3 B^2 d^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\ & 6 a^2 b B^2 c d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 a^3 B^2 d^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 2 b^3 B^2 c^2 d x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 12 a A b^2 B c d^2 x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a^2 b B^2 d^3 x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 A b^3 B c d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 b^3 B^2 c d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 a A b^2 B d^3 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^2 B^2 d^3 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 A b^3 B d^3 x^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 a^2 b B^2 c d^2 \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\ & 2 a^3 B^2 d^3 \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 a b^2 B^2 c d^2 x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^3 B^2 c d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 a b^2 B^2 d^3 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\ & 2 b^3 B^2 d^3 x^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 A b^3 B c^3 \text{Log}[c + d x] - 2 b^3 B^2 c^3 \text{Log}[c + d x] - 6 a A b^2 B c^2 d \text{Log}[c + d x] + 2 a b^2 B^2 c^2 d \text{Log}[c + d x] - \\ & 2 b^3 B^2 c^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + 6 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + 2 b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] - 6 a b^2 B^2 c^2 d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] + \\ & 2 b^3 B^2 c^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \text{Log}[c + d x] - 6 a b^2 B^2 c^2 d \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \text{Log}[c + d x] + 2 b^3 B^2 c^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\ & \left. 6 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 b^2 B^2 c^2 (b c - 3 a d) \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 a^2 B^2 d^2 (-3 b c + a d) \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \end{aligned}$$

Problem 58: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x) \left(A + B \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 dx$$

Optimal (type 4, 203 leaves, 7 steps):

$$\begin{aligned}
& - \frac{B (b c - a d) i (a + b x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)}{b^2} + \frac{i (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2}{2 d} \\
& + \frac{B^2 (b c - a d)^2 i \operatorname{Log}[c + d x]}{b^2 d} + \frac{B (b c - a d)^2 i \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 i \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^2 d}
\end{aligned}$$

Result (type 4, 734 leaves):

$$\begin{aligned}
& i \left(A^2 c x + \frac{1}{2} A^2 d x^2 - \frac{2 A B c \left(-a d \operatorname{Log}[a + b x] - b d x \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] + b c \operatorname{Log}[c + d x] \right)}{b d} \right) + \\
& A B \left(-c x + \frac{a d x}{b} - \frac{a^2 d \operatorname{Log}[a + b x]}{b^2} + d x^2 \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] + \frac{c^2 \operatorname{Log}[c + d x]}{d} \right) + \\
& \frac{1}{b d} B^2 c \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] \right) + \\
& 2 a d \operatorname{Log}[a + b x] \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] + b d x \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right]^2 + 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] - \\
& 2 b c \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c - a d} \right] - 2 b c \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) + \\
& \frac{1}{2} B^2 d \left(x^2 \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right]^2 - \frac{1}{b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) \right) + \right. \\
& b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right) \left(a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x]) \right) - \\
& \left. 2 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right)
\end{aligned}$$

Problem 59: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+b x)}}{c+d x} \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 286 leaves, 8 steps):

$$\begin{aligned}
& \frac{2 B (b c - a d) i \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)}{b^2 g} + \frac{d i (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2}{b^2 g} - \frac{(b c - a d) i \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2 \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g} + \\
& \frac{2 B^2 (b c - a d) i \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^2 g} + \frac{2 B (b c - a d) i \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g} + \frac{2 B^2 (b c - a d) i \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g}
\end{aligned}$$

Result (type 4, 1196 leaves):

$$\begin{aligned}
& \frac{1}{3 b^2 g} i \left(3 A^2 b d x + 3 A^2 (b c - a d) \operatorname{Log}[a + b x] - \right. \\
& 3 A B \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] (1 + \operatorname{Log}[a + b x]) + 2 \left(-b c + a d + \operatorname{Log}\left[\frac{c}{d} + x\right] \left(b c + a d \operatorname{Log}[a + b x] - a d \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) \right. \right. \\
& \quad \left. \left. (-b d x + a d \operatorname{Log}[a + b x]) \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) + 3 A b B c \\
& \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \operatorname{Log}[a + b x] \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) - \\
& B^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 3 d (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - 3 b (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \right. \\
& 3 d (b x - a \operatorname{Log}[a + b x]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 + 6 \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right. \\
& \quad \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) - \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \left(-2 b c + 2 a d - 2 d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
& \quad \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \left(b (c + d x) - a d \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) - \\
& 3 a d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& 3 a d \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \left. \right) + \\
& b B^2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 3 \operatorname{Log}[a + b x] \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 + \right. \\
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(-\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) - \\
& \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \left. \right)
\end{aligned}$$

Problem 60: Result more than twice size of optimal antiderivative.

$$\int \frac{(c + dx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{(ag + bgx)^2} dx$$

Optimal (type 4, 241 leaves, 7 steps):

$$\begin{aligned} & -\frac{2B^2i(c+dx)}{bg^2(a+bx)} - \frac{2Bi(c+dx)\left(A+B\operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)}{bg^2(a+bx)} - \frac{i(c+dx)\left(A+B\operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2}{bg^2(a+bx)} \\ & \frac{di\left(A+B\operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)^2\operatorname{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b^2g^2} + \frac{2Bdi\left(A+B\operatorname{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]\right)\operatorname{PolyLog}\left[2,\frac{b(c+dx)}{d(a+bx)}\right]}{b^2g^2} + \frac{2B^2di\operatorname{PolyLog}\left[3,\frac{b(c+dx)}{d(a+bx)}\right]}{b^2g^2} \end{aligned}$$

Result (type 4, 1155 leaves):

$$\begin{aligned}
& \frac{1}{3 b^2 g^2} i \left(\frac{3 A^2 (-b c + a d)}{a + b x} + 3 A^2 d \operatorname{Log}[a + b x] - \right. \\
& \frac{6 A b B c \left(-d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right) \right)}{(b c - a d) (a + b x)} - \frac{1}{(b c - a d) (a + b x)} \\
& \left. 3 b B^2 c \left(2 b c - 2 a d + 2 d (a + b x) \operatorname{Log}[a + b x] + 2 (b c - a d) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + b (c + d x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 - 2 d (a + b x) \operatorname{Log}[c + d x] \right) + \right. \\
& 3 A B d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right) \right) + \\
& \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \Bigg) + \\
& B^2 d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^3 + \frac{3 a \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{a + b x} + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \\
& \frac{3 \left(a + (a + b x) \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2}{a + b x} - \\
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \frac{1}{(b c - a d) (a + b x)} \\
& 3 a \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \\
& \left. \left((b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \\
& \frac{1}{(b c - a d) (a + b x)} 3 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \left(b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \\
& 3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \\
& \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} + \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right)}{(b c - a d) (a + b x)} - \right. \\
& \left. 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) - 6 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \Bigg) \Bigg)
\end{aligned}$$

Problem 64: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 (c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 711 leaves, 17 steps):

$$\begin{aligned} & \frac{3 B^2 (b c - a d)^5 g^3 i^2 x}{20 b^2 d^3} + \frac{B^2 (b c - a d)^2 g^3 i^2 (a + b x)^4}{60 b^3} - \frac{3 B^2 (b c - a d)^4 g^3 i^2 (c + d x)^2}{40 b d^4} + \frac{B^2 (b c - a d)^3 g^3 i^2 (c + d x)^3}{60 d^4} \\ & - \frac{B (b c - a d)^3 g^3 i^2 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{90 b^3 d} - \frac{B (b c - a d)^2 g^3 i^2 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{20 b^3} \\ & + \frac{B (b c - a d) g^3 i^2 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{15 b^2} + \frac{(b c - a d)^2 g^3 i^2 (a + b x)^4 \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)^2}{60 b^3} + \\ & + \frac{(b c - a d) g^3 i^2 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)^2}{15 b^2} + \frac{g^3 i^2 (a + b x)^4 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)^2}{6 b} \\ & - \frac{B (b c - a d)^4 g^3 i^2 (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{180 b^3 d^2} - \frac{B (b c - a d)^5 g^3 i^2 (a + b x) \left(6 A + 5 B + 6 B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{180 b^3 d^3} \\ & - \frac{B (b c - a d)^6 g^3 i^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(6 A + 11 B + 6 B \operatorname{Log} \left[\frac{e(a + b x)}{c + d x} \right] \right)}{180 b^3 d^4} - \frac{B^2 (b c - a d)^6 g^3 i^2 \operatorname{Log} [c + d x]}{20 b^3 d^4} - \frac{B^2 (b c - a d)^6 g^3 i^2 \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{b (c + d x)} \right]}{30 b^3 d^4} \end{aligned}$$

Result (type 4, 4173 leaves):

$$\begin{aligned} & \frac{1}{360 b^3 d^4} \\ & g^3 i^2 \left(-12 b^6 B^2 c^6 + 84 a b^5 B^2 c^5 d - 252 a^2 b^4 B^2 c^4 d^2 + 240 a^3 b^3 B^2 c^3 d^3 + 12 a^4 b^2 B^2 c^2 d^4 - 84 a^5 b B^2 c d^5 + 12 a^6 B^2 d^6 - 12 A b^6 B c^5 d x + 8 b^6 B^2 c^5 d x + \right. \\ & 72 a A b^5 B c^4 d^2 x - 54 a b^5 B^2 c^4 d^2 x - 180 a^2 A b^4 B c^3 d^3 x + 154 a^2 b^4 B^2 c^3 d^3 x + 360 a^3 A^2 b^3 c^2 d^4 x + 60 a^3 A b^3 B c^2 d^4 x - 194 a^3 b^3 B^2 c^2 d^4 x + \\ & 72 a^4 A b^2 B c d^5 x + 102 a^4 b^2 B^2 c d^5 x - 12 a^5 A b B d^6 x - 16 a^5 b B^2 d^6 x + 6 A b^6 B c^4 d^2 x^2 - 7 b^6 B^2 c^4 d^2 x^2 - 36 a A b^5 B c^3 d^3 x^2 + 46 a b^5 B^2 c^3 d^3 x^2 + \\ & 540 a^2 A^2 b^4 c^2 d^4 x^2 - 180 a^2 A b^4 B c^2 d^4 x^2 - 60 a^2 b^4 B^2 c^2 d^4 x^2 + 360 a^3 A^2 b^3 c d^5 x^2 + 204 a^3 A b^3 B c d^5 x^2 + 10 a^3 b^3 B^2 c d^5 x^2 + \\ & 6 a^4 A b^2 B d^6 x^2 + 11 a^4 b^2 B^2 d^6 x^2 - 4 A b^6 B c^3 d^3 x^3 + 6 b^6 B^2 c^3 d^3 x^3 + 360 a A^2 b^5 c^2 d^4 x^3 - 156 a A b^5 B c^2 d^4 x^3 + 6 a b^5 B^2 c^2 d^4 x^3 + \\ & 720 a^2 A^2 b^4 c d^5 x^3 + 84 a^2 A b^4 B c d^5 x^3 - 30 a^2 b^4 B^2 c d^5 x^3 + 120 a^3 A^2 b^3 d^6 x^3 + 76 a^3 A b^3 B d^6 x^3 + 18 a^3 b^3 B^2 d^6 x^3 + 90 A^2 b^6 c^2 d^4 x^4 - \\ & 42 A b^6 B c^2 d^4 x^4 + 6 b^6 B^2 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 - 36 a A b^5 B c d^5 x^4 - 12 a b^5 B^2 c d^5 x^4 + 270 a^2 A^2 b^4 d^6 x^4 + 78 a^2 A b^4 B d^6 x^4 + \\ & 6 a^2 b^4 B^2 d^6 x^4 + 144 A^2 b^6 c d^5 x^5 - 24 A b^6 B c d^5 x^5 + 216 a A^2 b^5 d^6 x^5 + 24 a A b^5 B d^6 x^5 + 60 A^2 b^6 d^6 x^6 - 12 a b^5 B^2 c^5 d \operatorname{Log} \left[\frac{a}{b} + x \right] + \\ & 72 a^2 b^4 B^2 c^4 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 180 a^3 b^3 B^2 c^3 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 60 a^4 b^2 B^2 c^2 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] + 72 a^5 b B^2 c d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] - 12 a^6 B^2 d^6 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\ & 90 a^4 b^2 B^2 c^2 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 36 a^5 b B^2 c d^5 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 a^6 B^2 d^6 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 12 b^6 B^2 c^6 \operatorname{Log} \left[\frac{c}{d} + x \right] - 72 a b^5 B^2 c^5 d \operatorname{Log} \left[\frac{c}{d} + x \right] + \end{aligned}$$

$$\begin{aligned}
& 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 60 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 72 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + 12 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 36 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 90 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 120 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 6 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[a + b x] + \\
& 32 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[a + b x] + 180 a^4 A b^2 B c^2 d^4 \operatorname{Log}[a + b x] + 66 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a + b x] - 72 a^5 A b B c d^5 \operatorname{Log}[a + b x] - \\
& 108 a^5 b B^2 c d^5 \operatorname{Log}[a + b x] + 12 a^6 A B d^6 \operatorname{Log}[a + b x] + 16 a^6 B^2 d^6 \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 12 b^6 B^2 c^5 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 72 a b^5 B^2 c^4 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 180 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a^3 A b^3 B c^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 60 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 72 a^4 b^2 B^2 c d^5 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 a^5 b B^2 d^6 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 b^6 B^2 c^4 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 36 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 180 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a^3 A b^3 B c d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 204 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 a^4 b^2 B^2 d^6 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 156 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 1440 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 84 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 240 a^3 A b^3 B d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 76 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 180 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 42 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 36 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 540 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 78 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 288 A b^6 B c d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 24 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 432 a A b^5 B d^6 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 120 A b^6 B d^6 x^6 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 72 a^5 b B^2 c d^5 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 a^6 B^2 d^6 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 360 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 360 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 360 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 720 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 120 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 90 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 270 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 +
\end{aligned}$$

$$\begin{aligned}
& 144 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 216 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 12 A b^6 B c^6 \operatorname{Log}[c+dx] - \\
& 8 b^6 B^2 c^6 \operatorname{Log}[c+dx] - 72 a A b^5 B c^5 d \operatorname{Log}[c+dx] + 60 a b^5 B^2 c^5 d \operatorname{Log}[c+dx] + 180 a^2 A b^4 B c^4 d^2 \operatorname{Log}[c+dx] - 186 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[c+dx] - \\
& 240 a^3 A b^3 B c^3 d^3 \operatorname{Log}[c+dx] + 128 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[c+dx] + 6 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[c+dx] - 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + \\
& 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 12 b^3 B^2 c^3 (b^3 c^3 - 6 a b^2 c^2 d + 15 a^2 b c d^2 - 20 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 12 a^4 B^2 d^4 (15 b^2 c^2 - 6 a b c d + a^2 d^2) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 65: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^2 (ci + dix)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 761 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^4 g^2 i^2 x}{10 b^2 d^2} - \frac{B^2 (bc - ad)^3 g^2 i^2 (c + dx)^2}{20 b d^3} + \frac{B^2 (bc - ad)^2 g^2 i^2 (c + dx)^3}{30 d^3} + \\
& \frac{B^2 (bc - ad)^5 g^2 i^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{30 b^3 d^3} - \frac{B (bc - ad)^3 g^2 i^2 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{30 b^3 d} - \\
& \frac{B (bc - ad)^2 g^2 i^2 (a + bx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{15 b^3} - \frac{B (bc - ad)^3 g^2 i^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{5 b d^3} + \\
& \frac{4 B (bc - ad)^2 g^2 i^2 (c + dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{15 d^3} - \frac{b B (bc - ad) g^2 i^2 (c + dx)^4 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{10 d^3} + \\
& \frac{(bc - ad)^2 g^2 i^2 (a + bx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{30 b^3} + \frac{(bc - ad) g^2 i^2 (a + bx)^3 (c + dx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{10 b^2} + \\
& \frac{g^2 i^2 (a + bx)^3 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{5 b} + \frac{B (bc - ad)^4 g^2 i^2 (a + bx) \left(2A + B + 2B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{30 b^3 d^2} + \\
& \frac{B (bc - ad)^5 g^2 i^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(2A + 3B + 2B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{30 b^3 d^3} + \frac{B^2 (bc - ad)^5 g^2 i^2 \operatorname{Log}[c + dx]}{10 b^3 d^3} + \frac{B^2 (bc - ad)^5 g^2 i^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{15 b^3 d^3}
\end{aligned}$$

Result (type 4, 3042 leaves):

$$\begin{aligned}
& \frac{1}{60 b^3 d^3} g^2 i^2 \left(4 b^5 B^2 c^5 - 24 a b^4 B^2 c^4 d + 20 a^2 b^3 B^2 c^3 d^2 + 20 a^3 b^2 B^2 c^2 d^3 - 24 a^4 b B^2 c d^4 + 4 a^5 B^2 d^5 + 4 A b^5 B c^4 d x - 4 b^5 B^2 c^4 d x - 20 a A b^4 B c^3 d^2 x + \right. \\
& 22 a b^4 B^2 c^3 d^2 x + 60 a^2 A^2 b^3 c^2 d^3 x - 36 a^2 b^3 B^2 c^2 d^3 x + 20 a^3 A b^2 B c d^4 x + 22 a^3 b^2 B^2 c d^4 x - 4 a^4 A b B d^5 x - 4 a^4 b B^2 d^5 x - \\
& 2 A b^5 B c^3 d^2 x^2 + 3 b^5 B^2 c^3 d^2 x^2 + 60 a A^2 b^4 c^2 d^3 x^2 - 30 a A b^4 B c^2 d^3 x^2 - 3 a b^4 B^2 c^2 d^3 x^2 + 60 a^2 A^2 b^3 c d^4 x^2 + 30 a^2 A b^3 B c d^4 x^2 - \\
& 3 a^2 b^3 B^2 c d^4 x^2 + 2 a^3 A b^2 B d^5 x^2 + 3 a^3 b^2 B^2 d^5 x^2 + 20 A^2 b^5 c^2 d^3 x^3 - 12 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 80 a A^2 b^4 c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\
& 20 a^2 A^2 b^3 d^5 x^3 + 12 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 30 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + 30 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 + \\
& 4 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 20 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] - 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
& 10 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 20 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 4 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 10 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 20 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + bx] + \\
& 40 a^3 A b^2 B c^2 d^3 \operatorname{Log}[a + bx] + 18 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + bx] - 20 a^4 A b B c d^4 \operatorname{Log}[a + bx] - 24 a^4 b B^2 c d^4 \operatorname{Log}[a + bx] + 4 a^5 A B d^5 \operatorname{Log}[a + bx] + \\
& 4 a^5 B^2 d^5 \operatorname{Log}[a + bx] - 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] - 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + \\
& 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] + 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - \\
& 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \\
& 4 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 20 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a^2 A b^3 B c^2 d^3 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 20 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] -
\end{aligned}$$

$$\begin{aligned}
& 4 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 2 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 30 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 120 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 30 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 40 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 12 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 160 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 40 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 12 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 60 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 20 a^4 b B^2 c d^4 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 4 a^5 B^2 d^5 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 60 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 20 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 80 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 20 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 30 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 30 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 4 A b^5 B c^5 \operatorname{Log}[c+dx] + \\
& 4 b^5 B^2 c^5 \operatorname{Log}[c+dx] + 20 a A b^4 B c^4 d \operatorname{Log}[c+dx] - 24 a b^4 B^2 c^4 d \operatorname{Log}[c+dx] - 40 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+dx] + 18 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+dx] + \\
& 2 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+dx] + 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 4 b^3 B^2 c^3 (b^2 c^2 - 5 a b c d + 10 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 4 a^3 B^2 d^3 (10 b^2 c^2 - 5 a b c d + a^2 d^2) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 66: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)(ci + dix)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 589 leaves, 14 steps):

$$\begin{aligned}
& \frac{B^2 (bc - ad)^3 g i^2 x}{12 b^2 d} + \frac{B^2 (bc - ad)^2 g i^2 (c + dx)^2}{12 b d^2} - \frac{B^2 (bc - ad)^4 g i^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{12 b^3 d^2} - \frac{B (bc - ad)^3 g i^2 (a + bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 b^3 d} \\
& \frac{B (bc - ad)^2 g i^2 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 b^3} + \frac{B (bc - ad)^2 g i^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{4 b d^2} - \\
& \frac{B (bc - ad) g i^2 (c + dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 d^2} + \frac{(bc - ad)^2 g i^2 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{12 b^3} + \\
& \frac{(bc - ad) g i^2 (a + bx)^2 (c + dx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{6 b^2} + \frac{g i^2 (a + bx)^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{4 b} - \\
& \frac{B (bc - ad)^4 g i^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{6 b^3 d^2} - \frac{B^2 (bc - ad)^4 g i^2 \operatorname{Log}[c + dx]}{4 b^3 d^2} - \frac{B^2 (bc - ad)^4 g i^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{6 b^3 d^2}
\end{aligned}$$

Result (type 4, 2268 leaves):

$$\begin{aligned}
& \frac{1}{12 b^3 d^2} g i^2 \left(-2 b^4 B^2 c^4 - 2 a b^3 B^2 c^3 d + 12 a^2 b^2 B^2 c^2 d^2 - 10 a^3 b B^2 c d^3 + 2 a^4 B^2 d^4 - 2 A b^4 B c^3 d x + 3 b^4 B^2 c^3 d x + 12 a A^2 b^3 c^2 d^2 x - \right. \\
& 4 a A b^3 B c^2 d^2 x - 7 a b^3 B^2 c^2 d^2 x + 8 a^2 A b^2 B c d^3 x + 5 a^2 b^2 B^2 c d^3 x - 2 a^3 A b B d^4 x - a^3 b B^2 d^4 x + 6 A^2 b^4 c^2 d^2 x^2 - 5 A b^4 B c^2 d^2 x^2 + \\
& b^4 B^2 c^2 d^2 x^2 + 12 a A^2 b^3 c d^3 x^2 + 4 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 8 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 x^3 + \\
& 4 a A^2 b^3 d^4 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - 2 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 4 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 4 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 8 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 4 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 12 a^2 A b^2 B c^2 d^2 \operatorname{Log}[a + b x] + 5 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] - 8 a^3 A b B c d^3 \operatorname{Log}[a + b x] - 6 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] + \\
& 2 a^4 A B d^4 \operatorname{Log}[a + b x] + a^4 B^2 d^4 \operatorname{Log}[a + b x] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 2 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a A b^3 B c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 8 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 5 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 16 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 8 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 8 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a^4 B^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 6 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 8 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 4 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 A b^4 B c^4 \operatorname{Log}[c + d x] - 3 b^4 B^2 c^4 \operatorname{Log}[c + d x] - 8 a A b^3 B c^3 d \operatorname{Log}[c + d x] + \\
& 2 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] + a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] - 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - \\
& 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& \left. 2 b^3 B^2 c^3 (b c - 4 a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 2 a^2 B^2 d^2 (6 b^2 c^2 - 4 a b c d + a^2 d^2) \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)
\end{aligned}$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 334 leaves, 11 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^2 i^2 x}{3 b^2} + \frac{B^2 (b c - a d)^3 i^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{3 b^3 d} - \frac{2 B (b c - a d)^2 i^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b^3} - \\ & \frac{B (b c - a d) i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{3 b d} + \frac{i^2 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{3 d} + \frac{B^2 (b c - a d)^3 i^2 \operatorname{Log} [c + d x]}{b^3 d} + \\ & \frac{2 B (b c - a d)^3 i^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{3 b^3 d} - \frac{2 B^2 (b c - a d)^3 i^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{3 b^3 d} \end{aligned}$$

Result (type 4, 1278 leaves):

$$\begin{aligned}
& \frac{1}{6 b^3 d} i^2 \left(6 A^2 b^3 c^2 d x + 6 A^2 b^3 c d^2 x^2 + 2 A^2 b^3 d^3 x^3 + 2 A b B d (b c - a d) x (2 b c + 2 a d - b d x) + 12 b B^2 c d (-b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - \right. \\
& 4 B^2 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 6 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 12 b^2 B^2 c (b c - a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 4 b B^2 (b c - a d) (b c + a d) (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 4 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 12 a^2 A b B c d^2 \operatorname{Log}[a + b x] + 4 a^3 A B d^3 \operatorname{Log}[a + b x] + B^2 d^2 (-b c + a d) \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + \\
& 4 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 6 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 + 2 b^3 B^2 d^3 x^3 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 - 4 A b^3 B c^3 \operatorname{Log}[c + d x] + \\
& 12 A b^2 B c^2 \left(a d \operatorname{Log}[a + b x] + b d x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] - b c \operatorname{Log}[c + d x] \right) - b^2 B^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) + \\
& 12 A b^2 B c \left(d (-b c + a d) x + b d^2 x^2 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + b c^2 \operatorname{Log}[c + d x] \right) + \\
& 2 B^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \operatorname{Log}[a + b x] + 2 b^3 c^3 \operatorname{Log}[c + d x]) + \\
& 12 b B^2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) (a^2 d^2 \operatorname{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log}[c + d x])) + \\
& 8 b^3 B^2 c^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& 12 a^2 b B^2 c d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) - 4 a^3 B^2 d^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \\
& 6 b^2 B^2 c^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \\
& 2 a d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + b d x \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 + 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& \left. 2 b c \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - 2 b c \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \left. \right)
\end{aligned}$$

Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 535 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B d (b c - a d) i^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{b^3 g} + \frac{2 B (b c - a d)^2 i^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{b^3 g} + \\
& \frac{d (b c - a d) i^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{b^3 g} + \frac{i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{2 b g} + \frac{B^2 (b c - a d)^2 i^2 \operatorname{Log} [c + d x]}{b^3 g} + \\
& \frac{B (b c - a d)^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} - \frac{(b c - a d)^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \\
& \frac{2 B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^3 g} - \frac{B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \\
& \frac{2 B (b c - a d)^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \frac{2 B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g}
\end{aligned}$$

Result (type 4, 2547 leaves):

$$\begin{aligned}
& \frac{1}{12 b^3 g} i^2 \left(12 A^2 b d (2 b c - a d) x + 6 A^2 b^2 d^2 x^2 + 12 A^2 (b c - a d)^2 \operatorname{Log} [a + b x] - \right. \\
& 24 A b B c \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] (1 + \operatorname{Log} [a + b x]) + 2 \left(-b c + a d + \operatorname{Log} \left[\frac{c}{d} + x \right] \left(b c + a d \operatorname{Log} [a + b x] - a d \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) \right) + \right. \\
& \left. (-b d x + a d \operatorname{Log} [a + b x]) \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + 12 A b^2 B c^2 \\
& \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 \operatorname{Log} [a + b x] \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + \\
& 6 A B \left(-4 a d^2 (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 a b d (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + \right. \\
& \left. d^2 \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \operatorname{Log} [a + b x] \right) - \right. \\
& \left. 2 d^2 (b x (-2 a + b x) + 2 a^2 \operatorname{Log} [a + b x]) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \right) + \\
& b^2 \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \operatorname{Log} [c + d x] \right) - 4 a^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) - \\
& 8 b B^2 c \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^3 - 3 d (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) - 3 b (c + d x) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) - \right. \\
& \left. 3 d (b x - a \operatorname{Log} [a + b x]) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 + 6 \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log} [c + d x] + \right.
\end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \Big) - \\
& 3 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \left(-2bc + 2ad - 2d(a+bx) \text{Log}\left[\frac{a}{b} + x\right] + ad \text{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
& \quad \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \left(b(c+dx) - ad \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2ad \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) - \\
& 3ad \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 3ad \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Big) + \\
& B^2 \left(4a^2d^2 \text{Log}\left[\frac{a}{b} + x\right]^3 - 12ad^2(a+bx) \left(2 - 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
& \quad 3d^2(a+bx) \left(7a - bx + (-6a + 2bx) \text{Log}\left[\frac{a}{b} + x\right] + 2(a-bx) \text{Log}\left[\frac{a}{b} + x\right]^2 \right) - 12abd(c+dx) \left(2 - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
& \quad 3b^2(c+dx) \left(7c - dx + (-6c + 2dx) \text{Log}\left[\frac{c}{d} + x\right] + 2(c-dx) \text{Log}\left[\frac{c}{d} + x\right]^2 \right) + 6d^2(bx(-2a+bx) + 2a^2 \text{Log}[a+bx]) \\
& \quad \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 - 6 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \left(-4ad^2(a+bx) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right] \right) + \right. \\
& \quad \left. 2a^2d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 4abd(c+dx) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + d^2 \left(bx(2a-bx) + 2b^2x^2 \text{Log}\left[\frac{a}{b} + x\right] - 2a^2 \text{Log}[a+bx] \right) + \right. \\
& \quad \left. b^2 \left(dx(-2c+dx) - 2d^2x^2 \text{Log}\left[\frac{c}{d} + x\right] + 2c^2 \text{Log}[c+dx] \right) - 4a^2d^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \Big) + \\
& 6 \left(2abcd + 3b^2cdx + 3abd^2x - b^2d^2x^2 - 2abd^2x \text{Log}\left[\frac{c}{d} + x\right] + b^2d^2x^2 \text{Log}\left[\frac{c}{d} + x\right] - a^2d^2 \text{Log}[a+bx] - b^2c^2 \text{Log}[c+dx] - \right. \\
& \quad 2abcd \text{Log}[c+dx] - \text{Log}\left[\frac{a}{b} + x\right] \left(bd(2ac+bx(2c-dx)) - 2d^2(a^2-b^2x^2) \text{Log}\left[\frac{c}{d} + x\right] + (-2b^2c^2 + 2a^2d^2) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \\
& \quad 2(b^2c^2 - a^2d^2) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 4ad \left(ad + 2bdx - bdx \text{Log}\left[\frac{c}{d} + x\right] - bc \text{Log}[c+dx] + \right. \\
& \quad \left. \text{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \\
& \quad 2a^2d^2 \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) \Big) + \\
& 12a^2d^2 \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Big) +
\end{aligned}$$

$$\begin{aligned}
& 4 b^2 B^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right]^3 + 3 \text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 3 \text{Log} [a+bx] \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2 + \right. \\
& 3 \text{Log} \left[\frac{a}{b} + x \right]^2 \left(-\text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + 6 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + 6 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - \\
& 3 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) \left(\text{Log} \left[\frac{a}{b} + x \right]^2 - 2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) - \\
& \left. 6 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] - 6 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right)
\end{aligned}$$

Problem 69: Result more than twice size of optimal antiderivative.

$$\int \frac{(cix + dix)^2 \left(A + B \text{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{(ag + bgx)^2} dx$$

Optimal (type 4, 442 leaves, 11 steps):

$$\begin{aligned}
& -\frac{2B^2(bc-ad)i^2(c+dx)}{b^2g^2(a+bx)} - \frac{2B(bc-ad)i^2(c+dx)\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^2g^2(a+bx)} + \frac{2Bd(bc-ad)i^2\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^3g^2} + \\
& \frac{d^2i^2(a+bx)\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^3g^2} - \frac{(bc-ad)i^2(c+dx)\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^2g^2(a+bx)} - \frac{2d(bc-ad)i^2\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2\text{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \\
& \frac{2B^2d(bc-ad)i^2\text{PolyLog}\left[2,\frac{d(a+bx)}{b(c+dx)}\right]}{b^3g^2} + \frac{4Bd(bc-ad)i^2\left(A+B\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)\text{PolyLog}\left[2,\frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \frac{4B^2d(bc-ad)i^2\text{PolyLog}\left[3,\frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2}
\end{aligned}$$

Result (type 4, 2775 leaves):

$$\begin{aligned}
& \frac{A^2d^2i^2x}{b^2g^2} + \frac{-A^2b^2c^2i^2+2aA^2bcdi^2-a^2A^2d^2i^2}{b^3g^2(a+bx)} - \frac{2(-A^2bcdi^2+aA^2d^2i^2)\text{Log}[a+bx]}{b^3g^2} + \frac{1}{b(bc-ad)g^2(a+bx)} \\
& B^2c^2i^2\left(-2bc+2ad-2d(a+bx)\text{Log}[a+bx]+(-2bc+2ad)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]-b(c+dx)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2+2d(a+bx)\text{Log}[c+dx]\right)+
\end{aligned}$$

$$\begin{aligned}
& \frac{2 A B c^2 i^2}{g^2} \left(-\frac{\left(\frac{a}{b}+x\right)\left(\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{(a+b x)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]} -\frac{\frac{b\left(\frac{c}{d}+x\right) \operatorname{Log}\left[\frac{c}{d}+x\right]}{\left(-a+\frac{b c}{d}\right)^2}+\frac{\operatorname{Log}\left[1-\frac{b\left(\frac{c}{d}+x\right)}{-a+\frac{b c}{d}}\right]}{-a+\frac{b c}{d}}}{b} -\frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]}{b(a+b x)} \right) + \\
& \frac{1}{g^2} 2 A B d^2 i^2 \left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2} -\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^3} -\frac{a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)} -\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^2} -\frac{a^2\left(\left(-b c+a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^3(b c-a d)(a+b x)} +\frac{\left(b x-\frac{a^2}{a+b x}-2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)}{b^3} +\frac{2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3} \right) + \\
& \frac{1}{g^2} 4 A B c d i^2 \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^2} +\frac{a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2(a+b x)} +\frac{a\left(\left(-b c+a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^2(b c-a d)(a+b x)} +\frac{\left(\frac{a}{a+b x}+\operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)}{b^2} -\frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b^2} \right) + \\
& \frac{1}{g^2} B^2 d^2 i^2 \left(-\frac{2 a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3} +\frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3} -\frac{a^2\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3(a+b x)} +\frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b^2 d} +\frac{\left(b x-\frac{a^2}{a+b x}-2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)^2}{b^3} +\frac{1}{b^3(b c-a d)(a+b x)} a^2\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) + \\
& 2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2}-\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^3}-\frac{a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^2}-\frac{a^2\left(\left(-b c+a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^3(b c-a d)(a+b x)}\right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2a \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) - 2 \left(\frac{1}{b^3 d} \left(ad + 2bdx - bdx \text{Log} \left[\frac{c}{d} + x \right] - bc \text{Log} [c + dx] + \right. \right. \\
& \left. \left. \text{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) + d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& \frac{1}{2b^3(bc-ad)(a+bx)} a^2 \left(d(a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) (\text{Log} [a+bx] - \text{Log} [c+dx]) \right) \right) - \\
& 2 \text{Log} \left[\frac{a}{b} + x \right] \left((bc-ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2d(a+bx) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - \frac{1}{b^3} \\
& a \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) - \\
& \left. \frac{2a \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) + \\
& \frac{1}{g^2} 2B^2 c d i^2 \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^3}{3b^2} + \frac{a \left(2 + 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^2(a+bx)} + \frac{\left(\frac{a}{a+bx} + \text{Log} [a+bx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)^2}{b^2} \right) - \\
& \frac{1}{b^2(bc-ad)(a+bx)} a \left(-b(c+dx) \text{Log} \left[\frac{c}{d} + x \right]^2 + 2d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2d(a+bx) \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) + \\
& 2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right) \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^2}{2b^2} + \frac{a \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^2(a+bx)} + \right. \\
& \left. \frac{a \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) (\text{Log} [a+bx] - \text{Log} [c+dx]) \right)}{b^2(bc-ad)(a+bx)} - \frac{\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right]}{b^2} \right) - \\
& 2 \left(-\frac{1}{2b^2(bc-ad)(a+bx)} a \left(d(a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) (\text{Log} [a+bx] - \text{Log} [c+dx]) \right) \right) - \right. \\
& \left. 2 \text{Log} \left[\frac{a}{b} + x \right] \left((bc-ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2d(a+bx) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \frac{1}{2b^2} \\
& \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& \left. \frac{\text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right]}{b^2} \right)
\end{aligned}$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{(a g + b g x)^3} dx$$

Optimal (type 4, 387 leaves, 10 steps):

$$\begin{aligned} & - \frac{2 B^2 d i^2 (c + d x)}{b^2 g^3 (a + b x)} - \frac{B^2 i^2 (c + d x)^2}{4 b g^3 (a + b x)^2} - \frac{2 B d i^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^2 g^3 (a + b x)} - \\ & \frac{B i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{2 b g^3 (a + b x)^2} - \frac{d i^2 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{b^2 g^3 (a + b x)} - \frac{i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{2 b g^3 (a + b x)^2} - \\ & \frac{d^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2 \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} + \frac{2 B d^2 i^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} + \frac{2 B^2 d^2 i^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} \end{aligned}$$

Result (type 4, 3601 leaves):

$$\begin{aligned} & - \frac{A^2 (b^2 c^2 - 2 a b c d + a^2 d^2) i^2}{2 b^3 g^3 (a + b x)^2} + \frac{2 (-A^2 b c d i^2 + a A^2 d^2 i^2)}{b^3 g^3 (a + b x)} + \frac{A^2 d^2 i^2 \operatorname{Log}[a + b x]}{b^3 g^3} - \\ & \left(B^2 c^2 i^2 \left(b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a + b x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d) (b c - 3 a d - 2 b d x) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] + \right. \right. \\ & \left. \left. 2 b (c + d x) (b c - 2 a d - b d x) \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right]^2 + 6 a^2 d^2 \operatorname{Log}[c + d x] + 12 a b d^2 x \operatorname{Log}[c + d x] + 6 b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) \right) / \\ & \left(4 b (b c - a d)^2 g^3 (a + b x)^2 + \frac{1}{g^3} 2 A B c^2 i^2 - \frac{\left(\frac{a}{b} + x \right) \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 4 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{8 (a + b x)^3 \operatorname{Log} \left[\frac{a}{b} + x \right]} \right) \end{aligned}$$

$$\left. \frac{\frac{b \left(\frac{c}{d}+x\right)}{\left(-a+\frac{bc}{d}\right)^3 \left(1-\frac{b \left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right)} - \left(\frac{b^2 \left(\frac{c}{d}+x\right)^2}{\left(-a+\frac{bc}{d}\right)^4 \left(1-\frac{b \left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right)^2} + \frac{2 b \left(\frac{c}{d}+x\right)}{\left(-a+\frac{bc}{d}\right)^3 \left(1-\frac{b \left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right)} \right) \operatorname{Log}\left[\frac{c}{d}+x\right] - \frac{\operatorname{Log}\left[1-\frac{b \left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right]}{\left(-a+\frac{bc}{d}\right)^2}}{2 b} - \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]}{2 b (a+b x)^2} \right. +$$

$$\left. \frac{1}{g^3} 4 A B c d i^2 \left(-\frac{1 + \operatorname{Log}\left[\frac{a}{b}+x\right]}{b^2 (a+b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^2 (a+b x)^2} - \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x])}{b^2 (b c - a d) (a+b x)} - \right. \right.$$

$$\left. \frac{a \left(\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d (a+b x) (b c - a d + d (a+b x) \operatorname{Log}[a+b x] - d (a+b x) \operatorname{Log}[c+d x])}{(b c - a d)^2}\right)}{2 b^2 (a+b x)^2} - \frac{(a+2 b x) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)}{2 b^2 (a+b x)^2} \right) + \frac{1}{g^3}$$

$$2 A B d^2 i^2 \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^3} + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3 (a+b x)} - \frac{a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^3 (a+b x)^2} + \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x])\right)}{b^3 (b c - a d) (a+b x)} \right) +$$

$$\frac{a^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d (a+b x) (b c - a d + d (a+b x) \operatorname{Log}[a+b x] - d (a+b x) \operatorname{Log}[c+d x])}{(b c - a d)^2}\right)}{2 b^3 (a+b x)^2} +$$

$$\frac{\left(\frac{a (3 a + 4 b x)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)}{2 b^3} - \frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{b c - a d}\right]}{b^3} \right) +$$

$$\frac{1}{g^3} 2 B^2 c d i^2 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^2 (a+b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{4 b^2 (a+b x)^2} + 2 \left(-\frac{1 + \operatorname{Log}\left[\frac{a}{b}+x\right]}{b^2 (a+b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^2 (a+b x)^2} - \right. \right.$$

$$\left. \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x])}{b^2 (b c - a d) (a+b x)} - \frac{a \left(\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d (a+b x) (b c - a d + d (a+b x) \operatorname{Log}[a+b x] - d (a+b x) \operatorname{Log}[c+d x])}{(b c - a d)^2}\right)}{2 b^2 (a+b x)^2} \right)$$

$$\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) - \frac{(a+2 b x) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)^2}{2 b^2 (a+b x)^2} -$$

$$2 \left(\frac{1}{2 b^2 (b c - a d) (a+b x)} \left(d (a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x]) \right) \right) - \right.$$

$$\left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left((b c - a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] \right) - 2 d (a+b x) \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) +$$

$$\begin{aligned}
& \left(a \left(-d (-bc + ad) (a + bx) + (bc - ad)^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right) \operatorname{Log} \left[\frac{c}{d} + x \right] + d^2 (a + bx)^2 \operatorname{Log} [a + bx] - d^2 (a + bx)^2 \operatorname{Log} [c + dx] + d (a + bx) \right. \right. \\
& \quad \left. \left(d (a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 (bc - ad) \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 2 d (a + bx) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) \right) \right) / \\
& \quad \left(4 b^2 (bc - ad)^2 (a + bx)^2 \right) + \frac{-b(c + dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 d (a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2 d (a + bx) \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right]}{b^2 (bc - ad) (a + bx)} + \\
& \left(a \left(b (c + dx) (-2ad + b(c - dx)) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 d^2 (a + bx)^2 \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2 d (a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \right. \right. \\
& \quad \left. \left(b (c + dx) + d (a + bx) \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] \right) + 2 d^2 (a + bx)^2 \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] \right) / \left(2 b^2 (bc - ad)^2 (a + bx)^2 \right) + \\
& \frac{1}{g^3} B^2 d^2 i^2 \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3 b^3} + \frac{2 a \left(2 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3 (a + bx)} - \frac{a^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4 b^3 (a + bx)^2} + \right. \\
& \quad \left. \frac{\left(\frac{a(3a + 4bx)}{(a + bx)^2} + 2 \operatorname{Log} [a + bx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c + dx} + \frac{bex}{c + dx} \right] \right)^2}{2 b^3} - \frac{1}{b^3 (bc - ad) (a + bx)} \right. \\
& \quad \left. 2 a \left(-b (c + dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 d (a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2 d (a + bx) \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] \right) - \\
& \quad \left(a^2 \left(b (c + dx) (-2ad + b(c - dx)) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 d^2 (a + bx)^2 \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + \right. \right. \\
& \quad \left. \left. 2 d (a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \left(b (c + dx) + d (a + bx) \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] \right) + 2 d^2 (a + bx)^2 \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] \right) \right) / \\
& \quad \left(2 b^3 (bc - ad)^2 (a + bx)^2 \right) + 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c + dx} + \frac{bex}{c + dx} \right] \right) \\
& \quad \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2 b^3} + \frac{2 a \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{b^3 (a + bx)} - \frac{a^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{4 b^3 (a + bx)^2} + \frac{2 a \left((-bc + ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + bx) \left(\operatorname{Log} [a + bx] - \operatorname{Log} [c + dx] \right) \right)}{b^3 (bc - ad) (a + bx)} \right) + \\
& \quad \left. \frac{a^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d(a + bx)(bc - ad + d(a + bx) \operatorname{Log} [a + bx] - d(a + bx) \operatorname{Log} [c + dx])}{(bc - ad)^2} \right)}{2 b^3 (a + bx)^2} - \frac{\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right]}{b^3} \right) - \\
& \quad 2 \left(-\frac{1}{b^3 (bc - ad) (a + bx)} a \left(d (a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc + ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + bx) \left(\operatorname{Log} [a + bx] - \operatorname{Log} [c + dx] \right) \right) \right) - \\
& \quad \left. 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \left((bc - ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + bx) \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] \right) - 2 d (a + bx) \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) -
\end{aligned}$$

$$\left(a^2 \left(-d (-bc + ad) (a + bx) + (bc - ad)^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right) \operatorname{Log} \left[\frac{c}{d} + x \right] + d^2 (a + bx)^2 \operatorname{Log} [a + bx] - d^2 (a + bx)^2 \operatorname{Log} [c + dx] + d (a + bx) \right. \right. \\ \left. \left(d (a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 (bc - ad) \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 2 d (a + bx) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) \right) \right) / \\ \left(4 b^3 (bc - ad)^2 (a + bx)^2 \right) + \frac{1}{2 b^3} \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] \right) - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] + \right. \\ \left. 2 \operatorname{PolyLog} \left[3, \frac{d(a + bx)}{-bc + ad} \right] \right) + \frac{\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] - 2 \operatorname{PolyLog} \left[3, \frac{b(c + dx)}{bc - ad} \right]}{b^3}$$

Problem 74: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^3 (ci + dix)^3 \left(A + B \operatorname{Log} \left[\frac{e(a + bx)}{c + dx} \right] \right)^2 dx$$

Optimal (type 4, 1089 leaves, 22 steps):

$$\begin{aligned}
& \frac{5 B^2 (b c - a d)^6 g^3 i^3 x}{84 b^3 d^3} + \frac{B^2 (b c - a d)^3 g^3 i^3 (a + b x)^4}{140 b^4} - \frac{29 B^2 (b c - a d)^5 g^3 i^3 (c + d x)^2}{840 b^2 d^4} + \\
& \frac{47 B^2 (b c - a d)^4 g^3 i^3 (c + d x)^3}{1260 b d^4} - \frac{13 B^2 (b c - a d)^3 g^3 i^3 (c + d x)^4}{420 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i^3 (c + d x)^5}{105 d^4} - \\
& \frac{B^2 (b c - a d)^7 g^3 i^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{210 b^4 d^4} - \frac{B (b c - a d)^4 g^3 i^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{210 b^4 d} - \\
& \frac{3 B (b c - a d)^3 g^3 i^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{140 b^4} - \frac{B (b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{35 b^3} + \\
& \frac{2 B (b c - a d)^4 g^3 i^3 (c + d x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{21 b d^4} - \frac{3 B (b c - a d)^3 g^3 i^3 (c + d x)^4 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{14 d^4} + \\
& \frac{6 b B (b c - a d)^2 g^3 i^3 (c + d x)^5 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{35 d^4} - \frac{b^2 B (b c - a d) g^3 i^3 (c + d x)^6 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{21 d^4} + \\
& \frac{(b c - a d)^3 g^3 i^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)^2}{140 b^4} + \frac{(b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)^2}{35 b^3} + \\
& \frac{(b c - a d) g^3 i^3 (a + b x)^4 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)^2}{14 b^2} + \frac{g^3 i^3 (a + b x)^4 (c + d x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)^2}{7 b} + \\
& \frac{B (b c - a d)^5 g^3 i^3 (a + b x)^2 \left(3 A + B + 3 B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{420 b^4 d^2} - \frac{B (b c - a d)^6 g^3 i^3 (a + b x) \left(6 A + 5 B + 6 B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{420 b^4 d^3} - \\
& \frac{B (b c - a d)^7 g^3 i^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(6 A + 11 B + 6 B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{420 b^4 d^4} - \frac{11 B^2 (b c - a d)^7 g^3 i^3 \operatorname{Log}[c + d x]}{420 b^4 d^4} - \frac{B^2 (b c - a d)^7 g^3 i^3 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{70 b^4 d^4}
\end{aligned}$$

Result (type 4, 5123 leaves):

1

2520 b⁴ d⁴

$$\begin{aligned}
& g^3 i^3 \left(-36 b^7 B^2 c^7 + 288 a b^6 B^2 c^6 d - 1008 a^2 b^5 B^2 c^5 d^2 + 756 a^3 b^4 B^2 c^4 d^3 + 756 a^4 b^3 B^2 c^3 d^4 - 1008 a^5 b^2 B^2 c^2 d^5 + 288 a^6 b B^2 c d^6 - 36 a^7 B^2 d^7 - 36 A b^7 B \right. \\
& c^6 d x + 36 b^7 B^2 c^6 d x + 252 a A b^6 B c^5 d^2 x - 270 a b^6 B^2 c^5 d^2 x - 756 a^2 A b^5 B c^4 d^3 x + 876 a^2 b^5 B^2 c^4 d^3 x + 2520 a^3 A^2 b^4 c^3 d^4 x - 1284 a^3 b^4 B^2 c^3 d^4 x + \\
& 756 a^4 A b^3 B c^2 d^5 x + 876 a^4 b^3 B^2 c^2 d^5 x - 252 a^5 A b^2 B c d^6 x - 270 a^5 b^2 B^2 c d^6 x + 36 a^6 A b B d^7 x + 36 a^6 b B^2 d^7 x + 18 A b^7 B c^5 d^2 x^2 - \\
& 27 b^7 B^2 c^5 d^2 x^2 - 126 a A b^6 B c^4 d^3 x^2 + 201 a b^6 B^2 c^4 d^3 x^2 + 3780 a^2 A^2 b^5 c^3 d^4 x^2 - 1512 a^2 A b^5 B c^3 d^4 x^2 - 174 a^2 b^5 B^2 c^3 d^4 x^2 + 3780 a^3 A^2 b^4 c^2 d^5 x^2 + \\
& 1512 a^3 A b^4 B c^2 d^5 x^2 - 174 a^3 b^4 B^2 c^2 d^5 x^2 + 126 a^4 A b^3 B c d^6 x^2 + 201 a^4 b^3 B^2 c d^6 x^2 - 18 a^5 A b^2 B d^7 x^2 - 27 a^5 b^2 B^2 d^7 x^2 - 12 A b^7 B c^4 d^3 x^3 + \\
& 22 b^7 B^2 c^4 d^3 x^3 + 2520 a A^2 b^6 c^3 d^4 x^3 - 1176 a A b^6 B c^3 d^4 x^3 + 152 a b^6 B^2 c^3 d^4 x^3 + 7560 a^2 A^2 b^5 c^2 d^5 x^3 - 348 a^2 b^5 B^2 c^2 d^5 x^3 + 2520 a^3 A^2 b^4 c d^6 x^3 + \\
& 1176 a^3 A b^4 B c d^6 x^3 + 152 a^3 b^4 B^2 c d^6 x^3 + 12 a^4 A b^3 B d^7 x^3 + 22 a^4 b^3 B^2 d^7 x^3 + 630 A^2 b^7 c^3 d^4 x^4 - 306 A b^7 B c^3 d^4 x^4 + 60 b^7 B^2 c^3 d^4 x^4 + \\
& 5670 a A^2 b^6 c^2 d^5 x^4 - 882 a A b^6 B c^2 d^5 x^4 - 60 a b^6 B^2 c^2 d^5 x^4 + 5670 a^2 A^2 b^5 c d^6 x^4 + 882 a^2 A b^5 B c d^6 x^4 - 60 a^2 b^5 B^2 c d^6 x^4 + 630 a^3 A^2 b^4 d^7 x^4 + \\
& 306 a^3 A b^4 B d^7 x^4 + 60 a^3 b^4 B^2 d^7 x^4 + 1512 A^2 b^7 c^2 d^5 x^5 - 360 A b^7 B c^2 d^5 x^5 + 24 b^7 B^2 c^2 d^5 x^5 + 4536 a A^2 b^6 c d^6 x^5 - 48 a b^6 B^2 c d^6 x^5 + \\
& 1512 a^2 A^2 b^5 d^7 x^5 + 360 a^2 A b^5 B d^7 x^5 + 24 a^2 b^5 B^2 d^7 x^5 + 1260 A^2 b^7 c d^6 x^6 - 120 A b^7 B c d^6 x^6 + 1260 a A^2 b^6 d^7 x^6 + 120 a A b^6 B d^7 x^6 + 360 A^2 b^7 d^7 x^7 -
\end{aligned}$$

$$\begin{aligned}
& 36 a^6 b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 252 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 756 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] - 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right] + 630 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 378 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 126 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d} + x\right] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 756 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + 252 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 36 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 126 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 378 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 630 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 18 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}[a + b x] + 114 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}[a + b x] + 1260 a^4 A b^3 B c^3 d^4 \operatorname{Log}[a + b x] + 642 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[a + b x] - \\
& 756 a^5 A b^2 B c^2 d^5 \operatorname{Log}[a + b x] - 990 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[a + b x] + 252 a^6 A b B c d^6 \operatorname{Log}[a + b x] + 288 a^6 b B^2 c d^6 \operatorname{Log}[a + b x] - \\
& 36 a^7 A B d^7 \operatorname{Log}[a + b x] - 36 a^7 B^2 d^7 \operatorname{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 36 b^7 B^2 c^6 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 252 a b^6 B^2 c^5 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 756 a^2 b^5 B^2 c^4 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 5040 a^3 A b^4 B c^3 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 756 a^4 b^3 B^2 c^2 d^5 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 252 a^5 b^2 B^2 c d^6 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a^6 b B^2 d^7 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 18 b^7 B^2 c^5 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 126 a b^6 B^2 c^4 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 7560 a^2 A b^5 B c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 1512 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 7560 a^3 A b^4 B c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1512 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 126 a^4 b^3 B^2 c d^6 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a^5 b^2 B^2 d^7 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 b^7 B^2 c^4 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 5040 a A b^6 B c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 1176 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 15120 a^2 A b^5 B c^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 5040 a^3 A b^4 B c d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 1176 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a^4 b^3 B^2 d^7 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1260 A b^7 B c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 306 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 11340 a A b^6 B c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 882 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 11340 a^2 A b^5 B c d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 882 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1260 a^3 A b^4 B d^7 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 306 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 3024 A b^7 B c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 360 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] +
\end{aligned}$$

$$\begin{aligned}
& 9072 a A b^6 B c d^6 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 3024 a^2 A b^5 B d^7 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 360 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 2520 A b^7 B c d^6 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 120 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2520 a A b^6 B d^7 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 720 A b^7 B d^7 x^7 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 252 a^6 b B^2 c d^6 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 36 a^7 B^2 d^7 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 2520 a^3 b^4 B^2 c^3 d^4 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 3780 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 3780 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 2520 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 7560 a^2 b^5 B^2 c^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 2520 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 630 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 5670 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 5670 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 630 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 1512 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 4536 a b^6 B^2 c d^6 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 1512 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 1260 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 1260 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 360 b^7 B^2 d^7 x^7 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 36 A b^7 B c^7 \operatorname{Log}[c+dx] - \\
& 36 b^7 B^2 c^7 \operatorname{Log}[c+dx] - 252 a A b^6 B c^6 d \operatorname{Log}[c+dx] + 288 a b^6 B^2 c^6 d \operatorname{Log}[c+dx] + 756 a^2 A b^5 B c^5 d^2 \operatorname{Log}[c+dx] - 990 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}[c+dx] - \\
& 1260 a^3 A b^4 B c^4 d^3 \operatorname{Log}[c+dx] + 642 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}[c+dx] + 114 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[c+dx] - 18 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[c+dx] - \\
& 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + \\
& 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + \\
& 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 36 b^4 B^2 c^4 (b^3 c^3 - 7 a b^2 c^2 d + 21 a^2 b c d^2 - 35 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 36 a^4 B^2 d^4 (-35 b^3 c^3 + 21 a b^2 c^2 d - 7 a^2 b c d^2 + a^3 d^3) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 (c i + d i x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 908 leaves, 20 steps):

$$\begin{aligned} & - \frac{7 B^2 (b c - a d)^5 g^2 i^3 x}{180 b^3 d^2} - \frac{7 B^2 (b c - a d)^4 g^2 i^3 (c + d x)^2}{360 b^2 d^3} - \frac{B^2 (b c - a d)^3 g^2 i^3 (c + d x)^3}{60 b d^3} + \\ & \frac{B^2 (b c - a d)^2 g^2 i^3 (c + d x)^4}{60 d^3} + \frac{B^2 (b c - a d)^6 g^2 i^3 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{36 b^4 d^3} - \frac{B (b c - a d)^4 g^2 i^3 (a + b x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^4 d} - \\ & \frac{B (b c - a d)^3 g^2 i^3 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{30 b^4} - \frac{B (b c - a d)^4 g^2 i^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{10 b^2 d^3} + \\ & \frac{B (b c - a d)^3 g^2 i^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{45 b d^3} + \frac{7 B (b c - a d)^2 g^2 i^3 (c + d x)^4 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 d^3} - \\ & \frac{b B (b c - a d) g^2 i^3 (c + d x)^5 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{15 d^3} + \frac{(b c - a d)^3 g^2 i^3 (a + b x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{60 b^4} + \\ & \frac{(b c - a d)^2 g^2 i^3 (a + b x)^3 (c + d x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{20 b^3} + \frac{(b c - a d) g^2 i^3 (a + b x)^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{10 b^2} + \\ & \frac{g^2 i^3 (a + b x)^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{6 b} + \frac{B (b c - a d)^5 g^2 i^3 (a + b x) \left(2 A + B + 2 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^4 d^2} + \\ & \frac{B (b c - a d)^6 g^2 i^3 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(2 A + 3 B + 2 B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{60 b^4 d^3} + \frac{11 B^2 (b c - a d)^6 g^2 i^3 \operatorname{Log} [c + d x]}{180 b^4 d^3} + \frac{B^2 (b c - a d)^6 g^2 i^3 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{30 b^4 d^3} \end{aligned}$$

Result (type 4, 4173 leaves):

$$\begin{aligned} & \frac{1}{360 b^4 d^3} \\ & g^2 i^3 \left(12 b^6 B^2 c^6 - 84 a b^5 B^2 c^5 d + 12 a^2 b^4 B^2 c^4 d^2 + 240 a^3 b^3 B^2 c^3 d^3 - 252 a^4 b^2 B^2 c^2 d^4 + 84 a^5 b B^2 c d^5 - 12 a^6 B^2 d^6 + 12 A b^6 B c^5 d x - 16 b^6 B^2 c^5 d x - \right. \\ & 72 a A b^5 B c^4 d^2 x + 102 a b^5 B^2 c^4 d^2 x + 360 a^2 A^2 b^4 c^3 d^3 x - 60 a^2 A b^4 B c^3 d^3 x - 194 a^2 b^4 B^2 c^3 d^3 x + 180 a^3 A b^3 B c^2 d^4 x + 154 a^3 b^3 B^2 c^2 d^4 x - \\ & 72 a^4 A b^2 B c d^5 x - 54 a^4 b^2 B^2 c d^5 x + 12 a^5 A b B d^6 x + 8 a^5 b B^2 d^6 x - 6 A b^6 B c^4 d^2 x^2 + 11 b^6 B^2 c^4 d^2 x^2 + 360 a A^2 b^5 c^3 d^3 x^2 - \\ & 204 a A b^5 B c^3 d^3 x^2 + 10 a b^5 B^2 c^3 d^3 x^2 + 540 a^2 A^2 b^4 c^2 d^4 x^2 + 180 a^2 A b^4 B c^2 d^4 x^2 - 60 a^2 b^4 B^2 c^2 d^4 x^2 + 36 a^3 A b^3 B c d^5 x^2 + 46 a^3 b^3 B^2 c d^5 x^2 - \\ & 6 a^4 A b^2 B d^6 x^2 - 7 a^4 b^2 B^2 d^6 x^2 + 120 A^2 b^6 c^3 d^3 x^3 - 76 A b^6 B c^3 d^3 x^3 + 18 b^6 B^2 c^3 d^3 x^3 + 720 a A^2 b^5 c^2 d^4 x^3 - 84 a A b^5 B c^2 d^4 x^3 - \\ & 30 a b^5 B^2 c^2 d^4 x^3 + 360 a^2 A^2 b^4 c d^5 x^3 + 156 a^2 A b^4 B c d^5 x^3 + 6 a^2 b^4 B^2 c d^5 x^3 + 4 a^3 A b^3 B d^6 x^3 + 6 a^3 b^3 B^2 d^6 x^3 + 270 A^2 b^6 c^2 d^4 x^4 - \\ & 78 A b^6 B c^2 d^4 x^4 + 6 b^6 B^2 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 + 36 a A b^5 B c d^5 x^4 - 12 a b^5 B^2 c d^5 x^4 + 90 a^2 A^2 b^4 d^6 x^4 + 42 a^2 A b^4 B d^6 x^4 + \\ & 6 a^2 b^4 B^2 d^6 x^4 + 216 A^2 b^6 c d^5 x^5 - 24 A b^6 B c d^5 x^5 + 144 a A^2 b^5 d^6 x^5 + 24 a A b^5 B d^6 x^5 + 60 A^2 b^6 d^6 x^6 + 12 a b^5 B^2 c^5 d \operatorname{Log} \left[\frac{a}{b} + x \right] - \\ & 72 a^2 b^4 B^2 c^4 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 60 a^3 b^3 B^2 c^3 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log} \left[\frac{a}{b} + x \right] - 72 a^5 b B^2 c d^5 \operatorname{Log} \left[\frac{a}{b} + x \right] + 12 a^6 B^2 d^6 \operatorname{Log} \left[\frac{a}{b} + x \right] + \end{aligned}$$

$$\begin{aligned}
& 120 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 90 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 36 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 6 a^6 B^2 d^6 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 180 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - 12 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 6 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 36 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 90 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[a + b x] + 240 a^3 A b^3 B c^3 d^3 \operatorname{Log}[a + b x] + \\
& 128 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[a + b x] - 180 a^4 A b^2 B c^2 d^4 \operatorname{Log}[a + b x] - 186 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a + b x] + 72 a^5 A b B c d^5 \operatorname{Log}[a + b x] + \\
& 60 a^5 b B^2 c d^5 \operatorname{Log}[a + b x] - 12 a^6 A B d^6 \operatorname{Log}[a + b x] - 8 a^6 B^2 d^6 \operatorname{Log}[a + b x] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 12 b^6 B^2 c^5 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 72 a b^5 B^2 c^4 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a^2 A b^4 B c^3 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 60 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 180 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 72 a^4 b^2 B^2 c d^5 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a^5 b B^2 d^6 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 6 b^6 B^2 c^4 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a A b^5 B c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 204 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 180 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 36 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 6 a^4 b^2 B^2 d^6 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 240 A b^6 B c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 76 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1440 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 84 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 720 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 156 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 540 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 78 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 180 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 42 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 432 A b^6 B c d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 24 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 288 a A b^5 B d^6 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 120 A b^6 B d^6 x^6 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 72 a^5 b B^2 c d^5 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 a^6 B^2 d^6 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 360 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 360 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 120 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 +
\end{aligned}$$

$$\begin{aligned}
& 720 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 360 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 270 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 90 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 216 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 144 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 12 A b^6 B c^6 \operatorname{Log}[c+dx] + 16 b^6 B^2 c^6 \operatorname{Log}[c+dx] + 72 a A b^5 B c^5 d \operatorname{Log}[c+dx] - 108 a b^5 B^2 c^5 d \operatorname{Log}[c+dx] - \\
& 180 a^2 A b^4 B c^4 d^2 \operatorname{Log}[c+dx] + 66 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[c+dx] + 32 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[c+dx] - 6 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[c+dx] + \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 12 b^4 B^2 c^4 (b^2 c^2 - 6 a b c d + 15 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 12 a^3 B^2 d^3 (-20 b^3 c^3 + 15 a b^2 c^2 d - 6 a^2 b c d^2 + a^3 d^3) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 76: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)(ci + dix)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 730 leaves, 19 steps):

$$\begin{aligned}
& \frac{B^2 (bc - ad)^4 g i^3 x}{60 b^3 d} + \frac{B^2 (bc - ad)^3 g i^3 (c + dx)^2}{30 b^2 d^2} + \frac{B^2 (bc - ad)^2 g i^3 (c + dx)^3}{30 b d^2} - \\
& \frac{B^2 (bc - ad)^5 g i^3 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{12 b^4 d^2} - \frac{B (bc - ad)^4 g i^3 (a + bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{10 b^4 d} - \\
& \frac{B (bc - ad)^3 g i^3 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{10 b^4} + \frac{3B (bc - ad)^3 g i^3 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{20 b^2 d^2} + \\
& \frac{B (bc - ad)^2 g i^3 (c + dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{30 b d^2} - \frac{B (bc - ad) g i^3 (c + dx)^4 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{10 d^2} + \\
& \frac{(bc - ad)^3 g i^3 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{20 b^4} + \frac{(bc - ad)^2 g i^3 (a + bx)^2 (c + dx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{10 b^3} + \\
& \frac{3 (bc - ad) g i^3 (a + bx)^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{20 b^2} + \frac{g i^3 (a + bx)^2 (c + dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{5 b} - \\
& \frac{B (bc - ad)^5 g i^3 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{10 b^4 d^2} - \frac{11 B^2 (bc - ad)^5 g i^3 \operatorname{Log}[c + dx]}{60 b^4 d^2} - \frac{B^2 (bc - ad)^5 g i^3 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{10 b^4 d^2}
\end{aligned}$$

Result (type 4, 3093 leaves):

$$\begin{aligned}
& \frac{1}{60 b^4 d^2} g i^3 \left(-6 b^5 B^2 c^5 - 24 a b^4 B^2 c^4 d + 90 a^2 b^3 B^2 c^3 d^2 - 90 a^3 b^2 B^2 c^2 d^3 + 36 a^4 b B^2 c d^4 - 6 a^5 B^2 d^5 - 6 A b^5 B c^4 d x + 11 b^5 B^2 c^4 d x + 60 a A^2 b^4 c^3 d^2 x - \right. \\
& 30 a A b^4 B c^3 d^2 x - 28 a b^4 B^2 c^3 d^2 x + 60 a^2 A b^3 B c^2 d^3 x + 24 a^2 b^3 B^2 c^2 d^3 x - 30 a^3 A b^2 B c d^4 x - 8 a^3 b^2 B^2 c d^4 x + 6 a^4 A b B d^5 x + a^4 b B^2 d^5 x + \\
& 30 A^2 b^5 c^3 d^2 x^2 - 27 A b^5 B c^3 d^2 x^2 + 8 b^5 B^2 c^3 d^2 x^2 + 90 a A^2 b^4 c^2 d^3 x^2 + 15 a A b^4 B c^2 d^3 x^2 - 18 a b^4 B^2 c^2 d^3 x^2 + 15 a^2 A b^3 B c d^4 x^2 + \\
& 12 a^2 b^3 B^2 c d^4 x^2 - 3 a^3 A b^2 B d^5 x^2 - 2 a^3 b^2 B^2 d^5 x^2 + 60 A^2 b^5 c^2 d^3 x^3 - 22 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 60 a A^2 b^4 c d^4 x^3 + 20 a A b^4 B c d^4 x^3 - \\
& 4 a b^4 B^2 c d^4 x^3 + 2 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 45 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + 15 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 - \\
& 6 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] - 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 15 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - 3 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 15 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 60 a^2 A b^3 B c^3 d^2 \operatorname{Log}[a + bx] + 27 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + bx] - 60 a^3 A b^2 B c^2 d^3 \operatorname{Log}[a + bx] - \\
& 37 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + bx] + 30 a^4 A b B c d^4 \operatorname{Log}[a + bx] + 11 a^4 b B^2 c d^4 \operatorname{Log}[a + bx] - 6 a^5 A B d^5 \operatorname{Log}[a + bx] - a^5 B^2 d^5 \operatorname{Log}[a + bx] - \\
& 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] - 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + \\
& 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + bx] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] + \\
& 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + bx] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] +
\end{aligned}$$

$$\begin{aligned}
& 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \\
& 6 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a A b^4 B c^3 d^2 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 30 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 30 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 6 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 27 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 180 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 15 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 15 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 3 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 120 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 22 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 2 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 90 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 30 a^4 b B^2 c d^4 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 6 a^5 B^2 d^5 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 30 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 90 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 60 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 45 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 6 A b^5 B c^5 \operatorname{Log}[c+dx] - 11 b^5 B^2 c^5 \operatorname{Log}[c+dx] - 30 a A b^4 B c^4 d \operatorname{Log}[c+dx] + a b^4 B^2 c^4 d \operatorname{Log}[c+dx] + \\
& 13 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+dx] - 3 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+dx] - 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + \\
& 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 6 b^4 B^2 c^4 (bc - 5ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 a^2 B^2 d^2 (-10 b^3 c^3 + 10 a b^2 c^2 d - 5 a^2 b c d^2 + a^3 d^3) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 77: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 420 leaves, 15 steps):

$$\begin{aligned}
& \frac{5 B^2 (b c - a d)^3 i^3 x}{12 b^3} + \frac{B^2 (b c - a d)^2 i^3 (c + d x)^2}{12 b^2 d} + \frac{5 B^2 (b c - a d)^4 i^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{12 b^4 d} - \frac{B (b c - a d)^3 i^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{2 b^4} - \\
& \frac{B (b c - a d)^2 i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{4 b^2 d} - \frac{B (b c - a d) i^3 (c + d x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{6 b d} + \frac{i^3 (c + d x)^4 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)^2}{4 d} + \\
& \frac{11 B^2 (b c - a d)^4 i^3 \operatorname{Log}[c + d x]}{12 b^4 d} + \frac{B (b c - a d)^4 i^3 \left(A + B \operatorname{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1 - \frac{b (c+d x)}{d (a+b x)}\right]}{2 b^4 d} - \frac{B^2 (b c - a d)^4 i^3 \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right]}{2 b^4 d}
\end{aligned}$$

Result (type 4, 2110 leaves):

$$\begin{aligned}
& \frac{1}{12 b^4 d} i^3 \left(-18 b^4 B^2 c^4 + 54 a b^3 B^2 c^3 d - 60 a^2 b^2 B^2 c^2 d^2 + 30 a^3 b B^2 c d^3 - 6 a^4 B^2 d^4 + 12 A^2 b^4 c^2 d x - 18 A b^4 B c^3 d x + 7 b^4 B^2 c^3 d x + 36 a A b^3 B c^2 d^2 x - \right. \\
& 19 a b^3 B^2 c^2 d^2 x - 24 a^2 A b^2 B c d^3 x + 17 a^2 b^2 B^2 c d^3 x + 6 a^3 A b B d^4 x - 5 a^3 b B^2 d^4 x + 18 A^2 b^4 c^2 d^2 x^2 - 9 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + \\
& 12 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 - 3 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 12 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - \\
& 18 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
& 18 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 18 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 24 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 24 a A b^3 B c^3 d \operatorname{Log}[a + b x] - 36 a^2 A b^2 B c^2 d^2 \operatorname{Log}[a + b x] + \\
& 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] + 24 a^3 A b B c d^3 \operatorname{Log}[a + b x] - 14 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] - 6 a^4 A B d^4 \operatorname{Log}[a + b x] + 5 a^4 B^2 d^4 \operatorname{Log}[a + b x] - \\
& 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + \\
& 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] - 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + \\
& 24 A b^4 B c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 24 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 6 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 9 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 3 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a b^3 B^2 c^3 d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 24 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 6 a^4 B^2 d^4 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\
& 18 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 12 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 - 6 A b^4 B c^4 \operatorname{Log}[c + d x] - \\
& 7 b^4 B^2 c^4 \operatorname{Log}[c + d x] + 10 a b^3 B^2 c^3 d \operatorname{Log}[c + d x] - 3 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{bc - ad}\right] - \\
& \left. 6 b^4 B^2 c^4 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-bc + ad}\right] + 6 a B^2 d (-4 b^3 c^3 + 6 a b^2 c^2 d - 4 a^2 b c d^2 + a^3 d^3) \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{bc - ad}\right] \right)
\end{aligned}$$

Problem 78: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 712 leaves, 26 steps):

$$\begin{aligned} & \frac{B^2 d (bc - ad)^2 i^3 x}{3 b^3 g} + \frac{B^2 (bc - ad)^3 i^3 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{3 b^4 g} - \frac{5 B d (bc - ad)^2 i^3 (a + bx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b^4 g} - \\ & \frac{B (bc - ad) i^3 (c + dx)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{3 b^2 g} + \frac{2 B (bc - ad)^3 i^3 \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)}{b^4 g} + \\ & \frac{d (bc - ad)^2 i^3 (a + bx) \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{b^4 g} + \frac{(bc - ad) i^3 (c + dx)^2 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{2 b^2 g} + \\ & \frac{i^3 (c + dx)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{3 b g} + \frac{2 B^2 (bc - ad)^3 i^3 \operatorname{Log} [c + dx]}{b^4 g} + \frac{5 B (bc - ad)^3 i^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{3 b^4 g} - \\ & \frac{(bc - ad)^3 i^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2 \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} + \frac{2 B^2 (bc - ad)^3 i^3 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{b^4 g} - \frac{5 B^2 (bc - ad)^3 i^3 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{3 b^4 g} + \\ & \frac{2 B (bc - ad)^3 i^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} + \frac{2 B^2 (bc - ad)^3 i^3 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} \end{aligned}$$

Result (type 4, 5055 leaves):

$$\begin{aligned} & \frac{1}{12 b^4 g} \\ & i^3 \left(72 A b^3 B c^3 + 9 b^3 B^2 c^3 - 144 a A b^2 B c^2 d - 23 a b^2 B^2 c^2 d + 96 a^2 A b B c d^2 - 51 a^2 b B^2 c d^2 - 24 a^3 A B d^3 + 21 a^3 B^2 d^3 + 36 A^2 b^3 c^2 d x - 28 A b^3 B c^2 d x + \right. \\ & 4 b^3 B^2 c^2 d x - 36 a A^2 b^2 c d^2 x + 48 a A b^2 B c d^2 x - 8 a b^2 B^2 c d^2 x + 12 a^2 A^2 b d^3 x - 20 a^2 A b B d^3 x + 4 a^2 b B^2 d^3 x + 18 A^2 b^3 c d^2 x^2 - \\ & 4 A b^3 B c d^2 x^2 - 6 a A^2 b^2 d^3 x^2 + 4 a A b^2 B d^3 x^2 + 4 A^2 b^3 d^3 x^3 - 72 b^3 B^2 c^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 72 a A b^2 B c^2 d \operatorname{Log} \left[\frac{a}{b} + x \right] + 116 a b^2 B^2 c^2 d \operatorname{Log} \left[\frac{a}{b} + x \right] - \\ & 72 a^2 A b B c d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 30 a^2 b B^2 c d^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 24 a^3 A B d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^3 B^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 12 A b^3 B c^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\ & 36 a A b^2 B c^2 d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 36 a b^2 B^2 c^2 d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 36 a^2 A b B c d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 18 a^2 b B^2 c d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\ & 12 a^3 A B d^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 a^3 B^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 8 b^3 B^2 c^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 + 24 a b^2 B^2 c^2 d \operatorname{Log} \left[\frac{a}{b} + x \right]^3 - 24 a^2 b B^2 c d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 + \\ & 8 a^3 B^2 d^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 - 72 A b^3 B c^3 \operatorname{Log} \left[\frac{c}{d} + x \right] + 54 b^3 B^2 c^3 \operatorname{Log} \left[\frac{c}{d} + x \right] + 72 a A b^2 B c^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] - 90 a b^2 B^2 c^2 d \operatorname{Log} \left[\frac{c}{d} + x \right] - \end{aligned}$$

$$\begin{aligned}
& 24 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 50 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 42 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 12 A^2 b^3 c^3 \operatorname{Log}[a + b x] - 36 a A^2 b^2 c^2 d \operatorname{Log}[a + b x] + \\
& 36 a^2 A^2 b c d^2 \operatorname{Log}[a + b x] - 36 a^2 A b B c d^2 \operatorname{Log}[a + b x] - 14 a^2 b B^2 c d^2 \operatorname{Log}[a + b x] - 12 a^3 A^2 d^3 \operatorname{Log}[a + b x] + \\
& 20 a^3 A B d^3 \operatorname{Log}[a + b x] - 6 a^3 B^2 d^3 \operatorname{Log}[a + b x] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}[a + b x] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}[a + b x] + \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}[a + b x] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}[a + b x] + 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}[a + b x] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}[a + b x] + \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}[a + b x] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}[a + b x] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 144 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 96 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 72 A b^3 B c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 28 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 72 a A b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 48 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a^2 A b B d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 20 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 36 A b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 a A b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] +
\end{aligned}$$

$$\begin{aligned}
& 8 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 24 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 24 A b^3 B c^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 72 a A b^2 B c^2 d \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 72 a^2 A b B c d^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 36 a^2 b B^2 c d^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 24 a^3 A B d^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 20 a^3 B^2 d^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + 36 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 36 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 12 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 18 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 6 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 4 b^3 B^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + \\
& 12 b^3 B^2 c^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 36 a b^2 B^2 c^2 d \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 36 a^2 b B^2 c d^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - \\
& 12 a^3 B^2 d^3 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 28 A b^3 B c^3 \operatorname{Log}[c+dx] + 42 b^3 B^2 c^3 \operatorname{Log}[c+dx] - 12 a A b^2 B c^2 d \operatorname{Log}[c+dx] - \\
& 98 a b^2 B^2 c^2 d \operatorname{Log}[c+dx] + 44 a^2 b B^2 c d^2 \operatorname{Log}[c+dx] - 28 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 12 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + \\
& 28 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 12 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 28 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 12 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 44 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 132 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] -
\end{aligned}$$

$$\begin{aligned}
& 132 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 44 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 4 B^2 (bc-ad)^3 \left(-11 + 6 \operatorname{Log}\left[\frac{a}{b} + x\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 24 B (bc-ad)^3 \left(A - B \operatorname{Log}\left[\frac{a}{b} + x\right] + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + \\
& 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 79: Result more than twice size of optimal antiderivative.

$$\int \frac{(cix+dx)^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{(ag+bgx)^2} dx$$

Optimal (type 4, 692 leaves, 17 steps):

$$\begin{aligned}
& -\frac{2 B^2 (bc-ad)^2 i^3 (c+dx)}{b^3 g^2 (a+bx)} - \frac{B d^2 (bc-ad) i^3 (a+bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^4 g^2} - \frac{2 B (bc-ad)^2 i^3 (c+dx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^3 g^2 (a+bx)} + \\
& \frac{4 B d (bc-ad)^2 i^3 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^4 g^2} + \frac{2 d^2 (bc-ad) i^3 (a+bx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^4 g^2} - \\
& \frac{(bc-ad)^2 i^3 (c+dx) \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^3 g^2 (a+bx)} + \frac{d i^3 (c+dx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{2 b^2 g^2} + \frac{B^2 d (bc-ad)^2 i^3 \operatorname{Log}[c+dx]}{b^4 g^2} + \\
& \frac{B d (bc-ad)^2 i^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} - \frac{3 d (bc-ad)^2 i^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} + \\
& \frac{4 B^2 d (bc-ad)^2 i^3 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^4 g^2} - \frac{B^2 d (bc-ad)^2 i^3 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} + \\
& \frac{6 B d (bc-ad)^2 i^3 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} + \frac{6 B^2 d (bc-ad)^2 i^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2}
\end{aligned}$$

Result (type 4, 4817 leaves):

$$\begin{aligned}
& \frac{A^2 d^2 (3bc - 2ad) i^3 x}{b^3 g^2} + \frac{A^2 d^3 i^3 x^2}{2 b^2 g^2} + \frac{-A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3}{b^4 g^2 (a + b x)} + \\
& \frac{3 (A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3) \operatorname{Log}[a + b x]}{b^4 g^2} + \frac{1}{b (bc - ad) g^2 (a + b x)} \\
& B^2 c^3 i^3 \left(-2bc + 2ad - 2d(a + bx) \operatorname{Log}[a + bx] + (-2bc + 2ad) \operatorname{Log}\left[\frac{e(a + bx)}{c + dx}\right] - b(c + dx) \operatorname{Log}\left[\frac{e(a + bx)}{c + dx}\right]^2 + 2d(a + bx) \operatorname{Log}[c + dx] \right) + \\
& 2ABc^3 i^3 \left(-\frac{\left(\frac{a}{b} + x\right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{(a + bx)^2 \operatorname{Log}\left[\frac{a}{b} + x\right]} - \frac{\frac{b\left(\frac{c}{d} + x\right) \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a - \frac{bc}{d}}\right]}}{\left(-a - \frac{bc}{d}\right)^2 \left(1 - \frac{b\left(\frac{c}{d} + x\right)}{-a - \frac{bc}{d}}\right)} - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]}}{b(a + bx)} \right) + \\
& \frac{1}{g^2} 2ABd^3 i^3 \left(-\frac{2a\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2b^4} + \frac{a^3 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + bx)} + \frac{2a\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \right. \\
& \left. -\frac{\frac{1}{2} b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \operatorname{Log}[a + bx]}{b^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{a + bx}{b}\right]}{b^2} + \frac{a^3 \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx]\right)\right)}{b^4 (bc - ad) (a + bx)} - \right. \\
& \left. -\frac{\frac{1}{2} d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \operatorname{Log}[c + dx]}{d^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c + dx}{d}\right]}{b^2} + \frac{\left(-4abx + b^2 x^2 + \frac{2a^3}{a + bx} + 6a^2 \operatorname{Log}[a + bx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]\right)}{2b^4} - \right. \\
& \left. \frac{3a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]\right)}{b^4} \right) + \frac{1}{g^2} \\
& 6ABcd^2 i^3 \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + bx)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} - \right. \\
& \left. \frac{a^2 \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx]\right)\right)}{b^3 (bc - ad) (a + bx)} + \right. \\
& \left. \frac{\left(bx - \frac{a^2}{a + bx} - 2a \operatorname{Log}[a + bx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]\right)}{b^3} + \frac{2a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]\right)}{b^3} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{g^2} 6 A B C^2 d i^3 \left(\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2 (a + b x)} + \frac{a \left((-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x])\right)}{b^2 (b c - a d) (a + b x)} \right) + \\
& \left. \frac{\left(\frac{a}{a + b x} + \text{Log}[a + b x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{b^2} - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]}{b^2} \right) + \\
& \frac{1}{g^2} B^2 d^3 i^3 \left(\frac{a^2 \text{Log}\left[\frac{a}{b} + x\right]^3}{b^4} - \frac{2 a (a + b x) \left(2 - 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4} + \frac{a^3 \left(2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4 (a + b x)} + \right. \\
& \frac{(a + b x) \left(-7 a + b x + (6 a - 2 b x) \text{Log}\left[\frac{a}{b} + x\right] - 2 (a - b x) \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{4 b^4} - \\
& \frac{2 a (c + d x) \left(2 - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{b^3 d} + \frac{(c + d x) \left(-7 c + d x + (6 c - 2 d x) \text{Log}\left[\frac{c}{d} + x\right] - 2 (c - d x) \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 b^2 d^2} + \\
& \left. \frac{\left(-4 a b x + b^2 x^2 + \frac{2 a^3}{a + b x} + 6 a^2 \text{Log}[a + b x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)^2}{2 b^4} - \frac{1}{b^4 (b c - a d) (a + b x)} \right) + \\
& a^3 \left(-b (c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 d (a + b x) \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] + 2 \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
& \left. \left. \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) \left(-\frac{2 a \left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3 a^2 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{a^3 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \frac{2 a \left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \right. \\
& \left. \frac{-\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a + b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a + b x}{b}\right]}{b^2} + \frac{a^3 \left((-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x])\right)}{b^4 (b c - a d) (a + b x)} - \right. \\
& \left. \frac{-\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c + d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c + d x}{d}\right]}{b^2} - \frac{3 a^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)}{b^4} \right) - \\
& 2 \left(-\frac{1}{b^4 d} 2 a \left(a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c + d x] + \text{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right]\right) \right) + \right. \\
& (b c - a d) \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \frac{1}{4 b^4 d^2} \left(-2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \text{Log}\left[\frac{c}{d} + x\right] - \right. \\
& \left. b^2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + a^2 d^2 \text{Log}[a + b x] + b^2 c^2 \text{Log}[c + d x] + 2 a b c d \text{Log}[c + d x] + \text{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - \right. \\
& \left. \left. 2 d^2 (a^2 - b^2 x^2) \text{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right]\right) + (-2 b^2 c^2 + 2 a^2 d^2) \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2 b^4 (b c - a d) (a + b x)} a^3 \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - \\
& 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \frac{1}{2 b^4} \\
& 3 a^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& \left. \frac{3 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right)}{b^4} \right) + \\
& \frac{1}{g^2} 3 B^2 c d^2 i^3 \left(-\frac{2 a \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b^3} + \frac{(a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^3} - \frac{a^2 \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^3 (a + b x)} + \right. \\
& \left. \frac{(c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b^2 d} + \frac{\left(b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{-a e}{c + d x} + \frac{b e x}{c + d x}\right] \right)^2}{b^3} + \right. \\
& \left. \frac{1}{b^3 (b c - a d) (a + b x)} a^2 \left(-b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \right. \\
& \left. 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) \right. \\
& \left. \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} - \right. \right. \\
& \left. \left. \frac{a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{b^3 (b c - a d) (a + b x)} + \frac{2 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right)}{b^3} \right) \right) - \\
& 2 \left(\frac{1}{b^3 d} \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) \right) + \right. \\
& \left. (b c - a d) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \frac{1}{2 b^3 (b c - a d) (a + b x)} \\
& a^2 \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - \\
& 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - \frac{1}{b^3} \\
& a \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 a \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3} \right) + \\
& \frac{1}{g^2} 3 B^2 c^2 d i^3 \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^2} + \frac{a \left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{b^2(a+b x)} + \frac{\left(\frac{-a}{a+b x}+\operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)^2}{b^2} \right. \\
& \frac{1}{b^2(b c-a d)(a+b x)} a \left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
& 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^2} + \frac{a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2(a+b x)} + \right. \\
& \left. \frac{a\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^2(b c-a d)(a+b x)} - \frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b^2} \right) - \\
& 2 \left(-\frac{1}{2 b^2(b c-a d)(a+b x)} a \left(d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right) \right) - \right. \\
& \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left(\left(b c-a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) + \frac{1}{2 b^2} \\
& \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) \left. + \right. \\
& \left. \frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b^2} \right)
\end{aligned}$$

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{(a g+b g x)^3} d x$$

Optimal (type 4, 604 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{4 B^2 d (b c - a d) i^3 (c + d x)}{b^3 g^3 (a + b x)} - \frac{B^2 (b c - a d) i^3 (c + d x)^2}{4 b^2 g^3 (a + b x)^2} - \frac{4 B d (b c - a d) i^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{b^3 g^3 (a + b x)} - \\
 & \frac{B (b c - a d) i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{2 b^2 g^3 (a + b x)^2} + \frac{2 B d^2 (b c - a d) i^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{b^4 g^3} + \\
 & \frac{d^3 i^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{b^4 g^3} - \frac{2 d (b c - a d) i^3 (c + d x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{2 b^2 g^3 (a + b x)^2} - \\
 & \frac{3 d^2 (b c - a d) i^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^3} + \frac{2 B^2 d^2 (b c - a d) i^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^4 g^3} + \\
 & \frac{6 B d^2 (b c - a d) i^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^3} + \frac{6 B^2 d^2 (b c - a d) i^3 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^3}
 \end{aligned}$$

Result (type 4, 5661 leaves):

$$\begin{aligned}
 & \frac{A^2 d^3 i^3 x}{b^3 g^3} - \frac{A^2 (b^3 c^3 - 3 a b^2 c^2 d + 3 a^2 b c d^2 - a^3 d^3) i^3}{2 b^4 g^3 (a + b x)^2} - \frac{3 (A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3)}{b^4 g^3 (a + b x)} - \frac{3 (-A^2 b c d^2 i^3 + a A^2 d^3 i^3) \operatorname{Log}[a + b x]}{b^4 g^3} - \\
 & \left(B^2 c^3 i^3 \left(b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a + b x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d) (b c - 3 a d - 2 b d x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \right. \right. \\
 & \left. \left. 2 b (c + d x) (b c - 2 a d - b d x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 + 6 a^2 d^2 \operatorname{Log}[c + d x] + 12 a b d^2 x \operatorname{Log}[c + d x] + 6 b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) \right) / \\
 & \left(4 b (b c - a d)^2 g^3 (a + b x)^2 \right) + \frac{1}{g^3} 2 A B c^3 i^3 \left(- \frac{\left(\frac{a}{b} + x\right) \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{8 (a + b x)^3 \operatorname{Log}\left[\frac{a}{b} + x\right]} - \right. \\
 & \left. \frac{\frac{b \left(\frac{c}{d} + x\right)}{\left(-a + \frac{b c}{d}\right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)}{\left(-a + \frac{b c}{d}\right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)^2} + \frac{2 b \left(\frac{c}{d} + x\right)}{\left(-a + \frac{b c}{d}\right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)} \right) \operatorname{Log}\left[\frac{c}{d} + x\right] - \frac{\operatorname{Log}\left[1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right]}{\left(-a + \frac{b c}{d}\right)^2} \right. \\
 & \left. - \frac{-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{-a e}{c + d x} + \frac{b e x}{c + d x}\right]}{2 b (a + b x)^2} \right) +
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{g^3} 6 A B c^2 d i^3 \left(-\frac{1 + \operatorname{Log}\left[\frac{a}{b} + x\right]}{b^2 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^2 (a + b x)^2} - \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])}{b^2 (b c - a d) (a + b x)} - \right. \\
& \left. \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 b^2 (a + b x)^2} - \frac{(a + 2 b x) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 b^2 (a + b x)^2} \right) + \\
& \frac{1}{g^3} 2 A B d^3 i^3 \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} - \frac{3 a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} - \frac{3 a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \frac{a^3 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^4 (a + b x)^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} - \right. \\
& \left. \frac{3 a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])\right)}{b^4 (b c - a d) (a + b x)} - \frac{a^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 b^4 (a + b x)^2} - \right. \\
& \left. \frac{\left(-2 b x + \frac{a^2 (5 a + 6 b x)}{(a + b x)^2} + 6 a \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 b^4} + \frac{3 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]\right)}{b^4} \right) + \\
& \frac{1}{g^3} 6 A B c d^2 i^3 \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^3 (a + b x)^2} + \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])\right)}{b^3 (b c - a d) (a + b x)} \right) + \\
& \frac{a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 b^3 (a + b x)^2} + \\
& \left. \frac{\left(\frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 b^3} - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^3} \right) + \\
& \frac{1}{g^3} 3 B^2 c^2 d i^3 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^2 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{4 b^2 (a + b x)^2} + 2 \left(-\frac{1 + \operatorname{Log}\left[\frac{a}{b} + x\right]}{b^2 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^2 (a + b x)^2} - \right. \\
& \left. \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])}{b^2 (b c - a d) (a + b x)} - \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 b^2 (a + b x)^2} \right) \\
& \left. \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) - \frac{(a + 2 b x) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)^2}{2 b^2 (a + b x)^2} - \right. \\
& \left. 2 \left(\frac{1}{2 b^2 (b c - a d) (a + b x)} \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((bc - ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \right) + \\
& \left(a \left(-d(-bc + ad)(a + bx) + (bc - ad)^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) \operatorname{Log}\left[\frac{c}{d} + x\right] + d^2(a + bx)^2 \operatorname{Log}[a + bx] - d^2(a + bx)^2 \operatorname{Log}[c + dx] + d(a + bx) \right. \right. \\
& \quad \left. \left. \left(d(a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2(bc - ad) \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2d(a + bx) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \right) \right) \right) \right) / \\
& \left(4b^2(bc - ad)^2(a + bx)^2 \right) + \frac{-b(c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]}{b^2(bc - ad)(a + bx)} + \\
& \left(a \left(b(c + dx)(-2ad + b(c - dx)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2d^2(a + bx)^2 \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \\
& \quad \left. \left. \left(b(c + dx) + d(a + bx) \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] \right) + 2d^2(a + bx)^2 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right] \right) \right) / \left(2b^2(bc - ad)^2(a + bx)^2 \right) + \\
& \frac{1}{g^3} B^2 d^3 i^3 \left(-\frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{b^4} + \frac{(a + bx) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^4} - \frac{3a^2 \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^4(a + bx)} + \right. \\
& \quad \left. \frac{a^3 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{4b^4(a + bx)^2} + \frac{(c + dx) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b^3 d} - \right. \\
& \quad \left. \frac{\left(-2bx + \frac{a^2(5a + 6bx)}{(a + bx)^2} + 6a \operatorname{Log}[a + bx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right] \right)^2}{2b^4} + \frac{1}{b^4(bc - ad)(a + bx)} \right. \\
& \quad \left. 3a^2 \left(-b(c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right] \right) + \right. \\
& \quad \left(a^3 \left(b(c + dx)(-2ad + b(c - dx)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2d^2(a + bx)^2 \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \\
& \quad \left. \left. \left(b(c + dx) + d(a + bx) \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] \right) + 2d^2(a + bx)^2 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right] \right) \right) / \left(2b^4(bc - ad)^2(a + bx)^2 \right) + \\
& \quad 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right] \right) \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} - \frac{3a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2b^4} - \frac{3a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^4(a + bx)} + \right. \\
& \quad \left. \frac{a^3 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{4b^4(a + bx)^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} - \frac{3a^2 \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right) \right)}{b^4(bc - ad)(a + bx)} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a^3 \left(\text{Log} \left[\frac{c}{d} + x \right] + \frac{d(a+bx)(bc-ad+d(a+bx)\text{Log}[a+bx]-d(a+bx)\text{Log}[c+dx])}{(bc-ad)^2} \right)}{2b^4(a+bx)^2} + \frac{3a \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^4} \right) - \\
& 2 \left(\frac{1}{b^4 d} \left(ad + 2bdx - bdx \text{Log} \left[\frac{c}{d} + x \right] - bc \text{Log} [c+dx] + \text{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) + d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) \right. \right. \\
& \quad \left. \left. (bc-ad) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \frac{1}{2b^4(bc-ad)(a+bx)} \\
& 3a^2 \left(d(a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) (\text{Log} [a+bx] - \text{Log} [c+dx]) \right) \right) - \\
& 2 \text{Log} \left[\frac{a}{b} + x \right] \left((bc-ad) \text{Log} \left[\frac{c}{d} + x \right] + d(a+bx) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2d(a+bx) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \Bigg) + \\
& \left(a^3 \left(-d(-bc+ad)(a+bx) + (bc-ad)^2 \left(1 + 2 \text{Log} \left[\frac{a}{b} + x \right] \right) \text{Log} \left[\frac{c}{d} + x \right] + d^2(a+bx)^2 \text{Log} [a+bx] - d^2(a+bx)^2 \text{Log} [c+dx] + d(a+bx) \right. \right. \\
& \quad \left. \left. \left(d(a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2(bc-ad) \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right) - 2d(a+bx) \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) \right) \right) \Bigg) / \\
& \left(4b^4(bc-ad)^2(a+bx)^2 \right) - \frac{1}{2b^4} 3a \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + \right. \\
& \quad \left. 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) \Bigg) - \frac{3a \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^4} \Bigg) + \\
& \frac{1}{g^3} 3B^2 c d^2 i^3 \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^3}{3b^3} + \frac{2a \left(2 + 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3(a+bx)} - \frac{a^2 \left(1 + 2 \text{Log} \left[\frac{a}{b} + x \right] + 2 \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4b^3(a+bx)^2} + \right. \\
& \quad \left. \frac{\left(\frac{a(3a+4bx)}{(a+bx)^2} + 2 \text{Log} [a+bx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)^2}{2b^3} - \frac{1}{b^3(bc-ad)(a+bx)} \right. \\
& 2a \left(-b(c+dx) \text{Log} \left[\frac{c}{d} + x \right]^2 + 2d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2d(a+bx) \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) - \\
& \left(a^2 \left(b(c+dx) (-2ad+b(c-dx)) \text{Log} \left[\frac{c}{d} + x \right]^2 - 2d^2(a+bx)^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \right. \right. \\
& \quad \left. \left. 2d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] \left(b(c+dx) + d(a+bx) \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) + 2d^2(a+bx)^2 \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) / \\
& \left(2b^3(bc-ad)^2(a+bx)^2 \right) + 2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{2 a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{a^2 \left(1 + 2 \text{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^3 (a + b x)^2} + \frac{2 a \left((-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x])\right)}{b^3 (b c - a d) (a + b x)} \right) + \\
& \frac{a^2 \left(\text{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x])}{(b c - a d)^2}\right)}{2 b^3 (a + b x)^2} - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^3} \Bigg) - \\
& 2 \left(-\frac{1}{b^3 (b c - a d) (a + b x)} a \left(d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) - \right. \\
& \quad \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \left((b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
& \left(a^2 \left(-d (-b c + a d) (a + b x) + (b c - a d)^2 \left(1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right) \text{Log}\left[\frac{c}{d} + x\right] + d^2 (a + b x)^2 \text{Log}[a + b x] - d^2 (a + b x)^2 \text{Log}[c + d x] + d (a + b x) \right. \right. \\
& \quad \left. \left. \left(d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 (b c - a d) \left(1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - 2 d (a + b x) \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right) \right) / \\
& \left(4 b^3 (b c - a d)^2 (a + b x)^2 \right) + \frac{1}{2 b^3} \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \right. \\
& \quad \left. 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) + \frac{\text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 \text{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b^3} \Bigg)
\end{aligned}$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{(a g + b g x)^5} dx$$

Optimal (type 3, 147 leaves, 3 steps):

$$-\frac{B^2 i^3 (c + d x)^4}{32 (b c - a d) g^5 (a + b x)^4} - \frac{B i^3 (c + d x)^4 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{8 (b c - a d) g^5 (a + b x)^4} - \frac{i^3 (c + d x)^4 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{4 (b c - a d) g^5 (a + b x)^4}$$

Result (type 3, 327 leaves):

$$\frac{1}{32 b^4 (b c - a d) g^5 (a + b x)^4}$$

$$i^3 \left(- (8 A^2 + 4 A B + B^2) (b c - a d)^4 + 4 (8 A^2 + 4 A B + B^2) d (-b c + a d)^3 (a + b x) - 6 (8 A^2 + 4 A B + B^2) d^2 (b c - a d)^2 (a + b x)^2 + \right.$$

$$4 (8 A^2 + 4 A B + B^2) d^3 (-b c + a d) (a + b x)^3 - 4 B (4 A + B) d^4 (a + b x)^4 \operatorname{Log}[a + b x] -$$

$$4 B (4 A + B) (b c - a d) \left((b c - a d)^3 + 4 d (b c - a d)^2 (a + b x) + 6 d^2 (b c - a d) (a + b x)^2 + 4 d^3 (a + b x)^3 \right) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] -$$

$$\left. 8 b^4 B^2 (c + d x)^4 \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 + 4 B (4 A + B) d^4 (a + b x)^4 \operatorname{Log}[c + d x] \right)$$

Problem 84: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 718 leaves, 25 steps):

$$\frac{b B^2 (b c - a d)^2 g^3 x}{3 d^3 i} + \frac{B^2 (b c - a d)^3 g^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]}{3 d^4 i} + \frac{7 B (b c - a d)^2 g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{3 d^3 i} -$$

$$\frac{b^2 B (b c - a d) g^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{3 d^4 i} + \frac{6 B (b c - a d)^3 g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{d^4 i} +$$

$$\frac{3 (b c - a d)^2 g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{d^3 i} - \frac{3 b^2 (b c - a d) g^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{2 d^4 i} +$$

$$\frac{b^3 g^3 (c + d x)^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{3 d^4 i} + \frac{(b c - a d)^3 g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{d^4 i} - \frac{2 B^2 (b c - a d)^3 g^3 \operatorname{Log}[c + d x]}{d^4 i} -$$

$$\frac{7 B (b c - a d)^3 g^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{3 d^4 i} + \frac{6 B^2 (b c - a d)^3 g^3 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i} +$$

$$\frac{2 B (b c - a d)^3 g^3 \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i} + \frac{7 B^2 (b c - a d)^3 g^3 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{3 d^4 i} - \frac{2 B^2 (b c - a d)^3 g^3 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i}$$

Result (type 4, 5057 leaves):

$$\frac{1}{12 d^4 i} g^3$$

$$\left(24 A b^3 B c^3 + 45 b^3 B^2 c^3 - 96 a A b^2 B c^2 d - 155 a b^2 B^2 c^2 d + 144 a^2 A b B c d^2 + 129 a^2 b B^2 c d^2 - 72 a^3 A B d^3 - 63 a^3 B^2 d^3 + 12 A^2 b^3 c^2 d x + 20 A b^3 B c^2 d x + \right.$$

$$\begin{aligned}
& 4 b^3 B^2 c^2 d x - 36 a A^2 b^2 c d^2 x - 48 a A b^2 B c d^2 x - 8 a b^2 B^2 c d^2 x + 36 a^2 A^2 b d^3 x + 28 a^2 A b B d^3 x + 4 a^2 b B^2 d^3 x - 6 A^2 b^3 c d^2 x^2 - 4 A b^3 B c d^2 x^2 + \\
& 18 a A^2 b^2 d^3 x^2 + 4 a A b^2 B d^3 x^2 + 4 A^2 b^3 d^3 x^3 - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 24 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 116 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 198 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 72 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 126 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] - 12 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 42 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 50 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 30 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 72 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 28 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] + 12 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 36 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 18 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 36 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 12 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 8 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^3 - 24 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 24 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^3 - 8 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + \\
& 12 a^2 A b B c d^2 \operatorname{Log}[a + b x] + 10 a^2 b B^2 c d^2 \operatorname{Log}[a + b x] - 28 a^3 A B d^3 \operatorname{Log}[a + b x] - 30 a^3 B^2 d^3 \operatorname{Log}[a + b x] - 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 28 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 28 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 96 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 144 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 72 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 A b^3 B c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 20 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 72 a A b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 48 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 72 a^2 A b B d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 28 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 A b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 4 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a A b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 8 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 24 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 72 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a^2 b B^2 c d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 28 a^3 B^2 d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
& 12 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 - 36 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 36 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 - 6 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 +
\end{aligned}$$

$$\begin{aligned}
& 18 a^2 b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 4 b^3 B^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 - 12 A^2 b^3 c^3 \operatorname{Log}[c+dx] - 20 A b^3 B c^3 \operatorname{Log}[c+dx] + \\
& 18 b^3 B^2 c^3 \operatorname{Log}[c+dx] + 36 a A^2 b^2 c^2 d \operatorname{Log}[c+dx] + 36 a A b^2 B c^2 d \operatorname{Log}[c+dx] - 74 a b^2 B^2 c^2 d \operatorname{Log}[c+dx] - 36 a^2 A^2 b c d^2 \operatorname{Log}[c+dx] + \\
& 44 a^2 b B^2 c d^2 \operatorname{Log}[c+dx] + 12 a^3 A^2 d^3 \operatorname{Log}[c+dx] + 24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - \\
& 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] + 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+dx] - 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+dx] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+dx] - \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+dx] + 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+dx] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] + 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+dx] - 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+dx] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+dx] - \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+dx] + 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+dx] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 24 a^3 A B d^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}[c+dx] - 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \operatorname{Log}[c+dx] + \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \operatorname{Log}[c+dx] - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \operatorname{Log}[c+dx] + 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \operatorname{Log}[c+dx] - \\
& 24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 44 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 132 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 132 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] +
\end{aligned}$$

$$\begin{aligned}
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 44 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 4 B (bc-ad)^3 \left(6 A + 11 B + 6 B \operatorname{Log}\left[\frac{c}{d} + x\right] + 6 B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 24 B^2 (bc-ad)^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \Big)
\end{aligned}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{ci + dix} dx$$

Optimal (type 4, 536 leaves, 15 steps):

$$\begin{aligned}
& \frac{B (b c - a d) g^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{d^2 i} - \frac{4 B (b c - a d)^2 g^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)}{d^3 i} - \\
& \frac{2 (b c - a d) g^2 (a + b x) \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{d^2 i} + \frac{b^2 g^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{2 d^3 i} - \frac{(b c - a d)^2 g^2 \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right] \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{d^3 i} + \\
& \frac{B^2 (b c - a d)^2 g^2 \operatorname{Log} [c + d x]}{d^3 i} + \frac{B (b c - a d)^2 g^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{d^3 i} - \frac{4 B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i} - \\
& \frac{2 B (b c - a d)^2 g^2 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i} - \frac{B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{d^3 i} + \frac{2 B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i}
\end{aligned}$$

Result (type 4, 2562 leaves):

$$\begin{aligned}
& \frac{1}{12 d^3 i} g^2 \left(-12 A^2 b d (b c - 2 a d) x + 6 A^2 b^2 d^2 x^2 + 12 A^2 (b c - a d)^2 \operatorname{Log} [c + d x] + \right. \\
& 12 A B \left(-2 b^2 c^2 + 2 a b c d - b^2 c d x + a b d^2 x + 2 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - a^2 d^2 \operatorname{Log} [a + b x] - 2 b^2 c d x \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + \right. \\
& b^2 d^2 x^2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + b^2 c^2 \operatorname{Log} [c + d x] + 2 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + 2 b^2 c^2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \operatorname{Log} [c + d x] - \\
& 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \left(a d + b c \operatorname{Log} [c + d x] - b c \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + 2 b^2 c^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \left. \right) - 12 a^2 A B d^2 \\
& \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \operatorname{Log} [c + d x] - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) - \\
& 24 a A B d \left(-2 d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\
& 2 b \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) (d x - c \operatorname{Log} [c + d x]) + 2 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \left. \right) + \\
& 4 a^2 B^2 d^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) + 3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 \operatorname{Log} [c + d x] + \right. \\
& 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) \left. \right) + \\
& 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - 6 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \left. \right) +
\end{aligned}$$

$$\begin{aligned}
& 8 a B^2 d \left(3 d (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 b (c + d x) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) + \right. \\
& 3 b \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 (d x - c \operatorname{Log} [c + d x]) - 6 \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log} [c + d x] + \right. \\
& \left. \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) + d (a + b x) \operatorname{Log} \left[\frac{c}{d} + x \right] + (b c - a d) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \left(-2 d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \right. \\
& \left. b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) - \\
& 3 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& 3 b c \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \right) - \\
& B^2 \left(12 b c d (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) + 3 d^2 (a + b x) \left(7 a - b x + (-6 a + 2 b x) \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 (a - b x) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) - \right. \\
& 4 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 12 b^2 c (c + d x) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) + \\
& 3 b^2 (c + d x) \left(7 c - d x + (-6 c + 2 d x) \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 (c - d x) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) - 6 b^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 \\
& (d x (-2 c + d x) + 2 c^2 \operatorname{Log} [c + d x]) + 6 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \left(-4 b c d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + \right. \\
& 4 b^2 c (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + d^2 \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \operatorname{Log} [a + b x] \right) + \\
& \left. b^2 \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \operatorname{Log} [c + d x] \right) + 4 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) - \\
& 12 b^2 c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] \right) - \\
& 6 \left(2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \operatorname{Log} \left[\frac{c}{d} + x \right] + b^2 d^2 x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - a^2 d^2 \operatorname{Log} [a + b x] - b^2 c^2 \operatorname{Log} [c + d x] - \right. \\
& 2 a b c d \operatorname{Log} [c + d x] - \operatorname{Log} \left[\frac{a}{b} + x \right] \left(b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \operatorname{Log} \left[\frac{c}{d} + x \right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + \\
& \left. 2 (b^2 c^2 - a^2 d^2) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 4 b c \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log} [c + d x] + \right. \right.
\end{aligned}$$

$$\begin{aligned} & \text{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \\ & 2b^2c^2 \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \end{aligned}$$

Problem 86: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2}{ci + dix} dx$$

Optimal (type 4, 283 leaves, 9 steps):

$$\begin{aligned} & \frac{2B(bc-ad)g \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)}{d^2i} + \frac{g(a+bx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2}{di} + \frac{(bc-ad)g \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2}{d^2i} + \\ & \frac{2B^2(bc-ad)g \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^2i} + \frac{2B(bc-ad)g \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^2i} - \frac{2B^2(bc-ad)g \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^2i} \end{aligned}$$

Result (type 4, 1209 leaves):

$$\begin{aligned}
& \frac{1}{3 d^2 i} g \left(3 A^2 b d x - 3 A^2 (b c - a d) \operatorname{Log}[c + d x] - 3 a A B d \right. \\
& \left. \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \operatorname{Log}[c + d x] - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) - \right. \\
& 3 A B \left(-2 d (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\
& \left. 2 b \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) (d x - c \operatorname{Log}[c + d x]) + 2 b c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) + \\
& a B^2 d \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) + 3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 \operatorname{Log}[c + d x] + \right. \\
& \left. 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \right. \\
& \left. 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) \right) + \\
& \left. 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) + \\
& B^2 \left(3 d (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 b (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + \right. \\
& \left. 3 b \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)^2 (d x - c \operatorname{Log}[c + d x]) - 6 \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& \left. 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \left(-2 d (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - \right. \\
& \left. b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) \right) - \\
& 3 b c \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& \left. 3 b c \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 87: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{cix + dix} dx$$

Optimal (type 4, 127 leaves, 4 steps):

$$\frac{\operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{di} - \frac{2B \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{di} + \frac{2B^2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{b(c+dx)} \right]}{di}$$

Result (type 4, 458 leaves):

$$\begin{aligned} & \frac{1}{3di} \left(3A^2 \operatorname{Log}[c+dx] - \right. \\ & 3AB \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \operatorname{Log}[c+dx] - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \\ & B^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) + \right. \\ & 3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2 \operatorname{Log}[c+dx] + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + \\ & 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \\ & \left. 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right) \end{aligned}$$

Problem 92: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx)^3 \left(A + B \operatorname{Log} \left[\frac{e^{(a+bx)}}{c+dx} \right] \right)^2}{(cix + dix)^2} dx$$

Optimal (type 4, 722 leaves, 18 steps):

$$\begin{aligned}
 & \frac{2AB(bc-ad)^2g^3(a+bx)}{d^3i^2(c+dx)} - \frac{2B^2(bc-ad)^2g^3(a+bx)}{d^3i^2(c+dx)} + \frac{2B^2(bc-ad)^2g^3(a+bx)\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]}{d^3i^2(c+dx)} - \\
 & \frac{bB(bc-ad)g^3(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{d^3i^2} - \frac{6bB(bc-ad)^2g^3\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{d^4i^2} - \\
 & \frac{3b(bc-ad)g^3(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^3i^2} - \frac{(bc-ad)^2g^3(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^3i^2(c+dx)} + \\
 & \frac{b^3g^3(c+dx)^2\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{2d^4i^2} - \frac{3b(bc-ad)^2g^3\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^4i^2} + \frac{bB^2(bc-ad)^2g^3\operatorname{Log}[c+dx]}{d^4i^2} + \\
 & \frac{bB(bc-ad)^2g^3\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)\operatorname{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{d^4i^2} - \frac{6bB^2(bc-ad)^2g^3\operatorname{PolyLog}\left[2,\frac{d(a+bx)}{b(c+dx)}\right]}{d^4i^2} - \\
 & \frac{6bB(bc-ad)^2g^3\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)\operatorname{PolyLog}\left[2,\frac{d(a+bx)}{b(c+dx)}\right]}{d^4i^2} - \frac{bB^2(bc-ad)^2g^3\operatorname{PolyLog}\left[2,\frac{b(c+dx)}{d(a+bx)}\right]}{d^4i^2} + \frac{6bB^2(bc-ad)^2g^3\operatorname{PolyLog}\left[3,\frac{d(a+bx)}{b(c+dx)}\right]}{d^4i^2}
 \end{aligned}$$

Result (type 4, 4743 leaves):

$$\begin{aligned}
 & -\frac{A^2b^2(2bc-3ad)g^3x}{d^3i^2} + \frac{A^2b^3g^3x^2}{2d^2i^2} + \frac{A^2b^3c^3g^3-3aA^2b^2c^2dg^3+3a^2A^2bcd^2g^3-a^3A^2d^3g^3}{d^4i^2(c+dx)} + \\
 & \frac{a^3B^2g^3(a+bx)\left(2-2\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]+\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2\right)}{(bc-ad)i^2(c+dx)} + \frac{3(A^2b^3c^2g^3-2aA^2b^2c^2dg^3+a^2A^2bd^2g^3)\operatorname{Log}[c+dx]}{d^4i^2} + \\
 & \frac{2a^3ABg^3\left(\frac{\left(\frac{c}{d}+x\right)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{(c+dx)^2\operatorname{Log}\left[\frac{c}{d}+x\right]} + \frac{\frac{d\left(\frac{a}{b}+x\right)\operatorname{Log}\left[\frac{a}{b}+x\right]}{\left(-c+\frac{ad}{b}\right)^2\left(1-\frac{d\left(\frac{a}{b}+x\right)}{-c+\frac{ad}{b}}\right)} + \frac{\operatorname{Log}\left[1-\frac{d\left(\frac{a}{b}+x\right)}{-c+\frac{ad}{b}}\right]}{-c+\frac{ad}{b}} - \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{ae}{c+dx}+\frac{bex}{c+dx}\right]}{d(c+dx)}\right)}{i^2} + \\
 & \frac{1}{i^2}2Ab^3Bg^3\left(-\frac{2c\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^3} + \frac{2c\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3} - \frac{3c^2\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^4} - \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{c^3 \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^4 (c + dx)} + \frac{-\frac{1}{2} b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \operatorname{Log}[a+bx]}{b^3} \right) + \frac{1}{2} x^2 \operatorname{Log} \left[\frac{a+bx}{b} \right]}{d^2} - \frac{c^3 \left(-\frac{\operatorname{Log} \left[\frac{a+x}{b} \right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} \right)}{d^3} \\
& - \frac{\frac{1}{2} d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \operatorname{Log}[c+dx]}{d^3} \right) + \frac{1}{2} x^2 \operatorname{Log} \left[\frac{c+dx}{d} \right]}{d^2} + \frac{\left(-4cdx + d^2 x^2 + \frac{2c^3}{c+dx} + 6c^2 \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)}{2d^4} + \\
& \left. \frac{3c^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d^4} \right) + \frac{1}{i^2} \\
6 a A b^2 B g^3 & \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{d^2} - \frac{\left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^2} + \frac{c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{d^3} + \frac{c^2 \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^3 (c + dx)} + \frac{c^2 \left(-\frac{\operatorname{Log} \left[\frac{a+x}{b} \right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} \right)}{d^2} \right) + \\
& \left. \frac{\left(dx - \frac{c^2}{c+dx} - 2c \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)}{d^3} - \frac{2c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d^3} \right) + \\
\frac{1}{i^2} 6 a^2 A b B g^3 & \left(-\frac{\operatorname{Log} \left[\frac{c}{d} + x \right]^2}{2d^2} - \frac{c \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^2 (c + dx)} - \frac{c \left(-\frac{\operatorname{Log} \left[\frac{a+x}{b} \right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} \right)}{d} \right) + \\
& \left. \frac{\left(\frac{c}{c+dx} + \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)}{d^2} + \frac{\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right]}{d^2} \right) + \\
\frac{1}{i^2} b^3 B^2 g^3 & \left(-\frac{2c(a+bx) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{bd^3} + \frac{(a+bx) \left(-7a+bx + (6a-2bx) \operatorname{Log} \left[\frac{a}{b} + x \right] - 2(a-bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4b^2 d^2} \right) + \\
& \frac{c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^3}{d^4} - \frac{2c(c+dx) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^4} + \frac{c^3 \left(2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^4 (c + dx)} +
\end{aligned}$$

$$\begin{aligned}
& \frac{(c+dx) \left(-7c+dx + (6c-2dx) \operatorname{Log}\left[\frac{c}{d}+x\right] - 2(c-dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{4d^4} + \\
& \frac{\left(-4cdx + d^2x^2 + \frac{2c^3}{c+dx} + 6c^2 \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2d^4} - \frac{1}{d^4(-bc+ad)(c+dx)} \\
& c^3 \left(-d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) \left(-\frac{2c\left(\frac{a}{b}+x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^3} + \frac{2c\left(\frac{c}{d}+x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3} - \right. \\
& \left. \frac{3c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^4} - \frac{c^3 \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^4(c+dx)} + \frac{-\frac{1}{2}b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \operatorname{Log}[a+bx]}{b^3}\right) + \frac{1}{2}x^2 \operatorname{Log}\left[\frac{a+bx}{b}\right]}{d^2} - \frac{c^3 \left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d^3} - \right. \\
& \left. - \frac{\frac{1}{2}d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \operatorname{Log}[c+dx]}{d^3}\right) + \frac{1}{2}x^2 \operatorname{Log}\left[\frac{c+dx}{d}\right]}{d^2} + \frac{3c^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^4} \right) + \\
& \frac{3c^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^4} - 2 \left(-\frac{1}{bd^4} 2c \left(ad + 2bdx - bdx \operatorname{Log}\left[\frac{c}{d}+x\right] - bc \right. \right. \\
& \left. \left. \operatorname{Log}[c+dx] + \operatorname{Log}\left[\frac{a}{b}+x\right] \left(-d(a+bx) + d(a+bx) \operatorname{Log}\left[\frac{c}{d}+x\right] + (bc-ad) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& \frac{1}{4b^2d^4} \left(-2abcd - 3b^2cdx - 3abd^2x + b^2d^2x^2 + 2abd^2x \operatorname{Log}\left[\frac{c}{d}+x\right] - b^2d^2x^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + a^2d^2 \operatorname{Log}[a+bx] + b^2c^2 \operatorname{Log}[c+dx] + \right. \\
& \left. 2abcd \operatorname{Log}[c+dx] + \operatorname{Log}\left[\frac{a}{b}+x\right] \left(bd(2ac+bx(2c-dx)) - 2d^2(a^2-b^2x^2) \operatorname{Log}\left[\frac{c}{d}+x\right] + (-2b^2c^2+2a^2d^2) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \right. \\
& \left. (-2b^2c^2+2a^2d^2) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \left(c^3 \left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+bx] - \right. \right. \right. \\
& \left. \left. \left. 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / (2d^4(-bc+ad)(c+dx)) + \frac{1}{2d^4}
\end{aligned}$$

$$\begin{aligned}
& \left. 3 c^2 \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) - 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] + 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right) \right) + \\
& \frac{1}{i^2} 3 a b^2 B^2 g^3 \left(\frac{(a+bx) \left(2 - 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b d^2} - \frac{2 c \text{Log} \left[\frac{c}{d} + x \right]^3}{3 d^3} + \frac{(c+dx) \left(2 - 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^3} - \right. \\
& \frac{c^2 \left(2 + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^3 (c+dx)} + \frac{\left(dx - \frac{c^2}{c+dx} - 2 c \text{Log} [c+dx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)^2}{d^3} + \\
& \left. \frac{1}{d^3 (-bc+ad) (c+dx)} c^2 \left(-d(a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 b(c+dx) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 b(c+dx) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \right. \\
& 2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{d^2} - \frac{\left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^2} + \frac{c \text{Log} \left[\frac{c}{d} + x \right]^2}{d^3} + \right. \\
& \left. \frac{c^2 \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^3 (c+dx)} + \frac{c^2 \left(-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d(c+dx)} - \frac{b \text{Log} [a+bx]}{d(-bc+ad)} + \frac{b \text{Log} [c+dx]}{d(-bc+ad)} \right)}{d^2} - \frac{2 c \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d^3} \right) - \\
& \frac{2 c \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d^3} - \\
& 2 \left(\frac{1}{b d^3} \left(a d + 2 b d x - b d x \text{Log} \left[\frac{c}{d} + x \right] - b c \text{Log} [c+dx] + \text{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) + d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + \right. \\
& (bc-ad) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \left(c^2 \left(2 (bc-ad) \text{Log} \left[\frac{a}{b} + x \right] \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + b(c+dx) \left(\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \text{Log} [a+bx] - \right. \right. \right. \\
& \left. \left. 2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} [c+dx] \right) - 2 b(c+dx) \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) / \left(2 d^3 (-bc+ad) (c+dx) \right) - \frac{1}{d^3} \\
& \left. c \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) - 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] + 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{i^2} 3 a^2 b B^2 g^3 \left(\frac{\text{Log}\left[\frac{c}{d} + x\right]^3}{3 d^2} + \frac{c \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^2 (c + d x)} + \frac{\left(\frac{-c}{c + d x} + \text{Log}[c + d x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)^2}{d^2} \right. \\
& \frac{1}{d^2 (-b c + a d) (c + d x)} c \left(-d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]\right) \\
& 2 \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) \\
& \left. \left(-\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c + d x)} - \frac{c \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)}\right)}{d} + \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^2}\right) \right) + \\
& \frac{\text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} - \\
& 2 \left(-\left(\left(c \left(2 (b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + b (c + d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a + b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \text{Log}[c + d x]\right) + 2 b (c + d x) \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]\right)\right) / \left(2 d^2 (-b c + a d) (c + d x)\right) + \frac{1}{2 d^2} \right. \\
& \left. \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right]\right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]\right)\right) \right)
\end{aligned}$$

Problem 93: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 469 leaves, 12 steps):

$$\begin{aligned}
& - \frac{2AB(bc-ad)g^2(a+bx)}{d^2i^2(c+dx)} + \frac{2B^2(bc-ad)g^2(a+bx)}{d^2i^2(c+dx)} - \frac{2B^2(bc-ad)g^2(a+bx)\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]}{d^2i^2(c+dx)} + \\
& \frac{2bB(bc-ad)g^2\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{d^3i^2} + \frac{bg^2(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^2i^2} + \frac{(bc-ad)g^2(a+bx)\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^2i^2(c+dx)} + \\
& \frac{2b(bc-ad)g^2\operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{d^3i^2} + \frac{2bB^2(bc-ad)g^2\operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3i^2} + \\
& \frac{4bB(bc-ad)g^2\left(A+B\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)\operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3i^2} - \frac{4bB^2(bc-ad)g^2\operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3i^2}
\end{aligned}$$

Result (type 4, 2704 leaves):

$$\begin{aligned}
& \frac{A^2b^2g^2x}{d^2i^2} + \frac{-A^2b^2c^2g^2 + 2aA^2bcdg^2 - a^2A^2d^2g^2}{d^3i^2(c+dx)} + \frac{a^2B^2g^2(a+bx)\left(2 - 2\operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right] + \operatorname{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2\right)}{(bc-ad)i^2(c+dx)} + \\
& \frac{2a^2ABg^2\left(\frac{\left(\frac{c}{d}+x\right)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{(c+dx)^2\operatorname{Log}\left[\frac{c}{d}+x\right]} + \frac{\frac{d\left(\frac{a}{b}+x\right)\operatorname{Log}\left[\frac{a}{b}+x\right]\operatorname{Log}\left[1-\frac{d\left(\frac{a}{b}+x\right)}{-c-\frac{ad}{b}}\right]}{\left(-c-\frac{ad}{b}\right)^2\left(1-\frac{d\left(\frac{a}{b}+x\right)}{-c-\frac{ad}{b}}\right)} - \frac{\operatorname{Log}\left[1-\frac{d\left(\frac{a}{b}+x\right)}{-c-\frac{ad}{b}}\right]}{-c-\frac{ad}{b}} - \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{ae}{c+dx}+\frac{bex}{c+dx}\right]}{d(c+dx)}\right)}{i^2} + \frac{1}{i^2} \\
& \frac{2(-A^2b^2c^2g^2 + aA^2bdg^2)\operatorname{Log}[c+dx]}{d^3i^2} + \frac{2A^2B^2g^2\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^2} - \frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^2} + \frac{c\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^3} + \frac{c^2\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3(c+dx)} + \frac{c^2\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b\operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b\operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2}\right)}{d^3} + \\
& \frac{\left(dx - \frac{c^2}{c+dx} - 2c\operatorname{Log}[c+dx]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right) - 2c\left(\operatorname{Log}\left[\frac{a}{b}+x\right]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} + \\
& \frac{1}{i^2} 4aABg^2\left(-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^2} - \frac{c\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^2(c+dx)} - \frac{c\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b\operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b\operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d}\right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{\left(\frac{c}{c+dx} + \text{Log}[c+dx]\right) \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right)}{d^2} + \frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2} \right\} + \\
& \frac{1}{i^2} b^2 B^2 g^2 \left(\frac{(a+bx) \left(2 - 2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{a}{b}+x\right]^2\right)}{b d^2} - \frac{2 c \text{Log}\left[\frac{c}{d}+x\right]^3}{3 d^3} + \frac{(c+dx) \left(2 - 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^3} - \right. \\
& \frac{c^2 \left(2 + 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^3 (c+dx)} + \frac{\left(dx - \frac{c^2}{c+dx} - 2 c \text{Log}[c+dx]\right) \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right)^2}{d^3} + \\
& \left. \frac{1}{d^3 (-bc+ad) (c+dx)} c^2 \left(-d(a+bx) \text{Log}\left[\frac{a}{b}+x\right]^2 + 2 b (c+dx) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 b (c+dx) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) \right\} + \\
& 2 \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right) \left(\frac{\left(\frac{a}{b}+x\right) \left(-1 + \text{Log}\left[\frac{a}{b}+x\right]\right)}{d^2} - \frac{\left(\frac{c}{d}+x\right) \left(-1 + \text{Log}\left[\frac{c}{d}+x\right]\right)}{d^2} + \frac{c \text{Log}\left[\frac{c}{d}+x\right]^2}{d^3} + \right. \\
& \left. \frac{c^2 \left(1 + \text{Log}\left[\frac{c}{d}+x\right]\right)}{d^3 (c+dx)} + \frac{c^2 \left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \text{Log}[a+bx]}{d(-bc+ad)} + \frac{b \text{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} - \frac{2 c \left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} \right\} - \\
& \frac{2 c \left(\text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} - \\
& 2 \left(\frac{1}{b d^3} \left(a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d}+x\right] - b c \text{Log}[c+dx] + \text{Log}\left[\frac{a}{b}+x\right] \left(-d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d}+x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) \right) + \right. \\
& \left(b c - a d \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \left(c^2 \left(2 (bc-ad) \text{Log}\left[\frac{a}{b}+x\right] \left(1 + \text{Log}\left[\frac{c}{d}+x\right]\right) + b (c+dx) \left(\text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+bx] - \right. \right. \right. \\
& \left. \left. 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}[c+dx]\right) - 2 b (c+dx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \left(2 d^3 (-bc+ad) (c+dx) \right) - \frac{1}{d^3} \\
& \left. c \left(\text{Log}\left[\frac{c}{d}+x\right]^2 \left(\text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right\} +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{i^2} 2 a b B^2 g^2 \left(\frac{\text{Log}\left[\frac{c}{d} + x\right]^3}{3 d^2} + \frac{c \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^2 (c + d x)} + \frac{\left(\frac{c}{c + d x} + \text{Log}[c + d x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)^2}{d^2} \right. \\
& \frac{1}{d^2 (-b c + a d) (c + d x)} c \left(-d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \\
& 2 \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) \\
& \left. \left(-\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c + d x)} - \frac{c \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)}\right)}{d} + \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} \right) \right) + \\
& \frac{\text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} - \\
& 2 \left(-\left(\left(c \left(2 (b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a + b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \text{Log}[c + d x] \right) \right) \right. \right. \\
& \left. \left. 2 b (c + d x) \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left(2 d^2 (-b c + a d) (c + d x) \right) + \frac{1}{2 d^2} \\
& \left. \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x) \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 261 leaves, 9 steps):

$$\begin{aligned}
& \frac{2 A B g (a + b x)}{d i^2 (c + d x)} - \frac{2 B^2 g (a + b x)}{d i^2 (c + d x)} + \frac{2 B^2 g (a + b x) \text{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{d i^2 (c + d x)} - \frac{g (a + b x) \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{d i^2 (c + d x)} - \\
& \frac{b g \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{d^2 i^2} - \frac{2 b B g \left(A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^2 i^2} + \frac{2 b B^2 g \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{d^2 i^2}
\end{aligned}$$

Result (type 4, 1145 leaves):

$$\frac{1}{i^2} g \left(\frac{A^2 (b c - a d)}{d^2 (c + d x)} + \frac{a B^2 (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right]^2 \right)}{(b c - a d) (c + d x)} + \frac{A^2 b \operatorname{Log} [c + d x]}{d^2} - \frac{1}{d (-b c + a d) (c + d x)} \right.$$

$$2 a A B \left(b c - a d + b (c + d x) \operatorname{Log} \left[\frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] - b c \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + \frac{1}{d^2}$$

$$A b B \left(-\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + d x] + 2 \left(-\frac{c}{c + d x} + \frac{b c \operatorname{Log} [a + b x]}{-b c + a d} + \frac{b c \operatorname{Log} [c + d x]}{b c - a d} - \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c + d x] + \right.$$

$$\left. \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \left(\frac{c}{c + d x} + \operatorname{Log} [c + d x] \right) + \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] +$$

$$\frac{1}{3 d^2 (b c - a d) (c + d x)} b B^2 \left((b c - a d) (c + d x) \operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 c (b c - a d) \left(2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) + \right.$$

$$3 (b c - a d) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2 (c + (c + d x) \operatorname{Log} [c + d x]) +$$

$$3 c \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 b (c + d x) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + 6 b c (c + d x) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] +$$

$$3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right) \left((b c - a d) (c + d x) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 c (b c - a d) \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + 2 c \left((-b c + a d) \operatorname{Log} \left[\frac{a}{b} + \right. \right.$$

$$\left. \left. x \right] + b (c + d x) (\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x]) \right) - 2 (b c - a d) (c + d x) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) +$$

$$3 (b c - a d) (c + d x) \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] \right) -$$

$$3 \left(c \left(2 (b c - a d) \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b (c + d x) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \operatorname{Log} [a + b x] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{Log} [c + d x] \right) - \right.$$

$$\left. 2 b (c + d x) \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + (b c - a d) (c + d x)$$

$$\left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \right) \right)$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[\frac{e (a + b x)}{c + d x} \right] \right)^2}{(c i + d i x)^3} dx$$

Optimal (type 4, 635 leaves, 14 steps):

$$\begin{aligned}
 & \frac{B^2 (bc - ad) g^3 (a + bx)^2}{4 d^2 i^3 (c + dx)^2} - \frac{4 A b B (bc - ad) g^3 (a + bx)}{d^3 i^3 (c + dx)} + \frac{4 b B^2 (bc - ad) g^3 (a + bx)}{d^3 i^3 (c + dx)} - \frac{4 b B^2 (bc - ad) g^3 (a + bx) \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]}{d^3 i^3 (c + dx)} \\
 & \frac{B (bc - ad) g^3 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)}{2 d^2 i^3 (c + dx)^2} + \frac{2 b^2 B (bc - ad) g^3 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)}{d^4 i^3} + \\
 & \frac{b^2 g^3 (a + bx) \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)^2}{d^3 i^3} + \frac{(bc - ad) g^3 (a + bx)^2 \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)^2}{2 d^2 i^3 (c + dx)^2} + \frac{2 b (bc - ad) g^3 (a + bx) \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)^2}{d^3 i^3 (c + dx)} + \\
 & \frac{3 b^2 (bc - ad) g^3 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right)^2}{d^4 i^3} + \frac{2 b^2 B^2 (bc - ad) g^3 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^3} + \\
 & \frac{6 b^2 B (bc - ad) g^3 \left(A + B \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^3} - \frac{6 b^2 B^2 (bc - ad) g^3 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^3}
 \end{aligned}$$

Result (type 4, 5648 leaves):

$$\begin{aligned}
 & \frac{A^2 b^3 g^3 x}{d^3 i^3} - \frac{A^2 (-b^3 c^3 + 3 a b^2 c^2 d - 3 a^2 b c d^2 + a^3 d^3) g^3}{2 d^4 i^3 (c + dx)^2} - \frac{3 (A^2 b^3 c^2 g^3 - 2 a A^2 b^2 c d g^3 + a^2 A^2 b d^2 g^3)}{d^4 i^3 (c + dx)} + \frac{3 (-A^2 b^3 c g^3 + a A^2 b^2 d g^3) \operatorname{Log}[c + dx]}{d^4 i^3} + \\
 & \left(a^3 B^2 g^3 \left(-7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c + dx)^2 \operatorname{Log}[a + bx] + 2 (bc - ad) (3 bc - ad + 2 b d x) \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right] - \right. \right. \\
 & \quad \left. \left. 2 d (a + bx) (-2 bc + ad - b d x) \operatorname{Log}\left[\frac{e^{-(a+bx)}}{c+dx}\right]^2 + 6 b^2 c^2 \operatorname{Log}[c + dx] + 12 b^2 c d x \operatorname{Log}[c + dx] + 6 b^2 d^2 x^2 \operatorname{Log}[c + dx] \right) \right) / \\
 & \left(4 d (bc - ad)^2 i^3 (c + dx)^2 + \frac{1}{i^3} 2 a^3 A B g^3 \frac{\left(\frac{c}{d} + x\right) \left(2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{8 (c + dx)^3 \operatorname{Log}\left[\frac{c}{d} + x\right]} + \right.
 \end{aligned}$$

$$\left. \begin{aligned}
& \frac{\frac{d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} - \left(\frac{d^2 \left(\frac{a}{b} + x\right)^2}{\left(-c + \frac{ad}{b}\right)^4 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)^2} + \frac{2 d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} \right) \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}} \right]}{\left(-c + \frac{ad}{b}\right)^2}}{2 d} - \frac{-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{-ae}{c+dx} + \frac{bex}{c+dx} \right]}{2 d (c + dx)^2} \right. + \\
& \frac{1}{i^3} 6 a^2 A b B g^3 \left(\frac{1 + \text{Log} \left[\frac{c}{d} + x \right]}{d^2 (c + dx)} - \frac{c \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^2 (c + dx)^2} + \frac{-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + dx)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)}}{d} - \right. \\
& \left. \frac{c \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^2 (c + dx)^2} - \frac{(c + 2 dx) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{-ae}{c+dx} + \frac{bex}{c+dx} \right] \right)}{2 d^2 (c + dx)^2} \right) + \\
& \frac{1}{i^3} 2 A b^3 B g^3 \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right]\right)}{d^3} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right]\right)}{d^3} + \frac{3 c \text{Log} \left[\frac{c}{d} + x \right]^2}{2 d^4} + \frac{3 c^2 \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^4 (c + dx)} - \frac{c^3 \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^4 (c + dx)^2} + \right. \\
& \left. \frac{3 c^2 \left(-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + dx)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)} \right)}{d^3} - \frac{c^3 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^4 (c + dx)^2} - \right. \\
& \left. \frac{\left(-2 dx + \frac{c^2 (5c+6dx)}{(c+dx)^2} + 6 c \text{Log} [c + dx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{-ae}{c+dx} + \frac{bex}{c+dx} \right] \right)}{2 d^4} - \frac{3 c \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d (a+bx)}{-bc+ad} \right] \right)}{d^4} \right) + \\
& \frac{1}{i^3} 6 a A b^2 B g^3 \left(-\frac{\text{Log} \left[\frac{c}{d} + x \right]^2}{2 d^3} - \frac{2 c \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^3 (c + dx)} + \frac{c^2 \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^3 (c + dx)^2} - \frac{2 c \left(-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + dx)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)} \right)}{d^2} + \right. \\
& \left. \frac{c^2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^3 (c + dx)^2} \right) +
\end{aligned} \right.$$

$$\left. \frac{\left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) + \frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3}}{2d^3} \right) +$$

$$\frac{1}{i^3} 3a^2 b B^2 g^3 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^2(c+dx)} + \frac{c(1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2)}{4d^2(c+dx)^2} +
\right.$$

$$2 \left(\frac{1 + \operatorname{Log}\left[\frac{c}{d}+x\right]}{d^2(c+dx)} - \frac{c(1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right])}{4d^2(c+dx)^2} + \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} - \frac{c \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx) \operatorname{Log}[a+bx] - b(c+dx) \operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{2d^2(c+dx)^2} \right)$$

$$\left. \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) - \frac{(c+2dx) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2d^2(c+dx)^2} +
\right.$$

$$\left. \frac{-d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2(-bc+ad)(c+dx)} +
\right.$$

$$\left. \left(c \left(d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \right.$$

$$\left. \left. \left(d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \left(2d^2(bc-ad)^2(c+dx)^2 \right) -$$

$$2 \left(\left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - \right. \right.$$

$$\left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) / \left(2d^2(-bc+ad)(c+dx) \right) + \left(c \left(-b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \right.$$

$$\left. \left. \left(1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - b^2(c+dx)^2 \operatorname{Log}[a+bx] + b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(bc-ad) \right. \right. \right.$$

$$\left. \left. \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - 2b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) / \left(4d^2(bc-ad)^2(c+dx)^2 \right) \right) +$$

$$\frac{1}{i^3} b^3 B^2 g^3 \left(\frac{(a+bx) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{bd^3} - \frac{c \operatorname{Log}\left[\frac{c}{d}+x\right]^3}{d^4} + \frac{(c+dx) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^4} -
\right.$$

$$\begin{aligned}
& \frac{3c^2 \left(2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^4 (c + dx)} + \frac{c^3 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{4d^4 (c + dx)^2} - \\
& \frac{\left(-2dx + \frac{c^2(5c+6dx)}{(c+dx)^2} + 6c \operatorname{Log}[c + dx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c+dx} + \frac{bex}{c+dx} \right] \right)^2}{2d^4} + \frac{1}{d^4 (-bc + ad) (c + dx)} \\
& 3c^2 \left(-d(a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2b(c + dx) \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + 2b(c + dx) \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) + \\
& \left(c^3 \left(d(a + bx) (ad - b(2c + dx)) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2b^2(c + dx)^2 \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + 2b(c + dx) \operatorname{Log} \left[\frac{a}{b} + x \right] \right. \right. \\
& \quad \left. \left. \left(d(a + bx) + b(c + dx) \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] \right) + 2b^2(c + dx)^2 \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) \right) / \left(2d^4 (bc - ad)^2 (c + dx)^2 \right) + \\
& 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{ae}{c + dx} + \frac{bex}{c + dx} \right] \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{d^3} - \frac{\left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^3} + \right. \\
& \frac{3c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{2d^4} + \frac{3c^2 \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{d^4 (c + dx)} - \frac{c^3 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{4d^4 (c + dx)^2} + \frac{3c^2 \left(-\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]}{d(c + dx)} - \frac{b \operatorname{Log}[a + bx]}{d(-bc + ad)} + \frac{b \operatorname{Log}[c + dx]}{d(-bc + ad)} \right)}{d^3} - \\
& \left. \frac{c^3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \frac{b(c + dx)(bc - ad + b(c + dx) \operatorname{Log}[a + bx] - b(c + dx) \operatorname{Log}[c + dx])}{(bc - ad)^2} \right)}{2d^4 (c + dx)^2} - \frac{3c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right)}{d^4} \right) - \\
& \frac{3c \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d(a + bx)}{-bc + ad} \right] \right)}{d^4} - \\
& 2 \left(\frac{1}{bd^4} \left(ad + 2bdx - bdx \operatorname{Log} \left[\frac{c}{d} + x \right] - bc \operatorname{Log}[c + dx] + \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d(a + bx) + d(a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] + (bc - ad) \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] \right) + \right. \right. \\
& \quad \left. \left(bc - ad \right) \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) + \left(3c^2 \left(2(bc - ad) \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + \right. \right. \\
& \quad \left. \left. b(c + dx) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \operatorname{Log}[a + bx] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2 \operatorname{Log}[c + dx] \right) - 2b(c + dx) \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] \right) \right) / \\
& \left(2d^4 (-bc + ad) (c + dx) \right) + \left(c^3 \left(-b(bc - ad) (c + dx) + (bc - ad)^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 (c + dx)^2 \operatorname{Log}[a + bx] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& b^2 (c + dx)^2 \operatorname{Log}[c + dx] + b (c + dx) \left(b (c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 (bc - ad) \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - \right. \\
& \quad \left. 2 b (c + dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \Big/ \left(4 d^4 (bc - ad)^2 (c + dx)^2 \right) - \frac{1}{2 d^4} \\
& \quad \left. 3 c \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \Bigg) + \\
& \frac{1}{i^3} 3 a b^2 B^2 g^3 \left(\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \frac{2 c \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^3 (c + dx)} - \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{4 d^3 (c + dx)^2} + \right. \\
& \quad \left. \frac{\left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c + dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2 d^3} - \frac{1}{d^3 (-bc + ad) (c + dx)} \right. \\
& \quad \left. 2 c \left(-d (a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 b (c + dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
& \quad \left(c^2 \left(d (a + bx) (ad - b(2c + dx)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \\
& \quad \left. \left. 2 b (c + dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(d (a + bx) + b (c + dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2 b^2 (c + dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \Big/ \\
& \quad \left(2 d^3 (bc - ad)^2 (c + dx)^2 \right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) \\
& \quad \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^3} - \frac{2 c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{d^3 (c + dx)} + \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{4 d^3 (c + dx)^2} - \frac{2 c \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} \right)}{d^2} + \right. \\
& \quad \left. \frac{c^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{2 d^3 (c + dx)^2} + \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) \Bigg) + \\
& \frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]}{d^3}
\end{aligned}$$

$$\begin{aligned}
& 2 \left(-\frac{1}{d^3 (-bc + ad) (c + dx)} c \left(2 (bc - ad) \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + \right. \\
& \quad \left. b (c + dx) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \operatorname{Log} [a + bx] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + bx)}{-bc + ad} \right] + 2 \operatorname{Log} [c + dx] \right) - 2 b (c + dx) \operatorname{PolyLog} \left[2, \frac{b (c + dx)}{bc - ad} \right] \right) - \\
& \left(c^2 \left(-b (bc - ad) (c + dx) + (bc - ad)^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b^2 (c + dx)^2 \operatorname{Log} [a + bx] + b^2 (c + dx)^2 \operatorname{Log} [c + dx] + b (c + dx) \right. \right. \\
& \quad \left. \left. \left(b (c + dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 (bc - ad) \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 2 b (c + dx) \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + bx)}{-bc + ad} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + dx)}{bc - ad} \right] \right) \right) \right) \right) / \\
& \left(4 d^3 (bc - ad)^2 (c + dx)^2 \right) + \frac{1}{2 d^3} \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d (a + bx)}{-bc + ad} \right] \right) - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + dx)}{bc - ad} \right] + \right. \\
& \quad \left. 2 \operatorname{PolyLog} \left[3, \frac{b (c + dx)}{bc - ad} \right] \right) \Bigg)
\end{aligned}$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx)^2 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{(ci + dix)^3} dx$$

Optimal (type 4, 410 leaves, 11 steps):

$$\begin{aligned}
& -\frac{B^2 g^2 (a + bx)^2}{4 d i^3 (c + dx)^2} + \frac{2 A b B g^2 (a + bx)}{d^2 i^3 (c + dx)} - \frac{2 b B^2 g^2 (a + bx)}{d^2 i^3 (c + dx)} + \frac{2 b B^2 g^2 (a + bx) \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right]}{d^2 i^3 (c + dx)} + \\
& \frac{B g^2 (a + bx)^2 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)}{2 d i^3 (c + dx)^2} - \frac{g^2 (a + bx)^2 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{2 d i^3 (c + dx)^2} - \frac{b g^2 (a + bx) \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{d^2 i^3 (c + dx)} - \\
& \frac{b^2 g^2 \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right] \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right)^2}{d^3 i^3} - \frac{2 b^2 B g^2 \left(A + B \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i^3} + \frac{2 b^2 B^2 g^2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i^3}
\end{aligned}$$

Result (type 4, 3591 leaves):

$$\begin{aligned}
& -\frac{A^2 (b^2 c^2 - 2 a b c d + a^2 d^2) g^2}{2 d^3 i^3 (c + dx)^2} - \frac{2 (-A^2 b^2 c g^2 + a A^2 b d g^2)}{d^3 i^3 (c + dx)} + \frac{A^2 b^2 g^2 \operatorname{Log} [c + dx]}{d^3 i^3} + \\
& \left(a^2 B^2 g^2 \left(-7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c + dx)^2 \operatorname{Log} [a + bx] + 2 (bc - ad) (3 bc - ad + 2 b dx) \operatorname{Log} \left[\frac{e(a+bx)}{c+dx} \right] \right) - \right.
\end{aligned}$$

$$\begin{aligned}
& 2 d (a + b x) (-2 b c + a d - b d x) \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]^2 + 6 b^2 c^2 \operatorname{Log}[c + d x] + 12 b^2 c d x \operatorname{Log}[c + d x] + 6 b^2 d^2 x^2 \operatorname{Log}[c + d x] \Big) \Big) / \\
& \left(4 d (b c - a d)^2 i^3 (c + d x)^2 + \frac{1}{i^3} 2 a^2 A B g^2 \left(\frac{\left(\frac{c}{d} + x\right) \left(2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{8 (c + d x)^3 \operatorname{Log}\left[\frac{c}{d} + x\right]} + \right. \right. \\
& \left. \left. \frac{\frac{d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{a d}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} - \left(\frac{d^2 \left(\frac{a}{b} + x\right)^2}{\left(-c + \frac{a d}{b}\right)^4 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)^2} + \frac{2 d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{a d}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} \right) \operatorname{Log}\left[\frac{a}{b} + x\right] - \frac{\operatorname{Log}\left[1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right]}{\left(-c + \frac{a d}{b}\right)^2} \right. \right. \\
& \left. \left. - \frac{-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]}{2 d (c + d x)^2} \right) + \right. \\
& \frac{1}{i^3} 4 a A b B g^2 \left(\frac{1 + \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)}}{d} - \right. \\
& \left. \frac{c \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c + d x) (b c - a d + b (c + d x) \operatorname{Log}[a + b x] - b (c + d x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 d^2 (c + d x)^2} - \frac{(c + 2 d x) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 d^2 (c + d x)^2} \right) + \\
& \frac{1}{i^3} 2 A b^2 B g^2 \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^3} - \frac{2 c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^3 (c + d x)^2} - \frac{2 c \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)}\right)}{d^2} + \right. \\
& \left. \frac{c^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c + d x) (b c - a d + b (c + d x) \operatorname{Log}[a + b x] - b (c + d x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{2 d^3 (c + d x)^2} + \right. \\
& \left. \frac{\left(\frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 d^3} + \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^3} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{i^3} 2 a b B^2 g^2 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2 (c + dx)} + \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 d^2 (c + dx)^2} + \right. \\
& 2 \left(\frac{1 + \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2 (c + dx)} - \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^2 (c + dx)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + dx)} - \frac{b \operatorname{Log}[a + bx]}{d (-bc + ad)} + \frac{b \operatorname{Log}[c + dx]}{d (-bc + ad)}}{d} - \frac{c \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c + dx) (bc - ad + b (c + dx) \operatorname{Log}[a + bx] - b (c + dx) \operatorname{Log}[c + dx])}{(bc - ad)^2}\right)}{2 d^2 (c + dx)^2} \right) \\
& \left. \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]\right) - \frac{(c + 2 dx) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]\right)^2}{2 d^2 (c + dx)^2} + \right. \\
& \left. \frac{-d (a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + dx)}{bc - ad}\right] + 2 b (c + dx) \operatorname{PolyLog}\left[2, \frac{d (a + bx)}{-bc + ad}\right]}{d^2 (-bc + ad) (c + dx)} + \right. \\
& \left(c \left(d (a + bx) (ad - b (2c + dx)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + dx)^2 \operatorname{Log}\left[\frac{b (c + dx)}{bc - ad}\right] + 2 b (c + dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
& \left. \left. \left(d (a + bx) + b (c + dx) \operatorname{Log}\left[\frac{b (c + dx)}{bc - ad}\right] \right) + 2 b^2 (c + dx)^2 \operatorname{PolyLog}\left[2, \frac{d (a + bx)}{-bc + ad}\right] \right) \right) / \left(2 d^2 (bc - ad)^2 (c + dx)^2 \right) - \\
& 2 \left(\left(2 (bc - ad) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b (c + dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a + bx] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + bx)}{-bc + ad}\right] + 2 \operatorname{Log}[c + dx] \right) - \right. \right. \\
& \left. \left. 2 b (c + dx) \operatorname{PolyLog}\left[2, \frac{b (c + dx)}{bc - ad}\right] \right) \right) / \left(2 d^2 (-bc + ad) (c + dx) \right) + \left(c \left(-b (bc - ad) (c + dx) + (bc - ad)^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
& \left. \left. \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2 (c + dx)^2 \operatorname{Log}[a + bx] + b^2 (c + dx)^2 \operatorname{Log}[c + dx] + b (c + dx) \left(b (c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 (bc - ad) \right. \right. \right. \\
& \left. \left. \left. \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b (c + dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + bx)}{-bc + ad}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + dx)}{bc - ad}\right] \right) \right) \right) \right) / \left(4 d^2 (bc - ad)^2 (c + dx)^2 \right) \left. \right) + \\
& \frac{1}{i^3} b^2 B^2 g^2 \left(\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \frac{2 c \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3 (c + dx)} - \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 d^3 (c + dx)^2} + \right. \\
& \left. \frac{\left(\frac{c (3c + 4dx)}{(c + dx)^2} + 2 \operatorname{Log}[c + dx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c + dx} + \frac{bex}{c + dx}\right]\right)^2}{2 d^3} - \frac{1}{d^3 (-bc + ad) (c + dx)} \right)
\end{aligned}$$

$$\begin{aligned}
& 2c \left(-d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \\
& \left(c^2 \left(d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \\
& \quad \left. \left. 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \\
& \left(2d^3(bc-ad)^2(c+dx)^2 \right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) \\
& \left(-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^3} - \frac{2c(1+\operatorname{Log}\left[\frac{c}{d}+x\right])}{d^3(c+dx)} + \frac{c^2(1+2\operatorname{Log}\left[\frac{c}{d}+x\right])}{4d^3(c+dx)^2} - \frac{2c\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b\operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b\operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} + \right. \\
& \quad \left. \frac{c^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^3(c+dx)^2} + \frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) + \\
& \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2\operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} - 2 \left(-\frac{1}{d^3(-bc+ad)(c+dx)} \right. \\
& \quad c \left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2\operatorname{Log}[a+bx] - 2\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2\operatorname{Log}[c+dx] \right) - \right. \\
& \quad \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) - \left(c^2 \left(-b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + 2\operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \\
& \quad \left. \left. b^2(c+dx)^2 \operatorname{Log}[a+bx] + b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(bc-ad) \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \right. \\
& \quad \left. \left. \left. 2b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) \right) / \left(4d^3(bc-ad)^2(c+dx)^2 \right) + \frac{1}{2d^3} \\
& \left. \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2\operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right)
\end{aligned}$$

Problem 113: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 150 leaves, 5 steps):

$$\frac{B i n (c + d x)}{b g^2 (a + b x)} - \frac{i (c + d x) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] \right)}{b g^2 (a + b x)} - \frac{d i \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] \right) \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^2 g^2} + \frac{B d i n \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^2 g^2}$$

Result (type 4, 403 leaves):

$$\frac{1}{2 b^2 g^2} i \left(- \frac{2 (b c - a d) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] - B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)}{a + b x} + 2 d \operatorname{Log}[a + b x] \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] - B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - \frac{2 b B c n \left(-d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad} \right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right)}{(b c - a d) (a + b x)} + B d n \left(\operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) \right)$$

Problem 114: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$\frac{B i n (c + d x)^2}{4 (b c - a d) g^3 (a + b x)^2} - \frac{i (c + d x)^2 \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] \right)}{2 (b c - a d) g^3 (a + b x)^2}$$

Result (type 3, 216 leaves):

$$\left(i \left(-2 A b^2 c^2 + 2 a^2 A d^2 - b^2 B c^2 n + a^2 B d^2 n - 4 A b^2 c d x + 4 a A b d^2 x - 2 b^2 B c d n x + 2 a b B d^2 n x - 2 B d^2 n (a + b x)^2 \operatorname{Log}[a + b x] - 2 B (b c - a d) (b c + a d + 2 b d x) \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx} \right)^n} \right] + 2 a^2 B d^2 n \operatorname{Log}[c + d x] + 4 a b B d^2 n x \operatorname{Log}[c + d x] + 2 b^2 B d^2 n x^2 \operatorname{Log}[c + d x] \right) \right) / \left(4 b^2 (b c - a d) g^3 (a + b x)^2 \right)$$

Problem 121: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{a g + b g x} dx$$

Optimal (type 4, 289 leaves, 10 steps):

$$\begin{aligned} & -\frac{B d (b c - a d) i^2 n x}{2 b^2 g} + \frac{d (b c - a d) i^2 (a + b x) (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{b^3 g} + \frac{i^2 (c + d x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{2 b g} - \frac{B (b c - a d)^2 i^2 n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{2 b^3 g} \\ & - \frac{3 B (b c - a d)^2 i^2 n \operatorname{Log}[c + d x]}{2 b^3 g} - \frac{(b c - a d)^2 i^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]) \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b^3 g} + \frac{B (b c - a d)^2 i^2 n \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^3 g} \end{aligned}$$

Result (type 4, 651 leaves):

$$\begin{aligned} & \frac{1}{2 b^3 g} i^2 \left(4 b^2 B c^2 n - 6 a b B c d n + 2 a^2 B d^2 n + 4 A b^2 c d x - 2 a A b d^2 x - b^2 B c d n x + a b B d^2 n x + A b^2 d^2 x^2 + \right. \\ & B (b c - a d)^2 n \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 A b^2 c^2 \operatorname{Log}[a + b x] - 4 a A b c d \operatorname{Log}[a + b x] + \\ & 2 a^2 A d^2 \operatorname{Log}[a + b x] - a^2 B d^2 n \operatorname{Log}[a + b x] + 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\ & 2 a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 B n \operatorname{Log}\left[\frac{a}{b} + x\right] (a d (-2 b c + a d) + (b c - a d)^2 \operatorname{Log}[a + b x]) - 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \\ & 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 2 a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 4 b^2 B c d x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \\ & 2 a b B d^2 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + b^2 B d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 b^2 B c^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 4 a b B c d \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\ & \left. 2 a^2 B d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + b^2 B c^2 n \operatorname{Log}[c + d x] - 2 B (b c - a d)^2 n \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \end{aligned}$$

Problem 122: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{(a g + b g x)^2} dx$$

Optimal (type 4, 259 leaves, 8 steps):

$$\begin{aligned}
& - \frac{B (b c - a d) i^2 n (c + d x)}{b^2 g^2 (a + b x)} + \frac{d^2 i^2 (a + b x) (A + B \operatorname{Log}[e^{(\frac{a+b x}{c+d x})^n}])}{b^3 g^2} - \frac{(b c - a d) i^2 (c + d x) (A + B \operatorname{Log}[e^{(\frac{a+b x}{c+d x})^n}])}{b^2 g^2 (a + b x)} - \\
& \frac{B d (b c - a d) i^2 n \operatorname{Log}[c + d x]}{b^3 g^2} - \frac{2 d (b c - a d) i^2 (A + B \operatorname{Log}[e^{(\frac{a+b x}{c+d x})^n}]) \operatorname{Log}[1 - \frac{b(c+d x)}{d(a+b x)}]}{b^3 g^2} + \frac{2 B d (b c - a d) i^2 n \operatorname{PolyLog}[2, \frac{b(c+d x)}{d(a+b x)}]}{b^3 g^2}
\end{aligned}$$

Result (type 4, 712 leaves):

$$\begin{aligned}
& \frac{1}{b^3 g^2} i^2 \left(b d^2 x \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) - \frac{(b c - a d)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right)}{a + b x} + 2 d (b c - a d) \operatorname{Log}[a + b x] \right. \\
& \left. \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) - \frac{b^2 B c^2 n \left(-d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d} \right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right)}{(b c - a d) (a + b x)} + \right. \\
& \left. b B c d n \left(\operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) + \right. \\
& \left. \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) - \\
& B d^2 n \left(- (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right) + a \operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \frac{a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{a + b x} + b \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x \right] \right) - \right. \\
& \left. \left(b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) + \right. \\
& \left. \frac{a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 a \left(\operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 123: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log}[e^{(\frac{a+b x}{c+d x})^n}])}{(a g + b g x)^3} dx$$

Optimal (type 4, 242 leaves, 7 steps):

$$-\frac{B d i^2 n (c+d x)}{b^2 g^3 (a+b x)} - \frac{B i^2 n (c+d x)^2}{4 b g^3 (a+b x)^2} - \frac{d i^2 (c+d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2 g^3 (a+b x)} -$$

$$\frac{i^2 (c+d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b g^3 (a+b x)^2} - \frac{d^2 i^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^3} + \frac{B d^2 i^2 n \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^3}$$

Result (type 4, 903 leaves):

$$\frac{1}{4 b^3 g^3} i^2 \left(-\frac{1}{(b c - a d)^2 (a+b x)^2} b^2 B c^2 n \left(b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + \right. \right.$$

$$\left. 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d} \right] + 2 b^2 c^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] - 4 a b c d \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] + 2 a^2 d^2 \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) -$$

$$\frac{2 (b c - a d)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right)}{(a+b x)^2} + \frac{8 d (-b c + a d) \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right)}{a+b x} +$$

$$4 d^2 \operatorname{Log}[a+b x] \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) -$$

$$\frac{1}{(b c - a d)^2 (a+b x)^2} 2 b B c d n \left(3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - \right.$$

$$2 d (-2 b c + a d) (a+b x)^2 \operatorname{Log}[a+b x] + 2 (b c - a d)^2 (a+2 b x) \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] - 4 a^2 b c d \operatorname{Log}[c+d x] +$$

$$\left. 2 a^3 d^2 \operatorname{Log}[c+d x] - 8 a b^2 c d x \operatorname{Log}[c+d x] + 4 a^2 b d^2 x \operatorname{Log}[c+d x] - 4 b^3 c d x^2 \operatorname{Log}[c+d x] + 2 a b^2 d^2 x^2 \operatorname{Log}[c+d x] \right) +$$

$$B d^2 n \left(2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \frac{8 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{a+b x} - \frac{a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{(a+b x)^2} + 2 \left(\frac{a (3 a + 4 b x)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x] \right) \right.$$

$$\left. \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a+b x}{c+d x} \right] \right) + \frac{8 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a+b x) \left(\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right)}{(b c - a d) (a+b x)} +$$

$$\left. \frac{2 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x \right] + \frac{d (a+b x) (b c - a d + d (a+b x) \operatorname{Log}[a+b x] - d (a+b x) \operatorname{Log}[c+d x])}{(b c - a d)^2} \right)}{(a+b x)^2} - 4 \left(\operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d} \right] \right) \right)$$

Problem 124: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(a g + b g x)^4} dx$$

Optimal (type 3, 93 leaves, 2 steps):

$$-\frac{B i^2 n (c+d x)^3}{9 (b c-a d) g^4 (a+b x)^3} - \frac{i^2 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{3 (b c-a d) g^4 (a+b x)^3}$$

Result (type 3, 329 leaves):

$$\frac{1}{9 b^3 (b c-a d) g^4 (a+b x)^3} i^2 \left(-3 A b^3 c^3 + 3 a^3 A d^3 - b^3 B c^3 n + a^3 B d^3 n - 9 A b^3 c^2 d x + 9 a^2 A b d^3 x - 3 b^3 B c^2 d n x + 3 a^2 b B d^3 n x - 9 A b^3 c d^2 x^2 + 9 a A b^2 d^3 x^2 - 3 b^3 B c d^2 n x^2 + 3 a b^2 B d^3 n x^2 - 3 B d^3 n (a+b x)^3 \operatorname{Log}[a+b x] - 3 B (b c-a d) \left(a^2 d^2 + a b d (c+3 d x) + b^2 (c^2+3 c d x+3 d^2 x^2) \right) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] + 3 a^3 B d^3 n \operatorname{Log}[c+d x] + 9 a^2 b B d^3 n x \operatorname{Log}[c+d x] + 9 a b^2 B d^3 n x^2 \operatorname{Log}[c+d x] + 3 b^3 B d^3 n x^3 \operatorname{Log}[c+d x] \right)$$

Problem 131: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i+d i x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{a g+b g x} d x$$

Optimal (type 4, 373 leaves, 14 steps):

$$-\frac{5 B d (b c-a d)^2 i^3 n x}{6 b^3 g} - \frac{B (b c-a d) i^3 n (c+d x)^2}{6 b^2 g} + \frac{d (b c-a d)^2 i^3 (a+b x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{b^4 g} + \frac{(b c-a d) i^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g} + \frac{i^3 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b g} - \frac{5 B (b c-a d)^3 i^3 n \operatorname{Log}\left[\frac{a+b x}{c+d x} \right]}{6 b^4 g} - \frac{11 B (b c-a d)^3 i^3 n \operatorname{Log}[c+d x]}{6 b^4 g} - \frac{(b c-a d)^3 i^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g} + \frac{B (b c-a d)^3 i^3 n \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g}$$

Result (type 4, 1061 leaves):

$$\begin{aligned}
& \frac{1}{6 b^4 g} i^3 \left(18 b^3 B c^3 n - 36 a b^2 B c^2 d n + 24 a^2 b B c d^2 n - 6 a^3 B d^3 n + 18 A b^3 c^2 d x - 18 a A b^2 c d^2 x + 6 a^2 A b d^3 x - \right. \\
& 7 b^3 B c^2 d n x + 12 a b^2 B c d^2 n x - 5 a^2 b B d^3 n x + 9 A b^3 c d^2 x^2 - 3 a A b^2 d^3 x^2 - b^3 B c d^2 n x^2 + a b^2 B d^3 n x^2 + 2 A b^3 d^3 x^3 + \\
& 3 B (b c - a d)^3 n \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 6 A b^3 c^3 \operatorname{Log}[a + b x] - \\
& 18 a A b^2 c^2 d \operatorname{Log}[a + b x] + 18 a^2 A b c d^2 \operatorname{Log}[a + b x] - 6 a^3 A d^3 \operatorname{Log}[a + b x] - 9 a^2 b B c d^2 n \operatorname{Log}[a + b x] + 5 a^3 B d^3 n \operatorname{Log}[a + b x] + \\
& 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 6 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 6 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d (3 b^2 c^2 - 3 a b c d + a^2 d^2) - (b c - a d)^3 \operatorname{Log}[a + b x] \right) - \\
& 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 6 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 b^3 B c^2 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 18 a b^2 B c d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 a^2 b B d^3 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 9 b^3 B c d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 a b^2 B d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 b^3 B d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 b^3 B c^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 18 a b^2 B c^2 d \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 18 a^2 b B c d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 6 a^3 B d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 7 b^3 B c^3 n \operatorname{Log}[c + d x] - 3 a b^2 B c^2 d n \operatorname{Log}[c + d x] - 6 B (b c - a d)^3 n \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \Big)
\end{aligned}$$

Problem 132: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 390 leaves, 11 steps):

$$\begin{aligned}
& - \frac{B d^2 (b c - a d) i^3 n x}{2 b^3 g^2} - \frac{B (b c - a d)^2 i^3 n (c + d x)}{b^3 g^2 (a + b x)} + \frac{2 d^2 (b c - a d) i^3 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{b^4 g^2} - \\
& \frac{(b c - a d)^2 i^3 (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{b^3 g^2 (a + b x)} + \frac{d i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{2 b^2 g^2} - \frac{B d (b c - a d)^2 i^3 n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]}{2 b^4 g^2} - \\
& \frac{5 B d (b c - a d)^2 i^3 n \operatorname{Log}[c + d x]}{2 b^4 g^2} - \frac{3 d (b c - a d)^2 i^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) \operatorname{Log}\left[1 - \frac{b(c + d x)}{d(a + b x)}\right]}{b^4 g^2} + \frac{3 B d (b c - a d)^2 i^3 n \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{d(a + b x)}\right]}{b^4 g^2}
\end{aligned}$$

Result (type 4, 1120 leaves):

$$\begin{aligned}
& \frac{1}{2 b^4 g^2} i^3 \left(2 b d^2 (3 b c - 2 a d) x \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + b^2 d^3 x^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \right. \\
& \frac{2 (b c - a d)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)}{a+b x} + 6 d (b c - a d)^2 \operatorname{Log}[a+b x] \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \\
& \frac{2 b^3 B c^3 n \left(-d (a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right)}{(b c - a d) (a+b x)} + \\
& B d^3 n \left(4 a^2 - \frac{4 a b c}{d} + a b x - \frac{b^2 c x}{d} + \frac{2 a^3}{a+b x} + 3 a^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{4 a b c \operatorname{Log}\left[\frac{c}{d}+x\right]}{d} - a^2 \operatorname{Log}[a+b x] + \frac{2 a^3 d \operatorname{Log}[a+b x]}{b c - a d} + \right. \\
& 6 a^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 2 a^2 \operatorname{Log}\left[\frac{a}{b}+x\right] (2 + 3 \operatorname{Log}[a+b x]) - 6 a^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 4 a b x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \\
& \left. b^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \frac{2 a^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{a+b x} + 6 a^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \frac{b^2 c^2 \operatorname{Log}[c+d x]}{d^2} + \frac{2 a^3 d \operatorname{Log}[c+d x]}{-b c+a d} - 6 a^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) + \\
& 3 b^2 B c^2 d n \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{a+b x} + 2 \left(\frac{a}{a+b x} + \operatorname{Log}[a+b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
& \left. \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x])\right)}{(b c - a d) (a+b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]\right) \right) - \\
& 6 b B c d^2 n \left(-(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right) + a \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{a+b x} + b \left(\frac{c}{d}+x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right]\right) - \right. \\
& \left(b x - \frac{a^2}{a+b x} - 2 a \operatorname{Log}[a+b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \\
& \left. \frac{a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x])\right)}{(b c - a d) (a+b x)} - 2 a \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]\right) \right) \right)
\end{aligned}$$

Problem 133: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 361 leaves, 9 steps):

$$\begin{aligned}
& - \frac{2 B d (b c - a d) i^3 n (c + d x)}{b^3 g^3 (a + b x)} - \frac{B (b c - a d) i^3 n (c + d x)^2}{4 b^2 g^3 (a + b x)^2} + \frac{d^3 i^3 (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b^4 g^3} - \\
& \frac{2 d (b c - a d) i^3 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{2 b^2 g^3 (a + b x)^2} - \frac{B d^2 (b c - a d) i^3 n \operatorname{Log}[c + d x]}{b^4 g^3} - \\
& \frac{3 d^2 (b c - a d) i^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^3} + \frac{3 B d^2 (b c - a d) i^3 n \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^3}
\end{aligned}$$

Result (type 4, 1324 leaves):

$$\begin{aligned}
& \frac{1}{4 b^4 g^3} i^3 \left(-\frac{1}{(b c - a d)^2 (a + b x)^2} b^3 B c^3 n \left(b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + \right. \right. \\
& \quad \left. \left. 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 b^2 c^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - 4 a b c d \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 a^2 d^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
& \quad \left. 4 b d^3 x \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \frac{2 (b c - a d)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)}{(a + b x)^2} - \right. \\
& \quad \left. \frac{12 d (b c - a d)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)}{a + b x} + 12 d^2 (b c - a d) \operatorname{Log}[a + b x] \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \right. \\
& \quad \left. \frac{1}{(b c - a d)^2 (a + b x)^2} 3 b^2 B c^2 d n \left(3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - \right. \right. \\
& \quad \left. \left. 2 d (-2 b c + a d) (a + b x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d)^2 (a + 2 b x) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - 4 a^2 b c d \operatorname{Log}[c + d x] + \right. \right. \\
& \quad \left. \left. 2 a^3 d^2 \operatorname{Log}[c + d x] - 8 a b^2 c d x \operatorname{Log}[c + d x] + 4 a^2 b d^2 x \operatorname{Log}[c + d x] - 4 b^3 c d x^2 \operatorname{Log}[c + d x] + 2 a b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) + \right. \\
& \quad \left. 3 b B c d^2 n \left(2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{8 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} - \frac{a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{(a + b x)^2} + 2 \left(\frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log}[a + b x] \right) \right. \right. \\
& \quad \left. \left. \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \frac{8 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} + \right. \right. \\
& \quad \left. \left. \frac{2 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(a + b x)^2} - 4 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right) - \right. \\
& \quad \left. B d^3 n \left(-4 (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 6 a \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{12 a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} - \frac{a^3 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{(a + b x)^2} + \right. \right. \\
& \quad \left. \left. 4 b \left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + 2 \left(-2 b x + \frac{a^2 (5 a + 6 b x)}{(a + b x)^2} + 6 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \right. \\
& \quad \left. \left. \frac{12 a^2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right)}{(b c - a d) (a + b x)} + \right. \right. \\
& \quad \left. \left. \frac{2 a^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{(a + b x)^2} - 12 a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right) \right)
\end{aligned}$$

Problem 134: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{(a g + b g x)^4} dx$$

Optimal (type 4, 326 leaves, 9 steps):

$$\begin{aligned} & -\frac{B d^2 i^3 n (c + d x)}{b^3 g^4 (a + b x)} - \frac{B d i^3 n (c + d x)^2}{4 b^2 g^4 (a + b x)^2} - \frac{B i^3 n (c + d x)^3}{9 b g^4 (a + b x)^3} - \frac{d^2 i^3 (c + d x) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{b^3 g^4 (a + b x)} - \frac{d i^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 b^2 g^4 (a + b x)^2} \\ & - \frac{i^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 b g^4 (a + b x)^3} - \frac{d^3 i^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g^4} + \frac{B d^3 i^3 n \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g^4} \end{aligned}$$

Result (type 4, 2243 leaves):

$$\begin{aligned} & \frac{d^3 i^3 \operatorname{Log} [a + b x] \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)}{b^4 g^4} + \frac{1}{b^4 g^4 (a + b x)} \\ & 3 \left(-A b c d^2 i^3 + a A d^3 i^3 - b B c d^2 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + a B d^3 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) - \\ & \frac{1}{2 b^4 g^4 (a + b x)^2} \left(A b^2 c^2 d i^3 - 2 a A b c d^2 i^3 + a^2 A d^3 i^3 + b^2 B c^2 d i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - \right. \\ & \quad \left. 2 a b B c d^2 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + a^2 B d^3 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) + \\ & \frac{1}{3 b^4 g^4 (a + b x)^3} \left(-A b^3 c^3 i^3 + 3 a A b^2 c^2 d i^3 - 3 a^2 A b c d^2 i^3 + a^3 A d^3 i^3 - b^3 B c^3 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + \right. \\ & \quad \left. 3 a b^2 B c^2 d i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - 3 a^2 b B c d^2 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + \right. \\ & \quad \left. a^3 B d^3 i^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) + \frac{1}{g^4} B c^3 i^3 n \left(-\frac{\left(\frac{a}{b} + x \right) \left(3 \operatorname{Log} \left[\frac{a}{b} + x \right] + 9 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{27 (a + b x)^4 \operatorname{Log} \left[\frac{a}{b} + x \right]} - \frac{1}{6 b} \right) \\ & \left(-\frac{b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{bc}{d} \right)^5 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)^2} - \frac{4 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{bc}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)} + \left(\frac{2 b^3 \left(\frac{c}{d} + x \right)^3}{\left(-a + \frac{bc}{d} \right)^6 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)^3} + \frac{6 b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{bc}{d} \right)^5 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)^2} + \frac{6 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{bc}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)} \right) \end{aligned}$$

$$\begin{aligned}
& \left. \log \left[\frac{c}{d} + x \right] + \frac{2 \log \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right]}{\left(-a + \frac{bc}{d} \right)^3} \right) - \frac{-\log \left[\frac{a}{b} + x \right] + \log \left[\frac{c}{d} + x \right] + \log \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right]}{3b(a+bx)^3} \right) + \frac{1}{g^4} \\
& 3Bc^2di^3n \left(-\frac{1+2\log\left[\frac{a}{b}+x\right]}{4b^2(a+bx)^2} + \frac{a\left(1+3\log\left[\frac{a}{b}+x\right]\right)}{9b^2(a+bx)^3} + \frac{a\left(-\frac{2\log\left[\frac{c}{d}+x\right]}{(a+bx)^3} + \frac{d\left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2\log[a+bx] - 2d^2\log[c+dx]\right)}{(bc-ad)^3}\right)}{6b^2} \right) + \\
& \left. \frac{\log\left[\frac{c}{d}+x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2}}{2b^2(a+bx)^2} - \frac{(a+3bx)\left(-\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{6b^2(a+bx)^3} \right) + \frac{1}{g^4} \\
& 3Bcd^2i^3n \left(-\frac{1+\log\left[\frac{a}{b}+x\right]}{b^3(a+bx)} + \frac{a\left(1+2\log\left[\frac{a}{b}+x\right]\right)}{2b^3(a+bx)^2} - \frac{a^2\left(1+3\log\left[\frac{a}{b}+x\right]\right)}{9b^3(a+bx)^3} - \frac{(-bc+ad)\log\left[\frac{c}{d}+x\right] + d(a+bx)\left(\log[a+bx] - \log[c+dx]\right)}{b^3(bc-ad)(a+bx)} \right) - \\
& \frac{a^2\left(-\frac{2\log\left[\frac{c}{d}+x\right]}{(a+bx)^3} + \frac{d\left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2\log[a+bx] - 2d^2\log[c+dx]\right)}{(bc-ad)^3}\right)}{6b^3} - \frac{a\left(\log\left[\frac{c}{d}+x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2}\right)}{b^3(a+bx)^2} - \\
& \left. \frac{(a^2+3abx+3b^2x^2)\left(-\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{3b^3(a+bx)^3} \right) + \\
& \frac{1}{g^4} B d^3 i^3 n \left(\frac{\log\left[\frac{a}{b}+x\right]^2}{2b^4} + \frac{3a\left(1+\log\left[\frac{a}{b}+x\right]\right)}{b^4(a+bx)} - \frac{3a^2\left(1+2\log\left[\frac{a}{b}+x\right]\right)}{4b^4(a+bx)^2} + \frac{a^3\left(1+3\log\left[\frac{a}{b}+x\right]\right)}{9b^4(a+bx)^3} + \right.
\end{aligned}$$

$$\frac{3 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{b^4 (b c - a d) (a + b x)} +$$

$$\frac{a^3 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left(\frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x] \right)}{(b c - a d)^3} \right)}{6 b^4} + \frac{3 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{2 b^4 (a + b x)^2} +$$

$$\left. \frac{\left(\frac{a (11 a^2 + 27 a b x + 18 b^2 x^2)}{(a + b x)^3} + 6 \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^4}}{6 b^4} \right)$$

Problem 135: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 269 leaves, 6 steps):

$$\frac{g^3 (a + b x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 d i} - \frac{(b c - a d) g^3 (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 d^2 i} +$$

$$\frac{(b c - a d)^2 g^3 (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 d^3 i} +$$

$$\frac{(b c - a d)^3 g^3 \left(6 A + 11 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)} \right]}{6 d^4 i} + \frac{B (b c - a d)^3 g^3 n \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^4 i}$$

Result (type 4, 1003 leaves):

$$\begin{aligned}
& \frac{1}{6 d^4 i} g^3 \left(6 b^3 B c^3 n - 24 a b^2 B c^2 d n + 36 a^2 b B c d^2 n - 18 a^3 B d^3 n + 6 A b^3 c^2 d x - 18 a A b^2 c d^2 x + 18 a^2 A b d^3 x + \right. \\
& 5 b^3 B c^2 d n x - 12 a b^2 B c d^2 n x + 7 a^2 b B d^3 n x - 3 A b^3 c d^2 x^2 + 9 a A b^2 d^3 x^2 - b^3 B c d^2 n x^2 + a b^2 B d^3 n x^2 + 2 A b^3 d^3 x^3 - \\
& 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 9 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 9 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 3 a^2 b B c d^2 n \operatorname{Log}[a + b x] - 7 a^3 B d^3 n \operatorname{Log}[a + b x] + 6 b^3 B c^2 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 18 a b^2 B c d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 18 a^2 b B d^3 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 b^3 B c d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 9 a b^2 B d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 2 b^3 B d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 A b^3 c^3 \operatorname{Log}[c + d x] + 18 a A b^2 c^2 d \operatorname{Log}[c + d x] - 18 a^2 A b c d^2 \operatorname{Log}[c + d x] + 6 a^3 A d^3 \operatorname{Log}[c + d x] - \\
& 5 b^3 B c^3 n \operatorname{Log}[c + d x] + 9 a b^2 B c^2 d n \operatorname{Log}[c + d x] - 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^3 B c^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + \\
& 18 a b^2 B c^2 d \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 18 a^2 b B c d^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 6 a^3 B d^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 6 B n \\
& \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-a d (b^2 c^2 - 3 a b c d + 3 a^2 d^2) - (b c - a d)^3 \operatorname{Log}[c + d x] + (b c - a d)^3 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 6 B (b c - a d)^3 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)
\end{aligned}$$

Problem 136: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{c i + d i x} dx$$

Optimal (type 4, 211 leaves, 5 steps):

$$\frac{g^2 (a + b x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{2 d i} - \frac{(b c - a d) g^2 (a + b x) (2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{2 d^2 i} - \frac{(b c - a d)^2 g^2 (2 A + 3 B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]) \operatorname{Log}\left[\frac{b c - a d}{b(c + d x)}\right]}{2 d^3 i} - \frac{B (b c - a d)^2 g^2 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{d^3 i}$$

Result (type 4, 610 leaves):

$$\frac{1}{2 d^3 i} g^2 \left(-2 b^2 B c^2 n + 6 a b B c d n - 4 a^2 B d^2 n - 2 A b^2 c d x + 4 a A b d^2 x - b^2 B c d n x + a b B d^2 n x + A b^2 d^2 x^2 + 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] - 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] - b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 n \operatorname{Log}[a + b x] - 2 b^2 B c d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 4 a b B d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + b^2 B d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 A b^2 c^2 \operatorname{Log}[c + d x] - 4 a A b c d \operatorname{Log}[c + d x] + 2 a^2 A d^2 \operatorname{Log}[c + d x] + b^2 B c^2 n \operatorname{Log}[c + d x] + 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 b^2 B c^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 4 a b B c d \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 2 a^2 B d^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 2 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d (b c - 2 a d) + (b c - a d)^2 \operatorname{Log}[c + d x] - (b c - a d)^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 2 B (b c - a d)^2 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)$$

Problem 137: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{c i + d i x} dx$$

Optimal (type 4, 134 leaves, 4 steps):

$$\frac{g(a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{d i} + \frac{(b c - a d) g \left(A + B n + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right) \operatorname{Log}\left[\frac{b c - a d}{b(c + d x)}\right]}{d^2 i} + \frac{B (b c - a d) g n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{d^2 i}$$

Result (type 4, 308 leaves):

$$\frac{1}{2 d^2 i} g \left(2 b B c n - 2 a B d n + 2 A b d x - 2 b B c n \operatorname{Log}\left[\frac{c}{d} + x\right] + b B c n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a B d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b B d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 A b c \operatorname{Log}[c + d x] + 2 a A d \operatorname{Log}[c + d x] - 2 b B c n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 a B d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 2 b B c \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 2 a B d \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 2 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d + (b c - a d) \operatorname{Log}[c + d x] + (-b c + a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 2 B (-b c + a d) n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)$$

Problem 143: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 359 leaves, 9 steps):

$$\begin{aligned} & \frac{3 B (b c - a d)^2 g^3 n (a + b x)}{d^3 i^2 (c + d x)} - \frac{(b c - a d)^2 g^3 (6 A + 5 B n) (a + b x)}{2 d^3 i^2 (c + d x)} - \frac{3 B (b c - a d)^2 g^3 (a + b x) \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]}{d^3 i^2 (c + d x)} + \\ & \frac{g^3 (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 d i^2 (c + d x)} - \frac{(b c - a d) g^3 (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 d^2 i^2 (c + d x)} - \\ & \frac{b (b c - a d)^2 g^3 \left(6 A + 5 B n + 6 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{2 d^4 i^2} - \frac{3 b B (b c - a d)^2 g^3 n \operatorname{PolyLog} \left[2, \frac{d (a+bx)}{b (c+dx)} \right]}{d^4 i^2} \end{aligned}$$

Result (type 4, 1109 leaves):

$$\begin{aligned}
& \frac{1}{2 d^4 i^2} g^3 \left(-2 b^2 d (2 b c - 3 a d) x \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) + b^3 d^2 x^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) + \right. \\
& \frac{2 (b c - a d)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right)}{c + d x} + 6 b (b c - a d)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \operatorname{Log}[c + d x] + \\
& \frac{1}{(b c - a d) (c + d x)} 2 a^3 B d^3 n \left(b c - a d + b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] - b c \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] - b d x \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] \right) + \\
& 3 a^2 b B d^2 n \left(-\operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] + 2 \left(-\frac{c}{c + d x} + \frac{b c \operatorname{Log}[a + b x]}{-b c + a d} + \frac{b c \operatorname{Log}[c + d x]}{b c - a d} - \right. \right. \\
& \left. \left. \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \left(\frac{c}{c + d x} + \operatorname{Log}[c + d x] \right) + \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& b^3 B n \left(-4 c^2 + \frac{4 a c d}{b} - c d x + \frac{a d^2 x}{b} - \frac{2 c^3}{c + d x} + 4 c^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - 3 c^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 - \frac{a^2 d^2 \operatorname{Log}[a + b x]}{b^2} + \frac{2 b c^3 \operatorname{Log}[a + b x]}{-b c + a d} - \right. \\
& 4 c d x \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] + d^2 x^2 \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] + \frac{2 c^3 \operatorname{Log}\left[\frac{a + b x}{c + d x} \right]}{c + d x} + c^2 \operatorname{Log}[c + d x] + \frac{2 b c^3 \operatorname{Log}[c + d x]}{b c - a d} + 6 c^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] + \\
& \left. 6 c^2 \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \operatorname{Log}[c + d x] - \frac{2 c \operatorname{Log}\left[\frac{a}{b} + x \right] \left(2 a d + 3 b c \operatorname{Log}[c + d x] - 3 b c \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] \right)}{b} + 6 c^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& 6 a b^2 B d n \left(d \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right) - (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x \right] \right) + c \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + \frac{c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x \right] \right)}{c + d x} + \right. \\
& c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x \right]}{c + d x} + \frac{b \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{b c - a d} \right) + \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \left(d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x] \right) - \\
& \left. 2 c \left(\operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 275 leaves, 8 steps):

$$\begin{aligned}
& - \frac{2B(bc-ad)g^2n(a+bx)}{d^2i^2(c+dx)} + \frac{(bc-ad)g^2(2A+Bn)(a+bx)}{d^2i^2(c+dx)} + \frac{2B(bc-ad)g^2(a+bx)\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{d^2i^2(c+dx)} + \\
& \frac{g^2(a+bx)^2\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{di^2(c+dx)} + \frac{b(bc-ad)g^2(2A+Bn+2B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^3i^2} + \frac{2bB(bc-ad)g^2n\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3i^2}
\end{aligned}$$

Result (type 4, 705 leaves):

$$\begin{aligned}
& \frac{1}{d^3i^2}g^2\left(b^2dx\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-Bn\text{Log}\left[\frac{a+bx}{c+dx}\right]\right)-\frac{(bc-ad)^2\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-Bn\text{Log}\left[\frac{a+bx}{c+dx}\right]\right)}{c+dx}-\right. \\
& \left.2b(bc-ad)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-Bn\text{Log}\left[\frac{a+bx}{c+dx}\right]\right)\text{Log}[c+dx]+\frac{1}{(bc-ad)(c+dx)}\right. \\
& \left.a^2Bd^2n\left(bc-ad+b(c+dx)\text{Log}\left[\frac{a}{b}+x\right]+(-bc+ad)\text{Log}\left[\frac{a+bx}{c+dx}\right]-bc\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]-bdx\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right)+\right. \\
& \left.abBdn\left(-\text{Log}\left[\frac{c}{d}+x\right]^2+2\text{Log}\left[\frac{c}{d}+x\right]\text{Log}[c+dx]+2\left(-\frac{c}{c+dx}+\frac{bc\text{Log}[a+bx]}{-bc+ad}+\frac{bc\text{Log}[c+dx]}{bc-ad}-\text{Log}\left[\frac{a}{b}+x\right]\text{Log}[c+dx]+\right.\right. \\
& \left.\left.\text{Log}\left[\frac{a+bx}{c+dx}\right]\left(\frac{c}{c+dx}+\text{Log}[c+dx]\right)+\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right)+2\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)+ \\
& \left.b^2Bn\left(d\left(\frac{a}{b}+x\right)\left(-1+\text{Log}\left[\frac{a}{b}+x\right]\right)-(c+dx)\left(-1+\text{Log}\left[\frac{c}{d}+x\right]\right)+c\text{Log}\left[\frac{c}{d}+x\right]^2+\frac{c^2\left(1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{c+dx}+\right. \\
& \left.c^2\left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{c+dx}+\frac{b\left(\text{Log}[a+bx]-\text{Log}[c+dx]\right)}{bc-ad}\right)+\left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{a+bx}{c+dx}\right]\right)\left(dx-\frac{c^2}{c+dx}-2c\text{Log}[c+dx]\right)- \\
& \left.2c\left(\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]+\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)\right)
\end{aligned}$$

Problem 145: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag+bgx)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{(ci+di)^2} dx$$

Optimal (type 4, 168 leaves, 7 steps):

$$\begin{aligned}
& - \frac{Ag(a+bx)}{di^2(c+dx)} + \frac{Bgn(a+bx)}{di^2(c+dx)} - \frac{Bg(a+bx)\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{di^2(c+dx)} - \frac{bg\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^2i^2} - \frac{bBgn\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^2i^2}
\end{aligned}$$

Result (type 4, 411 leaves):

$$\frac{1}{2 d^2 i^2} g \left(\frac{2 (b c - a d) \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)}{c+d x} + 2 b \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] + \frac{1}{(b c - a d) (c+d x)} \right. \\ \left. 2 a B d n \left(b c - a d + b (c+d x) \operatorname{Log} \left[\frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] - b c \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] \right) + \right. \\ \left. b B n \left(-\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c+d x] + 2 \left(-\frac{c}{c+d x} + \frac{b c \operatorname{Log} [a+b x]}{-b c + a d} + \frac{b c \operatorname{Log} [c+d x]}{b c - a d} - \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c+d x] + \right. \right. \right. \\ \left. \left. \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \left(\frac{c}{c+d x} + \operatorname{Log} [c+d x] \right) + \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right)$$

Problem 151: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 382 leaves, 9 steps):

$$-\frac{3 B (b c - a d) g^3 n (a+b x)^2}{4 d^2 i^3 (c+d x)^2} - \frac{3 b B (b c - a d) g^3 n (a+b x)}{d^3 i^3 (c+d x)} + \frac{b (b c - a d) g^3 (3 A + B n) (a+b x)}{d^3 i^3 (c+d x)} + \\ \frac{3 b B (b c - a d) g^3 (a+b x) \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right]}{d^3 i^3 (c+d x)} + \frac{g^3 (a+b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{d i^3 (c+d x)^2} + \frac{(b c - a d) g^3 (a+b x)^2 \left(3 A + B n + 3 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 d^2 i^3 (c+d x)^2} + \\ \frac{b^2 (b c - a d) g^3 \left(3 A + B n + 3 B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c+d x)} \right]}{d^4 i^3} + \frac{3 b^2 B (b c - a d) g^3 n \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^4 i^3}$$

Result (type 4, 1317 leaves):

$$\begin{aligned}
& \frac{1}{4 d^4 i^3} g^3 \left(4 b^3 d x \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) + \frac{2 (b c - a d)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)}{(c+d x)^2} - \right. \\
& \frac{12 b (b c - a d)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)}{c+d x} - 12 b^2 (b c - a d) \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \operatorname{Log}[c+d x] - \\
& \frac{1}{(b c - a d)^2 (c+d x)^2} 3 a^2 b B d^2 n \left(-b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - \right. \\
& \quad 2 b (b c - 2 a d) (c+d x)^2 \operatorname{Log}[a+b x] + 2 (b c - a d)^2 (c+2 d x) \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + 2 b^2 c^3 \operatorname{Log}[c+d x] - 4 a b c^2 d \operatorname{Log}[c+d x] + \\
& \quad \left. 4 b^2 c^2 d x \operatorname{Log}[c+d x] - 8 a b c d^2 x \operatorname{Log}[c+d x] + 2 b^2 c d^2 x^2 \operatorname{Log}[c+d x] - 4 a b d^3 x^2 \operatorname{Log}[c+d x] \right) - \\
& \frac{1}{(b c - a d)^2 (c+d x)^2} a^3 B d^3 n \left(-b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c+d x)^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \\
& \quad \left. 2 (b c - a d)^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + 2 b^2 c^2 \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + 4 b^2 c d x \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + 2 b^2 d^2 x^2 \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] \right) + \\
& 3 a b^2 B d n \left(-2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \frac{8 c \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^2 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{(c+d x)^2} + 8 c \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]}{c+d x} + \frac{b \left(\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right)}{-b c + a d} \right) \right) + \\
& 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \left(\frac{c (3 c + 4 d x)}{(c+d x)^2} + 2 \operatorname{Log}[c+d x] \right) + \\
& \frac{2 c^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+d x) (b c - a d + b (c+d x) \operatorname{Log}[a+b x] - b (c+d x) \operatorname{Log}[c+d x])}{(b c - a d)^2} \right)}{(c+d x)^2} + 4 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) - \\
& b^3 B n \left(-4 d \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 4 (c+d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - 6 c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \frac{12 c^2 \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^3 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{(c+d x)^2} - 12 c^2 \right. \\
& \quad \left(-\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]}{c+d x} + \frac{b \left(\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right)}{b c - a d} \right) + 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \left(-2 d x + \frac{c^2 (5 c + 6 d x)}{(c+d x)^2} + 6 c \operatorname{Log}[c+d x] \right) + \\
& \quad \left. \frac{2 c^3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+d x) (b c - a d + b (c+d x) \operatorname{Log}[a+b x] - b (c+d x) \operatorname{Log}[c+d x])}{(b c - a d)^2} \right)}{(c+d x)^2} + 12 c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 152: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 263 leaves, 8 steps):

$$\frac{B g^2 n (a + b x)^2}{4 d i^3 (c + d x)^2} - \frac{A b g^2 (a + b x)}{d^2 i^3 (c + d x)} + \frac{b B g^2 n (a + b x)}{d^2 i^3 (c + d x)} - \frac{b B g^2 (a + b x) \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right]}{d^2 i^3 (c + d x)} -$$

$$\frac{g^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 d i^3 (c + d x)^2} - \frac{b^2 g^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{d^3 i^3} - \frac{b^2 B g^2 n \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i^3}$$

Result (type 4, 907 leaves):

$$\begin{aligned}
& \frac{1}{4 d^3 i^3} g^2 \left(- \frac{2 (b c - a d)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)}{(c+d x)^2} + \right. \\
& \frac{8 b (b c - a d) \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right)}{c+d x} + 4 b^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] - \\
& \frac{1}{(b c - a d)^2 (c+d x)^2} 2 a b B d n \left(-b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - \right. \\
& 2 b (b c - 2 a d) (c+d x)^2 \operatorname{Log} [a+b x] + 2 (b c - a d)^2 (c+2 d x) \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + 2 b^2 c^3 \operatorname{Log} [c+d x] - 4 a b c^2 d \operatorname{Log} [c+d x] + \\
& \left. 4 b^2 c^2 d x \operatorname{Log} [c+d x] - 8 a b c d^2 x \operatorname{Log} [c+d x] + 2 b^2 c d^2 x^2 \operatorname{Log} [c+d x] - 4 a b d^3 x^2 \operatorname{Log} [c+d x] \right) - \\
& \frac{1}{(b c - a d)^2 (c+d x)^2} a^2 B d^2 n \left(-b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c+d x)^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \\
& \left. 2 (b c - a d)^2 \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] + 2 b^2 c^2 \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + 4 b^2 c d x \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + 2 b^2 d^2 x^2 \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] \right) + \\
& b^2 B n \left(-2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \frac{8 c \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^2 \left(1 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{(c+d x)^2} + 8 c \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]}{c+d x} + \frac{b \left(\operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{-b c + a d} \right) \right) + \\
& 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a+b x}{c+d x} \right] \right) \left(\frac{c (3 c + 4 d x)}{(c+d x)^2} + 2 \operatorname{Log} [c+d x] \right) + \\
& \left. \frac{2 c^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+d x) (b c - a d + b (c+d x) \operatorname{Log} [a+b x] - b (c+d x) \operatorname{Log} [c+d x])}{(b c - a d)^2} \right)}{(c+d x)^2} + 4 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 153: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x) \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$- \frac{B g n (a+b x)^2}{4 (b c - a d) i^3 (c+d x)^2} + \frac{g (a+b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] \right)}{2 (b c - a d) i^3 (c+d x)^2}$$

Result (type 3, 216 leaves):

$$\left(g \left(2 A b^2 c^2 - 2 a^2 A d^2 - b^2 B c^2 n + a^2 B d^2 n + 4 A b^2 c d x - 4 a A b d^2 x - \right. \right. \\ \left. \left. 2 b^2 B c d n x + 2 a b B d^2 n x - 2 b^2 B n (c + d x)^2 \operatorname{Log}[a + b x] + 2 B (b c - a d) (b c + a d + 2 b d x) \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] + \right. \right. \\ \left. \left. 2 b^2 B c^2 n \operatorname{Log}[c + d x] + 4 b^2 B c d n x \operatorname{Log}[c + d x] + 2 b^2 B d^2 n x^2 \operatorname{Log}[c + d x] \right) \right) / \left(4 d^2 (-b c + a d) i^3 (c + d x)^2 \right)$$

Problem 159: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 (c i + d i x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 584 leaves, 11 steps):

$$\frac{3 B^2 (b c - a d)^4 g^3 i n^2 x}{10 b d^3} - \frac{3 B^2 (b c - a d)^3 g^3 i n^2 (c + d x)^2}{20 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i n^2 (c + d x)^3}{30 d^4} - \\ \frac{B (b c - a d)^2 g^3 i n (a + b x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{30 b^2 d} - \frac{B (b c - a d) g^3 i n (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{10 b^2} + \\ \frac{(b c - a d) g^3 i (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{20 b^2} + \frac{g^3 i (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{5 b} + \\ \frac{B (b c - a d)^3 g^3 i n (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{60 b^2 d^2} - \frac{B (b c - a d)^4 g^3 i n (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{60 b^2 d^3} - \\ \frac{B (b c - a d)^5 g^3 i n \left(6 A + 11 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{60 b^2 d^4} - \frac{B^2 (b c - a d)^5 g^3 i n^2 \operatorname{Log}[c + d x]}{10 b^2 d^4} - \frac{B^2 (b c - a d)^5 g^3 i n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{10 b^2 d^4}$$

Result (type 4, 3427 leaves):

$$\frac{1}{60 b^2 d^4} \\ g^3 i \left(-6 b^5 B^2 c^5 n^2 + 36 a b^4 B^2 c^4 d n^2 - 90 a^2 b^3 B^2 c^3 d^2 n^2 + 90 a^3 b^2 B^2 c^2 d^3 n^2 - 24 a^4 b B^2 c d^4 n^2 - 6 a^5 B^2 d^5 n^2 + 60 a^3 A^2 b^2 c d^4 x - 6 A b^5 B c^4 d n x + \right. \\ 30 a A b^4 B c^3 d^2 n x - 60 a^2 A b^3 B c^2 d^3 n x + 30 a^3 A b^2 B c d^4 n x + 6 a^4 A b B d^5 n x + b^5 B^2 c^4 d n^2 x - 8 a b^4 B^2 c^3 d^2 n^2 x + 24 a^2 b^3 B^2 c^2 d^3 n^2 x - \\ 28 a^3 b^2 B^2 c d^4 n^2 x + 11 a^4 b B^2 d^5 n^2 x + 90 a^2 A^2 b^3 c d^4 x^2 + 30 a^3 A^2 b^2 d^5 x^2 + 3 A b^5 B c^3 d^2 n x^2 - 15 a A b^4 B c^2 d^3 n x^2 - 15 a^2 A b^3 B c d^4 n x^2 + \\ 27 a^3 A b^2 B d^5 n x^2 - 2 b^5 B^2 c^3 d^2 n^2 x^2 + 12 a b^4 B^2 c^2 d^3 n^2 x^2 - 18 a^2 b^3 B^2 c d^4 n^2 x^2 + 8 a^3 b^2 B^2 d^5 n^2 x^2 + 60 a A^2 b^4 c d^4 x^3 + 60 a^2 A^2 b^3 d^5 x^3 - \\ 2 A b^5 B c^2 d^3 n x^3 - 20 a A b^4 B c d^4 n x^3 + 22 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 15 A^2 b^5 c d^4 x^4 + \\ 45 a A^2 b^4 d^5 x^4 - 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 30 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\ 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 15 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right.$$

$$\begin{aligned}
& 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 3 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 15 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 30 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 30 a^4 A b B c d^4 n \operatorname{Log}[a + b x] - 6 a^5 A B d^5 n \operatorname{Log}[a + b x] - 3 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[a + b x] + 13 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[a + b x] + \\
& a^4 b B^2 c d^4 n^2 \operatorname{Log}[a + b x] - 11 a^5 B^2 d^5 n^2 \operatorname{Log}[a + b x] - 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 120 a^3 A b^2 B c d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 30 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 60 a^2 b^3 B^2 c^2 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 30 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 3 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 15 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 15 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 27 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 20 a b^4 B^2 c d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 22 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 30 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 90 a A b^4 B d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 30 a^4 b B^2 c d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^5 B^2 d^5 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 90 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 60 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 15 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 45 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 6 A b^5 B c^5 n \operatorname{Log}[c + d x] - 30 a A b^4 B c^4 d n \operatorname{Log}[c + d x] + 60 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[c + d x] - 60 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[c + d x] - b^5 B^2 c^5 n^2 \operatorname{Log}[c + d x] + \\
& 11 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c + d x] - 37 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c + d x] + 27 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c + d x] - 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
& 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 30 a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + \\
& 60 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 60 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] -
\end{aligned}$$

$$30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] +$$

$$6 b^2 B^2 c^2 (b^3 c^3 - 5 a b^2 c^2 d + 10 a^2 b c d^2 - 10 a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 a^4 B^2 d^4 (-5 b c + a d) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]$$

Problem 160: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 (c i + d i x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 487 leaves, 10 steps):

$$-\frac{B^2 (bc-ad)^3 g^2 i n^2 x}{3 b d^2} + \frac{B^2 (bc-ad)^2 g^2 i n^2 (c+dx)^2}{12 d^3} - \frac{B (bc-ad)^2 g^2 i n (a+bx)^2 (A+B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right])}{12 b^2 d} -$$

$$\frac{B (bc-ad) g^2 i n (a+bx)^3 (A+B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right])}{6 b^2} + \frac{(bc-ad) g^2 i (a+bx)^3 (A+B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right])^2}{12 b^2} +$$

$$\frac{g^2 i (a+bx)^3 (c+dx) (A+B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right])^2}{4 b} + \frac{B (bc-ad)^3 g^2 i n (a+bx) (2A+Bn+2B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right])}{12 b^2 d^2} +$$

$$\frac{B (bc-ad)^4 g^2 i n (2A+3Bn+2B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right]) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)} \right]}{12 b^2 d^3} + \frac{B^2 (bc-ad)^4 g^2 i n^2 \operatorname{Log}[c+dx]}{6 b^2 d^3} + \frac{B^2 (bc-ad)^4 g^2 i n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{6 b^2 d^3}$$

Result (type 4, 2520 leaves):

$$\frac{1}{12 b^2 d^3} g^2 i \left(2 b^4 B^2 c^4 n^2 - 10 a b^3 B^2 c^3 d n^2 + 12 a^2 b^2 B^2 c^2 d^2 n^2 - 2 a^3 b B^2 c d^3 n^2 - 2 a^4 B^2 d^4 n^2 + 12 a^2 A^2 b^2 c d^3 x + 2 A b^4 B c^3 d n x - 8 a A b^3 B c^2 d^2 n x + \right.$$

$$4 a^2 A b^2 B c d^3 n x + 2 a^3 A b B d^4 n x - b^4 B^2 c^3 d n^2 x + 5 a b^3 B^2 c^2 d^2 n^2 x - 7 a^2 b^2 B^2 c d^3 n^2 x + 3 a^3 b B^2 d^4 n^2 x + 12 a A^2 b^3 c d^3 x^2 +$$

$$6 a^2 A^2 b^2 d^4 x^2 - A b^4 B c^2 d^2 n x^2 - 4 a A b^3 B c d^3 n x^2 + 5 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 +$$

$$4 A^2 b^4 c d^3 x^3 + 8 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 + 2 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 8 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] +$$

$$4 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 4 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] +$$

$$8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 4 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 4 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 +$$

$$6 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 8 a^3 A b B c d^3 n \operatorname{Log}[a+bx] - 2 a^4 A B d^4 n \operatorname{Log}[a+bx] + a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a+bx] +$$

$$2 a^3 b B^2 c d^3 n^2 \operatorname{Log}[a+bx] - 3 a^4 B^2 d^4 n^2 \operatorname{Log}[a+bx] - 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+bx] + 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a+bx] +$$

$$8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+bx] - 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a+bx] - 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] +$$

$$\begin{aligned}
& 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 24 a^2 A b^2 B c d^3 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \\
& 8 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 4 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 12 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 4 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 5 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 8 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 16 a A b^3 B d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 8 a^3 b B^2 c d^3 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 a^4 B^2 d^4 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 12 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 6 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 4 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 8 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 2 A b^4 B c^4 n \operatorname{Log}[c+dx] + 8 a A b^3 B c^3 d n \operatorname{Log}[c+dx] - \\
& 12 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[c+dx] + b^4 B^2 c^4 n^2 \operatorname{Log}[c+dx] - 6 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+dx] + 5 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+dx] + \\
& 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] - 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] - \\
& 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] + 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - \\
& 2 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] + 8 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - 12 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - \\
& 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 2 b^2 B^2 c^2 (b^2 c^2 - 4 a b c d + 6 a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 a^3 B^2 d^3 (-4 b c + a d) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 161: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)(ci + dix) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 372 leaves, 9 steps):

$$\frac{B^2 (bc - ad)^2 g i n^2 x}{3 b d} - \frac{B (bc - ad)^2 g i n (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b^2 d} - \frac{B (bc - ad) g i n (a + b x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{3 b^2} +$$

$$\frac{(bc - ad) g i (a + b x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{6 b^2} + \frac{g i (a + b x)^2 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{3 b} -$$

$$\frac{B (bc - ad)^3 g i n \left(A + B n + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[\frac{bc - ad}{b(c + d x)} \right]}{3 b^2 d^2} - \frac{B^2 (bc - ad)^3 g i n^2 \operatorname{Log}[c + d x]}{3 b^2 d^2} - \frac{B^2 (bc - ad)^3 g i n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)} \right]}{3 b^2 d^2}$$

Result (type 4, 1606 leaves):

$$\frac{1}{6 b^2 d^2} g i \left(-2 b^3 B^2 c^3 n^2 + 2 a b^2 B^2 c^2 d n^2 + 2 a^2 b B^2 c d^2 n^2 - 2 a^3 B^2 d^3 n^2 + 6 a A^2 b^2 c d^2 x - 2 A b^3 B c^2 d n x + 2 a^2 A b B d^3 n x + \right.$$

$$2 b^3 B^2 c^2 d n^2 x - 4 a b^2 B^2 c d^2 n^2 x + 2 a^2 b B^2 d^3 n^2 x + 3 A^2 b^3 c d^2 x^2 + 3 a A^2 b^2 d^3 x^2 - 2 A b^3 B c d^2 n x^2 + 2 a A b^2 B d^3 n x^2 + 2 A^2 b^3 d^3 x^3 -$$

$$2 a b^2 B^2 c^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + 2 a^3 B^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + 3 a^2 b B^2 c d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 - a^3 B^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 + 2 b^3 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] -$$

$$2 a^2 b B^2 c d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - b^3 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 3 a b^2 B^2 c^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 6 a^2 A b B c d^2 n \operatorname{Log}[a + b x] - 2 a^3 A B d^3 n \operatorname{Log}[a + b x] +$$

$$2 a^2 b B^2 c d^2 n^2 \operatorname{Log}[a + b x] - 2 a^3 B^2 d^3 n^2 \operatorname{Log}[a + b x] - 6 a^2 b B^2 c d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 2 a^3 B^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] +$$

$$6 a^2 b B^2 c d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 2 a^3 B^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 6 a^2 b B^2 c d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d} \right] +$$

$$2 a^3 B^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d} \right] + 12 a A b^2 B c d^2 x \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 2 b^3 B^2 c^2 d n x \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] +$$

$$2 a^2 b B^2 d^3 n x \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 6 A b^3 B c d^2 x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 6 a A b^2 B d^3 x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - 2 b^3 B^2 c d^2 n x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] +$$

$$2 a b^2 B^2 d^3 n x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 4 A b^3 B d^3 x^3 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 6 a^2 b B^2 c d^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] -$$

$$2 a^3 B^2 d^3 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 6 a b^2 B^2 c d^2 x \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + 3 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 +$$

$$3 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + 2 b^3 B^2 d^3 x^3 \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + 2 A b^3 B c^3 n \operatorname{Log}[c + d x] - 6 a A b^2 B c^2 d n \operatorname{Log}[c + d x] -$$

$$2 b^3 B^2 c^3 n^2 \operatorname{Log}[c + d x] + 2 a b^2 B^2 c^2 d n^2 \operatorname{Log}[c + d x] - 2 b^3 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] + 6 a b^2 B^2 c^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] +$$

$$2 b^3 B^2 c^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] - 6 a b^2 B^2 c^2 d n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] + 2 b^3 B^2 c^3 n \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log}[c + d x] -$$

$$6 a b^2 B^2 c^2 d n \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log}[c + d x] + 2 b^3 B^2 c^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d} \right] - 6 a b^2 B^2 c^2 d n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d} \right] +$$

$$2 b^2 B^2 c^2 (b c - 3 a d) n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d} \right] + 2 a^2 B^2 d^2 (-3 b c + a d) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d} \right] \Big)$$

Problem 162: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 220 leaves, 7 steps):

$$\begin{aligned} & - \frac{B (b c - a d) i n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{b^2} + \frac{i (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 d} + \\ & \frac{B^2 (b c - a d)^2 i n^2 \operatorname{Log}[c + d x]}{b^2 d} + \frac{B (b c - a d)^2 i n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 i n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} \end{aligned}$$

Result (type 4, 941 leaves):

$$\begin{aligned} & \frac{1}{2 b^2 d} i \left(-2 b^2 B^2 c^2 n^2 + 4 a b B^2 c d n^2 - 2 a^2 B^2 d^2 n^2 + 2 A^2 b^2 c d x - 2 A b^2 B c d n x + 2 a A b B d^2 n x + A^2 b^2 d^2 x^2 - 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \\ & 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 2 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\ & b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 4 a A b B c d n \operatorname{Log}[a + b x] - 2 a^2 A B d^2 n \operatorname{Log}[a + b x] - 4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + \\ & 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[a + b x] - \\ & 4 a b B^2 c d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 4 A b^2 B c d x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - \\ & 2 b^2 B^2 c d n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 a b B^2 d^2 n x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 A b^2 B d^2 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 4 a b B^2 c d n \operatorname{Log}[a + b x] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - \\ & 2 a^2 B^2 d^2 n \operatorname{Log}[a + b x] \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] + 2 b^2 B^2 c d x \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 + b^2 B^2 d^2 x^2 \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 - 2 A b^2 B c^2 n \operatorname{Log}[c + d x] + \\ & 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log}[c + d x] - \\ & \left. 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] - 2 b^2 B^2 c^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a B^2 d (-2 b c + a d) n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \end{aligned}$$

Problem 163: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 306 leaves, 8 steps):

$$\begin{aligned}
& \frac{d \operatorname{Li}(a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{b^2 g} + \frac{2B(bc-ad) \operatorname{Li}\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{b^2 g} - \frac{(bc-ad) \operatorname{Li}\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b^2 g} + \\
& \frac{2B^2(bc-ad) \operatorname{Li}^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^2 g} + \frac{2B(bc-ad) \operatorname{Li}\left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^2 g} + \frac{2B^2(bc-ad) \operatorname{Li}^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b^2 g}
\end{aligned}$$

Result (type 4, 1354 leaves):

$$\begin{aligned}
& \frac{1}{3 b^2 g} i \left(3 b d x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + 3 (b c - a d) \operatorname{Log} [a + b x] \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 - \right. \\
& 3 B n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] (1 + \operatorname{Log} [a + b x]) + \right. \\
& 2 \left(-b c + a d + \operatorname{Log} \left[\frac{c}{d} + x \right] \left(b c + a d \operatorname{Log} [a + b x] - a d \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) + (-b d x + a d \operatorname{Log} [a + b x]) \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) - \\
& 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \left. + 3 b B c n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right. \\
& \left. \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 \operatorname{Log} [a + b x] \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) - \\
& B^2 n^2 \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^3 - 3 d (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) - 3 b (c + d x) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) - \right. \\
& 3 d (b x - a \operatorname{Log} [a + b x]) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + 6 \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log} [c + d x] + \right. \\
& \left. \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) + d (a + b x) \operatorname{Log} \left[\frac{c}{d} + x \right] + (b c - a d) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-2 b c + 2 a d - 2 d (a + b x) \operatorname{Log} \left[\frac{a}{b} + x \right] + a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \right. \\
& \left. 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \left(b (c + d x) - a d \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) - \\
& 3 a d \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& 3 a d \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \right) \left. \right) + \\
& b B^2 c n^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 3 \operatorname{Log} [a + b x] \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \right. \\
& 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(-\operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \left. \right) - \\
& 6 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \left. \right) \left. \right)
\end{aligned}$$

Problem 164: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(a g + b g x)^2} dx$$

Optimal (type 4, 261 leaves, 7 steps):

$$\frac{2 B^2 i n^2 (c + d x)}{b g^2 (a + b x)} - \frac{2 B i n (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{b g^2 (a + b x)} - \frac{i (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b g^2 (a + b x)}$$

$$\frac{d i \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^2 g^2} + \frac{2 B d i n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^2 g^2} + \frac{2 B^2 d i n^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^2 g^2}$$

Result (type 4, 1315 leaves):

$$\frac{1}{3 b^2 g^2} i \left(- \frac{3 (b c - a d) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2}{a + b x} + \right.$$

$$3 d \operatorname{Log}[a + b x] \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 + \frac{1}{(b c - a d) (a + b x)} 6 b B c n \left(-A - B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)$$

$$\left(-d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] + (b c - a d) \left(1 + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right) - \frac{1}{(b c - a d) (a + b x)}$$

$$3 b B^2 c n^2 \left(2 b c - 2 a d + 2 d (a + b x) \operatorname{Log}[a + b x] + 2 (b c - a d) \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] + b (c + d x) \operatorname{Log}\left[\frac{a + b x}{c + d x} \right]^2 - 2 d (a + b x) \operatorname{Log}[c + d x] \right) +$$

$$3 B d n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)$$

$$\left(\operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \frac{2 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{a + b x} + 2 \left(\frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) + \right.$$

$$\left. \frac{2 a \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right)}{(b c - a d) (a + b x)} - 2 \left(\operatorname{Log}\left[\frac{c}{d} + x \right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) +$$

$$B^2 d n^2 \left(\operatorname{Log}\left[\frac{a}{b} + x \right]^3 + \frac{3 a \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{a}{b} + x \right]^2 \right)}{a + b x} + 3 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] + \right.$$

$$\left. \frac{3 \left(a + (a + b x) \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2}{a + b x} - \right.$$

$$\begin{aligned}
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \frac{1}{(bc-ad)(a+bx)} \\
& 3a \left(d(a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) (\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]) \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \\
& \quad \left. \left((bc-ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2d(a+bx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
& \frac{1}{(bc-ad)(a+bx)} 3a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d} + x\right] - 2d(a+bx) \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2d(a+bx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
& 3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \\
& \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2a(1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{a+bx} + \frac{2a \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) (\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]) \right)}{(bc-ad)(a+bx)} - \right. \\
& \quad \left. 2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) - 6 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \Bigg)
\end{aligned}$$

Problem 165: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci+di x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ag+bg x)^3} dx$$

Optimal (type 3, 151 leaves, 3 steps):

$$-\frac{B^2 i n^2 (c+dx)^2}{4(bc-ad)g^3(a+bx)^2} - \frac{B i n (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2(bc-ad)g^3(a+bx)^2} - \frac{i(c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2(bc-ad)g^3(a+bx)^2}$$

Result (type 3, 582 leaves):

$$\begin{aligned}
& - \frac{1}{4 b^2 (b c - a d) g^3 (a + b x)^2} \\
& i \left(2 b^2 B^2 n^2 (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B d^2 n (a + b x)^2 \operatorname{Log}[a + b x] \left(2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
& \quad 2 B (b c - a d) n (a d + b (c + 2 d x)) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left(2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + (b c - a d)^2 \left(2 A^2 + 2 A B n + B^2 n^2 + \right. \\
& \quad \left. 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \left. \right) + \\
& \quad 2 d (b c - a d) (a + b x) \left(2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
& \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - 2 B d^2 n (a + b x)^2 \left(2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \operatorname{Log}[c + d x] \left. \right)
\end{aligned}$$

Problem 166: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(a g + b g x)^4} dx$$

Optimal (type 3, 307 leaves, 7 steps):

$$\begin{aligned}
& \frac{B^2 d i n^2 (c + d x)^2}{4 (b c - a d)^2 g^4 (a + b x)^2} - \frac{2 b B^2 i n^2 (c + d x)^3}{27 (b c - a d)^2 g^4 (a + b x)^3} + \frac{B d i n (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{2 (b c - a d)^2 g^4 (a + b x)^2} - \\
& \frac{2 b B i n (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{9 (b c - a d)^2 g^4 (a + b x)^3} + \frac{d i (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{2 (b c - a d)^2 g^4 (a + b x)^2} - \frac{b i (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{3 (b c - a d)^2 g^4 (a + b x)^3}
\end{aligned}$$

Result (type 3, 1015 leaves):

$$\begin{aligned}
& \frac{1}{g^4} i \left(\frac{B^2 n^2 (-2 b c^3 + 3 a c^2 d - 3 b c^2 d x + 6 a c d^2 x + 3 a d^3 x^2 + b d^3 x^3) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2}{6 (-bc+ad)^2 (a+bx)^3} + \right. \\
& \frac{B d^2 n (6 A + 5 B n + 6 B (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}]))}{18 b^2 (bc-ad) (a+bx)} + \frac{B d^3 n \operatorname{Log} [a+bx] (6 A + 5 B n + 6 B (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}]))}{18 b^2 (bc-ad)^2} + \\
& \frac{1}{18 b^2 (bc-ad) (a+bx)^3} B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \left(-12 A b^2 c^2 + 6 a A b c d + 6 a^2 A d^2 - 4 b^2 B c^2 n + 5 a b B c d n + 5 a^2 B d^2 n - \right. \\
& 18 A b^2 c d x + 18 a A b d^2 x - 3 b^2 B c d n x + 15 a b B d^2 n x + 6 b^2 B d^2 n x^2 - 12 b^2 B c^2 (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + \\
& 6 a b B c d (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + 6 a^2 B d^2 (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) - \\
& 18 b^2 B c d x (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + 18 a b B d^2 x (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) \left. - \frac{1}{27 b^2 (a+bx)^3} \right) \\
& (bc-ad) \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 18 A B (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + 6 B^2 n (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + \right. \\
& 9 B^2 (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}]))^2 \left. - \frac{1}{36 b^2 (a+bx)^2} \right) \\
& d \left(18 A^2 + 6 A B n - B^2 n^2 + 36 A B (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + 6 B^2 n (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) + \right. \\
& \left. 18 B^2 (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}]))^2 - \frac{B d^3 n (6 A + 5 B n + 6 B (\operatorname{Log} [e (\frac{a+bx}{c+dx})^n] - n \operatorname{Log} [\frac{a+bx}{c+dx}])) \operatorname{Log} [c+dx]}{18 b^2 (bc-ad)^2} \right)
\end{aligned}$$

Problem 168: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^3 (c i + d i x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 766 leaves, 17 steps):

$$\begin{aligned}
& \frac{3 B^2 (b c - a d)^5 g^3 i^2 n^2 x}{20 b^2 d^3} + \frac{B^2 (b c - a d)^2 g^3 i^2 n^2 (a + b x)^4}{60 b^3} - \frac{3 B^2 (b c - a d)^4 g^3 i^2 n^2 (c + d x)^2}{40 b d^4} + \\
& \frac{B^2 (b c - a d)^3 g^3 i^2 n^2 (c + d x)^3}{60 d^4} - \frac{B (b c - a d)^3 g^3 i^2 n (a + b x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{90 b^3 d} - \\
& \frac{B (b c - a d)^2 g^3 i^2 n (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{20 b^3} - \frac{B (b c - a d) g^3 i^2 n (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{15 b^2} + \\
& \frac{(b c - a d)^2 g^3 i^2 (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{60 b^3} + \frac{(b c - a d) g^3 i^2 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{15 b^2} + \\
& \frac{g^3 i^2 (a + b x)^4 (c + d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{6 b} + \frac{B (b c - a d)^4 g^3 i^2 n (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{180 b^3 d^2} - \\
& \frac{B (b c - a d)^5 g^3 i^2 n (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{180 b^3 d^3} - \frac{B (b c - a d)^6 g^3 i^2 n \left(6 A + 11 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)} \right]}{180 b^3 d^4} - \\
& \frac{B^2 (b c - a d)^6 g^3 i^2 n^2 \operatorname{Log}[c + d x]}{20 b^3 d^4} - \frac{B^2 (b c - a d)^6 g^3 i^2 n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{30 b^3 d^4}
\end{aligned}$$

Result (type 4, 4611 leaves):

$$\begin{aligned}
& \frac{1}{360 b^3 d^4} g^3 i^2 \\
& \left(-12 b^6 B^2 c^6 n^2 + 84 a b^5 B^2 c^5 d n^2 - 252 a^2 b^4 B^2 c^4 d^2 n^2 + 240 a^3 b^3 B^2 c^3 d^3 n^2 + 12 a^4 b^2 B^2 c^2 d^4 n^2 - 84 a^5 b B^2 c d^5 n^2 + 12 a^6 B^2 d^6 n^2 + 360 a^3 A^2 b^3 c^2 d^4 x - \right. \\
& 12 A b^6 B c^5 d n x + 72 a A b^5 B c^4 d^2 n x - 180 a^2 A b^4 B c^3 d^3 n x + 60 a^3 A b^3 B c^2 d^4 n x + 72 a^4 A b^2 B c d^5 n x - 12 a^5 A b B d^6 n x + 8 b^6 B^2 c^5 d n^2 x - \\
& 54 a b^5 B^2 c^4 d^2 n^2 x + 154 a^2 b^4 B^2 c^3 d^3 n^2 x - 194 a^3 b^3 B^2 c^2 d^4 n^2 x + 102 a^4 b^2 B^2 c d^5 n^2 x - 16 a^5 b B^2 d^6 n^2 x + 540 a^2 A^2 b^4 c^2 d^4 x^2 + \\
& 360 a^3 A^2 b^3 c d^5 x^2 + 6 A b^6 B c^4 d^2 n x^2 - 36 a A b^5 B c^3 d^3 n x^2 - 180 a^2 A b^4 B c^2 d^4 n x^2 + 204 a^3 A b^3 B c d^5 n x^2 + 6 a^4 A b^2 B d^6 n x^2 - 7 b^6 B^2 c^4 d^2 n^2 x^2 + \\
& 46 a b^5 B^2 c^3 d^3 n^2 x^2 - 60 a^2 b^4 B^2 c^2 d^4 n^2 x^2 + 10 a^3 b^3 B^2 c d^5 n^2 x^2 + 11 a^4 b^2 B^2 d^6 n^2 x^2 + 360 a A^2 b^5 c^2 d^4 x^3 + 720 a^2 A^2 b^4 c d^5 x^3 + 120 a^3 A^2 b^3 d^6 x^3 - \\
& 4 A b^6 B c^3 d^3 n x^3 - 156 a A b^5 B c^2 d^4 n x^3 + 84 a^2 A b^4 B c d^5 n x^3 + 76 a^3 A b^3 B d^6 n x^3 + 6 b^6 B^2 c^3 d^3 n^2 x^3 + 6 a b^5 B^2 c^2 d^4 n^2 x^3 - 30 a^2 b^4 B^2 c d^5 n^2 x^3 + \\
& 18 a^3 b^3 B^2 d^6 n^2 x^3 + 90 A^2 b^6 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 + 270 a^2 A^2 b^4 d^6 x^4 - 42 A b^6 B c^2 d^4 n x^4 - 36 a A b^5 B c d^5 n x^4 + 78 a^2 A b^4 B d^6 n x^4 + \\
& 6 b^6 B^2 c^2 d^4 n^2 x^4 - 12 a b^5 B^2 c d^5 n^2 x^4 + 6 a^2 b^4 B^2 d^6 n^2 x^4 + 144 A^2 b^6 c d^5 x^5 + 216 a A^2 b^5 d^6 x^5 - 24 A b^6 B c d^5 n x^5 + 24 a A b^5 B d^6 n x^5 + \\
& 60 A^2 b^6 d^6 x^6 - 12 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + 72 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] - 180 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + 60 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + \\
& 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] - 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right] + 90 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 - 36 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 + 6 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 + \\
& 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] + 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - 60 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - \\
& 72 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] + 12 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right] - 6 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 36 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 - \\
& 90 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 120 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x \right]^2 + 180 a^4 A b^2 B c^2 d^4 n \operatorname{Log}[a + b x] - 72 a^5 A b B c d^5 n \operatorname{Log}[a + b x] +
\end{aligned}$$

$$\begin{aligned}
& 12 a^6 A B d^6 n \operatorname{Log}[a + b x] - 6 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[a + b x] + 32 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[a + b x] + 66 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[a + b x] - \\
& 108 a^5 b B^2 c d^5 n^2 \operatorname{Log}[a + b x] + 16 a^6 B^2 d^6 n^2 \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 720 a^3 A b^3 B c^2 d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 12 b^6 B^2 c^5 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 72 a b^5 B^2 c^4 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 180 a^2 b^4 B^2 c^3 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 a^3 b^3 B^2 c^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 72 a^4 b^2 B^2 c d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 12 a^5 b B^2 d^6 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 720 a^3 A b^3 B c d^5 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 b^6 B^2 c^4 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a b^5 B^2 c^3 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 180 a^2 b^4 B^2 c^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 204 a^3 b^3 B^2 c d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^4 b^2 B^2 d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 720 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1440 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 240 a^3 A b^3 B d^6 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 4 b^6 B^2 c^3 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 156 a b^5 B^2 c^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 84 a^2 b^4 B^2 c d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 76 a^3 b^3 B^2 d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 540 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 42 b^6 B^2 c^2 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a b^5 B^2 c d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 78 a^2 b^4 B^2 d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 288 A b^6 B c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 432 a A b^5 B d^6 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 24 b^6 B^2 c d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 24 a b^5 B^2 d^6 n x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 A b^6 B d^6 x^6 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^4 b^2 B^2 c^2 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 72 a^5 b B^2 c d^5 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 a^6 B^2 d^6 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 360 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 360 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 360 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 720 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 120 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 90 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 270 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 144 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 216 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 A b^6 B c^6 n \operatorname{Log}[c + d x] - 72 a A b^5 B c^5 d n \operatorname{Log}[c + d x] + \\
& 180 a^2 A b^4 B c^4 d^2 n \operatorname{Log}[c + d x] - 240 a^3 A b^3 B c^3 d^3 n \operatorname{Log}[c + d x] - 8 b^6 B^2 c^6 n^2 \operatorname{Log}[c + d x] + 60 a b^5 B^2 c^5 d n^2 \operatorname{Log}[c + d x] -
\end{aligned}$$

$$\begin{aligned}
& 186 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[c + dx] + 128 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[c + dx] + 6 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[c + dx] - 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] + \\
& 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] - 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] + 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + dx] + \\
& 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] + 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] - \\
& 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + dx] + 12 b^6 B^2 c^6 n \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \operatorname{Log}[c + dx] - 72 a b^5 B^2 c^5 d n \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \operatorname{Log}[c + dx] + \\
& 180 a^2 b^4 B^2 c^4 d^2 n \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \operatorname{Log}[c + dx] - 240 a^3 b^3 B^2 c^3 d^3 n \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \operatorname{Log}[c + dx] + \\
& 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] - \\
& 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + dx)}{bc - ad}\right] + 12 b^3 B^2 c^3 (b^3 c^3 - 6 a b^2 c^2 d + 15 a^2 b c d^2 - 20 a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] - \\
& 12 a^4 B^2 d^4 (15 b^2 c^2 - 6 a b c d + a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]
\end{aligned}$$

Problem 169: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^2 (ci + dix)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]\right)^2 dx$$

Optimal (type 4, 819 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B^2 (bc - ad)^4 g^2 i^2 n^2 x}{10 b^2 d^2} - \frac{B^2 (bc - ad)^3 g^2 i^2 n^2 (c + dx)^2}{20 b d^3} + \frac{B^2 (bc - ad)^2 g^2 i^2 n^2 (c + dx)^3}{30 d^3} - \\
& \frac{B (bc - ad)^3 g^2 i^2 n (a + bx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{30 b^3 d} - \frac{B (bc - ad)^2 g^2 i^2 n (a + bx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{15 b^3} - \\
& \frac{B (bc - ad)^3 g^2 i^2 n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{5 b d^3} + \frac{4 B (bc - ad)^2 g^2 i^2 n (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{15 d^3} - \\
& \frac{b B (bc - ad) g^2 i^2 n (c + dx)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{10 d^3} + \frac{(bc - ad)^2 g^2 i^2 (a + bx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{30 b^3} + \\
& \frac{(bc - ad) g^2 i^2 (a + bx)^3 (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{10 b^2} + \frac{g^2 i^2 (a + bx)^3 (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{5 b} + \\
& \frac{B (bc - ad)^4 g^2 i^2 n (a + bx) \left(2A + Bn + 2B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{30 b^3 d^2} + \frac{B (bc - ad)^5 g^2 i^2 n \left(2A + 3Bn + 2B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{bc - ad}{b(c + dx)} \right]}{30 b^3 d^3} + \\
& \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{30 b^3 d^3} + \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \operatorname{Log} [c + dx]}{10 b^3 d^3} + \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{15 b^3 d^3}
\end{aligned}$$

Result (type 4, 3366 leaves):

$$\begin{aligned}
& \frac{1}{60 b^3 d^3} \\
& g^2 i^2 \left(4 b^5 B^2 c^5 n^2 - 24 a b^4 B^2 c^4 d n^2 + 20 a^2 b^3 B^2 c^3 d^2 n^2 + 20 a^3 b^2 B^2 c^2 d^3 n^2 - 24 a^4 b B^2 c d^4 n^2 + 4 a^5 B^2 d^5 n^2 + 60 a^2 A^2 b^3 c^2 d^3 x + 4 A b^5 B c^4 d n x - \right. \\
& 20 A A b^4 B c^3 d^2 n x + 20 a^3 A b^2 B c d^4 n x - 4 a^4 A b B d^5 n x - 4 b^5 B^2 c^4 d n^2 x + 22 a b^4 B^2 c^3 d^2 n^2 x - 36 a^2 b^3 B^2 c^2 d^3 n^2 x + 22 a^3 b^2 B^2 c d^4 n^2 x - \\
& 4 a^4 b B^2 d^5 n^2 x + 60 a A^2 b^4 c^2 d^3 x^2 + 60 a^2 A^2 b^3 c d^4 x^2 - 2 A b^5 B c^3 d^2 n x^2 - 30 a A b^4 B c^2 d^3 n x^2 + 30 a^2 A b^3 B c d^4 n x^2 + 2 a^3 A b^2 B d^5 n x^2 + \\
& 3 b^5 B^2 c^3 d^2 n^2 x^2 - 3 a b^4 B^2 c^2 d^3 n^2 x^2 - 3 a^2 b^3 B^2 c d^4 n^2 x^2 + 3 a^3 b^2 B^2 d^5 n^2 x^2 + 20 A^2 b^5 c^2 d^3 x^3 + 80 a A^2 b^4 c d^4 x^3 + 20 a^2 A^2 b^3 d^5 x^3 - \\
& 12 A b^5 B c^2 d^3 n x^3 + 12 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 30 A^2 b^5 c d^4 x^4 + 30 a A^2 b^4 d^5 x^4 - \\
& 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 + 4 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 20 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - \\
& 4 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 20 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 10 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 4 b^5 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \\
& 20 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 20 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 4 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 b^5 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 10 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
& 20 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 40 a^3 A b^2 B c^2 d^3 n \operatorname{Log} [a + bx] - 20 a^4 A b B c d^4 n \operatorname{Log} [a + bx] + 4 a^5 A B d^5 n \operatorname{Log} [a + bx] + \\
& 2 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} [a + bx] + 18 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} [a + bx] - 24 a^4 b B^2 c d^4 n^2 \operatorname{Log} [a + bx] + 4 a^5 B^2 d^5 n^2 \operatorname{Log} [a + bx] - \\
& 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] - 4 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] + \\
& 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] - 20 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] + 4 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] -
\end{aligned}$$

$$\begin{aligned}
& 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 4 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \\
& 120 a^2 A b^3 B c^2 d^3 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 4 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 20 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 20 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 4 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 120 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 120 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 30 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 30 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 40 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 160 a A b^4 B c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 40 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 12 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 12 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 60 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 60 a A b^4 B d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 40 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \\
& 20 a^4 b B^2 c d^4 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 4 a^5 B^2 d^5 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 60 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 20 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 80 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 20 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 30 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 30 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 4 A b^5 B c^5 n \operatorname{Log}[c+dx] + 20 a A b^4 B c^4 d n \operatorname{Log}[c+dx] - 40 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[c+dx] + \\
& 4 b^5 B^2 c^5 n^2 \operatorname{Log}[c+dx] - 24 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c+dx] + 18 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c+dx] + 2 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c+dx] + \\
& 4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] - 20 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + 40 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] + 20 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - 40 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] + 20 a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - 40 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - \\
& 4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 20 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 40 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
& 4 b^3 B^2 c^3 (b^2 c^2 - 5 a b c d + 10 a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 4 a^3 B^2 d^3 (10 b^2 c^2 - 5 a b c d + a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 170: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x) (c i + d i x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 635 leaves, 14 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^3 g i^2 n^2 x}{12 b^2 d} + \frac{B^2 (b c - a d)^2 g i^2 n^2 (c + d x)^2}{12 b d^2} - \\ & \frac{B (b c - a d)^3 g i^2 n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 b^3 d} - \frac{B (b c - a d)^2 g i^2 n (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 b^3} + \\ & \frac{B (b c - a d)^2 g i^2 n (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{4 b d^2} - \frac{B (b c - a d) g i^2 n (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 d^2} + \\ & \frac{(b c - a d)^2 g i^2 (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{12 b^3} + \frac{(b c - a d) g i^2 (a + b x)^2 (c + d x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{6 b^2} + \\ & \frac{g i^2 (a + b x)^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{4 b} - \frac{B (b c - a d)^4 g i^2 n \left(A + B n + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{6 b^3 d^2} - \\ & \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{12 b^3 d^2} - \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{Log} [c + d x]}{4 b^3 d^2} - \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{6 b^3 d^2} \end{aligned}$$

Result (type 4, 2518 leaves):

$$\begin{aligned} & \frac{1}{12 b^3 d^2} g i^2 \left(-2 b^4 B^2 c^4 n^2 - 2 a b^3 B^2 c^3 d n^2 + 12 a^2 b^2 B^2 c^2 d^2 n^2 - 10 a^3 b B^2 c d^3 n^2 + 2 a^4 B^2 d^4 n^2 + 12 a A^2 b^3 c^2 d^2 x - 2 A b^4 B c^3 d n x - 4 a A b^3 B c^2 d^2 n x + \right. \\ & 8 a^2 A b^2 B c d^3 n x - 2 a^3 A b B d^4 n x + 3 b^4 B^2 c^3 d n^2 x - 7 a b^3 B^2 c^2 d^2 n^2 x + 5 a^2 b^2 B^2 c d^3 n^2 x - a^3 b B^2 d^4 n^2 x + 6 A^2 b^4 c^2 d^2 x^2 + \\ & 12 a A^2 b^3 c d^3 x^2 - 5 A b^4 B c^2 d^2 n x^2 + 4 a A b^3 B c d^3 n x^2 + a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + \\ & 8 A^2 b^4 c d^3 x^3 + 4 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 2 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 4 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\ & 8 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 4 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \\ & 2 b^4 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 4 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 8 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 2 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - b^4 B^2 c^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\ & 4 a b^3 B^2 c^3 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 12 a^2 A b^2 B c^2 d^2 n \operatorname{Log} [a + b x] - 8 a^3 A b B c d^3 n \operatorname{Log} [a + b x] + 2 a^4 A B d^4 n \operatorname{Log} [a + b x] + \\ & 5 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} [a + b x] - 6 a^3 b B^2 c d^3 n^2 \operatorname{Log} [a + b x] + a^4 B^2 d^4 n^2 \operatorname{Log} [a + b x] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \\ & 8 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] - 2 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - \\ & 8 a^3 b B^2 c d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] + 2 a^4 B^2 d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \end{aligned}$$

$$\begin{aligned}
& 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 24 a A b^3 B c^2 d^2 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \\
& 2 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 4 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 8 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 12 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 5 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 4 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 16 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 8 a A b^3 B d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + \\
& 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 12 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - \\
& 8 a^3 b B^2 c d^3 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 2 a^4 B^2 d^4 n \operatorname{Log}[a+bx] \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + 12 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 6 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 8 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 4 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + \\
& 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 2 A b^4 B c^4 n \operatorname{Log}[c+dx] - 8 a A b^3 B c^3 d n \operatorname{Log}[c+dx] - 3 b^4 B^2 c^4 n^2 \operatorname{Log}[c+dx] + \\
& 2 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+dx] + a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+dx] - 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c+dx] + \\
& 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] - 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+dx] + 2 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] - \\
& 8 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[c+dx] + 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
& 2 b^3 B^2 c^3 (bc-4ad) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 a^2 B^2 d^2 (6b^2 c^2 - 4ab cd + a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]
\end{aligned}$$

Problem 171: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 361 leaves, 11 steps):

$$\begin{aligned}
& \frac{B^2 (bc-ad)^2 i^2 n^2 x}{3 b^2} - \frac{2 B (bc-ad)^2 i^2 n (a+bx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{3 b^3} - \frac{B (bc-ad) i^2 n (c+dx)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{3 b d} + \\
& \frac{i^2 (c+dx)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{3 d} + \frac{B^2 (bc-ad)^3 i^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]}{3 b^3 d} + \frac{B^2 (bc-ad)^3 i^2 n^2 \operatorname{Log}[c+dx]}{b^3 d} + \\
& \frac{2 B (bc-ad)^3 i^2 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right) \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{3 b^3 d} - \frac{2 B^2 (bc-ad)^3 i^2 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{3 b^3 d}
\end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned}
& i^2 \left(c^2 x \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + c d x^2 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + \\
& \frac{1}{3} d^2 x^3 \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right)^2 + 2 B c^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right] + \frac{(b c - a d) (a d \text{Log} [a + b x] - b c \text{Log} [c + d x])}{b^2 c d - a b d^2} \right) + 2 B d^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]}{6 b^3 d^3} \right) + \\
& 4 B c d n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right] - \frac{1}{2} (b c - a d) \left(\frac{x}{b d} + \frac{a^2 \text{Log} [a + b x]}{b^2 (b c - a d)} - \frac{c^2 \text{Log} [c + d x]}{d^2 (b c - a d)} \right) \right) + \\
& B^2 c^2 n^2 \left(x \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{b d} \left(-a d \text{Log} \left[\frac{a}{b} + x \right]^2 - b c \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 a d \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [a + b x] - 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [a + b x] + \right. \right. \\
& \quad 2 a d \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] - 2 a d \text{Log} [a + b x] \text{Log} \left[\frac{a + b x}{c + d x} \right] - 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [c + d x] + \\
& \quad \left. 2 b c \text{Log} \left[\frac{a + b x}{c + d x} \right] \text{Log} [c + d x] + 2 b c \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b c \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + 2 B^2 c \\
& d n^2 \left(\frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{2 b^2 d^2} \left(-2 d (-b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + a^2 d^2 \text{Log} \left[\frac{a}{b} + x \right]^2 - 2 b (b c - a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + \right. \right. \\
& \quad b^2 c^2 \text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (a^2 d^2 \text{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \text{Log} [c + d x])) - \\
& \quad \left. 2 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 a^2 d^2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + \\
& B^2 d^2 n^2 \left(\frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 - \frac{1}{6 b^3 d^3} \left(4 d (-b c + a d) (b c + a d) (a + b x) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) - 2 a^3 d^3 \text{Log} \left[\frac{a}{b} + x \right]^2 + \right. \right. \\
& \quad 4 b (b c - a d) (b c + a d) (c + d x) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^3 c^3 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (b c - a d) \\
& \quad \left(b x (2 a - b x) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a + b x] \right) + b^2 (b c - a d) \left(d x (-2 c + d x) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \text{Log} [c + d x] \right) - \\
& \quad \left. 2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log} [a + b x] + 2 b^3 c^3 \text{Log} [c + d x]) + \right. \\
& \quad \left. 4 b^3 c^3 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + 4 a^3 d^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 172: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 572 leaves, 15 steps):

$$\begin{aligned} & - \frac{B d (b c - a d) i^2 n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{b^3 g} + \frac{d (b c - a d) i^2 (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b^3 g} + \\ & \frac{i^2 (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 b g} + \frac{2 B (b c - a d)^2 i^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{b^3 g} + \frac{B^2 (b c - a d)^2 i^2 n^2 \operatorname{Log} [c + d x]}{b^3 g} + \\ & \frac{B (b c - a d)^2 i^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} - \frac{(b c - a d)^2 i^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \\ & \frac{2 B^2 (b c - a d)^2 i^2 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^3 g} - \frac{B^2 (b c - a d)^2 i^2 n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \\ & \frac{2 B (b c - a d)^2 i^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} + \frac{2 B^2 (b c - a d)^2 i^2 n^2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g} \end{aligned}$$

Result (type 4, 2784 leaves):

$$\begin{aligned} & \frac{1}{12 b^3 g} i^2 \left(12 b d (2 b c - a d) x \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + \right. \\ & 6 b^2 d^2 x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + 12 (b c - a d)^2 \operatorname{Log} [a + b x] \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - \\ & 24 b B c n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(a d \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log} \left[\frac{a}{b} + x \right] (1 + \operatorname{Log} [a + b x]) + \right. \\ & 2 \left(-b c + a d + \operatorname{Log} \left[\frac{c}{d} + x \right] \left(b c + a d \operatorname{Log} [a + b x] - a d \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) + (-b d x + a d \operatorname{Log} [a + b x]) \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) - \\ & \left. 2 a d \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) + 12 b^2 B c^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \\ & \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 \operatorname{Log} [a + b x] \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) + 6 \\ & B n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(-4 a d^2 (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 a^2 d^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 4 a b d (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + d^2 \right) \end{aligned}$$

$$\begin{aligned}
& \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) - 2 d^2 \left(b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a + b x] \right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \\
& b^2 \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - 4 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) - \\
& 8 b B^2 c n^2 \left(a d \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 3 d (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - 3 b (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \right. \\
& 3 d (b x - a \operatorname{Log}[a + b x]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 + 6 \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) - \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-2 b c + 2 a d - 2 d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
& \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \left(b (c + d x) - a d \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) - \\
& 3 a d \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& 3 a d \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) + \\
& B^2 n^2 \left(4 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 12 a d^2 (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
& 3 d^2 (a + b x) \left(7 a - b x + (-6 a + 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - 12 a b d (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
& 3 b^2 (c + d x) \left(7 c - d x + (-6 c + 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + 6 d^2 (b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a + b x]) \\
& \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 - 6 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-4 a d^2 (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + \right. \\
& \left. 2 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 a b d (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + d^2 (b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x]) \right) + \\
& \left. b^2 \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) - 4 a^2 d^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) + \\
& 6 \left(2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] + b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - a^2 d^2 \operatorname{Log}[a + b x] - b^2 c^2 \operatorname{Log}[c + d x] - \right. \\
& \left. 2 a b c d \operatorname{Log}[c + d x] - \operatorname{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) \right) + \\
& 2 (b^2 c^2 - a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 4 a d \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right.
\end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \Bigg) - \\
& 2a^2 d^2 \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) \Bigg) + \\
& 12a^2 d^2 \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg) + \\
& 4b^2 B^2 c^2 n^2 \left(\text{Log}\left[\frac{a}{b} + x\right]^3 + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}[a+bx] \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + \right. \\
& \left. 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \left(-\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \right. \\
& \left. 3 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(\text{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) - \\
& \left. 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg)
\end{aligned}$$

Problem 173: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci+di x)^2 \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ag+bg x)^2} dx$$

Optimal (type 4, 472 leaves, 11 steps):

$$\begin{aligned}
& -\frac{2B^2(bc-ad)i^2n^2(c+dx)}{b^2g^2(a+bx)} - \frac{2B(bc-ad)i^2n(c+dx)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{b^2g^2(a+bx)} + \frac{d^2i^2(a+bx)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{b^3g^2} \\
& \frac{(bc-ad)i^2(c+dx)\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{b^2g^2(a+bx)} + \frac{2Bd(bc-ad)i^2n\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{b^3g^2} - \\
& \frac{2d(bc-ad)i^2\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2\text{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \frac{2B^2d(bc-ad)i^2n^2\text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^3g^2} + \\
& \frac{4Bd(bc-ad)i^2n\left(A+B\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \frac{4B^2d(bc-ad)i^2n^2\text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2}
\end{aligned}$$

Result (type 4, 3257 leaves):

$$\begin{aligned}
& \frac{d^2 i^2 x \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^2 g^2} + \frac{2 d (bc - ad) i^2 \text{Log} [a + bx] \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^3 g^2} + \frac{1}{b^3 g^2 (a + bx)} \\
& \left(-A^2 b^2 c^2 i^2 + 2 a A^2 b c d i^2 - a^2 A^2 d^2 i^2 - 2 A b^2 B c^2 i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) + 4 a A b B c d i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) - \\
& 2 a^2 A B d^2 i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) - b^2 B^2 c^2 i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + \\
& 2 a b B^2 c d i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - a^2 B^2 d^2 i^2 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + \frac{1}{b (bc - ad) g^2 (a + bx)} \\
& B^2 c^2 i^2 n^2 \left(-2 bc + 2 ad - 2 d (a + bx) \text{Log} [a + bx] + (-2 bc + 2 ad) \text{Log} \left[\frac{a+bx}{c+dx} \right] - b (c + dx) \text{Log} \left[\frac{a+bx}{c+dx} \right]^2 + 2 d (a + bx) \text{Log} [c + dx] \right) + \\
& \frac{1}{g^2} 2 B c^2 i^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \\
& \left(- \frac{\left(\frac{a}{b} + x \right) \left(\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{(a + bx)^2 \text{Log} \left[\frac{a}{b} + x \right]} - \frac{\frac{b \left(\frac{c}{d} + x \right) \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right]}{b} - \frac{-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right]}{b (a + bx)} \right) + \\
& \frac{1}{g^2} 2 B d^2 i^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^2} - \frac{a \text{Log} \left[\frac{a}{b} + x \right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^3 (a + bx)} - \right. \\
& \left. \frac{\left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{b^2} - \frac{a^2 \left((-bc + ad) \text{Log} \left[\frac{c}{d} + x \right] + d (a + bx) \left(\text{Log} [a + bx] - \text{Log} [c + dx] \right) \right)}{b^3 (bc - ad) (a + bx)} \right) + \\
& \left. \frac{\left(bx - \frac{a^2}{a+bx} - 2 a \text{Log} [a + bx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{b^3} + \frac{2 a \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) + \\
& \frac{1}{g^2} 4 B c d i^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \\
& \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^2}{2 b^2} + \frac{a \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^2 (a + bx)} + \frac{a \left((-bc + ad) \text{Log} \left[\frac{c}{d} + x \right] + d (a + bx) \left(\text{Log} [a + bx] - \text{Log} [c + dx] \right) \right)}{b^2 (bc - ad) (a + bx)} \right) + \\
& \left. \frac{\left(\frac{a}{a+bx} + \text{Log} [a + bx] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{b^2} - \frac{\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right]}{b^2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{g^2} B^2 d^2 i^2 n^2 \left(-\frac{2 a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3} + \frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3} - \frac{a^2\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3(a+b x)} + \right. \\
& \frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b^2 d} + \frac{\left(b x-\frac{a^2}{a+b x}-2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2}{b^3} + \\
& \left. \frac{1}{b^3(b c-a d)(a+b x)} a^2\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) + \right. \\
& 2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2}-\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^3}-\frac{a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)} - \right. \\
& \left. \frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^2}-\frac{a^2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^3(b c-a d)(a+b x)} + \right. \\
& \left. \frac{2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3}\right) - 2\left(\frac{1}{b^3 d}\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+ \right. \right. \\
& \left. \left. \operatorname{Log}\left[\frac{a}{b}+x\right]\left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+(b c-a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) + \\
& \frac{1}{2 b^3(b c-a d)(a+b x)} a^2\left(d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) - \\
& 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left((b c-a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-\frac{1}{b^3} \\
& a\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right) - \\
& \left. \frac{2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3}\right) + \\
& \frac{1}{g^2} 2 B^2 c d i^2 n^2 \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^2} + \frac{a\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^2(a+b x)} + \frac{\left(\frac{a}{a+b x}+\operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2}{b^2} - \right. \\
& \frac{1}{b^2(b c-a d)(a+b x)} a\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) + \\
& 2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)\left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^2}+\frac{a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2(a+b x)} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{a \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right) \right)}{b^2 (bc - ad) (a + bx)} - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^2} \Bigg) - \\
& 2 \left(-\frac{1}{2b^2 (bc - ad) (a + bx)} a \left(d(a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right) \right) \right) - \right. \\
& \quad \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((bc - ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \frac{1}{2b^2} \\
& \quad \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) \Bigg) + \\
& \quad \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b^2} \right)
\end{aligned}$$

Problem 174: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci + dix)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ag + bgx)^3} dx$$

Optimal (type 4, 417 leaves, 10 steps):

$$\begin{aligned}
& -\frac{2B^2 d i^2 n^2 (c + dx)}{b^2 g^3 (a + bx)} - \frac{B^2 i^2 n^2 (c + dx)^2}{4 b g^3 (a + bx)^2} - \frac{2 B d i^2 n (c + dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{b^2 g^3 (a + bx)} - \\
& \frac{B i^2 n (c + dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 b g^3 (a + bx)^2} - \frac{d i^2 (c + dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b^2 g^3 (a + bx)} - \frac{i^2 (c + dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 b g^3 (a + bx)^2} - \\
& \frac{d^2 i^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} + \frac{2 B d^2 i^2 n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3} + \frac{2 B^2 d^2 i^2 n^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^3 g^3}
\end{aligned}$$

Result (type 4, 4257 leaves):

$$\begin{aligned}
& \frac{d^2 i^2 \operatorname{Log}[a + bx] \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^3 g^3} + \frac{1}{b^3 g^3 (a + bx)} \\
& 2 \left(-A^2 b c d i^2 + a A^2 d^2 i^2 - 2 A B b c d i^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + 2 a A B d^2 i^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - \right. \\
& \quad \left. b B^2 c d i^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 + a B^2 d^2 i^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 \right) + \frac{1}{2 b^3 g^3 (a + bx)^2}
\end{aligned}$$

$$\begin{aligned}
& \left(-A^2 b^2 c^2 i^2 + 2 a A^2 b c d i^2 - a^2 A^2 d^2 i^2 - 2 A b^2 B c^2 i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) + 4 a A b B c d i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) - \right. \\
& \quad 2 a^2 A B d^2 i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) - b^2 B^2 c^2 i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 + \\
& \quad \left. 2 a b B^2 c d i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 - a^2 B^2 d^2 i^2 \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right)^2 \right) - \\
& \left(B^2 c^2 i^2 n^2 \left(b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a+b x)^2 \text{Log}[a+b x] + 2 (b c - a d) (b c - 3 a d - 2 b d x) \text{Log} \left[\frac{a+b x}{c+d x} \right] + \right. \right. \\
& \quad \left. \left. 2 b (c+d x) (b c - 2 a d - b d x) \text{Log} \left[\frac{a+b x}{c+d x} \right]^2 + 6 a^2 d^2 \text{Log}[c+d x] + 12 a b d^2 x \text{Log}[c+d x] + 6 b^2 d^2 x^2 \text{Log}[c+d x] \right) \right) / \\
& \left(4 b (b c - a d)^2 g^3 (a+b x)^2 \right) + \frac{1}{g^3} 2 B c^2 i^2 n \left(A+B \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \\
& \left(\frac{\left(\frac{a}{b} + x \right) \left(2 \text{Log} \left[\frac{a}{b} + x \right] + 4 \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{8 (a+b x)^3 \text{Log} \left[\frac{a}{b} + x \right]} - \frac{\frac{b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{b c}{d} \right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} - \left(\frac{b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{b c}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{2 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{b c}{d} \right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{\left(-a + \frac{b c}{d} \right)^2}}{2 b} \right. \\
& \left. \frac{-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+d x} + \frac{b x}{c+d x} \right]}{2 b (a+b x)^2} + \frac{1}{g^3} 4 B c d i^2 n \left(A+B \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \right) \\
& \left(-\frac{1 + \text{Log} \left[\frac{a}{b} + x \right]}{b^2 (a+b x)} + \frac{a \left(1 + 2 \text{Log} \left[\frac{a}{b} + x \right] \right)}{4 b^2 (a+b x)^2} - \frac{(-b c + a d) \text{Log} \left[\frac{c}{d} + x \right] + d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x] \right)}{b^2 (b c - a d) (a+b x)} - \right. \\
& \left. \frac{a \left(\text{Log} \left[\frac{c}{d} + x \right] + \frac{d (a+b x) (b c - a d + d (a+b x) \text{Log}[a+b x] - d (a+b x) \text{Log}[c+d x])}{(b c - a d)^2} \right)}{2 b^2 (a+b x)^2} - \frac{(a+2 b x) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)}{2 b^2 (a+b x)^2} \right) + \\
& \frac{1}{g^3} 2 B d^2 i^2 n \left(A+B \left(\text{Log} \left[e \left(\frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[\frac{a+b x}{c+d x} \right] \right) \right) \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^2}{2 b^3} + \frac{2 a \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^3 (a+b x)} - \frac{a^2 \left(1 + 2 \text{Log} \left[\frac{a}{b} + x \right] \right)}{4 b^3 (a+b x)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2a \left((-bc + ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right) \right)}{b^3 (bc - ad)(a + bx)} + \frac{a^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d(a + bx)(bc - ad + d(a + bx) \operatorname{Log}[a + bx] - d(a + bx) \operatorname{Log}[c + dx])}{(bc - ad)^2} \right)}{2b^3 (a + bx)^2} + \\
& \frac{\left(\frac{a(3a + 4bx)}{(a + bx)^2} + 2 \operatorname{Log}[a + bx] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + dx} + \frac{bx}{c + dx} \right] \right)}{2b^3} - \frac{\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right]}{b^3} \Bigg) + \\
& \frac{1}{g^3} 2B^2 c d i^2 n^2 \left(-\frac{2 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{b^2 (a + bx)} + \frac{a \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4b^2 (a + bx)^2} + 2 \left(-\frac{1 + \operatorname{Log} \left[\frac{a}{b} + x \right]}{b^2 (a + bx)} + \frac{a \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{4b^2 (a + bx)^2} - \right. \right. \\
& \left. \left. \frac{(-bc + ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right)}{b^2 (bc - ad)(a + bx)} - \frac{a \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d(a + bx)(bc - ad + d(a + bx) \operatorname{Log}[a + bx] - d(a + bx) \operatorname{Log}[c + dx])}{(bc - ad)^2} \right)}{2b^2 (a + bx)^2} \right) \right) \\
& \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + dx} + \frac{bx}{c + dx} \right] \right) - \frac{(a + 2bx) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + dx} + \frac{bx}{c + dx} \right] \right)^2}{2b^2 (a + bx)^2} - \\
& 2 \left(\frac{1}{2b^2 (bc - ad)(a + bx)} \left(d(a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc + ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d(a + bx) \left(\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx] \right) \right) - \right. \right. \\
& \left. \left. 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \left((bc - ad) \operatorname{Log} \left[\frac{c}{d} + x \right] + d(a + bx) \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] \right) - 2d(a + bx) \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) + \right. \\
& \left(a \left(-d(-bc + ad)(a + bx) + (bc - ad)^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right) \operatorname{Log} \left[\frac{c}{d} + x \right] + d^2 (a + bx)^2 \operatorname{Log}[a + bx] - d^2 (a + bx)^2 \operatorname{Log}[c + dx] + d(a + bx) \right. \right. \\
& \left. \left. \left(d(a + bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2(bc - ad) \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 2d(a + bx) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] \right) \right) \right) \Bigg) / \\
& \left(4b^2 (bc - ad)^2 (a + bx)^2 \right) + \frac{-b(c + dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2d(a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2d(a + bx) \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right]}{b^2 (bc - ad)(a + bx)} + \\
& \left(a \left(b(c + dx) (-2ad + b(c - dx)) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2d^2 (a + bx)^2 \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 2d(a + bx) \operatorname{Log} \left[\frac{c}{d} + x \right] \right. \right. \\
& \left. \left. \left(b(c + dx) + d(a + bx) \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] \right) + 2d^2 (a + bx)^2 \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] \right) \right) / \left(2b^2 (bc - ad)^2 (a + bx)^2 \right) + \\
& \frac{1}{g^3} B^2 d^2 i^2 n^2 \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3b^3} + \frac{2a \left(2 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3 (a + bx)} - \frac{a^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4b^3 (a + bx)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\left(\frac{a(3a+4bx)}{(a+bx)^2} + 2 \operatorname{Log}[a+bx]\right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)^2}{2b^3} - \frac{1}{b^3(bc-ad)(a+bx)} \\
& 2a \left(-b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2d(a+bx) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2d(a+bx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right) - \\
& \left(a^2 \left(b(c+dx)(-2ad+b(c-dx)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2d^2(a+bx)^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
& \quad \left. \left. 2d(a+bx) \operatorname{Log}\left[\frac{c}{d}+x\right] \left(b(c+dx) + d(a+bx) \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]\right) + 2d^2(a+bx)^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)\right) / \\
& \left(2b^3(bc-ad)^2(a+bx)^2\right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right) \\
& \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^3} + \frac{2a(1+\operatorname{Log}\left[\frac{a}{b}+x\right])}{b^3(a+bx)} - \frac{a^2(1+2\operatorname{Log}\left[\frac{a}{b}+x\right])}{4b^3(a+bx)^2} + \frac{2a((-bc+ad)\operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+bx)(\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]))}{b^3(bc-ad)(a+bx)}\right) + \\
& \left.\frac{a^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2b^3(a+bx)^2} - \frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^3}\right) - \\
& 2 \left(-\frac{1}{b^3(bc-ad)(a+bx)} a \left(d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+bx)(\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx])\right)\right) - \right. \\
& \quad \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left((bc-ad) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+bx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) - 2d(a+bx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) - \\
& \left(a^2 \left(-d(-bc+ad)(a+bx) + (bc-ad)^2(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]) \operatorname{Log}\left[\frac{c}{d}+x\right] + d^2(a+bx)^2 \operatorname{Log}[a+bx] - d^2(a+bx)^2 \operatorname{Log}[c+dx] + d(a+bx) \right. \right. \\
& \quad \left. \left. \left(d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2(bc-ad)(1+\operatorname{Log}\left[\frac{a}{b}+x\right]) - 2d(a+bx) \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)\right)\right)\right) / \\
& \left(4b^3(bc-ad)^2(a+bx)^2\right) + \frac{1}{2b^3} \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]\right) + \frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b^3}
\end{aligned}$$

Problem 175: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci+di x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ag+bg x)^4} dx$$

Optimal (type 3, 157 leaves, 3 steps):

$$\frac{2 B^2 i^2 n^2 (c + d x)^3}{27 (b c - a d) g^4 (a + b x)^3} - \frac{2 B i^2 n (c + d x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{9 (b c - a d) g^4 (a + b x)^3} - \frac{i^2 (c + d x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{3 (b c - a d) g^4 (a + b x)^3}$$

Result (type 3, 774 leaves):

$$\frac{1}{27 b^3 (b c - a d) g^4 (a + b x)^3} i^2 \left(9 b^3 B^2 n^2 (c + d x)^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B d^3 n (a + b x)^3 \operatorname{Log}[a + b x] \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\ \left. 6 B (b c - a d) n (a^2 d^2 + a b d (c + 3 d x) + b^2 (c^2 + 3 c d x + 3 d^2 x^2)) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\ \left. (b c - a d)^3 \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \right. \\ \left. \left. 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 3 d (b c - a d)^2 (a + b x) \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \right. \right. \\ \left. \left. 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \right. \\ \left. 3 d^2 (b c - a d) (a + b x)^2 \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \right. \\ \left. \left. 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - 6 B d^3 n (a + b x)^3 \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \operatorname{Log}[c + d x] \right)$$

Problem 176: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{(a g + b g x)^5} dx$$

Optimal (type 3, 319 leaves, 7 steps):

$$\frac{2 B^2 d i^2 n^2 (c + d x)^3}{27 (b c - a d)^2 g^5 (a + b x)^3} - \frac{b B^2 i^2 n^2 (c + d x)^4}{32 (b c - a d)^2 g^5 (a + b x)^4} + \frac{2 B d i^2 n (c + d x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{9 (b c - a d)^2 g^5 (a + b x)^3} - \\ \frac{b B i^2 n (c + d x)^4 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{8 (b c - a d)^2 g^5 (a + b x)^4} + \frac{d i^2 (c + d x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{3 (b c - a d)^2 g^5 (a + b x)^3} - \frac{b i^2 (c + d x)^4 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{4 (b c - a d)^2 g^5 (a + b x)^4}$$

Result (type 3, 982 leaves):

$$\begin{aligned}
& \frac{1}{864 b^3 (bc - ad)^2 g^5 (a + bx)^4} \\
& i^2 \left(-72 b^3 B^2 n^2 (c + dx)^3 (3bc - 4ad - bdx) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 12 B d^3 (bc - ad) n (a + bx)^3 \left(12A + 7Bn + 12B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]\right) \right) + \right. \\
& \quad 12 B d^4 n (a + bx)^4 \operatorname{Log}[a + bx] \left(12A + 7Bn + 12B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]\right) \right) - \\
& \quad 4d (bc - ad)^3 (a + bx) \left(144A^2 + 60ABn + 11B^2 n^2 + 144B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 12Bn (24A + 5Bn) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \quad \left. 144B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 12B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(24A + 5Bn - 24Bn \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
& \quad 6d^2 (bc - ad)^2 (a + bx)^2 \left(72A^2 + 12ABn - 5B^2 n^2 + 72B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 12Bn (12A + Bn) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + 72B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + \right. \\
& \quad \quad 12B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(12A + Bn - 12Bn \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - 27 (bc - ad)^4 \left(8A^2 + 4ABn + B^2 n^2 + 8B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - \right. \\
& \quad \quad \left. 4Bn (4A + Bn) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + 8B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 4B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(4A + Bn - 4Bn \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + 12B (bc - ad) n \\
& \quad \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(12B d^3 n (a + bx)^3 + 6d^2 (-bc + ad) (a + bx)^2 \left(12A + Bn + 12B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 12Bn \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - 9 (bc - ad)^3 \right. \\
& \quad \quad \left(4A + Bn + 4B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 4Bn \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - 4d (bc - ad)^2 (a + bx) \left(24A + 5Bn + 24B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \right) - \\
& \quad \left. 12 B d^4 n (a + bx)^4 \left(12A + 7Bn + 12B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \operatorname{Log}[c + dx] \right)
\end{aligned}$$

Problem 177: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci + dix)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{(ag + bgx)^6} dx$$

Optimal (type 3, 493 leaves, 9 steps):

$$\begin{aligned}
& -\frac{2B^2 d^2 i^2 n^2 (c + dx)^3}{27 (bc - ad)^3 g^6 (a + bx)^3} + \frac{b B^2 d i^2 n^2 (c + dx)^4}{16 (bc - ad)^3 g^6 (a + bx)^4} - \frac{2 b^2 B^2 i^2 n^2 (c + dx)^5}{125 (bc - ad)^3 g^6 (a + bx)^5} - \\
& \frac{2 B d^2 i^2 n (c + dx)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{9 (bc - ad)^3 g^6 (a + bx)^3} + \frac{b B d i^2 n (c + dx)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{4 (bc - ad)^3 g^6 (a + bx)^4} - \frac{2 b^2 B i^2 n (c + dx)^5 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)}{25 (bc - ad)^3 g^6 (a + bx)^5} - \\
& \frac{d^2 i^2 (c + dx)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{3 (bc - ad)^3 g^6 (a + bx)^3} + \frac{b d i^2 (c + dx)^4 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{2 (bc - ad)^3 g^6 (a + bx)^4} - \frac{b^2 i^2 (c + dx)^5 \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right)^2}{5 (bc - ad)^3 g^6 (a + bx)^5}
\end{aligned}$$

Result (type 3, 1107 leaves):

$$\frac{1}{54000 b^3 (bc - ad)^3 g^6 (a + bx)^5} i^2 \left(-1800 b^3 B^2 n^2 (c + dx)^3 (10 a^2 d^2 + 5 a b d (-3 c + dx) + b^2 (6 c^2 - 3 c d x + d^2 x^2)) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + \right.$$

$$30 B d^3 (bc - ad)^2 n (a + bx)^3 \left(60 A - 13 B n + 60 B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]\right) \right) -$$

$$60 B d^4 (bc - ad) n (a + bx)^4 \left(60 A + 47 B n + 60 B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]\right) \right) -$$

$$60 B d^5 n (a + bx)^5 \operatorname{Log}[a + bx] \left(60 A + 47 B n + 60 B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]\right) \right) -$$

$$20 d^2 (bc - ad)^3 (a + bx)^2 \left(900 A^2 + 60 A B n - 43 B^2 n^2 + 900 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - \right.$$

$$60 B n (30 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + 900 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 60 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(30 A + B n - 30 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \left. \right) -$$

$$135 d (bc - ad)^4 (a + bx) \left(200 A^2 + 60 A B n + 7 B^2 n^2 + 200 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 20 B n (20 A + 3 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right.$$

$$200 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 20 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(20 A + 3 B n - 20 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \left. \right) - 432 (bc - ad)^5 \left(25 A^2 + 10 A B n + 2 B^2 n^2 + \right.$$

$$25 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 10 B n (5 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + 25 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 10 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(5 A + B n - 5 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \left. \right) +$$

$$60 B (bc - ad) n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(30 B d^3 (bc - ad) n (a + bx)^3 - 60 B d^4 n (a + bx)^4 + 45 d (-bc + ad)^3 (a + bx) \right.$$

$$\left. \left(20 A + 3 B n + 20 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 20 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - 72 (bc - ad)^4 \left(5 A + B n + 5 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 5 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - \right.$$

$$20 d^2 (bc - ad)^2 (a + bx)^2 \left(30 A + B n + 30 B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \left. \right) +$$

$$60 B d^5 n (a + bx)^5 \left(60 A + 47 B n + 60 B \left(\operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \operatorname{Log}[c + dx] \left. \right)$$

Problem 178: Result more than twice size of optimal antiderivative.

$$\int (ag + bgx)^3 (ci + dix)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 1172 leaves, 22 steps):

$$\begin{aligned}
& \frac{5 B^2 (b c - a d)^6 g^3 i^3 n^2 x}{84 b^3 d^3} + \frac{B^2 (b c - a d)^3 g^3 i^3 n^2 (a + b x)^4}{140 b^4} - \frac{29 B^2 (b c - a d)^5 g^3 i^3 n^2 (c + d x)^2}{840 b^2 d^4} + \\
& \frac{47 B^2 (b c - a d)^4 g^3 i^3 n^2 (c + d x)^3}{1260 b d^4} - \frac{13 B^2 (b c - a d)^3 g^3 i^3 n^2 (c + d x)^4}{420 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i^3 n^2 (c + d x)^5}{105 d^4} - \\
& \frac{B (b c - a d)^4 g^3 i^3 n (a + b x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{210 b^4 d} - \frac{3 B (b c - a d)^3 g^3 i^3 n (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{140 b^4} - \\
& \frac{B (b c - a d)^2 g^3 i^3 n (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{35 b^3} + \frac{2 B (b c - a d)^4 g^3 i^3 n (c + d x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{21 b d^4} - \\
& \frac{3 B (b c - a d)^3 g^3 i^3 n (c + d x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{14 d^4} + \frac{6 b B (b c - a d)^2 g^3 i^3 n (c + d x)^5 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{35 d^4} - \\
& \frac{b^2 B (b c - a d) g^3 i^3 n (c + d x)^6 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{21 d^4} + \frac{(b c - a d)^3 g^3 i^3 (a + b x)^4 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{140 b^4} + \\
& \frac{(b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{35 b^3} + \frac{(b c - a d) g^3 i^3 (a + b x)^4 (c + d x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{14 b^2} + \\
& \frac{g^3 i^3 (a + b x)^4 (c + d x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{7 b} + \frac{B (b c - a d)^5 g^3 i^3 n (a + b x)^2 \left(3 A + B n + 3 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{420 b^4 d^2} - \\
& \frac{B (b c - a d)^6 g^3 i^3 n (a + b x) \left(6 A + 5 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{420 b^4 d^3} - \frac{B (b c - a d)^7 g^3 i^3 n \left(6 A + 11 B n + 6 B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)} \right]}{420 b^4 d^4} - \\
& \frac{B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x} \right]}{210 b^4 d^4} - \frac{11 B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{Log}[c + d x]}{420 b^4 d^4} - \frac{B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{70 b^4 d^4}
\end{aligned}$$

Result (type 4, 5652 leaves):

$$\begin{aligned}
& \frac{1}{2520 b^4 d^4} \\
& g^3 i^3 \left(-36 b^7 B^2 c^7 n^2 + 288 a b^6 B^2 c^6 d n^2 - 1008 a^2 b^5 B^2 c^5 d^2 n^2 + 756 a^3 b^4 B^2 c^4 d^3 n^2 + 756 a^4 b^3 B^2 c^3 d^4 n^2 - 1008 a^5 b^2 B^2 c^2 d^5 n^2 + 288 a^6 b B^2 c d^6 n^2 - \right. \\
& 36 a^7 B^2 d^7 n^2 + 2520 a^3 A^2 b^4 c^3 d^4 x - 36 A b^7 B c^6 d n x + 252 a A b^6 B c^5 d^2 n x - 756 a^2 A b^5 B c^4 d^3 n x + 756 a^4 A b^3 B c^2 d^5 n x - 252 a^5 A b^2 B c d^6 n x + \\
& 36 a^6 A b B d^7 n x + 36 b^7 B^2 c^6 d n^2 x - 270 a b^6 B^2 c^5 d^2 n^2 x + 876 a^2 b^5 B^2 c^4 d^3 n^2 x - 1284 a^3 b^4 B^2 c^3 d^4 n^2 x + 876 a^4 b^3 B^2 c^2 d^5 n^2 x - \\
& 270 a^5 b^2 B^2 c d^6 n^2 x + 36 a^6 b B^2 d^7 n^2 x + 3780 a^2 A^2 b^5 c^3 d^4 x^2 + 3780 a^3 A^2 b^4 c^2 d^5 x^2 + 18 A b^7 B c^5 d^2 n x^2 - 126 a A b^6 B c^4 d^3 n x^2 - \\
& 1512 a^2 A b^5 B c^3 d^4 n x^2 + 1512 a^3 A b^4 B c^2 d^5 n x^2 + 126 a^4 A b^3 B c d^6 n x^2 - 18 a^5 A b^2 B d^7 n x^2 - 27 b^7 B^2 c^5 d^2 n^2 x^2 + 201 a b^6 B^2 c^4 d^3 n^2 x^2 - \\
& 174 a^2 b^5 B^2 c^3 d^4 n^2 x^2 - 174 a^3 b^4 B^2 c^2 d^5 n^2 x^2 + 201 a^4 b^3 B^2 c d^6 n^2 x^2 - 27 a^5 b^2 B^2 d^7 n^2 x^2 + 2520 a A^2 b^6 c^3 d^4 x^3 + 7560 a^2 A^2 b^5 c^2 d^5 x^3 + \\
& 2520 a^3 A^2 b^4 c d^6 x^3 - 12 A b^7 B c^4 d^3 n x^3 - 1176 a A b^6 B c^3 d^4 n x^3 + 1176 a^3 A b^4 B c d^6 n x^3 + 12 a^4 A b^3 B d^7 n x^3 + 22 b^7 B^2 c^4 d^3 n^2 x^3 + \\
& 152 a b^6 B^2 c^3 d^4 n^2 x^3 - 348 a^2 b^5 B^2 c^2 d^5 n^2 x^3 + 152 a^3 b^4 B^2 c d^6 n^2 x^3 + 22 a^4 b^3 B^2 d^7 n^2 x^3 + 630 A^2 b^7 c^3 d^4 x^4 + 5670 a A^2 b^6 c^2 d^5 x^4 + \\
& 5670 a^2 A^2 b^5 c d^6 x^4 + 630 a^3 A^2 b^4 d^7 x^4 - 306 A b^7 B c^3 d^4 n x^4 - 882 a A b^6 B c^2 d^5 n x^4 + 882 a^2 A b^5 B c d^6 n x^4 + 306 a^3 A b^4 B d^7 n x^4 + \\
& 60 b^7 B^2 c^3 d^4 n^2 x^4 - 60 a b^6 B^2 c^2 d^5 n^2 x^4 - 60 a^2 b^5 B^2 c d^6 n^2 x^4 + 60 a^3 b^4 B^2 d^7 n^2 x^4 + 1512 A^2 b^7 c^2 d^5 x^5 + 4536 a A^2 b^6 c d^6 x^5 +
\end{aligned}$$

$$\begin{aligned}
& 1512 a^2 A^2 b^5 d^7 x^5 - 360 A b^7 B c^2 d^5 n x^5 + 360 a^2 A b^5 B d^7 n x^5 + 24 b^7 B^2 c^2 d^5 n^2 x^5 - 48 a b^6 B^2 c d^6 n^2 x^5 + 24 a^2 b^5 B^2 d^7 n^2 x^5 + 1260 A^2 b^7 c d^6 x^6 + \\
& 1260 a A^2 b^6 d^7 x^6 - 120 A b^7 B c d^6 n x^6 + 120 a A b^6 B d^7 n x^6 + 360 A^2 b^7 d^7 x^7 - 36 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 252 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
& 756 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 756 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 252 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 630 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 378 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 126 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 756 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 252 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 126 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 378 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 630 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 1260 a^4 A b^3 B c^3 d^4 n \operatorname{Log}[a + b x] - 756 a^5 A b^2 B c^2 d^5 n \operatorname{Log}[a + b x] + \\
& 252 a^6 A b B c d^6 n \operatorname{Log}[a + b x] - 36 a^7 A B d^7 n \operatorname{Log}[a + b x] - 18 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}[a + b x] + 114 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}[a + b x] + \\
& 642 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}[a + b x] - 990 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}[a + b x] + 288 a^6 b B^2 c d^6 n^2 \operatorname{Log}[a + b x] - 36 a^7 B^2 d^7 n^2 \operatorname{Log}[a + b x] - \\
& 1260 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 756 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 252 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 36 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 1260 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 756 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 252 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 756 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 252 a^6 b B^2 c d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 5040 a^3 A b^4 B c^3 d^4 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 b^7 B^2 c^6 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 252 a b^6 B^2 c^5 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 756 a^2 b^5 B^2 c^4 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 756 a^4 b^3 B^2 c^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 252 a^5 b^2 B^2 c d^6 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 36 a^6 b B^2 d^7 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 7560 a^2 A b^5 B c^3 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 7560 a^3 A b^4 B c^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 18 b^7 B^2 c^5 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 126 a b^6 B^2 c^4 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 1512 a^2 b^5 B^2 c^3 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 1512 a^3 b^4 B^2 c^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 126 a^4 b^3 B^2 c d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 18 a^5 b^2 B^2 d^7 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 5040 a A b^6 B c^3 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 15120 a^2 A b^5 B c^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 5040 a^3 A b^4 B c d^6 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 12 b^7 B^2 c^4 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 1176 a b^6 B^2 c^3 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1176 a^3 b^4 B^2 c d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 12 a^4 b^3 B^2 d^7 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1260 A b^7 B c^3 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 11340 a A b^6 B c^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 11340 a^2 A b^5 B c d^6 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1260 a^3 A b^4 B d^7 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 306 b^7 B^2 c^3 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] -
\end{aligned}$$

$$\begin{aligned}
& 882 a b^6 B^2 c^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 882 a^2 b^5 B^2 c d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 306 a^3 b^4 B^2 d^7 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
& 3024 A b^7 B c^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 9072 a A b^6 B c d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 3024 a^2 A b^5 B d^7 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
& 360 b^7 B^2 c^2 d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 360 a^2 b^5 B^2 d^7 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2520 A b^7 B c d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
& 2520 a A b^6 B d^7 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 120 b^7 B^2 c d^6 n x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 120 a b^6 B^2 d^7 n x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
& 720 A b^7 B d^7 x^7 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 1260 a^4 b^3 B^2 c^3 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 756 a^5 b^2 B^2 c^2 d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
& 252 a^6 b B^2 c d^6 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 36 a^7 B^2 d^7 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2520 a^3 b^4 B^2 c^3 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 3780 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 3780 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2520 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 7560 a^2 b^5 B^2 c^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2520 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 630 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 5670 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 5670 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 630 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 1512 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 4536 a b^6 B^2 c d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 1512 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 1260 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 1260 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 360 b^7 B^2 d^7 x^7 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
& 36 A b^7 B c^7 n \operatorname{Log}[c+d x] - 252 a A b^6 B c^6 d n \operatorname{Log}[c+d x] + 756 a^2 A b^5 B c^5 d^2 n \operatorname{Log}[c+d x] - 1260 a^3 A b^4 B c^4 d^3 n \operatorname{Log}[c+d x] - \\
& 36 b^7 B^2 c^7 n^2 \operatorname{Log}[c+d x] + 288 a b^6 B^2 c^6 d n^2 \operatorname{Log}[c+d x] - 990 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}[c+d x] + 642 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}[c+d x] + \\
& 114 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}[c+d x] - 18 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}[c+d x] - 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
& 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
& 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
& 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 36 b^7 B^2 c^7 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
& 756 a^2 b^5 B^2 c^5 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 1260 a^3 b^4 B^2 c^4 d^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
& 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 36 b^4 B^2 c^4 (b^3 c^3 - 7 a b^2 c^2 d + 21 a^2 b c d^2 - 35 a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
& 36 a^4 B^2 d^4 \left(-35 b^3 c^3 + 21 a b^2 c^2 d - 7 a^2 b c d^2 + a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
\end{aligned}$$

Problem 179: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 (c i + d i x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 976 leaves, 20 steps):

$$\begin{aligned} & - \frac{7 B^2 (b c - a d)^5 g^2 i^3 n^2 x}{180 b^3 d^2} - \frac{7 B^2 (b c - a d)^4 g^2 i^3 n^2 (c + d x)^2}{360 b^2 d^3} - \frac{B^2 (b c - a d)^3 g^2 i^3 n^2 (c + d x)^3}{60 b d^3} + \frac{B^2 (b c - a d)^2 g^2 i^3 n^2 (c + d x)^4}{60 d^3} \\ & - \frac{B (b c - a d)^4 g^2 i^3 n (a + b x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b^4 d} - \frac{B (b c - a d)^3 g^2 i^3 n (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b^4} \\ & - \frac{B (b c - a d)^4 g^2 i^3 n (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{10 b^2 d^3} + \frac{B (b c - a d)^3 g^2 i^3 n (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{45 b d^3} + \\ & - \frac{7 B (b c - a d)^2 g^2 i^3 n (c + d x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{60 d^3} - \frac{b B (b c - a d) g^2 i^3 n (c + d x)^5 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{15 d^3} + \\ & + \frac{(b c - a d)^3 g^2 i^3 (a + b x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{60 b^4} + \frac{(b c - a d)^2 g^2 i^3 (a + b x)^3 (c + d x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{20 b^3} + \\ & + \frac{(b c - a d) g^2 i^3 (a + b x)^3 (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{10 b^2} + \frac{g^2 i^3 (a + b x)^3 (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{6 b} + \\ & + \frac{B (b c - a d)^5 g^2 i^3 n (a + b x) \left(2 A + B n + 2 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b^4 d^2} + \frac{B (b c - a d)^6 g^2 i^3 n \left(2 A + 3 B n + 2 B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[\frac{b c - a d}{b (c + d x)} \right]}{60 b^4 d^3} + \\ & + \frac{B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{36 b^4 d^3} + \frac{11 B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{Log} [c + d x]}{180 b^4 d^3} + \frac{B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{30 b^4 d^3} \end{aligned}$$

Result (type 4, 4611 leaves):

$$\begin{aligned} & \frac{1}{360 b^4 d^3} g^2 i^3 \\ & \left(12 b^6 B^2 c^6 n^2 - 84 a b^5 B^2 c^5 d n^2 + 12 a^2 b^4 B^2 c^4 d^2 n^2 + 240 a^3 b^3 B^2 c^3 d^3 n^2 - 252 a^4 b^2 B^2 c^2 d^4 n^2 + 84 a^5 b B^2 c d^5 n^2 - 12 a^6 B^2 d^6 n^2 + 360 a^2 A^2 b^4 c^3 d^3 x + \right. \\ & 12 A b^6 B c^5 d n x - 72 a A b^5 B c^4 d^2 n x - 60 a^2 A b^4 B c^3 d^3 n x + 180 a^3 A b^3 B c^2 d^4 n x - 72 a^4 A b^2 B c d^5 n x + 12 a^5 A b B d^6 n x - 16 b^6 B^2 c^5 d n^2 x + \\ & 102 a b^5 B^2 c^4 d^2 n^2 x - 194 a^2 b^4 B^2 c^3 d^3 n^2 x + 154 a^3 b^3 B^2 c^2 d^4 n^2 x - 54 a^4 b^2 B^2 c d^5 n^2 x + 8 a^5 b B^2 d^6 n^2 x + 360 a A^2 b^5 c^3 d^3 x^2 + \\ & 540 a^2 A^2 b^4 c^2 d^4 x^2 - 6 A b^6 B c^4 d^2 n x^2 - 204 a A b^5 B c^3 d^3 n x^2 + 180 a^2 A b^4 B c^2 d^4 n x^2 + 36 a^3 A b^3 B c d^5 n x^2 - 6 a^4 A b^2 B d^6 n x^2 + \\ & 11 b^6 B^2 c^4 d^2 n^2 x^2 + 10 a b^5 B^2 c^3 d^3 n^2 x^2 - 60 a^2 b^4 B^2 c^2 d^4 n^2 x^2 + 46 a^3 b^3 B^2 c d^5 n^2 x^2 - 7 a^4 b^2 B^2 d^6 n^2 x^2 + 120 A^2 b^6 c^3 d^3 x^3 + 720 a A^2 b^5 c^2 d^4 x^3 + \\ & 360 a^2 A^2 b^4 c d^5 x^3 - 76 A b^6 B c^3 d^3 n x^3 - 84 a A b^5 B c^2 d^4 n x^3 + 156 a^2 A b^4 B c d^5 n x^3 + 4 a^3 A b^3 B d^6 n x^3 + 18 b^6 B^2 c^3 d^3 n^2 x^3 - 30 a b^5 B^2 c^2 d^4 n^2 x^3 + \\ & 6 a^2 b^4 B^2 c d^5 n^2 x^3 + 6 a^3 b^3 B^2 d^6 n^2 x^3 + 270 A^2 b^6 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 + 90 a^2 A^2 b^4 d^6 x^4 - 78 A b^6 B c^2 d^4 n x^4 + 36 a A b^5 B c d^5 n x^4 + \\ & 42 a^2 A b^4 B d^6 n x^4 + 6 b^6 B^2 c^2 d^4 n^2 x^4 - 12 a b^5 B^2 c d^5 n^2 x^4 + 6 a^2 b^4 B^2 d^6 n^2 x^4 + 216 A^2 b^6 c d^5 x^5 + 144 a A^2 b^5 d^6 x^5 - 24 A b^6 B c d^5 n x^5 + \end{aligned}$$

$$\begin{aligned}
& 24 a A b^5 B d^6 n x^5 + 60 A^2 b^6 d^6 x^6 + 12 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 72 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 60 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 120 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
& 90 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 36 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 6 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 60 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 180 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 72 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 12 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 6 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 36 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 90 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 240 a^3 A b^3 B c^3 d^3 n \operatorname{Log}[a + b x] - \\
& 180 a^4 A b^2 B c^2 d^4 n \operatorname{Log}[a + b x] + 72 a^5 A b B c d^5 n \operatorname{Log}[a + b x] - 12 a^6 A B d^6 n \operatorname{Log}[a + b x] + 6 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[a + b x] + \\
& 128 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[a + b x] - 186 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[a + b x] + 60 a^5 b B^2 c d^5 n^2 \operatorname{Log}[a + b x] - 8 a^6 B^2 d^6 n^2 \operatorname{Log}[a + b x] - \\
& 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + \\
& 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] - 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-bc + ad}\right] + \\
& 720 a^2 A b^4 B c^3 d^3 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 b^6 B^2 c^5 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 72 a b^5 B^2 c^4 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 60 a^2 b^4 B^2 c^3 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^3 b^3 B^2 c^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 72 a^4 b^2 B^2 c d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 12 a^5 b B^2 d^6 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 720 a A b^5 B c^3 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 6 b^6 B^2 c^4 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 204 a b^5 B^2 c^3 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^2 b^4 B^2 c^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 36 a^3 b^3 B^2 c d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^4 b^2 B^2 d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 240 A b^6 B c^3 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 1440 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 720 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 76 b^6 B^2 c^3 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 84 a b^5 B^2 c^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 156 a^2 b^4 B^2 c d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 4 a^3 b^3 B^2 d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 540 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 78 b^6 B^2 c^2 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 a b^5 B^2 c d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 42 a^2 b^4 B^2 d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 432 A b^6 B c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 288 a A b^5 B d^6 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 24 b^6 B^2 c d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a b^5 B^2 d^6 n x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] +
\end{aligned}$$

$$\begin{aligned}
& 120 A b^6 B d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+240 a^3 b^3 B^2 c^3 d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-180 a^4 b^2 B^2 c^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 72 a^5 b B^2 c d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-12 a^6 B^2 d^6 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+360 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
& 360 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+120 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
& 720 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+360 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+270 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
& 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+90 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+216 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
& 144 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-12 A b^6 B c^6 n \operatorname{Log}[c+d x]+72 a A b^5 B c^5 d n \operatorname{Log}[c+d x]- \\
& 180 a^2 A b^4 B c^4 d^2 n \operatorname{Log}[c+d x]+16 b^6 B^2 c^6 n^2 \operatorname{Log}[c+d x]-108 a b^5 B^2 c^5 d n^2 \operatorname{Log}[c+d x]+66 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[c+d x]+ \\
& 32 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[c+d x]-6 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[c+d x]+12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
& 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-12 b^6 B^2 c^6 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]+72 a b^5 B^2 c^5 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]- \\
& 180 a^2 b^4 B^2 c^4 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]-12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
& 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-12 b^4 B^2 c^4\left(b^2 c^2-6 a b c d+15 a^2 d^2\right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
& 12 a^3 B^2 d^3\left(-20 b^3 c^3+15 a b^2 c^2 d-6 a^2 b c d^2+a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
\end{aligned}$$

Problem 180: Result more than twice size of optimal antiderivative.

$$\int(a g+b g x)(c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 d x$$

Optimal (type 4, 786 leaves, 19 steps):

$$\begin{aligned}
& \frac{B^2 (bc - ad)^4 g i^3 n^2 x}{60 b^3 d} + \frac{B^2 (bc - ad)^3 g i^3 n^2 (c + dx)^2}{30 b^2 d^2} + \frac{B^2 (bc - ad)^2 g i^3 n^2 (c + dx)^3}{30 b d^2} - \\
& \frac{B (bc - ad)^4 g i^3 n (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{10 b^4 d} - \frac{B (bc - ad)^3 g i^3 n (a + bx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{10 b^4} + \\
& \frac{3 B (bc - ad)^3 g i^3 n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{20 b^2 d^2} + \frac{B (bc - ad)^2 g i^3 n (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{30 b d^2} - \\
& \frac{B (bc - ad) g i^3 n (c + dx)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{10 d^2} + \frac{(bc - ad)^3 g i^3 (a + bx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{20 b^4} + \\
& \frac{(bc - ad)^2 g i^3 (a + bx)^2 (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{10 b^3} + \frac{3 (bc - ad) g i^3 (a + bx)^2 (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{20 b^2} + \\
& \frac{g i^3 (a + bx)^2 (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{5 b} - \frac{B (bc - ad)^5 g i^3 n \left(A + B n + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{bc - ad}{b (c + dx)} \right]}{10 b^4 d^2} - \\
& \frac{B^2 (bc - ad)^5 g i^3 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{12 b^4 d^2} - \frac{11 B^2 (bc - ad)^5 g i^3 n^2 \operatorname{Log} [c + dx]}{60 b^4 d^2} - \frac{B^2 (bc - ad)^5 g i^3 n^2 \operatorname{PolyLog} \left[2, \frac{d (a+bx)}{b (c+dx)} \right]}{10 b^4 d^2}
\end{aligned}$$

Result (type 4, 3427 leaves):

$$\begin{aligned}
& \frac{1}{60 b^4 d^2} \\
& g i^3 \left(-6 b^5 B^2 c^5 n^2 - 24 a b^4 B^2 c^4 d n^2 + 90 a^2 b^3 B^2 c^3 d^2 n^2 - 90 a^3 b^2 B^2 c^2 d^3 n^2 + 36 a^4 b B^2 c d^4 n^2 - 6 a^5 B^2 d^5 n^2 + 60 a A^2 b^4 c^3 d^2 x - 6 A b^5 B c^4 d n x - \right. \\
& 30 a A b^4 B c^3 d^2 n x + 60 a^2 A b^3 B c^2 d^3 n x - 30 a^3 A b^2 B c d^4 n x + 6 a^4 A b B d^5 n x + 11 b^5 B^2 c^4 d n^2 x - 28 a b^4 B^2 c^3 d^2 n^2 x + 24 a^2 b^3 B^2 c^2 d^3 n^2 x - \\
& 8 a^3 b^2 B^2 c d^4 n^2 x + a^4 b B^2 d^5 n^2 x + 30 A^2 b^5 c^3 d^2 x^2 + 90 a A^2 b^4 c^2 d^3 x^2 - 27 A b^5 B c^3 d^2 n x^2 + 15 a A b^4 B c^2 d^3 n x^2 + 15 a^2 A b^3 B c d^4 n x^2 - \\
& 3 a^3 A b^2 B d^5 n x^2 + 8 b^5 B^2 c^3 d^2 n^2 x^2 - 18 a b^4 B^2 c^2 d^3 n^2 x^2 + 12 a^2 b^3 B^2 c d^4 n^2 x^2 - 2 a^3 b^2 B^2 d^5 n^2 x^2 + 60 A^2 b^5 c^2 d^3 x^3 + 60 a A^2 b^4 c d^4 x^3 - \\
& 22 A b^5 B c^2 d^3 n x^3 + 20 a A b^4 B c d^4 n x^3 + 2 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 45 A^2 b^5 c d^4 x^4 + \\
& 15 a A^2 b^4 d^5 x^4 - 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 30 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \\
& 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] - 30 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 6 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 30 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - \\
& 30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 15 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 3 a^5 B^2 d^5 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 6 b^5 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 30 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - \\
& 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + 30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 6 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - 3 b^5 B^2 c^5 n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \\
& 15 a b^4 B^2 c^4 d n^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 60 a^2 A b^3 B c^3 d^2 n \operatorname{Log} [a + bx] - 60 a^3 A b^2 B c^2 d^3 n \operatorname{Log} [a + bx] + 30 a^4 A b B c d^4 n \operatorname{Log} [a + bx] - \\
& 6 a^5 A B d^5 n \operatorname{Log} [a + bx] + 27 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} [a + bx] - 37 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} [a + bx] + 11 a^4 b B^2 c d^4 n^2 \operatorname{Log} [a + bx] - a^5 B^2 d^5 n^2 \operatorname{Log} [a + bx] - \\
& 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] + 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] - 30 a^4 b B^2 c d^4 n^2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] +
\end{aligned}$$

$$\begin{aligned}
& 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \\
& 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 120 a A b^4 B c^3 d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 30 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 60 a^2 b^3 B^2 c^2 d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 30 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 180 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 27 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 15 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 15 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 22 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 20 a b^4 B^2 c d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 2 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 90 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 60 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 30 a^4 b B^2 c d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^5 B^2 d^5 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 30 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 90 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 60 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 45 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 6 A b^5 B c^5 n \operatorname{Log}[c + d x] - 30 a A b^4 B c^4 d n \operatorname{Log}[c + d x] - 11 b^5 B^2 c^5 n^2 \operatorname{Log}[c + d x] + a b^4 B^2 c^4 d n^2 \operatorname{Log}[c + d x] + \\
& 13 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c + d x] - 3 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c + d x] - 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
& 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 6 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - \\
& 30 a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\
& 6 b^4 B^2 c^4 (b c - 5 a d) n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 a^2 B^2 d^2 (-10 b^3 c^3 + 10 a b^2 c^2 d - 5 a^2 b c d^2 + a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]
\end{aligned}$$

Problem 181: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 454 leaves, 15 steps):

$$\begin{aligned} & \frac{5 B^2 (b c - a d)^3 i^3 n^2 x}{12 b^3} + \frac{B^2 (b c - a d)^2 i^3 n^2 (c + d x)^2}{12 b^2 d} - \frac{B (b c - a d)^3 i^3 n (a + b x) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{2 b^4} - \\ & \frac{B (b c - a d)^2 i^3 n (c + d x)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{4 b^2 d} - \frac{B (b c - a d) i^3 n (c + d x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)}{6 b d} + \\ & \frac{i^3 (c + d x)^4 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{4 d} + \frac{5 B^2 (b c - a d)^4 i^3 n^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right]}{12 b^4 d} + \frac{11 B^2 (b c - a d)^4 i^3 n^2 \operatorname{Log} [c + d x]}{12 b^4 d} + \\ & \frac{B (b c - a d)^4 i^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b (c + d x)}{d (a + b x)} \right]}{2 b^4 d} - \frac{B^2 (b c - a d)^4 i^3 n^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{d (a + b x)} \right]}{2 b^4 d} \end{aligned}$$

Result (type 4, 2348 leaves):

$$\begin{aligned}
& \frac{1}{12 b^4 d} i^3 \left(-18 b^4 B^2 c^4 n^2 + 54 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 30 a^3 b B^2 c d^3 n^2 - 6 a^4 B^2 d^4 n^2 + 12 A^2 b^4 c^3 d x - 18 A b^4 B c^3 d n x + 36 a A b^3 B c^2 d^2 n x - \right. \\
& 24 a^2 A b^2 B c d^3 n x + 6 a^3 A b B d^4 n x + 7 b^4 B^2 c^3 d n^2 x - 19 a b^3 B^2 c^2 d^2 n^2 x + 17 a^2 b^2 B^2 c d^3 n^2 x - 5 a^3 b B^2 d^4 n^2 x + 18 A^2 b^4 c^2 d^2 x^2 - \\
& 9 A b^4 B c^2 d^2 n x^2 + 12 a A b^3 B c d^3 n x^2 - 3 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + 12 A^2 b^4 c d^3 x^3 - \\
& 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 18 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
& 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 18 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 24 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 6 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 24 a A b^3 B c^3 d n \operatorname{Log}[a + b x] - 36 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[a + b x] + 24 a^3 A b B c d^3 n \operatorname{Log}[a + b x] - 6 a^4 A B d^4 n \operatorname{Log}[a + b x] + \\
& 9 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] - 14 a^3 b B^2 c d^3 n^2 \operatorname{Log}[a + b x] + 5 a^4 B^2 d^4 n^2 \operatorname{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 24 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 24 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 A b^4 B c^3 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 18 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 24 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 36 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 9 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 3 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 a b^3 B^2 c^3 d n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 36 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 24 a^3 b B^2 c d^3 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^4 B^2 d^4 n \operatorname{Log}[a + b x] \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 12 b^4 B^2 c^3 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\
& 18 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 12 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 A b^4 B c^4 n \operatorname{Log}[c + d x] - \\
& 7 b^4 B^2 c^4 n^2 \operatorname{Log}[c + d x] + 10 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c + d x] - 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c + d x] + 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - \\
& 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\
& \left. 6 b^4 B^2 c^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 6 a B^2 d (-4 b^3 c^3 + 6 a b^2 c^2 d - 4 a^2 b c d^2 + a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)
\end{aligned}$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 762 leaves, 26 steps):

$$\begin{aligned} & \frac{B^2 d (bc - ad)^2 i^3 n^2 x}{3 b^3 g} - \frac{5 B d (bc - ad)^2 i^3 n (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 b^4 g} - \frac{B (bc - ad) i^3 n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{3 b^2 g} + \\ & \frac{d (bc - ad)^2 i^3 (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b^4 g} + \frac{(bc - ad) i^3 (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 b^2 g} + \frac{i^3 (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 b g} + \\ & \frac{2 B (bc - ad)^3 i^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{bc - ad}{b (c + dx)} \right]}{b^4 g} + \frac{B^2 (bc - ad)^3 i^3 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]}{3 b^4 g} + \frac{2 B^2 (bc - ad)^3 i^3 n^2 \operatorname{Log} [c + dx]}{b^4 g} + \\ & \frac{5 B (bc - ad)^3 i^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{3 b^4 g} - \frac{(bc - ad)^3 i^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} + \\ & \frac{2 B^2 (bc - ad)^3 i^3 n^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{b^4 g} - \frac{5 B^2 (bc - ad)^3 i^3 n^2 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{3 b^4 g} + \\ & \frac{2 B (bc - ad)^3 i^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} + \frac{2 B^2 (bc - ad)^3 i^3 n^2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4 g} \end{aligned}$$

Result (type 4, 5616 leaves):

$$\begin{aligned} & \frac{d (3 b^2 c^2 - 3 a b c d + a^2 d^2) i^3 x \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^3 g} + \\ & \frac{d^2 (3 b c - a d) i^3 x^2 \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{2 b^2 g} + \frac{d^3 i^3 x^3 \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{3 b g} + \\ & \frac{(bc - ad)^3 i^3 \operatorname{Log} [a + bx] \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^4 g} + \frac{1}{g} 2 B c^3 i^3 n \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \\ & \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2 b} + \frac{\operatorname{Log} [a + bx] \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{b} - \frac{\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right]}{b} \right) + \end{aligned}$$

$$\begin{aligned}
& \frac{1}{g} 2 B d^3 i^3 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{a^2 \left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^3} - \frac{a^3 \text{Log} \left[\frac{a}{b} + x \right]^2}{2 b^4} - \frac{a^2 \left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{b^3} - \right. \\
& \frac{a \left(-\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a + b x]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{b} \right] \right)}{b^2} + \frac{-\frac{1}{3} b \left(\frac{a^2 x}{b^3} - \frac{a x^2}{2 b^2} + \frac{x^3}{3 b} - \frac{a^3 \text{Log}[a + b x]}{b^4} \right) + \frac{1}{3} x^3 \text{Log} \left[\frac{a + b x}{b} \right]}{b} + \\
& \frac{a \left(-\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c + d x]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[\frac{c + d x}{d} \right] \right)}{b^2} - \frac{-\frac{1}{3} d \left(\frac{c^2 x}{d^3} - \frac{c x^2}{2 d^2} + \frac{x^3}{3 d} - \frac{c^3 \text{Log}[c + d x]}{d^4} \right) + \frac{1}{3} x^3 \text{Log} \left[\frac{c + d x}{d} \right]}{b} + \left(\frac{a^2 x}{b^3} - \frac{a x^2}{2 b^2} + \frac{x^3}{3 b} - \frac{a^3 \text{Log}[a + b x]}{b^4} \right) \\
& \left. \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) + \frac{a^3 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b(c + d x)}{b c - a d} \right] \right)}{b^4} \right) + \\
& \frac{1}{g} 6 B c d^2 i^3 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(-\frac{a \left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^2} + \frac{a^2 \text{Log} \left[\frac{a}{b} + x \right]^2}{2 b^3} + \frac{a \left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{b^2} + \right. \\
& \frac{-\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a + b x]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[\frac{a + b x}{b} \right]}{b} - \frac{-\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c + d x]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[\frac{c + d x}{d} \right]}{b} + \\
& \left. \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a + b x]}{b^3} \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) - \frac{a^2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b(c + d x)}{b c - a d} \right] \right)}{b^3} \right) + \\
& \frac{1}{g} 6 B c^2 d i^3 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b} - \frac{a \text{Log} \left[\frac{a}{b} + x \right]^2}{2 b^2} - \frac{\left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{b} + \right. \\
& \left. \left(\frac{x}{b} - \frac{a \text{Log}[a + b x]}{b^2} \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) + \frac{a \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[2, \frac{b(c + d x)}{b c - a d} \right] \right)}{b^2} \right) + \\
& \frac{1}{g} B^2 c^3 i^3 n^2 \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^3}{3 b} + \frac{\text{Log}[a + b x] \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right)^2}{b} + \right. \\
& \left. 2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^2}{2 b} - \frac{\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right] + \text{PolyLog} \left[2, \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{b} \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{2 \left(\frac{1}{2} \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] - \operatorname{PolyLog} \left[3, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b} - \frac{1}{b} \\
& \left. 2 \left(\frac{1}{2} \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{bd \left(\frac{c+x}{d} \right)}{bc - ad} \right] \right) - \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, -\frac{d(a+bx)}{bc - ad} \right] + \operatorname{PolyLog} \left[3, -\frac{d(a+bx)}{bc - ad} \right] \right) \right) + \frac{1}{g} B^2 d^3 i^3 n^2 \\
& \left(-\frac{a^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3b^4} + \frac{a^2(a+bx) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^4} - \frac{a(a+bx) \left(-7a+bx + (6a-2bx) \operatorname{Log} \left[\frac{a}{b} + x \right] - 2(a-bx) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4b^4} \right) + \\
& \frac{a^2(c+dx) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{b^3 d} - \frac{a(c+dx) \left(-7c+dx + (6c-2dx) \operatorname{Log} \left[\frac{c}{d} + x \right] - 2(c-dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right)}{4b^2 d^2} + \frac{1}{54b^4} \\
& \left(bx(66a^2 - 15abx + 4b^2x^2) - 6bx(6a^2 - 3abx + 2b^2x^2) \operatorname{Log} \left[\frac{a}{b} + x \right] + 18(a^3 + b^3x^3) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 66a^3 \operatorname{Log} [a+bx] \right) + \\
& \frac{1}{54bd^3} \left(dx(66c^2 - 15cdx + 4d^2x^2) - 6dx(6c^2 - 3cdx + 2d^2x^2) \operatorname{Log} \left[\frac{c}{d} + x \right] + 18(c^3 + d^3x^3) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 66c^3 \operatorname{Log} [c+dx] \right) + \\
& \left(\frac{a^2x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b} - \frac{a^3 \operatorname{Log} [a+bx]}{b^4} \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2 + \\
& 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) \\
& \left(\frac{a^2 \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{b^3} - \frac{a^3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2b^4} - \frac{a^2 \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{b^3} - \frac{a \left(-\frac{1}{2}b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \operatorname{Log} [a+bx]}{b^3} \right) + \frac{1}{2}x^2 \operatorname{Log} \left[\frac{a+bx}{b} \right] \right)}{b^2} \right) + \\
& \frac{-\frac{1}{3}b \left(\frac{a^2x}{b^3} - \frac{ax^2}{2b^2} + \frac{x^3}{3b} - \frac{a^3 \operatorname{Log} [a+bx]}{b^4} \right) + \frac{1}{3}x^3 \operatorname{Log} \left[\frac{a+bx}{b} \right]}{b} + \frac{a \left(-\frac{1}{2}d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \operatorname{Log} [c+dx]}{d^3} \right) + \frac{1}{2}x^2 \operatorname{Log} \left[\frac{c+dx}{d} \right] \right)}{b^2} - \\
& \left. \frac{-\frac{1}{3}d \left(\frac{c^2x}{d^3} - \frac{cx^2}{2d^2} + \frac{x^3}{3d} - \frac{c^3 \operatorname{Log} [c+dx]}{d^4} \right) + \frac{1}{3}x^3 \operatorname{Log} \left[\frac{c+dx}{d} \right]}{b} + \frac{a^3 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^4} \right) - \\
& 2 \left(\frac{1}{b^4 d} a^2 \left(ad + 2bdx - bdx \operatorname{Log} \left[\frac{c}{d} + x \right] - bc \operatorname{Log} [c+dx] + \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) + d(a+bx) \operatorname{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) \right) + \right. \\
& \left. (bc-ad) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) - \frac{1}{4b^4 d^2} a \left(-2abcd - 3b^2cdx - 3abd^2x + b^2d^2x^2 + 2abd^2x \operatorname{Log} \left[\frac{c}{d} + x \right] - \right. \\
& \left. b^2d^2x^2 \operatorname{Log} \left[\frac{c}{d} + x \right] + a^2d^2 \operatorname{Log} [a+bx] + b^2c^2 \operatorname{Log} [c+dx] + 2abcd \operatorname{Log} [c+dx] + \operatorname{Log} \left[\frac{a}{b} + x \right] \left(bd(2ac+bx(2c-dx)) - 2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& \frac{1}{108 b^4 d^3} \left(36 a b^2 c^2 d + 48 b^3 c^2 dx + 36 a b^2 c d^2 x + 48 a^2 b d^3 x - 15 b^3 c d^2 x^2 - 15 a b^2 d^3 x^2 + 8 b^3 d^3 x^3 - 36 a^2 b d^3 x \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \\
& 18 a b^2 d^3 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 12 b^3 d^3 x^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 18 a^2 b c d^2 \operatorname{Log}[a+bx] - 12 a^3 d^3 \operatorname{Log}[a+bx] - 12 b^3 c^3 \operatorname{Log}[c+dx] - \\
& 18 a b^2 c^2 d \operatorname{Log}[c+dx] - 36 a^2 b c d^2 \operatorname{Log}[c+dx] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-b^2 d (6 a c^2 + b x (6 c^2 - 3 c d x + 2 d^2 x^2)) + \right. \\
& \left. 6 d^3 (a^3 + b^3 x^3) \operatorname{Log}\left[\frac{c}{d} + x\right] + 6 (b^3 c^3 - a^3 d^3) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 36 (b^3 c^3 - a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \frac{1}{2 b^4} \\
& a^3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) - \\
& \left. \frac{a^3 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right)}{b^4} \right) + \\
& \frac{1}{g} 3 B^2 c d^2 i^3 n^2 \left(\frac{a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b^3} - \frac{a(a+bx) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^3} + \right. \\
& \frac{(a+bx) \left(-7 a + b x + (6 a - 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{4 b^3} - \\
& \frac{a(c+dx) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b^2 d} + \frac{(c+dx) \left(-7 c + d x + (6 c - 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{4 b d^2} + \\
& \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \operatorname{Log}[a+bx]}{b^3} \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{b x}{c+dx}\right] \right)^2 + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{b x}{c+dx}\right] \right) \\
& \left(-\frac{a \left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right)}{b^2} + \frac{a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{a \left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{b^2} + \frac{-\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \operatorname{Log}[a+bx]}{b^3} \right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{a+bx}{b}\right]}{b} \right) - \\
& \left. \frac{-\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \operatorname{Log}[c+dx]}{d^3} \right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c+dx}{d}\right]}{b} - \frac{a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right)}{b^3} \right) - \\
& 2 \left(-\frac{1}{b^3 d} a \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c+dx] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \operatorname{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) \right) + \right. \\
& \left. (bc-ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \frac{1}{4 b^3 d^2} \left(-2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] - \right.
\end{aligned}$$

$$\begin{aligned}
& b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + a^2 d^2 \operatorname{Log}[a + b x] + b^2 c^2 \operatorname{Log}[c + d x] + 2 a b c d \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - \right. \\
& \left. 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \frac{1}{2 b^3} \\
& a^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& \left. \frac{a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right)}{b^3} \right) + \\
& \frac{1}{g} 3 B^2 c^2 d i^3 n^2 \left(-\frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b^2} + \frac{(a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^2} + \frac{(c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b d} + \right. \\
& \left(\frac{x}{b} - \frac{a \operatorname{Log}[a + b x]}{b^2} \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \\
& \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b} - \frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b} + \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right)}{b^2} \right) - \\
& 2 \left(\frac{1}{b^2 d} \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d(a + b x) + d(a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) \right) + \right. \\
& \left. (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) - \frac{1}{2 b^2} \\
& a \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right) - \\
& \left. \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right)}{b^2} \right)
\end{aligned}$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{(a g + b g x)^2} dx$$

Optimal (type 4, 739 leaves, 17 steps):

$$\begin{aligned}
& - \frac{2 B^2 (b c - a d)^2 i^3 n^2 (c + d x)}{b^3 g^2 (a + b x)} - \frac{B d^2 (b c - a d) i^3 n (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{b^4 g^2} - \frac{2 B (b c - a d)^2 i^3 n (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{b^3 g^2 (a + b x)} + \\
& \frac{2 d^2 (b c - a d) i^3 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{b^4 g^2} - \frac{(b c - a d)^2 i^3 (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{b^3 g^2 (a + b x)} + \\
& \frac{d i^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 b^2 g^2} + \frac{4 B d (b c - a d)^2 i^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{b^4 g^2} + \frac{B^2 d (b c - a d)^2 i^3 n^2 \operatorname{Log}[c + d x]}{b^4 g^2} + \\
& \frac{B d (b c - a d)^2 i^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^2} - \frac{3 d (b c - a d)^2 i^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^2} + \\
& \frac{4 B^2 d (b c - a d)^2 i^3 n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{b^4 g^2} - \frac{B^2 d (b c - a d)^2 i^3 n^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^2} + \\
& \frac{6 B d (b c - a d)^2 i^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^2} + \frac{6 B^2 d (b c - a d)^2 i^3 n^2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right]}{b^4 g^2}
\end{aligned}$$

Result (type 4, 5470 leaves):

$$\begin{aligned}
& \frac{d^2 (3 b c - 2 a d) i^3 x \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right)^2}{b^3 g^2} + \\
& \frac{d^3 i^3 x^2 \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right)^2}{2 b^2 g^2} + \frac{3 d (b c - a d)^2 i^3 \operatorname{Log}[a + b x] \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right)^2}{b^4 g^2} + \\
& \frac{1}{b^4 g^2 (a + b x)} \left(-A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - 2 A b^3 B c^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right) + \\
& 6 a A b^2 B c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - 6 a^2 A b B c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 2 a^3 A B d^3 i^3 \\
& \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - b^3 B^2 c^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + 3 a b^2 B^2 c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 - \\
& 3 a^2 b B^2 c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + a^3 B^2 d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + \frac{1}{b (b c - a d) g^2 (a + b x)} \\
& B^2 c^3 i^3 n^2 \left(-2 b c + 2 a d - 2 d (a + b x) \operatorname{Log}[a + b x] + (-2 b c + 2 a d) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - b (c + d x) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 2 d (a + b x) \operatorname{Log}[c + d x] \right) + \\
& \frac{1}{g^2} 2 B c^3 i^3 n \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right)
\end{aligned}$$

$$\left(-\frac{\left(\frac{a}{b} + x\right) \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{(a + b x)^2 \text{Log}\left[\frac{a}{b} + x\right]} - \frac{\frac{b\left(\frac{c}{d} + x\right) \text{Log}\left[\frac{c}{d} + x\right]}{\left(-a + \frac{bc}{d}\right)^2 \left(1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right)} + \frac{\text{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{bc}{d}}\right]}{-a + \frac{bc}{d}}}{b} - \frac{-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right]}{b(a + b x)} \right) +$$

$$\frac{1}{g^2} 2 B d^3 i^3 n \left(A + B \left(\text{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right)$$

$$\left(-\frac{2 a \left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3 a^2 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{a^3 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \frac{2 a \left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \right.$$

$$\left. -\frac{\frac{1}{2} b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \text{Log}[a+bx]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+bx}{b}\right]}{b^2} + \frac{a^3 \left((-bc + ad) \text{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left(\text{Log}[a + b x] - \text{Log}[c + d x]\right)\right)}{b^4 (bc - ad) (a + b x)} - \right.$$

$$\left. -\frac{\frac{1}{2} d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \text{Log}[c+dx]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+dx}{d}\right]}{b^2} + \frac{\left(-4 a b x + b^2 x^2 + \frac{2 a^3}{a + b x} + 6 a^2 \text{Log}[a + b x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right]\right)}{2 b^4} - \right.$$

$$\left. \frac{3 a^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)}{b^4} \right) + \frac{1}{g^2}$$

$$6 B c d^2 i^3 n \left(A + B \left(\text{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \right.$$

$$\left. \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} - \frac{a^2 \left((-bc + ad) \text{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left(\text{Log}[a + b x] - \text{Log}[c + d x]\right)\right)}{b^3 (bc - ad) (a + b x)} + \right.$$

$$\left. \frac{\left(b x - \frac{a^2}{a + b x} - 2 a \text{Log}[a + b x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right]\right)}{b^3} + \frac{2 a \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)}{b^3} \right) +$$

$$\frac{1}{g^2} 6 B c^2 d i^3 n \left(A + B \left(\text{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right)$$

$$\left(\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2 (a + b x)} + \frac{a \left((-bc + ad) \text{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left(\text{Log}[a + b x] - \text{Log}[c + d x]\right)\right)}{b^2 (bc - ad) (a + b x)} + \right.$$

$$\left. \frac{\left(\frac{a}{a + b x} + \text{Log}[a + b x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right]\right)}{b^2} - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^2} \right) +$$

$$\begin{aligned}
& \frac{1}{g^2} B^2 d^3 i^3 n^2 \left(\frac{a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{b^4} - \frac{2 a (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4} + \frac{a^3 \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4 (a + b x)} + \right. \\
& \left. \frac{(a + b x) \left(-7 a + b x + (6 a - 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{4 b^4} - \right. \\
& \left. \frac{2 a (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{b^3 d} + \frac{(c + d x) \left(-7 c + d x + (6 c - 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 b^2 d^2} + \right. \\
& \left. \frac{\left(-4 a b x + b^2 x^2 + \frac{2 a^3}{a + b x} + 6 a^2 \operatorname{Log}[a + b x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right]\right)^2}{2 b^4} - \frac{1}{b^4 (b c - a d) (a + b x)} \right. \\
& a^3 \left(-b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \left(-\frac{2 a \left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3 a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{a^3 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \frac{2 a \left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \right. \\
& \left. -\frac{\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \operatorname{Log}[a + b x]}{b^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{a + b x}{b}\right]}{b^2} + \frac{a^3 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right)\right)}{b^4 (b c - a d) (a + b x)} - \right. \\
& \left. -\frac{\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \operatorname{Log}[c + d x]}{d^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c + d x}{d}\right]}{b^2} - \frac{3 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]\right)}{b^4} \right) - \\
& 2 \left(-\frac{1}{b^4 d} 2 a \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right]\right) \right) + \right. \\
& \left. (b c - a d) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \frac{1}{4 b^4 d^2} \left(-2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\
& \left. b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + a^2 d^2 \operatorname{Log}[a + b x] + b^2 c^2 \operatorname{Log}[c + d x] + 2 a b c d \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - \right. \right. \\
& \left. \left. 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
& \frac{1}{2 b^4 (b c - a d) (a + b x)} a^3 \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right) \right) - \\
& 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \frac{1}{2 b^4} \\
& 3 a^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{3 a^2 \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^4} \right) + \\
& \frac{1}{g^2} 3 B^2 c d^2 i^3 n^2 \left(- \frac{2 a \text{Log} \left[\frac{a}{b} + x \right]^3}{3 b^3} + \frac{(a+bx) \left(2 - 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3} - \frac{a^2 \left(2 + 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3 (a+bx)} + \right. \\
& \frac{(c+dx) \left(2 - 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right)}{b^2 d} + \frac{\left(bx - \frac{a^2}{a+bx} - 2 a \text{Log} [a+bx] \right) \left(- \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2}{b^3} + \\
& \frac{1}{b^3 (bc-ad) (a+bx)} a^2 \left(-b (c+dx) \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 d (a+bx) \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 d (a+bx) \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) + \\
& 2 \left(- \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^2} - \frac{a \text{Log} \left[\frac{a}{b} + x \right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log} \left[\frac{a}{b} + x \right] \right)}{b^3 (a+bx)} - \right. \\
& \left. \frac{\left(\frac{c}{d} + x \right) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{b^2} - \frac{a^2 \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d (a+bx) \left(\text{Log} [a+bx] - \text{Log} [c+dx] \right) \right)}{b^3 (bc-ad) (a+bx)} \right) + \\
& \left. \frac{2 a \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) - 2 \left(\frac{1}{b^3 d} \left(a d + 2 b d x - b d x \text{Log} \left[\frac{c}{d} + x \right] - b c \text{Log} [c+dx] + \right. \right. \\
& \left. \left. \text{Log} \left[\frac{a}{b} + x \right] \left(-d (a+bx) + d (a+bx) \text{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& \frac{1}{2 b^3 (bc-ad) (a+bx)} a^2 \left(d (a+bx) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-bc+ad) \text{Log} \left[\frac{c}{d} + x \right] + d (a+bx) \left(\text{Log} [a+bx] - \text{Log} [c+dx] \right) \right) - \right. \\
& \left. 2 \text{Log} \left[\frac{a}{b} + x \right] \left((bc-ad) \text{Log} \left[\frac{c}{d} + x \right] + d (a+bx) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2 d (a+bx) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) - \frac{1}{b^3} \\
& a \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \left(\text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) - 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) \left. \right) - \\
& \left. \frac{2 a \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) + \\
& \frac{1}{g^2} 3 B^2 c^2 d i^3 n^2 \left(\frac{\text{Log} \left[\frac{a}{b} + x \right]^3}{3 b^2} + \frac{a \left(2 + 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^2 (a+bx)} + \frac{\left(\frac{a}{a+bx} + \text{Log} [a+bx] \right) \left(- \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2}{b^2} - \right. \\
& \left. \frac{1}{b^2 (bc-ad) (a+bx)} a \left(-b (c+dx) \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 d (a+bx) \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 d (a+bx) \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2b^2} + \frac{a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^2(a+bx)} + \right. \\
& \left. \frac{a \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) \left(\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]\right) \right)}{b^2(bc-ad)(a+bx)} - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^2} \right) - \\
& 2 \left(-\frac{1}{2b^2(bc-ad)(a+bx)} a \left(d(a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-bc+ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) \left(\operatorname{Log}[a+bx] - \operatorname{Log}[c+dx]\right) \right) \right) - \right. \\
& \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((bc-ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a+bx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2d(a+bx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \frac{1}{2b^2} \\
& \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b^2} \right)
\end{aligned}$$

Problem 184: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci+di x)^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ag+bgx)^3} dx$$

Optimal (type 4, 644 leaves, 13 steps):

$$\begin{aligned}
& -\frac{4B^2d(bc-ad)i^3n^2(c+dx)}{b^3g^3(a+bx)} - \frac{B^2(bc-ad)i^3n^2(c+dx)^2}{4b^2g^3(a+bx)^2} - \frac{4Bd(bc-ad)i^3n(c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{b^3g^3(a+bx)} - \\
& \frac{B(bc-ad)i^3n(c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2b^2g^3(a+bx)^2} + \frac{d^3i^3(a+bx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b^4g^3} - \frac{2d(bc-ad)i^3(c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{b^3g^3(a+bx)} - \\
& \frac{(bc-ad)i^3(c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2b^2g^3(a+bx)^2} + \frac{2Bd^2(bc-ad)i^3n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)} \right]}{b^4g^3} - \\
& \frac{3d^2(bc-ad)i^3 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{b^4g^3} + \frac{2Bd^2(bc-ad)i^3n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{b^4g^3} + \\
& \frac{6Bd^2(bc-ad)i^3n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4g^3} + \frac{6B^2d^2(bc-ad)i^3n^2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b^4g^3}
\end{aligned}$$

Result (type 4, 6613 leaves):

$$\begin{aligned}
 & \frac{d^3 i^3 x \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^3 g^3} + \frac{3 d^2 (bc - ad) i^3 \text{Log}[a + bx] \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{b^4 g^3} - \\
 & \frac{1}{b^4 g^3 (a + bx)} 3 \left(A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3 + 2 A b^2 B c^2 d i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) - 4 a A b B c d^2 i^3 \right. \\
 & \quad \left. \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) + 2 a^2 A B d^3 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) + b^2 B^2 c^2 d i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - \right. \\
 & \quad \left. 2 a b B^2 c d^2 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + a^2 B^2 d^3 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 \right) + \\
 & \frac{1}{2 b^4 g^3 (a + bx)^2} \left(-A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - 2 A b^3 B c^3 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) + \right. \\
 & \quad 6 a A b^2 B c^2 d i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) - 6 a^2 A b B c d^2 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) + 2 a^3 A B d^3 i^3 \\
 & \quad \left. \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) - b^3 B^2 c^3 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + 3 a b^2 B^2 c^2 d i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - \right. \\
 & \quad \left. 3 a^2 b B^2 c d^2 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + a^3 B^2 d^3 i^3 \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 \right) - \\
 & \left(B^2 c^3 i^3 n^2 \left(b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a + b x)^2 \text{Log}[a + b x] + 2 (bc - ad) (bc - 3 ad - 2 b d x) \text{Log} \left[\frac{a + b x}{c + d x} \right] + \right. \right. \\
 & \quad \left. \left. 2 b (c + d x) (bc - 2 ad - b d x) \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 + 6 a^2 d^2 \text{Log}[c + d x] + 12 a b d^2 x \text{Log}[c + d x] + 6 b^2 d^2 x^2 \text{Log}[c + d x] \right) \right) / \\
 & \left(4 b (bc - ad)^2 g^3 (a + bx)^2 \right) + \frac{1}{g^3} 2 B c^3 i^3 n \left(A + B \left(\text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \\
 & \left[\frac{\left(\frac{a}{b} + x \right) \left(2 \text{Log} \left[\frac{a}{b} + x \right] + 4 \text{Log} \left[\frac{a}{b} + x \right]^2 \right)}{8 (a + b x)^3 \text{Log} \left[\frac{a}{b} + x \right]} - \frac{\frac{b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{bc}{d} \right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)} - \left(\frac{b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{bc}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)^2} + \frac{2 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{bc}{d} \right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right)} \right) \text{Log} \left[\frac{c}{d} + x \right] - \frac{\text{Log} \left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{bc}{d}} \right]}{\left(-a + \frac{bc}{d} \right)^2}}{2 b} \right] -
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+dx}+\frac{bx}{c+dx}\right]}{2b(a+bx)^2}\right) + \frac{1}{g^3} 6Bc^2 d i^3 n \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \right) \\
& \left(-\frac{1+\operatorname{Log}\left[\frac{a}{b}+x\right]}{b^2(a+bx)} + \frac{a\left(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4b^2(a+bx)^2} - \frac{(-bc+ad)\operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+bx)\left(\operatorname{Log}[a+bx]-\operatorname{Log}[c+dx]\right)}{b^2(bc-ad)(a+bx)} - \right. \\
& \left. \frac{a\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2b^2(a+bx)^2} - \frac{(a+2bx)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+dx}+\frac{bx}{c+dx}\right]\right)}{2b^2(a+bx)^2} \right) + \\
& \frac{1}{g^3} 2Bd^3 i^3 n \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \right) \\
& \left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3} - \frac{3a\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^4} - \frac{3a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^4(a+bx)} + \frac{a^3\left(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4b^4(a+bx)^2} - \frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^3} - \right. \\
& \left. \frac{3a^2\left((-bc+ad)\operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+bx)\left(\operatorname{Log}[a+bx]-\operatorname{Log}[c+dx]\right)\right)}{b^4(bc-ad)(a+bx)} - \frac{a^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2b^4(a+bx)^2} - \right. \\
& \left. \frac{\left(-2bx+\frac{a^2(5a+6bx)}{(a+bx)^2}+6a\operatorname{Log}[a+bx]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+dx}+\frac{bx}{c+dx}\right]\right)}{2b^4} + \frac{3a\left(\operatorname{Log}\left[\frac{c}{d}+x\right]\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]+\operatorname{PolyLog}\left[2,\frac{b(c+dx)}{bc-ad}\right]\right)}{b^4} \right) + \\
& \frac{1}{g^3} 6Bc d^2 i^3 n \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]-n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^3} + \frac{2a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+bx)} - \frac{a^2\left(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4b^3(a+bx)^2} + \right. \\
& \left. \frac{2a\left((-bc+ad)\operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+bx)\left(\operatorname{Log}[a+bx]-\operatorname{Log}[c+dx]\right)\right)}{b^3(bc-ad)(a+bx)} + \frac{a^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2b^3(a+bx)^2} + \right. \\
& \left. \frac{\left(\frac{a(3a+4bx)}{(a+bx)^2}+2\operatorname{Log}[a+bx]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+dx}+\frac{bx}{c+dx}\right]\right)}{2b^3} - \frac{\operatorname{Log}\left[\frac{c}{d}+x\right]\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]+\operatorname{PolyLog}\left[2,\frac{b(c+dx)}{bc-ad}\right]}{b^3} \right) + \\
& \frac{1}{g^3} 3B^2 c^2 d i^3 n^2 \left(-\frac{2+2\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^2(a+bx)} + \frac{a\left(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]+2\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{4b^2(a+bx)^2} + 2 \left(-\frac{1+\operatorname{Log}\left[\frac{a}{b}+x\right]}{b^2(a+bx)} + \frac{a\left(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4b^2(a+bx)^2} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{(-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) (\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx])}{b^2 (bc - ad) (a + bx)} - \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{2b^2 (a + bx)^2} \right) \\
& \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) - \frac{(a + 2bx) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2b^2 (a + bx)^2} - \\
& 2 \left(\frac{1}{2b^2 (bc - ad) (a + bx)} \left(d(a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) (\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx]) \right) \right) - \right. \\
& \quad \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((bc - ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \right) + \\
& \quad \left(a \left(-d(-bc + ad)(a + bx) + (bc - ad)^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) \operatorname{Log}\left[\frac{c}{d} + x\right] + d^2 (a + bx)^2 \operatorname{Log}[a + bx] - d^2 (a + bx)^2 \operatorname{Log}[c + dx] + d(a + bx) \right. \right. \\
& \quad \left. \left. \left(d(a + bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2(bc - ad) \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2d(a + bx) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-bc + ad}\right] \right) \right) \right) \right) / \\
& \quad \left(4b^2 (bc - ad)^2 (a + bx)^2 \right) + \frac{-b(c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^2 (bc - ad) (a + bx)} + \\
& \quad \left(a \left(b(c + dx) (-2ad + b(c - dx)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2d^2 (a + bx)^2 \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \\
& \quad \left. \left. \left(b(c + dx) + d(a + bx) \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] \right) + 2d^2 (a + bx)^2 \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right] \right) \right) / \left(2b^2 (bc - ad)^2 (a + bx)^2 \right) + \\
& \frac{1}{g^3} B^2 d^3 i^3 n^2 \left(-\frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^3}{b^4} + \frac{(a + bx) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^4} - \frac{3a^2 \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^4 (a + bx)} + \right. \\
& \quad \frac{a^3 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{4b^4 (a + bx)^2} + \frac{(c + dx) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b^3 d} - \\
& \quad \frac{\left(-2bx + \frac{a^2(5a+6bx)}{(a+bx)^2} + 6a \operatorname{Log}[a + bx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2b^4} + \frac{1}{b^4 (bc - ad) (a + bx)} \\
& \quad \left. 3a^2 \left(-b(c + dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right] \right) + \right. \\
& \quad \left. \left(a^3 \left(b(c + dx) (-2ad + b(c - dx)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2d^2 (a + bx)^2 \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + 2d(a + bx) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left(b (c + d x) + d (a + b x) \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 d^2 (a + b x)^2 \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) / \left(2 b^4 (b c - a d)^2 (a + b x)^2 \right) + \\
& 2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \left(\frac{\left(\frac{a}{b} + x \right) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{b^3} - \frac{3 a \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2 b^4} - \frac{3 a^2 \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{b^4 (a + b x)} + \right. \\
& \frac{a^3 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right)}{4 b^4 (a + b x)^2} - \frac{\left(\frac{c}{d} + x \right) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right)}{b^3} - \frac{3 a^2 \left((-b c + a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x] \right) \right)}{b^4 (b c - a d) (a + b x)} - \\
& \left. \frac{a^3 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log} [a + b x] - d (a + b x) \operatorname{Log} [c + d x])}{(b c - a d)^2} \right)}{2 b^4 (a + b x)^2} + \frac{3 a \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right)}{b^4} \right) - \\
& 2 \left(\frac{1}{b^4 d} \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log} [c + d x] + \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) + d (a + b x) \operatorname{Log} \left[\frac{c}{d} + x \right] + (b c - a d) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) + \right. \right. \\
& \left. \left. (b c - a d) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \frac{1}{2 b^4 (b c - a d) (a + b x)} \right. \\
& \left. 3 a^2 \left(d (a + b x) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 \left((-b c + a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \left(\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x] \right) \right) \right) - \\
& \left. 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \left((b c - a d) \operatorname{Log} \left[\frac{c}{d} + x \right] + d (a + b x) \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) - 2 d (a + b x) \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& \left(a^3 \left(-d (-b c + a d) (a + b x) + (b c - a d)^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \right) \operatorname{Log} \left[\frac{c}{d} + x \right] + d^2 (a + b x)^2 \operatorname{Log} [a + b x] - d^2 (a + b x)^2 \operatorname{Log} [c + d x] + d (a + b x) \right. \right. \\
& \left. \left. \left(d (a + b x) \operatorname{Log} \left[\frac{a}{b} + x \right]^2 + 2 (b c - a d) \left(1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) - 2 d (a + b x) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) \right) / \\
& \left(4 b^4 (b c - a d)^2 (a + b x)^2 \right) - \frac{1}{2 b^4} 3 a \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + \right. \\
& \left. 2 \operatorname{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] \right) - \frac{3 a \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \right)}{b^4} \right) + \\
& \frac{1}{g^3} 3 B^2 c d^2 i^3 n^2 \left(\frac{\operatorname{Log} \left[\frac{a}{b} + x \right]^3}{3 b^3} + \frac{2 a \left(2 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{b^3 (a + b x)} - \frac{a^2 \left(1 + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right)}{4 b^3 (a + b x)^2} + \right. \\
& \left. \frac{\left(\frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log} [a + b x] \right) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right)^2}{2 b^3} - \frac{1}{b^3 (b c - a d) (a + b x)} \right)
\end{aligned}$$

$$\begin{aligned}
& 2 a \left(-b (c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) - \\
& \left(a^2 \left(b(c+d x)(-2 a d+b(c-d x)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2 d^2(a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \right. \right. \\
& \quad \left. \left. 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]\left(b(c+d x)+d(a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+2 d^2(a+b x)^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) \right) / \\
& \left(2 b^3(b c-a d)^2(a+b x)^2\right)+2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right) \\
& \left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^3}+\frac{2 a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)}-\frac{a^2\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^3(a+b x)^2}+\frac{2 a\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)}{b^3(b c-a d)(a+b x)}\right)+ \\
& \left.\frac{a^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x])}{(b c-a d)^2}\right)}{2 b^3(a+b x)^2}-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b^3}\right) - \\
& 2\left(-\frac{1}{b^3(b c-a d)(a+b x)} a\left(d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) - \\
& \quad 2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left((b c-a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) - \\
& \left(a^2\left(-d(-b c+a d)(a+b x)+(b c-a d)^2\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d^2(a+b x)^2 \operatorname{Log}[a+b x]-d^2(a+b x)^2 \operatorname{Log}[c+d x]+d(a+b x) \right. \right. \\
& \quad \left. \left. \left(d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2(b c-a d)\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-2 d(a+b x)\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)\right) \right) / \\
& \left(4 b^3(b c-a d)^2(a+b x)^2\right)+\frac{1}{2 b^3}\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \right. \\
& \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right)+\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]}{b^3}
\end{aligned}$$

Problem 185: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)^4} d x$$

Optimal (type 4, 561 leaves, 13 steps):

$$\begin{aligned}
& - \frac{2 B^2 d^2 i^3 n^2 (c+d x)}{b^3 g^4 (a+b x)} - \frac{B^2 d i^3 n^2 (c+d x)^2}{4 b^2 g^4 (a+b x)^2} - \frac{2 B^2 i^3 n^2 (c+d x)^3}{27 b g^4 (a+b x)^3} - \frac{2 B d^2 i^3 n (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{b^3 g^4 (a+b x)} \\
& - \frac{B d i^3 n (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 b^2 g^4 (a+b x)^2} - \frac{2 B i^3 n (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9 b g^4 (a+b x)^3} - \frac{d^2 i^3 (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{b^3 g^4 (a+b x)} \\
& - \frac{d i^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 b^2 g^4 (a+b x)^2} - \frac{i^3 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 b g^4 (a+b x)^3} - \frac{d^3 i^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g^4} + \\
& \frac{2 B d^3 i^3 n \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g^4} + \frac{2 B^2 d^3 i^3 n^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g^4}
\end{aligned}$$

Result (type 4, 8160 leaves):

$$\begin{aligned}
& \frac{d^3 i^3 \operatorname{Log}[a+b x] \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2}{b^4 g^4} + \frac{1}{b^4 g^4 (a+b x)} \\
& 3 \left(-A^2 b c d^2 i^3 + a A^2 d^3 i^3 - 2 A b B c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 2 a A B d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \right. \\
& \quad \left. b B^2 c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + a B^2 d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) - \\
& \frac{1}{2 b^4 g^4 (a+b x)^2} 3 \left(A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3 + 2 A b^2 B c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - 4 a A b B c d^2 i^3 \right. \\
& \quad \left. \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 2 a^2 A B d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + b^2 B^2 c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 - \right. \\
& \quad \left. 2 a b B^2 c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + a^2 B^2 d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) + \\
& \frac{1}{3 b^4 g^4 (a+b x)^3} \left(-A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - 2 A b^3 B c^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
& \quad 6 a A b^2 B c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - 6 a^2 A b B c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 2 a^3 A B d^3 i^3 \\
& \quad \left. \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - b^3 B^2 c^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + 3 a b^2 B^2 c^2 d i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 - \right. \\
& \quad \left. 3 a^2 b B^2 c d^2 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + a^3 B^2 d^3 i^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) + \\
& \frac{1}{54 b (b c - a d)^3 g^4 (a+b x)^3} B^2 c^3 i^3 n^2 \left(-4 (b c - a d)^3 + 15 d (b c - a d)^2 (a+b x) + 66 d^2 (-b c + a d) (a+b x)^2 - \right.
\end{aligned}$$

$$\begin{aligned}
& 66 d^3 (a + b x)^3 \operatorname{Log}[a + b x] - 6 (b c - a d) \left(2 (b c - a d)^2 + 3 d (-b c + a d) (a + b x) + 6 d^2 (a + b x)^2 \right) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - \\
& 18 b \left(3 a^2 d^2 (c + d x) + 3 a b d (-c^2 + d^2 x^2) + b^2 (c^3 + d^3 x^3) \right) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 66 d^3 (a + b x)^3 \operatorname{Log}[c + d x] + \frac{1}{g^4} \\
& 2 B c^3 i^3 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right) \left(- \frac{\left(\frac{a}{b} + x \right) \left(3 \operatorname{Log}\left[\frac{a}{b} + x \right] + 9 \operatorname{Log}\left[\frac{a}{b} + x \right]^2 \right)}{27 (a + b x)^4 \operatorname{Log}\left[\frac{a}{b} + x \right]} - \frac{1}{6 b} \left(- \frac{b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{b c}{d} \right)^5 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} - \right. \right. \\
& \left. \frac{4 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{b c}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} + \left(\frac{2 b^3 \left(\frac{c}{d} + x \right)^3}{\left(-a + \frac{b c}{d} \right)^6 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^3} + \frac{6 b^2 \left(\frac{c}{d} + x \right)^2}{\left(-a + \frac{b c}{d} \right)^5 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{6 b \left(\frac{c}{d} + x \right)}{\left(-a + \frac{b c}{d} \right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} \right) \operatorname{Log}\left[\frac{c}{d} + x \right] + \frac{2 \operatorname{Log}\left[1 - \frac{b \left(\frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{\left(-a + \frac{b c}{d} \right)^3} \right) - \\
& \left. \frac{- \operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right]}{3 b (a + b x)^3} \right) + \frac{1}{g^4} 6 B c^2 d i^3 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right) \\
& \left(- \frac{1 + 2 \operatorname{Log}\left[\frac{a}{b} + x \right]}{4 b^2 (a + b x)^2} + \frac{a \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{9 b^2 (a + b x)^3} + \frac{a \left(- \frac{2 \operatorname{Log}\left[\frac{a}{b} + x \right]}{(a + b x)^3} + \frac{d \left(\frac{(b c - a d) (-b c - 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x] \right)}{(b c - a d)^3} \right)}{6 b^2} \right) + \\
& \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x \right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}}{2 b^2 (a + b x)^2} - \frac{(a + 3 b x) \left(- \operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right)}{6 b^2 (a + b x)^3} \right) + \\
& \frac{1}{g^4} 6 B c d^2 i^3 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x} \right] \right) \right) \left(- \frac{1 + \operatorname{Log}\left[\frac{a}{b} + x \right]}{b^3 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{2 b^3 (a + b x)^2} - \frac{a^2 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x \right] \right)}{9 b^3 (a + b x)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{(-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) (\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx])}{b^3 (bc - ad) (a + bx)} - \frac{a^2 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + bx)^3} + \frac{d \left(\frac{(bc - ad)(-bc + 3ad + 2bdx)}{(a + bx)^2} + 2d^2 \operatorname{Log}[a + bx] - 2d^2 \operatorname{Log}[c + dx] \right)}{(bc - ad)^3} \right)}{6b^3} \\
& \left. \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a + bx)(bc - ad + d(a + bx) \operatorname{Log}[a + bx] - d(a + bx) \operatorname{Log}[c + dx])}{(bc - ad)^2} \right)}{b^3 (a + bx)^2} - \frac{(a^2 + 3abx + 3b^2x^2) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right] \right)}{3b^3 (a + bx)^3} \right) + \\
& \frac{1}{g^4} 2Bd^3 i^3 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a + bx}{c + dx} \right] \right) \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2b^4} + \frac{3a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right)}{b^4 (a + bx)} - \frac{3a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right)}{4b^4 (a + bx)^2} + \right. \\
& \frac{a^3 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right] \right)}{9b^4 (a + bx)^3} + \frac{3a \left((-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + bx) (\operatorname{Log}[a + bx] - \operatorname{Log}[c + dx]) \right)}{b^4 (bc - ad) (a + bx)} + \\
& \left. \frac{a^3 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + bx)^3} + \frac{d \left(\frac{(bc - ad)(-bc + 3ad + 2bdx)}{(a + bx)^2} + 2d^2 \operatorname{Log}[a + bx] - 2d^2 \operatorname{Log}[c + dx] \right)}{(bc - ad)^3} \right)}{6b^4} + \frac{3a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a + bx)(bc - ad + d(a + bx) \operatorname{Log}[a + bx] - d(a + bx) \operatorname{Log}[c + dx])}{(bc - ad)^2} \right)}{2b^4 (a + bx)^2} + \right. \\
& \left. \frac{\left(\frac{a(11a^2 + 27abx + 18b^2x^2)}{(a + bx)^3} + 6 \operatorname{Log}[a + bx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right] \right)}{6b^4} - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + bx)}{-bc + ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + dx)}{bc - ad}\right]}{b^4} \right) + \\
& \frac{1}{g^4} 3B^2 c d^2 i^3 n^2 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^3 (a + bx)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{2b^3 (a + bx)^2} - \frac{a^2 \left(2 + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] + 9 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{27b^3 (a + bx)^3} + \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left(-\frac{1 + \operatorname{Log}\left[\frac{a}{b} + x\right]}{b^3 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{2 b^3 (a + b x)^2} - \frac{a^2 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^3 (a + b x)^3} - \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x])}{b^3 (b c - a d) (a + b x)} - \right. \\
& \left. \frac{a^2 \left(-\frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left(\frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x]\right)}{(b c - a d)^3}\right)}{6 b^3} - \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}\right)}{b^3 (a + b x)^2} \right) \\
& \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right]\right) - \frac{(a^2 + 3 a b x + 3 b^2 x^2) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right]\right)^2}{3 b^3 (a + b x)^3} - \\
& 2 \left(\frac{1}{2 b^3 (b c - a d) (a + b x)} \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left((-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - \right. \\
& \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left((b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& \left(a \left(-d (-b c + a d) (a + b x) + (b c - a d)^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) \operatorname{Log}\left[\frac{c}{d} + x\right] + d^2 (a + b x)^2 \operatorname{Log}[a + b x] - d^2 (a + b x)^2 \operatorname{Log}[c + d x] + d (a + b x) \right. \right. \\
& \left. \left. \left(d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 (b c - a d) \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2 d (a + b x) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right) \right) / \\
& \left(2 b^3 (b c - a d)^2 (a + b x)^2 \right) + \frac{1}{36 b^3 (b c - a d)^3 (a + b x)^3} a^2 \left(-2 d (b c - a d)^2 (a + b x) + 4 d^2 (b c - a d) (a + b x)^2 - \right. \\
& 4 (b c - a d)^3 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 d^3 (a + b x)^3 \operatorname{Log}[a + b x] - 4 d^3 (a + b x)^3 \operatorname{Log}[c + d x] + \\
& 3 d (a + b x) \left(2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 d (b c - a d) (a + b x) \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - (b c - a d)^2 \right. \\
& \left. \left. \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 4 d^2 (a + b x)^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right) \right) + \\
& \frac{-b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^3 (b c - a d) (a + b x)} + \frac{1}{b^3 (b c - a d)^2 (a + b x)^2} \\
& a \left(b (c + d x) (-2 a d + b (c - d x)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right.
\end{aligned}$$

$$\begin{aligned}
& 2d(a+bx) \operatorname{Log}\left[\frac{c}{d}+x\right] \left(b(c+dx) + d(a+bx) \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + 2d^2(a+bx)^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \Bigg) + \\
& \left(a^2 \left(-b(3a^2d^2(c+dx) + 3abd(-c^2+d^2x^2) + b^2(c^3+d^3x^3)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - d^2(a+bx)^2 \left(b(c+dx) + 3d(a+bx) \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + \right. \right. \\
& \quad \left. \left. d(a+bx) \operatorname{Log}\left[\frac{c}{d}+x\right] \left(-b(c+dx)(-4ad+b(c-3dx)) + 2d^2(a+bx)^2 \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + 2d^3(a+bx)^3 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \\
& \left(3b^3(bc-ad)^3(a+bx)^3 \right) + \frac{1}{g^4} 3B^2c^2di^3n^2 \left(-\frac{1+2\operatorname{Log}\left[\frac{a}{b}+x\right]+2\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{4b^2(a+bx)^2} + \frac{a(2+6\operatorname{Log}\left[\frac{a}{b}+x\right]+9\operatorname{Log}\left[\frac{a}{b}+x\right]^2)}{27b^2(a+bx)^3} + \right. \\
& \left. 2 \left(-\frac{1+2\operatorname{Log}\left[\frac{a}{b}+x\right]}{4b^2(a+bx)^2} + \frac{a(1+3\operatorname{Log}\left[\frac{a}{b}+x\right])}{9b^2(a+bx)^3} + \frac{a \left(-\frac{2\operatorname{Log}\left[\frac{c}{d}+x\right]}{(a+bx)^3} + \frac{d \left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2\operatorname{Log}[a+bx] - 2d^2\operatorname{Log}[c+dx] \right)}{(bc-ad)^3} \right)}{6b^2} + \right. \right. \\
& \quad \left. \left. \frac{\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}}{2b^2(a+bx)^2} \right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) - \right. \\
& \quad \left. \frac{(a+3bx) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{-a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{6b^2(a+bx)^3} - 2 \left(\left(-d(-bc+ad)(a+bx) + (bc-ad)^2(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]) \right) \operatorname{Log}\left[\frac{c}{d}+x\right] + \right. \right. \\
& \quad \left. \left. d^2(a+bx)^2 \operatorname{Log}[a+bx] - d^2(a+bx)^2 \operatorname{Log}[c+dx] + d(a+bx) \left(d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2(bc-ad)(1+\operatorname{Log}\left[\frac{a}{b}+x\right]) - \right. \right. \right. \\
& \quad \left. \left. \left. 2d(a+bx) \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) / \left(4b^2(bc-ad)^2(a+bx)^2 \right) \Bigg) - \\
& \quad \frac{1}{36b^2(bc-ad)^3(a+bx)^3} a \left(-2d(bc-ad)^2(a+bx) + 4d^2(bc-ad)(a+bx)^2 - 4(bc-ad)^3(1+3\operatorname{Log}\left[\frac{a}{b}+x\right]) \operatorname{Log}\left[\frac{c}{d}+x\right] + \right. \\
& \quad \left. 4d^3(a+bx)^3 \operatorname{Log}[a+bx] - 4d^3(a+bx)^3 \operatorname{Log}[c+dx] + 3d(a+bx) \left(2d^2(a+bx)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 4d(bc-ad)(a+bx) \right. \right. \\
& \quad \left. \left. \left(1+\operatorname{Log}\left[\frac{a}{b}+x\right] \right) - (bc-ad)^2(1+2\operatorname{Log}\left[\frac{a}{b}+x\right]) - 4d^2(a+bx)^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) \Bigg) -
\end{aligned}$$

$$\begin{aligned}
& \left(b (c + d x) (-2 a d + b (c - d x)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \\
& \quad \left. \left(b (c + d x) + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) + 2 d^2 (a + b x)^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) / \left(2 b^2 (b c - a d)^2 (a + b x)^2 \right) - \\
& \left(a \left(-b (3 a^2 d^2 (c + d x) + 3 a b d (-c^2 + d^2 x^2) + b^2 (c^3 + d^3 x^3)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - d^2 (a + b x)^2 \left(b (c + d x) + 3 d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) \right. \right. \\
& \quad \left. \left. d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \left(-b (c + d x) (-4 a d + b (c - 3 d x)) + 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) \right) + \right. \\
& \quad \left. \left. 2 d^3 (a + b x)^3 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left(3 b^2 (b c - a d)^3 (a + b x)^3 \right) + \\
& \frac{1}{g^4} B^2 d^3 i^3 n^2 \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b^4} + \frac{3 a \left(2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^4 (a + b x)} - \frac{3 a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{4 b^4 (a + b x)^2} + \frac{a^3 \left(2 + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] + 9 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{27 b^4 (a + b x)^3} + \right. \\
& \quad \left. \frac{\left(\frac{a (11 a^2 + 27 a b x + 18 b^2 x^2)}{(a + b x)^3} + 6 \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2}{6 b^4} - \frac{1}{b^4 (b c - a d) (a + b x)} \right) \\
& 3 a \left(-b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) - \\
& \left(3 a^2 \left(b (c + d x) (-2 a d + b (c - d x)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \right. \\
& \quad \left. \left. \left(b (c + d x) + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) + 2 d^2 (a + b x)^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left(2 b^4 (b c - a d)^2 (a + b x)^2 \right) - \\
& \left(a^3 \left(-b (3 a^2 d^2 (c + d x) + 3 a b d (-c^2 + d^2 x^2) + b^2 (c^3 + d^3 x^3)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - d^2 (a + b x)^2 \left(b (c + d x) + 3 d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) \right. \right. \\
& \quad \left. \left. d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \left(-b (c + d x) (-4 a d + b (c - 3 d x)) + 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) + 2 d^3 (a + b x)^3 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / \\
& \left(3 b^4 (b c - a d)^3 (a + b x)^3 \right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2b^4} + \frac{3a\left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4(a+bx)} - \frac{3a^2\left(1 + 2\text{Log}\left[\frac{a}{b} + x\right]\right)}{4b^4(a+bx)^2} + \frac{a^3\left(1 + 3\text{Log}\left[\frac{a}{b} + x\right]\right)}{9b^4(a+bx)^3} + \right. \\
& \frac{3a\left((-bc+ad)\text{Log}\left[\frac{c}{d} + x\right] + d(a+bx)\left(\text{Log}[a+bx] - \text{Log}[c+dx]\right)\right)}{b^4(bc-ad)(a+bx)} + \frac{a^3\left(-\frac{2\text{Log}\left[\frac{c}{d} + x\right]}{(a+bx)^3} + \frac{d\left(\frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2\text{Log}[a+bx] - 2d^2\text{Log}[c+dx]\right)}{(bc-ad)^3}\right)}{6b^4} + \\
& \left. \frac{3a^2\left(\text{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\text{Log}[a+bx]-d(a+bx)\text{Log}[c+dx])}{(bc-ad)^2}\right)}{2b^4(a+bx)^2} - \frac{\text{Log}\left[\frac{c}{d} + x\right]\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^4} \right) - \\
& 2\left(-\frac{1}{2b^4(bc-ad)(a+bx)} - 3a\left(d(a+bx)\text{Log}\left[\frac{a}{b} + x\right]^2 + 2\left((-bc+ad)\text{Log}\left[\frac{c}{d} + x\right] + d(a+bx)\left(\text{Log}[a+bx] - \text{Log}[c+dx]\right)\right)\right) - \\
& 2\text{Log}\left[\frac{a}{b} + x\right]\left((bc-ad)\text{Log}\left[\frac{c}{d} + x\right] + d(a+bx)\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) - 2d(a+bx)\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right) - \\
& \left(3a^2\left(-d(-bc+ad)(a+bx) + (bc-ad)^2\left(1 + 2\text{Log}\left[\frac{a}{b} + x\right]\right)\text{Log}\left[\frac{c}{d} + x\right] + d^2(a+bx)^2\text{Log}[a+bx] - d^2(a+bx)^2\text{Log}[c+dx] + d(a+bx)\right.\right. \\
& \left.\left(d(a+bx)\text{Log}\left[\frac{a}{b} + x\right]^2 + 2(bc-ad)\left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right) - 2d(a+bx)\left(\text{Log}\left[\frac{a}{b} + x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)\right)\right) / \\
& \left(4b^4(bc-ad)^2(a+bx)^2\right) - \frac{1}{36b^4(bc-ad)^3(a+bx)^3} a^3\left(-2d(bc-ad)^2(a+bx) + 4d^2(bc-ad)(a+bx)^2 - \right. \\
& 4(bc-ad)^3\left(1 + 3\text{Log}\left[\frac{a}{b} + x\right]\right)\text{Log}\left[\frac{c}{d} + x\right] + 4d^3(a+bx)^3\text{Log}[a+bx] - 4d^3(a+bx)^3\text{Log}[c+dx] + \\
& 3d(a+bx)\left(2d^2(a+bx)^2\text{Log}\left[\frac{a}{b} + x\right]^2 + 4d(bc-ad)(a+bx)\left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right) - (bc-ad)^2\right. \\
& \left.\left(1 + 2\text{Log}\left[\frac{a}{b} + x\right]\right) - 4d^2(a+bx)^2\left(\text{Log}\left[\frac{a}{b} + x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)\right)\right) + \frac{1}{2b^4} \\
& \left(\text{Log}\left[\frac{a}{b} + x\right]^2\left(\text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]\right) - 2\text{Log}\left[\frac{a}{b} + x\right]\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2\text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]\right) +
\end{aligned}$$

$$\left. \frac{\text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b^4} \right\}$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx)^3 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{cix + dix} dx$$

Optimal (type 4, 768 leaves, 25 steps):

$$\begin{aligned} & \frac{bB^2(bc-ad)^2 g^3 n^2 x}{3d^3 i} + \frac{7B(bc-ad)^2 g^3 n(a+bx) \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{3d^3 i} - \frac{b^2 B(bc-ad) g^3 n(c+dx)^2 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{3d^4 i} + \\ & \frac{3(bc-ad)^2 g^3 (a+bx) \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{d^3 i} - \frac{3b^2(bc-ad) g^3 (c+dx)^2 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2d^4 i} + \frac{b^3 g^3 (c+dx)^3 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{3d^4 i} + \\ & \frac{6B(bc-ad)^3 g^3 n \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^4 i} + \frac{(bc-ad)^3 g^3 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^4 i} + \\ & \frac{B^2(bc-ad)^3 g^3 n^2 \text{Log}\left[\frac{a+bx}{c+dx}\right]}{3d^4 i} - \frac{2B^2(bc-ad)^3 g^3 n^2 \text{Log}[c+dx]}{d^4 i} - \frac{7B(bc-ad)^3 g^3 n \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \text{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{3d^4 i} + \\ & \frac{6B^2(bc-ad)^3 g^3 n^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i} + \frac{2B(bc-ad)^3 g^3 n \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i} + \\ & \frac{7B^2(bc-ad)^3 g^3 n^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{3d^4 i} - \frac{2B^2(bc-ad)^3 g^3 n^2 \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i} \end{aligned}$$

Result (type 4, 4914 leaves):

$$\begin{aligned} & \frac{1}{12d^4 i} g^3 \\ & \left(12bd(b^2c^2 - 3abcd + 3a^2d^2) x \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \text{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 - 6b^2d^2(bc-3ad) x^2 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \text{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 + \right. \\ & 4b^3d^3x^3 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \text{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 - 12(bc-ad)^3 \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \text{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 \text{Log}[c+dx] + \\ & \left. 36abd n \left(A + B \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - Bn \text{Log}\left[\frac{a+bx}{c+dx}\right]\right) \left(-2b^2c^2 + 2abcd - b^2cdx + abd^2x + 2b^2c^2 \text{Log}\left[\frac{c}{d} + x\right] - b^2c^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right. \end{aligned}$$

$$\begin{aligned}
& a^2 d^2 \operatorname{Log}[a + b x] - 2 b^2 c d x \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + b^2 d^2 x^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + b^2 c^2 \operatorname{Log}[c + d x] + 2 b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\
& 2 b^2 c^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log}\left[\frac{a}{b} + x\right] \left(a d + b c \operatorname{Log}[c + d x] - b c \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 2 b^2 c^2 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\
& 4 B n \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(6 b^3 c^3 - 6 a b^2 c^2 d + 5 b^3 c^2 d x - 3 a b^2 c d^2 x - 2 a^2 b d^3 x - b^3 c d^2 x^2 + a b^2 d^3 x^2 - \right. \\
& 6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 3 a^2 b c d^2 \operatorname{Log}[a + b x] + 2 a^3 d^3 \operatorname{Log}[a + b x] + 6 b^3 c^2 d x \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - 3 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \\
& 2 b^3 d^3 x^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - 5 b^3 c^3 \operatorname{Log}[c + d x] - 6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^3 c^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \operatorname{Log}[c + d x] + 6 b^2 c^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \\
& \left. \left(a d + b c \operatorname{Log}[c + d x] - b c \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - 6 b^3 c^3 \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) - 12 a^3 B d^3 n \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
& \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \operatorname{Log}[c + d x] - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) - \\
& 36 a^2 B d^2 n \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-2 d(a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right) + 2 b(c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\
& 2 b \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) (d x - c \operatorname{Log}[c + d x]) + 2 b c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \left. \right) + \\
& 4 a^3 B^2 d^3 n^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) + 3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \operatorname{Log}[c + d x] + \right. \\
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \right) \left. \right) + \\
& 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \left. \right) + \\
& B^2 n^2 \left(45 b^3 c^3 - 20 a b^2 c^2 d + 21 a^2 b c d^2 + 4 b^3 c^2 d x - 8 a b^2 c d^2 x + 4 a^2 b d^3 x - 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 44 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] - \right. \\
& 18 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 12 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 6 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 24 a b^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] + \\
& 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
& 8 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 10 a^2 b c d^2 \operatorname{Log}[a + b x] - 12 a^3 d^3 \operatorname{Log}[a + b x] - 12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
& 12 a^2 b c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 8 a^3 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 24 b^3 c^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] - \left. \right)
\end{aligned}$$

$$\begin{aligned}
& 24 a b^2 c^2 d \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 20 b^3 c^2 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - 12 a b^2 c d^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - 8 a^2 b d^3 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - 4 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \\
& 4 a b^2 d^3 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 24 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - 24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \\
& 12 a^2 b c d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 8 a^3 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 12 b^3 c^2 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 6 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + \\
& 4 b^3 d^3 x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 18 b^3 c^3 \operatorname{Log}[c+d x] + 16 a b^2 c^2 d \operatorname{Log}[c+d x] + 8 a^2 b c d^2 \operatorname{Log}[c+d x] + 20 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
& 12 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x] - 20 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
& 12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x] - 20 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x] + 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x] - \\
& 24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x] - 12 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 \operatorname{Log}[c+d x] - 44 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 24 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
& 12 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
& 4 \left(11 b^3 c^3 - 6 a b^2 c^2 d - 3 a^2 b c d^2 - 2 a^3 d^3 + 6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] + 6 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
& 24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 24 b^3 c^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + 24 b^3 c^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \Big) + \\
& 12 a^2 b^2 d^2 n^2 \left(3 d(a+b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right) - b c \operatorname{Log}\left[\frac{c}{d}+x\right]^3 + 3 b(c+d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right) + \right. \\
& 3 b \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 (d x - c \operatorname{Log}[c+d x]) - 6 \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d}+x\right] - b c \operatorname{Log}[c+d x] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{b}+x\right] \left(-d(a+b x) + d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \Big) + \\
& 3 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \left(-2 d(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + 2 b(c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \\
& \left. b c \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 b c \left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \Big) - \\
& 3 b c \left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) + \\
& 3 b c \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \Big) -
\end{aligned}$$

$$\begin{aligned}
& 3 a B^2 d n^2 \left(12 b c d (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) + 3 d^2 (a + b x) \left(7 a - b x + (-6 a + 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
& 4 b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 12 b^2 c (c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + \\
& 3 b^2 (c + d x) \left(7 c - d x + (-6 c + 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - 6 b^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \\
& \left(d x (-2 c + d x) + 2 c^2 \operatorname{Log}[c + d x] \right) + 6 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-4 b c d (a + b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + \right. \\
& 4 b^2 c (c + d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b^2 c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + d^2 \left(b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a + b x] \right) + \\
& \left. b^2 \left(d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c + d x] \right) + 4 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) - \\
& 12 b^2 c^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
& 6 \left(2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] + b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - a^2 d^2 \operatorname{Log}[a + b x] - b^2 c^2 \operatorname{Log}[c + d x] - \right. \\
& 2 a b c d \operatorname{Log}[c + d x] - \operatorname{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \\
& 2 (b^2 c^2 - a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 4 b c \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + (b c - a d) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
& \left. 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right)
\end{aligned}$$

Problem 187: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 573 leaves, 15 steps):

$$\begin{aligned}
& - \frac{B (bc - ad) g^2 n (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{d^2 i} - \frac{2 (bc - ad) g^2 (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^2 i} + \frac{b^2 g^2 (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 d^3 i} \\
& - \frac{4 B (bc - ad)^2 g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right]}{d^3 i} - \frac{(bc - ad)^2 g^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log} \left[\frac{bc-ad}{b(c+dx)} \right]}{d^3 i} + \\
& - \frac{B^2 (bc - ad)^2 g^2 n^2 \operatorname{Log} [c + dx]}{d^3 i} + \frac{B (bc - ad)^2 g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[1 - \frac{b(c+dx)}{d(a+bx)} \right]}{d^3 i} - \\
& - \frac{4 B^2 (bc - ad)^2 g^2 n^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i} - \frac{2 B (bc - ad)^2 g^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i} - \\
& - \frac{B^2 (bc - ad)^2 g^2 n^2 \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{d^3 i} + \frac{2 B^2 (bc - ad)^2 g^2 n^2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{b(c+dx)} \right]}{d^3 i}
\end{aligned}$$

Result (type 4, 2797 leaves):

$$\begin{aligned}
& \frac{1}{12 d^3 i} g^2 \left(-12 b d (bc - 2 a d) x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + \right. \\
& 6 b^2 d^2 x^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 + 12 (bc - a d)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \operatorname{Log} [c + dx] + \\
& 12 B n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-2 b^2 c^2 + 2 a b c d - b^2 c d x + a b d^2 x + 2 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] - b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \right. \\
& a^2 d^2 \operatorname{Log} [a + bx] - 2 b^2 c d x \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b^2 d^2 x^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] + b^2 c^2 \operatorname{Log} [c + dx] + 2 b^2 c^2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c + dx] + \\
& \left. 2 b^2 c^2 \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \operatorname{Log} [c + dx] - 2 b c \operatorname{Log} \left[\frac{a}{b} + x \right] \left(a d + b c \operatorname{Log} [c + dx] - b c \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + 2 b^2 c^2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) - \\
& 12 a^2 B d^2 n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \operatorname{Log} [c + dx] - \right. \\
& \left. 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) - \\
& 24 a B d n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-2 d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c + dx) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\
& \left. 2 b \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) (dx - c \operatorname{Log} [c + dx]) + 2 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \\
& 4 a^2 B^2 d^2 n^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) + 3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \operatorname{Log} [c + dx] + \right. \\
& \left. 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \\
& 6 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 6 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] - 6 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] + \\
& 8 a B^2 d n^2 \left(3 d (a+bx) \left(2 - 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right) - bc \text{Log} \left[\frac{c}{d} + x \right]^3 + 3 b (c+dx) \left(2 - 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right) + \right. \\
& 3 b \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 (dx - c \text{Log} [c+dx]) - 6 \left(ad + 2 b dx - b dx \text{Log} \left[\frac{c}{d} + x \right] - bc \text{Log} [c+dx] + \right. \\
& \left. \text{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) + d(a+bx) \text{Log} \left[\frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad) \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& 3 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(-2 d (a+bx) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c+dx) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - \right. \\
& \left. bc \text{Log} \left[\frac{c}{d} + x \right]^2 + 2 bc \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) - \\
& 3 bc \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& 3 bc \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) - 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] + 2 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right) - \\
& B^2 n^2 \left(12 b c d (a+bx) \left(2 - 2 \text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{a}{b} + x \right]^2 \right) + 3 d^2 (a+bx) \left(7 a - bx + (-6 a + 2 b x) \text{Log} \left[\frac{a}{b} + x \right] + 2 (a - bx) \text{Log} \left[\frac{a}{b} + x \right]^2 \right) - \right. \\
& 4 b^2 c^2 \text{Log} \left[\frac{c}{d} + x \right]^3 + 12 b^2 c (c+dx) \left(2 - 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right) + \\
& 3 b^2 (c+dx) \left(7 c - dx + (-6 c + 2 d x) \text{Log} \left[\frac{c}{d} + x \right] + 2 (c - dx) \text{Log} \left[\frac{c}{d} + x \right]^2 \right) - 6 b^2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 \\
& (dx (-2c+dx) + 2c^2 \text{Log} [c+dx]) + 6 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(-4 b c d (a+bx) \left(-1 + \text{Log} \left[\frac{a}{b} + x \right] \right) + \right. \\
& 4 b^2 c (c+dx) \left(-1 + \text{Log} \left[\frac{c}{d} + x \right] \right) - 2 b^2 c^2 \text{Log} \left[\frac{c}{d} + x \right]^2 + d^2 (bx (2a - bx) + 2 b^2 x^2 \text{Log} \left[\frac{a}{b} + x \right] - 2 a^2 \text{Log} [a+bx]) + \\
& \left. b^2 (dx (-2c+dx) - 2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] + 2 c^2 \text{Log} [c+dx]) + 4 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) - \\
& 12 b^2 c^2 \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) - \\
& 6 \left(2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \text{Log} \left[\frac{c}{d} + x \right] + b^2 d^2 x^2 \text{Log} \left[\frac{c}{d} + x \right] - a^2 d^2 \text{Log} [a+bx] - b^2 c^2 \text{Log} [c+dx] - \right.
\end{aligned}$$

$$\begin{aligned}
& 2 a b c d \operatorname{Log}[c+d x] - \operatorname{Log}\left[\frac{a}{b}+x\right] \left(b d (2 a c+b x (2 c-d x)) - 2 d^2 (a^2-b^2 x^2) \operatorname{Log}\left[\frac{c}{d}+x\right] + (-2 b^2 c^2+2 a^2 d^2) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + \\
& 2 (b^2 c^2-a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 4 b c \left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right] - b c \operatorname{Log}[c+d x] + \right. \\
& \left. \operatorname{Log}\left[\frac{a}{b}+x\right] \left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + (b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c-a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
& 2 b^2 c^2 \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 188: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g+b g x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{c i+d i x} d x$$

Optimal (type 4, 303 leaves, 9 steps):

$$\begin{aligned}
& \frac{g(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{d i} + \frac{2 B(b c-a d) g n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{d^2 i} + \frac{(b c-a d) g\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{d^2 i} + \\
& \frac{2 B^2(b c-a d) g n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i} + \frac{2 B(b c-a d) g n\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i} - \frac{2 B^2(b c-a d) g n^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i}
\end{aligned}$$

Result (type 4, 1367 leaves):

$$\begin{aligned}
& \frac{1}{3 d^2 i} g \left(3 b d x \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 - \right. \\
& 3 (b c - a d) \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \operatorname{Log}[c + d x] - 3 a B d n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \\
& \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \operatorname{Log}[c + d x] - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] \right) \right) - \\
& 3 B n \left(A + B \operatorname{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-2 d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + \right. \\
& \left. 2 b \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) (d x - c \operatorname{Log}[c + d x]) + 2 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] \right) \right) + \\
& a B^2 d n^2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] \right) + 3 \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \operatorname{Log}[c + d x] + \right. \\
& \left. 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] + \right. \\
& \left. 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] \right) \right) \right) + \\
& 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c + d x)}{b c - a d} \right] - 6 \operatorname{PolyLog} \left[3, \frac{d(a + b x)}{-b c + a d} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c + d x)}{b c - a d} \right] \right) + \\
& B^2 n^2 \left(3 d (a + b x) \left(2 - 2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \right) - b c \operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3 b (c + d x) \left(2 - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) + \right. \\
& 3 b \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 (d x - c \operatorname{Log}[c + d x]) - 6 \left(a d + 2 b d x - b d x \operatorname{Log} \left[\frac{c}{d} + x \right] - b c \operatorname{Log}[c + d x] + \right. \\
& \left. \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) + d (a + b x) \operatorname{Log} \left[\frac{c}{d} + x \right] + (b c - a d) \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] \right) + (b c - a d) \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] \right) + \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(-2 d (a + b x) \left(-1 + \operatorname{Log} \left[\frac{a}{b} + x \right] \right) + 2 b (c + d x) \left(-1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) - \right. \\
& \left. b c \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] \right) \right) - \\
& 3 b c \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c + d x)}{b c - a d} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a + b x)}{-b c + a d} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d(a + b x)}{-b c + a d} \right] \right) + \\
& \left. 3 b c \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d(a + b x)}{-b c + a d} \right] \right) - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c + d x)}{b c - a d} \right] + 2 \operatorname{PolyLog} \left[3, \frac{b(c + d x)}{b c - a d} \right] \right) \right) \right)
\end{aligned}$$

Problem 189: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)^2}{ci + dix} dx$$

Optimal (type 4, 137 leaves, 4 steps):

$$\frac{\left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{di} - \frac{2Bn \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{di} + \frac{2B^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{di}$$

Result (type 4, 537 leaves):

$$\begin{aligned} & \frac{1}{3di} \left(3 \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right] - Bn \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 \operatorname{Log}[c+dx] - 3Bn \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right] - Bn \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right. \\ & \left. \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \operatorname{Log}[c+dx] - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) + \\ & B^2 n^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + 3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 \operatorname{Log}[c+dx] + \right. \\ & \left. 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \right. \\ & \left. 3 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) + \\ & \left. 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \end{aligned}$$

Problem 191: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)^2}{(ag + bgx)^2 (ci + dix)} dx$$

Optimal (type 3, 199 leaves, 7 steps):

$$\frac{2B^2 n^2 (c+dx)}{(bc-ad)^2 g^2 i (a+bx)} - \frac{2Bn (c+dx) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)}{(bc-ad)^2 g^2 i (a+bx)} - \frac{b(c+dx) \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)^2}{(bc-ad)^2 g^2 i (a+bx)} - \frac{d \left(A + B \operatorname{Log}\left[e^{\left(\frac{a+bx}{c+dx}\right)^n}\right]\right)^3}{3B (bc-ad)^2 g^2 i n}$$

Result (type 3, 793 leaves):

$$\begin{aligned}
& - \frac{B^2 d n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^3}{3(bc-ad)^2 g^2 i} + \frac{2 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \left(A + B n + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right)}{(-bc+ad) g^2 i (a+bx)} + \frac{1}{(-bc+ad)^2 g^2 i (a+bx)} \operatorname{Log}\left[\frac{a+bx}{c+dx} \right]^2 \\
& \left(-a A B d n - b B^2 c n^2 - A b B d n x - b B^2 d n^2 x - a B^2 d n \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - b B^2 d n x \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right) + \\
& \frac{1}{(bc-ad) g^2 i (a+bx)} \left(-A^2 - 2 A B n - 2 B^2 n^2 - 2 A B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - \right. \\
& \left. 2 B^2 n \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - B^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 \right) - \frac{1}{(bc-ad)^2 g^2 i} \\
& d \operatorname{Log}[a+bx] \left(A^2 + 2 A B n + 2 B^2 n^2 + 2 A B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + 2 B^2 n \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + \right. \\
& \left. B^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 \right) + \frac{1}{(bc-ad)^2 g^2 i} d \left(A^2 + 2 A B n + 2 B^2 n^2 + 2 A B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - \right. \\
& \left. 2 B^2 n \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + B^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 \right) \operatorname{Log}[c+dx]
\end{aligned}$$

Problem 192: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ag+bgx)^3 (ci+dix)} dx$$

Optimal (type 3, 369 leaves, 9 steps):

$$\begin{aligned}
& \frac{4 b B^2 d n^2 (c+dx)}{(bc-ad)^3 g^3 i (a+bx)} - \frac{b^2 B^2 n^2 (c+dx)^2}{4 (bc-ad)^3 g^3 i (a+bx)^2} + \frac{4 b B d n (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{(bc-ad)^3 g^3 i (a+bx)} - \frac{b^2 B n (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 (bc-ad)^3 g^3 i (a+bx)^2} + \\
& \frac{2 b d (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(bc-ad)^3 g^3 i (a+bx)} - \frac{b^2 (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 (bc-ad)^3 g^3 i (a+bx)^2} + \frac{d^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^3}{3 B (bc-ad)^3 g^3 i n}
\end{aligned}$$

Result (type 3, 975 leaves):

$$\begin{aligned}
& \frac{1}{12 (bc - ad)^3 g^3 i (a + bx)^2} \\
& \left(4 B^2 d^2 n^2 (a + bx)^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^3 + 6 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 \left(2 a^2 A d^2 - b^2 B c^2 n + 4 a b B c d n + 4 a A b d^2 x + 2 b^2 B c d n x + 4 a b B d^2 n x + \right. \right. \\
& \quad \left. \left. 2 A b^2 d^2 x^2 + 3 b^2 B d^2 n x^2 + 2 B d^2 (a + bx)^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 2 B d^2 n (a + bx)^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] - 6 B (bc - ad) n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right. \right. \\
& \quad \left. \left. \left(2 A b c - 6 a A d + b B c n - 7 a B d n - 4 A b d x - 6 b B d n x + 2 B (-3 a d + b (c - 2 d x)) \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] + 2 B n (-b c + 3 a d + 2 b d x) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) - \right. \right. \\
& \quad \left. \left. 3 (bc - ad)^2 \left(2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - 2 B n (2 A + B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + \right. \right. \right. \\
& \quad \left. \left. 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(2 A + B n - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) + 6 d (bc - ad) (a + bx) \left(2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - \right. \right. \\
& \quad \left. \left. 2 B n (2 A + 3 B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(2 A + 3 B n - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) \right) + \\
& \quad \left. \left. 6 d^2 (a + bx)^2 \operatorname{Log} [a + bx] \left(2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - 2 B n (2 A + 3 B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + \right. \right. \right. \\
& \quad \left. \left. 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(2 A + 3 B n - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) \right) - \\
& \quad \left. \left. 6 d^2 (a + bx)^2 \left(2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - 2 B n (2 A + 3 B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + \right. \right. \right. \\
& \quad \left. \left. 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(2 A + 3 B n - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) \right) \operatorname{Log} [c + dx] \right)
\end{aligned}$$

Problem 193: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{(a g + b g x)^4 (c i + d i x)} dx$$

Optimal (type 3, 543 leaves, 11 steps):

$$\begin{aligned}
& - \frac{6 b B^2 d^2 n^2 (c + dx)}{(bc - ad)^4 g^4 i (a + bx)} + \frac{3 b^2 B^2 d n^2 (c + dx)^2}{4 (bc - ad)^4 g^4 i (a + bx)^2} - \frac{2 b^3 B^2 n^2 (c + dx)^3}{27 (bc - ad)^4 g^4 i (a + bx)^3} - \frac{6 b B d^2 n (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)}{(bc - ad)^4 g^4 i (a + bx)} + \\
& \frac{3 b^2 B d n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)}{2 (bc - ad)^4 g^4 i (a + bx)^2} - \frac{2 b^3 B n (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)}{9 (bc - ad)^4 g^4 i (a + bx)^3} - \frac{3 b d^2 (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{(bc - ad)^4 g^4 i (a + bx)} + \\
& \frac{3 b^2 d (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{2 (bc - ad)^4 g^4 i (a + bx)^2} - \frac{b^3 (c + dx)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{3 (bc - ad)^4 g^4 i (a + bx)^3} - \frac{d^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^3}{3 B (bc - ad)^4 g^4 i n}
\end{aligned}$$

Result (type 3, 1295 leaves):

$$\begin{aligned}
 & - \frac{1}{108 (bc - ad)^4 g^4 i (a + bx)^3} \left(36 B^2 d^3 n^2 (a + bx)^3 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^3 + 18 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 \right. \\
 & \quad \left(6 a^3 A d^3 + 2 b^3 B c^3 n - 9 a b^2 B c^2 d n + 18 a^2 b B c d^2 n + 18 a^2 A b d^3 x - 3 b^3 B c^2 d n x + 18 a b^2 B c d^2 n x + 18 a^2 b B d^3 n x + 18 a A b^2 d^3 x^2 + \right. \\
 & \quad \left. 6 b^3 B c d^2 n x^2 + 27 a b^2 B d^3 n x^2 + 6 A b^3 d^3 x^3 + 11 b^3 B d^3 n x^3 + 6 B d^3 (a + bx)^3 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 6 B d^3 n (a + bx)^3 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - \\
 & 3 d (bc - ad)^2 (a + bx) \left(18 A^2 + 30 A B n + 19 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
 & 6 d^2 (bc - ad) (a + bx)^2 \left(18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
 & 6 d^3 (a + bx)^3 \operatorname{Log}[a + bx] \left(18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
 & 4 (bc - ad)^3 \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + \right. \\
 & \quad \left. 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
 & 6 B (bc - ad) n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(3 d (-bc + ad) (a + bx) \left(6 A + 5 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + \right. \\
 & \quad \left. 6 d^2 (a + bx)^2 \left(6 A + 11 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + 4 (bc - ad)^2 \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
 & 6 d^3 (a + bx)^3 \left(18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \operatorname{Log}[c + dx] \Big)
 \end{aligned}$$

Problem 194: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 770 leaves, 18 steps):

$$\begin{aligned}
& \frac{2AB(bc-ad)^2 g^3 n(a+bx)}{d^3 i^2 (c+dx)} - \frac{2B^2(bc-ad)^2 g^3 n^2(a+bx)}{d^3 i^2 (c+dx)} + \frac{2B^2(bc-ad)^2 g^3 n(a+bx) \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{d^3 i^2 (c+dx)} - \\
& \frac{bB(bc-ad) g^3 n(a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{d^3 i^2} - \frac{3b(bc-ad) g^3 (a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{d^3 i^2} - \\
& \frac{(bc-ad)^2 g^3 (a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{d^3 i^2 (c+dx)} + \frac{b^3 g^3 (c+dx)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2d^4 i^2} - \\
& \frac{6bB(bc-ad)^2 g^3 n \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^4 i^2} - \frac{3b(bc-ad)^2 g^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^4 i^2} + \\
& \frac{bB^2(bc-ad)^2 g^3 n^2 \operatorname{Log}[c+dx]}{d^4 i^2} + \frac{bB(bc-ad)^2 g^3 n \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{d^4 i^2} - \\
& \frac{6bB^2(bc-ad)^2 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^2} - \frac{6bB(bc-ad)^2 g^3 n \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^2} - \\
& \frac{bB^2(bc-ad)^2 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{d^4 i^2} + \frac{6bB^2(bc-ad)^2 g^3 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^4 i^2}
\end{aligned}$$

Result (type 4, 5396 leaves):

$$\begin{aligned}
& \frac{a^3 B^2 g^3 n^2 (a+bx) \left(2 - 2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2\right)}{(bc-ad) i^2 (c+dx)} - \\
& \frac{b^2 (2bc-3ad) g^3 x \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)^2}{d^3 i^2} + \frac{b^3 g^3 x^2 \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)^2}{2d^2 i^2} + \\
& \frac{1}{d^4 i^2 (c+dx)} \left(A^2 b^3 c^3 g^3 - 3aA^2 b^2 c^2 d g^3 + 3a^2 A^2 bc d^2 g^3 - a^3 A^2 d^3 g^3 + 2Ab^3 Bc^3 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - \right. \\
& \quad 6aAb^2 Bc^2 d g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + 6a^2 ABc d^2 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - 2a^3 ABd^3 g^3 \\
& \quad \left. \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + b^3 B^2 c^3 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 - 3ab^2 B^2 c^2 d g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 + \right. \\
& \quad \left. 3a^2 b B^2 c d^2 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 - a^3 B^2 d^3 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2 \right) + \\
& \frac{3b(bc-ad)^2 g^3 \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)^2 \operatorname{Log}[c+dx]}{d^4 i^2} + \frac{1}{i^2} 2a^3 B g^3 n \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)
\end{aligned}$$

$$\left(\frac{\left(\frac{c}{d} + x\right) \left(\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{(c + dx)^2 \text{Log}\left[\frac{c}{d} + x\right]} + \frac{\frac{d\left(\frac{a}{b} + x\right) \text{Log}\left[\frac{a}{b} + x\right]}{\left(-c + \frac{ad}{b}\right)^2 \left(1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right)} + \frac{\text{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right]}{-c + \frac{ad}{b}}}{d} - \frac{-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]}{d(c + dx)} \right) +$$

$$\frac{1}{i^2} 2 b^3 B g^3 n \left(A + B \left(\text{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \text{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \left(-\frac{2c\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^3} + \frac{2c\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3} - \right.$$

$$\frac{3c^2 \text{Log}\left[\frac{c}{d} + x\right]^2}{2d^4} - \frac{c^3 \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^4(c + dx)} + \frac{-\frac{1}{2}b\left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \text{Log}[a+bx]}{b^3}\right) + \frac{1}{2}x^2 \text{Log}\left[\frac{a+bx}{b}\right]}{d^2} - \frac{c^3 \left(-\frac{\text{Log}\left[\frac{a+x}{b}\right]}{d(c+dx)} - \frac{b \text{Log}[a+bx]}{d(-bc+ad)} + \frac{b \text{Log}[c+dx]}{d(-bc+ad)}\right)}{d^3} -$$

$$\frac{-\frac{1}{2}d\left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \text{Log}[c+dx]}{d^3}\right) + \frac{1}{2}x^2 \text{Log}\left[\frac{c+dx}{d}\right]}{d^2} + \frac{\left(-4cdx + d^2x^2 + \frac{2c^3}{c+dx} + 6c^2 \text{Log}[c + dx]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{2d^4} +$$

$$\left. \frac{3c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^4} \right) + \frac{1}{i^2} 6 a b^2 B g^3 n \left(A + B \left(\text{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \text{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right)$$

$$\left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \text{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \frac{c^2 \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3(c + dx)} + \frac{c^2 \left(-\frac{\text{Log}\left[\frac{a+x}{b}\right]}{d(c+dx)} - \frac{b \text{Log}[a+bx]}{d(-bc+ad)} + \frac{b \text{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} +$$

$$\left. \frac{\left(dx - \frac{c^2}{c+dx} - 2c \text{Log}[c + dx]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{d^3} - \frac{2c \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} \right) +$$

$$\frac{1}{i^2} 6 a^2 b B g^3 n \left(A + B \left(\text{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - n \text{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \left(-\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2(c + dx)} - \frac{c \left(-\frac{\text{Log}\left[\frac{a+x}{b}\right]}{d(c+dx)} - \frac{b \text{Log}[a+bx]}{d(-bc+ad)} + \frac{b \text{Log}[c+dx]}{d(-bc+ad)}\right)}{d} +$$

$$\begin{aligned}
& \left. \left(\frac{\left(\frac{c}{c+dx} + \text{Log}[c+dx] \right) \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)}{d^2} + \frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2} \right) \right. \\
& \frac{1}{i^2} b^3 B^2 g^3 n^2 \left(-\frac{2c(a+bx) \left(2 - 2\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{a}{b}+x\right]^2 \right)}{bd^3} + \frac{(a+bx) \left(-7a+bx + (6a-2bx)\text{Log}\left[\frac{a}{b}+x\right] - 2(a-bx)\text{Log}\left[\frac{a}{b}+x\right]^2 \right)}{4b^2d^2} \right. \\
& \frac{c^2 \text{Log}\left[\frac{c}{d}+x\right]^3}{d^4} - \frac{2c(c+dx) \left(2 - 2\text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^4} + \frac{c^3 \left(2 + 2\text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^4(c+dx)} + \\
& \frac{(c+dx) \left(-7c+dx + (6c-2dx)\text{Log}\left[\frac{c}{d}+x\right] - 2(c-dx)\text{Log}\left[\frac{c}{d}+x\right]^2 \right)}{4d^4} + \\
& \frac{\left(-4cdx + d^2x^2 + \frac{2c^3}{c+dx} + 6c^2 \text{Log}[c+dx] \right) \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2d^4} - \frac{1}{d^4(-bc+ad)(c+dx)} \\
& c^3 \left(-d(a+bx)\text{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx)\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx)\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 2 \left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \left(-\frac{2c\left(\frac{a}{b}+x\right) \left(-1 + \text{Log}\left[\frac{a}{b}+x\right] \right)}{d^3} + \frac{2c\left(\frac{c}{d}+x\right) \left(-1 + \text{Log}\left[\frac{c}{d}+x\right] \right)}{d^3} - \right. \\
& \frac{3c^2 \text{Log}\left[\frac{c}{d}+x\right]^2}{2d^4} - \frac{c^3 \left(1 + \text{Log}\left[\frac{c}{d}+x\right] \right)}{d^4(c+dx)} + \frac{-\frac{1}{2}b \left(-\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \text{Log}[a+bx]}{b^3} \right) + \frac{1}{2}x^2 \text{Log}\left[\frac{a+bx}{b}\right]}{d^2} - \frac{c^3 \left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \text{Log}[a+bx]}{d(-bc+ad)} + \frac{b \text{Log}[c+dx]}{d(-bc+ad)} \right)}{d^3} \\
& \left. - \frac{\frac{1}{2}d \left(-\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \text{Log}[c+dx]}{d^3} \right) + \frac{1}{2}x^2 \text{Log}\left[\frac{c+dx}{d}\right]}{d^2} + \frac{3c^2 \left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{d^4} \right) + \\
& \frac{3c^2 \left(\text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2\text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2\text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right)}{d^4} - 2 \left(-\frac{1}{bd^4} 2c \left(ad + 2bdx - bdx \text{Log}\left[\frac{c}{d}+x\right] - bc \right. \right. \\
& \left. \left. \text{Log}[c+dx] + \text{Log}\left[\frac{a}{b}+x\right] \left(-d(a+bx) + d(a+bx)\text{Log}\left[\frac{c}{d}+x\right] + (bc-ad)\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad)\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{4 b^2 d^4} \left(-2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] - b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + a^2 d^2 \operatorname{Log}[a + b x] + b^2 c^2 \operatorname{Log}[c + d x] + \right. \\
& \quad 2 a b c d \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + \\
& \quad (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - \left(c^3 \left(2 (b c - a d) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a + b x] - \right. \right. \right. \\
& \quad \left. \left. \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}[c + d x] \right) - 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) / (2 d^4 (-b c + a d) (c + d x)) + \frac{1}{2 d^4} \\
& \quad \left. \left. \left. 3 c^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right) \right) + \\
& \frac{1}{i^2} 3 a b^2 B^2 g^3 n^2 \left(\frac{(a + b x) (2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2)}{b d^2} - \frac{2 c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \frac{(c + d x) (2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2)}{d^3} - \right. \\
& \quad \frac{c^2 (2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2)}{d^3 (c + d x)} + \frac{(d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x]) (-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right])^2}{d^3} + \\
& \quad \frac{1}{d^3 (-b c + a d) (c + d x)} c^2 \left(-d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& \quad 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \left(\frac{\left(\frac{a}{b} + x\right) (-1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{d^2} - \frac{\left(\frac{c}{d} + x\right) (-1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{d^2} + \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right. \\
& \quad \left. \frac{c^2 (1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{d^3 (c + d x)} + \frac{c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)} \right)}{d^2} - \frac{2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)}{d^3} \right) - \\
& \quad \frac{2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a + b x)}{-b c + a d}\right] \right)}{d^3} - \\
& \quad 2 \left(\frac{1}{b d^3} \left(a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& (bc - ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \left(c^2 \left(2(bc - ad) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a+bx] - \right. \right. \right. \\
& \left. \left. \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \left(2d^3(-bc+ad)(c+dx) \right) - \frac{1}{d^3} \\
& c \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg) + \\
& \frac{1}{i^2} 3a^2 b B^2 g^3 n^2 \left(\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3d^2} + \frac{c \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^2(c+dx)} + \frac{\left(\frac{c}{c+dx} + \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{d^2} - \right. \\
& \frac{1}{d^2(-bc+ad)(c+dx)} c \left(-d(a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \\
& \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2d^2} - \frac{c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{d^2(c+dx)} - \frac{c \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)} \right)}{d} + \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2} \right) + \\
& \frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]}{d^2} - \\
& 2 \left(- \left(\left(c \left(2(bc - ad) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - \right. \right. \right. \right. \\
& \left. \left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) / \left(2d^2(-bc+ad)(c+dx) \right) + \frac{1}{2d^2} \\
& \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg)
\end{aligned}$$

Problem 195: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 500 leaves, 12 steps):

$$\begin{aligned} & - \frac{2 A B (b c - a d) g^2 n (a + b x)}{d^2 i^2 (c + d x)} + \frac{2 B^2 (b c - a d) g^2 n^2 (a + b x)}{d^2 i^2 (c + d x)} - \frac{2 B^2 (b c - a d) g^2 n (a + b x) \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right]}{d^2 i^2 (c + d x)} + \\ & \frac{b g^2 (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^2 i^2} + \frac{(b c - a d) g^2 (a + b x) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^2 i^2 (c + d x)} + \frac{2 b B (b c - a d) g^2 n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)} \right]}{d^3 i^2} + \\ & \frac{2 b (b c - a d) g^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)} \right]}{d^3 i^2} + \frac{2 b B^2 (b c - a d) g^2 n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i^2} + \\ & \frac{4 b B (b c - a d) g^2 n \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i^2} - \frac{4 b B^2 (b c - a d) g^2 n^2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)} \right]}{d^3 i^2} \end{aligned}$$

Result (type 4, 3186 leaves):

$$\begin{aligned} & \frac{a^2 B^2 g^2 n^2 (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] + \operatorname{Log}\left[\frac{a+bx}{c+dx} \right]^2 \right)}{(b c - a d) i^2 (c + d x)} + \frac{b^2 g^2 x \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{d^2 i^2} + \frac{1}{d^3 i^2 (c + d x)} \\ & \left(-A^2 b^2 c^2 g^2 + 2 a A^2 b c d g^2 - a^2 A^2 d^2 g^2 - 2 A b^2 B c^2 g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) + 4 a A b B c d g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - \right. \\ & \quad 2 a^2 A B d^2 g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) - b^2 B^2 c^2 g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 + \\ & \quad \left. 2 a b B^2 c d g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 - a^2 B^2 d^2 g^2 \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right)^2 \right) - \\ & \frac{2 b (b c - a d) g^2 \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right)^2 \operatorname{Log}[c + d x]}{d^3 i^2} + \frac{1}{i^2} 2 a^2 B g^2 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right) \\ & \left(\frac{\left(\frac{c}{d} + x \right) \left(\operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right]^2 \right)}{(c + d x)^2 \operatorname{Log}\left[\frac{c}{d} + x \right]} + \frac{\frac{d \left(\frac{a}{b} + x \right) \operatorname{Log}\left[\frac{a}{b} + x \right]}{\left(-c + \frac{a d}{b} \right)^2 \left(1 - \frac{d \left(\frac{a}{b} + x \right)}{-c + \frac{a d}{b}} \right)} + \frac{\operatorname{Log}\left[1 - \frac{d \left(\frac{a}{b} + x \right)}{-c + \frac{a d}{b}} \right]}{-c + \frac{a d}{b}} - \frac{-\operatorname{Log}\left[\frac{a}{b} + x \right] + \operatorname{Log}\left[\frac{c}{d} + x \right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right]}{d (c + d x)} \right) + \\ & \frac{1}{i^2} 2 b^2 B g^2 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx} \right] \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \frac{c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + dx)} + \frac{c^2 \left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d (-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d (-bc+ad)}\right)}{d^2} \right. \\
& \left. + \frac{\left(dx - \frac{c^2}{c+dx} - 2c \operatorname{Log}[c+dx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{d^3} - \frac{2c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} \right) + \\
& \frac{1}{i^2} 4 a b B g^2 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c + dx)} - \frac{c \left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d (-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d (-bc+ad)}\right)}{d} \right. \\
& \left. + \frac{\left(\frac{c}{c+dx} + \operatorname{Log}[c+dx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)}{d^2} + \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2} \right) + \\
& \frac{1}{i^2} b^2 B^2 g^2 n^2 \left(\frac{(a+bx) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{b d^2} - \frac{2c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \frac{(c+dx) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3} - \right. \\
& \frac{c^2 \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3 (c + dx)} + \frac{\left(dx - \frac{c^2}{c+dx} - 2c \operatorname{Log}[c+dx]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)^2}{d^3} + \\
& \frac{1}{d^3 (-bc+ad) (c+dx)} c^2 \left(-d (a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2b (c+dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b (c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
& 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right. \\
& \left. \frac{c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + dx)} + \frac{c^2 \left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d (-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d (-bc+ad)}\right)}{d^2} - \frac{2c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^3} \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{2c \left(\text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d^3} - \\
& 2 \left(\frac{1}{b d^3} \left(a d + 2 b d x - b d x \text{Log} \left[\frac{c}{d} + x \right] - b c \text{Log} [c + d x] + \text{Log} \left[\frac{a}{b} + x \right] \left(-d (a + b x) + d (a + b x) \text{Log} \left[\frac{c}{d} + x \right] + (b c - a d) \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] \right) \right. \right. \\
& \quad \left. \left. (b c - a d) \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \left(c^2 \left(2 (b c - a d) \text{Log} \left[\frac{a}{b} + x \right] \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + b (c + d x) \left(\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \text{Log} [a + b x] - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 \text{Log} [c + d x] \right) - 2 b (c + d x) \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) / \left(2 d^3 (-b c + a d) (c + d x) \right) - \frac{1}{d^3} \\
& \quad \left. \left. c \left(\text{Log} \left[\frac{c}{d} + x \right]^2 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) - 2 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] + 2 \text{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) + \\
& \frac{1}{i^2} 2 a b B^2 g^2 n^2 \left(\frac{\text{Log} \left[\frac{c}{d} + x \right]^3}{3 d^2} + \frac{c \left(2 + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2 \right)}{d^2 (c + d x)} + \frac{\left(\frac{c}{c + d x} + \text{Log} [c + d x] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right)^2}{d^2} - \right. \\
& \quad \frac{1}{d^2 (-b c + a d) (c + d x)} c \left(-d (a + b x) \text{Log} \left[\frac{a}{b} + x \right]^2 + 2 b (c + d x) \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 b (c + d x) \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& \quad 2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \\
& \quad \left(-\frac{\text{Log} \left[\frac{c}{d} + x \right]^2}{2 d^2} - \frac{c \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^2 (c + d x)} - \frac{c \left(-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a + b x]}{d (-b c + a d)} + \frac{b \text{Log} [c + d x]}{d (-b c + a d)} \right)}{d} + \frac{\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right]}{d^2} \right) + \\
& \quad \frac{\text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] - 2 \text{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right]}{d^2} - \\
& \quad 2 \left(- \left(\left(c \left(2 (b c - a d) \text{Log} \left[\frac{a}{b} + x \right] \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right) + b (c + d x) \left(\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \text{Log} [a + b x] - 2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] + 2 \text{Log} [c + d x] \right) \right) \right. \right. \\
& \quad \left. \left. 2 b (c + d x) \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) / \left(2 d^2 (-b c + a d) (c + d x) \right) + \frac{1}{2 d^2}
\end{aligned}$$

$$\left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right)$$

Problem 196: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx) \left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ci + dix)^2} dx$$

Optimal (type 4, 282 leaves, 9 steps):

$$\frac{2ABgn(a+bx)}{di^2(c+dx)} - \frac{2B^2gn^2(a+bx)}{di^2(c+dx)} + \frac{2B^2gn(a+bx)\text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right]}{di^2(c+dx)} - \frac{g(a+bx)\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{di^2(c+dx)} -$$

$$\frac{bg\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)} \right]}{d^2i^2} - \frac{2bBgn\left(A + B \text{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^2i^2} + \frac{2bB^2gn^2 \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)} \right]}{d^2i^2}$$

Result (type 4, 1305 leaves):

$$\begin{aligned}
& \frac{1}{i^2} g \left(\frac{(bc - ad) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - Bn \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2}{d^2 (c+dx)} + \frac{aB^2n^2 (a+bx) \left(2 - 2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] + \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 \right)}{(bc - ad) (c+dx)} + \right. \\
& \frac{b \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - Bn \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 \operatorname{Log} [c+dx]}{d^2} + \frac{1}{d(-bc+ad)(c+dx)} 2aBn \left(-A - B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + Bn \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \\
& \left(bc - ad + b(c+dx) \operatorname{Log} \left[\frac{a}{b} + x \right] + (-bc+ad) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] - bc \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] - bdx \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + \frac{1}{d^2} \\
& bBn \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - Bn \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left(-\operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [c+dx] + 2 \left(-\frac{c}{c+dx} + \frac{bc \operatorname{Log} [a+bx]}{-bc+ad} + \frac{bc \operatorname{Log} [c+dx]}{bc-ad} - \right. \right. \\
& \left. \left. \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [c+dx] + \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \left(\frac{c}{c+dx} + \operatorname{Log} [c+dx] \right) + \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
& \frac{1}{3d^2(bc-ad)(c+dx)} bB^2n^2 \left((bc-ad)(c+dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^3 + 3c(bc-ad) \left(2 + 2 \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \right) + \right. \\
& 3(bc-ad) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 (c + (c+dx) \operatorname{Log} [c+dx]) + \\
& 3c \operatorname{Log} \left[\frac{a}{b} + x \right] \left(-d(a+bx) \operatorname{Log} \left[\frac{a}{b} + x \right] + 2b(c+dx) \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) + 6bc(c+dx) \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + 3 \\
& \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \left((bc-ad)(c+dx) \operatorname{Log} \left[\frac{c}{d} + x \right]^2 + 2c(bc-ad) \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + 2c \left((-bc+ad) \operatorname{Log} \left[\frac{a}{b} + x \right] + \right. \right. \\
& \left. \left. b(c+dx) (\operatorname{Log} [a+bx] - \operatorname{Log} [c+dx]) \right) - 2(bc-ad)(c+dx) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) + \\
& 3(bc-ad)(c+dx) \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) - \\
& 3 \left(c \left(2(bc-ad) \operatorname{Log} \left[\frac{a}{b} + x \right] \left(1 + \operatorname{Log} \left[\frac{c}{d} + x \right] \right) + b(c+dx) \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 - 2 \operatorname{Log} [a+bx] - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 2 \operatorname{Log} [c+dx] \right) - \right. \\
& \left. 2b(c+dx) \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad)(c+dx) \\
& \left. \left(\operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) - 2 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] + 2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \right) \right) \right)
\end{aligned}$$

Problem 197: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ci+di)^2} dx$$

Optimal (type 3, 163 leaves, 4 steps):

$$-\frac{2ABn(a+bx)}{(bc-ad)i^2(c+dx)} + \frac{2B^2n^2(a+bx)}{(bc-ad)i^2(c+dx)} - \frac{2B^2n(a+bx)\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{(bc-ad)i^2(c+dx)} + \frac{(a+bx)\left(A+B\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)i^2(c+dx)}$$

Result (type 3, 391 leaves):

$$\frac{1}{d(-bc+ad)i^2(c+dx)} \left(A^2bc - aA^2d - 2ABc n + 2ABdn + 2bB^2cn^2 - 2aB^2dn^2 + B^2(bc-ad)\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - bB^2cn^2\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 - bB^2dn^2x\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + \right. \\ \left. 2bBn(c+dx)\operatorname{Log}[a+bx] \left(-A+Bn - B\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] + Bn\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + 2ABc n\operatorname{Log}[c+dx] - 2bB^2cn^2\operatorname{Log}[c+dx] + \right. \\ \left. 2ABdnx\operatorname{Log}[c+dx] - 2bB^2dn^2x\operatorname{Log}[c+dx] - 2bB^2cn^2\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\operatorname{Log}[c+dx] - \right. \\ \left. 2bB^2dn^2x\operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\operatorname{Log}[c+dx] + 2B\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left((bc-ad)(A-Bn) + bBn(c+dx)\operatorname{Log}[c+dx]\right) \right)$$

Problem 198: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ag+bg)(ci+di)^2} dx$$

Optimal (type 3, 231 leaves, 7 steps):

$$\frac{2ABdn(a+bx)}{(bc-ad)^2gi^2(c+dx)} - \frac{2B^2dn^2(a+bx)}{(bc-ad)^2gi^2(c+dx)} + \\ \frac{2B^2dn(a+bx)\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{(bc-ad)^2gi^2(c+dx)} - \frac{d(a+bx)\left(A+B\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)^2gi^2(c+dx)} + \frac{b\left(A+B\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3}{3B(bc-ad)^2gi^2n}$$

Result (type 3, 789 leaves):

$$\begin{aligned}
& \frac{b B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^3}{3 (bc-ad)^2 g i^2} - \frac{2 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \left(-A + B n - B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)}{(bc-ad) g i^2 (c+dx)} + \frac{1}{(bc-ad)^2 g i^2 (c+dx)} \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 \\
& \left(A b B c n - a B^2 d n^2 + A b B d n x - b B^2 d n^2 x + b B^2 c n \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + b B^2 d n x \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \\
& \frac{1}{(bc-ad) g i^2 (c+dx)} \left(A^2 - 2 A B n + 2 B^2 n^2 + 2 A B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - \right. \\
& \left. 2 B^2 n \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + B^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2\right) + \frac{1}{(bc-ad)^2 g i^2} \\
& b \operatorname{Log}[a+bx] \left(A^2 - 2 A B n + 2 B^2 n^2 + 2 A B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - 2 B^2 n \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + \right. \\
& \left. B^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2\right) - \frac{1}{(bc-ad)^2 g i^2} b \left(A^2 - 2 A B n + 2 B^2 n^2 + 2 A B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - \right. \\
& \left. 2 B^2 n \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + B^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)^2\right) \operatorname{Log}[c+dx]
\end{aligned}$$

Problem 199: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ag+bgx)^2 (ci+dix)^2} dx$$

Optimal (type 3, 392 leaves, 10 steps):

$$\begin{aligned}
& -\frac{2 A B d^2 n (a+bx)}{(bc-ad)^3 g^2 i^2 (c+dx)} + \frac{2 B^2 d^2 n^2 (a+bx)}{(bc-ad)^3 g^2 i^2 (c+dx)} - \frac{2 b^2 B^2 n^2 (c+dx)}{(bc-ad)^3 g^2 i^2 (a+bx)} - \frac{2 B^2 d^2 n (a+bx) \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{(bc-ad)^3 g^2 i^2 (c+dx)} \\
& \frac{2 b^2 B n (c+dx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{(bc-ad)^3 g^2 i^2 (a+bx)} + \frac{d^2 (a+bx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)^3 g^2 i^2 (c+dx)} - \frac{b^2 (c+dx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)^3 g^2 i^2 (a+bx)} - \frac{2 b d \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3}{3 B (bc-ad)^3 g^2 i^2 n}
\end{aligned}$$

Result (type 3, 870 leaves):

$$\begin{aligned}
& - \frac{1}{3 (bc - ad)^3 g^2 i^2 (a + bx) (c + dx)} \\
& \left(2 b B^2 d n^2 (a + bx) (c + dx) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^3 + 3 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 \left(2 a A b c d + b^2 B c^2 n - a^2 B d^2 n + 2 A b^2 c d x + 2 a A b d^2 x + 2 b^2 B c d n x - \right. \right. \\
& \quad \left. \left. 2 a b B d^2 n x + 2 A b^2 d^2 x^2 + 2 b B d (a + bx) (c + dx) \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 2 b B d n (a + bx) (c + dx) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + 6 B (bc - ad) n \right. \\
& \quad \left. \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \left(A b c + a A d + b B c n - a B d n + 2 A b d x + B (a d + b (c + 2 d x)) \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - B n (bc + a d + 2 b d x) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + \right. \\
& \quad \left. 6 b d (a + bx) (c + dx) \operatorname{Log} [a + bx] \left(A^2 + 2 B^2 n^2 + 2 A B \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + B^2 \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right)^2 \right) + \right. \\
& \quad \left. 3 b (bc - ad) (c + dx) \left(A^2 + 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2 - 2 B n (A + B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + \right. \\
& \quad \left. 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(A + B n - B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) + 3 d (bc - ad) (a + bx) \left(A^2 - 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2 + \\
& \quad \left. 2 B n (-A + B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 - 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(-A + B n + B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) - \\
& \quad \left. 6 b d (a + bx) (c + dx) \left(A^2 + 2 B^2 n^2 + 2 A B \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + B^2 \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right)^2 \right) \operatorname{Log} [c + dx] \right)
\end{aligned}$$

Problem 200: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{(ag + b gx)^3 (ci + dix)^2} dx$$

Optimal (type 3, 560 leaves, 12 steps):

$$\begin{aligned}
& \frac{2 A B d^3 n (a + bx)}{(bc - ad)^4 g^3 i^2 (c + dx)} - \frac{2 B^2 d^3 n^2 (a + bx)}{(bc - ad)^4 g^3 i^2 (c + dx)} + \frac{6 b^2 B^2 d n^2 (c + dx)}{(bc - ad)^4 g^3 i^2 (a + bx)} - \frac{b^3 B^2 n^2 (c + dx)^2}{4 (bc - ad)^4 g^3 i^2 (a + bx)^2} + \\
& \frac{2 B^2 d^3 n (a + bx) \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]}{(bc - ad)^4 g^3 i^2 (c + dx)} + \frac{6 b^2 B d n (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)}{(bc - ad)^4 g^3 i^2 (a + bx)} - \frac{b^3 B n (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)}{2 (bc - ad)^4 g^3 i^2 (a + bx)^2} - \\
& \frac{d^3 (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{(bc - ad)^4 g^3 i^2 (c + dx)} + \frac{3 b^2 d (c + dx) \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{(bc - ad)^4 g^3 i^2 (a + bx)} - \frac{b^3 (c + dx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^2}{2 (bc - ad)^4 g^3 i^2 (a + bx)^2} + \frac{b d^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \right)^3}{B (bc - ad)^4 g^3 i^2 n}
\end{aligned}$$

Result (type 3, 1340 leaves):

$$\begin{aligned}
& \frac{1}{4 (bc - ad)^4 g^3 i^2 (a + bx)^2 (c + dx)} \\
& \left(4 b B^2 d^2 n^2 (a + bx)^2 (c + dx) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^3 + 2 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 \left(6 a^2 A b c d^2 - b^3 B c^3 n + 6 a b^2 B c^2 d n - 2 a^3 B d^3 n + \right. \right. \\
& \quad 12 a A b^2 c d^2 x + 6 a^2 A b d^3 x + 3 b^3 B c^2 d n x + 12 a b^2 B c d^2 n x - 6 a^2 b B d^3 n x + 6 A b^3 c d^2 x^2 + 12 a A b^2 d^3 x^2 + 9 b^3 B c d^2 n x^2 + \\
& \quad \left. 6 A b^3 d^3 x^3 + 3 b^3 B d^3 n x^3 + 6 b B d^2 (a + bx)^2 (c + dx) \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 6 b B d^2 n (a + bx)^2 (c + dx) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + \\
& \quad 2 b d (bc - ad) (a + bx) (c + dx) \left(4 A^2 + 10 A B n + 11 B^2 n^2 + 4 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 2 B n (4 A + 5 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 4 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(4 A + 5 B n - 4 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
& \quad b (bc - ad)^2 (c + dx) \left(2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& \quad 6 b d^2 (a + bx)^2 (c + dx) \operatorname{Log}[a + bx] \left(2 A^2 + 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& \quad 2 B (bc - ad) n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(2 b d (a + bx) (c + dx) \left(4 A + 5 B n + 4 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 4 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - \right. \\
& \quad \left. b (bc - ad) (c + dx) \left(2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + 4 d^2 (a + bx)^2 \left(A - B n + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& \quad 4 d^2 (bc - ad) (a + bx)^2 \left(A^2 - 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 + 2 B n (-A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(-A + B n + B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
& \quad 6 b d^2 (a + bx)^2 (c + dx) \left(2 A^2 + 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \operatorname{Log}[c + dx] \Big)
\end{aligned}$$

Problem 201: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 \right)^2}{(ag + bgx)^4 (ci + dix)^2} dx$$

Optimal (type 3, 729 leaves, 14 steps):

$$\begin{aligned}
& - \frac{2 A B d^4 n (a + b x)}{(b c - a d)^5 g^4 i^2 (c + d x)} + \frac{2 B^2 d^4 n^2 (a + b x)}{(b c - a d)^5 g^4 i^2 (c + d x)} - \frac{12 b^2 B^2 d^2 n^2 (c + d x)}{(b c - a d)^5 g^4 i^2 (a + b x)} + \frac{b^3 B^2 d n^2 (c + d x)^2}{(b c - a d)^5 g^4 i^2 (a + b x)^2} - \frac{2 b^4 B^2 n^2 (c + d x)^3}{27 (b c - a d)^5 g^4 i^2 (a + b x)^3} - \\
& \frac{2 B^2 d^4 n (a + b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c - a d)^5 g^4 i^2 (c + d x)} - \frac{12 b^2 B d^2 n (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c - a d)^5 g^4 i^2 (a + b x)} + \frac{2 b^3 B d n (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c - a d)^5 g^4 i^2 (a + b x)^2} - \\
& \frac{2 b^4 B n (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9 (b c - a d)^5 g^4 i^2 (a + b x)^3} + \frac{d^4 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^5 g^4 i^2 (c + d x)} - \frac{6 b^2 d^2 (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^5 g^4 i^2 (a + b x)} + \\
& \frac{2 b^3 d (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^5 g^4 i^2 (a + b x)^2} - \frac{b^4 (c + d x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 (b c - a d)^5 g^4 i^2 (a + b x)^3} - \frac{4 b d^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B (b c - a d)^5 g^4 i^2 n}
\end{aligned}$$

Result (type 3, 1695 leaves):

1

$$\begin{aligned}
& - \frac{1}{27 (bc - ad)^5 g^4 i^2 (a + bx)^3 (c + dx)} \\
& \left(36 b B^2 d^3 n^2 (a + bx)^3 (c + dx) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^3 + 9 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 \left(12 a^3 A b c d^3 + b^4 B c^4 n - 6 a b^3 B c^3 d n + 18 a^2 b^2 B c^2 d^2 n - 3 a^4 B d^4 n + \right. \right. \\
& \quad 36 a^2 A b^2 c d^3 x + 12 a^3 A b d^4 x - 2 b^4 B c^3 d n x + 18 a b^3 B c^2 d^2 n x + 36 a^2 b^2 B c d^3 n x - 12 a^3 b B d^4 n x + 36 a A b^3 c d^3 x^2 + \\
& \quad 36 a^2 A b^2 d^4 x^2 + 6 b^4 B c^2 d^2 n x^2 + 54 a b^3 B c d^3 n x^2 + 12 A b^4 c d^3 x^3 + 36 a A b^3 d^4 x^3 + 22 b^4 B c d^3 n x^3 + 18 a b^3 B d^4 n x^3 + \\
& \quad \left. 12 A b^4 d^4 x^4 + 10 b^4 B d^4 n x^4 + 12 b B d^3 (a + bx)^3 (c + dx) \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 12 b B d^3 n (a + bx)^3 (c + dx) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + \\
& 3 b d^2 (bc - ad) (a + bx)^2 (c + dx) \left(27 A^2 + 78 A B n + 92 B^2 n^2 + 27 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (9 A + 13 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 27 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(9 A + 13 B n - 9 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& 6 b d^3 (a + bx)^3 (c + dx) \operatorname{Log}[a + bx] \left(18 A^2 + 30 A B n + 55 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& b (bc - ad)^3 (c + dx) \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 9 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
& 3 b d (bc - ad)^2 (a + bx) (c + dx) \left(9 A^2 + 12 A B n + 7 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (3 A + 2 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 9 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(3 A + 2 B n - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& 6 B (bc - ad) n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(3 b d^2 (a + bx)^2 (c + dx) \left(9 A + 13 B n + 9 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 9 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + \right. \\
& \quad b (bc - ad)^2 (c + dx) \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) - 3 b d (bc - ad) (a + bx) (c + dx) \\
& \quad \left. \left(3 A + 2 B n + 3 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + 9 d^3 (a + bx)^3 \left(A - B n + B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) + \\
& 27 d^3 (bc - ad) (a + bx)^3 \left(A^2 - 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 + 2 B n (-A + B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(-A + B n + B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\
& 6 b d^3 (a + bx)^3 (c + dx) \left(18 A^2 + 30 A B n + 55 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right]^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\
& \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + bx}{c + dx}\right)^n\right] \left(6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) \operatorname{Log}[c + dx]
\end{aligned}$$

Problem 202: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(c i + d i x)^3} dx$$

Optimal (type 4, 676 leaves, 14 steps):

$$\begin{aligned} & \frac{B^2 (bc - ad) g^3 n^2 (a + bx)^2}{4 d^2 i^3 (c + dx)^2} - \frac{4 A b B (bc - ad) g^3 n (a + bx)}{d^3 i^3 (c + dx)} + \frac{4 b B^2 (bc - ad) g^3 n^2 (a + bx)}{d^3 i^3 (c + dx)} - \frac{4 b B^2 (bc - ad) g^3 n (a + bx) \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]}{d^3 i^3 (c + dx)} \\ & \frac{B (bc - ad) g^3 n (a + bx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{2 d^2 i^3 (c + dx)^2} + \frac{b^2 g^3 (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^3 i^3} + \frac{(bc - ad) g^3 (a + bx)^2 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 d^2 i^3 (c + dx)^2} + \\ & \frac{2 b (bc - ad) g^3 (a + bx) \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^3 i^3 (c + dx)} + \frac{2 b^2 B (bc - ad) g^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{Log} \left[\frac{bc - ad}{b (c + dx)} \right]}{d^4 i^3} + \\ & \frac{3 b^2 (bc - ad) g^3 \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2 \operatorname{Log} \left[\frac{bc - ad}{b (c + dx)} \right]}{d^4 i^3} + \frac{2 b^2 B^2 (bc - ad) g^3 n^2 \operatorname{PolyLog} \left[2, \frac{d (a + bx)}{b (c + dx)} \right]}{d^4 i^3} + \\ & \frac{6 b^2 B (bc - ad) g^3 n \left(A + B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right) \operatorname{PolyLog} \left[2, \frac{d (a + bx)}{b (c + dx)} \right]}{d^4 i^3} - \frac{6 b^2 B^2 (bc - ad) g^3 n^2 \operatorname{PolyLog} \left[3, \frac{d (a + bx)}{b (c + dx)} \right]}{d^4 i^3} \end{aligned}$$

Result (type 4, 6600 leaves):

$$\begin{aligned} & \frac{b^3 g^3 x \left(A + B \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right)^2}{d^3 i^3} - \\ & \frac{1}{d^4 i^3 (c + dx)} \left(A^2 b^3 c^2 g^3 - 2 a A^2 b^2 c d g^3 + a^2 A^2 b d^2 g^3 + 2 A b^3 B c^2 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - 4 a A b^2 B c d g^3 \right. \\ & \quad \left. \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + 2 a^2 A b B d^2 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + b^3 B^2 c^2 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - \right. \\ & \quad \left. 2 a b^2 B^2 c d g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + a^2 b B^2 d^2 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 \right) + \\ & \frac{1}{2 d^4 i^3 (c + dx)^2} \left(A^2 b^3 c^3 g^3 - 3 a A^2 b^2 c^2 d g^3 + 3 a^2 A^2 b c d^2 g^3 - a^3 A^2 d^3 g^3 + 2 A b^3 B c^3 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - \right. \\ & \quad \left. 6 a A b^2 B c^2 d g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + 6 a^2 A b B c d^2 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - 2 a^3 A B d^3 g^3 \right. \\ & \quad \left. \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + b^3 B^2 c^3 g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 - 3 a b^2 B^2 c^2 d g^3 \left(\operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right)^2 + \right. \end{aligned}$$

$$\begin{aligned}
 & 3 a^2 b B^2 c d^2 g^3 \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 - a^3 B^2 d^3 g^3 \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 - \\
 & \frac{3 b^2 (bc - ad) g^3 \left(A + B \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right)^2 \text{Log}[c+dx]}{d^4 i^3} + \\
 & \left(a^3 B^2 g^3 n^2 \left(-7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c+dx)^2 \text{Log}[a+bx] + 2 (bc - ad) (3 bc - ad + 2 b d x) \text{Log}\left[\frac{a+bx}{c+dx}\right] - \right. \right. \\
 & \quad \left. \left. 2 d (a+bx) (-2 bc + ad - b d x) \text{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 6 b^2 c^2 \text{Log}[c+dx] + 12 b^2 c d x \text{Log}[c+dx] + 6 b^2 d^2 x^2 \text{Log}[c+dx] \right) \right) / \\
 & \left(4 d (bc - ad)^2 i^3 (c+dx)^2 + \frac{1}{i^3} 2 a^3 B g^3 n \left(A + B \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \right) \left(\frac{\left(\frac{c}{d} + x\right) \left(2 \text{Log}\left[\frac{c}{d} + x\right] + 4 \text{Log}\left[\frac{c}{d} + x\right]^2 \right)}{8 (c+dx)^3 \text{Log}\left[\frac{c}{d} + x\right]} + \right. \\
 & \left. \frac{\frac{d\left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} - \left(\frac{d^2\left(\frac{a}{b} + x\right)^2}{\left(-c + \frac{ad}{b}\right)^4 \left(1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)^2} + \frac{2 d\left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} \right) \text{Log}\left[\frac{a}{b} + x\right] - \frac{\text{Log}\left[1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right]}{\left(-c + \frac{ad}{b}\right)^2}}{2 d} - \frac{-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]}{2 d (c+dx)^2} + \frac{1}{i^3} \right) \\
 & 6 a^2 b B g^3 n \left(A + B \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \left(\frac{1 + \text{Log}\left[\frac{c}{d} + x\right]}{d^2 (c+dx)} - \frac{c (1 + 2 \text{Log}\left[\frac{c}{d} + x\right])}{4 d^2 (c+dx)^2} + \frac{-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c+dx)} - \frac{b \text{Log}[a+bx]}{d (-b c + a d)} + \frac{b \text{Log}[c+dx]}{d (-b c + a d)}}{d} - \right. \\
 & \left. \frac{c \left(-\text{Log}\left[\frac{a}{b} + x\right] + \frac{b (c+dx) (bc - ad + b (c+dx) \text{Log}[a+bx] - b (c+dx) \text{Log}[c+dx])}{(bc - ad)^2} \right)}{2 d^2 (c+dx)^2} - \frac{(c + 2 dx) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)}{2 d^2 (c+dx)^2} + \frac{1}{i^3} 2 b^3 B g^3 n \right) \\
 & \left(A + B \left(\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \left(\frac{\left(\frac{a}{b} + x\right) (-1 + \text{Log}\left[\frac{a}{b} + x\right])}{d^3} - \frac{\left(\frac{c}{d} + x\right) (-1 + \text{Log}\left[\frac{c}{d} + x\right])}{d^3} + \frac{3 c \text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^4} + \frac{3 c^2 (1 + \text{Log}\left[\frac{c}{d} + x\right])}{d^4 (c+dx)} \right) -
 \end{aligned}$$

$$\begin{aligned}
& \frac{c^3 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^4 (c + d x)^2} + \frac{3 c^2 \left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+d x)} - \frac{b \operatorname{Log}[a+b x]}{d (-b c+a d)} + \frac{b \operatorname{Log}[c+d x]}{d (-b c+a d)}\right)}{d^3} - \frac{c^3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c+d x) (b c-a d+b (c+d x) \operatorname{Log}[a+b x]-b (c+d x) \operatorname{Log}[c+d x])}{(b c-a d)^2}\right)}{2 d^4 (c + d x)^2} \\
& \left. \frac{\left(-2 d x + \frac{c^2 (5 c+6 d x)}{(c+d x)^2} + 6 c \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right)}{2 d^4} - \frac{3 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]\right)}{d^4} \right) + \\
& \frac{1}{i^3} 6 a b^2 B g^3 n \left(A + B \left(\operatorname{Log}\left[e \left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right) \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^3} - \frac{2 c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^3 (c + d x)^2} - \right. \\
& \left. \frac{2 c \left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+d x)} - \frac{b \operatorname{Log}[a+b x]}{d (-b c+a d)} + \frac{b \operatorname{Log}[c+d x]}{d (-b c+a d)}\right)}{d^2} + \frac{c^2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c+d x) (b c-a d+b (c+d x) \operatorname{Log}[a+b x]-b (c+d x) \operatorname{Log}[c+d x])}{(b c-a d)^2}\right)}{2 d^3 (c + d x)^2} + \right. \\
& \left. \frac{\left(\frac{c (3 c+4 d x)}{(c+d x)^2} + 2 \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right)}{2 d^3} + \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]}{d^3} \right) + \\
& \frac{1}{i^3} 3 a^2 b B^2 g^3 n^2 \left(-\frac{2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2 (c + d x)} + \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 d^2 (c + d x)^2} + \right. \\
& \left. 2 \left(\frac{1 + \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d (c+d x)} - \frac{b \operatorname{Log}[a+b x]}{d (-b c+a d)} + \frac{b \operatorname{Log}[c+d x]}{d (-b c+a d)}}{d} - \frac{c \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b (c+d x) (b c-a d+b (c+d x) \operatorname{Log}[a+b x]-b (c+d x) \operatorname{Log}[c+d x])}{(b c-a d)^2}\right)}{2 d^2 (c + d x)^2}\right) \right. \\
& \left. \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right) - \frac{(c + 2 d x) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right)^2}{2 d^2 (c + d x)^2} + \right. \\
& \left. \frac{-d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]}{d^2 (-b c+a d) (c + d x)} + \right. \\
& \left. \left(c \left(d (a + b x) (a d - b (2 c + d x)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + d x)^2 \operatorname{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right]\right)\right)
\end{aligned}$$

$$\begin{aligned}
& \left(d (a + b x) + b (c + d x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 b^2 (c + d x)^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \Bigg) / \left(2 d^2 (b c - a d)^2 (c + d x)^2 \right) - \\
& 2 \left(\left(2 (b c - a d) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a + b x] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}[c + d x] \right) - \right. \right. \\
& \quad \left. \left. 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) / \left(2 d^2 (-b c + a d) (c + d x) \right) + \left(c \left(-b (b c - a d) (c + d x) + (b c - a d)^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \right. \right. \\
& \quad \left. \left. \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2 (c + d x)^2 \operatorname{Log}[a + b x] + b^2 (c + d x)^2 \operatorname{Log}[c + d x] + b (c + d x) \left(b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 (b c - a d) \right. \right. \right. \\
& \quad \left. \left. \left. \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b (c + d x) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) / \left(4 d^2 (b c - a d)^2 (c + d x)^2 \right) \Bigg) + \\
& \frac{1}{i^3} b^3 B^2 g^3 n^2 \left(\frac{(a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b d^3} - \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{d^4} + \frac{(c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^4} - \right. \\
& \quad \frac{3 c^2 \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^4 (c + d x)} + \frac{c^3 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{4 d^4 (c + d x)^2} - \\
& \quad \left. \frac{\left(-2 d x + \frac{c^2 (5 c + 6 d x)}{(c + d x)^2} + 6 c \operatorname{Log}[c + d x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2}{2 d^4} + \frac{1}{d^4 (-b c + a d) (c + d x)} \right) \\
& 3 c^2 \left(-d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
& \left(c^3 \left(d (a + b x) (a d - b (2 c + d x)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + d x)^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
& \quad \left. \left. \left(d (a + b x) + b (c + d x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 b^2 (c + d x)^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) / \left(2 d^4 (b c - a d)^2 (c + d x)^2 \right) + \\
& 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \left(\frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{d^3} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3} \right) + \\
& \frac{3 c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^4} + \frac{3 c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{d^4 (c + d x)} - \frac{c^3 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{4 d^4 (c + d x)^2} + \frac{3 c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)} \right)}{d^3} -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{c^3 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right) - 3c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{2d^4(c+dx)^2} \right. \\
& \left. - \frac{3c \left(\operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right)}{d^4} \right. \\
& 2 \left(\frac{1}{bd^4} \left(ad + 2bdx - bdx \operatorname{Log}\left[\frac{c}{d} + x\right] - bc \operatorname{Log}[c+dx] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left(-d(a+bx) + d(a+bx) \operatorname{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) \right) \right. \\
& \quad \left. (bc-ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \left(3c^2 \left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \right. \\
& \quad \left. \left. b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \\
& \quad \left(2d^4(-bc+ad)(c+dx) \right) + \left(c^3 \left(-b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2(c+dx)^2 \operatorname{Log}[a+bx] + \right. \right. \\
& \quad \left. \left. b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2(bc-ad) \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - \right. \right. \right. \\
& \quad \left. \left. \left. 2b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) \right) / \left(4d^4(bc-ad)^2(c+dx)^2 \right) - \frac{1}{2d^4} \\
& \left. 3c \left(\operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) + \\
& \frac{1}{i^3} 3ab^2B^2g^3n^2 \left(\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3d^3} + \frac{2c \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^3(c+dx)} - \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{4d^3(c+dx)^2} + \right. \\
& \left. \frac{\left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2d^3} - \frac{1}{d^3(-bc+ad)(c+dx)} \right. \\
& \left. 2c \left(-d(a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
& \left. \left(c^2 \left(d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) / \\
& \left(2d^3(bc-ad)^2(c+dx)^2 + 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \right. \\
& \left(-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^3} - \frac{2c(1+\operatorname{Log}\left[\frac{c}{d}+x\right])}{d^3(c+dx)} + \frac{c^2(1+2\operatorname{Log}\left[\frac{c}{d}+x\right])}{4d^3(c+dx)^2} - \frac{2c\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b\operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b\operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} + \right. \\
& \left. \left. \frac{c^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^3(c+dx)^2} + \frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) + \\
& \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2\operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} - \\
& 2 \left(-\frac{1}{d^3(-bc+ad)(c+dx)} c \left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + \right. \\
& \left. b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2\operatorname{Log}[a+bx] - 2\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2\operatorname{Log}[c+dx] \right) - 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) - \\
& \left(c^2 \left(-b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + 2\operatorname{Log}\left[\frac{c}{d}+x\right] \right) - b^2(c+dx)^2 \operatorname{Log}[a+bx] + b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \right. \right. \\
& \left. \left. \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(bc-ad) \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - 2b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) / \\
& \left(4d^3(bc-ad)^2(c+dx)^2 + \frac{1}{2d^3} \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \right. \\
& \left. \left. 2\operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right)
\end{aligned}$$

Problem 203: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag+bgx)^2 \left(A+B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ci+dix)^3} dx$$

Optimal (type 4, 441 leaves, 11 steps):

$$\begin{aligned}
 & -\frac{B^2 g^2 n^2 (a+bx)^2}{4 d i^3 (c+dx)^2} + \frac{2 A b B g^2 n (a+bx)}{d^2 i^3 (c+dx)} - \frac{2 b B^2 g^2 n^2 (a+bx)}{d^2 i^3 (c+dx)} + \frac{2 b B^2 g^2 n (a+bx) \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{d^2 i^3 (c+dx)} + \\
 & \frac{B g^2 n (a+bx)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{2 d i^3 (c+dx)^2} - \frac{g^2 (a+bx)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2 d i^3 (c+dx)^2} - \frac{b g^2 (a+bx) \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{d^2 i^3 (c+dx)} - \\
 & \frac{b^2 g^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{d^3 i^3} - \frac{2 b^2 B g^2 n \left(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3 i^3} + \frac{2 b^2 B^2 g^2 n^2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3 i^3}
 \end{aligned}$$

Result (type 4, 4247 leaves):

$$\begin{aligned}
 & -\frac{1}{d^3 i^3 (c+dx)^2} \left(-A^2 b^2 c g^2 + a A^2 b d g^2 - 2 A b^2 B c g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) + 2 a A b B d g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) - \right. \\
 & \quad \left. b^2 B^2 c g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + a b B^2 d g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 \right) + \frac{1}{2 d^3 i^3 (c+dx)^2} \\
 & \quad \left(-A^2 b^2 c^2 g^2 + 2 a A^2 b c d g^2 - a^2 A^2 d^2 g^2 - 2 A b^2 B c^2 g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) + 4 a A b B c d g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) - \right. \\
 & \quad \left. 2 a^2 A B d^2 g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) - b^2 B^2 c^2 g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + \right. \\
 & \quad \left. 2 a b B^2 c d g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 - a^2 B^2 d^2 g^2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 \right) + \\
 & \quad \frac{b^2 g^2 \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right)^2 \operatorname{Log}[c+dx]}{d^3 i^3} + \\
 & \quad \left(a^2 B^2 g^2 n^2 \left(-7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c+dx)^2 \operatorname{Log}[a+bx] + 2 (bc-ad) (3bc-ad+2bdx) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] - \right. \right. \\
 & \quad \left. \left. 2 d (a+bx) (-2bc+ad-bdx) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 6 b^2 c^2 \operatorname{Log}[c+dx] + 12 b^2 c d x \operatorname{Log}[c+dx] + 6 b^2 d^2 x^2 \operatorname{Log}[c+dx] \right) \right) / \\
 & \quad \left(4 d (bc-ad)^2 i^3 (c+dx)^2 + \frac{1}{i^3} 2 a^2 B g^2 n \left(A+B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \right) \left(\frac{\left(\frac{c}{d}+x\right) \left(2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{8 (c+dx)^3 \operatorname{Log}\left[\frac{c}{d}+x\right]} + \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{\frac{d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} - \left(\frac{d^2 \left(\frac{a}{b} + x\right)^2}{\left(-c + \frac{ad}{b}\right)^4 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)^2} + \frac{2 d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{ad}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right)} \right) \text{Log} \left[\frac{a}{b} + x \right] - \frac{\text{Log} \left[1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}} \right]}{\left(-c + \frac{ad}{b}\right)^2}}{2 d} - \frac{-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right]}{2 d (c + d x)^2} \right. + \frac{1}{i^3} \\
& 4 a b B g^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(\frac{1 + \text{Log} \left[\frac{c}{d} + x \right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)}}{d} - \right. \\
& \left. \frac{c \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^2 (c + d x)^2} - \frac{(c + 2 d x) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{2 d^2 (c + d x)^2} \right) + \\
& \frac{1}{i^3} 2 b^2 B g^2 n \left(A + B \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \right) \left(-\frac{\text{Log} \left[\frac{c}{d} + x \right]^2}{2 d^3} - \frac{2 c \left(1 + \text{Log} \left[\frac{c}{d} + x \right] \right)}{d^3 (c + d x)} + \frac{c^2 \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^3 (c + d x)^2} - \right. \\
& \frac{2 c \left(-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)} \right)}{d^2} + \frac{c^2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^3 (c + d x)^2} + \\
& \left. \frac{\left(\frac{c (3c+4dx)}{(c+dx)^2} + 2 \text{Log} [c + d x] \right) \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{2 d^3} + \frac{\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c+dx)}{bc-ad} \right] + \text{PolyLog} \left[2, \frac{d (a+bx)}{-bc+ad} \right]}{d^3} \right) + \\
& \frac{1}{i^3} 2 a b B^2 g^2 n^2 \left(-\frac{2 + 2 \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{c}{d} + x \right]^2}{d^2 (c + d x)} + \frac{c \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] + 2 \text{Log} \left[\frac{c}{d} + x \right]^2 \right)}{4 d^2 (c + d x)^2} + \right. \\
& \left. 2 \left(\frac{1 + \text{Log} \left[\frac{c}{d} + x \right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \text{Log} \left[\frac{c}{d} + x \right] \right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\text{Log} \left[\frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a+bx]}{d (-bc+ad)} + \frac{b \text{Log} [c+dx]}{d (-bc+ad)}}{d} - \frac{c \left(-\text{Log} \left[\frac{a}{b} + x \right] + \frac{b (c+dx) (bc-ad+b (c+dx) \text{Log} [a+bx] - b (c+dx) \text{Log} [c+dx])}{(bc-ad)^2} \right)}{2 d^2 (c + d x)^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) - \frac{(c+2dx) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2d^2(c+dx)^2} + \\
& \frac{-d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^2(-bc+ad)(c+dx)} + \\
& \left(c \left(d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
& \quad \left. \left. \left(d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \left(2d^2(bc-ad)^2(c+dx)^2 \right) - \\
& 2 \left(\left(2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) \right. \right. \\
& \quad \left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \left(2d^2(-bc+ad)(c+dx) \right) + \left(c \left(-b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
& \quad \left. \left. \left(1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - b^2(c+dx)^2 \operatorname{Log}[a+bx] + b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \left(b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(bc-ad) \right. \right. \right. \\
& \quad \left. \left. \left. \left(1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - 2b(c+dx) \left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) \right) / \left(4d^2(bc-ad)^2(c+dx)^2 \right) \Bigg) + \\
& \frac{1}{i^3} b^2 B^2 g^2 n^2 \left(\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^3}{3d^3} + \frac{2c \left(2 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^3(c+dx)} - \frac{c^2 \left(1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{4d^3(c+dx)^2} + \right. \\
& \quad \left. \frac{\left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c+dx] \right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2d^3} - \frac{1}{d^3(-bc+ad)(c+dx)} \right. \\
& \quad \left. 2c \left(-d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
& \quad \left(c^2 \left(d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \\
& \quad \left. \left. 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \\
& \quad \left(2d^3(bc-ad)^2(c+dx)^2 \right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left(-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2d^3} - \frac{2c\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3(c+dx)} + \frac{c^2\left(1+2\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{4d^3(c+dx)^2} - \frac{2c\left(-\frac{\operatorname{Log}\left[\frac{a+x}{b}\right]}{d(c+dx)} - \frac{b\operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b\operatorname{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} \right. \\
& \left. + \frac{c^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\operatorname{Log}[a+bx]-b(c+dx)\operatorname{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^3(c+dx)^2} + \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) + \\
& \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2\operatorname{Log}\left[\frac{a}{b}+x\right]\operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 2\operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} - 2\left(-\frac{1}{d^3(-bc+ad)(c+dx)} \right. \\
& c\left(2(bc-ad)\operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right) + b(c+dx)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2\operatorname{Log}[a+bx] - 2\operatorname{Log}\left[\frac{c}{d}+x\right]\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2\operatorname{Log}[c+dx]\right) - \right. \\
& \left. 2b(c+dx)\operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right) - \left(c^2\left(-b(bc-ad)(c+dx) + (bc-ad)^2\operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+2\operatorname{Log}\left[\frac{c}{d}+x\right]\right) - \right. \right. \\
& \left. \left. b^2(c+dx)^2\operatorname{Log}[a+bx] + b^2(c+dx)^2\operatorname{Log}[c+dx] + b(c+dx)\left(b(c+dx)\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(bc-ad)\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right) - \right. \right. \right. \\
& \left. \left. \left. 2b(c+dx)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)\right)\right) \right) / \left(4d^3(bc-ad)^2(c+dx)^2\right) + \frac{1}{2d^3} \\
& \left. \left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right]\right) - 2\operatorname{Log}\left[\frac{c}{d}+x\right]\operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2\operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]\right)\right)
\end{aligned}$$

Problem 204: Result more than twice size of optimal antiderivative.

$$\int \frac{(ag + bgx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(ci + dix)^3} dx$$

Optimal (type 3, 151 leaves, 3 steps):

$$\frac{B^2 g n^2 (a+bx)^2}{4(bc-ad)i^3(c+dx)^2} - \frac{Bgn(a+bx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{2(bc-ad)i^3(c+dx)^2} + \frac{g(a+bx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2(bc-ad)i^3(c+dx)^2}$$

Result (type 3, 582 leaves):

$$\frac{1}{4 d^2 (b c - a d) i^3 (c + d x)^2}$$

$$g \left(2 B^2 d^2 n^2 (a + b x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 b^2 B n (c + d x)^2 \operatorname{Log}[a + b x] \left(-2 A + B n - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right.$$

$$2 B (b c - a d) n (a d + b (c + 2 d x)) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left(-2 A + B n - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + (b c - a d)^2 \left(2 A^2 - 2 A B n + B^2 n^2 + \right.$$

$$2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left. \right) -$$

$$2 b (b c - a d) (c + d x) \left(2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - \right.$$

$$\left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 b^2 B n (c + d x)^2 \left(-2 A + B n - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \operatorname{Log}[c + d x] \left. \right)$$

Problem 206: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(a g + b g x) (c i + d i x)^3} dx$$

Optimal (type 3, 402 leaves, 15 steps):

$$\frac{B^2 d^2 n^2 (a + b x)^2}{4 (b c - a d)^3 g i^3 (c + d x)^2} + \frac{4 A b B d n (a + b x)}{(b c - a d)^3 g i^3 (c + d x)} - \frac{4 b B^2 d n^2 (a + b x)}{(b c - a d)^3 g i^3 (c + d x)} + \frac{4 b B^2 d n (a + b x) \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]}{(b c - a d)^3 g i^3 (c + d x)} -$$

$$\frac{B d^2 n (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)}{2 (b c - a d)^3 g i^3 (c + d x)^2} + \frac{d^2 (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{2 (b c - a d)^3 g i^3 (c + d x)^2} - \frac{2 b d (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(b c - a d)^3 g i^3 (c + d x)} + \frac{b^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^3}{3 B (b c - a d)^3 g i^3 n}$$

Result (type 3, 971 leaves):

$$\begin{aligned}
& \frac{1}{12 (bc - ad)^3 g i^3} \\
& \left(4 b^2 B^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^3 - \frac{1}{(c+dx)^2} 6 B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 \left(-2 A b^2 c^2 + 4 a b B c d n - a^2 B d^2 n - 4 A b^2 c d x + 4 b^2 B c d n x + 2 a b B d^2 n x - 2 A b^2 d^2 x^2 + \right. \right. \\
& \quad \left. \left. 3 b^2 B d^2 n x^2 - 2 b^2 B (c+dx)^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 b^2 B n (c+dx)^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) - \frac{1}{(c+dx)^2} 6 B (bc - ad) n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right. \\
& \quad \left. \left(-6 A b c + 2 a A d + 7 b B c n - a B d n - 4 A b d x + 6 b B d n x + 2 B (-3 b c + a d - 2 b d x) \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] + 2 B n (3 b c - a d + 2 b d x) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) + \right. \\
& \quad \left. \frac{1}{(c+dx)^2} 3 (bc - ad)^2 \left(2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + 2 B n (-2 A + B n) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] + \right. \right. \\
& \quad \left. \left. 2 B^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 - 2 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \left(-2 A + B n + 2 B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) + \frac{1}{c+dx} \right. \\
& \quad \left. 6 b (bc - ad) \left(2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + 2 B n (-2 A + 3 B n) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 - \right. \right. \\
& \quad \left. \left. 2 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \left(-2 A + 3 B n + 2 B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) + 6 b^2 \operatorname{Log} [a+bx] \left(2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + \right. \right. \\
& \quad \left. \left. 2 B n (-2 A + 3 B n) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 - 2 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \left(-2 A + 3 B n + 2 B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) - \right. \\
& \quad \left. 6 b^2 \left(2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right]^2 + 2 B n (-2 A + 3 B n) \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] + 2 B^2 n^2 \operatorname{Log} \left[\frac{a+bx}{c+dx} \right]^2 - \right. \right. \\
& \quad \left. \left. 2 B \operatorname{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \left(-2 A + 3 B n + 2 B n \operatorname{Log} \left[\frac{a+bx}{c+dx} \right] \right) \right) \operatorname{Log} [c+dx] \right)
\end{aligned}$$

Problem 207: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log} [e (\frac{a+bx}{c+dx})^n])^2}{(ag + bgx)^2 (ci + dix)^3} dx$$

Optimal (type 3, 562 leaves, 12 steps):

$$\begin{aligned}
& - \frac{B^2 d^3 n^2 (a + b x)^2}{4 (b c - a d)^4 g^2 i^3 (c + d x)^2} - \frac{6 A b B d^2 n (a + b x)}{(b c - a d)^4 g^2 i^3 (c + d x)} + \frac{6 b B^2 d^2 n^2 (a + b x)}{(b c - a d)^4 g^2 i^3 (c + d x)} - \frac{2 b^3 B^2 n^2 (c + d x)}{(b c - a d)^4 g^2 i^3 (a + b x)} - \\
& \frac{6 b B^2 d^2 n (a + b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c - a d)^4 g^2 i^3 (c + d x)} + \frac{B d^3 n (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c - a d)^4 g^2 i^3 (c + d x)^2} - \frac{2 b^3 B n (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c - a d)^4 g^2 i^3 (a + b x)} - \\
& \frac{d^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c - a d)^4 g^2 i^3 (c + d x)^2} + \frac{3 b d^2 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^4 g^2 i^3 (c + d x)} - \frac{b^3 (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^4 g^2 i^3 (a + b x)} - \frac{b^2 d \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{B (b c - a d)^4 g^2 i^3 n}
\end{aligned}$$

Result (type 3, 1334 leaves):

$$\begin{aligned}
& - \frac{1}{4 (b c - a d)^4 g^2 i^3 (a + b x) (c + d x)^2} \\
& \left(4 b^2 B^2 d n^2 (a + b x) (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 \left(6 a A b^2 c^2 d + 2 b^3 B c^3 n - 6 a^2 b B c d^2 n + a^3 B d^3 n + \right. \right. \\
& \quad 6 A b^3 c^2 d x + 12 a A b^2 c d^2 x + 6 b^3 B c^2 d n x - 12 a b^2 B c d^2 n x - 3 a^2 b B d^3 n x + 12 A b^3 c d^2 x^2 + 6 a A b^2 d^3 x^2 - 9 a b^2 B d^3 n x^2 + \\
& \quad \left. \left. 6 A b^3 d^3 x^3 - 3 b^3 B d^3 n x^3 + 6 b^2 B d (a + b x) (c + d x)^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^2 B d n (a + b x) (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
& \quad 4 b^2 (b c - a d) (c + d x)^2 \left(A^2 + 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
& \quad \left. B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(A + B n - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
& \quad 2 B (b c - a d) n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left(2 b d (a + b x) (c + d x) \left(4 A - 5 B n + 4 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
& \quad \left. d (b c - a d) (a + b x) \left(2 A - B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + 4 b^2 (c + d x)^2 \left(A + B n + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
& \quad d (b c - a d)^2 (a + b x) \left(2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
& \quad 6 b^2 d (a + b x) (c + d x)^2 \operatorname{Log}[a + b x] \left(2 A^2 - 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
& \quad 2 b d (b c - a d) (a + b x) (c + d x) \left(4 A^2 - 10 A B n + 11 B^2 n^2 + 4 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-4 A + 5 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
& \quad \left. 4 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-4 A + 5 B n + 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \\
& \quad 6 b^2 d (a + b x) (c + d x)^2 \left(2 A^2 - 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \operatorname{Log}[c + d x] \Big)
\end{aligned}$$

Problem 208: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(a g + b g x)^3 (c i + d i x)^3} dx$$

Optimal (type 3, 732 leaves, 14 steps):

$$\begin{aligned}
& \frac{B^2 d^4 n^2 (a + b x)^2}{4 (b c - a d)^5 g^3 i^3 (c + d x)^2} + \frac{8 A b B d^3 n (a + b x)}{(b c - a d)^5 g^3 i^3 (c + d x)} - \frac{8 b B^2 d^3 n^2 (a + b x)}{(b c - a d)^5 g^3 i^3 (c + d x)} + \frac{8 b^3 B^2 d n^2 (c + d x)}{(b c - a d)^5 g^3 i^3 (a + b x)} - \frac{b^4 B^2 n^2 (c + d x)^2}{4 (b c - a d)^5 g^3 i^3 (a + b x)^2} + \\
& \frac{8 b B^2 d^3 n (a + b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c - a d)^5 g^3 i^3 (c + d x)} - \frac{B d^4 n (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c - a d)^5 g^3 i^3 (c + d x)^2} + \frac{8 b^3 B d n (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c - a d)^5 g^3 i^3 (a + b x)} - \\
& \frac{b^4 B n (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c - a d)^5 g^3 i^3 (a + b x)^2} + \frac{d^4 (a + b x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c - a d)^5 g^3 i^3 (c + d x)^2} - \frac{4 b d^3 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^5 g^3 i^3 (c + d x)} + \\
& \frac{4 b^3 d (c + d x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^5 g^3 i^3 (a + b x)} - \frac{b^4 (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c - a d)^5 g^3 i^3 (a + b x)^2} + \frac{2 b^2 d^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{B (b c - a d)^5 g^3 i^3 n}
\end{aligned}$$

Result (type 3, 1653 leaves):

$$\begin{aligned}
& 4 (bc - ad)^5 g^3 i^3 (a + bx)^2 (c + dx)^2 \\
& \left(8 b^2 B^2 d^2 n^2 (a + bx)^2 (c + dx)^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^3 + 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 \left(12 a^2 A b^2 c^2 d^2 - b^4 B c^4 n + 8 a b^3 B c^3 d n - 8 a^3 b B c d^3 n + a^4 B d^4 n + \right. \right. \\
& \quad 24 a A b^3 c^2 d^2 x + 24 a^2 A b^2 c d^3 x + 4 b^4 B c^3 d n x + 24 a b^3 B c^2 d^2 n x - 24 a^2 b^2 B c d^3 n x - 4 a^3 b B d^4 n x + 12 A b^4 c^2 d^2 x^2 + \\
& \quad 48 a A b^3 c d^3 x^2 + 12 a^2 A b^2 d^4 x^2 + 18 b^4 B c^2 d^2 n x^2 - 18 a^2 b^2 B d^4 n x^2 + 24 A b^4 c d^3 x^3 + 24 a A b^3 d^4 x^3 + 12 b^4 B c d^3 n x^3 - \\
& \quad \left. 12 a b^3 B d^4 n x^3 + 12 A b^4 d^4 x^4 + 12 b^2 B d^2 (a + bx)^2 (c + dx)^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 12 b^2 B d^2 n (a + bx)^2 (c + dx)^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + \\
& 12 b^2 d^2 (a + bx)^2 (c + dx)^2 \operatorname{Log}[a + bx] \left(2 A^2 + 5 B^2 n^2 + 4 A B \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + 2 B^2 \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right)^2 \right) + \\
& 2 b^2 d (bc - ad) (a + bx) (c + dx)^2 \left(6 A^2 + 14 A B n + 15 B^2 n^2 + 6 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - \right. \\
& \quad \left. 2 B n (6 A + 7 B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + 6 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(6 A + 7 B n - 6 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) - \\
& b^2 (bc - ad)^2 (c + dx)^2 \left(2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 - 2 B n (2 A + B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(2 A + B n - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) + \\
& 2 B (bc - ad) n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \left(2 b d^2 (a + bx)^2 (c + dx) \left(6 A - 7 B n + 6 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 6 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + \right. \\
& \quad \left. 2 b^2 d (a + bx) (c + dx)^2 \left(6 A + 7 B n + 6 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 6 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + d^2 (bc - ad) (a + bx)^2 \right. \\
& \quad \left. \left(2 A - B n + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) - b^2 (bc - ad) (c + dx)^2 \left(2 A + B n + 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) + \\
& d^2 (bc - ad)^2 (a + bx)^2 \left(2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 + 2 B n (-2 A + B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 - 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(-2 A + B n + 2 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) + \\
& 2 b d^2 (bc - ad) (a + bx)^2 (c + dx) \left(6 A^2 - 14 A B n + 15 B^2 n^2 + 6 B^2 \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right]^2 + 2 B n (-6 A + 7 B n) \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] + \right. \\
& \quad \left. 6 B^2 n^2 \operatorname{Log} \left[\frac{a + bx}{c + dx} \right]^2 - 2 B \operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] \left(-6 A + 7 B n + 6 B n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) \right) - \\
& 12 b^2 d^2 (a + bx)^2 (c + dx)^2 \left(2 A^2 + 5 B^2 n^2 + 4 A B \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right) + 2 B^2 \left(\operatorname{Log} \left[e \left(\frac{a + bx}{c + dx} \right)^n \right] - n \operatorname{Log} \left[\frac{a + bx}{c + dx} \right] \right)^2 \right) \operatorname{Log}[c + dx]
\end{aligned}$$

Problem 209: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{(ag + bgx)^4 (ci + dix)^3} dx$$

Optimal (type 3, 908 leaves, 16 steps):

$$\begin{aligned} & - \frac{B^2 d^5 n^2 (a + bx)^2}{4 (bc - ad)^6 g^4 i^3 (c + dx)^2} - \frac{10 A B d^4 n (a + bx)}{(bc - ad)^6 g^4 i^3 (c + dx)} + \frac{10 b B^2 d^4 n^2 (a + bx)}{(bc - ad)^6 g^4 i^3 (c + dx)} - \frac{20 b^3 B^2 d^2 n^2 (c + dx)}{(bc - ad)^6 g^4 i^3 (a + bx)} + \\ & \frac{5 b^4 B^2 d n^2 (c + dx)^2}{4 (bc - ad)^6 g^4 i^3 (a + bx)^2} - \frac{2 b^5 B^2 n^2 (c + dx)^3}{27 (bc - ad)^6 g^4 i^3 (a + bx)^3} - \frac{10 b B^2 d^4 n (a + bx) \operatorname{Log}[e(\frac{a+bx}{c+dx})^n]}{(bc - ad)^6 g^4 i^3 (c + dx)} + \frac{B d^5 n (a + bx)^2 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])}{2 (bc - ad)^6 g^4 i^3 (c + dx)^2} - \\ & \frac{20 b^3 B d^2 n (c + dx) (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])}{(bc - ad)^6 g^4 i^3 (a + bx)} + \frac{5 b^4 B d n (c + dx)^2 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])}{2 (bc - ad)^6 g^4 i^3 (a + bx)^2} - \frac{2 b^5 B n (c + dx)^3 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])}{9 (bc - ad)^6 g^4 i^3 (a + bx)^3} - \\ & \frac{d^5 (a + bx)^2 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{2 (bc - ad)^6 g^4 i^3 (c + dx)^2} + \frac{5 b d^4 (a + bx) (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{(bc - ad)^6 g^4 i^3 (c + dx)} - \frac{10 b^3 d^2 (c + dx) (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{(bc - ad)^6 g^4 i^3 (a + bx)} + \\ & \frac{5 b^4 d (c + dx)^2 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{2 (bc - ad)^6 g^4 i^3 (a + bx)^2} - \frac{b^5 (c + dx)^3 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^2}{3 (bc - ad)^6 g^4 i^3 (a + bx)^3} - \frac{10 b^2 d^3 (A + B \operatorname{Log}[e(\frac{a+bx}{c+dx})^n])^3}{3 B (bc - ad)^6 g^4 i^3 n} \end{aligned}$$

Result (type 3, 2138 leaves):

$$\begin{aligned} & - \frac{1}{108 (bc - ad)^6 g^4 i^3 (a + bx)^3 (c + dx)^2} \left(360 b^2 B^2 d^3 n^2 (a + bx)^3 (c + dx)^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^3 + \right. \\ & 18 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 \left(60 a^3 A b^2 c^2 d^3 + 2 b^5 B c^5 n - 15 a b^4 B c^4 d n + 60 a^2 b^3 B c^3 d^2 n - 30 a^4 b B c d^4 n + 3 a^5 B d^5 n + 180 a^2 A b^3 c^2 d^3 x + \right. \\ & 120 a^3 A b^2 c d^4 x - 5 b^5 B c^4 d n x + 60 a b^4 B c^3 d^2 n x + 180 a^2 b^3 B c^2 d^3 n x - 120 a^3 b^2 B c d^4 n x - 15 a^4 b B d^5 n x + 180 a A b^4 c^2 d^3 x^2 + \\ & 360 a^2 A b^3 c d^4 x^2 + 60 a^3 A b^2 d^5 x^2 + 20 b^5 B c^3 d^2 n x^2 + 270 a b^4 B c^2 d^3 n x^2 - 90 a^3 b^2 B d^5 n x^2 + 60 A b^5 c^2 d^3 x^3 + 360 a A b^4 c d^4 x^3 + \\ & 180 a^2 A b^3 d^5 x^3 + 110 b^5 B c^2 d^3 n x^3 + 180 a b^4 B c d^4 n x^3 - 90 a^2 b^3 B d^5 n x^3 + 120 A b^5 c d^4 x^4 + 180 a A b^4 d^5 x^4 + 100 b^5 B c d^4 n x^4 + \\ & \left. 60 A b^5 d^5 x^5 + 20 b^5 B d^5 n x^5 + 60 b^2 B d^3 (a + bx)^3 (c + dx)^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] - 60 b^2 B d^3 n (a + bx)^3 (c + dx)^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) + \\ & 6 b^2 d^2 (bc - ad) (a + bx)^2 (c + dx)^2 \left(108 A^2 + 282 A B n + 319 B^2 n^2 + 108 B^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 - 6 B n (36 A + 47 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \\ & \left. 108 B^2 n^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 + 6 B \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \left(36 A + 47 B n - 36 B n \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] \right) \right) - \\ & 3 b^2 d (bc - ad)^2 (a + bx) (c + dx)^2 \left(54 A^2 + 66 A B n + 37 B^2 n^2 + 54 B^2 \operatorname{Log}\left[\frac{a + bx}{c + dx}\right]^2 - 6 B n (18 A + 11 B n) \operatorname{Log}\left[\frac{a + bx}{c + dx}\right] + \right. \end{aligned}$$

$$\begin{aligned}
& 54 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(18 A + 11 B n - 18 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + \\
& 4 b^2 (bc-ad)^3 (c+dx)^2 \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \right. \\
& \quad \left. 9 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \\
& 60 b^2 d^3 (a+bx)^3 (c+dx)^2 \operatorname{Log}[a+bx] \left(18 A^2 + 12 A B n + 49 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 12 B n (3 A + B n) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \right. \\
& \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 12 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \\
& 27 d^3 (bc-ad)^2 (a+bx)^3 \left(2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \right. \\
& \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(-2 A + B n + 2 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \\
& 54 b d^3 (bc-ad) (a+bx)^3 (c+dx) \left(8 A^2 - 18 A B n + 19 B^2 n^2 + 8 B^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 + 2 B n (-8 A + 9 B n) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \right. \\
& \quad \left. 8 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(-8 A + 9 B n + 8 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \\
& 6 B (bc-ad) n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \left(18 b d^3 (a+bx)^3 (c+dx) \left(8 A - 9 B n + 8 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 8 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + 4 b^2 (bc-ad)^2 (c+dx)^2 \right. \\
& \quad \left. \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) + 9 d^3 (bc-ad) (a+bx)^3 \left(2 A - B n + 2 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) - \right. \\
& \quad \left. 3 b^2 d (bc-ad) (a+bx) (c+dx)^2 \left(18 A + 11 B n + 18 B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) + \right. \\
& \quad \left. 6 b^2 d^2 (a+bx)^2 (c+dx)^2 \left(36 A + 47 B n + 36 B \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right)\right) - \\
& 60 b^2 d^3 (a+bx)^3 (c+dx)^2 \left(18 A^2 + 12 A B n + 49 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 - 12 B n (3 A + B n) \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + \right. \\
& \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 + 12 B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) \operatorname{Log}[c+dx]
\end{aligned}$$

Problem 210: Unable to integrate problem.

$$\int (ag + bgx)^m (ci + dix)^{-2-m} \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^p dx$$

Optimal (type 4, 189 leaves, 3 steps):

$$\left(e^{-\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^m \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \text{Gamma} \left[1+p, -\frac{(1+m)(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n])}{Bn} \right] \right. \\ \left. \left(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n] \right)^p \left(-\frac{(1+m)(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n])}{Bn} \right)^{-p} \right) / ((bc-ad) i^2 (1+m) (c+dx))$$

Result (type 8, 51 leaves):

$$\int (ag+bgx)^m (ci+dix)^{-2-m} \left(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n] \right)^p dx$$

Problem 211: Unable to integrate problem.

$$\int (ag+bgx)^{-2-m} (ci+dix)^m \left(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n] \right)^p dx$$

Optimal (type 4, 190 leaves, 3 steps):

$$- \left(\left(e^{\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^{-2-m} \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \text{Gamma} \left[1+p, \frac{(1+m)(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n])}{Bn} \right] \right. \right. \\ \left. \left. \left(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n] \right)^p \left(\frac{(1+m)(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n])}{Bn} \right)^{-p} \right) \right) / ((bc-ad) i^2 (1+m) (c+dx))$$

Result (type 8, 51 leaves):

$$\int (ag+bgx)^{-2-m} (ci+dix)^m \left(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n] \right)^p dx$$

Problem 215: Unable to integrate problem.

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n]} dx$$

Optimal (type 4, 125 leaves, 3 steps):

$$\frac{e^{-\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^m \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \text{ExpIntegralEi} \left[\frac{(1+m)(A+B \text{Log} [e \left(\frac{a+bx}{c+dx} \right)^n])}{Bn} \right]}{B(bc-ad) i^2 n (c+dx)}$$

Result (type 8, 51 leaves):

$$\int \frac{(a g + b g x)^m (c i + d i x)^{-2-m}}{A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]} dx$$

Problem 216: Unable to integrate problem.

$$\int \frac{(a g + b g x)^m (c i + d i x)^{-2-m}}{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2} dx$$

Optimal (type 4, 206 leaves, 4 steps):

$$\left(e^{-\frac{A(1+m)}{Bn}} (1+m) (a+bx) (g(a+bx))^m \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \operatorname{ExpIntegralEi}\left[\frac{(1+m) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) /$$

$$(B^2 (bc - ad) i^2 n^2 (c+dx)) - \frac{(a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{B (bc - ad) i^2 n (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(a g + b g x)^m (c i + d i x)^{-2-m}}{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2} dx$$

Problem 217: Unable to integrate problem.

$$\int \frac{(a g + b g x)^m (c i + d i x)^{-2-m}}{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3} dx$$

Optimal (type 4, 295 leaves, 5 steps):

$$\left(e^{-\frac{A(1+m)}{Bn}} (1+m)^2 (a+bx) (g(a+bx))^m \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \operatorname{ExpIntegralEi}\left[\frac{(1+m) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) /$$

$$(2B^3 (bc - ad) i^2 n^3 (c+dx)) - \frac{(a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{2B (bc - ad) i^2 n (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2} - \frac{(1+m) (a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{2B^2 (bc - ad) i^2 n^2 (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(a g + b g x)^m (c i + d i x)^{-2-m}}{\left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3} dx$$

Problem 221: Unable to integrate problem.

$$\int \frac{(a g + b g x)^{-2-m} (c i + d i x)^m}{A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]} dx$$

Optimal (type 4, 128 leaves, 3 steps):

$$\frac{e^{\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^{-2-m} \left(e\left(\frac{a+bx}{c+dx}\right)^n\right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \operatorname{ExpIntegralEi}\left[-\frac{(1+m)(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{Bn}\right]}{B(bc-ad) i^2 n (c+dx)}$$

Result (type 8, 51 leaves):

$$\int \frac{(a g + b g x)^{-2-m} (c i + d i x)^m}{A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]} dx$$

Problem 222: Unable to integrate problem.

$$\int \frac{(a g + b g x)^{-2-m} (c i + d i x)^m}{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2} dx$$

Optimal (type 4, 214 leaves, 4 steps):

$$-\left(\left(e^{\frac{A(1+m)}{Bn}} (1+m) (a+bx) (g(a+bx))^{-2-m} \left(e\left(\frac{a+bx}{c+dx}\right)^n\right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \operatorname{ExpIntegralEi}\left[-\frac{(1+m)(A+B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{Bn}\right]\right)\right) /$$

$$\left(B^2 (bc-ad) i^2 n^2 (c+dx)\right) - \frac{(a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{B(bc-ad) i^2 n (c+dx) \left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(a g + b g x)^{-2-m} (c i + d i x)^m}{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2} dx$$

Problem 223: Unable to integrate problem.

$$\int \frac{(a g + b g x)^{-2-m} (c i + d i x)^m}{\left(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3} dx$$

Optimal (type 4, 306 leaves, 5 steps):

$$\left(e^{\frac{A(1+m)}{Bn}} (1+m)^2 (a+bx) (g(a+bx))^{-2-m} \left(e \left(\frac{a+bx}{c+dx} \right)^n \right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \text{ExpIntegralEi} \left[-\frac{(1+m) \left(A+B \text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) /$$

$$(2B^3 (bc-ad) i^2 n^3 (c+dx)) - \frac{(a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{2B (bc-ad) i^2 n (c+dx) \left(A+B \text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^2} + \frac{(1+m) (a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{2B^2 (bc-ad) i^2 n^2 (c+dx) \left(A+B \text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{\left(A+B \text{Log} \left[e \left(\frac{a+bx}{c+dx} \right)^n \right] \right)^3} dx$$

Problem 226: Unable to integrate problem.

$$\int (ag+bgx)^m (ci+dix)^{-2-m} \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)^p dx$$

Optimal (type 4, 193 leaves, 4 steps):

$$\left(e^{-\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^m (i(c+dx))^{-m} \left(e (a+bx)^n (c+dx)^{-n} \right)^{-\frac{1+m}{n}} \text{Gamma} \left[1+p, -\frac{(1+m) \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)}{Bn} \right] \right)$$

$$\left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)^p \left(-\frac{(1+m) \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)}{Bn} \right)^{-p} / \left((bc-ad) i^2 (1+m) (c+dx) \right)$$

Result (type 8, 52 leaves):

$$\int (ag+bgx)^m (ci+dix)^{-2-m} \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)^p dx$$

Problem 227: Unable to integrate problem.

$$\int (ag+bgx)^{-2-m} (ci+dix)^m \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)^p dx$$

Optimal (type 4, 194 leaves, 4 steps):

$$- \left(\left(e^{\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m} \left(e (a+bx)^n (c+dx)^{-n} \right)^{\frac{1+m}{n}} \text{Gamma} \left[1+p, \frac{(1+m) \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)}{Bn} \right] \right) \right)$$

$$\left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)^p \left(\frac{(1+m) \left(A+B \text{Log} \left[e (a+bx)^n (c+dx)^{-n} \right] \right)}{Bn} \right)^{-p} / \left((bc-ad) i^2 (1+m) (c+dx) \right)$$

Result (type 8, 52 leaves):

$$\int (a g + b g x)^{-2-m} (c i + d i x)^m (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^p dx$$

Problem 228: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(a + b x) (c + d x)} dx$$

Optimal (type 3, 45 leaves, 4 steps):

$$\frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^4}{4 B (b c - a d) n}$$

Result (type 3, 118 leaves):

$$\frac{1}{4 b c n - 4 a d n} (4 A^3 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 6 A^2 B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^2 + 4 A B^2 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^3 + B^3 \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]^4)$$

Problem 240: Unable to integrate problem.

$$\int \frac{(a + b x)^m (c + d x)^{-2-m}}{\operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]} dx$$

Optimal (type 4, 88 leaves, 4 steps):

$$\frac{(a + b x)^{1+m} (c + d x)^{-1-m} (e (a + b x)^n (c + d x)^{-n})^{-\frac{1+m}{n}} \operatorname{ExpIntegralEi}\left[\frac{(1+m) \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]}{n}\right]}{(b c - a d) n}$$

Result (type 8, 42 leaves):

$$\int \frac{(a + b x)^m (c + d x)^{-2-m}}{\operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]} dx$$

Problem 249: Unable to integrate problem.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^4}{(f + g x) (a h + b h x)} dx$$

Optimal (type 4, 361 leaves, 8 steps):

$$\begin{aligned}
& - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^4 \operatorname{Log}\left[1 - \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \\
& \frac{4 B n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3 \operatorname{PolyLog}\left[2, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{12 B^2 n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{PolyLog}\left[3, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \\
& \frac{24 B^3 n^3 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[4, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{24 B^4 n^4 \operatorname{PolyLog}\left[5, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h}
\end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^4}{(f + g x)(a h + b h x)} dx$$

Problem 250: Unable to integrate problem.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(f + g x)(a h + b h x)} dx$$

Optimal (type 4, 282 leaves, 7 steps):

$$\begin{aligned}
& - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3 \operatorname{Log}\left[1 - \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{3 B n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{PolyLog}\left[2, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \\
& \frac{6 B^2 n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[3, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{6 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h}
\end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(f + g x)(a h + b h x)} dx$$

Problem 251: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{(f + g x)(a h + b h x)} dx$$

Optimal (type 4, 203 leaves, 6 steps):

$$\begin{aligned}
& - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{Log}\left[1 - \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \\
& \frac{2 B n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h}
\end{aligned}$$

Result (type 4, 1415 leaves):

$$\begin{aligned}
& \frac{1}{3 (b f - a g) h} \left(3 \operatorname{Log}[a + b x] \left(A + B \left(-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n} \right] \right) \right)^2 - \right. \\
& 3 \left(A + B \left(-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n} \right] \right) \right)^2 \operatorname{Log}[f + g x] + \\
& 3 B n \left(A + B \left(-n \operatorname{Log}[a + b x] + n \operatorname{Log}[c + d x] + \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n} \right] \right) \right) \\
& \left(\operatorname{Log}[a + b x]^2 - 2 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] + \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g} \right] \right) \right) - \\
& 6 A B n \left(\operatorname{Log}[c + d x] \left(\operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] - \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g} \right] \right) + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d} \right] - \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g} \right] \right) + \\
& 6 B^2 n \left(n \operatorname{Log}[a + b x] - n \operatorname{Log}[c + d x] - \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n} \right] \right) \\
& \left(\operatorname{Log}[c + d x] \left(\operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] - \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g} \right] \right) + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d} \right] - \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g} \right] \right) + \\
& B^2 n^2 \left(\operatorname{Log}[a + b x]^2 \left(\operatorname{Log}[a + b x] - 3 \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] \right) - 6 \operatorname{Log}[a + b x] \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g} \right] + 6 \operatorname{PolyLog}\left[3, \frac{g (a + b x)}{-b f + a g} \right] \right) + \\
& 3 B^2 n^2 \left(\operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d} \right] \operatorname{Log}[c + d x]^2 - \operatorname{Log}[c + d x]^2 \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g} \right] + 2 \operatorname{Log}[c + d x] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d} \right] - \right. \\
& \left. 2 \operatorname{Log}[c + d x] \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g} \right] - 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d} \right] + 2 \operatorname{PolyLog}\left[3, \frac{g (c + d x)}{-d f + c g} \right] \right) - \\
& 6 B^2 n^2 \left(\frac{1}{2} \operatorname{Log}[a + b x]^2 \left(\operatorname{Log}[c + d x] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d} \right] \right) - \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] - \right. \\
& \left. \frac{1}{2} \operatorname{Log}\left[\frac{g (c + d x)}{-d f + c g} \right] \left(-2 \operatorname{Log}[a + b x] + \operatorname{Log}\left[\frac{g (c + d x)}{-d f + c g} \right] \right) \left(\operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g} \right] \right) + \right. \\
& \left. \operatorname{Log}\left[\frac{g (c + d x)}{-d f + c g} \right] \operatorname{Log}\left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \left(\operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g} \right] \right) - \right. \\
& \left. \frac{1}{2} \operatorname{Log}\left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right]^2 \left(\operatorname{Log}\left[\frac{-b c + a d}{d (a + b x)} \right] + \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g} \right] - \operatorname{Log}\left[\frac{(-b c + a d) (f + g x)}{(d f - c g) (a + b x)} \right] \right) - \operatorname{Log}[a + b x] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d} \right] - \right. \\
& \left(\operatorname{Log}[c + d x] - \operatorname{Log}\left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g} \right] - \left(\operatorname{Log}[a + b x] + \operatorname{Log}\left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g} \right] - \\
& \operatorname{Log}\left[\frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \left(\operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)} \right] - \operatorname{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) + \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d} \right] + \\
& \left. \operatorname{PolyLog}\left[3, \frac{g (a + b x)}{-b f + a g} \right] + \operatorname{PolyLog}\left[3, \frac{g (c + d x)}{-d f + c g} \right] + \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)} \right] - \operatorname{PolyLog}\left[3, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)} \right] \right) \left. \right)
\end{aligned}$$

Problem 252: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]}{(f + g x) (a h + b h x)} dx$$

Optimal (type 4, 123 leaves, 5 steps):

$$-\frac{(A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{Log}\left[1 - \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \frac{B n \operatorname{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h}$$

Result (type 4, 304 leaves):

$$\begin{aligned} & -\frac{1}{2 (b f - a g) h} \left(-2 A \operatorname{Log}[a + b x] + B n \operatorname{Log}[a + b x]^2 - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + \right. \\ & 2 B n \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] - 2 B \operatorname{Log}[a + b x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + 2 A \operatorname{Log}[f + g x] - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[f + g x] + \\ & 2 B n \operatorname{Log}[c + d x] \operatorname{Log}[f + g x] + 2 B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] \operatorname{Log}[f + g x] + 2 B n \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \\ & \left. 2 B n \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g}\right] + 2 B n \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g}\right] + 2 B n \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 B n \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g}\right] \right) \end{aligned}$$

Problem 255: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{c + d x}{a + b x}\right]}{(a + b x) ((a - c) h + (b - d) h x)} dx$$

Optimal (type 4, 33 leaves, 2 steps):

$$-\frac{\operatorname{PolyLog}\left[2, 1 - \frac{c + d x}{a + b x}\right]}{(b c - a d) h}$$

Result (type 4, 324 leaves):

$$\frac{1}{(2bc - 2ad)h} \left(\text{Log}\left[\frac{a}{b} + x\right]^2 - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + bx] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + bx] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a - c + bx - dx] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a - c + bx - dx] - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(a-c+bx-dx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a-c+bx-dx)}{-bc+ad}\right] - 2 \text{Log}[a + bx] \text{Log}\left[\frac{c+dx}{a+bx}\right] + 2 \text{Log}[a - c + bx - dx] \text{Log}\left[\frac{c+dx}{a+bx}\right] - 2 \text{PolyLog}\left[2, \frac{(b-d)(a+bx)}{bc-ad}\right] - 2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[2, \frac{(b-d)(c+dx)}{bc-ad}\right] \right)$$

Problem 256: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{a-cg+(b-dg)x}{a+bx}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 27 leaves, 2 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c+dx)}{a+bx}\right]}{bc-ad}$$

Result (type 4, 375 leaves):

$$\frac{1}{2bc - 2ad} \left(-\text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + bx] - 2 \text{Log}\left[\frac{a-cg}{b-dg} + x\right] \text{Log}[a + bx] + 2 \text{Log}\left[\frac{a-cg}{b-dg} + x\right] \text{Log}\left[\frac{(b-dg)(a+bx)}{(bc-ad)g}\right] - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + dx] + 2 \text{Log}\left[\frac{a-cg}{b-dg} + x\right] \text{Log}[c + dx] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 \text{Log}\left[\frac{a-cg}{b-dg} + x\right] \text{Log}\left[\frac{(b-dg)(c+dx)}{bc-ad}\right] + 2 \text{Log}[a + bx] \text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] - 2 \text{Log}[c + dx] \text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] + 2 \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2 \text{PolyLog}\left[2, -\frac{b(a-cg+bx-dgx)}{(bc-ad)g}\right] - 2 \text{PolyLog}\left[2, -\frac{d(-a+cg-bx+dgx)}{-bc+ad}\right] \right)$$

Problem 257: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[1 - \frac{g(c+dx)}{a+bx}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 27 leaves, 3 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c+dx)}{a+bx}\right]}{bc-ad}$$

Result (type 4, 375 leaves):

$$\begin{aligned} & \frac{1}{2bc-2ad} \left(-\text{Log}\left[\frac{a}{b}+x\right]^2 + 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}[a+bx] - 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}[a+bx] + \right. \\ & 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}\left[\frac{(b-dg)(a+bx)}{(bc-ad)g}\right] - 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}[c+dx] + 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}[c+dx] + 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\ & 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}\left[\frac{(b-dg)(c+dx)}{bc-ad}\right] + 2\text{Log}[a+bx]\text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] - 2\text{Log}[c+dx]\text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] + \\ & \left. 2\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2\text{PolyLog}\left[2, -\frac{b(a-cg+bx-dgx)}{(bc-ad)g}\right] - 2\text{PolyLog}\left[2, -\frac{d(-a+cg-bx+dgx)}{-bc+ad}\right] \right) \end{aligned}$$

Problem 258: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 27 leaves, 3 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c+dx)}{a+bx}\right]}{bc-ad}$$

Result (type 4, 375 leaves):

$$\begin{aligned} & \frac{1}{2bc-2ad} \left(-\text{Log}\left[\frac{a}{b}+x\right]^2 + 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}[a+bx] - 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}[a+bx] + \right. \\ & 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}\left[\frac{(b-dg)(a+bx)}{(bc-ad)g}\right] - 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}[c+dx] + 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}[c+dx] + 2\text{Log}\left[\frac{a}{b}+x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\ & 2\text{Log}\left[\frac{a-cg}{b-dg}+x\right]\text{Log}\left[\frac{(b-dg)(c+dx)}{bc-ad}\right] + 2\text{Log}[a+bx]\text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] - 2\text{Log}[c+dx]\text{Log}\left[\frac{a-cg+bx-dgx}{a+bx}\right] + \\ & \left. 2\text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 2\text{PolyLog}\left[2, -\frac{b(a-cg+bx-dgx)}{(bc-ad)g}\right] - 2\text{PolyLog}\left[2, -\frac{d(-a+cg-bx+dgx)}{-bc+ad}\right] \right) \end{aligned}$$

Problem 259: Unable to integrate problem.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{a f h + b g h x^2 + h (b f x + a g x)} dx$$

Optimal (type 4, 282 leaves, 8 steps):

$$\begin{aligned} & - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3 \operatorname{Log}\left[1 - \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{3 B n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{PolyLog}\left[2, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} \\ & + \frac{6 B^2 n^2 (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[3, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{6 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} \end{aligned}$$

Result (type 8, 53 leaves):

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{a f h + b g h x^2 + h (b f x + a g x)} dx$$

Problem 260: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2}{a f h + b g h x^2 + h (b f x + a g x)} dx$$

Optimal (type 4, 203 leaves, 7 steps):

$$\begin{aligned} & - \frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \operatorname{Log}\left[1 - \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \\ & + \frac{2 B n (A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} \end{aligned}$$

Result (type 4, 1415 leaves):

$$\begin{aligned}
& \frac{1}{3(bf-ag)h} \left(3 \operatorname{Log}[a+bx] \left(A+B(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]) \right)^2 - \right. \\
& 3(A+B(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}]))^2 \operatorname{Log}[f+gx] + \\
& 3Bn(A+B(-n \operatorname{Log}[a+bx] + n \operatorname{Log}[c+dx] + \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}])) \\
& \left. \left(\operatorname{Log}[a+bx]^2 - 2 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \operatorname{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] \right) \right) \right) - \\
& 6ABn \left(\operatorname{Log}[c+dx] \left(\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] \right) + \\
& 6B^2n \left(n \operatorname{Log}[a+bx] - n \operatorname{Log}[c+dx] - \operatorname{Log}[e(a+bx)^n(c+dx)^{-n}] \right) \\
& \left(\operatorname{Log}[c+dx] \left(\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) + \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] \right) + \\
& B^2n^2 \left(\operatorname{Log}[a+bx]^2 \left(\operatorname{Log}[a+bx] - 3 \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] \right) - 6 \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] + 6 \operatorname{PolyLog}\left[3, \frac{g(a+bx)}{-bf+ag}\right] \right) + \\
& 3B^2n^2 \left(\operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \operatorname{Log}[c+dx]^2 - \operatorname{Log}[c+dx]^2 \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] + 2 \operatorname{Log}[c+dx] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \right. \\
& \left. 2 \operatorname{Log}[c+dx] \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{g(c+dx)}{-df+cg}\right] \right) - \\
& 6B^2n^2 \left(\frac{1}{2} \operatorname{Log}[a+bx]^2 \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \right. \\
& \left. \frac{1}{2} \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \left(-2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \right) \left(\operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) + \right. \\
& \left. \operatorname{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \left(\operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \operatorname{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) - \right. \\
& \left. \frac{1}{2} \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 \left(\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \operatorname{Log}\left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)}\right] \right) - \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \right. \\
& \left. \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] - \left(\operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - \right. \\
& \left. \operatorname{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \left(\operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \operatorname{PolyLog}\left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) + \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& \left. \operatorname{PolyLog}\left[3, \frac{g(a+bx)}{-bf+ag}\right] + \operatorname{PolyLog}\left[3, \frac{g(c+dx)}{-df+cg}\right] + \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] - \operatorname{PolyLog}\left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \right)
\end{aligned}$$

Problem 261: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]}{a f h + b g h x^2 + h (b f x + a g x)} dx$$

Optimal (type 4, 123 leaves, 6 steps):

$$-\frac{(A + B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}]) \operatorname{Log}\left[1 - \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h} + \frac{B n \operatorname{PolyLog}\left[2, \frac{(b f - a g)(c + d x)}{(d f - c g)(a + b x)}\right]}{(b f - a g) h}$$

Result (type 4, 303 leaves):

$$\begin{aligned} & -\frac{1}{(2 b f - 2 a g) h} \left(-2 A \operatorname{Log}[a + b x] + B n \operatorname{Log}[a + b x]^2 - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + \right. \\ & 2 B n \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] - 2 B \operatorname{Log}[a + b x] \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] + 2 A \operatorname{Log}[f + g x] - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[f + g x] + \\ & 2 B n \operatorname{Log}[c + d x] \operatorname{Log}[f + g x] + 2 B \operatorname{Log}[e (a + b x)^n (c + d x)^{-n}] \operatorname{Log}[f + g x] + 2 B n \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \\ & \left. 2 B n \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g}\right] + 2 B n \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g}\right] + 2 B n \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 B n \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g}\right] \right) \end{aligned}$$

Test results for the 108 problems in "3.2.3 u log(e (f (a+b x)^p (c+d x)^q)^r)^s.m"

Problem 16: Result more than twice size of optimal antiderivative.

$$\int (a + b x)^4 \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2 dx$$

Optimal (type 4, 920 leaves, 32 steps):

$$\begin{aligned}
& - \frac{a (b c - a d)^3 p q r^2 x}{5 d^3} + \frac{2 (b c - a d)^4 p q r^2 x}{25 d^4} + \frac{77 (b c - a d)^4 q^2 r^2 x}{150 d^4} + \frac{2 (b c - a d)^4 q (p + q) r^2 x}{5 d^4} - \\
& \frac{b (b c - a d)^3 p q r^2 x^2}{10 d^3} - \frac{(b c - a d)^3 p q r^2 (a + b x)^2}{25 b d^3} - \frac{77 (b c - a d)^3 q^2 r^2 (a + b x)^2}{300 b d^3} + \frac{16 (b c - a d)^2 p q r^2 (a + b x)^3}{225 b d^2} + \\
& \frac{47 (b c - a d)^2 q^2 r^2 (a + b x)^3}{450 b d^2} - \frac{9 (b c - a d) p q r^2 (a + b x)^4}{200 b d} - \frac{9 (b c - a d) q^2 r^2 (a + b x)^4}{200 b d} + \frac{2 p^2 r^2 (a + b x)^5}{125 b} + \\
& \frac{4 p q r^2 (a + b x)^5}{125 b} + \frac{2 q^2 r^2 (a + b x)^5}{125 b} - \frac{2 (b c - a d)^5 p q r^2 \text{Log}[c + d x]}{25 b d^5} - \frac{137 (b c - a d)^5 q^2 r^2 \text{Log}[c + d x]}{150 b d^5} - \\
& \frac{2 (b c - a d)^5 p q r^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c + d x]}{5 b d^5} - \frac{(b c - a d)^5 q^2 r^2 \text{Log}[c + d x]^2}{5 b d^5} - \frac{2 (b c - a d)^4 q r (a + b x) \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^4} + \\
& \frac{(b c - a d)^3 q r (a + b x)^2 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^3} - \frac{2 (b c - a d)^2 q r (a + b x)^3 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{15 b d^2} + \\
& \frac{(b c - a d) q r (a + b x)^4 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{10 b d} - \frac{2 p r (a + b x)^5 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{25 b} - \\
& \frac{2 q r (a + b x)^5 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{25 b} + \frac{2 (b c - a d)^5 q r \text{Log}[c + d x] \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^5} + \\
& \frac{(a + b x)^5 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]^2}{5 b} - \frac{2 (b c - a d)^5 p q r^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{5 b d^5}
\end{aligned}$$

Result (type 4, 2508 leaves):

$$\begin{aligned}
& \frac{2 a^5 p q r^2}{b} + \frac{2 a b^3 c^4 p q r^2}{5 d^4} - \frac{2 a^2 b^2 c^3 p q r^2}{d^3} + \frac{4 a^3 b c^2 p q r^2}{d^2} - \frac{4 a^4 c p q r^2}{d} + \frac{2}{25} a^4 p^2 r^2 x + \frac{197}{150} a^4 p q r^2 x + \frac{12 b^4 c^4 p q r^2 x}{25 d^4} - \\
& \frac{11 a b^3 c^3 p q r^2 x}{5 d^3} + \frac{59 a^2 b^2 c^2 p q r^2 x}{15 d^2} - \frac{101 a^3 b c p q r^2 x}{30 d} + 2 a^4 q^2 r^2 x + \frac{137 b^4 c^4 q^2 r^2 x}{150 d^4} - \frac{25 a b^3 c^3 q^2 r^2 x}{6 d^3} + \frac{22 a^2 b^2 c^2 q^2 r^2 x}{3 d^2} - \\
& \frac{6 a^3 b c q^2 r^2 x}{d} + \frac{4}{25} a^3 b p^2 r^2 x^2 + \frac{283}{300} a^3 b p q r^2 x^2 - \frac{7 b^4 c^3 p q r^2 x^2}{50 d^3} + \frac{19 a b^3 c^2 p q r^2 x^2}{30 d^2} - \frac{67 a^2 b^2 c p q r^2 x^2}{60 d} + a^3 b q^2 r^2 x^2 - \\
& \frac{77 b^4 c^3 q^2 r^2 x^2}{300 d^3} + \frac{13 a b^3 c^2 q^2 r^2 x^2}{12 d^2} - \frac{5 a^2 b^2 c q^2 r^2 x^2}{3 d} + \frac{4}{25} a^2 b^2 p^2 r^2 x^3 + \frac{257}{450} a^2 b^2 p q r^2 x^3 + \frac{16 b^4 c^2 p q r^2 x^3}{225 d^2} - \frac{29 a b^3 c p q r^2 x^3}{90 d} + \\
& \frac{4}{9} a^2 b^2 q^2 r^2 x^3 + \frac{47 b^4 c^2 q^2 r^2 x^3}{450 d^2} - \frac{7 a b^3 c q^2 r^2 x^3}{18 d} + \frac{2}{25} a b^3 p^2 r^2 x^4 + \frac{41}{200} a b^3 p q r^2 x^4 - \frac{9 b^4 c p q r^2 x^4}{200 d} + \frac{1}{8} a b^3 q^2 r^2 x^4 - \frac{9 b^4 c q^2 r^2 x^4}{200 d} + \\
& \frac{2}{125} b^4 p^2 r^2 x^5 + \frac{4}{125} b^4 p q r^2 x^5 + \frac{2}{125} b^4 q^2 r^2 x^5 - \frac{a^5 p^2 r^2 \text{Log}[a + b x]^2}{5 b} + \frac{2 a^5 p q r^2 \text{Log}[c + d x]}{b} - \frac{2 b^4 c^5 p q r^2 \text{Log}[c + d x]}{25 d^5} + \\
& \frac{2 a b^3 c^4 p q r^2 \text{Log}[c + d x]}{5 d^4} - \frac{4 a^2 b^2 c^3 p q r^2 \text{Log}[c + d x]}{5 d^3} + \frac{4 a^3 b c^2 p q r^2 \text{Log}[c + d x]}{5 d^2} - \frac{2 a^4 c p q r^2 \text{Log}[c + d x]}{5 d} - \\
& \frac{137 b^4 c^5 q^2 r^2 \text{Log}[c + d x]}{150 d^5} + \frac{25 a b^3 c^4 q^2 r^2 \text{Log}[c + d x]}{6 d^4} - \frac{22 a^2 b^2 c^3 q^2 r^2 \text{Log}[c + d x]}{3 d^3} + \frac{6 a^3 b c^2 q^2 r^2 \text{Log}[c + d x]}{d^2} - \frac{2 a^4 c q^2 r^2 \text{Log}[c + d x]}{d} -
\end{aligned}$$

$$\begin{aligned}
& \frac{b^4 c^5 q^2 r^2 \operatorname{Log}[c + dx]^2}{5 d^5} + \frac{a b^3 c^4 q^2 r^2 \operatorname{Log}[c + dx]^2}{d^4} - \frac{2 a^2 b^2 c^3 q^2 r^2 \operatorname{Log}[c + dx]^2}{d^3} + \frac{2 a^3 b c^2 q^2 r^2 \operatorname{Log}[c + dx]^2}{d^2} - \frac{a^4 c q^2 r^2 \operatorname{Log}[c + dx]^2}{d} \\
& \frac{2 a^5 p r \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{b} - \frac{2}{5} a^4 p r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - 2 a^4 q r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - \\
& \frac{2 b^4 c^4 q r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{5 d^4} + \frac{2 a b^3 c^3 q r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^3} - \frac{4 a^2 b^2 c^2 q r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^2} + \\
& \frac{4 a^3 b c q r x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d} - \frac{4}{5} a^3 b p r x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - 2 a^3 b q r x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] + \\
& \frac{b^4 c^3 q r x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{5 d^3} - \frac{a b^3 c^2 q r x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^2} + \frac{2 a^2 b^2 c q r x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d} - \\
& \frac{4}{5} a^2 b^2 p r x^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - \frac{4}{3} a^2 b^2 q r x^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - \frac{2 b^4 c^2 q r x^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{15 d^2} + \\
& \frac{2 a b^3 c q r x^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{3 d} - \frac{2}{5} a b^3 p r x^4 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - \frac{1}{2} a b^3 q r x^4 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] + \\
& \frac{b^4 c q r x^4 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{10 d} - \frac{2}{25} b^4 p r x^5 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] - \frac{2}{25} b^4 q r x^5 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] + \\
& \frac{2 b^4 c^5 q r \operatorname{Log}[c + dx] \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{5 d^5} - \frac{2 a b^3 c^4 q r \operatorname{Log}[c + dx] \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^4} + \\
& \frac{4 a^2 b^2 c^3 q r \operatorname{Log}[c + dx] \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^3} - \frac{4 a^3 b c^2 q r \operatorname{Log}[c + dx] \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d^2} + \\
& \frac{2 a^4 c q r \operatorname{Log}[c + dx] \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]}{d} + a^4 x \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 + 2 a^3 b x^2 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 + \\
& 2 a^2 b^2 x^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 + a b^3 x^4 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 + \frac{1}{5} b^4 x^5 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 + \\
& \frac{1}{150 b d^5} p r \operatorname{Log}[a + bx] \left(a d (a^4 d^4 (288 p - 137 q) - 60 b^4 c^4 q + 270 a b^3 c^3 d q - 470 a^2 b^2 c^2 d^2 q + 385 a^3 b c d^3 q) r - \right. \\
& \left. 60 b c (b^4 c^4 - 5 a b^3 c^3 d + 10 a^2 b^2 c^2 d^2 - 10 a^3 b c d^3 + 5 a^4 d^4) q r \operatorname{Log}[c + dx] + 60 (b c - a d)^5 q r \operatorname{Log}\left[\frac{b(c + dx)}{b c - a d}\right] + \right. \\
& \left. 60 a^5 d^5 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r] \right) + \frac{2 (b c - a d)^5 p q r^2 \operatorname{PolyLog}\left[2, \frac{d(a + bx)}{-b c + a d}\right]}{5 b d^5}
\end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int (a + bx)^3 \operatorname{Log}[e (f(a + bx)^p (c + dx)^q)^r]^2 dx$$

Optimal (type 4, 805 leaves, 28 steps):

$$\begin{aligned}
& \frac{a (b c - a d)^2 p q r^2 x}{4 d^2} - \frac{(b c - a d)^3 p q r^2 x}{8 d^3} - \frac{13 (b c - a d)^3 q^2 r^2 x}{24 d^3} - \frac{(b c - a d)^3 q (p + q) r^2 x}{2 d^3} + \frac{b (b c - a d)^2 p q r^2 x^2}{8 d^2} + \\
& \frac{(b c - a d)^2 p q r^2 (a + b x)^2}{16 b d^2} + \frac{13 (b c - a d)^2 q^2 r^2 (a + b x)^2}{48 b d^2} - \frac{7 (b c - a d) p q r^2 (a + b x)^3}{72 b d} - \frac{7 (b c - a d) q^2 r^2 (a + b x)^3}{72 b d} + \\
& \frac{p^2 r^2 (a + b x)^4}{32 b} + \frac{p q r^2 (a + b x)^4}{16 b} + \frac{q^2 r^2 (a + b x)^4}{32 b} + \frac{(b c - a d)^4 p q r^2 \text{Log}[c + d x]}{8 b d^4} + \frac{25 (b c - a d)^4 q^2 r^2 \text{Log}[c + d x]}{24 b d^4} + \\
& \frac{(b c - a d)^4 p q r^2 \text{Log}\left[-\frac{d(a+b x)}{b c - a d}\right] \text{Log}[c + d x]}{2 b d^4} + \frac{(b c - a d)^4 q^2 r^2 \text{Log}[c + d x]^2}{4 b d^4} + \frac{(b c - a d)^3 q r (a + b x) \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{2 b d^3} - \\
& \frac{(b c - a d)^2 q r (a + b x)^2 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{4 b d^2} + \frac{(b c - a d) q r (a + b x)^3 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{6 b d} - \\
& \frac{p r (a + b x)^4 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{8 b} - \frac{q r (a + b x)^4 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{8 b} - \\
& \frac{(b c - a d)^4 q r \text{Log}[c + d x] \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{2 b d^4} + \frac{(a + b x)^4 \text{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]^2}{4 b} + \frac{(b c - a d)^4 p q r^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]}{2 b d^4}
\end{aligned}$$

Result (type 4, 1853 leaves):

$$\begin{aligned}
& \frac{2 a^4 p q r^2}{b} - \frac{a b^2 c^3 p q r^2}{2 d^3} + \frac{2 a^2 b c^2 p q r^2}{d^2} - \frac{3 a^3 c p q r^2}{d} + \frac{1}{8} a^3 p^2 r^2 x + \frac{37}{24} a^3 p q r^2 x - \frac{5 b^3 c^3 p q r^2 x}{8 d^3} + \frac{9 a b^2 c^2 p q r^2 x}{4 d^2} - \\
& \frac{35 a^2 b c p q r^2 x}{12 d} + 2 a^3 q^2 r^2 x - \frac{25 b^3 c^3 q^2 r^2 x}{24 d^3} + \frac{11 a b^2 c^2 q^2 r^2 x}{3 d^2} - \frac{9 a^2 b c q^2 r^2 x}{2 d} + \frac{3}{16} a^2 b p^2 r^2 x^2 + \frac{41}{48} a^2 b p q r^2 x^2 + \\
& \frac{3 b^3 c^2 p q r^2 x^2}{16 d^2} - \frac{2 a b^2 c p q r^2 x^2}{3 d} + \frac{3}{4} a^2 b q^2 r^2 x^2 + \frac{13 b^3 c^2 q^2 r^2 x^2}{48 d^2} - \frac{5 a b^2 c q^2 r^2 x^2}{6 d} + \frac{1}{8} a b^2 p^2 r^2 x^3 + \frac{25}{72} a b^2 p q r^2 x^3 - \\
& \frac{7 b^3 c p q r^2 x^3}{72 d} + \frac{2}{9} a b^2 q^2 r^2 x^3 - \frac{7 b^3 c q^2 r^2 x^3}{72 d} + \frac{1}{32} b^3 p^2 r^2 x^4 + \frac{1}{16} b^3 p q r^2 x^4 + \frac{1}{32} b^3 q^2 r^2 x^4 - \frac{a^4 p^2 r^2 \text{Log}[a + b x]^2}{4 b} + \\
& \frac{2 a^4 p q r^2 \text{Log}[c + d x]}{b} + \frac{b^3 c^4 p q r^2 \text{Log}[c + d x]}{8 d^4} - \frac{a b^2 c^3 p q r^2 \text{Log}[c + d x]}{2 d^3} + \frac{3 a^2 b c^2 p q r^2 \text{Log}[c + d x]}{4 d^2} - \frac{a^3 c p q r^2 \text{Log}[c + d x]}{2 d} + \\
& \frac{25 b^3 c^4 q^2 r^2 \text{Log}[c + d x]}{24 d^4} - \frac{11 a b^2 c^3 q^2 r^2 \text{Log}[c + d x]}{3 d^3} + \frac{9 a^2 b c^2 q^2 r^2 \text{Log}[c + d x]}{2 d^2} - \frac{2 a^3 c q^2 r^2 \text{Log}[c + d x]}{d} + \frac{b^3 c^4 q^2 r^2 \text{Log}[c + d x]^2}{4 d^4} - \\
& \frac{a b^2 c^3 q^2 r^2 \text{Log}[c + d x]^2}{d^3} + \frac{3 a^2 b c^2 q^2 r^2 \text{Log}[c + d x]^2}{2 d^2} - \frac{a^3 c q^2 r^2 \text{Log}[c + d x]^2}{d} - \frac{2 a^4 p r \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{b} - \\
& \frac{1}{2} a^3 p r x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - 2 a^3 q r x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] + \frac{b^3 c^3 q r x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{2 d^3} - \\
& \frac{2 a b^2 c^2 q r x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d^2} + \frac{3 a^2 b c q r x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d} - \frac{3}{4} a^2 b p r x^2 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - \\
& \frac{3}{2} a^2 b q r x^2 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - \frac{b^3 c^2 q r x^2 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{4 d^2} + \frac{a b^2 c q r x^2 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d} - \\
& \frac{1}{2} a b^2 p r x^3 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - \frac{2}{3} a b^2 q r x^3 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] + \frac{b^3 c q r x^3 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{6 d} - \\
& \frac{1}{8} b^3 p r x^4 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - \frac{1}{8} b^3 q r x^4 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] - \frac{b^3 c^4 q r \text{Log}[c + d x] \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{2 d^4} + \\
& \frac{2 a b^2 c^3 q r \text{Log}[c + d x] \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d^3} - \frac{3 a^2 b c^2 q r \text{Log}[c + d x] \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d^2} + \\
& \frac{2 a^3 c q r \text{Log}[c + d x] \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]}{d} + a^3 x \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2 + \\
& \frac{3}{2} a^2 b x^2 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2 + a b^2 x^3 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2 + \frac{1}{4} b^3 x^4 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2 + \frac{1}{24 b d^4} \\
& p r \text{Log}[a + b x] \left(a d (5 a^3 d^3 (9 p - 5 q) + 12 b^3 c^3 q - 42 a b^2 c^2 d q + 52 a^2 b c d^2 q) r + 12 b c (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) q r \text{Log}[c + d x] - \right. \\
& \left. 12 (b c - a d)^4 q r \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 12 a^4 d^4 \text{Log}[e (f (a + b x)^p (c + d x)^q)^r] \right) - \frac{(b c - a d)^4 p q r^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{2 b d^4}
\end{aligned}$$

Problem 23: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]^2}{(a+bx)^4} dx$$

Optimal (type 4, 764 leaves, 28 steps):

$$\begin{aligned} & -\frac{2p^2r^2}{27b(a+bx)^3} - \frac{5dpqr^2}{18b(bc-ad)(a+bx)^2} + \frac{8d^2pqr^2}{9b(bc-ad)^2(a+bx)} - \frac{d^2q^2r^2}{3b(bc-ad)^2(a+bx)} + \\ & \frac{2d^3pqr^2\text{Log}[a+bx]}{9b(bc-ad)^3} - \frac{d^3q^2r^2\text{Log}[a+bx]}{b(bc-ad)^3} - \frac{d^3pqr^2\text{Log}[a+bx]^2}{3b(bc-ad)^3} - \frac{2d^3pqr^2\text{Log}[c+dx]}{9b(bc-ad)^3} + \frac{d^3q^2r^2\text{Log}[c+dx]}{b(bc-ad)^3} + \\ & \frac{2d^3pqr^2\text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right]\text{Log}[c+dx]}{3b(bc-ad)^3} + \frac{d^3q^2r^2\text{Log}[c+dx]^2}{3b(bc-ad)^3} - \frac{2d^3q^2r^2\text{Log}[a+bx]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{3b(bc-ad)^3} - \\ & \frac{2pr\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]}{9b(a+bx)^3} - \frac{dqr\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]}{3b(bc-ad)(a+bx)^2} + \frac{2d^2qr\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]}{3b(bc-ad)^2(a+bx)} + \\ & \frac{2d^3qr\text{Log}[a+bx]\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]}{3b(bc-ad)^3} - \frac{2d^3qr\text{Log}[c+dx]\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]}{3b(bc-ad)^3} - \\ & \frac{\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]^2}{3b(a+bx)^3} - \frac{2d^3q^2r^2\text{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right]}{3b(bc-ad)^3} + \frac{2d^3pqr^2\text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{3b(bc-ad)^3} \end{aligned}$$

Result (type 4, 10507 leaves):

$$\begin{aligned} & -\frac{p^2r^2(6\text{Log}[a+bx]+18\text{Log}[a+bx]^2+27\text{Log}[a+bx]^3)}{81b(a+bx)^3\text{Log}[a+bx]} + \frac{q^2r^2(b^2c^3-3ab^2cd+3a^2cd^2+3a^2d^3x+3abd^3x^2+b^2d^3x^3)\text{Log}[c+dx]^2}{3(-bc+ad)^3(a+bx)^3} - \\ & \frac{1}{3b(a+bx)^3} \left(-pr\text{Log}[a+bx] - \text{Log}\left[f(a+bx)^p(c+dx)^q\right] \left(r - \frac{r(-q\text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]} \right) + \right. \\ & \left. \text{Log}\left[e^{r(-p\text{Log}[a+bx]-q\text{Log}[c+dx]+\text{Log}\left[f(a+bx)^p(c+dx)^q\right])} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^r - \frac{r(-q\text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]} \right]^2 - \right. \\ & \frac{1}{9b(bc-ad)^2(a+bx)} d^2qr \left(-2pr+3qr-6r(-p\text{Log}[a+bx]-q\text{Log}[c+dx]+\text{Log}\left[f(a+bx)^p(c+dx)^q\right]) - \right. \\ & \left. 6 \left(-pr\text{Log}[a+bx] - r(-p\text{Log}[a+bx]-q\text{Log}[c+dx]+\text{Log}\left[f(a+bx)^p(c+dx)^q\right]) - \right. \right. \\ & \left. \left. \text{Log}\left[f(a+bx)^p(c+dx)^q\right] \left(r - \frac{r(-q\text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]} \right) \right) + \end{aligned}$$

$$\begin{aligned}
& q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q] - \operatorname{Log}[f(a + bx)^p (c + dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q])}{\operatorname{Log}[f(a + bx)^p (c + dx)^q]} \right) + \\
& \operatorname{Log}\left[e^{r(-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q])} (a + bx)^{pr} (f(a + bx)^p (c + dx)^q)^{r - \frac{r(-q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q])}{\operatorname{Log}[f(a + bx)^p (c + dx)^q]}} \right] \Bigg) - \\
& \frac{1}{3(bc - ad)^3} 8a^2 b^2 d^4 q^2 r^2 \left(\frac{c^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} + \frac{(3ab^2c^2 - 3a^2bcd + a^3d^2)(1 + \operatorname{Log}[a + bx])}{b^2(bc - ad)^3(ab + b^2x)} - \frac{(3a^2bc - 2a^3d)(1 + 2\operatorname{Log}[a + bx])}{4b^3(bc - ad)^2(a + bx)^2} + \right. \\
& \left. \frac{a^3(1 + 3\operatorname{Log}[a + bx])}{9b^3(bc - ad)(a + bx)^3} - \frac{c^3(\operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc - ad)^4} \right) - \frac{1}{3(bc - ad)^3} \\
& 2b^3 d^4 q^2 r^2 \left(- \frac{(4ab^3c^3 - 6a^2b^2c^2d + 4a^3bcd^2 - a^4d^3) \operatorname{Log}[a + bx]^2}{2b^4(bc - ad)^4} - \frac{(6a^2b^2c^2 - 8a^3bcd + 3a^4d^2)(1 + \operatorname{Log}[a + bx])}{b^3(bc - ad)^3(ab + b^2x)} + \right. \\
& \left. \frac{(4a^3bc - 3a^4d)(1 + 2\operatorname{Log}[a + bx])}{4b^4(bc - ad)^2(a + bx)^2} - \frac{a^4(1 + 3\operatorname{Log}[a + bx])}{9b^4(bc - ad)(a + bx)^3} + \frac{c^4(\operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{d(bc - ad)^4} \right) - \\
& \frac{1}{(bc - ad)^3} 4a^2 b d^4 q^2 r^2 \left(- \frac{c^2 d \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{bc^2(1 + \operatorname{Log}[a + bx])}{(bc - ad)^3(ab + b^2x)} + \frac{(2abc - a^2d)(1 + 2\operatorname{Log}[a + bx])}{4b^2(bc - ad)^2(a + bx)^2} - \right. \\
& \left. \frac{a^2(1 + 3\operatorname{Log}[a + bx])}{9b^2(bc - ad)(a + bx)^3} + \frac{c^2 d(\operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc - ad)^4} \right) + \\
& \frac{1}{3(bc - ad)^3} 2b^3 c^3 dpqr^2 \left(\frac{cd^2 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} + \frac{bcd(1 + \operatorname{Log}[a + bx])}{(bc - ad)^3(ab + b^2x)} - \frac{c(1 + 2\operatorname{Log}[a + bx])}{4(bc - ad)^2(a + bx)^2} - \right. \\
& \left. \frac{a(1 + 3\operatorname{Log}[a + bx])}{9b(-bc + ad)(a + bx)^3} - \frac{cd^2(\operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc - ad)^4} \right) - \\
& \frac{1}{(bc - ad)^3} 2a^2 b^2 c^2 d^2 pqr^2 \left(\frac{cd^2 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} + \frac{bcd(1 + \operatorname{Log}[a + bx])}{(bc - ad)^3(ab + b^2x)} - \frac{c(1 + 2\operatorname{Log}[a + bx])}{4(bc - ad)^2(a + bx)^2} - \right. \\
& \left. \frac{a(1 + 3\operatorname{Log}[a + bx])}{9b(-bc + ad)(a + bx)^3} - \frac{cd^2(\operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc - ad)^4} \right) + \\
& \frac{1}{(bc - ad)^3} 2a^2 bcd^3 pqr^2 \left(\frac{cd^2 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} + \frac{bcd(1 + \operatorname{Log}[a + bx])}{(bc - ad)^3(ab + b^2x)} - \frac{c(1 + 2\operatorname{Log}[a + bx])}{4(bc - ad)^2(a + bx)^2} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{3(bc-ad)^3} 2a^3 d^4 p q r^2 \left(\frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(a+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{3(bc-ad)^3} 8a^3 d^4 q^2 r^2 \left(\frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(a+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 2b^3 c^3 d p r^2 (-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) \\
& \left(\frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(a+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc-ad)^3} 6a^2 b^2 c^2 d^2 p r^2 (-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) \\
& \left(\frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(a+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 6a^2 b c d^3 p r^2 (-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) \\
& \left(\frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(a+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc-ad)^3} 2a^3d^4pr^2(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) \\
& \left(\frac{cd^2\operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
& \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 2b^3c^3dpr\left(-pr\operatorname{Log}[a+bx] - r(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{e^{r(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(\frac{cd^2\operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \right. \\
& \left. \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc-ad)^3} 6a^2b^2c^2d^2pr\left(-pr\operatorname{Log}[a+bx] - r(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{e^{r(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(\frac{cd^2\operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \right. \\
& \left. \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2\left(\operatorname{Log}[a+bx]\operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 6a^2bcd^3pr\left(-pr\operatorname{Log}[a+bx] - r(-p\operatorname{Log}[a+bx] - q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q\operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \text{Log} \left[e^{e^{r(-p \text{Log}[a+bx]-q \text{Log}[c+dx]+\text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r-\frac{-q \text{Log}[c+dx]+\text{Log}[f(a+bx)^p(c+dx)^q]}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(\frac{cd^2 \text{Log}[a+bx]^2}{2(bc-a)^4} + \right. \\
& \left. \frac{bcd(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} - \frac{c(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} - \frac{a(1+3\text{Log}[a+bx])}{9b(-bc+a)(a+bx)^3} - \frac{cd^2 \left(\text{Log}[a+bx] \text{Log} \left[\frac{b(c+dx)}{bc-a} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+a} \right] \right)}{(bc-a)^4} \right) - \\
& \frac{1}{(bc-a)^3} 2a^3 d^4 p r \left(-p r \text{Log}[a+bx] - r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \text{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \text{Log} \left[e^{e^{r(-p \text{Log}[a+bx]-q \text{Log}[c+dx]+\text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r-\frac{-q \text{Log}[c+dx]+\text{Log}[f(a+bx)^p(c+dx)^q]}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(\frac{cd^2 \text{Log}[a+bx]^2}{2(bc-a)^4} + \right. \\
& \left. \frac{bcd(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} - \frac{c(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} - \frac{a(1+3\text{Log}[a+bx])}{9b(-bc+a)(a+bx)^3} - \frac{cd^2 \left(\text{Log}[a+bx] \text{Log} \left[\frac{b(c+dx)}{bc-a} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+a} \right] \right)}{(bc-a)^4} \right) + \\
& \frac{1}{3(bc-a)^3} 2ab^2 c^3 d p q r^2 \left(-\frac{d^3 \text{Log}[a+bx]^2}{2(bc-a)^4} - \frac{bd^2(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} + \frac{d(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} + \right. \\
& \left. \frac{1+3\text{Log}[a+bx]}{9(-bc+a)(a+bx)^3} + \frac{d^3 \left(\text{Log}[a+bx] \text{Log} \left[\frac{b(c+dx)}{bc-a} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+a} \right] \right)}{(bc-a)^4} \right) - \\
& \frac{1}{(bc-a)^3} 2a^2 b c^2 d^2 p q r^2 \left(-\frac{d^3 \text{Log}[a+bx]^2}{2(bc-a)^4} - \frac{bd^2(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} + \frac{d(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} + \right. \\
& \left. \frac{1+3\text{Log}[a+bx]}{9(-bc+a)(a+bx)^3} + \frac{d^3 \left(\text{Log}[a+bx] \text{Log} \left[\frac{b(c+dx)}{bc-a} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+a} \right] \right)}{(bc-a)^4} \right) + \\
& \frac{1}{(bc-a)^3} 2a^3 c d^3 p q r^2 \left(-\frac{d^3 \text{Log}[a+bx]^2}{2(bc-a)^4} - \frac{bd^2(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} + \frac{d(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} + \right. \\
& \left. \frac{1+3\text{Log}[a+bx]}{9(-bc+a)(a+bx)^3} + \frac{d^3 \left(\text{Log}[a+bx] \text{Log} \left[\frac{b(c+dx)}{bc-a} \right] + \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+a} \right] \right)}{(bc-a)^4} \right) - \\
& \frac{1}{3b(bc-a)^3} 2a^4 d^4 p q r^2 \left(-\frac{d^3 \text{Log}[a+bx]^2}{2(bc-a)^4} - \frac{bd^2(1+\text{Log}[a+bx])}{(bc-a)^3(ab+b^2x)} + \frac{d(1+2\text{Log}[a+bx])}{4(bc-a)^2(a+bx)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{3 b (bc - ad)^3} 2 a^4 d^4 q^2 r^2 \left(-\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (bc - ad)^2 (a + b x)^2} + \right. \\
& \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc - ad)^3} 2 b^3 c^4 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
& \left(-\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (bc - ad)^2 (a + b x)^2} + \right. \\
& \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc - ad)^3} 6 a b^2 c^3 d p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
& \left(-\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (bc - ad)^2 (a + b x)^2} + \right. \\
& \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc - ad)^3} 6 a^2 b c^2 d^2 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
& \left(-\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (bc - ad)^2 (a + b x)^2} + \right. \\
& \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc - ad)^3} 2 a^3 c d^3 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])
\end{aligned}$$

$$\begin{aligned}
& \left(-\frac{d^3 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} - \frac{bd^2(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} + \frac{d(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} + \right. \\
& \left. \frac{1+3\operatorname{Log}[a+bx]}{9(-bc+ad)(a+bx)^3} + \frac{d^3 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 2b^3c^4pr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(-\frac{d^3 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} - \right. \\
& \left. \frac{bd^2(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} + \frac{d(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} + \frac{1+3\operatorname{Log}[a+bx]}{9(-bc+ad)(a+bx)^3} + \frac{d^3 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^4} \right) - \\
& \frac{1}{(bc-ad)^3} 6a^2b^2c^3dpr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(-\frac{d^3 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} - \right. \\
& \left. \frac{bd^2(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} + \frac{d(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} + \frac{1+3\operatorname{Log}[a+bx]}{9(-bc+ad)(a+bx)^3} + \frac{d^3 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^4} \right) + \\
& \frac{1}{(bc-ad)^3} 6a^2bc^2d^2pr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \left(-\frac{d^3 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} - \right.
\end{aligned}$$

$$\frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} + \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \Bigg) -$$

$$\frac{1}{(b c - a d)^3} 2 a^3 c d^3 p r \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right.$$

$$\operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) +$$

$$\operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \Bigg) \left(-\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} - \right.$$

$$\frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} + \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \Bigg)$$

Problem 24: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]^2}{(a + b x)^5} dx$$

Optimal (type 4, 884 leaves, 32 steps):

$$-\frac{p^2 r^2}{32 b (a + b x)^4} - \frac{7 d p q r^2}{72 b (b c - a d) (a + b x)^3} + \frac{3 d^2 p q r^2}{16 b (b c - a d)^2 (a + b x)^2} - \frac{d^2 q^2 r^2}{12 b (b c - a d)^2 (a + b x)^2} - \frac{5 d^3 p q r^2}{8 b (b c - a d)^3 (a + b x)} +$$

$$\frac{5 d^3 q^2 r^2}{12 b (b c - a d)^3 (a + b x)} - \frac{d^4 p q r^2 \operatorname{Log}[a + b x]}{8 b (b c - a d)^4} + \frac{11 d^4 q^2 r^2 \operatorname{Log}[a + b x]}{12 b (b c - a d)^4} + \frac{d^4 p q r^2 \operatorname{Log}[a + b x]^2}{4 b (b c - a d)^4} + \frac{d^4 p q r^2 \operatorname{Log}[c + d x]}{8 b (b c - a d)^4} -$$

$$\frac{11 d^4 q^2 r^2 \operatorname{Log}[c + d x]}{12 b (b c - a d)^4} - \frac{d^4 p q r^2 \operatorname{Log}\left[-\frac{d(a+b x)}{b c - a d}\right] \operatorname{Log}[c + d x]}{2 b (b c - a d)^4} - \frac{d^4 q^2 r^2 \operatorname{Log}[c + d x]^2}{4 b (b c - a d)^4} + \frac{d^4 q^2 r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right]}{2 b (b c - a d)^4} -$$

$$\frac{p r \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{8 b (a + b x)^4} - \frac{d q r \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{6 b (b c - a d) (a + b x)^3} + \frac{d^2 q r \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{4 b (b c - a d)^2 (a + b x)^2} -$$

$$\frac{d^3 q r \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{2 b (b c - a d)^3 (a + b x)} - \frac{d^4 q r \operatorname{Log}[a + b x] \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{2 b (b c - a d)^4} + \frac{d^4 q r \operatorname{Log}[c + d x] \operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]}{2 b (b c - a d)^4} -$$

$$\frac{\operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q \right)^r \right]^2}{4 b (a + b x)^4} + \frac{d^4 q^2 r^2 \operatorname{PolyLog}\left[2, -\frac{d(a+b x)}{b c - a d}\right]}{2 b (b c - a d)^4} - \frac{d^4 p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]}{2 b (b c - a d)^4}$$

Result (type 4, 14321 leaves):

$$\begin{aligned}
& - \frac{p^2 r^2 (8 \operatorname{Log}[a + b x] + 32 \operatorname{Log}[a + b x]^2 + 64 \operatorname{Log}[a + b x]^3)}{256 b (a + b x)^4 \operatorname{Log}[a + b x]} + \frac{1}{4 (-b c + a d)^4 (a + b x)^4} \\
& q^2 r^2 (-b^3 c^4 + 4 a b^2 c^3 d - 6 a^2 b c^2 d^2 + 4 a^3 c d^3 + 4 a^3 d^4 x + 6 a^2 b d^4 x^2 + 4 a b^2 d^4 x^3 + b^3 d^4 x^4) \operatorname{Log}[c + d x]^2 - \\
& \frac{1}{4 b (a + b x)^4} \left(-p r \operatorname{Log}[a + b x] - \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
& \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right]^2 - \\
& \frac{1}{48 b (b c - a d)^2 (a + b x)^2} d^2 q r \left(-3 p r + 4 q r - 12 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& 12 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \Bigg) + \\
& \frac{1}{24 b (b c - a d)^3 (a + b x)} d^3 q r \left(-3 p r + 10 q r - 12 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& 12 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \Bigg) + \\
& \frac{1}{24 b (b c - a d)^4} d^4 q r \operatorname{Log}[a + b x] \left(-3 p r + 22 q r - 12 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& 12 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
& \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \Bigg) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{24 b (b c - a d)^4} d^4 q r \operatorname{Log}[c + d x] \left(-3 p r + 22 q r - 12 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& 12 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) + \right. \\
& \left. \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \right) - \\
& \frac{1}{24 b (b c - a d) (a + b x)^3} d q r \left(p r + 4 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) + \right. \\
& 4 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) + \right. \\
& \left. \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \right) + \\
& \operatorname{Log}[c + d x] \left(-\frac{d q^2 r^2}{6 b (b c - a d) (a + b x)^3} + \frac{d^2 q^2 r^2}{4 b (b c - a d)^2 (a + b x)^2} - \frac{d^3 q^2 r^2}{2 b (b c - a d)^3 (a + b x)} - \frac{d^4 q^2 r^2 \operatorname{Log}[a + b x]}{2 b (b c - a d)^4} - \frac{p q r^2 \operatorname{Log}[a + b x]}{2 b (a + b x)^4} - \right. \\
& \frac{1}{8 b (a + b x)^4} q r \left(p r + 4 r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) + 4 \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - \right. \right. \\
& \left. \left. q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \right. \\
& \left. \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \right) \right) + \\
& \frac{1}{2 (b c - a d)^4} 5 a b^3 d^5 q^2 r^2 \left(\frac{c^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{(4 a b^3 c^3 - 6 a^2 b^2 c^2 d + 4 a^3 b c d^2 - a^4 d^3) (1 + \operatorname{Log}[a + b x])}{b^3 (b c - a d)^4 (a b + b^2 x)} - \right. \\
& \frac{(6 a^2 b^2 c^2 - 8 a^3 b c d + 3 a^4 d^2) (1 + 2 \operatorname{Log}[a + b x])}{4 b^4 (b c - a d)^3 (a + b x)^2} + \frac{(4 a^3 b c - 3 a^4 d) (1 + 3 \operatorname{Log}[a + b x])}{9 b^4 (b c - a d)^2 (a + b x)^3} - \\
& \left. \frac{a^4 (1 + 4 \operatorname{Log}[a + b x])}{16 b^4 (b c - a d) (a + b x)^4} - \frac{c^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d} \right] \right)}{(b c - a d)^5} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2(b c - a d)^4} b^4 d^5 q^2 r^2 \left(- \frac{(5 a b^4 c^4 - 10 a^2 b^3 c^3 d + 10 a^3 b^2 c^2 d^2 - 5 a^4 b c d^3 + a^5 d^4) \operatorname{Log}[a + b x]^2}{2 b^5 (b c - a d)^5} - \right. \\
& \quad \frac{(10 a^2 b^3 c^3 - 20 a^3 b^2 c^2 d + 15 a^4 b c d^2 - 4 a^5 d^3) (1 + \operatorname{Log}[a + b x])}{b^4 (b c - a d)^4 (a b + b^2 x)} + \frac{(10 a^3 b^2 c^2 - 15 a^4 b c d + 6 a^5 d^2) (1 + 2 \operatorname{Log}[a + b x])}{4 b^5 (b c - a d)^3 (a + b x)^2} \\
& \quad \left. \frac{(5 a^4 b c - 4 a^5 d) (1 + 3 \operatorname{Log}[a + b x])}{9 b^5 (b c - a d)^2 (a + b x)^3} + \frac{a^5 (1 + 4 \operatorname{Log}[a + b x])}{16 b^5 (b c - a d) (a + b x)^4} + \frac{c^5 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{d (b c - a d)^5} \right) + \\
& \frac{1}{(b c - a d)^4} 5 a^2 b^2 d^5 q^2 r^2 \left(- \frac{c^3 d \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{(3 a b^2 c^2 - 3 a^2 b c d + a^3 d^2) (1 + 2 \operatorname{Log}[a + b x])}{4 b^3 (b c - a d)^3 (a + b x)^2} - \right. \\
& \quad \left. \frac{(3 a^2 b c - 2 a^3 d) (1 + 3 \operatorname{Log}[a + b x])}{9 b^3 (b c - a d)^2 (a + b x)^3} + \frac{a^3 (1 + 4 \operatorname{Log}[a + b x])}{16 b^3 (b c - a d) (a + b x)^4} + \frac{c^3 d \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \\
& \frac{1}{(b c - a d)^4} 5 a^3 b d^5 q^2 r^2 \left(\frac{c^2 d^2 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b c^2 d (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{c^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{(2 a b c - a^2 d) (1 + 3 \operatorname{Log}[a + b x])}{9 b^2 (b c - a d)^2 (a + b x)^3} - \right. \\
& \quad \left. \frac{a^2 (1 + 4 \operatorname{Log}[a + b x])}{16 b^2 (b c - a d) (a + b x)^4} - \frac{c^2 d^2 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \frac{1}{2 (b c - a d)^4} \\
& b^4 c^4 d p q r^2 \left(- \frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \right. \\
& \quad \left. \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) - \frac{1}{(b c - a d)^4} \\
& 2 a b^3 c^3 d^2 p q r^2 \left(- \frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \right. \\
& \quad \left. \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \frac{1}{(b c - a d)^4} \\
& 3 a^2 b^2 c^2 d^3 p q r^2 \left(- \frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \right. \\
& \quad \left. \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) - \frac{1}{(b c - a d)^4}
\end{aligned}$$

$$2 a^3 b c d^4 p q r^2 \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(b c - a d)^5} \right) + \frac{1}{2 (b c - a d)^4}$$

$$a^4 d^5 p q r^2 \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(b c - a d)^5} \right) + \frac{1}{2 (b c - a d)^4}$$

$$5 a^4 d^5 q^2 r^2 \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(b c - a d)^5} \right) +$$

$$\frac{1}{(b c - a d)^4} 2 b^4 c^4 d p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(b c - a d)^5} \right) -$$

$$\frac{1}{(b c - a d)^4} 8 a b^3 c^3 d^2 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(b c - a d)^5} \right) +$$

$$\frac{1}{(b c - a d)^4} 12 a^2 b^2 c^2 d^3 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\begin{aligned}
& \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} \right. \\
& \left. - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(b c - a d)^5} \right) - \\
& \frac{1}{(b c - a d)^4} 8 a^3 b c d^4 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
& \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} \right. \\
& \left. - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(b c - a d)^5} \right) + \\
& \frac{1}{(b c - a d)^4} 2 a^4 d^5 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
& \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} \right. \\
& \left. - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(b c - a d)^5} \right) + \\
& \frac{1}{(b c - a d)^4} 2 b^4 c^4 d p r \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
& \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) + \right. \\
& \left. \operatorname{Log}\left[e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \right) \\
& \left(-\frac{c d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} \right. \\
& \left. - \frac{a (1 + 4 \operatorname{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \frac{c d^3 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(b c - a d)^5} \right) - \\
& \frac{1}{(b c - a d)^4} 8 a b^3 c^3 d^2 p r \left(-p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right.
\end{aligned}$$

$$\begin{aligned}
& \text{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
& \text{Log}\left[e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right] \\
& \left(-\frac{cd^3 \text{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{bcd^2(1+\text{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} + \frac{cd(1+2\text{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} - \frac{c(1+3\text{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} - \right. \\
& \left. \frac{a(1+4\text{Log}[a+bx])}{16b(-bc+ad)(a+bx)^4} + \frac{cd^3(\text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc-ad)^5} \right) + \\
& \frac{1}{(bc-ad)^4} 12a^2b^2c^2d^3pr \left(-pr \text{Log}[a+bx] - r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \text{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \right. \\
& \left. \text{Log}\left[e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \\
& \left(-\frac{cd^3 \text{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{bcd^2(1+\text{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} + \frac{cd(1+2\text{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} - \frac{c(1+3\text{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} - \right. \\
& \left. \frac{a(1+4\text{Log}[a+bx])}{16b(-bc+ad)(a+bx)^4} + \frac{cd^3(\text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc-ad)^5} \right) - \\
& \frac{1}{(bc-ad)^4} 8a^3bcd^4pr \left(-pr \text{Log}[a+bx] - r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\
& \left. \text{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \right. \\
& \left. \text{Log}\left[e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right) \\
& \left(-\frac{cd^3 \text{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{bcd^2(1+\text{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} + \frac{cd(1+2\text{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} - \frac{c(1+3\text{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} - \right. \\
& \left. \frac{a(1+4\text{Log}[a+bx])}{16b(-bc+ad)(a+bx)^4} + \frac{cd^3(\text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right])}{(bc-ad)^5} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{(bc-ad)^4} 2a^4 d^5 p r \left(-p r \operatorname{Log}[a+bx] - r \left(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q] \right) - \right. \\
& \quad \left. \operatorname{Log}[f(a+bx)^p (c+dx)^q] \left(r - \frac{r \left(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q] \right)}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]} \right) + \right. \\
& \quad \left. \operatorname{Log}\left[e^{e^{r \left(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q] \right)}} (a+bx)^{pr} (f(a+bx)^p (c+dx)^q)^{r - \frac{r \left(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q] \right)}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]}} \right] \right) \\
& \left(-\frac{c d^3 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{b c d^2 (1 + \operatorname{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} + \frac{c d (1 + 2 \operatorname{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} - \frac{c (1 + 3 \operatorname{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} - \right. \\
& \quad \left. \frac{a (1 + 4 \operatorname{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} + \frac{c d^3 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \frac{1}{2(bc-ad)^4} \\
& a b^3 c^4 d p q r^2 \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} + \right. \\
& \quad \left. \frac{1 + 4 \operatorname{Log}[a+bx]}{16 (-bc+ad) (a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) - \frac{1}{(bc-ad)^4} \\
& 2 a^2 b^2 c^3 d^2 p q r^2 \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} + \right. \\
& \quad \left. \frac{1 + 4 \operatorname{Log}[a+bx]}{16 (-bc+ad) (a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \frac{1}{(bc-ad)^4} \\
& 3 a^3 b c^2 d^3 p q r^2 \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} + \right. \\
& \quad \left. \frac{1 + 4 \operatorname{Log}[a+bx]}{16 (-bc+ad) (a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) - \frac{1}{(bc-ad)^4} \\
& 2 a^4 c d^4 p q r^2 \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} + \right. \\
& \quad \left. \frac{1 + 4 \operatorname{Log}[a+bx]}{16 (-bc+ad) (a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \frac{1}{2 b (bc-ad)^4}
\end{aligned}$$

$$a^5 d^5 p q r^2 \left(\frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-b c + a d}\right] \right)}{(b c - a d)^5} \right) + \frac{1}{2 b (b c - a d)^4}$$

$$a^5 d^5 q^2 r^2 \left(\frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-b c + a d}\right] \right)}{(b c - a d)^5} \right) +$$

$$\frac{1}{(b c - a d)^4} 2 b^4 c^5 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\left(\frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-b c + a d}\right] \right)}{(b c - a d)^5} \right) -$$

$$\frac{1}{(b c - a d)^4} 8 a b^3 c^4 d p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\left(\frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-b c + a d}\right] \right)}{(b c - a d)^5} \right) +$$

$$\frac{1}{(b c - a d)^4} 12 a^2 b^2 c^3 d^2 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])$$

$$\left(\frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-b c + a d}\right] \right)}{(b c - a d)^5} \right) -$$

$$\begin{aligned}
& \frac{1}{(bc-ad)^4} 8a^3 b c^2 d^3 p r^2 (-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q]) \\
& \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\
& \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \\
& \frac{1}{(bc-ad)^4} 2a^4 c d^4 p r^2 (-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q]) \\
& \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\
& \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \\
& \frac{1}{(bc-ad)^4} 2b^4 c^5 p r \left(-p r \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p (c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]} \right) + \right. \\
& \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]}} \right] \right) \\
& \left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\
& \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) - \\
& \frac{1}{(bc-ad)^4} 8a b^3 c^4 d p r \left(-p r \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q]) - \right. \\
& \left. \operatorname{Log}[f(a+bx)^p (c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]} \right) + \right. \\
& \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p (c+dx)^q])}{\operatorname{Log}[f(a+bx)^p (c+dx)^q]}} \right] \right)
\end{aligned}$$

$$\left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\ \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \\ \frac{1}{(bc-ad)^4} 12a^2b^2c^3d^2pr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\ \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\ \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right)$$

$$\left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\ \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) - \\ \frac{1}{(bc-ad)^4} 8a^3bc^2d^3pr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\ \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) + \\ \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]}} \right] \right)$$

$$\left(\frac{d^4 \operatorname{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\operatorname{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\operatorname{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\ \left. \frac{1+4\operatorname{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \\ \frac{1}{(bc-ad)^4} 2a^4c^4d^4pr \left(-pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q]) - \right. \\ \left. \operatorname{Log}[f(a+bx)^p(c+dx)^q] \left(r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f(a+bx)^p(c+dx)^q])}{\operatorname{Log}[f(a+bx)^p(c+dx)^q]} \right) \right) +$$

$$\begin{aligned} & \text{Log}\left[e^{e^r \left(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p (c+dx)^q]\right)} (a+bx)^{pr} (f(a+bx)^p (c+dx)^q)^r - \frac{r \left(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p (c+dx)^q]\right)}{\text{Log}[f(a+bx)^p (c+dx)^q]}\right] \\ & \left(\frac{d^4 \text{Log}[a+bx]^2}{2(bc-ad)^5} + \frac{bd^3(1+\text{Log}[a+bx])}{(bc-ad)^4(ab+b^2x)} - \frac{d^2(1+2\text{Log}[a+bx])}{4(bc-ad)^3(a+bx)^2} + \frac{d(1+3\text{Log}[a+bx])}{9(bc-ad)^2(a+bx)^3} + \right. \\ & \left. \frac{1+4\text{Log}[a+bx]}{16(-bc+ad)(a+bx)^4} - \frac{d^4 \left(\text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) \end{aligned}$$

Problem 40: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e \left(f(a+bx)^p (c+dx)^q\right)^r\right]^2}{(g+hx)^2} dx$$

Optimal (type 4, 832 leaves, 31 steps):

$$\begin{aligned} & \frac{2bpqr^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c+dx]}{h(bg-ah)} + \frac{2dpqr^2 \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{h(dg-ch)} - \\ & \frac{2bpr \text{Log}[a+bx] (pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}[e(f(a+bx)^p (c+dx)^q)^r])}{h(bg-ah)} - \\ & \frac{2dqr \text{Log}[c+dx] (pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}[e(f(a+bx)^p (c+dx)^q)^r])}{h(dg-ch)} - \\ & \frac{\text{Log}[e(f(a+bx)^p (c+dx)^q)^r]^2}{h(g+hx)} + \frac{2bpr (pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}[e(f(a+bx)^p (c+dx)^q)^r]) \text{Log}[g+hx]}{h(bg-ah)} + \\ & \frac{2dqr (pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}[e(f(a+bx)^p (c+dx)^q)^r]) \text{Log}[g+hx]}{h(dg-ch)} - \frac{2dpqr^2 \text{Log}[a+bx] \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right]}{h(dg-ch)} - \\ & \frac{2bpqr^2 \text{Log}[c+dx] \text{Log}\left[\frac{d(g+hx)}{dg-ch}\right]}{h(bg-ah)} - \frac{2bp^2r^2 \text{Log}[a+bx] \text{Log}\left[1 + \frac{bg-ah}{h(a+bx)}\right]}{h(bg-ah)} - \frac{2dq^2r^2 \text{Log}[c+dx] \text{Log}\left[1 + \frac{dg-ch}{h(c+dx)}\right]}{h(dg-ch)} + \\ & \frac{2bp^2r^2 \text{PolyLog}\left[2, -\frac{bg-ah}{h(a+bx)}\right]}{h(bg-ah)} + \frac{2dpqr^2 \text{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right]}{h(dg-ch)} - \frac{2dpqr^2 \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(dg-ch)} + \\ & \frac{2dq^2r^2 \text{PolyLog}\left[2, -\frac{dg-ch}{h(c+dx)}\right]}{h(dg-ch)} + \frac{2bpqr^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{h(bg-ah)} - \frac{2bpqr^2 \text{PolyLog}\left[2, -\frac{h(c+dx)}{dg-ch}\right]}{h(bg-ah)} \end{aligned}$$

Result (type 4, 2930 leaves):

1

$$\begin{aligned}
& h(-bg+ah)(-dg+ch)(g+hx) \\
& \left(-bdg^2p^2r^2 \operatorname{Log}[a+bx]^2 + bcghp^2r^2 \operatorname{Log}[a+bx]^2 - bdghp^2r^2x \operatorname{Log}[a+bx]^2 + bch^2p^2r^2x \operatorname{Log}[a+bx]^2 - 2bdg^2pqr^2 \operatorname{Log}[a+bx] \right. \\
& \quad \operatorname{Log}[c+dx] + 2adghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] - 2bdghpqr^2x \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] + 2adh^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] - \\
& \quad bdg^2q^2r^2 \operatorname{Log}[c+dx]^2 + adghq^2r^2 \operatorname{Log}[c+dx]^2 - bdghq^2r^2x \operatorname{Log}[c+dx]^2 + adh^2q^2r^2x \operatorname{Log}[c+dx]^2 + \\
& \quad 2bcghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - 2adghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] + 2bch^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - \\
& \quad 2adh^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - bcghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + adghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 - \\
& \quad bc h^2 p q r^2 x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + adh^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + 2bcghpqr^2 \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - \\
& \quad 2adghpqr^2 \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] + 2bch^2pqr^2x \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - \\
& \quad 2adh^2pqr^2x \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] + 2bcghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - \\
& \quad 2adghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] + 2bch^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - \\
& \quad 2adh^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - bcghpqr^2 \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right]^2 + adghpqr^2 \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right]^2 - \\
& \quad bc h^2 p q r^2 x \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right]^2 + adh^2pqr^2x \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right]^2 + 2bdg^2pr \operatorname{Log}[a+bx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] - \\
& \quad 2bcghpr \operatorname{Log}[a+bx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] + 2bdghprx \operatorname{Log}[a+bx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] - \\
& \quad 2bch^2prx \operatorname{Log}[a+bx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] + 2bdg^2qr \operatorname{Log}[c+dx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] - \\
& \quad 2adghqr \operatorname{Log}[c+dx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] + 2bdghqr x \operatorname{Log}[c+dx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] - \\
& \quad 2adh^2qr x \operatorname{Log}[c+dx] \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r] - bdg^2 \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]^2 + bcgh \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]^2 + \\
& \quad adgh \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]^2 - ach^2 \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]^2 - 2bdg^2pqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \\
& \quad 2adghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - 2bdghpqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + 2adh^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \\
& \quad 2bdg^2pqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - 2bcghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \\
& \quad 2bdghpqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - 2bch^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] -
\end{aligned}$$

$$\begin{aligned}
& 2 b d g^2 p r \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b c g h p r \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]- \\
& 2 b d g h p r x \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+2 b c h^2 p r x \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]+ \\
& 2 b d g^2 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 a d g h p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 b d g h p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]- \\
& 2 a d h^2 p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b d g^2 p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
& 2 b c g h p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b d g h p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
& 2 b c h^2 p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b d g^2 q r \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
& 2 a d g h q r \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]-2 b d g h q r x \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+ \\
& 2 a d h^2 q r x \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]+2 p(b c h p+a d h q-b d g(p+q)) r^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(a+b x)}{-b g+a h}\right]+ \\
& 2 q(b c h p+a d h q-b d g(p+q)) r^2(g+h x) \operatorname{PolyLog}\left[2, \frac{h(c+d x)}{-d g+c h}\right]+2 b c g h p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]- \\
& 2 a d g h p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]+2 b c h^2 p q r^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]-2 a d h^2 p q r^2 x \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]
\end{aligned}$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2}{(g+h x)^3} d x$$

Optimal (type 4, 1304 leaves, 43 steps):

$$\begin{aligned}
& - \frac{b d p q r^2 \operatorname{Log}[a + b x]}{h (b g - a h) (d g - c h)} + \frac{d p q r^2 \operatorname{Log}[a + b x]}{h (d g - c h) (g + h x)} - \frac{b p^2 r^2 (a + b x) \operatorname{Log}[a + b x]}{(b g - a h)^2 (g + h x)} - \\
& \frac{b d p q r^2 \operatorname{Log}[c + d x]}{h (b g - a h) (d g - c h)} + \frac{b p q r^2 \operatorname{Log}[c + d x]}{h (b g - a h) (g + h x)} - \frac{d q^2 r^2 (c + d x) \operatorname{Log}[c + d x]}{(d g - c h)^2 (g + h x)} + \frac{b^2 p q r^2 \operatorname{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \operatorname{Log}[c + d x]}{h (b g - a h)^2} + \\
& \frac{d^2 p q r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{h (d g - c h)^2} - \frac{b p r (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{h (b g - a h) (g + h x)} - \\
& \frac{d q r (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{h (d g - c h) (g + h x)} - \\
& \frac{b^2 p r \operatorname{Log}[a + b x] (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{h (b g - a h)^2} - \\
& \frac{d^2 q r \operatorname{Log}[c + d x] (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{h (d g - c h)^2} - \frac{\operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r]^2}{2 h (g + h x)^2} + \frac{b^2 p^2 r^2 \operatorname{Log}[g + h x]}{h (b g - a h)^2} + \\
& \frac{2 b d p q r^2 \operatorname{Log}[g + h x]}{h (b g - a h) (d g - c h)} + \frac{d^2 q^2 r^2 \operatorname{Log}[g + h x]}{h (d g - c h)^2} + \frac{b^2 p r (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r]) \operatorname{Log}[g + h x]}{h (b g - a h)^2} + \\
& \frac{d^2 q r (p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}[e (f (a + b x)^p (c + d x)^q)^r]) \operatorname{Log}[g + h x]}{h (d g - c h)^2} - \frac{d^2 p q r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right]}{h (d g - c h)^2} - \\
& \frac{b^2 p q r^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right]}{h (b g - a h)^2} - \frac{b^2 p^2 r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[1 + \frac{bg-ah}{h(a+bx)}\right]}{h (b g - a h)^2} - \frac{d^2 q^2 r^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[1 + \frac{dg-ch}{h(c+dx)}\right]}{h (d g - c h)^2} + \\
& \frac{b^2 p^2 r^2 \operatorname{PolyLog}\left[2, -\frac{bg-ah}{h(a+bx)}\right]}{h (b g - a h)^2} + \frac{d^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right]}{h (d g - c h)^2} - \frac{d^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h (d g - c h)^2} + \\
& \frac{d^2 q^2 r^2 \operatorname{PolyLog}\left[2, -\frac{dg-ch}{h(c+dx)}\right]}{h (d g - c h)^2} + \frac{b^2 p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{h (b g - a h)^2} - \frac{b^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{h(c+dx)}{dg-ch}\right]}{h (b g - a h)^2}
\end{aligned}$$

Result (type 4, 15976 leaves):

$$\begin{aligned}
& - \frac{1}{2 h (g + h x)^2} \left(-p r \operatorname{Log}[a + b x] - \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left(r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) + \right. \\
& \left. \operatorname{Log}\left[e e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{h} p r \left(-p r \operatorname{Log}[a + b x] - \operatorname{Log}[f(a + b x)^p (c + d x)^q] \left(r - \frac{r(-q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}{\operatorname{Log}[f(a + b x)^p (c + d x)^q]} \right) + \right. \\
& \quad \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}} (a + b x)^{p r} (f(a + b x)^p (c + d x)^q)^{r - \frac{r(-q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}{\operatorname{Log}[f(a + b x)^p (c + d x)^q]}} \right] \right) \\
& \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)} - \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)} \right) \operatorname{Log}[a + b x] - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a + b x)}{-b g + a h} \right]}{(-b g + a h)^2} \right) + \\
& \frac{1}{h} q r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q]) \\
& \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} - \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} \right) \operatorname{Log}[c + d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c + d x)}{-d g + c h} \right]}{(-d g + c h)^2} \right) + \\
& \frac{1}{h} q r \left(-p r \operatorname{Log}[a + b x] - r(-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q]) - \right. \\
& \quad \left. \operatorname{Log}[f(a + b x)^p (c + d x)^q] \left(r - \frac{r(-q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}{\operatorname{Log}[f(a + b x)^p (c + d x)^q]} \right) + \right. \\
& \quad \left. \operatorname{Log}\left[e^{e^{r(-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}} (a + b x)^{p r} (f(a + b x)^p (c + d x)^q)^{r - \frac{r(-q \operatorname{Log}[c + d x] + \operatorname{Log}[f(a + b x)^p (c + d x)^q])}{\operatorname{Log}[f(a + b x)^p (c + d x)^q]}} \right] \right) \\
& \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} - \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} \right) \operatorname{Log}[c + d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c + d x)}{-d g + c h} \right]}{(-d g + c h)^2} \right) + \\
& \frac{1}{h} p^2 r^2 \left(-\frac{1}{2} \left(\frac{b^2 h^2 (a + b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)^2} + \frac{2 b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)} \right) \operatorname{Log}[a + b x]^2 + \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a + b x)}{-b g + a h} \right]}{(-b g + a h)^2} + \right. \\
& \quad \left. \operatorname{Log}[a + b x] \left(\frac{b^2 h (a + b x)}{(-b g + a h)^3 \left(1 - \frac{h(a + b x)}{-b g + a h} \right)} - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a + b x)}{-b g + a h} \right]}{(-b g + a h)^2} \right) - \frac{b^2 \operatorname{PolyLog}\left[2, \frac{h(a + b x)}{-b g + a h} \right]}{(-b g + a h)^2} \right) + \\
& \frac{1}{h} q^2 r^2 \left(-\frac{1}{2} \left(\frac{d^2 h^2 (c + d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)^2} + \frac{2 d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} \right) \operatorname{Log}[c + d x]^2 + \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c + d x)}{-d g + c h} \right]}{(-d g + c h)^2} + \right. \\
& \quad \left. \operatorname{Log}[c + d x] \left(\frac{d^2 h (c + d x)}{(-d g + c h)^3 \left(1 - \frac{h(c + d x)}{-d g + c h} \right)} - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c + d x)}{-d g + c h} \right]}{(-d g + c h)^2} \right) - \frac{d^2 \operatorname{PolyLog}\left[2, \frac{h(c + d x)}{-d g + c h} \right]}{(-d g + c h)^2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{g^2} p q r^2 \left(\frac{1}{h} 2 \left(\text{Log}[a + b x] \text{Log}[c + d x] \text{Log}\left[\frac{b(g + h x)}{b g - a h}\right] + \frac{1}{2} \text{Log}\left[\frac{h(c + d x)}{-d g + c h}\right] \left(-2 \text{Log}[a + b x] + \text{Log}\left[\frac{h(c + d x)}{-d g + c h}\right] \right) \right. \right. \\
& \left. \left(\text{Log}\left[\frac{b(g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{d(g + h x)}{-d g + c h}\right] \right) + \text{Log}\left[\frac{h(c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \left(-\text{Log}\left[\frac{b(g + h x)}{b g - a h}\right] + \text{Log}\left[-\frac{d(g + h x)}{-d g + c h}\right] \right) \right. \\
& \left. \frac{1}{2} \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right]^2 \left(\text{Log}\left[\frac{-b c + a d}{d(a + b x)}\right] + \text{Log}\left[\frac{b(g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{(-b c + a d)(g + h x)}{(-d g + c h)(a + b x)}\right] \right) + \right. \\
& \left. \left(\text{Log}[c + d x] - \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a + b x)}{b g - a h}\right] + \left(\text{Log}[a + b x] + \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \right) \right. \\
& \left. \text{PolyLog}\left[2, \frac{h(c + d x)}{-d g + c h}\right] + \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \left(\text{PolyLog}\left[2, \frac{b(c + d x)}{d(a + b x)}\right] - \text{PolyLog}\left[2, -\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \right) \right. \\
& \left. \text{PolyLog}\left[3, -\frac{h(a + b x)}{b g - a h}\right] - \text{PolyLog}\left[3, \frac{h(c + d x)}{-d g + c h}\right] - \text{PolyLog}\left[3, \frac{b(c + d x)}{d(a + b x)}\right] + \text{PolyLog}\left[3, -\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] \right) + \\
& h^2 \left(\frac{1}{h} \left(\left(\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b(g + h x)} - \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)^2} - \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)} \right) \text{Log}[a + b x] \text{Log}[c + d x] - \right. \\
& \frac{1}{(b g - a h)(c + d x)} 2(-d g + c h)(a + b x) \left(\frac{c(b g - a h)(c + d x)}{(-d g + c h)^2(a + b x)} + \frac{a(c + d x)}{(-d g + c h)(a + b x)} \right) \left(\frac{(b g - a h) \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)} + \right. \\
& \left. \frac{(-d g + c h)(a + b x) \left(-\frac{(-b c + a d) x}{(-d g + c h)(a + b x)} + \frac{c(-b c + a d)(g + h x)}{(-d g + c h)^2(a + b x)} \right)}{(-b c + a d)(g + h x)} \right) \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] + \left(-\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b(g + h x)} + \right. \\
& \left. \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)^2} + \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)} - \frac{(-d g + c h) \left(\frac{2 c d x}{(-d g + c h)^2} - \frac{2 c^2 d (g + h x)}{(-d g + c h)^3} \right)}{d(g + h x)} + \frac{(-d g + c h) x \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d(g + h x)^2} - \right. \\
& \left. \frac{c \left(-\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d(g + h x)} \right) \text{Log}\left[\frac{h(c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h)(c + d x)}{(-d g + c h)(a + b x)}\right] + \frac{1}{2} \left(\frac{(b g - a h) \left(\frac{2 a b x}{(b g - a h)^2} + \frac{2 a^2 b (g + h x)}{(b g - a h)^3} \right)}{b(g + h x)} - \right. \\
& \left. \frac{(b g - a h) x \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)^2} - \frac{a \left(\frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b(g + h x)} + \frac{(-d g + c h)(a + b x) \left(\frac{2 c(-b c + a d) x}{(-d g + c h)^2(a + b x)} - \frac{2 c^2(-b c + a d)(g + h x)}{(-d g + c h)^3(a + b x)} \right)}{(-b c + a d)(g + h x)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{(-dg+ch) \times (a+bx) \left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right) + \frac{c(a+bx) \left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right)}{(-bc+ad)(g+hx)^2} \\
& \text{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]^2 + 2 \left(-\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} - \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \\
& \left(-\frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{Log} \left[\frac{h(c+dx)}{-dg+ch} \right] + \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)h(c+dx)} \right) + \\
& \frac{1}{h(c+dx)} (-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \right. \\
& \left. \left(-2 \text{Log}[a+bx] + \text{Log} \left[\frac{h(c+dx)}{-dg+ch} \right] \right) \right) + \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\text{Log} \left[\frac{b(g+hx)}{bg-ah} \right] - \text{Log} \left[-\frac{d(g+hx)}{-dg+ch} \right] \right)}{h(c+dx)} + \\
& \frac{1}{2} \text{Log} \left[\frac{h(c+dx)}{-dg+ch} \right] \left(\frac{2(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right)}{h(c+dx)} + \right. \\
& \left(\frac{(bg-ah) \left(\frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} - \frac{(bg-ah)x \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)^2} - \frac{a \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(\frac{2cdx}{(-dg+ch)^2} - \frac{2c^2d(g+hx)}{(-dg+ch)^3} \right)}{d(g+hx)} \right. \\
& \left. \frac{(-dg+ch)x \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right) + \frac{c \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)^2} \right) \left(-2 \text{Log}[a+bx] + \text{Log} \left[\frac{h(c+dx)}{-dg+ch} \right] \right) + \\
& \left(\frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right)}{h(c+dx)} + \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h(c+dx)} - \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2(c+dx)} \right) \\
& \left. \left(\text{Log} \left[\frac{b(g+hx)}{bg-ah} \right] - \text{Log} \left[-\frac{d(g+hx)}{-dg+ch} \right] \right) \right) + \frac{1}{2} \left(\frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right)}{h(c+dx)} + \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h(c+dx)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2(c+dx)} \right) \left(-2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch} \right] \right) \left(\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah} \right] - \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch} \right] \right) + \\
& \left(-\frac{2(-dg+ch)^2(a+bx) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{h(bg-ah)(c+dx)^2} + \right. \\
& \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} - \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch} \right] + \\
& \left(\frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right)}{h(c+dx)} + \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h(c+dx)} - \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h^2(c+dx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \Big) \\
& \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah} \right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch} \right] \right) + \frac{1}{2} \left(\frac{2(-dg+ch)^2(a+bx)^2 \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)^2}{(bg-ah)^2(c+dx)^2} - \right. \\
& \frac{2(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \\
& \frac{2c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \\
& \left. \frac{2a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)^2(c+dx)} \right) \\
& \left(\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)} \right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah} \right] - \operatorname{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)} \right] \right) + \frac{(bg-ah)^2 \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right)^2 \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)^2} + \\
& \frac{2(-dg+ch) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(c+dx)} + \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \right) \\
& \left(\frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\frac{ah(a+bx)}{(bg-ah)^2} + \frac{a+bx}{bg-ah} \right)}{h(a+bx) \left(1 + \frac{h(a+bx)}{bg-ah} \right)} + \frac{(bg-ah) \left(-\frac{2a^2h(a+bx)}{(bg-ah)^3} - \frac{2a(a+bx)}{(bg-ah)^2} \right) \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{a \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{Log} \left[1 + \frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)} \right) + \\
& \frac{(-dg+ch)^2 \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)^2 \operatorname{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h^2(c+dx)^2} + \frac{1}{h(bg-ah)(c+dx)^2} 2(-dg+ch)^2(a+bx) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \\
& \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right] + \left(\operatorname{Log}[a+bx] + \operatorname{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \right) \\
& \left(-\frac{(-dg+ch) \left(\frac{ch(c+dx)}{(-dg+ch)^2} - \frac{c+dx}{-dg+ch} \right) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right)}{h(c+dx) \left(1 - \frac{h(c+dx)}{-dg+ch} \right)} - \frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right) \operatorname{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} - \right. \\
& \left. \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h(c+dx)} + \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{Log} \left[1 - \frac{h(c+dx)}{-dg+ch} \right]}{h^2(c+dx)} \right) + \\
& \frac{(-dg+ch)^2(a+bx)^2 \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)^2 \operatorname{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)^2(c+dx)^2} + \operatorname{Log} \left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \\
& \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} - \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx) \left(1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right)} - \right. \\
& \left. \frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \operatorname{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log} \left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]}{(bg-ah)^2(c+dx)} \right) + \\
& \frac{(bg-ah) \left(-\frac{2a^2h(a+bx)}{(bg-ah)^3} - \frac{2a(a+bx)}{(bg-ah)^2} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \frac{a \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h(a+bx)} - \\
& \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog} \left[2, -\frac{h(a+bx)}{bg-ah} \right]}{h^2(a+bx)} + \left(\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) + a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} + \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] - \\
& \frac{(-dg+ch) \left(\frac{2c^2h(c+dx)}{(-dg+ch)^3} - \frac{2c(c+dx)}{(-dg+ch)^2} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{c \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} + \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h^2(c+dx)} + \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) - a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \\
& \left(-\frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right)}{(bg-ah)(c+dx)} - \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} - \right. \\
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)^2(c+dx)} \right) \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \frac{(-dg+ch)(a+bx) \left(-\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)(c+dx)} - \\
& \frac{c(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)(c+dx)} - \\
& \left. \frac{a(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)^2(c+dx)} \right) - \\
& \frac{1}{h^2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right) \text{Log}[a+bx] \text{Log}[c+dx]}{b(g+hx)} + \frac{1}{2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \right) \\
& \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(-\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} - \frac{(-dg+ch)\left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2}\right)}{d(g+hx)} \right) \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{1}{2} \left(\frac{(bg-ah)\left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2}\right)}{b(g+hx)} + \frac{(-dg+ch)(a+bx)\left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)}\right)}{(-bc+ad)(g+hx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 + \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right)}{2h(c+dx)} + \frac{1}{2h(c+dx)}(-dg+ch) \\
& \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(-2\operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]\right) \left(\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right) - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right) + \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right]\right)}{h(c+dx)} - \frac{1}{(bg-ah)(c+dx)}(-dg+ch) \\
& (a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right]\right) + \\
& \frac{(bg-ah)\left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah}\right) \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \left(\operatorname{Log}[a+bx] + \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \\
& \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \frac{(bg-ah)\left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah}\right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \\
& \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{(bg-ah)(c+dx)} - \\
& \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)}\right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{(bg-ah)(c+dx)}
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{(bg-ah)(c+dx)}(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& - \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \left(-\frac{(-dg+ch)(a+bx)}{(bg-ah)(c+dx)} \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \frac{1}{h^3} 2 \left(\text{Log}[a+bx] \text{Log}[c+dx] \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \right) \\
& \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \\
& \frac{1}{2} \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \left. \text{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \text{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \text{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& 4h \left(\frac{1}{h} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right) \text{Log}[a+bx] \text{Log}[c+dx]}{b(g+hx)} + \frac{1}{2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \right) \right) \\
& \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \text{Log}[a+bx] + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) + \\
& \left(-\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} - \frac{(-dg+ch) \left(-\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{1}{2} \left(\frac{(bg-ah) \left(\frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \frac{(-dg+ch)(a+bx) \left(-\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right)}{(-bc+ad)(g+hx)} \right) \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 + \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right)}{2h(c+dx)} + \frac{1}{2h(c+dx)}
\end{aligned}$$

$$\begin{aligned}
& (-dg + ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(-2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \left(\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) - \\
& \frac{1}{(bg-ah)(c+dx)} (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \\
& \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right)}{h(c+dx)} - \\
& \frac{1}{(bg-ah)(c+dx)} (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \\
& \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left(\operatorname{Log}[c+dx] - \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \left(\operatorname{Log}[a+bx] + \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] + \\
& \frac{(bg-ah) \left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{(bg-ah)(c+dx)} - \\
& \frac{(-dg+ch) \left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \\
& \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{(bg-ah)(c+dx)} - \frac{1}{(bg-ah)(c+dx)} \\
& (-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left(\operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \operatorname{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \frac{(-dg+ch)(a+bx) \left(\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]}{(bg-ah)(c+dx)} - \\
& \frac{1}{h^2} \left(\operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \left(-2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \text{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(-\text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \text{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \\
& \frac{1}{2} \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \left(\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \text{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
& \left(\text{Log}[c+dx] - \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \left(\text{Log}[a+bx] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \\
& \left. \text{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \text{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \text{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right)
\end{aligned}$$

Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right]^2}{(g+hx)^4} dx$$

Optimal (type 4, 1957 leaves, 57 steps):

$$\begin{aligned}
& -\frac{b^2 p^2 r^2}{3h(bg-ah)^2(g+hx)} - \frac{2bdpq r^2}{3h(bg-ah)(dg-ch)(g+hx)} - \frac{d^2 q^2 r^2}{3h(dg-ch)^2(g+hx)} - \frac{b^3 p^2 r^2 \text{Log}[a+bx]}{3h(bg-ah)^3} - \\
& \frac{2bd^2 p q r^2 \text{Log}[a+bx]}{3h(bg-ah)(dg-ch)^2} - \frac{b^2 d p q r^2 \text{Log}[a+bx]}{3h(bg-ah)^2(dg-ch)} + \frac{bp^2 r^2 \text{Log}[a+bx]}{3h(bg-ah)(g+hx)^2} + \frac{dpq r^2 \text{Log}[a+bx]}{3h(dg-ch)(g+hx)^2} + \frac{2d^2 p q r^2 \text{Log}[a+bx]}{3h(dg-ch)^2(g+hx)} - \\
& \frac{2b^2 p^2 r^2 (a+bx) \text{Log}[a+bx]}{3(bg-ah)^3(g+hx)} - \frac{bd^2 p q r^2 \text{Log}[c+dx]}{3h(bg-ah)(dg-ch)^2} - \frac{2b^2 d p q r^2 \text{Log}[c+dx]}{3h(bg-ah)^2(dg-ch)} - \frac{d^3 q^2 r^2 \text{Log}[c+dx]}{3h(dg-ch)^3} + \frac{bpq r^2 \text{Log}[c+dx]}{3h(bg-ah)(g+hx)^2} + \\
& \frac{dq^2 r^2 \text{Log}[c+dx]}{3h(dg-ch)(g+hx)^2} + \frac{2b^2 p q r^2 \text{Log}[c+dx]}{3h(bg-ah)^2(g+hx)} - \frac{2d^2 q^2 r^2 (c+dx) \text{Log}[c+dx]}{3(dg-ch)^3(g+hx)} + \frac{2b^3 p q r^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c+dx]}{3h(bg-ah)^3} + \\
& \frac{2d^3 p q r^2 \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{3h(dg-ch)^3} - \frac{bpr(pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right])}{3h(bg-ah)(g+hx)^2} - \\
& \frac{dqr(pr \text{Log}[a+bx] + qr \text{Log}[c+dx] - \text{Log}\left[e\left(f(a+bx)^p(c+dx)^q\right)^r\right])}{3h(dg-ch)(g+hx)^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{2 b^2 p r (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right])}{3 h(b g-a h)^2(g+h x)} - \\
& \frac{2 d^2 q r (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right])}{3 h(d g-c h)^2(g+h x)} - \\
& \frac{2 b^3 p r \operatorname{Log}[a+b x] (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right])}{3 h(b g-a h)^3} - \\
& \frac{2 d^3 q r \operatorname{Log}[c+d x] (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right])}{3 h(d g-c h)^3} - \\
& \frac{\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2}{3 h(g+h x)^3} + \frac{b^3 p^2 r^2 \operatorname{Log}[g+h x]}{h(b g-a h)^3} + \frac{b d^2 p q r^2 \operatorname{Log}[g+h x]}{h(b g-a h)(d g-c h)^2} + \frac{b^2 d p q r^2 \operatorname{Log}[g+h x]}{h(b g-a h)^2(d g-c h)} + \\
& \frac{d^3 q^2 r^2 \operatorname{Log}[g+h x]}{h(d g-c h)^3} + \frac{2 b^3 p r (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]) \operatorname{Log}[g+h x]}{3 h(b g-a h)^3} + \\
& \frac{2 d^3 q r (p r \operatorname{Log}[a+b x]+q r \operatorname{Log}[c+d x]-\operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]) \operatorname{Log}[g+h x]}{3 h(d g-c h)^3} - \frac{2 d^3 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]}{3 h(d g-c h)^3} - \\
& \frac{2 b^3 p q r^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]}{3 h(b g-a h)^3} - \frac{2 b^3 p^2 r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[1+\frac{b g-a h}{h(a+b x)}\right]}{3 h(b g-a h)^3} - \frac{2 d^3 q^2 r^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1+\frac{d g-c h}{h(c+d x)}\right]}{3 h(d g-c h)^3} + \\
& \frac{2 b^3 p^2 r^2 \operatorname{PolyLog}\left[2,-\frac{b g-a h}{h(a+b x)}\right]}{3 h(b g-a h)^3} + \frac{2 d^3 p q r^2 \operatorname{PolyLog}\left[2,-\frac{d(a+b x)}{b c-a d}\right]}{3 h(d g-c h)^3} - \frac{2 d^3 p q r^2 \operatorname{PolyLog}\left[2,-\frac{h(a+b x)}{b g-a h}\right]}{3 h(d g-c h)^3} + \\
& \frac{2 d^3 q^2 r^2 \operatorname{PolyLog}\left[2,-\frac{d g-c h}{h(c+d x)}\right]}{3 h(d g-c h)^3} + \frac{2 b^3 p q r^2 \operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]}{3 h(b g-a h)^3} - \frac{2 b^3 p q r^2 \operatorname{PolyLog}\left[2,-\frac{h(c+d x)}{d g-c h}\right]}{3 h(b g-a h)^3}
\end{aligned}$$

Result (type 4, 47 110 leaves): Display of huge result suppressed!

Problem 44: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b \operatorname{Log}\left[\frac{\sqrt{1-c x}}{\sqrt{1+c x}}\right]\right)^3}{1-c^2 x^2} dx$$

Optimal (type 3, 37 leaves, 5 steps):

$$\frac{\left(a + b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^4}{4bc}$$

Result (type 3, 117 leaves):

$$\frac{\operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] \left(4a^3 + 6a^2 b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] + 4ab^2 \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]^2 + b^3 \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]^3\right)}{4c}$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2}{1 - c^2 x^2} dx$$

Optimal (type 3, 37 leaves, 5 steps):

$$\frac{\left(a + b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3}{3bc}$$

Result (type 3, 86 leaves):

$$\frac{\operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] \left(3a^2 + 3ab \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] + b^2 \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]^2\right)}{3c}$$

Problem 51: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e \left(f(a+bx)^p (c+dx)^q\right)^r\right] \left(s + t \operatorname{Log}\left[i(g+hx)^n\right]\right)^2}{gk + hkx} dx$$

Optimal (type 4, 410 leaves, 11 steps):

$$\begin{aligned}
& - \frac{p r \operatorname{Log}\left[-\frac{h(a+bx)}{bg-ah}\right] (s+t \operatorname{Log}[i(g+hx)^n])^3}{3 h k n t} - \frac{q r \operatorname{Log}\left[-\frac{h(c+dx)}{dg-ch}\right] (s+t \operatorname{Log}[i(g+hx)^n])^3}{3 h k n t} + \\
& \frac{\operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right] (s+t \operatorname{Log}[i(g+hx)^n])^3}{3 h k n t} - \frac{p r (s+t \operatorname{Log}[i(g+hx)^n])^2 \operatorname{PolyLog}\left[2, \frac{b(g+hx)}{bg-ah}\right]}{h k} - \\
& \frac{q r (s+t \operatorname{Log}[i(g+hx)^n])^2 \operatorname{PolyLog}\left[2, \frac{d(g+hx)}{dg-ch}\right]}{h k} + \frac{2 n p r t (s+t \operatorname{Log}[i(g+hx)^n]) \operatorname{PolyLog}\left[3, \frac{b(g+hx)}{bg-ah}\right]}{h k} + \\
& \frac{2 n q r t (s+t \operatorname{Log}[i(g+hx)^n]) \operatorname{PolyLog}\left[3, \frac{d(g+hx)}{dg-ch}\right]}{h k} - \frac{2 n^2 p r t^2 \operatorname{PolyLog}\left[4, \frac{b(g+hx)}{bg-ah}\right]}{h k} - \frac{2 n^2 q r t^2 \operatorname{PolyLog}\left[4, \frac{d(g+hx)}{dg-ch}\right]}{h k}
\end{aligned}$$

Result (type 4, 22 595 leaves): Display of huge result suppressed!

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[i(j(hx)^t)^u]^3 \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]}{x} dx$$

Optimal (type 4, 328 leaves, 13 steps):

$$\begin{aligned}
& - \frac{p r \operatorname{Log}[i(j(hx)^t)^u]^4 \operatorname{Log}\left[1 + \frac{bx}{a}\right]}{4 t u} + \frac{\operatorname{Log}[i(j(hx)^t)^u]^4 \operatorname{Log}[e(f(a+bx)^p(c+dx)^q)^r]}{4 t u} - \frac{q r \operatorname{Log}[i(j(hx)^t)^u]^4 \operatorname{Log}\left[1 + \frac{dx}{c}\right]}{4 t u} - \\
& p r \operatorname{Log}[i(j(hx)^t)^u]^3 \operatorname{PolyLog}\left[2, -\frac{bx}{a}\right] - q r \operatorname{Log}[i(j(hx)^t)^u]^3 \operatorname{PolyLog}\left[2, -\frac{dx}{c}\right] + 3 p r t u \operatorname{Log}[i(j(hx)^t)^u]^2 \operatorname{PolyLog}\left[3, -\frac{bx}{a}\right] + \\
& 3 q r t u \operatorname{Log}[i(j(hx)^t)^u]^2 \operatorname{PolyLog}\left[3, -\frac{dx}{c}\right] - 6 p r t^2 u^2 \operatorname{Log}[i(j(hx)^t)^u] \operatorname{PolyLog}\left[4, -\frac{bx}{a}\right] - \\
& 6 q r t^2 u^2 \operatorname{Log}[i(j(hx)^t)^u] \operatorname{PolyLog}\left[4, -\frac{dx}{c}\right] + 6 p r t^3 u^3 \operatorname{PolyLog}\left[5, -\frac{bx}{a}\right] + 6 q r t^3 u^3 \operatorname{PolyLog}\left[5, -\frac{dx}{c}\right]
\end{aligned}$$

Result (type 4, 1241 leaves):

$$\begin{aligned}
& p r t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}[a+b x] - p r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}[a+b x] - 3 p r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + \\
& 3 p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + 3 p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[a+b x] - \\
& 3 p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[a+b x] - p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[a+b x] + p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[a+b x] + \\
& \frac{1}{4} p r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[1+\frac{b x}{a}\right] - p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right] + \frac{3}{2} p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - \\
& p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{b x}{a}\right] + q r t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}[c+d x] - q r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}[c+d x] - \\
& 3 q r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] + 3 q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] + \\
& 3 q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] - 3 q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] - \\
& q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[c+d x] + q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[c+d x] - t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{3}{4} t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + 3 t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
& 2 t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - 3 t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{3}{2} t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{1}{4} q r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[1+\frac{d x}{c}\right] - q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right] + \frac{3}{2} q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right] - \\
& q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{d x}{c}\right] - p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + \\
& 3 p r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + 3 q r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right] - 6 p r t^2 u^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[4,-\frac{b x}{a}\right] - \\
& 6 q r t^2 u^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[4,-\frac{d x}{c}\right] + 6 p r t^3 u^3 \operatorname{PolyLog}\left[5,-\frac{b x}{a}\right] + 6 q r t^3 u^3 \operatorname{PolyLog}\left[5,-\frac{d x}{c}\right]
\end{aligned}$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{x} dx$$

Optimal (type 4, 262 leaves, 11 steps):

$$\begin{aligned}
& -\frac{p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{b x}{a}\right]}{3 t u} + \frac{\operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{3 t u} - \frac{q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{d x}{c}\right]}{3 t u} - \\
& p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + 2 p r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + \\
& 2 q r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right] - 2 p r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{b x}{a}\right] - 2 q r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{d x}{c}\right]
\end{aligned}$$

Result (type 4, 839 leaves):

$$\begin{aligned}
& -p r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}[a+b x] + p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}[a+b x] + 2 p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] - \\
& 2 p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] - p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[a+b x] + \\
& p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - \frac{1}{3} p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[1+\frac{b x}{a}\right] + p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right] - \\
& p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - q r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}[c+d x] + q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}[c+d x] + \\
& 2 q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] - 2 q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] - \\
& q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] + q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] + t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
& \frac{2}{3} t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - 2 t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
& \frac{1}{3} q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[1+\frac{d x}{c}\right] + q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right] - q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right] - \\
& p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + 2 p r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + \\
& 2 q r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right] - 2 p r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{b x}{a}\right] - 2 q r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{d x}{c}\right]
\end{aligned}$$

Problem 58: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{x} dx$$

Optimal (type 4, 194 leaves, 9 steps):

$$\begin{aligned}
& -\frac{p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right]}{2 t u} + \frac{\operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{2 t u} - \frac{q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right]}{2 t u} - \\
& p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + p r t u \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + q r t u \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right]
\end{aligned}$$

Result (type 4, 451 leaves):

$$\begin{aligned}
& p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}[a+b x] - p r t u \operatorname{Log}[h x]^2 \operatorname{Log}[a+b x] - p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + \\
& p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + \frac{1}{2} p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right] + \\
& q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}[c+d x] - q r t u \operatorname{Log}[h x]^2 \operatorname{Log}[c+d x] - q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] + \\
& q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] - t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \frac{1}{2} t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \frac{1}{2} q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right] - q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right] - \\
& p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + p r t u \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + q r t u \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right]
\end{aligned}$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{Log}[h(f+g x)^m]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 620 leaves, 14 steps):

$$\begin{aligned}
& \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{4(b c-a d) n} + \frac{\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}[h(f+g x)^m]}{4(b c-a d) n} - \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{4(b c-a d) n} + \\
& \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{PolyLog}\left[2,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} - \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{PolyLog}\left[2,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} - \frac{3 m n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 \operatorname{PolyLog}\left[3,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} + \\
& \frac{3 m n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 \operatorname{PolyLog}\left[3,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} + \frac{6 m n^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{PolyLog}\left[4,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} - \\
& \frac{6 m n^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{PolyLog}\left[4,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} - \frac{6 m n^3 \operatorname{PolyLog}\left[5,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} + \frac{6 m n^3 \operatorname{PolyLog}\left[5,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d}
\end{aligned}$$

Result (type 4, 31404 leaves): Display of huge result suppressed!

Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 \operatorname{Log}[h(f+g x)^m]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 496 leaves, 12 steps):

$$\frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{3(bc-ad)n} + \frac{\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \operatorname{Log}[h(f+gx)^m]}{3(bc-ad)n} - \frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{3(bc-ad)n} +$$

$$\frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} - \frac{2mn \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} +$$

$$\frac{2mn \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{PolyLog}\left[3, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} + \frac{2mn^2 \operatorname{PolyLog}\left[4, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \frac{2mn^2 \operatorname{PolyLog}\left[4, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad}$$

Result (type 4, 25557 leaves): Display of huge result suppressed!

Problem 69: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{Log}[h(f+gx)^m]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 371 leaves, 10 steps):

$$\frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \operatorname{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{2(bc-ad)n} + \frac{\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \operatorname{Log}[h(f+gx)^m]}{2(bc-ad)n} - \frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \operatorname{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{2(bc-ad)n} +$$

$$\frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \frac{m \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \operatorname{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} - \frac{mn \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} + \frac{mn \operatorname{PolyLog}\left[3, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad}$$

Result (type 4, 6704 leaves):

$$\frac{m \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] \left(n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right] + 2 \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right)\right) \operatorname{Log}[f+gx]}{2(bc-ad)} -$$

$$\frac{\operatorname{Log}[a+bx] \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \left(-m \operatorname{Log}[f+gx] + \operatorname{Log}[h(f+gx)^m]\right)}{-bc+ad} +$$

$$\frac{\left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \operatorname{Log}[c+dx] \left(-m \operatorname{Log}[f+gx] + \operatorname{Log}[h(f+gx)^m]\right)}{-bc+ad} +$$

$$\frac{1}{-bc+ad} b d g m \left(\operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]\right) \left(\frac{a^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^3 \left(-\frac{a}{b}+\frac{c}{d}\right) d \left(-\frac{a}{b}+\frac{f}{g}\right) g} + \frac{c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2b \left(-\frac{a}{b}+\frac{c}{d}\right) d^3 \left(-\frac{c}{d}+\frac{f}{g}\right) g}\right) +$$

$$\left(\frac{a^2 \operatorname{Log}[a+bx]}{b(bc-ad)(bf-ag)} + \frac{c^2 \operatorname{Log}[c+dx]}{d(bc-ad)(-df+cg)} + \frac{f^2 \operatorname{Log}[f+gx]}{g(bf-ag)(df-cg)}\right) \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right) -$$

$$\begin{aligned}
& \frac{c^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \text{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d^3 \left(-\frac{c}{d} + \frac{f}{g}\right) g} - \frac{f^2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^3} - \\
& \left. \frac{a^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] \right)}{b^3 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \frac{f^2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^3} \right) + \\
& \frac{1}{-b c + a d} b c g m \left(\text{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-\frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \frac{c \text{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d^2 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \left. \left((a (d f - c g) \text{Log}[a + b x] + (-b c f + a c g) \text{Log}[c + d x] + (b c - a d) f \text{Log}[f + g x]) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) / \right. \\
& \left. (b c - a d) (b f - a g) (-d f + c g) + \frac{c \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \text{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d^2 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \left. \frac{f \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^2} + \frac{a \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] \right)}{b^2 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \right. \\
& \left. \frac{f \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^2} \right) + \\
& \frac{1}{-b c + a d} a d g m \left(\text{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(-\frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \frac{c \text{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d^2 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \left. \left((a (d f - c g) \text{Log}[a + b x] + (-b c f + a c g) \text{Log}[c + d x] + (b c - a d) f \text{Log}[f + g x]) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) / \right)
\end{aligned}$$

$$\begin{aligned}
& \left((bc - ad)(bf - ag)(-df + cg) + \frac{c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[1 - \frac{d \left(\frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right] + \operatorname{PolyLog} \left[2, \frac{d \left(\frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d} \right) d^2 \left(-\frac{c}{d} + \frac{f}{g} \right) g} + \right. \\
& \frac{f \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] + \operatorname{PolyLog} \left[2, \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] \right)}{bd \left(\frac{c}{d} - \frac{f}{g} \right) \left(-\frac{a}{b} + \frac{f}{g} \right) g^2} + \frac{a \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b^2 \left(-\frac{a}{b} + \frac{c}{d} \right) d \left(-\frac{a}{b} + \frac{f}{g} \right) g} - \\
& \left. \frac{f \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] \right)}{bd \left(\frac{c}{d} - \frac{f}{g} \right) \left(-\frac{a}{b} + \frac{f}{g} \right) g^2} \right) - \\
& \frac{1}{-bc + ad} bcgn \left(-m \operatorname{Log}[f + gx] + \operatorname{Log}[h(f + gx)^m] \right) \left(-\frac{a \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2b^2 \left(-\frac{a}{b} + \frac{c}{d} \right) d \left(-\frac{a}{b} + \frac{f}{g} \right) g} - \frac{c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{2b \left(-\frac{a}{b} + \frac{c}{d} \right) d^2 \left(-\frac{c}{d} + \frac{f}{g} \right) g} + \right. \\
& \left. \left((a(df - cg) \operatorname{Log}[a + bx] + (-bcf + acg) \operatorname{Log}[c + dx] + (bc - ad) f \operatorname{Log}[f + gx]) \left(-\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{a}{c + dx} + \frac{bx}{c + dx} \right] \right) \right) / \right. \\
& \left((bc - ad)(bf - ag)(-df + cg) + \frac{c \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[1 - \frac{d \left(\frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right] + \operatorname{PolyLog} \left[2, \frac{d \left(\frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d} \right) d^2 \left(-\frac{c}{d} + \frac{f}{g} \right) g} + \right. \\
& \frac{f \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[1 - \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] + \operatorname{PolyLog} \left[2, \frac{g \left(\frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] \right)}{bd \left(\frac{c}{d} - \frac{f}{g} \right) \left(-\frac{a}{b} + \frac{f}{g} \right) g^2} + \frac{a \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{b \left(\frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b^2 \left(-\frac{a}{b} + \frac{c}{d} \right) d \left(-\frac{a}{b} + \frac{f}{g} \right) g} - \\
& \left. \frac{f \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[1 - \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] + \operatorname{PolyLog} \left[2, \frac{g \left(\frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] \right)}{bd \left(\frac{c}{d} - \frac{f}{g} \right) \left(-\frac{a}{b} + \frac{f}{g} \right) g^2} \right) + \\
& \frac{1}{-bc + ad} adgn \left(-m \operatorname{Log}[f + gx] + \operatorname{Log}[h(f + gx)^m] \right) \left(-\frac{a \operatorname{Log} \left[\frac{a}{b} + x \right]^2}{2b^2 \left(-\frac{a}{b} + \frac{c}{d} \right) d \left(-\frac{a}{b} + \frac{f}{g} \right) g} - \frac{c \operatorname{Log} \left[\frac{c}{d} + x \right]^2}{2b \left(-\frac{a}{b} + \frac{c}{d} \right) d^2 \left(-\frac{c}{d} + \frac{f}{g} \right) g} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left((a(d f - c g) \operatorname{Log}[a + b x] + (-b c f + a c g) \operatorname{Log}[c + d x] + (b c - a d) f \operatorname{Log}[f + g x]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) / \\
& \quad \left((b c - a d) (b f - a g) (-d f + c g) + \frac{c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d^2 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \quad \left. \frac{f \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^2} + \frac{a \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] \right)}{b^2 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \right. \\
& \quad \left. \frac{f \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^2} \right) + \\
& \quad \frac{1}{-b c + a d} a c g m \left(\operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \quad \left. \left((b(-d f + c g) \operatorname{Log}[a + b x] + d(b f - a g) \operatorname{Log}[c + d x] + (-b c + a d) g \operatorname{Log}[f + g x]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) / \right. \\
& \quad \left. \left((b c - a d) (b f - a g) (-d f + c g) - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right]}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{c}{d} + \frac{f}{g}\right) g} - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right]}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \right. \\
& \quad \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right]}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right]}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g} \right) - \\
& \quad \frac{1}{-b c + a d} b c f n \left(-m \operatorname{Log}[f + g x] + \operatorname{Log}[h (f + g x)^m] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
& \quad \left. \left((b(-d f + c g) \operatorname{Log}[a + b x] + d(b f - a g) \operatorname{Log}[c + d x] + (-b c + a d) g \operatorname{Log}[f + g x]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) / \right)
\end{aligned}$$

$$\begin{aligned}
& \left((bc - ad)(bf - ag)(-df + cg) - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{c}{d} + \frac{f}{g}\right)g} - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} \right. \\
& \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} \right) + \\
& \frac{1}{-bc + ad} adfn \left(-m \operatorname{Log}[f + gx] + \operatorname{Log}[h(f + gx)^m] \right) \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{c}{d} + \frac{f}{g}\right)g} + \right. \\
& \left. \left((b(-df + cg) \operatorname{Log}[a + bx] + d(bf - ag) \operatorname{Log}[c + dx] + (-bc + ad)g \operatorname{Log}[f + gx]) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right] \right) \right) \right) / \\
& \left((bc - ad)(bf - ag)(-df + cg) - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{c}{d} + \frac{f}{g}\right)g} - \frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} \right. \\
& \left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} + \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} \right) - \\
& \frac{1}{2(bc - ad)} gmn \left(\frac{\operatorname{Log}[f + gx] \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right] \right)^2}{g} + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + dx} + \frac{bx}{c + dx}\right] \right) \right. \\
& \left. \left(\frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{g} - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{g} \right) \right) + \\
& \frac{2}{g} \left(\frac{1}{2} \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] - \operatorname{PolyLog}\left[3, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] \right) +
\end{aligned}$$

$$\begin{aligned}
& 2 \left(\frac{1}{2} \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[1 - \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right] + \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right] - \operatorname{PolyLog} \left[3, \frac{g \left(\frac{c}{d} + x \right)}{-f + \frac{cg}{d}} \right] \right) \\
& \qquad \qquad \qquad g \\
& \frac{1}{g} 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{b (f + gx)}{bf - ag} \right] + \frac{1}{2} \operatorname{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \right) \right. \\
& \quad \left(\operatorname{Log} \left[\frac{b (f + gx)}{bf - ag} \right] - \operatorname{Log} \left[-\frac{d (f + gx)}{-df + cg} \right] \right) + \operatorname{Log} \left[\frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] \operatorname{Log} \left[-\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(-\operatorname{Log} \left[\frac{b (f + gx)}{bf - ag} \right] + \operatorname{Log} \left[-\frac{d (f + gx)}{-df + cg} \right] \right) + \\
& \quad \frac{1}{2} \operatorname{Log} \left[-\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right]^2 \left(\operatorname{Log} \left[\frac{-bc + ad}{bd \left(\frac{a}{b} + x \right)} \right] + \operatorname{Log} \left[\frac{b (f + gx)}{bf - ag} \right] - \operatorname{Log} \left[-\frac{(-bc + ad) (f + gx)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) + \\
& \quad \left(\operatorname{Log} \left[\frac{c}{d} + x \right] - \operatorname{Log} \left[-\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \operatorname{PolyLog} \left[2, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right] + \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[-\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) \\
& \quad \operatorname{PolyLog} \left[2, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] + \operatorname{Log} \left[-\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \left(\operatorname{PolyLog} \left[2, \frac{c}{\frac{a}{b} + x} \right] - \operatorname{PolyLog} \left[2, -\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \right) - \\
& \quad \left. \operatorname{PolyLog} \left[3, -\frac{bg \left(\frac{a}{b} + x \right)}{bf - ag} \right] - \operatorname{PolyLog} \left[3, \frac{dg \left(\frac{c}{d} + x \right)}{-df + cg} \right] - \operatorname{PolyLog} \left[3, \frac{c}{\frac{a}{b} + x} \right] + \operatorname{PolyLog} \left[3, -\frac{d (bf - ag) \left(\frac{c}{d} + x \right)}{b (-df + cg) \left(\frac{a}{b} + x \right)} \right] \right)
\end{aligned}$$

Problem 90: Unable to integrate problem.

$$\int \frac{\operatorname{Log} \left[\frac{-a}{a+bx} \right] \operatorname{Log} \left[\frac{-cx}{a+bx} \right]^2}{x (a + bx)} dx$$

Optimal (type 4, 82 leaves, 3 steps):

$$-\frac{\operatorname{Log} \left[\frac{-cx}{a+bx} \right]^2 \operatorname{PolyLog} \left[2, 1 - \frac{a}{a+bx} \right]}{a} + \frac{2 \operatorname{Log} \left[\frac{-cx}{a+bx} \right] \operatorname{PolyLog} \left[3, 1 - \frac{a}{a+bx} \right]}{a} - \frac{2 \operatorname{PolyLog} \left[4, 1 - \frac{a}{a+bx} \right]}{a}$$

Result (type 8, 36 leaves):

$$\int \frac{\operatorname{Log} \left[\frac{-a}{a+bx} \right] \operatorname{Log} \left[\frac{-cx}{a+bx} \right]^2}{x (a + bx)} dx$$

Problem 91: Unable to integrate problem.

$$\int \frac{\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2}{(c+dx)(ag+bgx)} dx$$

Optimal (type 4, 150 leaves, 3 steps):

$$-\frac{\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 \text{PolyLog}\left[2, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} + \frac{2 \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \text{PolyLog}\left[3, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} - \frac{2 \text{PolyLog}\left[4, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g}$$

Result (type 8, 57 leaves):

$$\int \frac{\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2}{(c+dx)(ag+bgx)} dx$$

Problem 92: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{(c+dx)(ag+bgx)} dx$$

Optimal (type 4, 160 leaves, 3 steps):

$$-\frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{PolyLog}\left[2, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} + \frac{2n \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[3, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} - \frac{2n^2 \text{PolyLog}\left[4, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g}$$

Result (type 4, 785 leaves):

$$\begin{aligned}
& \frac{1}{3 (b c - a d) g} \left(\text{Log} \left[\frac{a + b x}{c + d x} \right] \left(3 \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right]^2 - 3 n \text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] \text{Log} \left[\frac{a + b x}{c + d x} \right] + n^2 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 \right) \text{Log} \left[\frac{b c - a d}{b c + b d x} \right] + \right. \\
& \frac{3}{2} \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \left(-\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log} [c + d x] + 2 \text{Log} \left[\frac{c}{d} + x \right] \text{Log} [c + d x] + \right. \\
& \left. 2 \text{Log} \left[\frac{a + b x}{c + d x} \right] \text{Log} [c + d x] + 2 \text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 2 \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
& n \left(\text{Log} \left[e \left(\frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\text{Log} \left[\frac{c}{d} + x \right]^3 + 3 \text{Log} \left[\frac{c}{d} + x \right]^2 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{d (a + b x)}{-b c + a d} \right] \right) \right) + \\
& 3 \left(-\text{Log} \left[\frac{a}{b} + x \right] + \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{a + b x}{c + d x} \right] \right)^2 \text{Log} [c + d x] + 3 \text{Log} \left[\frac{a}{b} + x \right]^2 \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + 6 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] + \\
& 3 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] - \text{Log} \left[\frac{a + b x}{c + d x} \right] \right) \left(\text{Log} \left[\frac{c}{d} + x \right]^2 - 2 \left(\text{Log} \left[\frac{a}{b} + x \right] \text{Log} \left[\frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) + \\
& 6 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b (c + d x)}{b c - a d} \right] - 6 \text{PolyLog} \left[3, \frac{d (a + b x)}{-b c + a d} \right] - 6 \text{PolyLog} \left[3, \frac{b (c + d x)}{b c - a d} \right] - n^2 \\
& \left. \left(\text{Log} \left[\frac{a + b x}{c + d x} \right]^3 \text{Log} \left[\frac{b c - a d}{b c + b d x} \right] + 3 \text{Log} \left[\frac{a + b x}{c + d x} \right]^2 \text{PolyLog} \left[2, \frac{d (a + b x)}{b (c + d x)} \right] - 6 \text{Log} \left[\frac{a + b x}{c + d x} \right] \text{PolyLog} \left[3, \frac{d (a + b x)}{b (c + d x)} \right] + 6 \text{PolyLog} \left[4, \frac{d (a + b x)}{b (c + d x)} \right] \right) \right)
\end{aligned}$$

Problem 98: Unable to integrate problem.

$$\int \text{Log} \left[\frac{c (b + a x)^2}{x^2} \right]^3 dx$$

Optimal (type 4, 102 leaves, 5 steps):

$$x \text{Log} \left[\frac{c (b + a x)^2}{x^2} \right]^3 - \frac{6 b \text{Log} \left[\frac{c (b + a x)^2}{x^2} \right]^2 \text{Log} \left[1 - \frac{a x}{b + a x} \right]}{a} + \frac{24 b \text{Log} \left[\frac{c (b + a x)^2}{x^2} \right] \text{PolyLog} \left[2, \frac{a x}{b + a x} \right]}{a} + \frac{48 b \text{PolyLog} \left[3, \frac{a x}{b + a x} \right]}{a}$$

Result (type 8, 17 leaves):

$$\int \text{Log} \left[\frac{c (b + a x)^2}{x^2} \right]^3 dx$$

Problem 101: Unable to integrate problem.

$$\int \text{Log} \left[\frac{c x^2}{(b + a x)^2} \right]^3 dx$$

Optimal (type 4, 98 leaves, 5 steps):

$$x \operatorname{Log}\left[\frac{c x^2}{(b+a x)^2}\right]^3 + \frac{6 b \operatorname{Log}\left[\frac{c x^2}{(b+a x)^2}\right]^2 \operatorname{Log}\left[\frac{b}{b+a x}\right]}{a} + \frac{24 b \operatorname{Log}\left[\frac{c x^2}{(b+a x)^2}\right] \operatorname{PolyLog}\left[2, \frac{a x}{b+a x}\right]}{a} - \frac{48 b \operatorname{PolyLog}\left[3, \frac{a x}{b+a x}\right]}{a}$$

Result (type 8, 17 leaves):

$$\int \operatorname{Log}\left[\frac{c x^2}{(b+a x)^2}\right]^3 dx$$

Problem 102: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{PolyLog}\left[2, 1 + \frac{b c - a d}{d (a+b x)}\right]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 35 leaves, 1 step):

$$-\frac{\operatorname{PolyLog}\left[3, 1 + \frac{b c - a d}{d (a+b x)}\right]}{b c - a d}$$

Result (type 4, 1037 leaves):

$$\begin{aligned}
& \frac{(\text{Log}[a + b x] - \text{Log}[c + d x]) \text{PolyLog}\left[2, \frac{bc}{d(a+bx)} + \frac{bx}{a+bx}\right]}{bc - ad} - \\
& \frac{1}{6bc - 6ad} \left(-3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] + 2 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right]^3 - 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[a + b x] + \right. \\
& 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[a + b x] + 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[a + b x] + \\
& 6 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right]^2 \text{Log}[a + b x] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x]^2 + 6 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[a + b x]^2 - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc + ad}\right] + \\
& 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc + ad}\right] - 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}\left[\frac{d(a+bx)}{-bc + ad}\right] + 9 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[c + d x] - \\
& 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[c + d x] - 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[c + d x] - \\
& 12 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] \text{Log}[c + d x] - 12 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[a + b x] \text{Log}[c + d x] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x]^2 + \\
& 6 \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}[c + d x]^2 - 9 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc - ad}\right] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc - ad}\right] - \\
& 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \text{Log}\left[\frac{b(c+dx)}{bc - ad}\right] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc - ad}\right] - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] \text{Log}\left[\frac{b(c+dx)}{bc - ad}\right] - \\
& 6 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] - \text{Log}[a + b x] + \text{Log}[c + d x] \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc + ad}\right] - \\
& 6 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{-bc + ad}{d(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc - ad}\right] - 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc + ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc - ad}\right] \Big)
\end{aligned}$$

Problem 103: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 85 leaves, 2 steps):

$$\frac{\text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{PolyLog}\left[2, 1 + \frac{bc-ad}{d(a+bx)}\right]}{bc - ad} - \frac{\text{PolyLog}\left[3, 1 + \frac{bc-ad}{d(a+bx)}\right]}{bc - ad}$$

Result (type 4, 617 leaves):

$$\begin{aligned}
& \frac{1}{6(bc-ad)} \left(2 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \right) + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \left(-\operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) \right) + \\
& 6 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \right) \left(\operatorname{Log} [a+bx] - \operatorname{Log} [c+dx] \right) \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \right) + \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - \\
& 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{c}{d} + x \right] + \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \right) \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) \right) - \\
& 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 3 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \right) \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 + \operatorname{Log} \left[\frac{c}{d} + x \right]^2 - \right. \\
& \quad \left. 2 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] \right) - 2 \left(\operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) - \\
& 6 \left(\operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] - 2 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] \right) - \\
& 6 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] + 6 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \Big)
\end{aligned}$$

Problem 104: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right]^2}{a+bx} dx$$

Optimal (type 4, 140 leaves, 4 steps):

$$-\frac{\operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right]^2}{b} - \frac{2 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right]}{b} + \frac{2 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right]}{b}$$

Result (type 4, 363 leaves):

$$\begin{aligned} & \frac{1}{3b} \left(\text{Log} \left[\frac{a}{b} + x \right]^3 + 3 \text{Log} \left[\frac{c}{d} + x \right]^2 \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 3 \text{Log} \left[\frac{a}{b} + x \right]^2 \left(-\text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{b(c+dx)}{bc-ad} \right] \right) \right) + \\ & 3 \text{Log} [a+bx] \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)} \right] \right)^2 + 6 \text{Log} \left[\frac{a}{b} + x \right] \text{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + \\ & 6 \text{Log} \left[\frac{c}{d} + x \right] \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 3 \left(\text{Log} \left[\frac{a}{b} + x \right] - \text{Log} \left[\frac{c}{d} + x \right] + \text{Log} \left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)} \right] \right) \\ & \left(\text{Log} \left[\frac{a}{b} + x \right]^2 - 2 \left(\text{Log} \left[\frac{c}{d} + x \right] \text{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) - 6 \text{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] - 6 \text{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] \end{aligned}$$

Problem 105: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log} \left[\frac{e(c+dx)}{a+bx} \right] \text{Log} \left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)} \right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 109 leaves, 2 steps):

$$\frac{\text{Log} \left[\frac{e(c+dx)}{a+bx} \right] \text{PolyLog} \left[2, 1 + \frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)} \right]}{bc-ad} - \frac{\text{PolyLog} \left[3, 1 + \frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)} \right]}{bc-ad}$$

Result (type 4, 1681 leaves):

$$\begin{aligned}
& - \frac{1}{6bc - 6ad} \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [a + bx] - 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [a + bx] + \right. \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] - 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c+dx)}{bc-ad} \right] - \\
& 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] - 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] + \\
& 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a+bx)}{-bc+ad} \right] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] + 3 \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right]^2 + 3 \operatorname{Log} \left[\frac{-bc+ad}{d(a+bx)} \right] \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right]^2 - \\
& 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [e + fx] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [e + fx] - 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [e + fx] - \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{Log} [e + fx] + 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{Log} [e + fx] - 3 \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right]^2 \operatorname{Log} [e + fx] + \\
& 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] - 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right] \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] + 3 \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right]^2 \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] + \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] - 6 \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right] \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] + \\
& 3 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{b(e+fx)}{be-af} \right] - 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] + \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right] \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] - 3 \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right]^2 \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] - 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] + \\
& 6 \operatorname{Log} \left[\frac{f(c+dx)}{-de+cf} \right] \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{Log} \left[\frac{d(e+fx)}{de-cf} \right] + 3 \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right]^2 \operatorname{Log} \left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)} \right] - \\
& 3 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right]^2 \operatorname{Log} \left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a+bx)}{-bc+ad} \right] + \\
& 6 \left(\operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] - \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{f(a+bx)}{-be+af} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] + \\
& 6 \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{bc-ad} \right] - 6 \operatorname{Log} \left[\frac{e(c+dx)}{a+bx} \right] \operatorname{PolyLog} \left[2, \frac{f(c+dx)}{-de+cf} \right] + 6 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{f(c+dx)}{-de+cf} \right] + \\
& 6 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c+dx)}{d(a+bx)} \right] - 6 \operatorname{Log} \left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \operatorname{PolyLog} \left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] - \\
& 6 \operatorname{PolyLog} \left[3, \frac{d(a+bx)}{-bc+ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{bc-ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c+dx)}{d(a+bx)} \right] + 6 \operatorname{PolyLog} \left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)} \right] \Big)
\end{aligned}$$

Problem 106: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{(a+bx)(e+fx)} dx$$

Optimal (type 4, 204 leaves, 4 steps):

$$-\frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[1 - \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af} - \frac{2 \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af} + \frac{2 \text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af}$$

Result (type 4, 1636 leaves):

$$\begin{aligned}
& \frac{1}{3be - 3af} \left(-2 \operatorname{Log} \left[\frac{a}{b} + x \right]^3 + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [a + bx] - \right. \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [a + bx] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] - \\
& 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(c + dx)}{bc - ad} \right] - 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] + \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] - 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] + \\
& 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(a + bx)}{-bc + ad} \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] + 3 \operatorname{Log} \left[\frac{-bc + ad}{d(a + bx)} \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right]^2 + \\
& 3 \operatorname{Log} [a + bx] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right]^2 - 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} [e + fx] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} [e + fx] - \\
& 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} [e + fx] - 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} [e + fx] + 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} [e + fx] - \\
& 3 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right]^2 \operatorname{Log} [e + fx] + 3 \operatorname{Log} \left[\frac{a}{b} + x \right]^2 \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] - 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right] \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] + \\
& 3 \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right]^2 \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] - \\
& 6 \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] + 3 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right]^2 \operatorname{Log} \left[\frac{b(e + fx)}{be - af} \right] - \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] + 3 \operatorname{Log} \left[\frac{c}{d} + x \right]^2 \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] + 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right] \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] - \\
& 3 \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right]^2 \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] - 6 \operatorname{Log} \left[\frac{c}{d} + x \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] + \\
& 6 \operatorname{Log} \left[\frac{f(c + dx)}{-de + cf} \right] \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{Log} \left[\frac{d(e + fx)}{de - cf} \right] - 3 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right]^2 \operatorname{Log} \left[\frac{(-bc + ad)(e + fx)}{(de - cf)(a + bx)} \right] + \\
& 6 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{PolyLog} \left[2, \frac{d(a + bx)}{-bc + ad} \right] + 6 \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \right) \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{bc - ad} \right] + \\
& 6 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{PolyLog} \left[2, \frac{b(c + dx)}{d(a + bx)} \right] - 6 \operatorname{Log} \left[\frac{(-be + af)(c + dx)}{(-de + cf)(a + bx)} \right] \operatorname{PolyLog} \left[2, \frac{(be - af)(c + dx)}{(de - cf)(a + bx)} \right] - \\
& 6 \operatorname{PolyLog} \left[3, \frac{d(a + bx)}{-bc + ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c + dx)}{bc - ad} \right] - 6 \operatorname{PolyLog} \left[3, \frac{b(c + dx)}{d(a + bx)} \right] + 6 \operatorname{PolyLog} \left[3, \frac{(be - af)(c + dx)}{(de - cf)(a + bx)} \right] \Big)
\end{aligned}$$

Problem 107: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{e+fx} dx$$

Optimal (type 4, 322 leaves, 9 steps):

$$\frac{\text{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{f} + \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[1-\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f} - \frac{2 \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{f} +$$

$$\frac{2 \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f} + \frac{2 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{f} - \frac{2 \text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f}$$

Result (type 4, 1080 leaves):

$$\frac{1}{f} \left(-\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 + \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}[e+fx] - \right.$$

$$2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[e+fx] + \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}[e+fx] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}[e+fx] -$$

$$2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}[e+fx] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \text{Log}[e+fx] -$$

$$\text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] - \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] -$$

$$2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + 2 \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] -$$

$$\text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] -$$

$$\text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] - 2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] +$$

$$2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] - 2 \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] +$$

$$\text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] - 2 \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] +$$

$$2 \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] - 2 \text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \left. \right)$$

Problem 108: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 433 leaves, 10 steps):

$$\frac{\text{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{2(bc-ad)} - \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right]}{2(bc-ad)} + \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[1 - \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{2(bc-ad)} - \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bc-ad} + \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{bc-ad} + \frac{\text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bc-ad} - \frac{\text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{bc-ad}$$

Result (type 4, 1855 leaves):

$$\begin{aligned} & \frac{1}{2(bc-ad)} \left(2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{e}{f} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{e}{f} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \right. \\ & 2 \left(\text{Log}[a+bx] - \text{Log}[c+dx] \right) \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \left(\text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \\ & \left(\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \text{Log}\left[\frac{f(a+bx)}{-be+af}\right] \right) \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \left(-2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \\ & \text{Log}\left[\frac{a}{b} + x\right]^2 \left(-\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \left(\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \right) \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \right) + \\ & \text{Log}\left[\frac{c}{d} + x\right]^2 \left(-\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \right) + 2 \left(-\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \right) \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] + \\ & \left(\text{Log}\left[\frac{-be+af}{f(a+bx)}\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right]^2 + \\ & 2 \left(-\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{Log}\left[\frac{f(a+bx)}{-be+af}\right] \right) \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] + \\ & \left(\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{Log}\left[\frac{-de+cf}{f(c+dx)}\right] - \text{Log}\left[\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}\right] \right) \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right]^2 + \\ & 2 \left(\text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\ & 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{f(a+bx)}{-be+af}\right] + 2 \left(\text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \right) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \end{aligned}$$

$$\begin{aligned}
& \left(\text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) \left(\text{Log}\left[\frac{a}{b} + x\right]^2 + \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) - \\
& 2 \left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{f(c+dx)}{-de+cf}\right] + \\
& 2 \left(\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \right) \text{PolyLog}\left[2, \frac{b(e+fx)}{be-af}\right] + 2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \\
& \left(\text{Log}\left[\frac{e}{f} + x\right] \left(\text{Log}\left[\frac{f(a+bx)}{-be+af}\right] - \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \right) + \text{PolyLog}\left[2, \frac{b(e+fx)}{be-af}\right] - \text{PolyLog}\left[2, \frac{d(e+fx)}{de-cf}\right] \right) + \\
& 2 \left(\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{d(e+fx)}{de-cf}\right] + \\
& 2 \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] \left(\text{PolyLog}\left[2, \frac{b(e+fx)}{f(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)}\right] \right) + \\
& 2 \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \left(\text{PolyLog}\left[2, \frac{d(e+fx)}{f(c+dx)}\right] - \text{PolyLog}\left[2, \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \right) - 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 2 \text{PolyLog}\left[3, \frac{f(a+bx)}{-be+af}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{f(c+dx)}{-de+cf}\right] - 2 \text{PolyLog}\left[3, \frac{b(e+fx)}{be-af}\right] - 2 \text{PolyLog}\left[3, \frac{d(e+fx)}{de-cf}\right] - \\
& 2 \text{PolyLog}\left[3, \frac{b(e+fx)}{f(a+bx)}\right] + 2 \text{PolyLog}\left[3, -\frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)}\right] - 2 \text{PolyLog}\left[3, \frac{d(e+fx)}{f(c+dx)}\right] + 2 \text{PolyLog}\left[3, \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \Big)
\end{aligned}$$

Test results for the 547 problems in "3.3 u (a+b log(c (d+e x)^n))^p.m"

Problem 17: Result more than twice size of optimal antiderivative.

$$\int (a + b \text{Log}[c (d + e x)^n])^4 dx$$

Optimal (type 3, 131 leaves, 6 steps):

$$\begin{aligned}
& -24 a b^3 n^3 x + 24 b^4 n^4 x - \frac{24 b^4 n^3 (d + e x) \text{Log}[c (d + e x)^n]}{e} + \\
& \frac{12 b^2 n^2 (d + e x) (a + b \text{Log}[c (d + e x)^n])^2}{e} - \frac{4 b n (d + e x) (a + b \text{Log}[c (d + e x)^n])^3}{e} + \frac{(d + e x) (a + b \text{Log}[c (d + e x)^n])^4}{e}
\end{aligned}$$

Result (type 3, 390 leaves):

$$\frac{1}{e} \left(-b^4 d n^4 \operatorname{Log}[d + e x]^4 + 4 b^3 d n^3 \operatorname{Log}[d + e x]^3 (a - b n + b \operatorname{Log}[c (d + e x)^n]) - \right. \\ \left. 6 b^2 d n^2 \operatorname{Log}[d + e x]^2 (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c (d + e x)^n] + b^2 \operatorname{Log}[c (d + e x)^n]^2) + 4 b d n \operatorname{Log}[d + e x] \right. \\ \left. (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 b (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d + e x)^n] + 3 b^2 (a - b n) \operatorname{Log}[c (d + e x)^n]^2 + b^3 \operatorname{Log}[c (d + e x)^n]^3) + \right. \\ \left. e x (a^4 - 4 a^3 b n + 12 a^2 b^2 n^2 - 24 a b^3 n^3 + 24 b^4 n^4 + 4 b (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3) \operatorname{Log}[c (d + e x)^n] + \right. \\ \left. 6 b^2 (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d + e x)^n]^2 + 4 b^3 (a - b n) \operatorname{Log}[c (d + e x)^n]^3 + b^4 \operatorname{Log}[c (d + e x)^n]^4) \right)$$

Problem 18: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^3 dx$$

Optimal (type 3, 99 leaves, 5 steps):

$$6 a b^2 n^2 x - 6 b^3 n^3 x + \frac{6 b^3 n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} - \frac{3 b n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e}$$

Result (type 3, 219 leaves):

$$\frac{1}{e} \left(b^3 d n^3 \operatorname{Log}[d + e x]^3 - 3 b^2 d n^2 \operatorname{Log}[d + e x]^2 (a - b n + b \operatorname{Log}[c (d + e x)^n]) + \right. \\ \left. 3 b d n \operatorname{Log}[d + e x] (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c (d + e x)^n] + b^2 \operatorname{Log}[c (d + e x)^n]^2) + \right. \\ \left. e x (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 b (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d + e x)^n] + 3 b^2 (a - b n) \operatorname{Log}[c (d + e x)^n]^2 + b^3 \operatorname{Log}[c (d + e x)^n]^3) \right)$$

Problem 24: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^{5/2} dx$$

Optimal (type 4, 179 leaves, 7 steps):

$$- \frac{15 b^{5/2} e^{-\frac{a}{b n}} n^{5/2} \sqrt{\pi} (d + e x) (c (d + e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e} + \\ \frac{15 b^2 n^2 (d + e x) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{4 e} - \frac{5 b n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^{3/2}}{2 e} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^{5/2}}{e}$$

Result (type 8, 20 leaves):

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^{5/2} dx$$

Problem 25: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^{3/2} dx$$

Optimal (type 4, 143 leaves, 6 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{bn}} n^{3/2} \sqrt{\pi} (d + e x) (c (d + e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e} - \frac{3 b n (d + e x) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{2 e} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^{3/2}}{e}$$

Result (type 8, 20 leaves):

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^{3/2} dx$$

Problem 26: Unable to integrate problem.

$$\int \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} dx$$

Optimal (type 4, 111 leaves, 5 steps):

$$-\frac{\sqrt{b} e^{-\frac{a}{bn}} \sqrt{n} \sqrt{\pi} (d + e x) (c (d + e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e} + \frac{(d + e x) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}{e}$$

Result (type 8, 20 leaves):

$$\int \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} dx$$

Problem 52: Result more than twice size of optimal antiderivative.

$$\int (f + g x)^3 (a + b \operatorname{Log}[c (d + e x)^n])^3 dx$$

Optimal (type 3, 598 leaves, 19 steps):

$$\begin{aligned}
& \frac{6ab^2(e f - dg)^3 n^2 x}{e^3} - \frac{6b^3(e f - dg)^3 n^3 x}{e^3} - \frac{9b^3 g(e f - dg)^2 n^3 (d + ex)^2}{8e^4} - \frac{2b^3 g^2(e f - dg) n^3 (d + ex)^3}{9e^4} - \\
& \frac{3b^3 g^3 n^3 (d + ex)^4}{128e^4} + \frac{6b^3(e f - dg)^3 n^2 (d + ex) \operatorname{Log}[c(d + ex)^n]}{e^4} + \frac{9b^2 g(e f - dg)^2 n^2 (d + ex)^2 (a + b \operatorname{Log}[c(d + ex)^n])}{4e^4} + \\
& \frac{2b^2 g^2(e f - dg) n^2 (d + ex)^3 (a + b \operatorname{Log}[c(d + ex)^n])}{3e^4} + \frac{3b^2 g^3 n^2 (d + ex)^4 (a + b \operatorname{Log}[c(d + ex)^n])}{32e^4} - \\
& \frac{3b(e f - dg)^3 n (d + ex) (a + b \operatorname{Log}[c(d + ex)^n])^2}{e^4} - \frac{9bg(e f - dg)^2 n (d + ex)^2 (a + b \operatorname{Log}[c(d + ex)^n])^2}{4e^4} - \\
& \frac{bg^2(e f - dg) n (d + ex)^3 (a + b \operatorname{Log}[c(d + ex)^n])^2}{e^4} - \frac{3bg^3 n (d + ex)^4 (a + b \operatorname{Log}[c(d + ex)^n])^2}{16e^4} + \frac{(e f - dg)^3 (d + ex) (a + b \operatorname{Log}[c(d + ex)^n])^3}{e^4} + \\
& \frac{3g(e f - dg)^2 (d + ex)^2 (a + b \operatorname{Log}[c(d + ex)^n])^3}{2e^4} + \frac{g^2(e f - dg) (d + ex)^3 (a + b \operatorname{Log}[c(d + ex)^n])^3}{e^4} + \frac{g^3 (d + ex)^4 (a + b \operatorname{Log}[c(d + ex)^n])^3}{4e^4}
\end{aligned}$$

Result (type 3, 1241 leaves):

$$\begin{aligned}
& \frac{1}{1152e^4} \left(-288b^3 d (-4e^3 f^3 + 6de^2 f^2 g - 4d^2 e f g^2 + d^3 g^3) n^3 \operatorname{Log}[d + ex]^3 + \right. \\
& 72b^2 d n^2 \operatorname{Log}[d + ex]^2 (-12a(4e^3 f^3 - 6de^2 f^2 g + 4d^2 e f g^2 - d^3 g^3) + b(48e^3 f^3 - 108de^2 f^2 g + 88d^2 e f g^2 - 25d^3 g^3) n - \\
& 12b(4e^3 f^3 - 6de^2 f^2 g + 4d^2 e f g^2 - d^3 g^3) \operatorname{Log}[c(d + ex)^n]) - 12bdn \operatorname{Log}[d + ex] (-72a^2(4e^3 f^3 - 6de^2 f^2 g + 4d^2 e f g^2 - d^3 g^3) + \\
& 12ab(48e^3 f^3 - 108de^2 f^2 g + 88d^2 e f g^2 - 25d^3 g^3) n + b^2(-576e^3 f^3 + 1512de^2 f^2 g - 1360d^2 e f g^2 + 415d^3 g^3) n^2 - \\
& 12b(12a(4e^3 f^3 - 6de^2 f^2 g + 4d^2 e f g^2 - d^3 g^3) + b(-48e^3 f^3 + 108de^2 f^2 g - 88d^2 e f g^2 + 25d^3 g^3) n) \operatorname{Log}[c(d + ex)^n] - \\
& 72b^2(4e^3 f^3 - 6de^2 f^2 g + 4d^2 e f g^2 - d^3 g^3) \operatorname{Log}[c(d + ex)^n]^2) + ex(288a^3 e^3(4f^3 + 6f^2 g x + 4f g^2 x^2 + g^3 x^3) - \\
& 72a^2 b n(-12d^3 g^3 + 6d^2 e g^2(8f + gx) - 4de^2 g(18f^2 + 6f g x + g^2 x^2) + e^3(48f^3 + 36f^2 g x + 16f g^2 x^2 + 3g^3 x^3)) + \\
& 12ab^2 n^2(-300d^3 g^3 + 6d^2 e g^2(176f + 13gx) - 4de^2 g(324f^2 + 60f g x + 7g^2 x^2) + e^3(576f^3 + 216f^2 g x + 64f g^2 x^2 + 9g^3 x^3)) - \\
& b^3 n^3(-4980d^3 g^3 + 30d^2 e g^2(544f + 23gx) - 4de^2 g(4536f^2 + 456f g x + 37g^2 x^2) + e^3(6912f^3 + 1296f^2 g x + 256f g^2 x^2 + 27g^3 x^3)) + \\
& 12b(72a^2 e^3(4f^3 + 6f^2 g x + 4f g^2 x^2 + g^3 x^3) - \\
& 12abn(-12d^3 g^3 + 6d^2 e g^2(8f + gx) - 4de^2 g(18f^2 + 6f g x + g^2 x^2) + e^3(48f^3 + 36f^2 g x + 16f g^2 x^2 + 3g^3 x^3)) + \\
& b^2 n^2(-300d^3 g^3 + 6d^2 e g^2(176f + 13gx) - 4de^2 g(324f^2 + 60f g x + 7g^2 x^2) + e^3(576f^3 + 216f^2 g x + 64f g^2 x^2 + 9g^3 x^3))) \\
& \left. \operatorname{Log}[c(d + ex)^n] + 72b^2(12ae^3(4f^3 + 6f^2 g x + 4f g^2 x^2 + g^3 x^3) - bn(-12d^3 g^3 + 6d^2 e g^2(8f + gx) - 4de^2 g(18f^2 + 6f g x + g^2 x^2) + \right. \\
& \left. e^3(48f^3 + 36f^2 g x + 16f g^2 x^2 + 3g^3 x^3))) \operatorname{Log}[c(d + ex)^n]^2 + 288b^3 e^3(4f^3 + 6f^2 g x + 4f g^2 x^2 + g^3 x^3) \operatorname{Log}[c(d + ex)^n]^3 \right)
\end{aligned}$$

Problem 55: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c(d + ex)^n])^3 dx$$

Optimal (type 3, 99 leaves, 5 steps):

$$6 a b^2 n^2 x - 6 b^3 n^3 x + \frac{6 b^3 n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} - \frac{3 b n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e}$$

Result (type 3, 219 leaves):

$$\frac{1}{e} \left(b^3 d n^3 \operatorname{Log}[d + e x]^3 - 3 b^2 d n^2 \operatorname{Log}[d + e x]^2 (a - b n + b \operatorname{Log}[c (d + e x)^n]) + \right. \\ \left. 3 b d n \operatorname{Log}[d + e x] (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a - b n) \operatorname{Log}[c (d + e x)^n] + b^2 \operatorname{Log}[c (d + e x)^n]^2) + \right. \\ \left. e x (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + 3 b (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d + e x)^n] + 3 b^2 (a - b n) \operatorname{Log}[c (d + e x)^n]^2 + b^3 \operatorname{Log}[c (d + e x)^n]^3) \right)$$

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^3}{f + g x} dx$$

Optimal (type 4, 158 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right]}{g} + \frac{3 b n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g} - \\ \frac{6 b^2 n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g} + \frac{6 b^3 n^3 \operatorname{PolyLog}\left[4, -\frac{g(d+ex)}{ef-dg}\right]}{g}$$

Result (type 4, 335 leaves):

$$\frac{1}{g} \left((a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}[f + g x] + 3 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right. \\ \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] \right) + 6 b^2 n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\ \left(\frac{1}{2} \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] - \operatorname{PolyLog}\left[3, \frac{g(d+ex)}{-ef+dg}\right] \right) + b^3 n^3 \\ \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + 3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g(d+ex)}{-ef+dg}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g(d+ex)}{-ef+dg}\right] \right) \left. \right)$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^3}{(f + g x)^2} dx$$

Optimal (type 4, 190 leaves, 5 steps):

$$\frac{(d+ex)(a+b\log[c(d+ex)^n])^3}{(ef-dg)(f+gx)} - \frac{3ben(a+b\log[c(d+ex)^n])^2 \log\left[\frac{e(f+gx)}{ef-dg}\right]}{g(ef-dg)} -$$

$$\frac{6b^2e n^2(a+b\log[c(d+ex)^n]) \operatorname{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g(ef-dg)} + \frac{6b^3e n^3 \operatorname{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g(ef-dg)}$$

Result (type 4, 410 leaves):

$$\frac{1}{g(ef-dg)(f+gx)} \left(-3b(ef-dg)n \log[d+ex] (a-bn \log[d+ex] + b \log[c(d+ex)^n])^2 + \right.$$

$$3ben(f+gx) \log[d+ex] (a-bn \log[d+ex] + b \log[c(d+ex)^n])^2 - (ef-dg)(a-bn \log[d+ex] + b \log[c(d+ex)^n])^3 -$$

$$3ben(f+gx)(a-bn \log[d+ex] + b \log[c(d+ex)^n])^2 \log[f+gx] + 3b^2n^2(a-bn \log[d+ex] + b \log[c(d+ex)^n])$$

$$\left(\log[d+ex] \left(g(d+ex) \log[d+ex] - 2e(f+gx) \log\left[\frac{e(f+gx)}{ef-dg}\right] \right) - 2e(f+gx) \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] \right) +$$

$$b^3n^3 \left(\log[d+ex]^2 \left(g(d+ex) \log[d+ex] - 3e(f+gx) \log\left[\frac{e(f+gx)}{ef-dg}\right] \right) - \right.$$

$$\left. \left. 6e(f+gx) \log[d+ex] \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] + 6e(f+gx) \operatorname{PolyLog}\left[3, \frac{g(d+ex)}{-ef+dg}\right] \right) \right)$$

Problem 60: Result more than twice size of optimal antiderivative.

$$\int (f+gx)(a+b\log[c(d+ex)^n])^4 dx$$

Optimal (type 3, 340 leaves, 13 steps):

$$-\frac{24ab^3(ef-dg)n^3x}{e} + \frac{24b^4(ef-dg)n^4x}{e} + \frac{3b^4gn^4(d+ex)^2}{4e^2} - \frac{24b^4(ef-dg)n^3(d+ex)\log[c(d+ex)^n]}{e^2} -$$

$$\frac{3b^3gn^3(d+ex)^2(a+b\log[c(d+ex)^n])}{2e^2} + \frac{12b^2(ef-dg)n^2(d+ex)(a+b\log[c(d+ex)^n])^2}{e^2} +$$

$$\frac{3b^2gn^2(d+ex)^2(a+b\log[c(d+ex)^n])^2}{2e^2} - \frac{4b(ef-dg)n(d+ex)(a+b\log[c(d+ex)^n])^3}{e^2} -$$

$$\frac{bgn(d+ex)^2(a+b\log[c(d+ex)^n])^3}{e^2} + \frac{(ef-dg)(d+ex)(a+b\log[c(d+ex)^n])^4}{e^2} + \frac{g(d+ex)^2(a+b\log[c(d+ex)^n])^4}{2e^2}$$

Result (type 3, 748 leaves):

$$\begin{aligned} & \frac{1}{4e^2} \left(2b^4d(-2ef+dg)n^4 \operatorname{Log}[d+ex]^4 - 4b^3dn^3 \operatorname{Log}[d+ex]^3 (-4aef+2adg+4befn-3bdgn+b(-4ef+2dg) \operatorname{Log}[c(d+ex)^n]) \right) + \\ & 6b^2dn^2 \operatorname{Log}[d+ex]^2 \left(a^2(-4ef+2dg) + 2ab(4ef-3dg)n + b^2(-8ef+7dg)n^2 + \right. \\ & \quad \left. 2b(-4aef+2adg+4befn-3bdgn) \operatorname{Log}[c(d+ex)^n] + 2b^2(-2ef+dg) \operatorname{Log}[c(d+ex)^n]^2 \right) - \\ & 2bdn \operatorname{Log}[d+ex] \left(a^3(-8ef+4dg) + 6a^2b(4ef-3dg)n - 6ab^2(8ef-7dg)n^2 + 3b^3(16ef-15dg)n^3 - \right. \\ & \quad \left. 6b(a^2(4ef-2dg) + b^2(8ef-7dg)n^2 + ab(-8efn+6dgn)) \operatorname{Log}[c(d+ex)^n] + \right. \\ & \quad \left. 6b^2(-4aef+2adg+4befn-3bdgn) \operatorname{Log}[c(d+ex)^n]^2 + 4b^3(-2ef+dg) \operatorname{Log}[c(d+ex)^n]^3 \right) + \\ & ex \left(2a^4e(2f+gx) + 3b^4n^4(32ef-30dg+egx) - 6ab^3n^3(16ef-14dg+egx) + 6a^2b^2n^2(8ef-6dg+egx) - \right. \\ & \quad \left. 4a^3bn(4ef-2dg+egx) + 2b(4a^3e(2f+gx) - 3b^3n^3(16ef-14dg+egx) + 6ab^2n^2(8ef-6dg+egx) - 6a^2bn(4ef-2dg+egx)) \right. \\ & \quad \left. \operatorname{Log}[c(d+ex)^n] + 6b^2(2a^2e(2f+gx) + b^2n^2(8ef-6dg+egx) - 2abn(4ef-2dg+egx)) \operatorname{Log}[c(d+ex)^n]^2 + \right. \\ & \quad \left. 4b^3(2ae(2f+gx) - bn(4ef-2dg+egx)) \operatorname{Log}[c(d+ex)^n]^3 + 2b^4e(2f+gx) \operatorname{Log}[c(d+ex)^n]^4 \right) \end{aligned}$$

Problem 61: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c(d+ex)^n])^4 dx$$

Optimal (type 3, 131 leaves, 6 steps):

$$\begin{aligned} & -24ab^3n^3x + 24b^4n^4x - \frac{24b^4n^3(d+ex) \operatorname{Log}[c(d+ex)^n]}{e} + \\ & \frac{12b^2n^2(d+ex)(a+b \operatorname{Log}[c(d+ex)^n])^2}{e} - \frac{4bn(d+ex)(a+b \operatorname{Log}[c(d+ex)^n])^3}{e} + \frac{(d+ex)(a+b \operatorname{Log}[c(d+ex)^n])^4}{e} \end{aligned}$$

Result (type 3, 390 leaves):

$$\begin{aligned} & \frac{1}{e} \left(-b^4dn^4 \operatorname{Log}[d+ex]^4 + 4b^3dn^3 \operatorname{Log}[d+ex]^3 (a-bn+b \operatorname{Log}[c(d+ex)^n]) \right) - \\ & 6b^2dn^2 \operatorname{Log}[d+ex]^2 \left(a^2 - 2abn + 2b^2n^2 + 2b(a-bn) \operatorname{Log}[c(d+ex)^n] + b^2 \operatorname{Log}[c(d+ex)^n]^2 \right) + 4bdn \operatorname{Log}[d+ex] \\ & \quad \left(a^3 - 3a^2bn + 6ab^2n^2 - 6b^3n^3 + 3b(a^2 - 2abn + 2b^2n^2) \operatorname{Log}[c(d+ex)^n] + 3b^2(a-bn) \operatorname{Log}[c(d+ex)^n]^2 + b^3 \operatorname{Log}[c(d+ex)^n]^3 \right) + \\ & ex \left(a^4 - 4a^3bn + 12a^2b^2n^2 - 24ab^3n^3 + 24b^4n^4 + 4b(a^3 - 3a^2bn + 6ab^2n^2 - 6b^3n^3) \operatorname{Log}[c(d+ex)^n] + \right. \\ & \quad \left. 6b^2(a^2 - 2abn + 2b^2n^2) \operatorname{Log}[c(d+ex)^n]^2 + 4b^3(a-bn) \operatorname{Log}[c(d+ex)^n]^3 + b^4 \operatorname{Log}[c(d+ex)^n]^4 \right) \end{aligned}$$

Problem 62: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c(d+ex)^n])^4}{f+gx} dx$$

Optimal (type 4, 205 leaves, 6 steps):

$$\frac{(a + b \operatorname{Log}[c(d + ex)^n])^4 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right]}{g} + \frac{4bn(a + b \operatorname{Log}[c(d + ex)^n])^3 \operatorname{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g} -$$

$$\frac{12b^2n^2(a + b \operatorname{Log}[c(d + ex)^n])^2 \operatorname{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g} + \frac{24b^3n^3(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{PolyLog}\left[4, -\frac{g(d+ex)}{ef-dg}\right]}{g} - \frac{24b^4n^4 \operatorname{PolyLog}\left[5, -\frac{g(d+ex)}{ef-dg}\right]}{g}$$

Result (type 4, 503 leaves):

$$\frac{1}{g} \left((a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^4 \operatorname{Log}[f + gx] + \right.$$

$$4bn(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^3 \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] \right) +$$

$$6b^2n^2(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^2 \left(\operatorname{Log}[d + ex]^2 \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + \right.$$

$$2 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] - 2 \operatorname{PolyLog}\left[3, \frac{g(d + ex)}{-ef + dg}\right] \left. \right) - 4b^3n^3(-a + bn \operatorname{Log}[d + ex] - b \operatorname{Log}[c(d + ex)^n])$$

$$\left(\operatorname{Log}[d + ex]^3 \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + 3 \operatorname{Log}[d + ex]^2 \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] - 6 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[3, \frac{g(d + ex)}{-ef + dg}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g(d + ex)}{-ef + dg}\right] \right) +$$

$$b^4n^4 \left(\operatorname{Log}[d + ex]^4 \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + 4 \operatorname{Log}[d + ex]^3 \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] - 12 \operatorname{Log}[d + ex]^2 \operatorname{PolyLog}\left[3, \frac{g(d + ex)}{-ef + dg}\right] + \right.$$

$$\left. \left. 24 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[4, \frac{g(d + ex)}{-ef + dg}\right] - 24 \operatorname{PolyLog}\left[5, \frac{g(d + ex)}{-ef + dg}\right] \right) \right)$$

Problem 63: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c(d + ex)^n])^4}{(f + gx)^2} dx$$

Optimal (type 4, 248 leaves, 6 steps):

$$\frac{(d + ex)(a + b \operatorname{Log}[c(d + ex)^n])^4}{(ef - dg)(f + gx)} - \frac{4ben(a + b \operatorname{Log}[c(d + ex)^n])^3 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right]}{g(ef - dg)} - \frac{12b^2e n^2(a + b \operatorname{Log}[c(d + ex)^n])^2 \operatorname{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g(ef - dg)} +$$

$$\frac{24b^3e n^3(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g(ef - dg)} - \frac{24b^4e n^4 \operatorname{PolyLog}\left[4, -\frac{g(d+ex)}{ef-dg}\right]}{g(ef - dg)}$$

Result (type 4, 531 leaves):

$$\frac{1}{g(e f - d g)(f + g x)} \left(- (e f - d g) (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^4 + 4 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 \right. \\ \left. \left(g (d + e x) \operatorname{Log}[d + e x] - e (f + g x) \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] \right) + 6 b^2 n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right. \\ \left. \left(\operatorname{Log}[d + e x] \left(g (d + e x) \operatorname{Log}[d + e x] - 2 e (f + g x) \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] \right) - 2 e (f + g x) \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) + \right. \\ \left. 4 b^3 n^3 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(\operatorname{Log}[d + e x]^2 \left(g (d + e x) \operatorname{Log}[d + e x] - 3 e (f + g x) \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] \right) - \right. \right. \\ \left. \left. 6 e (f + g x) \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] + 6 e (f + g x) \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) + \right. \\ \left. b^4 n^4 \left(g (d + e x) \operatorname{Log}[d + e x]^4 - 4 e (f + g x) \operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] - 12 e (f + g x) \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] + \right. \right. \\ \left. \left. 24 e (f + g x) \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] - 24 e (f + g x) \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \right) \right)$$

Problem 71: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[-\frac{g(d+ex)}{ef-dg}\right]}{f+gx} dx$$

Optimal (type 4, 24 leaves, 2 steps):

$$\frac{\operatorname{PolyLog}\left[2, \frac{e(f+gx)}{ef-dg}\right]}{g}$$

Result (type 4, 61 leaves):

$$\frac{\operatorname{Log}\left[\frac{g(d+ex)}{-ef+dg}\right] \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + \operatorname{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right]}{g}$$

Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{(f+gx)^3}{(a+b \operatorname{Log}[c(d+ex)^n])^2} dx$$

Optimal (type 4, 339 leaves, 26 steps):

$$\begin{aligned}
& \frac{e^{-\frac{a}{bn}} (ef - dg)^3 (d + ex) (c(d + ex)^n)^{-1/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right]}{b^2 e^4 n^2} + \\
& \frac{6 e^{-\frac{2a}{bn}} g (ef - dg)^2 (d + ex)^2 (c(d + ex)^n)^{-2/n} \text{ExpIntegralEi}\left[\frac{2(a + b \text{Log}[c(d + ex)^n])}{bn}\right]}{b^2 e^4 n^2} + \\
& \frac{9 e^{-\frac{3a}{bn}} g^2 (ef - dg) (d + ex)^3 (c(d + ex)^n)^{-3/n} \text{ExpIntegralEi}\left[\frac{3(a + b \text{Log}[c(d + ex)^n])}{bn}\right]}{b^2 e^4 n^2} + \\
& \frac{4 e^{-\frac{4a}{bn}} g^3 (d + ex)^4 (c(d + ex)^n)^{-4/n} \text{ExpIntegralEi}\left[\frac{4(a + b \text{Log}[c(d + ex)^n])}{bn}\right]}{b^2 e^4 n^2} - \frac{(d + ex) (f + gx)^3}{b e n (a + b \text{Log}[c(d + ex)^n])}
\end{aligned}$$

Result (type 4, 1674 leaves):

$$\begin{aligned}
& \frac{1}{b^2 e^4 n^2 (a + b \text{Log}[c(d + ex)^n])} \\
& e^{-\frac{4a}{bn}} (c(d + ex)^n)^{-4/n} \left(-b d e^3 e^{\frac{4a}{bn}} f^3 n (c(d + ex)^n)^{4/n} - b e^4 e^{\frac{4a}{bn}} f^3 n x (c(d + ex)^n)^{4/n} - 3 b d e^3 e^{\frac{4a}{bn}} f^2 g n x (c(d + ex)^n)^{4/n} - \right. \\
& 3 b e^4 e^{\frac{4a}{bn}} f^2 g n x^2 (c(d + ex)^n)^{4/n} - 3 b d e^3 e^{\frac{4a}{bn}} f g^2 n x^2 (c(d + ex)^n)^{4/n} - 3 b e^4 e^{\frac{4a}{bn}} f g^2 n x^3 (c(d + ex)^n)^{4/n} - b d e^3 e^{\frac{4a}{bn}} g^3 n x^3 (c(d + ex)^n)^{4/n} - \\
& \left. b e^4 e^{\frac{4a}{bn}} g^3 n x^4 (c(d + ex)^n)^{4/n} + a e^3 e^{\frac{3a}{bn}} f^3 (d + ex) (c(d + ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] - \right. \\
& 3 a d e^2 e^{\frac{3a}{bn}} f^2 g (d + ex) (c(d + ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] + \\
& 3 a d^2 e e^{\frac{3a}{bn}} f g^2 (d + ex) (c(d + ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] - a d^3 e^{\frac{3a}{bn}} g^3 (d + ex) (c(d + ex)^n)^{3/n} \\
& \left. \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] + 6 a e^2 e^{\frac{2a}{bn}} f^2 g (d + ex)^2 (c(d + ex)^n)^{2/n} \text{ExpIntegralEi}\left[\frac{2(a + b \text{Log}[c(d + ex)^n])}{bn}\right] - \right. \\
& 12 a d e e^{\frac{2a}{bn}} f g^2 (d + ex)^2 (c(d + ex)^n)^{2/n} \text{ExpIntegralEi}\left[\frac{2(a + b \text{Log}[c(d + ex)^n])}{bn}\right] + 6 a d^2 e^{\frac{2a}{bn}} g^3 (d + ex)^2 (c(d + ex)^n)^{2/n} \\
& \left. \text{ExpIntegralEi}\left[\frac{2(a + b \text{Log}[c(d + ex)^n])}{bn}\right] + 9 a e e^{\frac{a}{bn}} f g^2 (d + ex)^3 (c(d + ex)^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left[\frac{3(a + b \text{Log}[c(d + ex)^n])}{bn}\right] - \right. \\
& 9 a d e^{\frac{a}{bn}} g^3 (d + ex)^3 (c(d + ex)^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left[\frac{3(a + b \text{Log}[c(d + ex)^n])}{bn}\right] + 4 a g^3 (d + ex)^4 \text{ExpIntegralEi}\left[\frac{4(a + b \text{Log}[c(d + ex)^n])}{bn}\right] + \\
& \left. b e^3 e^{\frac{3a}{bn}} f^3 (d + ex) (c(d + ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] \text{Log}[c(d + ex)^n] - \right. \\
& \left. 3 b d e^2 e^{\frac{3a}{bn}} f^2 g (d + ex) (c(d + ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a + b \text{Log}[c(d + ex)^n]}{bn}\right] \text{Log}[c(d + ex)^n] + \right.
\end{aligned}$$

$$\begin{aligned}
& 3 b d^2 e^{\frac{3a}{bn}} f g^2 (d+ex) (c(d+ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a+b \text{Log}[c(d+ex)^n]}{bn}\right] \text{Log}[c(d+ex)^n] - \\
& b d^3 e^{\frac{3a}{bn}} g^3 (d+ex) (c(d+ex)^n)^{3/n} \text{ExpIntegralEi}\left[\frac{a+b \text{Log}[c(d+ex)^n]}{bn}\right] \text{Log}[c(d+ex)^n] + \\
& 6 b e^2 e^{\frac{2a}{bn}} f^2 g (d+ex)^2 (c(d+ex)^n)^{2/n} \text{ExpIntegralEi}\left[\frac{2(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n] - \\
& 12 b d e e^{\frac{2a}{bn}} f g^2 (d+ex)^2 (c(d+ex)^n)^{2/n} \text{ExpIntegralEi}\left[\frac{2(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n] + \\
& 6 b d^2 e^{\frac{2a}{bn}} g^3 (d+ex)^2 (c(d+ex)^n)^{2/n} \text{ExpIntegralEi}\left[\frac{2(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n] + \\
& 9 b e e^{\frac{a}{bn}} f g^2 (d+ex)^3 (c(d+ex)^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left[\frac{3(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n] - \\
& 9 b d e^{\frac{a}{bn}} g^3 (d+ex)^3 (c(d+ex)^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left[\frac{3(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n] + \\
& 4 b g^3 (d+ex)^4 \text{ExpIntegralEi}\left[\frac{4(a+b \text{Log}[c(d+ex)^n])}{bn}\right] \text{Log}[c(d+ex)^n]
\end{aligned}$$

Problem 95: Result more than twice size of optimal antiderivative.

$$\int \frac{(f+gx)^2}{(a+b \text{Log}[c(d+ex)^n])^2} dx$$

Optimal (type 4, 259 leaves, 20 steps):

$$\begin{aligned}
& \frac{e^{-\frac{a}{bn}} (ef-dg)^2 (d+ex) (c(d+ex)^n)^{-1/n} \text{ExpIntegralEi}\left[\frac{a+b \text{Log}[c(d+ex)^n]}{bn}\right]}{b^2 e^3 n^2} + \\
& \frac{4 e^{-\frac{2a}{bn}} g (ef-dg) (d+ex)^2 (c(d+ex)^n)^{-2/n} \text{ExpIntegralEi}\left[\frac{2(a+b \text{Log}[c(d+ex)^n])}{bn}\right]}{b^2 e^3 n^2} + \\
& \frac{3 e^{-\frac{3a}{bn}} g^2 (d+ex)^3 (c(d+ex)^n)^{-3/n} \text{ExpIntegralEi}\left[\frac{3(a+b \text{Log}[c(d+ex)^n])}{bn}\right]}{b^2 e^3 n^2} - \frac{(d+ex) (f+gx)^2}{b e n (a+b \text{Log}[c(d+ex)^n])}
\end{aligned}$$

Result (type 4, 1015 leaves):

$$\begin{aligned}
& \frac{1}{b^2 e^3 n^2 (a + b \operatorname{Log}[c (d + e x)^n])} e^{-\frac{3a}{bn}} (c (d + e x)^n)^{-3/n} \\
& \left(-b d e^2 e^{\frac{3a}{bn}} f^2 n (c (d + e x)^n)^{3/n} - b e^3 e^{\frac{3a}{bn}} f^2 n x (c (d + e x)^n)^{3/n} - 2 b d e^2 e^{\frac{3a}{bn}} f g n x (c (d + e x)^n)^{3/n} - 2 b e^3 e^{\frac{3a}{bn}} f g n x^2 (c (d + e x)^n)^{3/n} - \right. \\
& b d e^2 e^{\frac{3a}{bn}} g^2 n x^2 (c (d + e x)^n)^{3/n} - b e^3 e^{\frac{3a}{bn}} g^2 n x^3 (c (d + e x)^n)^{3/n} + a e^2 e^{\frac{2a}{bn}} f^2 (d + e x) (c (d + e x)^n)^{2/n} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] - \\
& 2 a d e e^{\frac{2a}{bn}} f g (d + e x) (c (d + e x)^n)^{2/n} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] + a d^2 e^{\frac{2a}{bn}} g^2 (d + e x) (c (d + e x)^n)^{2/n} \\
& \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] + 4 a e e^{\frac{a}{bn}} f g (d + e x)^2 (c (d + e x)^n)^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] - \\
& 4 a d e^{\frac{a}{bn}} g^2 (d + e x)^2 (c (d + e x)^n)^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] + 3 a g^2 (d + e x)^3 \operatorname{ExpIntegralEi}\left[\frac{3 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] + \\
& b e^2 e^{\frac{2a}{bn}} f^2 (d + e x) (c (d + e x)^n)^{2/n} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] \operatorname{Log}[c (d + e x)^n] - \\
& 2 b d e e^{\frac{2a}{bn}} f g (d + e x) (c (d + e x)^n)^{2/n} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] \operatorname{Log}[c (d + e x)^n] + \\
& b d^2 e^{\frac{2a}{bn}} g^2 (d + e x) (c (d + e x)^n)^{2/n} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d + e x)^n]}{bn}\right] \operatorname{Log}[c (d + e x)^n] + \\
& 4 b e e^{\frac{a}{bn}} f g (d + e x)^2 (c (d + e x)^n)^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] \operatorname{Log}[c (d + e x)^n] - \\
& 4 b d e^{\frac{a}{bn}} g^2 (d + e x)^2 (c (d + e x)^n)^{\frac{1}{n}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] \operatorname{Log}[c (d + e x)^n] + \\
& \left. 3 b g^2 (d + e x)^3 \operatorname{ExpIntegralEi}\left[\frac{3 (a + b \operatorname{Log}[c (d + e x)^n])}{bn}\right] \operatorname{Log}[c (d + e x)^n] \right)
\end{aligned}$$

Problem 105: Unable to integrate problem.

$$\int (f + g x)^2 \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} dx$$

Optimal (type 4, 404 leaves, 17 steps):

$$\begin{aligned}
& - \frac{\sqrt{b} e^{-\frac{a}{bn}} (ef - dg)^2 \sqrt{n} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e^3} \\
& - \frac{\sqrt{b} e^{-\frac{2a}{bn}} g (ef - dg) \sqrt{n} \sqrt{\frac{\pi}{2}} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e^3} \\
& + \frac{\sqrt{b} e^{-\frac{3a}{bn}} g^2 \sqrt{n} \sqrt{\frac{\pi}{3}} (d + ex)^3 (c (d + ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{6 e^3} + \frac{(ef - dg)^2 (d + ex) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{e^3} \\
& + \frac{g (ef - dg) (d + ex)^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{e^3} + \frac{g^2 (d + ex)^3 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{3 e^3}
\end{aligned}$$

Result (type 8, 28 leaves):

$$\int (f + gx)^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} \, dx$$

Problem 106: Unable to integrate problem.

$$\int (f + gx) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} \, dx$$

Optimal (type 4, 255 leaves, 12 steps):

$$\begin{aligned}
& - \frac{\sqrt{b} e^{-\frac{a}{bn}} (ef - dg) \sqrt{n} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e^2} \\
& - \frac{\sqrt{b} e^{-\frac{2a}{bn}} g \sqrt{n} \sqrt{\frac{\pi}{2}} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e^2} \\
& + \frac{(ef - dg) (d + ex) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{e^2} + \frac{g (d + ex)^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{2 e^2}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int (f + gx) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} \, dx$$

Problem 107: Unable to integrate problem.

$$\int \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} \, dx$$

Optimal (type 4, 111 leaves, 5 steps):

$$-\frac{\sqrt{b} e^{-\frac{a}{bn}} \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2e} + \frac{(d+ex) \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{e}$$

Result (type 8, 20 leaves):

$$\int \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} dx$$

Problem 111: Unable to integrate problem.

$$\int (f+gx)^2 (a+b \operatorname{Log}[c(d+ex)^n])^{3/2} dx$$

Optimal (type 4, 526 leaves, 20 steps):

$$\begin{aligned} & \frac{3b^{3/2} e^{-\frac{a}{bn}} (ef-dg)^2 n^{3/2} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4e^3} + \\ & \frac{3b^{3/2} e^{-\frac{2a}{bn}} g (ef-dg) n^{3/2} \sqrt{\frac{\pi}{2}} (d+ex)^2 (c(d+ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8e^3} + \\ & \frac{b^{3/2} e^{-\frac{3a}{bn}} g^2 n^{3/2} \sqrt{\frac{\pi}{3}} (d+ex)^3 (c(d+ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{12e^3} - \frac{3b (ef-dg)^2 n (d+ex) \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{2e^3} - \\ & \frac{3bg (ef-dg) n (d+ex)^2 \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{4e^3} - \frac{bg^2 n (d+ex)^3 \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{6e^3} + \\ & \frac{(ef-dg)^2 (d+ex) (a+b \operatorname{Log}[c(d+ex)^n])^{3/2}}{e^3} + \frac{g (ef-dg) (d+ex)^2 (a+b \operatorname{Log}[c(d+ex)^n])^{3/2}}{e^3} + \frac{g^2 (d+ex)^3 (a+b \operatorname{Log}[c(d+ex)^n])^{3/2}}{3e^3} \end{aligned}$$

Result (type 8, 28 leaves):

$$\int (f+gx)^2 (a+b \operatorname{Log}[c(d+ex)^n])^{3/2} dx$$

Problem 112: Unable to integrate problem.

$$\int (f+gx) (a+b \operatorname{Log}[c(d+ex)^n])^{3/2} dx$$

Optimal (type 4, 330 leaves, 14 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{bn}} (ef - dg) n^{3/2} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e^2} +$$

$$\frac{3 b^{3/2} e^{-\frac{2a}{bn}} g n^{3/2} \sqrt{\frac{\pi}{2}} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{16 e^2} - \frac{3 b (ef - dg) n (d + ex) \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{2 e^2} -$$

$$\frac{3 b g n (d + ex)^2 \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{8 e^2} + \frac{(ef - dg) (d + ex) (a+b \operatorname{Log}[c (d+ex)^n])^{3/2}}{e^2} + \frac{g (d + ex)^2 (a+b \operatorname{Log}[c (d+ex)^n])^{3/2}}{2 e^2}$$

Result (type 8, 26 leaves):

$$\int (f + gx) (a + b \operatorname{Log}[c (d + ex)^n])^{3/2} dx$$

Problem 113: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d + ex)^n])^{3/2} dx$$

Optimal (type 4, 143 leaves, 6 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{bn}} n^{3/2} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e} -$$

$$\frac{3 b n (d + ex) \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{2 e} + \frac{(d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{e}$$

Result (type 8, 20 leaves):

$$\int (a + b \operatorname{Log}[c (d + ex)^n])^{3/2} dx$$

Problem 117: Unable to integrate problem.

$$\int (f + gx)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Optimal (type 4, 660 leaves, 23 steps):

$$\frac{15 b^{5/2} e^{-\frac{a}{bn}} (ef - dg)^2 n^{5/2} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e^3}$$

$$\frac{15 b^{5/2} e^{-\frac{2a}{bn}} g (ef - dg) n^{5/2} \sqrt{\frac{\pi}{2}} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{32 e^3}$$

$$\frac{5 b^{5/2} e^{-\frac{3a}{bn}} g^2 n^{5/2} \sqrt{\frac{\pi}{3}} (d + ex)^3 (c (d + ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{72 e^3} + \frac{15 b^2 (ef - dg)^2 n^2 (d + ex) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{4 e^3} +$$

$$\frac{15 b^2 g (ef - dg) n^2 (d + ex)^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{16 e^3} + \frac{5 b^2 g^2 n^2 (d + ex)^3 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{36 e^3} -$$

$$\frac{5 b (ef - dg)^2 n (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{2 e^3} - \frac{5 b g (ef - dg) n (d + ex)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{4 e^3} -$$

$$\frac{5 b g^2 n (d + ex)^3 (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{18 e^3} + \frac{(ef - dg)^2 (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{e^3} +$$

$$\frac{g (ef - dg) (d + ex)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{e^3} + \frac{g^2 (d + ex)^3 (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{3 e^3}$$

Result (type 8, 28 leaves):

$$\int (f + gx)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Problem 118: Unable to integrate problem.

$$\int (f + gx) (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Optimal (type 4, 413 leaves, 16 steps):

$$\begin{aligned}
& - \frac{15 b^{5/2} e^{-\frac{a}{bn}} (ef - dg) n^{5/2} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e^2} \\
& + \frac{15 b^{5/2} e^{-\frac{2a}{bn}} g n^{5/2} \sqrt{\frac{\pi}{2}} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{64 e^2} + \frac{15 b^2 (ef - dg) n^2 (d + ex) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{4 e^2} + \\
& - \frac{15 b^2 g n^2 (d + ex)^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{32 e^2} - \frac{5 b (ef - dg) n (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{2 e^2} - \\
& + \frac{5 b g n (d + ex)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{8 e^2} + \frac{(ef - dg) (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{e^2} + \frac{g (d + ex)^2 (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{2 e^2}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int (f + gx) (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Problem 119: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Optimal (type 4, 179 leaves, 7 steps):

$$\begin{aligned}
& - \frac{15 b^{5/2} e^{-\frac{a}{bn}} n^{5/2} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e} + \\
& - \frac{15 b^2 n^2 (d + ex) \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{4 e} - \frac{5 b n (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}}{2 e} + \frac{(d + ex) (a + b \operatorname{Log}[c (d + ex)^n])^{5/2}}{e}
\end{aligned}$$

Result (type 8, 20 leaves):

$$\int (a + b \operatorname{Log}[c (d + ex)^n])^{5/2} dx$$

Problem 123: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + gx)^3}{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}} dx$$

Optimal (type 4, 383 leaves, 18 steps):

$$\frac{e^{-\frac{a}{bn}} (ef - dg)^3 \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^4 \sqrt{n}} +$$

$$\frac{e^{-\frac{4a}{bn}} g^3 \sqrt{\pi} (d+ex)^4 (c(d+ex)^n)^{-4/n} \operatorname{Erfi}\left[\frac{2\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2\sqrt{b} e^4 \sqrt{n}} + \frac{3 e^{-\frac{2a}{bn}} g (ef - dg)^2 \sqrt{\frac{\pi}{2}} (d+ex)^2 (c(d+ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^4 \sqrt{n}} +$$

$$\frac{e^{-\frac{3a}{bn}} g^2 (ef - dg) \sqrt{3\pi} (d+ex)^3 (c(d+ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^4 \sqrt{n}}$$

Result (type 4, 1485 leaves):

$$\left(e^{-\frac{a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} f^3 \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} \right) /$$

$$\left(\sqrt{b} e \sqrt{n} \sqrt{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])} \right) +$$

$$\left(3 e^{-\frac{2(a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} f^2 g \sqrt{\pi} \left(-2 d e^{\frac{a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \right) + \right.$$

$$\left. \sqrt{2} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \right) \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} \right) /$$

$$\left(2 \sqrt{b} e^2 \sqrt{n} \sqrt{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])} \right) + \frac{1}{e^3 (a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n]))}$$

$$e^{-\frac{3(a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} f g^2 \sqrt{\pi} \left(\sqrt{3} - 3 \sqrt{2} d e^{\frac{a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} + 3 d^2 e^{\frac{2(a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} - \right.$$

$$3 d^2 e^{\frac{2(a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} \operatorname{Erf}\left[\sqrt{-\frac{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}}\right] +$$

$$3 \sqrt{2} d e^{\frac{a-b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}}\right] -$$

$$\left. \sqrt{3} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+bn \operatorname{Log}[d+ex] + b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n])}{bn}}\right] \right)$$

$$\begin{aligned}
& \frac{\sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}}{1} \\
& 2 e^4 (a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])) \\
& e^{-\frac{4(a+b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} g^3 \sqrt{\pi} \left(-1 + 2 \sqrt{3} d e^{\frac{a-b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} - 3 \sqrt{2} d^2 e^{\frac{2(a+b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} + \right. \\
& \left. 2 d^3 e^{\frac{3(a+b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} - 2 d^3 e^{\frac{3(a+b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} \operatorname{Erf}\left[\sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}\right] + \right. \\
& \left. \operatorname{Erf}\left[2 \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}\right] + \right. \\
& \left. 3 \sqrt{2} d^2 e^{\frac{2(a+b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}\right] - \right. \\
& \left. 2 \sqrt{3} d e^{\frac{a-b(-n \operatorname{Log}[d+e x]+\operatorname{Log}[c(d+e x)^n])}{b n}} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}\right] \right) \\
& \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{b n}}
\end{aligned}$$

Problem 124: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x)^2}{\sqrt{a + b \operatorname{Log}[c (d + e x)^n]} dx$$

Optimal (type 4, 283 leaves, 14 steps):

$$\frac{e^{-\frac{a}{bn}} (ef - dg)^2 \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^3 \sqrt{n}} +$$

$$\frac{e^{-\frac{2a}{bn}} g (ef - dg) \sqrt{2\pi} (d+ex)^2 (c(d+ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^3 \sqrt{n}} + \frac{e^{-\frac{3a}{bn}} g^2 \sqrt{\frac{\pi}{3}} (d+ex)^3 (c(d+ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} e^3 \sqrt{n}}$$

Result (type 4, 573 leaves):

$$\frac{1}{3e^3} e^{-\frac{3a}{bn}} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-3/n} \left(\frac{3e^2 e^{\frac{2a}{bn}} f^2 (c(d+ex)^n)^{2/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} \sqrt{n}} - \frac{1}{\sqrt{b} \sqrt{n}} 3e e^{\frac{a}{bn}} fg (c(d+ex)^n)^{\frac{1}{n}} \right.$$

$$\left. \left(\frac{2d e^{\frac{a}{bn}} (c(d+ex)^n)^{\frac{1}{n}} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{\sqrt{b} \sqrt{n}} - \sqrt{2} (d+ex) \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]} \right) + \frac{1}{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}$$

$$g^2 (d+ex)^2 \left(\sqrt{3} - \frac{3\sqrt{2} d e^{\frac{a}{bn}} (c(d+ex)^n)^{\frac{1}{n}}}{d+ex} + \frac{3d^2 e^{\frac{2a}{bn}} (c(d+ex)^n)^{2/n}}{(d+ex)^2} - \frac{3d^2 e^{\frac{2a}{bn}} (c(d+ex)^n)^{2/n} \operatorname{Erf}\left[\sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right]}{(d+ex)^2} + \right.$$

$$\left. \frac{3\sqrt{2} d e^{\frac{a}{bn}} (c(d+ex)^n)^{\frac{1}{n}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right]}{d+ex} - \sqrt{3} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \right) \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int \frac{(f+gx)^3}{(a+b \operatorname{Log}[c(d+ex)^n])^{3/2}} dx$$

Optimal (type 4, 422 leaves, 33 steps):

$$\frac{2 e^{-\frac{a}{bn}} (ef - dg)^3 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^4 n^{3/2}} + \frac{4 e^{-\frac{4a}{bn}} g^3 \sqrt{\pi} (d + ex)^4 (c (d + ex)^n)^{-4/n} \operatorname{Erfi}\left[\frac{2\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^4 n^{3/2}} +$$

$$\frac{6 e^{-\frac{2a}{bn}} g (ef - dg)^2 \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^4 n^{3/2}} +$$

$$\frac{6 e^{-\frac{3a}{bn}} g^2 (ef - dg) \sqrt{3\pi} (d + ex)^3 (c (d + ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^4 n^{3/2}} - \frac{2 (d + ex) (f + gx)^3}{b e n \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}$$

Result (type 4, 2217 leaves):

$$\frac{1}{b^{3/2} e^4 n^{3/2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}$$

$$2 e^{-\frac{4a}{bn}} (c (d + ex)^n)^{-4/n} \left(-\sqrt{b} d e^3 e^{\frac{4a}{bn}} f^3 \sqrt{n} (c (d + ex)^n)^{4/n} - \sqrt{b} e^4 e^{\frac{4a}{bn}} f^3 \sqrt{n} x (c (d + ex)^n)^{4/n} - 3 \sqrt{b} d e^3 e^{\frac{4a}{bn}} f^2 g \sqrt{n} x (c (d + ex)^n)^{4/n} - \right.$$

$$3 \sqrt{b} e^4 e^{\frac{4a}{bn}} f^2 g \sqrt{n} x^2 (c (d + ex)^n)^{4/n} - 3 \sqrt{b} d e^3 e^{\frac{4a}{bn}} f g^2 \sqrt{n} x^2 (c (d + ex)^n)^{4/n} -$$

$$3 \sqrt{b} e^4 e^{\frac{4a}{bn}} f g^2 \sqrt{n} x^3 (c (d + ex)^n)^{4/n} - \sqrt{b} d e^3 e^{\frac{4a}{bn}} g^3 \sqrt{n} x^3 (c (d + ex)^n)^{4/n} - \sqrt{b} e^4 e^{\frac{4a}{bn}} g^3 \sqrt{n} x^4 (c (d + ex)^n)^{4/n} +$$

$$e^3 e^{\frac{3a}{bn}} f^3 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{3/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} -$$

$$3 d e^2 e^{\frac{3a}{bn}} f^2 g \sqrt{\pi} (d + ex) (c (d + ex)^n)^{3/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} -$$

$$6 d^2 e e^{\frac{3a}{bn}} f g^2 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{3/n} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} +$$

$$3 e^2 e^{\frac{2a}{bn}} f^2 g \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} +$$

$$3 d e e^{\frac{2a}{bn}} f g^2 \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} +$$

$$2 \sqrt{b} g^3 \sqrt{n} \sqrt{\pi} (d + ex)^4 \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} + 3 \sqrt{b} e e^{\frac{a}{bn}} f g^2 \sqrt{n} \sqrt{3\pi} (d + ex)^3 (c (d + ex)^n)^{\frac{1}{n}} \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} -$$

$$\begin{aligned}
& 3 \sqrt{b} d e^{\frac{a}{bn}} g^3 \sqrt{n} \sqrt{3\pi} (d+ex)^3 (c(d+ex)^n)^{\frac{1}{n}} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \\
& 9 \sqrt{b} d e e^{\frac{2a}{bn}} f g^2 \sqrt{n} \sqrt{2\pi} (d+ex)^2 (c(d+ex)^n)^{2/n} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} + \\
& 3 \sqrt{b} d^2 e^{\frac{2a}{bn}} g^3 \sqrt{n} \sqrt{2\pi} (d+ex)^2 (c(d+ex)^n)^{2/n} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} + 9 \sqrt{b} d^2 e e^{\frac{3a}{bn}} f g^2 \sqrt{n} \sqrt{\pi} (d+ex) \\
& (c(d+ex)^n)^{3/n} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \sqrt{b} d^3 e^{\frac{3a}{bn}} g^3 \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{3/n} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \\
& 9 \sqrt{b} d^2 e e^{\frac{3a}{bn}} f g^2 \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{3/n} \operatorname{Erf}\left[\sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} + \\
& \sqrt{b} d^3 e^{\frac{3a}{bn}} g^3 \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{3/n} \operatorname{Erf}\left[\sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \\
& 2 \sqrt{b} g^3 \sqrt{n} \sqrt{\pi} (d+ex)^4 \operatorname{Erf}\left[2 \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} + \\
& 9 \sqrt{b} d e e^{\frac{2a}{bn}} f g^2 \sqrt{n} \sqrt{2\pi} (d+ex)^2 (c(d+ex)^n)^{2/n} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \\
& 3 \sqrt{b} d^2 e^{\frac{2a}{bn}} g^3 \sqrt{n} \sqrt{2\pi} (d+ex)^2 (c(d+ex)^n)^{2/n} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} - \\
& 3 \sqrt{b} e e^{\frac{a}{bn}} f g^2 \sqrt{n} \sqrt{3\pi} (d+ex)^3 (c(d+ex)^n)^{\frac{1}{n}} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}} + \\
& 3 \sqrt{b} d e e^{\frac{a}{bn}} g^3 \sqrt{n} \sqrt{3\pi} (d+ex)^3 (c(d+ex)^n)^{\frac{1}{n}} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d+ex)^n]}{bn}}
\end{aligned}$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x)^2}{(a + b \operatorname{Log}[c (d + e x)^n])^{3/2}} dx$$

Optimal (type 4, 325 leaves, 25 steps):

$$\frac{2 e^{-\frac{a}{bn}} (ef - dg)^2 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^3 n^{3/2}} +$$

$$\frac{4 e^{-\frac{2a}{bn}} g (ef - dg) \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^3 n^{3/2}} +$$

$$\frac{2 e^{-\frac{3a}{bn}} g^2 \sqrt{3\pi} (d + ex)^3 (c (d + ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{3/2} e^3 n^{3/2}} - \frac{2 (d + ex) (f + g x)^2}{b e n \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}$$

Result (type 4, 1319 leaves):

$$\begin{aligned}
& \frac{1}{b^{3/2} e^3 n^{3/2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}} \\
& 2 e^{-\frac{3a}{bn}} (c (d + ex)^n)^{-3/n} \left(-\sqrt{b} d e^2 e^{\frac{3a}{bn}} f^2 \sqrt{n} (c (d + ex)^n)^{3/n} - \sqrt{b} e^3 e^{\frac{3a}{bn}} f^2 \sqrt{n} x (c (d + ex)^n)^{3/n} - 2 \sqrt{b} d e^2 e^{\frac{3a}{bn}} f g \sqrt{n} x (c (d + ex)^n)^{3/n} - \right. \\
& 2 \sqrt{b} e^3 e^{\frac{3a}{bn}} f g \sqrt{n} x^2 (c (d + ex)^n)^{3/n} - \sqrt{b} d e^2 e^{\frac{3a}{bn}} g^2 \sqrt{n} x^2 (c (d + ex)^n)^{3/n} - \sqrt{b} e^3 e^{\frac{3a}{bn}} g^2 \sqrt{n} x^3 (c (d + ex)^n)^{3/n} + \\
& e^2 e^{\frac{2a}{bn}} f^2 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{2/n} \operatorname{Erfi} \left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}} \right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} - \\
& 2 d e e^{\frac{2a}{bn}} f g \sqrt{\pi} (d + ex) (c (d + ex)^n)^{2/n} \operatorname{Erfi} \left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}} \right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} - \\
& 2 d^2 e^{\frac{2a}{bn}} g^2 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{2/n} \operatorname{Erfi} \left[\frac{\sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}} \right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} + \\
& 2 e e^{\frac{a}{bn}} f g \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{\frac{1}{n}} \operatorname{Erfi} \left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}} \right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} + \\
& d e^{\frac{a}{bn}} g^2 \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{\frac{1}{n}} \operatorname{Erfi} \left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}}{\sqrt{b} \sqrt{n}} \right] \sqrt{a + b \operatorname{Log}[c (d + ex)^n]} + \\
& \sqrt{b} g^2 \sqrt{n} \sqrt{3\pi} (d + ex)^3 \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} - 3 \sqrt{b} d e^{\frac{a}{bn}} g^2 \sqrt{n} \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{\frac{1}{n}} \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} + \\
& 3 \sqrt{b} d^2 e^{\frac{2a}{bn}} g^2 \sqrt{n} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{2/n} \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} - \\
& 3 \sqrt{b} d^2 e^{\frac{2a}{bn}} g^2 \sqrt{n} \sqrt{\pi} (d + ex) (c (d + ex)^n)^{2/n} \operatorname{Erf} \left[\sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} \right] \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} + \\
& 3 \sqrt{b} d e^{\frac{a}{bn}} g^2 \sqrt{n} \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{\frac{1}{n}} \operatorname{Erf} \left[\sqrt{2} \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} \right] \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} - \\
& \left. \sqrt{b} g^2 \sqrt{n} \sqrt{3\pi} (d + ex)^3 \operatorname{Erf} \left[\sqrt{3} \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} \right] \sqrt{-\frac{a + b \operatorname{Log}[c (d + ex)^n]}{bn}} \right)
\end{aligned}$$

Problem 133: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x)^3}{(a + b \operatorname{Log}[c (d + e x)^n])^{5/2}} dx$$

Optimal (type 4, 520 leaves, 59 steps):

$$\begin{aligned} & \frac{4 e^{-\frac{a}{bn}} (ef - dg)^3 \sqrt{\pi} (d + ex) (c (d + ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{3 b^{5/2} e^4 n^{5/2}} + \frac{32 e^{-\frac{4a}{bn}} g^3 \sqrt{\pi} (d + ex)^4 (c (d + ex)^n)^{-4/n} \operatorname{Erfi}\left[\frac{2\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{3 b^{5/2} e^4 n^{5/2}} + \\ & \frac{8 e^{-\frac{2a}{bn}} g (ef - dg)^2 \sqrt{2\pi} (d + ex)^2 (c (d + ex)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{5/2} e^4 n^{5/2}} + \\ & \frac{12 e^{-\frac{3a}{bn}} g^2 (ef - dg) \sqrt{3\pi} (d + ex)^3 (c (d + ex)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{5/2} e^4 n^{5/2}} - \\ & \frac{2 (d + ex) (f + gx)^3}{3 b e n (a + b \operatorname{Log}[c (d + ex)^n])^{3/2}} + \frac{4 (ef - dg) (d + ex) (f + gx)^2}{b^2 e^2 n^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}} - \frac{16 (d + ex) (f + gx)^3}{3 b^2 e n^2 \sqrt{a + b \operatorname{Log}[c (d + ex)^n]}} \end{aligned}$$

Result (type 4, 2997 leaves):

$$\begin{aligned} & \left(4 e^{-\frac{a-b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}{bn}} f^3 \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} \right) / \\ & \left(3 b^{5/2} e n^{5/2} \sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])} \right) + \\ & \left(12 d e^{-\frac{a-b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}{bn}} f^2 g \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} \right) / \\ & \left(b^{5/2} e^2 n^{5/2} \sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])} \right) + \\ & \left(8 d^2 e^{-\frac{a-b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}{bn}} f g^2 \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} \right) / \\ & \left(b^{5/2} e^3 n^{5/2} \sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])} \right) + \\ & \left(8 e^{-\frac{2(a-b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}{bn}} f^2 g \sqrt{\pi} \left(-2 d e^{-\frac{a-b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}{bn}} \operatorname{Erfi}\left[\frac{\sqrt{a+bn \operatorname{Log}[d+ex]+b(-n \operatorname{Log}[d+ex]+\operatorname{Log}[c(d+ex)^n])}}{\sqrt{b} \sqrt{n}}\right] \right) \right) + \end{aligned}$$

$$\begin{aligned}
& \left. \sqrt{2} \operatorname{Erfi} \left[\frac{\sqrt{2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}}{\sqrt{b} \sqrt{n}} \right] \right) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \Big/ \\
& \left(b^{5/2} e^2 n^{5/2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \right) + \\
& \left(20 d e^{-\frac{2(a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn})} f g^2 \sqrt{\pi} \left(-2 d e^{\frac{a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn}} \operatorname{Erfi} \left[\frac{\sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}}{\sqrt{b} \sqrt{n}} \right] \right) + \right. \\
& \left. \sqrt{2} \operatorname{Erfi} \left[\frac{\sqrt{2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}}{\sqrt{b} \sqrt{n}} \right] \right) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \Big/ \\
& \left(b^{5/2} e^3 n^{5/2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \right) + \\
& \left(4 d^2 e^{-\frac{2(a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn})} g^3 \sqrt{\pi} \left(-2 d e^{\frac{a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn}} \operatorname{Erfi} \left[\frac{\sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}}{\sqrt{b} \sqrt{n}} \right] \right) + \right. \\
& \left. \sqrt{2} \operatorname{Erfi} \left[\frac{\sqrt{2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}}{\sqrt{b} \sqrt{n}} \right] \right) \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \Big/ \\
& \left(b^{5/2} e^4 n^{5/2} \sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \right) + \frac{1}{b^2 e^3 n^2 (a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \\
& 12 e^{-\frac{3(a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn})} f g^2 \sqrt{\pi} \left(\sqrt{3} - 3\sqrt{2} d e^{\frac{a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn}} + 3 d^2 e^{\frac{2(a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn})} - \right. \\
& 3 d^2 e^{\frac{2(a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn})} \operatorname{Erf} \left[\sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{bn}} \right] + \\
& 3 \sqrt{2} d e^{\frac{a-b(-n \operatorname{Log}[d+e x] + \operatorname{Log}[c(d+e x)^n])}{bn}} \operatorname{Erf} \left[\sqrt{2} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{bn}} \right] - \\
& \left. \sqrt{3} \operatorname{Erf} \left[\sqrt{3} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{bn}} \right] \right) \\
& \sqrt{a + b \operatorname{Log}[c (d + e x)^n]} \sqrt{-\frac{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])}{bn}} +
\end{aligned}$$

$$\begin{aligned}
& \left(28 d e^{-\frac{3(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} g^3 \sqrt{\pi} \left(\sqrt{3} - 3\sqrt{2} d e^{\frac{a-b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} + 3 d^2 e^{\frac{2(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} - \right. \right. \\
& 3 d^2 e^{\frac{2(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} \operatorname{Erf} \left[\sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] + \\
& 3\sqrt{2} d e^{\frac{a-b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \operatorname{Erf} \left[\sqrt{2} \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] - \\
& \left. \left. \sqrt{3} \operatorname{Erf} \left[\sqrt{3} \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] \right) \sqrt{a+b\log[c(d+ex)^n]} \right. \\
& \left. \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] / (3b^2 e^4 n^2 (a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n]))) - \\
& \left(32 e^{-\frac{4(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} g^3 \sqrt{\pi} \left(-1 + 2\sqrt{3} d e^{\frac{a-b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} - 3\sqrt{2} d^2 e^{\frac{2(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} + 2 d^3 e^{\frac{3(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} - \right. \right. \\
& 2 d^3 e^{\frac{3(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} \operatorname{Erf} \left[\sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] + \\
& \operatorname{Erf} \left[2 \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] + \\
& 3\sqrt{2} d^2 e^{\frac{2(a-b(-n\log[d+ex]+\log[c(d+ex)^n]))}{bn}} \operatorname{Erf} \left[\sqrt{2} \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] - \\
& \left. \left. 2\sqrt{3} d e^{\frac{a-b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \operatorname{Erf} \left[\sqrt{3} \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] \right) \right. \\
& \left. \sqrt{a+b\log[c(d+ex)^n]} \sqrt{-\frac{a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n])}{bn}} \right] / \\
& (3b^2 e^4 n^2 (a+bn\log[d+ex]+b(-n\log[d+ex]+\log[c(d+ex)^n]))) +
\end{aligned}$$

$$\sqrt{a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \left(-\frac{2 (d + e x) (f + g x)^3}{3 b e n (a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])^2} - \frac{4 (d + e x) (f + g x)^2 (e f + 3 d g + 4 e g x)}{3 b^2 e^2 n^2 (a + b n \operatorname{Log}[d + e x] + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n])} \right)$$

Problem 134: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x)^2}{(a + b \operatorname{Log}[c (d + e x)^n])^{5/2}} dx$$

Optimal (type 4, 421 leaves, 41 steps):

$$\frac{4 e^{-\frac{a}{bn}} (e f - d g)^2 \sqrt{\pi} (d + e x) (c (d + e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{3 b^{5/2} e^3 n^{5/2}} +$$

$$\frac{16 e^{-\frac{2a}{bn}} g (e f - d g) \sqrt{2 \pi} (d + e x)^2 (c (d + e x)^n)^{-2/n} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{3 b^{5/2} e^3 n^{5/2}} +$$

$$\frac{4 e^{-\frac{3a}{bn}} g^2 \sqrt{3 \pi} (d + e x)^3 (c (d + e x)^n)^{-3/n} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right]}{b^{5/2} e^3 n^{5/2}} -$$

$$\frac{2 (d + e x) (f + g x)^2}{3 b e n (a + b \operatorname{Log}[c (d + e x)^n])^{3/2}} + \frac{8 (e f - d g) (d + e x) (f + g x)}{3 b^2 e^2 n^2 \sqrt{a + b \operatorname{Log}[c (d + e x)^n]}} - \frac{4 (d + e x) (f + g x)^2}{b^2 e n^2 \sqrt{a + b \operatorname{Log}[c (d + e x)^n]}}$$

Result (type 4, 951 leaves):

$$\begin{aligned}
& \frac{1}{3 b^{5/2} e^3 n^{5/2}} 2 (d+e x) \\
& \left(2 e^2 e^{-\frac{a}{b n}} f^2 \sqrt{\pi} (c (d+e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] + 12 d e e^{-\frac{a}{b n}} f g \sqrt{\pi} (c (d+e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] + \right. \\
& 4 d^2 e^{-\frac{a}{b n}} g^2 \sqrt{\pi} (c (d+e x)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] - 10 d e^{-\frac{2 a}{b n}} g^2 \sqrt{\pi} (c (d+e x)^n)^{-2/n} \\
& \left. \left(2 d e^{\frac{a}{b n}} (c (d+e x)^n)^{\frac{1}{n}} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] - \sqrt{2} (d+e x) \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] \right) + 8 e e^{-\frac{2 a}{b n}} f g \sqrt{\pi} \right. \\
& \left. (c (d+e x)^n)^{-2/n} \left(-2 d e^{\frac{a}{b n}} (c (d+e x)^n)^{\frac{1}{n}} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] + \sqrt{2} (d+e x) \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c (d+e x)^n]}}{\sqrt{b} \sqrt{n}}\right] \right) + \right. \\
& \frac{1}{\sqrt{a+b \operatorname{Log}[c (d+e x)^n]}} 6 \sqrt{b} e^{-\frac{3 a}{b n}} g^2 \sqrt{n} \sqrt{\pi} (d+e x)^2 (c (d+e x)^n)^{-3/n} \\
& \left(\sqrt{3} - \frac{3 \sqrt{2} d e^{\frac{a}{b n}} (c (d+e x)^n)^{\frac{1}{n}}}{d+e x} + \frac{3 d^2 e^{\frac{2 a}{b n}} (c (d+e x)^n)^{2/n}}{(d+e x)^2} - \frac{3 d^2 e^{\frac{2 a}{b n}} (c (d+e x)^n)^{2/n} \operatorname{Erf}\left[\sqrt{-\frac{a+b \operatorname{Log}[c (d+e x)^n]}{b n}}\right]}{(d+e x)^2} + \right. \\
& \frac{3 \sqrt{2} d e^{\frac{a}{b n}} (c (d+e x)^n)^{\frac{1}{n}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+b \operatorname{Log}[c (d+e x)^n]}{b n}}\right]}{d+e x} - \sqrt{3} \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+b \operatorname{Log}[c (d+e x)^n]}{b n}}\right] \left. \right) \sqrt{-\frac{a+b \operatorname{Log}[c (d+e x)^n]}{b n}} - \\
& \left. \left(\sqrt{b} e \sqrt{n} (f+g x) (b e n (f+g x) + 2 a (e f+2 d g+3 e g x) + 2 b (2 d g+e (f+3 g x)) \operatorname{Log}[c (d+e x)^n]) \right) / (a+b \operatorname{Log}[c (d+e x)^n])^{3/2} \right)
\end{aligned}$$

Problem 145: Result unnecessarily involves higher level functions.

$$\int (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])^2 dx$$

Optimal (type 4, 590 leaves, 28 steps):

$$\begin{aligned} & \frac{368 b^2 (e f - d g)^2 n^2 \sqrt{f + g x}}{75 e^2 g} + \frac{128 b^2 (e f - d g) n^2 (f + g x)^{3/2}}{225 e g} + \frac{16 b^2 n^2 (f + g x)^{5/2}}{125 g} - \frac{368 b^2 (e f - d g)^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{75 e^{5/2} g} \\ & - \frac{8 b^2 (e f - d g)^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{5 e^{5/2} g} - \frac{8 b (e f - d g)^2 n \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])}{5 e^2 g} \\ & - \frac{8 b (e f - d g) n (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])}{15 e g} - \frac{8 b n (f + g x)^{5/2} (a + b \operatorname{Log}[c (d + e x)^n])}{25 g} + \\ & \frac{8 b (e f - d g)^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{5 e^{5/2} g} + \frac{2 (f + g x)^{5/2} (a + b \operatorname{Log}[c (d + e x)^n])^2}{5 g} + \\ & \frac{16 b^2 (e f - d g)^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{5 e^{5/2} g} + \frac{8 b^2 (e f - d g)^{5/2} n^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{5 e^{5/2} g} \end{aligned}$$

Result (type 5, 1143 leaves):

$$\begin{aligned} & \frac{1}{225 g} 2 \left(\frac{1}{e^2 \sqrt{\frac{e (f + g x)}{e f - d g}}} 15 b^2 n^2 \sqrt{f + g x} \left(10 g (-e f + d g) (d + e x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] - 15 d^2 g^2 \right. \right. \\ & \left. \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] - 15 d e g^2 x \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] \right) + \\ & 4 e^2 f^2 \operatorname{Log}[d + e x] - 8 d e f g \operatorname{Log}[d + e x] + 4 d^2 g^2 \operatorname{Log}[d + e x] - 4 e^2 f^2 \sqrt{\frac{e (f + g x)}{e f - d g}} \operatorname{Log}[d + e x] - 8 e^2 f g x \sqrt{\frac{e (f + g x)}{e f - d g}} \operatorname{Log}[d + e x] - \\ & 4 e^2 g^2 x^2 \sqrt{\frac{e (f + g x)}{e f - d g}} \operatorname{Log}[d + e x] + 15 d^2 g^2 \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] \operatorname{Log}[d + e x] + \end{aligned}$$

$$\begin{aligned}
& 15 d e g^2 x \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g(d+ex)}{-ef+dg}\right] \operatorname{Log}[d+ex] + 2 e^2 f^2 \operatorname{Log}[d+ex]^2 + d e f g \operatorname{Log}[d+ex]^2 - \\
& 3 d^2 g^2 \operatorname{Log}[d+ex]^2 - 2 e^2 f^2 \sqrt{\frac{e(f+gx)}{ef-dg}} \operatorname{Log}[d+ex]^2 + e^2 f g x \sqrt{\frac{e(f+gx)}{ef-dg}} \operatorname{Log}[d+ex]^2 + 3 e^2 g^2 x^2 \sqrt{\frac{e(f+gx)}{ef-dg}} \operatorname{Log}[d+ex]^2 - \\
& 10 g(-ef+dg)(d+ex) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1\right\}, \{2, 2\}, \frac{g(d+ex)}{-ef+dg}\right] (1 + \operatorname{Log}[d+ex]) \Bigg) + \frac{1}{e \sqrt{\frac{e(f+gx)}{ef-dg}}} \\
& 75 b^2 f n^2 \sqrt{f+gx} \left(3 g(d+ex) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g(d+ex)}{-ef+dg}\right] + \operatorname{Log}[d+ex] \left(-3 g(d+ex) \right. \right. \\
& \left. \left. \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g(d+ex)}{-ef+dg}\right] + \left(d g + e g x \sqrt{\frac{e(f+gx)}{ef-dg}} + e f \left(-1 + \sqrt{\frac{e(f+gx)}{ef-dg}} \right) \right) \operatorname{Log}[d+ex] \right) \right) - \\
& \frac{1}{e^{3/2}} 50 b f n \left(6 (ef-dg)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+gx}}{\sqrt{ef-dg}}\right] + \sqrt{e} \sqrt{f+gx} (6 dg - 2 e (4 f + g x) + 3 e (f + g x) \operatorname{Log}[d + e x]) \right) \\
& (-a + b n \operatorname{Log}[d + e x] - b \operatorname{Log}[c (d + e x)^n]) + \\
& \frac{1}{e^{5/2}} 2 b n \left(30 \sqrt{ef-dg} (2 e^2 f^2 + d e f g - 3 d^2 g^2) \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+gx}}{\sqrt{ef-dg}}\right] + \right. \\
& \left. \sqrt{e} \sqrt{f+gx} (90 d^2 g^2 - 30 d e g (2 f + g x) + 2 e^2 (-31 f^2 + 8 f g x + 9 g^2 x^2) + 15 e^2 (2 f^2 - f g x - 3 g^2 x^2) \operatorname{Log}[d + e x]) \right) \\
& \left. (-a + b n \operatorname{Log}[d + e x] - b \operatorname{Log}[c (d + e x)^n]) + 45 (f + g x)^{5/2} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right)
\end{aligned}$$

Problem 146: Result unnecessarily involves higher level functions.

$$\int \sqrt{f+gx} (a + b \operatorname{Log}[c (d+ex)^n])^2 dx$$

Optimal (type 4, 510 leaves, 21 steps):

$$\begin{aligned}
& \frac{64 b^2 (e f - d g) n^2 \sqrt{f + g x}}{9 e g} + \frac{16 b^2 n^2 (f + g x)^{3/2}}{27 g} - \frac{64 b^2 (e f - d g)^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{9 e^{3/2} g} - \\
& \frac{8 b^2 (e f - d g)^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{3 e^{3/2} g} - \frac{8 b (e f - d g) n \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])}{3 e g} - \frac{8 b n (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])}{9 g} + \\
& \frac{8 b (e f - d g)^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{3 e^{3/2} g} + \frac{2 (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])^2}{3 g} + \\
& \frac{16 b^2 (e f - d g)^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{3 e^{3/2} g} + \frac{8 b^2 (e f - d g)^{3/2} n^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{3 e^{3/2} g}
\end{aligned}$$

Result (type 5, 351 leaves):

$$\begin{aligned}
& \frac{1}{9 g} 2 \left(\frac{1}{e \sqrt{\frac{e (f + g x)}{e f - d g}}} \right. \\
& 3 b^2 n^2 \sqrt{f + g x} \left(3 g (d + e x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] + \operatorname{Log}[d + e x] \left(-3 g (d + e x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] + \left(d g + e g x \sqrt{\frac{e (f + g x)}{e f - d g}} + e f \left(-1 + \sqrt{\frac{e (f + g x)}{e f - d g}} \right) \right) \operatorname{Log}[d + e x] \right) \right) - \\
& \frac{1}{e^{3/2}} 2 b n \left(6 (e f - d g)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] + \sqrt{e} \sqrt{f + g x} (6 d g - 2 e (4 f + g x) + 3 e (f + g x) \operatorname{Log}[d + e x]) \right) \\
& \left. (-a + b n \operatorname{Log}[d + e x] - b \operatorname{Log}[c (d + e x)^n]) + 3 (f + g x)^{3/2} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right)
\end{aligned}$$

Problem 147: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{\sqrt{f + g x}} dx$$

Optimal (type 4, 418 leaves, 15 steps):

$$\begin{aligned} & \frac{16 b^2 n^2 \sqrt{f + g x}}{g} - \frac{16 b^2 \sqrt{e f - d g} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{\sqrt{e} g} - \frac{8 b^2 \sqrt{e f - d g} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{\sqrt{e} g} \\ & + \frac{8 b n \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])}{g} + \frac{8 b \sqrt{e f - d g} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{\sqrt{e} g} + \\ & + \frac{2 \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])^2}{g} + \frac{16 b^2 \sqrt{e f - d g} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{\sqrt{e} g} + \frac{8 b^2 \sqrt{e f - d g} n^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{\sqrt{e} g} \end{aligned}$$

Result (type 5, 301 leaves):

$$\begin{aligned} & \frac{1}{e g \sqrt{f + g x}} 2 \left(b^2 n^2 \sqrt{\frac{e (f + g x)}{e f - d g}} \left(g (d + e x) \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] - \right. \right. \\ & \quad \left. \left. g (d + e x) \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] \operatorname{Log}[d + e x] + (e f - d g) \left(-1 + \sqrt{\frac{e (f + g x)}{e f - d g}}\right) \operatorname{Log}[d + e x]^2 \right) + \right. \\ & \quad \left. 2 b n \sqrt{f + g x} \left(2 \sqrt{e} \sqrt{e f - d g} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] + e \sqrt{f + g x} (-2 + \operatorname{Log}[d + e x]) \right) (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \right. \\ & \quad \left. e (f + g x) (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right) \end{aligned}$$

Problem 148: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{(f + g x)^{3/2}} dx$$

Optimal (type 4, 312 leaves, 10 steps):

$$\frac{8 b^2 \sqrt{e} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]^2}{g \sqrt{e f-d g}} - \frac{8 b \sqrt{e} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] (a+b \operatorname{Log}[c (d+e x)^n])}{g \sqrt{e f-d g}} - \frac{2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{g \sqrt{f+g x}} - \frac{16 b^2 \sqrt{e} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{g \sqrt{e f-d g}} - \frac{8 b^2 \sqrt{e} n^2 \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{g \sqrt{e f-d g}}$$

Result (type 5, 342 leaves):

$$\frac{1}{g} 2 \left(\frac{1}{\sqrt{e f-d g} (f+g x)} 2 b n \left(2 \sqrt{e} (f+g x) \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] + \sqrt{e f-d g} \sqrt{f+g x} \operatorname{Log}[d+e x] \right) (-a+b n \operatorname{Log}[d+e x] - b \operatorname{Log}[c (d+e x)^n]) - \frac{(a-b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n])^2}{\sqrt{f+g x}} + \frac{1}{(e f-d g) \sqrt{f+g x}} \right. \\ \left. b^2 n^2 \left(g (d+e x) \sqrt{\frac{e (f+g x)}{e f-d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{3}{2}\right\}, \{2, 2, 2\}, \frac{g (d+e x)}{-e f+d g}\right] + (e f-d g) \operatorname{Log}[d+e x] \left(\left(-1 + \sqrt{\frac{e (f+g x)}{e f-d g}} \right) \operatorname{Log}[d+e x] - 4 \sqrt{\frac{e (f+g x)}{e f-d g}} \operatorname{Log}\left[\frac{1}{2} \left(1 + \sqrt{\frac{e (f+g x)}{e f-d g}} \right) \right] \right) \right) \right)$$

Problem 149: Result unnecessarily involves higher level functions.

$$\int \frac{(a+b \operatorname{Log}[c (d+e x)^n])^2}{(f+g x)^{5/2}} dx$$

Optimal (type 4, 423 leaves, 14 steps):

$$\frac{16 b^2 e^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]}{3 g (e f-d g)^{3/2}} + \frac{8 b^2 e^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]^2}{3 g (e f-d g)^{3/2}} +$$

$$\frac{8 b e n (a+b \operatorname{Log}[c (d+e x)^n])}{3 g (e f-d g) \sqrt{f+g x}} - \frac{8 b e^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] (a+b \operatorname{Log}[c (d+e x)^n])}{3 g (e f-d g)^{3/2}} -$$

$$\frac{2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{3 g (f+g x)^{3/2}} - \frac{16 b^2 e^{3/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{3 g (e f-d g)^{3/2}} - \frac{8 b^2 e^{3/2} n^2 \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{3 g (e f-d g)^{3/2}}$$

Result (type 5, 419 leaves):

$$\frac{1}{3 g (e f-d g)^2 (f+g x)^{3/2}} 2 \left(-2 b \sqrt{e f-d g} n \left(2 e^{3/2} (f+g x)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] - \sqrt{e f-d g} (2 e (f+g x) + (-e f+d g) \operatorname{Log}[d+e x]) \right) \right.$$

$$\left. (a-b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n]) - (e f-d g)^2 (a-b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n])^2 + \right.$$

$$\left. b^2 n^2 \left(3 e g (d+e x) (f+g x) \sqrt{\frac{e (f+g x)}{e f-d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{5}{2}\right\}, \left\{2, 2, 2\right\}, \frac{g (d+e x)}{-e f+d g}\right] + \right.$$

$$\left. (e f-d g) \operatorname{Log}[d+e x] \left(\left(d g+e g x \sqrt{\frac{e (f+g x)}{e f-d g}} + e f \left(-1 + \sqrt{\frac{e (f+g x)}{e f-d g}} \right) \right) \operatorname{Log}[d+e x] - \right.$$

$$\left. \left. 4 e (f+g x) \left(-1 + \sqrt{\frac{e (f+g x)}{e f-d g}} + \sqrt{\frac{e (f+g x)}{e f-d g}} \operatorname{Log}\left[\frac{1}{2} \left(1 + \sqrt{\frac{e (f+g x)}{e f-d g}} \right) \right] \right) \right) \right)$$

Problem 150: Result unnecessarily involves higher level functions.

$$\int \frac{(a+b \operatorname{Log}[c (d+e x)^n])^2}{(f+g x)^{7/2}} dx$$

Optimal (type 4, 503 leaves, 19 steps):

$$\begin{aligned}
& - \frac{16 b^2 e^2 n^2}{15 g (e f - d g)^2 \sqrt{f + g x}} + \frac{64 b^2 e^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{15 g (e f - d g)^{5/2}} + \frac{8 b^2 e^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{5 g (e f - d g)^{5/2}} + \\
& \frac{8 b e n (a + b \operatorname{Log}[c (d + e x)^n])}{15 g (e f - d g) (f + g x)^{3/2}} + \frac{8 b e^2 n (a + b \operatorname{Log}[c (d + e x)^n])}{5 g (e f - d g)^2 \sqrt{f + g x}} - \frac{8 b e^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{5 g (e f - d g)^{5/2}} - \\
& \frac{2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{5 g (f + g x)^{5/2}} - \frac{16 b^2 e^{5/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{5 g (e f - d g)^{5/2}} - \frac{8 b^2 e^{5/2} n^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{5 g (e f - d g)^{5/2}}
\end{aligned}$$

Result (type 5, 705 leaves):

$$\begin{aligned}
& \frac{1}{5 g (e f - d g)^3 (e f + e g x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e}}} \\
& 2 b^2 e^2 n^2 \left(5 g (d + e x) (e f + e g x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{7}{2}\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] - \right. \\
& 5 g (d + e x) (e f + e g x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, \frac{7}{2}\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] \operatorname{Log}[d + e x] + \\
& (e f - d g) \left(e^2 f^2 \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) - 2 e f g \left(-(d + e x) \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + d \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) \right) \right) + \\
& g^2 \left(-2 d (d + e x) \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + (d + e x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + d^2 \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) \right) \operatorname{Log}[d + e x]^2 + \frac{1}{15 g} \\
& 4 b e^{5/2} n \left(-\frac{6 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{\frac{e f - d g + g (d + e x)}{e}}}{\sqrt{e f - d g}}\right]}{(e f - d g)^{5/2}} + \frac{\sqrt{e} \sqrt{\frac{e f - d g + g (d + e x)}{e}} (2 (e f - d g) (e f + e g x) + 6 (e f + e g x)^2 - 3 (e f - d g)^2 \operatorname{Log}[d + e x])}{(e f - d g)^2 (e f + e g x)^3} \right) \\
& \frac{(a + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n]) - 2 (a + b (-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n]))^2}{5 g (f + g x)^{5/2}}
\end{aligned}$$

Problem 151: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{(f + g x)^{9/2}} dx$$

Optimal (type 4, 583 leaves, 25 steps):

$$\begin{aligned}
& - \frac{16 b^2 e^2 n^2}{105 g (e f - d g)^2 (f + g x)^{3/2}} - \frac{128 b^2 e^3 n^2}{105 g (e f - d g)^3 \sqrt{f + g x}} + \frac{368 b^2 e^{7/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{105 g (e f - d g)^{7/2}} + \\
& \frac{8 b^2 e^{7/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{7 g (e f - d g)^{7/2}} + \frac{8 b e n (a + b \operatorname{Log}[c (d + e x)^n])}{35 g (e f - d g) (f + g x)^{5/2}} + \frac{8 b e^2 n (a + b \operatorname{Log}[c (d + e x)^n])}{21 g (e f - d g)^2 (f + g x)^{3/2}} + \\
& \frac{8 b e^3 n (a + b \operatorname{Log}[c (d + e x)^n])}{7 g (e f - d g)^3 \sqrt{f + g x}} - \frac{8 b e^{7/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{7 g (e f - d g)^{7/2}} - \\
& \frac{2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{7 g (f + g x)^{7/2}} - \frac{16 b^2 e^{7/2} n^2 \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{7 g (e f - d g)^{7/2}} - \frac{8 b^2 e^{7/2} n^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{7 g (e f - d g)^{7/2}}
\end{aligned}$$

Result (type 5, 894 leaves):

$$\begin{aligned}
& \frac{1}{7 g (e f - d g)^4 (e f + e g x)^3 \sqrt{\frac{e f - d g + g (d + e x)}{e}}} \\
& 2 b^2 e^3 n^2 \left(7 g (d + e x) (e f + e g x)^3 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{9}{2}\right\}, \{2, 2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] - \right. \\
& \left. 7 g (d + e x) (e f + e g x)^3 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, \frac{9}{2}\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] \operatorname{Log}[d + e x] + \right. \\
& \left. (e f - d g) \left(e^3 f^3 \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) - 3 e^2 f^2 g \left(- (d + e x) \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + d \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) \right) \right) + \right. \\
& \left. 3 e f g^2 \left(-2 d (d + e x) \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + (d + e x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + d^2 \left(-1 + \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \right) \right) \right) + \\
& g^3 \left(3 d^2 (d + e x) \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} - 3 d (d + e x)^2 \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left((d+ex)^3 \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} - d^3 \left(-1 + \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \right) \right) \right) \text{Log}[d+ex]^2 + \\
& \frac{1}{105g} 4be^{7/2}n \left(-\frac{30 \text{ArcTanh}\left[\frac{\sqrt{e}\sqrt{\frac{ef-dg+g(d+ex)}{e}}}{\sqrt{ef-dg}}\right]}{(ef-dg)^{7/2}} + \frac{1}{(ef-dg)^3(ef+egx)^4} \sqrt{e}\sqrt{\frac{ef-dg+g(d+ex)}{e}} \right. \\
& \left. \left(6(ef-dg)^2(ef+egx) + 10(ef-dg)(ef+egx)^2 + 30(ef+egx)^3 - 15(ef-dg)^3 \text{Log}[d+ex] \right) \right) \\
& \left. \left(a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]) \right) - \frac{2(a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]))^2}{7g(f+gx)^{7/2}} \right)
\end{aligned}$$

Problem 187: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \text{Log}[c(e+fx)])^2}{de+dfx} dx$$

Optimal (type 3, 27 leaves, 4 steps):

$$\frac{(a+b \text{Log}[c(e+fx)])^3}{3bdf}$$

Result (type 3, 61 leaves):

$$\frac{a^2 \text{Log}[c(e+fx)]}{df} + \frac{ab \text{Log}[c(e+fx)]^2}{df} + \frac{b^2 \text{Log}[c(e+fx)]^3}{3df}$$

Problem 198: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f+gx)^{5/2} (a+b \text{Log}[c(d+ex)^n])}{d+ex} dx$$

Optimal (type 4, 485 leaves, 27 steps):

$$\begin{aligned}
 & - \frac{92 b (e f - d g)^2 n \sqrt{f + g x}}{15 e^3} - \frac{32 b (e f - d g) n (f + g x)^{3/2}}{45 e^2} - \frac{4 b n (f + g x)^{5/2}}{25 e} + \frac{92 b (e f - d g)^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{15 e^{7/2}} + \\
 & \frac{2 b (e f - d g)^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{e^{7/2}} + \frac{2 (e f - d g)^2 \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])}{e^3} + \frac{2 (e f - d g) (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])}{3 e^2} + \\
 & \frac{2 (f + g x)^{5/2} (a + b \operatorname{Log}[c (d + e x)^n])}{5 e} - \frac{2 (e f - d g)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{e^{7/2}} - \\
 & \frac{4 b (e f - d g)^{5/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{e^{7/2}} - \frac{2 b (e f - d g)^{5/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{e^{7/2}}
 \end{aligned}$$

Result (type 5, 2046 leaves):

$$\begin{aligned}
 & \frac{1}{e \sqrt{g} \sqrt{d + e x} \sqrt{\frac{e f + e g x}{g (d + e x)}}} 2 b f^2 n \sqrt{\frac{e f - d g + g (d + e x)}{e}} \\
 & \left(-2 \sqrt{g} \sqrt{d + e x} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-e f + d g}{g (d + e x)}\right] + \sqrt{g} \sqrt{d + e x} \sqrt{\frac{e f - d g + g (d + e x)}{g (d + e x)}} \operatorname{Log}[d + e x] - \right. \\
 & \left. \sqrt{e f - d g} \operatorname{ArcSinh}\left[\frac{\sqrt{e f - d g}}{\sqrt{g} \sqrt{d + e x}}\right] \operatorname{Log}[d + e x] \right) + \frac{1}{3 e^2 \sqrt{d + e x} \sqrt{\frac{e f + e g x}{g (d + e x)}} \sqrt{1 + \frac{g (d + e x)}{e f - d g}}} \\
 & 2 b f n \sqrt{\frac{e f - d g + g (d + e x)}{e}} \left(12 d g \sqrt{d + e x} \sqrt{\frac{e f - d g + g (d + e x)}{e f - d g}} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-e f + d g}{g (d + e x)}\right] - \right. \\
 & \left. 3 g (d + e x)^{3/2} \sqrt{\frac{e f + e g x}{g (d + e x)}} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g (d + e x)}{-e f + d g}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 2\sqrt{d+ex} \sqrt{\frac{ef+egx}{g(d+ex)}} \left(ef \left(-1 + \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \right) + g \left(d - 4d \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} + (d+ex) \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \right) \right) \\
& \left. \text{Log}[d+ex] + 6d\sqrt{g}\sqrt{ef-dg} \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \text{ArcSinh}\left[\frac{\sqrt{ef-dg}}{\sqrt{g}\sqrt{d+ex}}\right] \text{Log}[d+ex] \right) + \\
& \frac{1}{e^3} b g^2 n \left(-\frac{1}{\sqrt{1+\frac{g(d+ex)}{ef-dg}}} 2d(d+ex) \sqrt{\frac{ef-dg}{e} + \frac{g(d+ex)}{e}} \left(-\text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, -\frac{g(d+ex)}{ef-dg}\right] + \right. \right. \\
& \left. \frac{1}{3g(d+ex)} 2 \left(-ef+dg+ef \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} - dg \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + g(d+ex) \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} \right) \right. \\
& \left. \text{Log}[d+ex] \right) + \frac{1}{\sqrt{1+\frac{g(d+ex)}{ef-dg}}} (d+ex)^2 \sqrt{\frac{ef-dg}{e} + \frac{g(d+ex)}{e}} \\
& \left(\frac{1}{4} \left(-\frac{1}{15g^2(d+ex)^2} 16 \left(-e^2f^2 + 2defg - d^2g^2 + e^2f^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} - 2defg \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + \right. \right. \right. \\
& \left. d^2g^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + 2efg(d+ex) \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} - 2dg^2(d+ex) \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + \right. \\
& \left. \left. g^2(d+ex)^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} \right) - \frac{8(-ef+dg) \text{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1\right\}, \{2, 2\}, -\frac{g(d+ex)}{ef-dg}\right]}{3g(d+ex)} \right) + \frac{1}{15g^2(d+ex)^2} \\
& 2 \left(2e^2f^2 - 4defg + 2d^2g^2 - 2e^2f^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + 4defg \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} - 2d^2g^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + efg \right)
\end{aligned}$$

$$\begin{aligned}
& \left. (d+ex) \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} - dg^2(d+ex) \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} + 3g^2(d+ex)^2 \sqrt{\frac{-ef+dg-g(d+ex)}{-ef+dg}} \right) \text{Log}[d+ex] + \\
& \frac{1}{\sqrt{1+\frac{ef-dg}{g(d+ex)}}} d^2 \sqrt{\frac{ef-dg}{e} + \frac{g(d+ex)}{e}} \left(-4 \text{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2} \right\}, \left\{ \frac{1}{2}, \frac{1}{2} \right\}, -\frac{ef-dg}{g(d+ex)} \right] - \right. \\
& \left. \frac{2 \left(1 + \frac{ef-dg}{g(d+ex)} \right)^{3/2} \left(1 - \frac{\sqrt{ef-dg} \text{ArcSinh} \left[\frac{\sqrt{ef-dg}}{\sqrt{g} \sqrt{d+ex}} \right]}{\sqrt{g} \sqrt{d+ex} \sqrt{1+\frac{ef-dg}{g(d+ex)}}} \right) \text{Log}[d+ex]}{-1 - \frac{ef-dg}{g(d+ex)}} \right) \right) - \\
& \frac{2(ef-dg)^{5/2} \text{ArcTanh} \left[\frac{\sqrt{e} \sqrt{f+gx}}{\sqrt{ef-dg}} \right] (a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]))}{e^{7/2}} + \\
& \frac{\sqrt{f+gx}}{15e^3} \left(\frac{2(23e^2f^2 - 35defg + 15d^2g^2)(a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]))}{15e^3} + \right. \\
& \frac{2g(11ef - 5dg)x(a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]))}{15e^2} + \\
& \left. \frac{2g^2x^2(a+b(-n \text{Log}[d+ex] + \text{Log}[c(d+ex)^n]))}{5e} \right)
\end{aligned}$$

Problem 199: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f+gx)^{3/2} (a+b \text{Log}[c(d+ex)^n])}{d+ex} dx$$

Optimal (type 4, 417 leaves, 20 steps):

$$\begin{aligned}
& - \frac{16 b (e f - d g) n \sqrt{f + g x}}{3 e^2} - \frac{4 b n (f + g x)^{3/2}}{9 e} + \frac{16 b (e f - d g)^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]}{3 e^{5/2}} + \\
& \frac{2 b (e f - d g)^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right]^2}{e^{5/2}} + \frac{2 (e f - d g) \sqrt{f + g x} (a + b \operatorname{Log}[c (d + e x)^n])}{e^2} + \\
& \frac{2 (f + g x)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])}{3 e} - \frac{2 (e f - d g)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{e^{5/2}} - \\
& \frac{4 b (e f - d g)^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{e^{5/2}} - \frac{2 b (e f - d g)^{3/2} n \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}}}\right]}{e^{5/2}}
\end{aligned}$$

Result (type 5, 840 leaves):

$$\begin{aligned}
& \frac{1}{e \sqrt{g} \sqrt{d+ex} \sqrt{\frac{ef+egx}{g(d+ex)}}} - 2 b f n \sqrt{\frac{ef-dg+g(d+ex)}{e}} \\
& \left(-2 \sqrt{g} \sqrt{d+ex} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-ef+dg}{g(d+ex)}\right] + \sqrt{g} \sqrt{d+ex} \sqrt{\frac{ef-dg+g(d+ex)}{g(d+ex)}} \operatorname{Log}[d+ex] - \right. \\
& \left. \sqrt{ef-dg} \operatorname{ArcSinh}\left[\frac{\sqrt{ef-dg}}{\sqrt{g} \sqrt{d+ex}}\right] \operatorname{Log}[d+ex] \right) + \frac{1}{3 e^2 \sqrt{d+ex} \sqrt{\frac{ef+egx}{g(d+ex)}} \sqrt{1+\frac{g(d+ex)}{ef-dg}}} \\
& b n \sqrt{\frac{ef-dg+g(d+ex)}{e}} \left(12 d g \sqrt{d+ex} \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-ef+dg}{g(d+ex)}\right] - \right. \\
& 3 g (d+ex)^{3/2} \sqrt{\frac{ef+egx}{g(d+ex)}} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{g(d+ex)}{-ef+dg}\right] + \\
& \left. 2 \sqrt{d+ex} \sqrt{\frac{ef+egx}{g(d+ex)}} \left(e f \left(-1 + \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \right) + g \left(d - 4 d \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} + (d+ex) \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \right) \right) \right) \\
& \left. \operatorname{Log}[d+ex] + 6 d \sqrt{g} \sqrt{ef-dg} \sqrt{\frac{ef-dg+g(d+ex)}{ef-dg}} \operatorname{ArcSinh}\left[\frac{\sqrt{ef-dg}}{\sqrt{g} \sqrt{d+ex}}\right] \operatorname{Log}[d+ex] \right) - \\
& \frac{2 (ef-dg)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+gx}}{\sqrt{ef-dg}}\right] (a+b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n]))}{e^{5/2}} + \\
& \sqrt{f+gx} \left(\frac{2(4ef-3dg)(a+b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n]))}{3e^2} + \frac{2gx(a+b(-n \operatorname{Log}[d+ex] + \operatorname{Log}[c(d+ex)^n]))}{3e} \right)
\end{aligned}$$

Problem 200: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{f+gx} (a+b \operatorname{Log}[c(d+ex)^n])}{d+ex} dx$$

Optimal (type 4, 349 leaves, 14 steps):

$$\begin{aligned}
& -\frac{4bn\sqrt{f+gx}}{e} + \frac{4b\sqrt{ef-dg}n\operatorname{ArcTanh}\left[\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}\right]}{e^{3/2}} + \frac{2b\sqrt{ef-dg}n\operatorname{ArcTanh}\left[\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}\right]^2}{e^{3/2}} + \\
& \frac{2\sqrt{f+gx}(a+b\operatorname{Log}[c(d+ex)^n])}{e} - \frac{2\sqrt{ef-dg}\operatorname{ArcTanh}\left[\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}\right](a+b\operatorname{Log}[c(d+ex)^n])}{e^{3/2}} - \\
& \frac{4b\sqrt{ef-dg}n\operatorname{ArcTanh}\left[\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}\right]\operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}}\right]}{e^{3/2}} - \frac{2b\sqrt{ef-dg}n\operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}}\right]}{e^{3/2}}
\end{aligned}$$

Result (type 5, 268 leaves):

$$\begin{aligned}
& \frac{1}{e^2} \left(-\frac{2ben\sqrt{f+gx}\operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-ef+dg}{g(d+ex)}\right]}{\sqrt{\frac{e(f+gx)}{g(d+ex)}}} - \right. \\
& \frac{b\sqrt{g}\sqrt{ef-dg}n\sqrt{d+ex}\sqrt{\frac{e(f+gx)}{g(d+ex)}}\operatorname{ArcSinh}\left[\frac{\sqrt{ef-dg}}{\sqrt{g}\sqrt{d+ex}}\right]\operatorname{Log}[d+ex]}{\sqrt{f+gx}} + e\sqrt{f+gx}(a+b\operatorname{Log}[c(d+ex)^n]) - \\
& \left. \sqrt{e}\sqrt{ef-dg}\operatorname{ArcTanh}\left[\frac{\sqrt{e}\sqrt{f+gx}}{\sqrt{ef-dg}}\right](a-bn\operatorname{Log}[d+ex]+b\operatorname{Log}[c(d+ex)^n]) \right)
\end{aligned}$$

Problem 202: Result unnecessarily involves higher level functions.

$$\int \frac{a+b\operatorname{Log}[c(d+ex)^n]}{(d+ex)(f+gx)^{3/2}} dx$$

Optimal (type 4, 340 leaves, 13 steps):

$$\frac{4 b \sqrt{e} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]}{(e f-d g)^{3/2}} + \frac{2 b \sqrt{e} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]^2}{(e f-d g)^{3/2}} + \frac{2(a+b \operatorname{Log}[c(d+e x)^n])}{(e f-d g) \sqrt{f+g x}} -$$

$$\frac{2 \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right](a+b \operatorname{Log}[c(d+e x)^n])}{(e f-d g)^{3/2}} - \frac{4 b \sqrt{e} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{(e f-d g)^{3/2}} - \frac{2 b \sqrt{e} n \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{(e f-d g)^{3/2}}$$

Result (type 5, 267 leaves):

$$\frac{1}{9(f+g x)^{3/2}} {}_2F_1\left(-\frac{2 b n \left(\frac{e(f+g x)}{g(d+e x)}\right)^{3/2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, \frac{-e f+d g}{g(d+e x)}\right]}{e}\right) +$$

$$\frac{1}{(e f-d g)^{3/2}} 9(f+g x) \left(-b \sqrt{g} n \sqrt{d+e x} \sqrt{\frac{e(f+g x)}{g(d+e x)}} \operatorname{ArcSinh}\left[\frac{\sqrt{e f-d g}}{\sqrt{g} \sqrt{d+e x}}\right] \operatorname{Log}[d+e x] + \right.$$

$$\left. \sqrt{e f-d g} (a+b \operatorname{Log}[c(d+e x)^n]) - \sqrt{e} \sqrt{f+g x} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] (a-b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c(d+e x)^n]) \right)$$

Problem 203: Result unnecessarily involves higher level functions.

$$\int \frac{a+b \operatorname{Log}[c(d+e x)^n]}{(d+e x)(f+g x)^{5/2}} dx$$

Optimal (type 4, 406 leaves, 18 steps):

$$-\frac{4 b e n}{3(e f-d g)^2 \sqrt{f+g x}} + \frac{16 b e^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]}{3(e f-d g)^{5/2}} + \frac{2 b e^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right]^2}{(e f-d g)^{5/2}} +$$

$$\frac{2(a+b \operatorname{Log}[c(d+e x)^n])}{3(e f-d g)(f+g x)^{3/2}} + \frac{2 e(a+b \operatorname{Log}[c(d+e x)^n])}{(e f-d g)^2 \sqrt{f+g x}} - \frac{2 e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right](a+b \operatorname{Log}[c(d+e x)^n])}{(e f-d g)^{5/2}} -$$

$$\frac{4 b e^{3/2} n \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{(e f-d g)^{5/2}} - \frac{2 b e^{3/2} n \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{e} \sqrt{f+g x}}{\sqrt{e f-d g}}}\right]}{(e f-d g)^{5/2}}$$

Result (type 5, 487 leaves):

$$\begin{aligned}
 & - \left(\left(2 b n (e f + e g x) \left(6 (e f - d g)^3 (e f + e g x)^2 \text{HypergeometricPFQ} \left[\left\{ \frac{5}{2}, \frac{5}{2}, \frac{5}{2} \right\}, \left\{ \frac{7}{2}, \frac{7}{2} \right\}, \frac{-e f + d g}{g (d + e x)} \right] - \right. \right. \right. \\
 & \quad 25 g^3 (e f - d g)^2 (d + e x)^3 \sqrt{\frac{e f + e g x}{g (d + e x)}} \text{Log}[d + e x] + 75 g^4 (-e f + d g) (d + e x)^4 \left(\frac{e f + e g x}{g (d + e x)} \right)^{3/2} \text{Log}[d + e x] + \\
 & \quad \left. \left. \left. 75 g^{5/2} \sqrt{e f - d g} (d + e x)^{5/2} (e f + e g x)^2 \text{ArcSinh} \left[\frac{\sqrt{e f - d g}}{\sqrt{g} \sqrt{d + e x}} \right] \text{Log}[d + e x] \right) \right) \right) / \\
 & \left(75 e g^3 (e f - d g)^3 (d + e x)^3 \sqrt{\frac{e f + e g x}{g (d + e x)}} \left(\frac{e f - d g + g (d + e x)}{e} \right)^{5/2} \right) - \\
 & \frac{2 e^{3/2} \text{ArcTanh} \left[\frac{\sqrt{e} \sqrt{f + g x}}{\sqrt{e f - d g}} \right] (a + b (-n \text{Log}[d + e x] + \text{Log}[c (d + e x)^n]))}{(e f - d g)^{5/2}} + \\
 & \frac{\sqrt{f + g x}}{\left(-\frac{2 (a + b (-n \text{Log}[d + e x] + \text{Log}[c (d + e x)^n]))}{3 (-e f + d g) (f + g x)^2} + \frac{2 e (a + b (-n \text{Log}[d + e x] + \text{Log}[c (d + e x)^n]))}{(e f - d g)^2 (f + g x)} \right)}
 \end{aligned}$$

Problem 204: Result unnecessarily involves higher level functions.

$$\int \frac{(d + e x)^{3/2} \text{Log}[a + b x]}{a + b x} dx$$

Optimal (type 4, 381 leaves, 20 steps):

$$\begin{aligned}
 & - \frac{16 (b d - a e) \sqrt{d + e x}}{3 b^2} - \frac{4 (d + e x)^{3/2}}{9 b} + \frac{16 (b d - a e)^{3/2} \text{ArcTanh} \left[\frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}} \right]}{3 b^{5/2}} + \frac{2 (b d - a e)^{3/2} \text{ArcTanh} \left[\frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}} \right]^2}{b^{5/2}} + \\
 & \frac{2 (b d - a e) \sqrt{d + e x} \text{Log}[a + b x]}{b^2} + \frac{2 (d + e x)^{3/2} \text{Log}[a + b x]}{3 b} - \frac{2 (b d - a e)^{3/2} \text{ArcTanh} \left[\frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}} \right] \text{Log}[a + b x]}{b^{5/2}} - \\
 & \frac{4 (b d - a e)^{3/2} \text{ArcTanh} \left[\frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}} \right] \text{Log} \left[\frac{2}{1 - \frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}}} \right]}{b^{5/2}} - \frac{2 (b d - a e)^{3/2} \text{PolyLog} \left[2, 1 - \frac{2}{1 - \frac{\sqrt{b} \sqrt{d + e x}}{\sqrt{b d - a e}}} \right]}{b^{5/2}}
 \end{aligned}$$

Result (type 5, 407 leaves):

$$\frac{1}{3 b^3 \sqrt{d+e x} \sqrt{\frac{b(d+e x)}{b d-a e}}} \sqrt{e} \sqrt{a+b x} \sqrt{\frac{b(d+e x)}{e(a+b x)}} \left(-\frac{12 b \sqrt{e} \sqrt{a+b x} (d+e x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-b d+a e}{e(a+b x)}\right]}{\sqrt{\frac{b(d+e x)}{b d-a e}}} \right) -$$

$$3 e^{3/2} (a+b x)^{3/2} \sqrt{\frac{b(d+e x)}{e(a+b x)}} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{e(a+b x)}{-b d+a e}\right] +$$

$$2 \left(\sqrt{e} \sqrt{a+b x} \sqrt{\frac{b(d+e x)}{e(a+b x)}} \left(b e x \sqrt{\frac{b(d+e x)}{b d-a e}} + a e \left(1 - 3 \sqrt{\frac{b(d+e x)}{b d-a e}} \right) + b d \left(-1 + 4 \sqrt{\frac{b(d+e x)}{b d-a e}} \right) \right) \right) -$$

$$3 (b d-a e)^{3/2} \sqrt{\frac{b(d+e x)}{b d-a e}} \operatorname{ArcSinh}\left[\frac{\sqrt{b d-a e}}{\sqrt{e} \sqrt{a+b x}}\right] \operatorname{Log}[a+b x]$$

Problem 205: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{d+e x} \operatorname{Log}[a+b x]}{a+b x} dx$$

Optimal (type 4, 323 leaves, 14 steps):

$$\frac{4 \sqrt{d+e x}}{b} + \frac{4 \sqrt{b d-a e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}\right]}{b^{3/2}} + \frac{2 \sqrt{b d-a e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}\right]^2}{b^{3/2}} + \frac{2 \sqrt{d+e x} \operatorname{Log}[a+b x]}{b} -$$

$$\frac{2 \sqrt{b d-a e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}\right] \operatorname{Log}[a+b x]}{b^{3/2}} - \frac{4 \sqrt{b d-a e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}}\right]}{b^{3/2}} - \frac{2 \sqrt{b d-a e} \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{b} \sqrt{d+e x}}{\sqrt{b d-a e}}}\right]}{b^{3/2}}$$

Result (type 5, 186 leaves):

$$-\left(\left(2 (d+e x)^{3/2} \left(2 \sqrt{e} \sqrt{a+b x} \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}\right\}, \left\{\frac{1}{2}, \frac{1}{2}\right\}, \frac{-b d+a e}{e(a+b x)}\right] + \right. \right. \right.$$

$$\left. \left. \left(-\sqrt{e} \sqrt{a+b x} \sqrt{\frac{b(d+e x)}{e(a+b x)}} + \sqrt{b d-a e} \operatorname{ArcSinh}\left[\frac{\sqrt{b d-a e}}{\sqrt{e} \sqrt{a+b x}}\right] \right) \operatorname{Log}[a+b x] \right) \right) / \left(e^{3/2} (a+b x)^{3/2} \left(\frac{b(d+e x)}{e(a+b x)} \right)^{3/2} \right)$$

Problem 207: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Log}[a + b x]}{(a + b x) (d + e x)^{3/2}} dx$$

Optimal (type 4, 316 leaves, 13 steps):

$$\frac{4 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right]}{(bd-ae)^{3/2}} + \frac{2 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right]^2}{(bd-ae)^{3/2}} + \frac{2 \text{Log}[a + b x]}{(bd-ae) \sqrt{d+ex}} -$$

$$\frac{2 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right] \text{Log}[a + b x]}{(bd-ae)^{3/2}} - \frac{4 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right] \text{Log}\left[\frac{2}{1 - \frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}}\right]}{(bd-ae)^{3/2}} - \frac{2 \sqrt{b} \text{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}}\right]}{(bd-ae)^{3/2}}$$

Result (type 5, 183 leaves):

$$\frac{1}{9 \sqrt{d+ex}}$$

$$2 \left(\frac{2 \sqrt{\frac{b(d+ex)}{e(a+bx)}} \text{HypergeometricPFQ}\left[\left\{\frac{3}{2}, \frac{3}{2}, \frac{3}{2}\right\}, \left\{\frac{5}{2}, \frac{5}{2}\right\}, -\frac{bd-ae}{ae+bx}\right]}{ae+bx} + \frac{9 \left(\sqrt{bd-ae} - \sqrt{e} \sqrt{a+bx} \sqrt{\frac{b(d+ex)}{e(a+bx)}} \text{ArcSinh}\left[\frac{\sqrt{bd-ae}}{\sqrt{e} \sqrt{a+bx}}\right] \right) \text{Log}[a + b x]}{(bd-ae)^{3/2}} \right)$$

Problem 208: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Log}[a + b x]}{(a + b x) (d + e x)^{5/2}} dx$$

Optimal (type 4, 372 leaves, 18 steps):

$$-\frac{4b}{3(bd-ae)^2 \sqrt{d+ex}} + \frac{16b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right]}{3(bd-ae)^{5/2}} + \frac{2b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right]^2}{(bd-ae)^{5/2}} + \frac{2 \text{Log}[a + b x]}{3(bd-ae)(d+ex)^{3/2}} + \frac{2b \text{Log}[a + b x]}{(bd-ae)^2 \sqrt{d+ex}} -$$

$$\frac{2b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right] \text{Log}[a + b x]}{(bd-ae)^{5/2}} - \frac{4b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}\right] \text{Log}\left[\frac{2}{1 - \frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}}\right]}{(bd-ae)^{5/2}} - \frac{2b^{3/2} \text{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{b} \sqrt{d+ex}}{\sqrt{bd-ae}}}\right]}{(bd-ae)^{5/2}}$$

Result (type 5, 197 leaves):

$$\frac{1}{75 (d+ex)^{3/2}} \left(2 \left(- \frac{6 \left(\frac{b(d+ex)}{e(a+bx)} \right)^{3/2} \text{HypergeometricPFQ} \left[\left\{ \frac{5}{2}, \frac{5}{2}, \frac{5}{2} \right\}, \left\{ \frac{7}{2}, \frac{7}{2} \right\}, \frac{-bd+ae}{e(a+bx)} \right]}{e(a+bx)} + \right. \right. \\ \left. \left. \frac{25 \left(\sqrt{bd-ae} (4bd-ae+3bex) - 3e^{3/2} (a+bx)^{3/2} \left(\frac{b(d+ex)}{e(a+bx)} \right)^{3/2} \text{ArcSinh} \left[\frac{\sqrt{bd-ae}}{\sqrt{e} \sqrt{a+bx}} \right] \right) \text{Log}[a+bx]}{(bd-ae)^{5/2}} \right) \right)$$

Problem 225: Result more than twice size of optimal antiderivative.

$$\int \frac{(h+ix) (a+b \text{Log}[c(d+ex)^n])^2}{f+gx} dx$$

Optimal (type 4, 215 leaves, 10 steps):

$$- \frac{2abix}{g} + \frac{2b^2in^2x}{g} - \frac{2b^2in(d+ex) \text{Log}[c(d+ex)^n]}{eg} + \\ \frac{i(d+ex) (a+b \text{Log}[c(d+ex)^n])^2}{eg} + \frac{(gh-fi) (a+b \text{Log}[c(d+ex)^n])^2 \text{Log}\left[\frac{e(f+gx)}{ef-dg}\right]}{g^2} + \\ \frac{2b(gh-fi)n(a+b \text{Log}[c(d+ex)^n]) \text{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g^2} - \frac{2b^2(gh-fi)n^2 \text{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g^2}$$

Result (type 4, 451 leaves):

$$\frac{1}{eg^2} \left(egi x (a-bn \text{Log}[d+ex] + b \text{Log}[c(d+ex)^n])^2 + e(gh-fi) (a-bn \text{Log}[d+ex] + b \text{Log}[c(d+ex)^n])^2 \text{Log}[f+gx] + \right. \\ \left. 2b eghn (a-bn \text{Log}[d+ex] + b \text{Log}[c(d+ex)^n]) \left(\text{Log}[d+ex] \text{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + \text{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] \right) - 2bin \right. \\ \left. (a-bn \text{Log}[d+ex] + b \text{Log}[c(d+ex)^n]) \left(-g(d+ex) (-1 + \text{Log}[d+ex]) + ef \left(\text{Log}[d+ex] \text{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + \text{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] \right) \right) \right) + \\ b^2in^2 \left(g(d+ex) (2 - 2 \text{Log}[d+ex] + \text{Log}[d+ex]^2) - \right. \\ \left. ef \left(\text{Log}[d+ex]^2 \text{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + 2 \text{Log}[d+ex] \text{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] - 2 \text{PolyLog}\left[3, \frac{g(d+ex)}{-ef+dg}\right] \right) \right) + \\ b^2eghn^2 \left(\text{Log}[d+ex]^2 \text{Log}\left[\frac{e(f+gx)}{ef-dg}\right] + 2 \text{Log}[d+ex] \text{PolyLog}\left[2, \frac{g(d+ex)}{-ef+dg}\right] - 2 \text{PolyLog}\left[3, \frac{g(d+ex)}{-ef+dg}\right] \right) \right)$$

Problem 229: Result more than twice size of optimal antiderivative.

$$\int \frac{(h + i x)^2 (a + b \operatorname{Log}[c (d + e x)^n])^3}{f + g x} dx$$

Optimal (type 4, 660 leaves, 23 steps):

$$\begin{aligned} & \frac{6 a b^2 i (e h - d i) n^2 x}{e g} + \frac{6 a b^2 i (g h - f i) n^2 x}{g^2} - \frac{6 b^3 i (e h - d i) n^3 x}{e g} - \frac{6 b^3 i (g h - f i) n^3 x}{g^2} - \\ & \frac{3 b^3 i^2 n^3 (d + e x)^2}{8 e^2 g} + \frac{6 b^3 i (e h - d i) n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e^2 g} + \frac{6 b^3 i (g h - f i) n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e g^2} + \\ & \frac{3 b^2 i^2 n^2 (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{4 e^2 g} - \frac{3 b i (e h - d i) n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e^2 g} - \\ & \frac{3 b i (g h - f i) n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e g^2} - \frac{3 b i^2 n (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 e^2 g} + \\ & \frac{i (e h - d i) (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e^2 g} + \frac{i (g h - f i) (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e g^2} + \frac{i^2 (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])^3}{2 e^2 g} + \\ & \frac{(g h - f i)^2 (a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right]}{g^3} + \frac{3 b (g h - f i)^2 n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{g (d + e x)}{e f - d g}\right]}{g^3} - \\ & \frac{6 b^2 (g h - f i)^2 n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, -\frac{g (d + e x)}{e f - d g}\right]}{g^3} + \frac{6 b^3 (g h - f i)^2 n^3 \operatorname{PolyLog}\left[4, -\frac{g (d + e x)}{e f - d g}\right]}{g^3} \end{aligned}$$

Result (type 4, 1474 leaves):

$$\begin{aligned}
& \frac{1}{8 e^2 g^3} \left(8 e^2 g i (2 g h - f i) x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 + 4 e^2 g^2 i^2 x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 + \right. \\
& 8 e^2 (g h - f i)^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}[f + g x] + 24 b e^2 g^2 h^2 n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \\
& \left. \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) + 6 b i^2 n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \right. \\
& \left. \left(e g (e x (4 f - g x) + 2 d (2 f + g x)) - 2 \operatorname{Log}[d + e x] \left(g (d + e x) (2 e f + d g - e g x) - 2 e^2 f^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] \right) + 4 e^2 f^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) - \right. \\
& 48 b e g h i n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \\
& \left. \left(-g (d + e x) (-1 + \operatorname{Log}[d + e x]) + e f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) \right) + \\
& 48 b^2 e g h i n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(g (d + e x) (2 - 2 \operatorname{Log}[d + e x] + \operatorname{Log}[d + e x]^2) - \right. \\
& \left. e f \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 2 \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) - \\
& 6 b^2 i^2 n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(4 e f g (d + e x) (2 - 2 \operatorname{Log}[d + e x] + \operatorname{Log}[d + e x]^2) - \right. \\
& g^2 (e x (-6 d + e x) + (6 d^2 + 4 d e x - 2 e^2 x^2) \operatorname{Log}[d + e x] - 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x]^2) - \\
& \left. 4 e^2 f^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 2 \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) + \\
& 48 b^2 e^2 g^2 h^2 n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\
& \left(\frac{1}{2} \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) + 8 b^3 e^2 g^2 h^2 n^3 \\
& \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + 3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \right) - \\
& 16 b^3 e g h i n^3 \left(-g (d + e x) (-6 + 6 \operatorname{Log}[d + e x] - 3 \operatorname{Log}[d + e x]^2 + \operatorname{Log}[d + e x]^3) + e f \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \right. \right. \\
& \left. \left. 3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) + \\
& b^3 i^2 n^3 \left(-8 e f g (d + e x) (-6 + 6 \operatorname{Log}[d + e x] - 3 \operatorname{Log}[d + e x]^2 + \operatorname{Log}[d + e x]^3) - g^2 (3 e x (-14 d + e x) + 6 (7 d^2 + 6 d e x - e^2 x^2) \operatorname{Log}[d + e x] - \right. \\
& 6 (3 d^2 + 2 d e x - e^2 x^2) \operatorname{Log}[d + e x]^2 + 4 (d^2 - e^2 x^2) \operatorname{Log}[d + e x]^3) + 8 e^2 f^2 \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \right. \\
& \left. \left. 3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) \right)
\end{aligned}$$

Problem 230: Result more than twice size of optimal antiderivative.

$$\int \frac{(h + i x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{f + g x} dx$$

Optimal (type 4, 308 leaves, 12 steps):

$$\frac{6 a b^2 i n^2 x}{g} - \frac{6 b^3 i n^3 x}{g} + \frac{6 b^3 i n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e g} - \frac{3 b i n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e g} + \frac{i (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e g} +$$

$$\frac{(g h - f i) (a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right]}{g^2} + \frac{3 b (g h - f i) n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{g (d + e x)}{e f - d g}\right]}{g^2} -$$

$$\frac{6 b^2 (g h - f i) n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, -\frac{g (d + e x)}{e f - d g}\right]}{g^2} + \frac{6 b^3 (g h - f i) n^3 \operatorname{PolyLog}\left[4, -\frac{g (d + e x)}{e f - d g}\right]}{g^2}$$

Result (type 4, 776 leaves):

$$\frac{1}{e g^2} \left(e g i x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 + e (g h - f i) (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}[f + g x] + \right.$$

$$3 b e g h n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) - 3 b i n$$

$$(a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \left(-g (d + e x) (-1 + \operatorname{Log}[d + e x]) + e f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] \right) \right) \left. \right) +$$

$$3 b^2 i n^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(g (d + e x) (2 - 2 \operatorname{Log}[d + e x] + \operatorname{Log}[d + e x]^2) - \right.$$

$$e f \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 2 \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) \left. \right) + 6 b^2 e g h n^2$$

$$(a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(\frac{1}{2} \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] \right) \left. \right) +$$

$$b^3 e g h n^3 \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + 3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] + \right.$$

$$6 \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \left. \right) - b^3 i n^3 \left(-g (d + e x) (-6 + 6 \operatorname{Log}[d + e x] - 3 \operatorname{Log}[d + e x]^2 + \operatorname{Log}[d + e x]^3) + e f \left(\operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e (f + g x)}{e f - d g}\right] + \right.$$

$$3 \operatorname{Log}[d + e x]^2 \operatorname{PolyLog}\left[2, \frac{g (d + e x)}{-e f + d g}\right] - 6 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[3, \frac{g (d + e x)}{-e f + d g}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g (d + e x)}{-e f + d g}\right] \right) \left. \right)$$

Problem 231: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c(d + ex)^n])^3}{f + gx} dx$$

Optimal (type 4, 158 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[c(d + ex)^n])^3 \operatorname{Log}\left[\frac{e(f+gx)}{ef-dg}\right]}{g} + \frac{3bn(a + b \operatorname{Log}[c(d + ex)^n])^2 \operatorname{PolyLog}\left[2, -\frac{g(d+ex)}{ef-dg}\right]}{g} - \frac{6b^2n^2(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{PolyLog}\left[3, -\frac{g(d+ex)}{ef-dg}\right]}{g} + \frac{6b^3n^3 \operatorname{PolyLog}\left[4, -\frac{g(d+ex)}{ef-dg}\right]}{g}$$

Result (type 4, 335 leaves):

$$\frac{1}{g} \left((a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^3 \operatorname{Log}[f + gx] + 3bn(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^2 \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] \right) + 6b^2n^2(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n]) \left(\frac{1}{2} \operatorname{Log}[d + ex]^2 \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] - \operatorname{PolyLog}\left[3, \frac{g(d + ex)}{-ef + dg}\right] \right) + b^3n^3 \left(\operatorname{Log}[d + ex]^3 \operatorname{Log}\left[\frac{e(f + gx)}{ef - dg}\right] + 3 \operatorname{Log}[d + ex]^2 \operatorname{PolyLog}\left[2, \frac{g(d + ex)}{-ef + dg}\right] - 6 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[3, \frac{g(d + ex)}{-ef + dg}\right] + 6 \operatorname{PolyLog}\left[4, \frac{g(d + ex)}{-ef + dg}\right] \right) \right)$$

Problem 256: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 (a + b \operatorname{Log}[c(d + ex)^n])}{f + gx^2} dx$$

Optimal (type 4, 397 leaves, 16 steps):

$$-\frac{bdfnx}{2e^2g^2} + \frac{bd^3nx}{4e^3g} + \frac{bfnx^2}{4g^2} - \frac{bd^2nx^2}{8e^2g} + \frac{bdnx^3}{12eg} - \frac{bnx^4}{16g} + \frac{bd^2fn \operatorname{Log}[d + ex]}{2e^2g^2} - \frac{bd^4n \operatorname{Log}[d + ex]}{4e^4g} - \frac{fx^2(a + b \operatorname{Log}[c(d + ex)^n])}{2g^2} + \frac{x^4(a + b \operatorname{Log}[c(d + ex)^n])}{4g} + \frac{f^2(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g}x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2g^3} + \frac{f^2(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g}x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2g^3} + \frac{bf^2n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2g^3} + \frac{bf^2n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2g^3}$$

Result (type 4, 373 leaves):

$$\begin{aligned} & \frac{1}{48 g^3} \left(-24 f g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \right. \\ & 12 g^2 x^4 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + 24 f^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + \\ & \left. b n \left(\frac{12 f g (e x (-2 d + e x) + 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x])}{e^2} + \frac{g^2 (e x (12 d^3 - 6 d^2 e x + 4 d e^2 x^2 - 3 e^3 x^3) - 12 (d^4 - e^4 x^4) \operatorname{Log}[d + e x])}{e^4} \right) + \right. \\ & 24 f^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\ & \left. 24 f^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \end{aligned}$$

Problem 257: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 (a + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} dx$$

Optimal (type 4, 278 leaves, 13 steps):

$$\begin{aligned} & \frac{b d n x}{2 e g} - \frac{b n x^2}{4 g} - \frac{b d^2 n \operatorname{Log}[d + e x]}{2 e^2 g} + \frac{x^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 g} - \frac{f (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2} - \\ & \frac{f (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2} - \frac{b f n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2} - \frac{b f n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2} \end{aligned}$$

Result (type 4, 283 leaves):

$$\begin{aligned} & \frac{1}{4 e^2 g^2} \left(2 e^2 g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) - 2 e^2 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + \right. \\ & b n \left(e g x (2 d - e x) - 2 g (d^2 - e^2 x^2) \operatorname{Log}[d + e x] - 2 e^2 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right. \\ & \left. \left. 2 e^2 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right) \end{aligned}$$

Problem 258: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x (a + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} dx$$

Optimal (type 4, 203 leaves, 8 steps):

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2g} +$$

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2g} + \frac{bn \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2g} + \frac{bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2g}$$

Result (type 4, 189 leaves):

$$\frac{1}{2g} \left((a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + \right.$$

$$\left. bn \left(\operatorname{Log}[d + ex] \left(\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right)$$

Problem 259: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x (f + g x^2)} dx$$

Optimal (type 4, 245 leaves, 12 steps):

$$\frac{\operatorname{Log}\left[-\frac{ex}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{f} - \frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2f} -$$

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2f} - \frac{bn \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2f} - \frac{bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2f} + \frac{bn \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right]}{f}$$

Result (type 4, 264 leaves):

$$\begin{aligned}
& -\frac{1}{2f} \left(-2a \operatorname{Log}[x] - 2b \operatorname{Log}[x] \operatorname{Log}[c(d+ex)^n] + 2bn \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + a \operatorname{Log}[f+gx^2] - \right. \\
& \quad \left. bn \operatorname{Log}[d+ex] \operatorname{Log}[f+gx^2] + b \operatorname{Log}[c(d+ex)^n] \operatorname{Log}[f+gx^2] + bn \operatorname{Log}[d+ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \right. \\
& \quad \left. bn \operatorname{Log}[d+ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2bn \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] + bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right)
\end{aligned}$$

Problem 260: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c(d+ex)^n]}{x^3(f+gx^2)} dx$$

Optimal (type 4, 331 leaves, 15 steps):

$$\begin{aligned}
& -\frac{ben}{2dfx} - \frac{be^2n \operatorname{Log}[x]}{2d^2f} + \frac{be^2n \operatorname{Log}[d+ex]}{2d^2f} - \frac{a + b \operatorname{Log}[c(d+ex)^n]}{2fx^2} - \frac{g \operatorname{Log}\left[-\frac{ex}{d}\right] (a + b \operatorname{Log}[c(d+ex)^n])}{f^2} + \\
& \frac{g(a + b \operatorname{Log}[c(d+ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g}x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2f^2} + \frac{g(a + b \operatorname{Log}[c(d+ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g}x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2f^2} + \\
& \frac{bgn \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2f^2} + \frac{bgn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2f^2} - \frac{bgn \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right]}{f^2}
\end{aligned}$$

Result (type 4, 340 leaves):

$$\begin{aligned}
& \frac{1}{2f^2} \left(-\frac{af}{x^2} - \frac{befn}{dx} - 2ag \operatorname{Log}[x] - \frac{be^2fn \operatorname{Log}[x]}{d^2} + \frac{be^2fn \operatorname{Log}[d+ex]}{d^2} - \frac{bf \operatorname{Log}[c(d+ex)^n]}{x^2} - \right. \\
& \quad \left. 2bg \operatorname{Log}[x] \operatorname{Log}[c(d+ex)^n] + 2bgn \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + ag \operatorname{Log}[f+gx^2] - bgn \operatorname{Log}[d+ex] \operatorname{Log}[f+gx^2] + \right. \\
& \quad \left. bg \operatorname{Log}[c(d+ex)^n] \operatorname{Log}[f+gx^2] + bgn \operatorname{Log}[d+ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + bgn \operatorname{Log}[d+ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \right. \\
& \quad \left. 2bgn \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] + bgn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + bgn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right)
\end{aligned}$$

Problem 261: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4 (a + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} dx$$

Optimal (type 4, 369 leaves, 16 steps):

$$\begin{aligned} & -\frac{a f x}{g^2} + \frac{b f n x}{g^2} - \frac{b d^2 n x}{3 e^2 g} + \frac{b d n x^2}{6 e g} - \frac{b n x^3}{9 g} + \frac{b d^3 n \operatorname{Log}[d + e x]}{3 e^3 g} - \\ & \frac{b f (d + e x) \operatorname{Log}[c (d + e x)^n]}{e g^2} + \frac{x^3 (a + b \operatorname{Log}[c (d + e x)^n])}{3 g} + \frac{(-f)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^{5/2}} - \\ & \frac{(-f)^{3/2} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^{5/2}} - \frac{b (-f)^{3/2} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^{5/2}} + \frac{b (-f)^{3/2} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^{5/2}} \end{aligned}$$

Result (type 4, 374 leaves):

$$\begin{aligned} & \frac{1}{6 g^{5/2}} \left(-6 f \sqrt{g} x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \right. \\ & 2 g^{3/2} x^3 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + 6 f^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \\ & 3 b n \left(-\frac{2 f \sqrt{g} (d + e x) (-1 + \operatorname{Log}[d + e x])}{e} + \frac{g^{3/2} (e x (-6 d^2 + 3 d e x - 2 e^2 x^2) + 6 (d^3 + e^3 x^3) \operatorname{Log}[d + e x])}{9 e^3} + \right. \\ & \left. i f^{3/2} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right. \\ & \left. \left. i f^{3/2} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right) \end{aligned}$$

Problem 262: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 (a + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} dx$$

Optimal (type 4, 276 leaves, 13 steps):

$$\frac{a x}{g} - \frac{b n x}{g} + \frac{b (d+e x) \operatorname{Log}[c (d+e x)^n]}{e g} + \frac{\sqrt{-f} (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e\sqrt{-f}+d\sqrt{g}}\right] - \sqrt{-f} (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e\sqrt{-f}-d\sqrt{g}}\right] - \frac{b \sqrt{-f} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f}-d\sqrt{g}}\right] + \frac{b \sqrt{-f} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2 g^{3/2}}}{2 g^{3/2}}$$

Result (type 4, 287 leaves):

$$x (a+b (-n \operatorname{Log}[d+e x] + \operatorname{Log}[c (d+e x)^n])) \frac{\sqrt{f} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a+b (-n \operatorname{Log}[d+e x] + \operatorname{Log}[c (d+e x)^n]))}{g} + \frac{b n \left(\frac{(d+e x) (-1 + \operatorname{Log}[d+e x])}{e g} - \frac{i \sqrt{f} \left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right]\right)}{2 g^{3/2}} + \frac{i \sqrt{f} \left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right]\right)}{2 g^{3/2}} \right)}{g^{3/2}}$$

Problem 263: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a+b \operatorname{Log}[c (d+e x)^n]}{f+g x^2} dx$$

Optimal (type 4, 239 leaves, 8 steps):

$$\frac{(a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2 \sqrt{-f} \sqrt{g}} - \frac{(a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2 \sqrt{-f} \sqrt{g}} - \frac{b n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2 \sqrt{-f} \sqrt{g}} + \frac{b n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2 \sqrt{-f} \sqrt{g}}$$

Result (type 4, 209 leaves):

$$\frac{1}{2 \sqrt{f} \sqrt{g}} \left(2 \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a-b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n]) + i b n \left(\operatorname{Log}[d+e x] \left(\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right]\right) + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right)$$

Problem 264: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x^2 (f + g x^2)} dx$$

Optimal (type 4, 290 leaves, 14 steps):

$$\frac{b e n \operatorname{Log}[x]}{d f} - \frac{b e n \operatorname{Log}[d + e x]}{d f} - \frac{a + b \operatorname{Log}[c (d + e x)^n]}{f x} + \frac{\sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{3/2}} -$$

$$\frac{\sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{3/2}} - \frac{b \sqrt{g} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{3/2}} + \frac{b \sqrt{g} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{3/2}}$$

Result (type 4, 298 leaves):

$$\frac{1}{2 d f^{3/2} x} \left(-2 d \sqrt{f} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) - 2 d \sqrt{g} x \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \right.$$

$$\left. b n \left(2 \sqrt{f} (e x \operatorname{Log}[x] - (d + e x) \operatorname{Log}[d + e x]) - i d \sqrt{g} x \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right]\right) + \right.$$

$$\left. i d \sqrt{g} x \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right]\right) \right)$$

Problem 265: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x^4 (f + g x^2)} dx$$

Optimal (type 4, 388 leaves, 17 steps):

$$\begin{aligned}
& - \frac{b e n}{6 d f x^2} + \frac{b e^2 n}{3 d^2 f x} + \frac{b e^3 n \operatorname{Log}[x]}{3 d^3 f} - \frac{b e g n \operatorname{Log}[x]}{d f^2} - \frac{b e^3 n \operatorname{Log}[d + e x]}{3 d^3 f} + \frac{b e g n \operatorname{Log}[d + e x]}{d f^2} - \\
& \frac{a + b \operatorname{Log}[c (d + e x)^n]}{3 f x^3} + \frac{g (a + b \operatorname{Log}[c (d + e x)^n])}{f^2 x} + \frac{g^{3/2} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{5/2}} - \\
& \frac{g^{3/2} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2}} - \frac{b g^{3/2} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2}} + \frac{b g^{3/2} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{5/2}}
\end{aligned}$$

Result (type 4, 383 leaves):

$$\begin{aligned}
& \frac{1}{6 f^{5/2}} \left(- \frac{2 f^{3/2} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{x^3} + \right. \\
& \frac{6 \sqrt{f} g (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{x} + 6 g^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \\
& b n \left(- \frac{6 \sqrt{f} g (e x \operatorname{Log}[x] - (d + e x) \operatorname{Log}[d + e x])}{d x} + \frac{f^{3/2} (-d e x (d - 2 e x) + 2 e^3 x^3 \operatorname{Log}[x] - 2 (d^3 + e^3 x^3) \operatorname{Log}[d + e x])}{d^3 x^3} + \right. \\
& \left. 3 i g^{3/2} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right. \\
& \left. \left. 3 i g^{3/2} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right)
\end{aligned}$$

Problem 266: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 (a + b \operatorname{Log}[c (d + e x)^n])}{(f + g x^2)^2} dx$$

Optimal (type 4, 417 leaves, 19 steps):

$$\frac{b d n x}{2 e g^2} - \frac{b n x^2}{4 g^2} + \frac{b d e f^{3/2} n \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]}{2 g^{5/2} (e^2 f + d^2 g)} - \frac{b d^2 n \operatorname{Log}[d + e x]}{2 e^2 g^2} + \frac{b e^2 f^2 n \operatorname{Log}[d + e x]}{2 g^3 (e^2 f + d^2 g)} +$$

$$\frac{x^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 g^2} - \frac{f^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 g^3 (f + g x^2)} - \frac{f (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^3} -$$

$$\frac{f (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^3} - \frac{b e^2 f^2 n \operatorname{Log}[f + g x^2]}{4 g^3 (e^2 f + d^2 g)} - \frac{b f n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^3} - \frac{b f n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^3}$$

Result (type 4, 560 leaves):

$$\frac{1}{8 g^3} \left(4 g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) - \frac{4 f^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} - \right.$$

$$8 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + b n \left(-\frac{2 g (e x (-2 d + e x) + 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x])}{e^2} + \right.$$

$$\left. \left(f^{3/2} \left(2 e (-i \sqrt{f} + \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] - e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right.$$

$$\left. (\sqrt{f} + i \sqrt{g} x) \right) + \left(i f^{3/2} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 8 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right.$$

$$\left. \left. 8 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right)$$

Problem 267: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 (a + b \operatorname{Log}[c (d + e x)^n])}{(f + g x^2)^2} dx$$

Optimal (type 4, 344 leaves, 16 steps):

$$\begin{aligned}
& - \frac{b d e \sqrt{f} n \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]}{2 g^{3/2} (e^2 f + d^2 g)} - \frac{b e^2 f n \operatorname{Log}[d + e x]}{2 g^2 (e^2 f + d^2 g)} + \frac{f (a + b \operatorname{Log}[c (d + e x)^n])}{2 g^2 (f + g x^2)} + \frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^2} + \\
& \frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^2} + \frac{b e^2 f n \operatorname{Log}[f + g x^2]}{4 g^2 (e^2 f + d^2 g)} + \frac{b n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^2} + \frac{b n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^2}
\end{aligned}$$

Result (type 4, 488 leaves):

$$\begin{aligned}
& \frac{1}{8 g^2} \left(\frac{4 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} + 4 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + \right. \\
& \left. b n \left(\left(\sqrt{f} \left(2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \right. \\
& \left. \left. (\sqrt{f} + i \sqrt{g} x) \right) - \left(i \sqrt{f} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) \right) / \\
& \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) + 4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\
& \left. 4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 269: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x (f + g x^2)^2} dx$$

Optimal (type 4, 383 leaves, 18 steps):

$$\begin{aligned}
& - \frac{b d e \sqrt{g} n \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]}{2 f^{3/2} (e^2 f + d^2 g)} - \frac{b e^2 n \operatorname{Log}[d + e x]}{2 f (e^2 f + d^2 g)} + \frac{a + b \operatorname{Log}[c (d + e x)^n]}{2 f (f + g x^2)} + \frac{\operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{f^2} - \\
& \frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 f^2} - \frac{(a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 f^2} + \\
& \frac{b e^2 n \operatorname{Log}[f + g x^2]}{4 f (e^2 f + d^2 g)} - \frac{b n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 f^2} - \frac{b n \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 f^2} + \frac{b n \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{f^2}
\end{aligned}$$

Result (type 4, 559 leaves):

$$\frac{a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]}{2 f^2 + 2 f g x^2} + \frac{\operatorname{Log}[x] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f^2} -$$

$$\frac{(a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2]}{2 f^2} + \frac{1}{8 f^2} b n \left(8 \operatorname{Log}[x] \left(\operatorname{Log}[d + e x] - \operatorname{Log}\left[1 + \frac{e x}{d}\right]\right) + \right.$$

$$\left. \left(\sqrt{f} \left(2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right.$$

$$\left. (\sqrt{f} + i \sqrt{g} x) - \left(i \sqrt{f} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) \right) /$$

$$\left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 8 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] - 4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) -$$

$$4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right)$$

Problem 270: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x^3 (f + g x^2)^2} dx$$

Optimal (type 4, 460 leaves, 21 steps):

$$-\frac{b e n}{2 d f^2 x} + \frac{b d e g^{3/2} n \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]}{2 f^{5/2} (e^2 f + d^2 g)} - \frac{b e^2 n \operatorname{Log}[x]}{2 d^2 f^2} + \frac{b e^2 n \operatorname{Log}[d + e x]}{2 d^2 f^2} + \frac{b e^2 g n \operatorname{Log}[d + e x]}{2 f^2 (e^2 f + d^2 g)} - \frac{a + b \operatorname{Log}[c (d + e x)^n]}{2 f^2 x^2} - \frac{g (a + b \operatorname{Log}[c (d + e x)^n])}{2 f^2 (f + g x^2)} -$$

$$\frac{2 g \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{f^3} + \frac{g (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^3} + \frac{g (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^3} -$$

$$\frac{b e^2 g n \operatorname{Log}[f + g x^2]}{4 f^2 (e^2 f + d^2 g)} + \frac{b g n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^3} + \frac{b g n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^3} - \frac{2 b g n \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{f^3}$$

Result (type 4, 631 leaves):

$$\begin{aligned}
& \frac{1}{8 f^3} \left(- \frac{4 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{x^2} - \right. \\
& \frac{4 f g (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} - 16 g \operatorname{Log}[x] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + \\
& 8 g (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[f + g x^2] + b n \left(- \frac{4 f (d e x + e^2 x^2 \operatorname{Log}[x] + (d^2 - e^2 x^2) \operatorname{Log}[d + e x])}{d^2 x^2} + \right. \\
& \left. \left(\sqrt{f} g \left(2 e (-i \sqrt{f} + \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] - e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \right. \\
& \left. \left. (\sqrt{f} + i \sqrt{g} x) \right) + \left(i \sqrt{f} g \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) \right) / \\
& \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 16 g \left(\operatorname{Log}[x] \left(\operatorname{Log}[d + e x] - \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) - \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right) + \\
& 8 g \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\
& \left. \left. 8 g \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right)
\end{aligned}$$

Problem 271: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4 (a + b \operatorname{Log}[c (d + e x)^n])}{(f + g x^2)^2} dx$$

Optimal (type 4, 534 leaves, 31 steps):

$$\begin{aligned}
& \frac{a x}{g^2} - \frac{b n x}{g^2} - \frac{b e f n \operatorname{Log}[d + e x]}{4 (e \sqrt{-f} - d \sqrt{g}) g^{5/2}} + \frac{b e f n \operatorname{Log}[d + e x]}{4 (e \sqrt{-f} + d \sqrt{g}) g^{5/2}} + \frac{b (d + e x) \operatorname{Log}[c (d + e x)^n]}{e g^2} - \frac{f (a + b \operatorname{Log}[c (d + e x)^n])}{4 g^{5/2} (\sqrt{-f} - \sqrt{g} x)} + \\
& \frac{f (a + b \operatorname{Log}[c (d + e x)^n])}{4 g^{5/2} (\sqrt{-f} + \sqrt{g} x)} - \frac{b e f n \operatorname{Log}[\sqrt{-f} - \sqrt{g} x]}{4 (e \sqrt{-f} + d \sqrt{g}) g^{5/2}} + \frac{3 \sqrt{-f} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 g^{5/2}} + \frac{b e f n \operatorname{Log}[\sqrt{-f} + \sqrt{g} x]}{4 (e \sqrt{-f} - d \sqrt{g}) g^{5/2}} - \\
& \frac{3 \sqrt{-f} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 g^{5/2}} - \frac{3 b \sqrt{-f} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 g^{5/2}} + \frac{3 b \sqrt{-f} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 g^{5/2}}
\end{aligned}$$

Result (type 4, 564 leaves):

$$\begin{aligned}
& \frac{1}{8g^{5/2}} \left(8\sqrt{g} x (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n]) + \frac{4f\sqrt{g} x (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])}{f + gx^2} - \right. \\
& 12\sqrt{f} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n]) + bn \left(\frac{8\sqrt{g} (d + ex) (-1 + \operatorname{Log}[d + ex])}{e} + \right. \\
& \left. \left(f \left(-2e (\sqrt{f} + i\sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + ie (\sqrt{f} + i\sqrt{g} x) \operatorname{Log}[f + gx^2] \right) \right) / \left((e\sqrt{f} - id\sqrt{g}) \right. \\
& \left. (\sqrt{f} + i\sqrt{g} x) \right) - \left(f \left(2e (\sqrt{f} - i\sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + e (i\sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + gx^2] \right) \right) / \\
& \left. \left((e\sqrt{f} + id\sqrt{g}) (\sqrt{f} - i\sqrt{g} x) \right) - 6ie\sqrt{f} \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& \left. 6ie\sqrt{f} \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) \Bigg)
\end{aligned}$$

Problem 272: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 (a + b \operatorname{Log}[c (d + ex)^n])}{(f + gx^2)^2} dx$$

Optimal (type 4, 491 leaves, 28 steps):

$$\begin{aligned}
& \frac{ben \operatorname{Log}[d + ex]}{4(e\sqrt{-f} - d\sqrt{g})g^{3/2}} - \frac{ben \operatorname{Log}[d + ex]}{4(e\sqrt{-f} + d\sqrt{g})g^{3/2}} + \frac{a + b \operatorname{Log}[c (d + ex)^n]}{4g^{3/2}(\sqrt{-f} - \sqrt{g}x)} - \frac{a + b \operatorname{Log}[c (d + ex)^n]}{4g^{3/2}(\sqrt{-f} + \sqrt{g}x)} + \\
& \frac{ben \operatorname{Log}[\sqrt{-f} - \sqrt{g}x]}{4(e\sqrt{-f} + d\sqrt{g})g^{3/2}} + \frac{(a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g}x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{4\sqrt{-f}g^{3/2}} - \frac{ben \operatorname{Log}[\sqrt{-f} + \sqrt{g}x]}{4(e\sqrt{-f} - d\sqrt{g})g^{3/2}} - \\
& \frac{(a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g}x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{4\sqrt{-f}g^{3/2}} - \frac{bn \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d + ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{4\sqrt{-f}g^{3/2}} + \frac{bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{4\sqrt{-f}g^{3/2}}
\end{aligned}$$

Result (type 4, 503 leaves):

$$\frac{1}{8g^{3/2}} \left(-\frac{4\sqrt{g}x(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])}{f + gx^2} + \frac{4 \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right](a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])}{\sqrt{f}} + \right. \\ \left. bn \left(\frac{2e(\sqrt{f} + i\sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + e(-i\sqrt{f} + \sqrt{g}x) \operatorname{Log}[f + gx^2]}{(e\sqrt{f} - id\sqrt{g})(\sqrt{f} + i\sqrt{g}x)} + \right. \right. \\ \left. \frac{2e(\sqrt{f} - i\sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + e(i\sqrt{f} + \sqrt{g}x) \operatorname{Log}[f + gx^2]}{(e\sqrt{f} + id\sqrt{g})(\sqrt{f} - i\sqrt{g}x)} + \right. \\ \left. \left. \frac{2i \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right]\right)}{\sqrt{f}} - \frac{2i \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right]\right)}{\sqrt{f}} \right) \right)$$

Problem 273: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c(d + ex)^n]}{(f + gx^2)^2} dx$$

Optimal (type 4, 503 leaves, 18 steps):

$$\frac{ben \operatorname{Log}[d + ex]}{4f(e\sqrt{-f} + d\sqrt{g})\sqrt{g}} + \frac{ben \operatorname{Log}[d + ex]}{4(e(-f)^{3/2} + df\sqrt{g})\sqrt{g}} - \frac{a + b \operatorname{Log}[c(d + ex)^n]}{4f\sqrt{g}(\sqrt{-f} - \sqrt{g}x)} + \frac{a + b \operatorname{Log}[c(d + ex)^n]}{4f\sqrt{g}(\sqrt{-f} + \sqrt{g}x)} - \\ \frac{ben \operatorname{Log}[\sqrt{-f} - \sqrt{g}x]}{4f(e\sqrt{-f} + d\sqrt{g})\sqrt{g}} - \frac{(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g}x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}} - \frac{ben \operatorname{Log}[\sqrt{-f} + \sqrt{g}x]}{4(e(-f)^{3/2} + df\sqrt{g})\sqrt{g}} + \\ \frac{(a + b \operatorname{Log}[c(d + ex)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g}x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}} + \frac{bn \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d + ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}} - \frac{bn \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}}$$

Result (type 4, 511 leaves):

$$\frac{1}{8 f^{3/2}} \left(\frac{4 \sqrt{f} x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} + \frac{4 \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{\sqrt{g}} + \right.$$

$$\left. \frac{1}{\sqrt{g}} b n \left(\left(\sqrt{f} \left(-2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \right.$$

$$\left. \left. (\sqrt{f} + i \sqrt{g} x) \right) - \left(\sqrt{f} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \right.$$

$$\left. \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) + 2 i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right.$$

$$\left. \left. 2 i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right)$$

Problem 274: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{x^2 (f + g x^2)^2} dx$$

Optimal (type 4, 560 leaves, 32 steps):

$$\frac{b e n \operatorname{Log}[x]}{d f^2} - \frac{b e n \operatorname{Log}[d + e x]}{d f^2} - \frac{b e \sqrt{g} n \operatorname{Log}[d + e x]}{4 f^2 (e \sqrt{-f} + d \sqrt{g})} - \frac{b e \sqrt{g} n \operatorname{Log}[d + e x]}{4 f (e (-f)^{3/2} + d f \sqrt{g})} - \frac{a + b \operatorname{Log}[c (d + e x)^n]}{f^2 x} + \frac{\sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n])}{4 f^2 (\sqrt{-f} - \sqrt{g} x)} -$$

$$\frac{\sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n])}{4 f^2 (\sqrt{-f} + \sqrt{g} x)} + \frac{b e \sqrt{g} n \operatorname{Log}[\sqrt{-f} - \sqrt{g} x]}{4 f^2 (e \sqrt{-f} + d \sqrt{g})} - \frac{3 \sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 (-f)^{5/2}} + \frac{b e \sqrt{g} n \operatorname{Log}[\sqrt{-f} + \sqrt{g} x]}{4 f (e (-f)^{3/2} + d f \sqrt{g})} +$$

$$\frac{3 \sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 (-f)^{5/2}} + \frac{3 b \sqrt{g} n \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 (-f)^{5/2}} - \frac{3 b \sqrt{g} n \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 (-f)^{5/2}}$$

Result (type 4, 593 leaves):

$$\frac{1}{8 f^{5/2}} \left(- \frac{8 \sqrt{f} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{x} - \frac{4 \sqrt{f} g x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])}{f + g x^2} - \right.$$

$$12 \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) + b n \left(\frac{8 \sqrt{f} (e x \operatorname{Log}[x] - (d + e x) \operatorname{Log}[d + e x])}{d x} - \right.$$

$$\left. \left(\sqrt{f} \sqrt{g} \left(-2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right.$$

$$\left. (\sqrt{f} + i \sqrt{g} x) \right) + \left(\sqrt{f} \sqrt{g} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 6 i \sqrt{g} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right.$$

$$\left. \left. 6 i \sqrt{g} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right)$$

Problem 275: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{\sqrt{2 + g x^2}} dx$$

Optimal (type 4, 326 leaves, 10 steps):

$$\frac{b n \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right]^2}{2 \sqrt{g}} - \frac{b n \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{\sqrt{2} e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right]}}{d \sqrt{g} - \sqrt{2 e^2 + d^2 g}}\right]}{\sqrt{g}} - \frac{b n \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{\sqrt{2} e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right]}}{d \sqrt{g} + \sqrt{2 e^2 + d^2 g}}\right]}{\sqrt{g}} +$$

$$\frac{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{\sqrt{g}} - \frac{b n \operatorname{PolyLog}\left[2, -\frac{\sqrt{2} e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right]}}{d \sqrt{g} - \sqrt{2 e^2 + d^2 g}}\right]}{\sqrt{g}} - \frac{b n \operatorname{PolyLog}\left[2, -\frac{\sqrt{2} e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{2}}\right]}}{d \sqrt{g} + \sqrt{2 e^2 + d^2 g}}\right]}{\sqrt{g}}$$

Result (type 1, 1 leaves):

???

Problem 276: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{\sqrt{f + g x^2}} dx$$

Optimal (type 4, 506 leaves, 11 steps):

$$\frac{b \sqrt{f} n \sqrt{1 + \frac{g x^2}{f}} \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]^2}{2 \sqrt{g} \sqrt{f + g x^2}} - \frac{b \sqrt{f} n \sqrt{1 + \frac{g x^2}{f}} \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] \operatorname{Log}\left[1 + \frac{e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]} \sqrt{f}}{d \sqrt{g} - \sqrt{e^2 f + d^2 g}}\right]}{\sqrt{g} \sqrt{f + g x^2}} -$$

$$\frac{b \sqrt{f} n \sqrt{1 + \frac{g x^2}{f}} \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] \operatorname{Log}\left[1 + \frac{e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]} \sqrt{f}}{d \sqrt{g} + \sqrt{e^2 f + d^2 g}}\right]}{\sqrt{g} \sqrt{f + g x^2}} + \frac{\sqrt{f} \sqrt{1 + \frac{g x^2}{f}} \operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{\sqrt{g} \sqrt{f + g x^2}} -$$

$$\frac{b \sqrt{f} n \sqrt{1 + \frac{g x^2}{f}} \operatorname{PolyLog}\left[2, -\frac{e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]} \sqrt{f}}{d \sqrt{g} - \sqrt{e^2 f + d^2 g}}\right]}{\sqrt{g} \sqrt{f + g x^2}} - \frac{b \sqrt{f} n \sqrt{1 + \frac{g x^2}{f}} \operatorname{PolyLog}\left[2, -\frac{e e^{\operatorname{ArcSinh}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right]} \sqrt{f}}{d \sqrt{g} + \sqrt{e^2 f + d^2 g}}\right]}{\sqrt{g} \sqrt{f + g x^2}}$$

Result (type 1, 1 leaves):

???

Problem 277: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{\sqrt{2 - g x} \sqrt{2 + g x}} dx$$

Optimal (type 4, 278 leaves, 9 steps):

$$\frac{i b n \operatorname{ArcSin}\left[\frac{g x}{2}\right]^2}{2 g} - \frac{b n \operatorname{ArcSin}\left[\frac{g x}{2}\right] \operatorname{Log}\left[1 + \frac{2 e e^{i \operatorname{ArcSin}\left[\frac{g x}{2}\right]}}{i d g - \sqrt{4 e^2 - d^2 g^2}}\right]}{g} - \frac{b n \operatorname{ArcSin}\left[\frac{g x}{2}\right] \operatorname{Log}\left[1 + \frac{2 e e^{i \operatorname{ArcSin}\left[\frac{g x}{2}\right]}}{i d g + \sqrt{4 e^2 - d^2 g^2}}\right]}{g} +$$

$$\frac{\operatorname{ArcSin}\left[\frac{g x}{2}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{g} + \frac{i b n \operatorname{PolyLog}\left[2, -\frac{2 e e^{i \operatorname{ArcSin}\left[\frac{g x}{2}\right]}}{i d g - \sqrt{4 e^2 - d^2 g^2}}\right]}{g} + \frac{i b n \operatorname{PolyLog}\left[2, -\frac{2 e e^{i \operatorname{ArcSin}\left[\frac{g x}{2}\right]}}{i d g + \sqrt{4 e^2 - d^2 g^2}}\right]}{g}$$

Result (type 1, 1 leaves):

???

Problem 278: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d + e x)^n]}{\sqrt{f - g x} \sqrt{f + g x}} dx$$

Optimal (type 4, 510 leaves, 11 steps):

$$\begin{aligned} & \frac{i b f n \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{ArcSin}\left[\frac{g x}{f}\right]^2 - b f n \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{ArcSin}\left[\frac{g x}{f}\right] \operatorname{Log}\left[1 + \frac{e e^{i \operatorname{ArcSin}\left[\frac{g x}{f}\right]} f}{i d g - \sqrt{e^2 f^2 - d^2 g^2}}\right]}{2 g \sqrt{f - g x} \sqrt{f + g x}} - \frac{b f n \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{ArcSin}\left[\frac{g x}{f}\right] \operatorname{Log}\left[1 + \frac{e e^{i \operatorname{ArcSin}\left[\frac{g x}{f}\right]} f}{i d g + \sqrt{e^2 f^2 - d^2 g^2}}\right]}{g \sqrt{f - g x} \sqrt{f + g x}} + \frac{f \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{ArcSin}\left[\frac{g x}{f}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{g \sqrt{f - g x} \sqrt{f + g x}} + \\ & \frac{i b f n \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{PolyLog}\left[2, -\frac{e e^{i \operatorname{ArcSin}\left[\frac{g x}{f}\right]} f}{i d g - \sqrt{e^2 f^2 - d^2 g^2}}\right]}{g \sqrt{f - g x} \sqrt{f + g x}} + \frac{i b f n \sqrt{1 - \frac{g^2 x^2}{f^2}} \operatorname{PolyLog}\left[2, -\frac{e e^{i \operatorname{ArcSin}\left[\frac{g x}{f}\right]} f}{i d g + \sqrt{e^2 f^2 - d^2 g^2}}\right]}{g \sqrt{f - g x} \sqrt{f + g x}} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 279: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{2e}{e+fx}\right]}{e^2 - f^2 x^2} dx$$

Optimal (type 4, 24 leaves, 2 steps):

$$\frac{\operatorname{PolyLog}\left[2, 1 - \frac{2e}{e+fx}\right]}{2ef}$$

Result (type 4, 89 leaves):

$$\frac{1}{4ef} \left(4 \operatorname{ArcTanh}\left[\frac{fx}{e}\right] \left(\operatorname{Log}\left[\frac{e}{f} + x\right] + \operatorname{Log}\left[\frac{2e}{e+fx}\right] \right) - \operatorname{Log}\left[\frac{e}{f} + x\right] \left(\operatorname{Log}[4] + \operatorname{Log}\left[\frac{e}{f} + x\right] - 2 \operatorname{Log}\left[1 - \frac{fx}{e}\right] \right) + 2 \operatorname{PolyLog}\left[2, \frac{e+fx}{2e}\right] \right)$$

Problem 280: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{-e}{e+fx}\right]}{e^2 - f^2 x^2} dx$$

Optimal (type 4, 42 leaves, 4 steps):

$$-\frac{\text{ArcTanh}\left[\frac{fx}{e}\right] \text{Log}[2]}{ef} + \frac{\text{PolyLog}\left[2, 1 - \frac{2e}{e+fx}\right]}{2ef}$$

Result (type 4, 88 leaves):

$$\frac{1}{4ef} \left(4 \text{ArcTanh}\left[\frac{fx}{e}\right] \left(\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{e}{e+fx}\right] \right) - \text{Log}\left[\frac{e}{f} + x\right] \left(\text{Log}[4] + \text{Log}\left[\frac{e}{f} + x\right] - 2 \text{Log}\left[1 - \frac{fx}{e}\right] \right) + 2 \text{PolyLog}\left[2, \frac{e+fx}{2e}\right] \right)$$

Problem 281: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \text{Log}\left[\frac{2e}{e+fx}\right]}{e^2 - f^2 x^2} dx$$

Optimal (type 4, 41 leaves, 4 steps):

$$\frac{a \text{ArcTanh}\left[\frac{fx}{e}\right]}{ef} + \frac{b \text{PolyLog}\left[2, 1 - \frac{2e}{e+fx}\right]}{2ef}$$

Result (type 4, 115 leaves):

$$\frac{1}{4ef} \left(-b \text{Log}\left[\frac{e}{f} + x\right]^2 - 2a \text{Log}[e - fx] + 2b \text{Log}\left[\frac{e}{f} + x\right] \text{Log}\left[\frac{e - fx}{2e}\right] + 4b \text{ArcTanh}\left[\frac{fx}{e}\right] \left(\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{2e}{e+fx}\right] \right) + 2a \text{Log}[e + fx] + 2b \text{PolyLog}\left[2, \frac{e+fx}{2e}\right] \right)$$

Problem 282: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \text{Log}\left[\frac{-e}{e+fx}\right]}{e^2 - f^2 x^2} dx$$

Optimal (type 4, 47 leaves, 4 steps):

$$\frac{\text{ArcTanh}\left[\frac{fx}{e}\right] (a - b \text{Log}[2])}{ef} + \frac{b \text{PolyLog}\left[2, 1 - \frac{2e}{e+fx}\right]}{2ef}$$

Result (type 4, 114 leaves):

$$\frac{1}{4 e f} \left(-b \operatorname{Log} \left[\frac{e}{f} + x \right]^2 - 2 a \operatorname{Log} [e - f x] + 2 b \operatorname{Log} \left[\frac{e}{f} + x \right] \operatorname{Log} \left[\frac{e - f x}{2 e} \right] + \right. \\ \left. 4 b \operatorname{ArcTanh} \left[\frac{f x}{e} \right] \left(\operatorname{Log} \left[\frac{e}{f} + x \right] + \operatorname{Log} \left[\frac{e}{e + f x} \right] \right) + 2 a \operatorname{Log} [e + f x] + 2 b \operatorname{PolyLog} \left[2, \frac{e + f x}{2 e} \right] \right)$$

Problem 293: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^7 \operatorname{Log} [c + d x]}{a + b x^4} dx$$

Optimal (type 4, 498 leaves, 23 steps):

$$\frac{c^3 x}{4 b d^3} - \frac{c^2 x^2}{8 b d^2} + \frac{c x^3}{12 b d} - \frac{x^4}{16 b} - \frac{c^4 \operatorname{Log} [c + d x]}{4 b d^4} + \frac{x^4 \operatorname{Log} [c + d x]}{4 b} - \frac{a \operatorname{Log} \left[\frac{d \left(\sqrt{-\sqrt{-a}} - b^{1/4} x \right)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d} \right] \operatorname{Log} [c + d x]}{4 b^2} - \\ \frac{a \operatorname{Log} \left[\frac{d \left((-a)^{1/4} - b^{1/4} x \right)}{b^{1/4} c + (-a)^{1/4} d} \right] \operatorname{Log} [c + d x]}{4 b^2} - \frac{a \operatorname{Log} \left[-\frac{d \left(\sqrt{-\sqrt{-a}} + b^{1/4} x \right)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d} \right] \operatorname{Log} [c + d x]}{4 b^2} - \frac{a \operatorname{Log} \left[-\frac{d \left((-a)^{1/4} + b^{1/4} x \right)}{b^{1/4} c - (-a)^{1/4} d} \right] \operatorname{Log} [c + d x]}{4 b^2} - \\ \frac{a \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d} \right]}{4 b^2} - \frac{a \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d} \right]}{4 b^2} - \frac{a \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-a)^{1/4} d} \right]}{4 b^2} - \frac{a \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-a)^{1/4} d} \right]}{4 b^2}$$

Result (type 4, 441 leaves):

$$-\frac{1}{48 b^2 d^4} \left(-12 b c^3 d x + 6 b c^2 d^2 x^2 - 4 b c d^3 x^3 + 3 b d^4 x^4 + 12 b c^4 \operatorname{Log} [c + d x] - 12 b d^4 x^4 \operatorname{Log} [c + d x] + 12 a d^4 \operatorname{Log} [c + d x] \operatorname{Log} \left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d} \right] + \right. \\ \left. 12 a d^4 \operatorname{Log} [c + d x] \operatorname{Log} \left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d} \right] + 12 a d^4 \operatorname{Log} [c + d x] \operatorname{Log} \left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d} \right] + \right. \\ \left. 12 a d^4 \operatorname{Log} [c + d x] \operatorname{Log} \left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d} \right] + 12 a d^4 \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d} \right] + \right. \\ \left. 12 a d^4 \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d} \right] + 12 a d^4 \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d} \right] + 12 a d^4 \operatorname{PolyLog} \left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d} \right] \right)$$

Problem 294: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 \operatorname{Log}[c + d x]}{a + b x^4} dx$$

Optimal (type 4, 401 leaves, 18 steps):

$$\frac{\operatorname{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}}-b^{1/4}x\right)}{b^{1/4}c+\sqrt{-\sqrt{-a}}d}\right] \operatorname{Log}[c+dx]}{4b} + \frac{\operatorname{Log}\left[\frac{d\left((-a)^{1/4}-b^{1/4}x\right)}{b^{1/4}c+(-a)^{1/4}d}\right] \operatorname{Log}[c+dx]}{4b} + \frac{\operatorname{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}}+b^{1/4}x\right)}{b^{1/4}c-\sqrt{-\sqrt{-a}}d}\right] \operatorname{Log}[c+dx]}{4b} + \frac{\operatorname{Log}\left[-\frac{d\left((-a)^{1/4}+b^{1/4}x\right)}{b^{1/4}c-(-a)^{1/4}d}\right] \operatorname{Log}[c+dx]}{4b} +$$

$$\frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-\sqrt{-\sqrt{-a}}d}\right]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+\sqrt{-\sqrt{-a}}d}\right]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-(-a)^{1/4}d}\right]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+(-a)^{1/4}d}\right]}{4b}$$

Result (type 4, 328 leaves):

$$\frac{1}{4b} \left(\operatorname{Log}[c+dx] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+dx)}{b^{1/4}c - (-1)^{1/4}a^{1/4}d}\right] + \operatorname{Log}[c+dx] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+dx)}{b^{1/4}c + (-1)^{1/4}a^{1/4}d}\right] + \right.$$

$$\left. \operatorname{Log}[c+dx] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+dx)}{b^{1/4}c - (-1)^{3/4}a^{1/4}d}\right] + \operatorname{Log}[c+dx] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+dx)}{b^{1/4}c + (-1)^{3/4}a^{1/4}d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c - (-1)^{1/4}a^{1/4}d}\right] + \right.$$

$$\left. \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c + (-1)^{1/4}a^{1/4}d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c - (-1)^{3/4}a^{1/4}d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c + (-1)^{3/4}a^{1/4}d}\right] \right)$$

Problem 295: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[c + d x]}{x(a + b x^4)} dx$$

Optimal (type 4, 433 leaves, 22 steps):

$$\begin{aligned}
& \frac{\text{Log}\left[-\frac{dx}{c}\right] \text{Log}[c+dx]}{a} - \frac{\text{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}}-b^{1/4}x\right)}{b^{1/4}c+\sqrt{-\sqrt{-a}}d}\right] \text{Log}[c+dx]}{4a} - \frac{\text{Log}\left[\frac{d\left((-a)^{1/4}-b^{1/4}x\right)}{b^{1/4}c+(-a)^{1/4}d}\right] \text{Log}[c+dx]}{4a} \\
& \frac{\text{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}}+b^{1/4}x\right)}{b^{1/4}c-\sqrt{-\sqrt{-a}}d}\right] \text{Log}[c+dx]}{4a} - \frac{\text{Log}\left[-\frac{d\left((-a)^{1/4}+b^{1/4}x\right)}{b^{1/4}c-(-a)^{1/4}d}\right] \text{Log}[c+dx]}{4a} - \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-\sqrt{-\sqrt{-a}}d}\right]}{4a} \\
& \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+\sqrt{-\sqrt{-a}}d}\right]}{4a} - \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-(-a)^{1/4}d}\right]}{4a} - \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+(-a)^{1/4}d}\right]}{4a} + \frac{\text{PolyLog}\left[2, 1+\frac{dx}{c}\right]}{a}
\end{aligned}$$

Result (type 4, 362 leaves):

$$\begin{aligned}
& -\frac{1}{4a} \left(-4 \text{Log}[x] \text{Log}[c+dx] + 4 \text{Log}[x] \text{Log}\left[1+\frac{dx}{c}\right] + \text{Log}[c+dx] \text{Log}\left[1-\frac{b^{1/4}(c+dx)}{b^{1/4}c-(-1)^{1/4}a^{1/4}d}\right] + \right. \\
& \quad \text{Log}[c+dx] \text{Log}\left[1-\frac{b^{1/4}(c+dx)}{b^{1/4}c+(-1)^{1/4}a^{1/4}d}\right] + \text{Log}[c+dx] \text{Log}\left[1-\frac{b^{1/4}(c+dx)}{b^{1/4}c-(-1)^{3/4}a^{1/4}d}\right] + \\
& \quad \text{Log}[c+dx] \text{Log}\left[1-\frac{b^{1/4}(c+dx)}{b^{1/4}c+(-1)^{3/4}a^{1/4}d}\right] + 4 \text{PolyLog}\left[2, -\frac{dx}{c}\right] + \text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-(-1)^{1/4}a^{1/4}d}\right] + \\
& \quad \left. \text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+(-1)^{1/4}a^{1/4}d}\right] + \text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c-(-1)^{3/4}a^{1/4}d}\right] + \text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4}c+(-1)^{3/4}a^{1/4}d}\right] \right)
\end{aligned}$$

Problem 296: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 \text{Log}[c+dx]}{a+bx^4} dx$$

Optimal (type 4, 530 leaves, 23 steps):

$$\frac{c x}{2 b d} - \frac{x^2}{4 b} - \frac{c^2 \operatorname{Log}[c+d x]}{2 b d^2} + \frac{x^2 \operatorname{Log}[c+d x]}{2 b} - \frac{\sqrt{-a} \operatorname{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}}-b^{1/4} x\right)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4 b^{3/2}} + \frac{\sqrt{-a} \operatorname{Log}\left[\frac{d\left((-a)^{1/4}-b^{1/4} x\right)}{b^{1/4} c+(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4 b^{3/2}} -$$

$$\frac{\sqrt{-a} \operatorname{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}}+b^{1/4} x\right)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4 b^{3/2}} + \frac{\sqrt{-a} \operatorname{Log}\left[-\frac{d\left((-a)^{1/4}+b^{1/4} x\right)}{b^{1/4} c-(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4 b^{3/2}} - \frac{\sqrt{-a} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right]}{4 b^{3/2}} -$$

$$\frac{\sqrt{-a} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right]}{4 b^{3/2}} + \frac{\sqrt{-a} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-(-a)^{1/4} d}\right]}{4 b^{3/2}} + \frac{\sqrt{-a} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+(-a)^{1/4} d}\right]}{4 b^{3/2}}$$

Result (type 4, 473 leaves):

$$-\frac{1}{4 b^{3/2} d^2} \left(2 i \sqrt{b} c d x - i \sqrt{b} d^2 x^2 - 2 i \sqrt{b} c^2 \operatorname{Log}[c+d x] + 2 i \sqrt{b} d^2 x^2 \operatorname{Log}[c+d x] - \sqrt{a} d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - \right.$$

$$\left. \sqrt{a} d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \sqrt{a} d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + \right.$$

$$\left. \sqrt{a} d^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] - \sqrt{a} d^2 \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - \right.$$

$$\left. \sqrt{a} d^2 \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \sqrt{a} d^2 \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + \sqrt{a} d^2 \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right)$$

Problem 297: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x \operatorname{Log}[c+d x]}{a+b x^4} dx$$

Optimal (type 4, 473 leaves, 18 steps):

$$-\frac{\operatorname{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}}-b^{1/4} x\right)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4 \sqrt{-a} \sqrt{b}} + \frac{\operatorname{Log}\left[\frac{d\left((-a)^{1/4}-b^{1/4} x\right)}{b^{1/4} c+(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4 \sqrt{-a} \sqrt{b}} - \frac{\operatorname{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}}+b^{1/4} x\right)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4 \sqrt{-a} \sqrt{b}} + \frac{\operatorname{Log}\left[-\frac{d\left((-a)^{1/4}+b^{1/4} x\right)}{b^{1/4} c-(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4 \sqrt{-a} \sqrt{b}} -$$

$$\frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right]}{4 \sqrt{-a} \sqrt{b}} - \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right]}{4 \sqrt{-a} \sqrt{b}} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-(-a)^{1/4} d}\right]}{4 \sqrt{-a} \sqrt{b}} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+(-a)^{1/4} d}\right]}{4 \sqrt{-a} \sqrt{b}}$$

Result (type 4, 343 leaves):

$$\begin{aligned}
& - \frac{1}{4 \sqrt{a} \sqrt{b}} \\
& i \left(\text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] - \right. \\
& \quad \left. \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] + \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - \right. \\
& \quad \left. \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] - \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right)
\end{aligned}$$

Problem 298: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c + d x]}{x^3 (a + b x^4)} dx$$

Optimal (type 4, 537 leaves, 23 steps):

$$\begin{aligned}
& - \frac{d}{2 a c x} - \frac{d^2 \text{Log}[x]}{2 a c^2} + \frac{d^2 \text{Log}[c + d x]}{2 a c^2} - \frac{\text{Log}[c + d x]}{2 a x^2} - \frac{\sqrt{b} \text{Log}\left[\frac{d \left(\sqrt{-\sqrt{-a}} - b^{1/4} x\right)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right] \text{Log}[c + d x]}{4 (-a)^{3/2}} + \\
& \frac{\sqrt{b} \text{Log}\left[\frac{d \left((-a)^{1/4} - b^{1/4} x\right)}{b^{1/4} c + (-a)^{1/4} d}\right] \text{Log}[c + d x]}{4 (-a)^{3/2}} - \frac{\sqrt{b} \text{Log}\left[-\frac{d \left(\sqrt{-\sqrt{-a}} + b^{1/4} x\right)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right] \text{Log}[c + d x]}{4 (-a)^{3/2}} + \frac{\sqrt{b} \text{Log}\left[-\frac{d \left((-a)^{1/4} + b^{1/4} x\right)}{b^{1/4} c - (-a)^{1/4} d}\right] \text{Log}[c + d x]}{4 (-a)^{3/2}} - \\
& \frac{\sqrt{b} \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right]}{4 (-a)^{3/2}} - \frac{\sqrt{b} \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right]}{4 (-a)^{3/2}} + \frac{\sqrt{b} \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4 (-a)^{3/2}} + \frac{\sqrt{b} \text{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4 (-a)^{3/2}}
\end{aligned}$$

Result (type 4, 416 leaves):

$$\frac{1}{4 a^{3/2}} \left(-\frac{2 \sqrt{a} (c d x + d^2 x^2 \operatorname{Log}[x] + (c^2 - d^2 x^2) \operatorname{Log}[c + d x])}{c^2 x^2} + i \sqrt{b} \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] \right) + i \sqrt{b} \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] \right) - i \sqrt{b} \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] \right) - i \sqrt{b} \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right) \right)$$

Problem 299: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4 \operatorname{Log}[c + d x]}{a + b x^4} dx$$

Optimal (type 4, 521 leaves, 22 steps):

$$\begin{aligned} & -\frac{x}{b} + \frac{(c + d x) \operatorname{Log}[c + d x]}{b d} + \frac{\sqrt{-\sqrt{-a}} \operatorname{Log}\left[\frac{d(\sqrt{-\sqrt{-a}} - b^{1/4} x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c + d x]}{4 b^{5/4}} + \frac{(-a)^{1/4} \operatorname{Log}\left[\frac{d((-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4 b^{5/4}} - \\ & \frac{\sqrt{-\sqrt{-a}} \operatorname{Log}\left[-\frac{d(\sqrt{-\sqrt{-a}} + b^{1/4} x)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c + d x]}{4 b^{5/4}} - \frac{(-a)^{1/4} \operatorname{Log}\left[-\frac{d((-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4 b^{5/4}} - \frac{\sqrt{-\sqrt{-a}} \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right]}{4 b^{5/4}} + \\ & \frac{\sqrt{-\sqrt{-a}} \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right]}{4 b^{5/4}} - \frac{(-a)^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4 b^{5/4}} + \frac{(-a)^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4 b^{5/4}} \end{aligned}$$

Result (type 4, 470 leaves):

$$\frac{1}{4 b^{5/4} d} (-1)^{3/4} \left(4 (-1)^{1/4} b^{1/4} c + 4 (-1)^{1/4} b^{1/4} d x - 4 (-1)^{1/4} b^{1/4} c \operatorname{Log}[c + d x] - 4 (-1)^{1/4} b^{1/4} d x \operatorname{Log}[c + d x] + \right. \\ \left. i a^{1/4} d \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - i a^{1/4} d \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - \right. \\ \left. a^{1/4} d \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + a^{1/4} d \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] + \right. \\ \left. i a^{1/4} d \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - i a^{1/4} d \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - \right. \\ \left. a^{1/4} d \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + a^{1/4} d \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right)$$

Problem 300: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 \operatorname{Log}[c + d x]}{a + b x^4} dx$$

Optimal (type 4, 497 leaves, 18 steps):

$$\frac{\operatorname{Log}\left[\frac{d(\sqrt{-\sqrt{-a}} - b^{1/4} x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c + d x]}{4 \sqrt{-\sqrt{-a}} b^{3/4}} + \frac{\operatorname{Log}\left[\frac{d((-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4 (-a)^{1/4} b^{3/4}} - \frac{\operatorname{Log}\left[-\frac{d(\sqrt{-\sqrt{-a}} + b^{1/4} x)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c + d x]}{4 \sqrt{-\sqrt{-a}} b^{3/4}} - \frac{\operatorname{Log}\left[-\frac{d((-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4 (-a)^{1/4} b^{3/4}} - \\ \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right]}{4 \sqrt{-\sqrt{-a}} b^{3/4}} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4 \sqrt{-\sqrt{-a}} b^{3/4}} - \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4 (-a)^{1/4} b^{3/4}} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4 (-a)^{1/4} b^{3/4}}$$

Result (type 4, 357 leaves):

$$\frac{1}{4 a^{1/4} b^{3/4}} (-1)^{3/4} \left(\operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - i \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + \right. \\ \left. i \operatorname{Log}[c + d x] \operatorname{Log}\left[1 - \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] - \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] - \right. \\ \left. i \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + i \operatorname{PolyLog}\left[2, \frac{b^{1/4} (c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right)$$

Problem 301: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c + d x]}{a + b x^4} dx$$

Optimal (type 4, 497 leaves, 18 steps):

$$\frac{\text{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}} - b^{1/4} x\right)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right] \text{Log}[c + d x]}{4\left(-\sqrt{-a}\right)^{3/2} b^{1/4}} + \frac{\text{Log}\left[\frac{d\left((-a)^{1/4} - b^{1/4} x\right)}{b^{1/4} c + (-a)^{1/4} d}\right] \text{Log}[c + d x]}{4(-a)^{3/4} b^{1/4}} - \frac{\text{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}} + b^{1/4} x\right)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right] \text{Log}[c + d x]}{4\left(-\sqrt{-a}\right)^{3/2} b^{1/4}} - \frac{\text{Log}\left[-\frac{d\left((-a)^{1/4} + b^{1/4} x\right)}{b^{1/4} c - (-a)^{1/4} d}\right] \text{Log}[c + d x]}{4(-a)^{3/4} b^{1/4}} -$$

$$\frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4} c - \sqrt{-\sqrt{-a}} d}\right]}{4\left(-\sqrt{-a}\right)^{3/2} b^{1/4}} + \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4} c + \sqrt{-\sqrt{-a}} d}\right]}{4\left(-\sqrt{-a}\right)^{3/2} b^{1/4}} - \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4(-a)^{3/4} b^{1/4}} + \frac{\text{PolyLog}\left[2, \frac{b^{1/4}(c+dx)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4(-a)^{3/4} b^{1/4}}$$

Result (type 4, 357 leaves):

$$\frac{1}{4 a^{3/4} b^{1/4}} (-1)^{3/4} \left(-i \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + i \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \right.$$

$$\left. \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] - \text{Log}[c + d x] \text{Log}\left[1 - \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] - i \text{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + \right.$$

$$\left. i \text{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \text{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] - \text{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right)$$

Problem 302: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c + d x]}{x^2 (a + b x^4)} dx$$

Optimal (type 4, 536 leaves, 24 steps):

$$\begin{aligned} & \frac{d \operatorname{Log}[x]}{a c} - \frac{d \operatorname{Log}[c+d x]}{a c} - \frac{\operatorname{Log}[c+d x]}{a x} + \frac{b^{1/4} \operatorname{Log}\left[\frac{d\left(\sqrt{-\sqrt{-a}}-b^{1/4} x\right)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4\left(-\sqrt{-a}\right)^{5/2}} + \frac{b^{1/4} \operatorname{Log}\left[\frac{d\left((-a)^{1/4}-b^{1/4} x\right)}{b^{1/4} c+(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4(-a)^{5/4}} - \\ & \frac{b^{1/4} \operatorname{Log}\left[-\frac{d\left(\sqrt{-\sqrt{-a}}+b^{1/4} x\right)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right] \operatorname{Log}[c+d x]}{4\left(-\sqrt{-a}\right)^{5/2}} - \frac{b^{1/4} \operatorname{Log}\left[-\frac{d\left((-a)^{1/4}+b^{1/4} x\right)}{b^{1/4} c-(-a)^{1/4} d}\right] \operatorname{Log}[c+d x]}{4(-a)^{5/4}} - \frac{b^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-\sqrt{-\sqrt{-a}} d}\right]}{4\left(-\sqrt{-a}\right)^{5/2}} + \\ & \frac{b^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+\sqrt{-\sqrt{-a}} d}\right]}{4\left(-\sqrt{-a}\right)^{5/2}} - \frac{b^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c-(-a)^{1/4} d}\right]}{4(-a)^{5/4}} + \frac{b^{1/4} \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c+(-a)^{1/4} d}\right]}{4(-a)^{5/4}} \end{aligned}$$

Result (type 4, 412 leaves):

$$\begin{aligned} & \frac{1}{4 a^{5/4}} \left(\frac{4 a^{1/4} (d x \operatorname{Log}[x] - (c+d x) \operatorname{Log}[c+d x])}{c x} - (-1)^{3/4} b^{1/4} \left(\operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{1/4} a^{1/4} d}\right] \right) \right) + \\ & (-1)^{3/4} b^{1/4} \left(\operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{1/4} a^{1/4} d}\right] \right) - \\ & (-1)^{1/4} b^{1/4} \left(\operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c - (-1)^{3/4} a^{1/4} d}\right] \right) + \\ & (-1)^{1/4} b^{1/4} \left(\operatorname{Log}[c+d x] \operatorname{Log}\left[1 - \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] + \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c+d x)}{b^{1/4} c + (-1)^{3/4} a^{1/4} d}\right] \right) \end{aligned}$$

Problem 309: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[a+b x]}{c + \frac{d}{x^2}} dx$$

Optimal (type 4, 247 leaves, 12 steps):

$$\begin{aligned} & -\frac{x}{c} + \frac{(a+b x) \operatorname{Log}[a+b x]}{b c} - \frac{\sqrt{d} \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b\left(\sqrt{d}-\sqrt{-c} x\right)}{a \sqrt{-c}+b \sqrt{d}}\right]}{2(-c)^{3/2}} + \\ & \frac{\sqrt{d} \operatorname{Log}[a+b x] \operatorname{Log}\left[-\frac{b\left(\sqrt{d}+\sqrt{-c} x\right)}{a \sqrt{-c}-b \sqrt{d}}\right]}{2(-c)^{3/2}} + \frac{\sqrt{d} \operatorname{PolyLog}\left[2, \frac{\sqrt{-c}(a+b x)}{a \sqrt{-c}-b \sqrt{d}}\right]}{2(-c)^{3/2}} - \frac{\sqrt{d} \operatorname{PolyLog}\left[2, \frac{\sqrt{-c}(a+b x)}{a \sqrt{-c}+b \sqrt{d}}\right]}{2(-c)^{3/2}} \end{aligned}$$

Result (type 4, 205 leaves):

$$\frac{(a + b x) (-1 + \operatorname{Log}[a + b x])}{b c} - \frac{i \sqrt{d} \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[1 - \frac{\sqrt{c} (a + b x)}{a \sqrt{c} - i b \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{c} (a + b x)}{a \sqrt{c} - i b \sqrt{d}}\right]\right)}{2 c^{3/2}} +$$

$$\frac{i \sqrt{d} \left(\operatorname{Log}[a + b x] \operatorname{Log}\left[1 - \frac{\sqrt{c} (a + b x)}{a \sqrt{c} + i b \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{c} (a + b x)}{a \sqrt{c} + i b \sqrt{d}}\right]\right)}{2 c^{3/2}}$$

Problem 310: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 (a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 831 leaves, 28 steps):

$$\begin{aligned} & - \frac{2 a b d f n x}{e g^2} + \frac{2 b^2 d f n^2 x}{e g^2} - \frac{2 b^2 d^3 n^2 x}{e^3 g} - \frac{b^2 f n^2 (d + e x)^2}{4 e^2 g^2} + \frac{3 b^2 d^2 n^2 (d + e x)^2}{4 e^4 g} - \frac{2 b^2 d n^2 (d + e x)^3}{9 e^4 g} + \\ & \frac{b^2 n^2 (d + e x)^4}{32 e^4 g} + \frac{b^2 d^4 n^2 \operatorname{Log}[d + e x]^2}{4 e^4 g} - \frac{2 b^2 d f n (d + e x) \operatorname{Log}[c (d + e x)^n]}{e^2 g^2} + \frac{2 b d^3 n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])}{e^4 g} + \\ & \frac{b f n (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 e^2 g^2} - \frac{3 b d^2 n (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 e^4 g} + \frac{2 b d n (d + e x)^3 (a + b \operatorname{Log}[c (d + e x)^n])}{3 e^4 g} - \\ & \frac{b n (d + e x)^4 (a + b \operatorname{Log}[c (d + e x)^n])}{8 e^4 g} - \frac{b d^4 n \operatorname{Log}[d + e x] (a + b \operatorname{Log}[c (d + e x)^n])}{2 e^4 g} + \frac{x^4 (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 g} + \\ & \frac{d f (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e^2 g^2} - \frac{f (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 e^2 g^2} + \frac{f^2 (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^3} + \\ & \frac{f^2 (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^3} + \frac{b f^2 n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{g^3} + \\ & \frac{b f^2 n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{g^3} - \frac{b^2 f^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{g^3} - \frac{b^2 f^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{g^3} \end{aligned}$$

Result (type 4, 861 leaves):

$$\begin{aligned}
& - \frac{1}{288 e^4 g^3} \left(144 e^4 f g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - 72 e^4 g^2 x^4 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - \right. \\
& 144 e^4 f^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + 12 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\
& \left. \left(12 e^2 f g (e x (2 d - e x) - 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x]) + g^2 (e x (-12 d^3 + 6 d^2 e x - 4 d e^2 x^2 + 3 e^3 x^3) + 12 (d^4 - e^4 x^4) \operatorname{Log}[d + e x]) \right) - \right. \\
& 24 e^4 f^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& 24 e^4 f^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. \right) + \\
& b^2 n^2 \left(72 e^2 f g (e x (-6 d + e x) + (6 d^2 + 4 d e x - 2 e^2 x^2) \operatorname{Log}[d + e x] - 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x]^2) + \right. \\
& g^2 (e x (300 d^3 - 78 d^2 e x + 28 d e^2 x^2 - 9 e^3 x^3) - 12 (25 d^4 + 12 d^3 e x - 6 d^2 e^2 x^2 + 4 d e^3 x^3 - 3 e^4 x^4) \operatorname{Log}[d + e x] + 72 (d^4 - e^4 x^4) \operatorname{Log}[d + e x]^2) - \\
& 144 e^4 f^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& 144 e^4 f^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 311: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 (a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 499 leaves, 21 steps):

$$\frac{2 a b d n x}{e g} - \frac{2 b^2 d n^2 x}{e g} + \frac{b^2 n^2 (d + e x)^2}{4 e^2 g} + \frac{2 b^2 d n (d + e x) \operatorname{Log}[c (d + e x)^n]}{e^2 g} - \frac{b n (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{2 e^2 g} -$$

$$\frac{d (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e^2 g} + \frac{(d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 e^2 g} - \frac{f (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2} -$$

$$\frac{f (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2} - \frac{b f n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^2} -$$

$$\frac{b f n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^2} + \frac{b^2 f n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^2} + \frac{b^2 f n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^2}$$

Result (type 4, 635 leaves):

$$\frac{1}{4 e^2 g^2} \left(2 e^2 g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - \right.$$

$$2 e^2 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + 2 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])$$

$$\left(e g x (2 d - e x) - 2 g (d^2 - e^2 x^2) \operatorname{Log}[d + e x] - 2 e^2 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right.$$

$$2 e^2 f \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. \right) +$$

$$b^2 n^2 \left(g (e x (-6 d + e x) + (6 d^2 + 4 d e x - 2 e^2 x^2) \operatorname{Log}[d + e x] - 2 (d^2 - e^2 x^2) \operatorname{Log}[d + e x]^2) - \right.$$

$$2 e^2 f \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) -$$

$$2 e^2 f \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. \right) \left. \right)$$

Problem 312: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x (a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 317 leaves, 10 steps):

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} - \sqrt{g} x}}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{2g} + \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} + \sqrt{g} x}}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{2g} + \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{g} +$$

$$\frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{g} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{g} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{g}$$

Result (type 4, 464 leaves):

$$\frac{1}{2g} \left((a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + 2 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \right.$$

$$\left. \left(\operatorname{Log}[d + e x] \left(\operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] + \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right) + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right) +$$

$$b^2 n^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] + \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] +$$

$$\left. \left. 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right) \right)$$

Problem 313: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{x (f + g x^2)} dx$$

Optimal (type 4, 397 leaves, 16 steps):

$$\frac{\operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])^2}{f} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} - \sqrt{g} x}}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{2f} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} + \sqrt{g} x}}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{2f} -$$

$$\frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{f} - \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{f} +$$

$$\frac{2 b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{f} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{f} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{f} - \frac{2 b^2 n^2 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{f}$$

Result (type 4, 584 leaves):

$$\begin{aligned}
& -\frac{1}{2f} \left(-2 \operatorname{Log}[x] (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 + (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \operatorname{Log}[f + gx^2] - \right. \\
& 2bn(-a + bn \operatorname{Log}[d + ex] - b \operatorname{Log}[c (d + ex)^n]) \left(-2 \operatorname{Log}[x] \operatorname{Log}[d + ex] + 2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + \operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \right. \\
& \left. \left. \operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2 \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) + \right. \\
& b^2 n^2 \left(-2 \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d + ex]^2 + \operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \right. \\
& 2 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] - \right. \\
& \left. \left. 4 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 4 \operatorname{PolyLog}\left[3, 1 + \frac{ex}{d}\right] \right) \right)
\end{aligned}$$

Problem 314: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + ex)^n])^2}{x^3 (f + gx^2)} dx$$

Optimal (type 4, 551 leaves, 23 steps):

$$\begin{aligned}
& \frac{b^2 e^2 n^2 \operatorname{Log}[x]}{d^2 f} - \frac{b e n (d + ex) (a + b \operatorname{Log}[c (d + ex)^n])}{d^2 f x} - \frac{(a + b \operatorname{Log}[c (d + ex)^n])^2}{2 f x^2} - \frac{g \operatorname{Log}\left[-\frac{ex}{d}\right] (a + b \operatorname{Log}[c (d + ex)^n])^2}{f^2} + \\
& \frac{g (a + b \operatorname{Log}[c (d + ex)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 f^2} + \frac{g (a + b \operatorname{Log}[c (d + ex)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 f^2} - \\
& \frac{b e^2 n (a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{Log}\left[1 - \frac{d}{d + ex}\right]}{d^2 f} + \frac{b^2 e^2 n^2 \operatorname{PolyLog}\left[2, \frac{d}{d + ex}\right]}{d^2 f} + \frac{b g n (a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d + ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{f^2} + \\
& \frac{b g n (a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{f^2} - \frac{2 b g n (a + b \operatorname{Log}[c (d + ex)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right]}{f^2} - \\
& \frac{b^2 g n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g}(d + ex)}{e\sqrt{-f} - d\sqrt{g}}\right]}{f^2} - \frac{b^2 g n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{e\sqrt{-f} + d\sqrt{g}}\right]}{f^2} + \frac{2 b^2 g n^2 \operatorname{PolyLog}\left[3, 1 + \frac{ex}{d}\right]}{f^2}
\end{aligned}$$

Result (type 4, 801 leaves):

$$\begin{aligned}
& - \frac{1}{2 d^2 f^2 x^2} \left(d^2 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + 2 d^2 g x^2 \operatorname{Log}[x] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - \right. \\
& \quad d^2 g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + 2 b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\
& \quad \left. \left(f (d e x + e^2 x^2 \operatorname{Log}[x] + (d^2 - e^2 x^2) \operatorname{Log}[d + e x]) + 2 d^2 g x^2 \left(\operatorname{Log}[x] \left(\operatorname{Log}[d + e x] - \operatorname{Log}\left[1 + \frac{e x}{d}\right]\right) - \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]\right) - \right. \right. \\
& \quad \quad d^2 g x^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& \quad \quad \left. \left. d^2 g x^2 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \right) + \\
& \quad b^2 n^2 \left(f \left(2 e^2 x^2 \operatorname{Log}\left[-\frac{e x}{d}\right] (-1 + \operatorname{Log}[d + e x]) + (d + e x) \operatorname{Log}[d + e x] (2 e x + (d - e x) \operatorname{Log}[d + e x]) + 2 e^2 x^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] \right) - \right. \\
& \quad \quad d^2 g x^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& \quad \quad d^2 g x^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\
& \quad \quad \left. \left. 2 d^2 g x^2 \left(\operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d + e x]^2 + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] - 2 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right] \right) \right) \right)
\end{aligned}$$

Problem 315: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4 (a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 701 leaves, 23 steps):

$$\begin{aligned}
& \frac{2 a b f n x}{g^2} - \frac{2 b^2 f n^2 x}{g^2} + \frac{2 b^2 d^2 n^2 x}{e^2 g} - \frac{b^2 d n^2 (d+e x)^2}{2 e^3 g} + \frac{2 b^2 n^2 (d+e x)^3}{27 e^3 g} - \frac{b^2 d^3 n^2 \operatorname{Log}[d+e x]^2}{3 e^3 g} + \\
& \frac{2 b^2 f n (d+e x) \operatorname{Log}[c (d+e x)^n]}{e g^2} - \frac{2 b d^2 n (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])}{e^3 g} + \frac{b d n (d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])}{e^3 g} - \\
& \frac{2 b n (d+e x)^3 (a+b \operatorname{Log}[c (d+e x)^n])}{9 e^3 g} + \frac{2 b d^3 n \operatorname{Log}[d+e x] (a+b \operatorname{Log}[c (d+e x)^n])}{3 e^3 g} + \frac{x^3 (a+b \operatorname{Log}[c (d+e x)^n])^2}{3 g} - \\
& \frac{f (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^2}{e g^2} + \frac{(-f)^{3/2} (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2 g^{5/2}} - \\
& \frac{(-f)^{3/2} (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2 g^{5/2}} - \frac{b (-f)^{3/2} n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{g^{5/2}} + \\
& \frac{b (-f)^{3/2} n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{g^{5/2}} + \frac{b^2 (-f)^{3/2} n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g}(d+e x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{g^{5/2}} - \frac{b^2 (-f)^{3/2} n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d+e x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{g^{5/2}}
\end{aligned}$$

Result (type 4, 816 leaves):

$$\begin{aligned}
& \frac{1}{54 e^3 g^{5/2}} \left(-54 e^3 f \sqrt{g} x (a - b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n])^2 + 18 e^3 g^{3/2} x^3 (a - b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n])^2 + \right. \\
& 54 e^3 f^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n])^2 + 6 b n (a - b n \operatorname{Log}[d+e x] + b \operatorname{Log}[c (d+e x)^n]) \\
& \left(-18 e^2 f \sqrt{g} (d+e x) (-1 + \operatorname{Log}[d+e x]) + g^{3/2} (e x (-6 d^2 + 3 d e x - 2 e^2 x^2) + 6 (d^3 + e^3 x^3) \operatorname{Log}[d+e x]) + \right. \\
& 9 i e^3 f^{3/2} \left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - 9 i e^3 f^{3/2} \\
& \left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. + i b^2 n^2 \left(54 i e^2 f \sqrt{g} (d+e x) (2 - 2 \operatorname{Log}[d+e x] + \operatorname{Log}[d+e x]^2) + \right. \right. \\
& i g^{3/2} (e x (-66 d^2 + 15 d e x - 4 e^2 x^2) + 6 (11 d^3 + 6 d^2 e x - 3 d e^2 x^2 + 2 e^3 x^3) \operatorname{Log}[d+e x] - 18 (d^3 + e^3 x^3) \operatorname{Log}[d+e x]^2) + \\
& 27 e^3 f^{3/2} \left(\operatorname{Log}[d+e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d+e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d+e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& \left. 27 e^3 f^{3/2} \left(\operatorname{Log}[d+e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d+e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d+e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 316: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 447 leaves, 16 steps):

$$\begin{aligned} & -\frac{2 a b n x}{g} + \frac{2 b^2 n^2 x}{g} - \frac{2 b^2 n (d + e x) \operatorname{Log}[c (d + e x)^n]}{e g} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e g} + \frac{\sqrt{-f} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 g^{3/2}} \\ & - \frac{\sqrt{-f} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 g^{3/2}} - \frac{b \sqrt{-f} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{g^{3/2}} + \\ & \frac{b \sqrt{-f} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{g^{3/2}} + \frac{b^2 \sqrt{-f} n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{g^{3/2}} - \frac{b^2 \sqrt{-f} n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{g^{3/2}} \end{aligned}$$

Result (type 4, 614 leaves):

$$\begin{aligned} & \frac{1}{e g^{3/2}} \left(e \sqrt{g} x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - \right. \\ & \left. e \sqrt{f} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + i b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \right. \\ & \left. \left(-2 i \sqrt{g} (d + e x) (-1 + \operatorname{Log}[d + e x]) - e \sqrt{f} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right. \\ & \left. e \sqrt{f} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) + b^2 n^2 \left(\sqrt{g} (d + e x) (2 - 2 \operatorname{Log}[d + e x] + \operatorname{Log}[d + e x]^2) - \right. \\ & \left. \frac{1}{2} i e \sqrt{f} \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right. \\ & \left. \frac{1}{2} i e \sqrt{f} \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) \end{aligned}$$

Problem 317: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} dx$$

Optimal (type 4, 371 leaves, 10 steps):

$$\frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} - \sqrt{g} x}}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{2 \sqrt{-f} \sqrt{g}} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e^{\sqrt{-f} + \sqrt{g} x}}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{2 \sqrt{-f} \sqrt{g}} - \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{\sqrt{-f} \sqrt{g}} +$$

$$\frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{\sqrt{-f} \sqrt{g}} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} - d \sqrt{g}}}\right]}{\sqrt{-f} \sqrt{g}} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e^{\sqrt{-f} + d \sqrt{g}}}\right]}{\sqrt{-f} \sqrt{g}}$$

Result (type 4, 485 leaves):

$$\frac{1}{\sqrt{f} \sqrt{g}} \left(\operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + i b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \right.$$

$$\left. \left(\operatorname{Log}[d + e x] \left(\operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] - \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right) + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] - \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right) +$$

$$\frac{1}{2} i b^2 n^2 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] - \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] -$$

$$2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e^{\sqrt{f} + d \sqrt{g}}}\right] + 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e^{\sqrt{f} + d \sqrt{g}}}\right] \right)$$

Problem 318: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{x^2 (f + g x^2)} dx$$

Optimal (type 4, 461 leaves, 15 steps):

$$\frac{2 b e n \operatorname{Log}\left[-\frac{e x}{d}\right] (a+b \operatorname{Log}[c(d+e x)^n])}{d f}-\frac{(d+e x)(a+b \operatorname{Log}[c(d+e x)^n])^2}{d f x}+$$

$$\frac{\sqrt{g}(a+b \operatorname{Log}[c(d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{2(-f)^{3 / 2}}-\frac{\sqrt{g}(a+b \operatorname{Log}[c(d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{2(-f)^{3 / 2}}-$$

$$\frac{b \sqrt{g} n(a+b \operatorname{Log}[c(d+e x)^n]) \operatorname{PolyLog}\left[2,-\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{(-f)^{3 / 2}}+\frac{b \sqrt{g} n(a+b \operatorname{Log}[c(d+e x)^n]) \operatorname{PolyLog}\left[2,\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{(-f)^{3 / 2}}+$$

$$\frac{2 b^2 e n^2 \operatorname{PolyLog}\left[2,1+\frac{e x}{d}\right]}{d f}+\frac{b^2 \sqrt{g} n^2 \operatorname{PolyLog}\left[3,-\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{(-f)^{3 / 2}}-\frac{b^2 \sqrt{g} n^2 \operatorname{PolyLog}\left[3,\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{(-f)^{3 / 2}}$$

Result (type 4, 654 leaves):

$$\frac{1}{2 d f^{3 / 2} x}\left(-2 d \sqrt{f}(a-b n \operatorname{Log}[d+e x]+b \operatorname{Log}[c(d+e x)^n])^2-\right.$$

$$2 d \sqrt{g} x \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right](a-b n \operatorname{Log}[d+e x]+b \operatorname{Log}[c(d+e x)^n])^2+2 b n(a-b n \operatorname{Log}[d+e x]+b \operatorname{Log}[c(d+e x)^n])$$

$$\left(2 \sqrt{f}(e x \operatorname{Log}[x]-(d+e x) \operatorname{Log}[d+e x])-\mathrm{i} d \sqrt{g} x\left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1-\frac{\sqrt{g}(d+e x)}{-\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]+\operatorname{PolyLog}\left[2,\frac{\sqrt{g}(d+e x)}{-\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]\right)+\right.$$

$$\left.\left.\mathrm{i} d \sqrt{g} x\left(\operatorname{Log}[d+e x] \operatorname{Log}\left[1-\frac{\sqrt{g}(d+e x)}{\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]+\operatorname{PolyLog}\left[2,\frac{\sqrt{g}(d+e x)}{\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]\right)\right)\right)$$

$$b^2 n^2\left(2 \sqrt{f}\left(2 e x \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d+e x]-(d+e x) \operatorname{Log}[d+e x]^2+2 e x \operatorname{PolyLog}\left[2,1+\frac{e x}{d}\right]\right)-\right.$$

$$\left.\mathrm{i} d \sqrt{g} x\left(\operatorname{Log}[d+e x]^2 \operatorname{Log}\left[1-\frac{\sqrt{g}(d+e x)}{-\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]+2 \operatorname{Log}[d+e x] \operatorname{PolyLog}\left[2,\frac{\sqrt{g}(d+e x)}{-\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]-2 \operatorname{PolyLog}\left[3,\frac{\sqrt{g}(d+e x)}{-\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]\right)+\right.$$

$$\left.\left.\mathrm{i} d \sqrt{g} x\left(\operatorname{Log}[d+e x]^2 \operatorname{Log}\left[1-\frac{\sqrt{g}(d+e x)}{\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]+2 \operatorname{Log}[d+e x] \operatorname{PolyLog}\left[2,\frac{\sqrt{g}(d+e x)}{\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]-2 \operatorname{PolyLog}\left[3,\frac{\sqrt{g}(d+e x)}{\mathrm{i} e \sqrt{f}+d \sqrt{g}}\right]\right)\right)\right)$$

Problem 319: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a+b \operatorname{Log}[c(d+e x)^n])^2}{x^4(f+g x^2)} d x$$

Optimal (type 4, 694 leaves, 26 steps):

$$\begin{aligned}
 & -\frac{b^2 e^2 n^2}{3 d^2 f x} - \frac{b^2 e^3 n^2 \operatorname{Log}[x]}{d^3 f} + \frac{b^2 e^3 n^2 \operatorname{Log}[d + e x]}{3 d^3 f} - \frac{b e n (a + b \operatorname{Log}[c (d + e x)^n])}{3 d f x^2} + \\
 & \frac{2 b e^2 n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])}{3 d^3 f x} - \frac{2 b e g n \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{d f^2} - \\
 & \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{3 f x^3} + \frac{g (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{d f^2 x} + \frac{g^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{5/2}} - \\
 & \frac{g^{3/2} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2}} + \frac{2 b e^3 n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[1 - \frac{d}{d + e x}\right]}{3 d^3 f} - \frac{2 b^2 e^3 n^2 \operatorname{PolyLog}\left[2, \frac{d}{d + e x}\right]}{3 d^3 f} - \\
 & \frac{b g^{3/2} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{(-f)^{5/2}} + \frac{b g^{3/2} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{(-f)^{5/2}} - \\
 & \frac{2 b^2 e g n^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{d f^2} + \frac{b^2 g^{3/2} n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{(-f)^{5/2}} - \frac{b^2 g^{3/2} n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{(-f)^{5/2}}
 \end{aligned}$$

Result (type 4, 886 leaves):

$$\begin{aligned}
& \frac{1}{6 d^3 f^{5/2} x^3} \left(-2 d^3 f^{3/2} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + 6 d^3 \sqrt{f} g x^2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + \right. \\
& 6 d^3 g^{3/2} x^3 \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + 2 i b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\
& \left. \left(6 i d^2 \sqrt{f} g x^2 (e x \operatorname{Log}[x] - (d + e x) \operatorname{Log}[d + e x]) + i f^{3/2} (d e x (d - 2 e x) - 2 e^3 x^3 \operatorname{Log}[x] + 2 (d^3 + e^3 x^3) \operatorname{Log}[d + e x]) + \right. \right. \\
& 3 d^3 g^{3/2} x^3 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& \left. 3 d^3 g^{3/2} x^3 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) - \\
& b^2 n^2 \left(6 d^2 \sqrt{f} g x^2 \left(2 e x \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d + e x] - (d + e x) \operatorname{Log}[d + e x]^2 + 2 e x \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] \right) - 2 f^{3/2} \left(e^3 x^3 \operatorname{Log}\left[-\frac{e x}{d}\right] \right. \right. \\
& \left. \left. (-3 + 2 \operatorname{Log}[d + e x]) - (d + e x) (e^2 x^2 + e x (d - 3 e x) \operatorname{Log}[d + e x] + (d^2 - d e x + e^2 x^2) \operatorname{Log}[d + e x]^2) + 2 e^3 x^3 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] \right) \right) - \\
& 3 i d^3 g^{3/2} x^3 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\
& 3 i d^3 g^{3/2} x^3 \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 320: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^5 (a + b \operatorname{Log}[c (d + e x)^n])^2}{(f + g x^2)^2} dx$$

Optimal (type 4, 936 leaves, 34 steps):

$$\begin{aligned}
& \frac{2 a b d n x}{e g^2} - \frac{2 b^2 d n^2 x}{e g^2} + \frac{b^2 n^2 (d+e x)^2}{4 e^2 g^2} + \frac{2 b^2 d n (d+e x) \operatorname{Log}[c (d+e x)^n]}{e^2 g^2} - \frac{b n (d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])}{2 e^2 g^2} + \\
& \frac{e^2 f^2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{2 g^3 (e^2 f+d^2 g)} - \frac{d (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^2}{e^2 g^2} + \frac{(d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{2 e^2 g^2} - \\
& \frac{f^2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{2 g^3 (f+g x^2)} - \frac{b e f (e f+d \sqrt{-f} \sqrt{g}) n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{2 g^3 (e^2 f+d^2 g)} - \\
& \frac{f (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g} x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{g^3} - \frac{b e (-f)^{3/2} (e \sqrt{-f}+d \sqrt{g}) n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{2 g^3 (e^2 f+d^2 g)} - \\
& \frac{f (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g} x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{g^3} - \frac{b^2 e (-f)^{3/2} (e \sqrt{-f}+d \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{2 g^3 (e^2 f+d^2 g)} - \\
& \frac{2 b f n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{g^3} - \frac{b^2 e (-f)^{3/2} (e \sqrt{-f}-d \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{2 g^3 (e^2 f+d^2 g)} - \\
& \frac{2 b f n (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+e x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{g^3} + \frac{2 b^2 f n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g}(d+e x)}{e \sqrt{-f}-d \sqrt{g}}\right]}{g^3} + \frac{2 b^2 f n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d+e x)}{e \sqrt{-f}+d \sqrt{g}}\right]}{g^3}
\end{aligned}$$

Result (type 4, 1272 leaves):

$$\begin{aligned}
& \frac{1}{4g^3} \left(2gx^2 (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 - \right. \\
& \frac{2f^2 (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2}{f + gx^2} - 4f (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \operatorname{Log}[f + gx^2] + \\
& bn (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n]) \left(-\frac{2g (ex(-2d + ex) + 2(d^2 - e^2x^2) \operatorname{Log}[d + ex])}{e^2} + \right. \\
& \left. \left(f^{3/2} \left(2e (-i\sqrt{f} + \sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] + 2i\sqrt{g} (d + ex) \operatorname{Log}[d + ex] - e (\sqrt{f} + i\sqrt{g}x) \operatorname{Log}[f + gx^2] \right) \right) / \left((e\sqrt{f} - id\sqrt{g}) \right. \\
& \left. (\sqrt{f} + i\sqrt{g}x) \right) + \left(i f^{3/2} \left(2e (\sqrt{f} - i\sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + e (i\sqrt{f} + \sqrt{g}x) \operatorname{Log}[f + gx^2] \right) \right) / \\
& \left. \left((e\sqrt{f} + id\sqrt{g}) (\sqrt{f} - i\sqrt{g}x) \right) - 8f \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) - \right. \\
& \left. 8f \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) + \\
& b^2 n^2 \left(\frac{g (ex(-6d + ex) + (6d^2 + 4dex - 2e^2x^2) \operatorname{Log}[d + ex] - 2(d^2 - e^2x^2) \operatorname{Log}[d + ex]^2)}{e^2} + \left(i f^{3/2} \left(-\sqrt{g} (d + ex) \operatorname{Log}[d + ex]^2 + \right. \right. \right. \\
& \left. \left. 2e (i\sqrt{f} + \sqrt{g}x) \operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2e (i\sqrt{f} + \sqrt{g}x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \\
& \left. \left((e\sqrt{f} + id\sqrt{g}) (\sqrt{f} - i\sqrt{g}x) \right) - \left(f^{3/2} \left(\operatorname{Log}[d + ex] \left(-i\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + 2e (\sqrt{f} + i\sqrt{g}x) \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) \right) + \right. \\
& \left. 2e (\sqrt{f} + i\sqrt{g}x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \left((e\sqrt{f} - id\sqrt{g}) (\sqrt{f} + i\sqrt{g}x) \right) - \\
& 4f \left(\operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) - \\
& \left. 4f \left(\operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) \right)
\end{aligned}$$

Problem 321: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 (a + b \operatorname{Log}[c (d + e x)^n])^2}{(f + g x^2)^2} dx$$

Optimal (type 4, 739 leaves, 25 steps):

$$\begin{aligned} & - \frac{e^2 f (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 g^2 (e^2 f + d^2 g)} + \frac{f (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 g^2 (f + g x^2)} + \frac{b e (e f + d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2 (e^2 f + d^2 g)} + \\ & \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2} + \frac{b e (e f - d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2 (e^2 f + d^2 g)} + \\ & \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2} - \frac{b^2 e \sqrt{-f} (e \sqrt{-f} + d \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 g^2 (e^2 f + d^2 g)} + \\ & \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^2} + \frac{b^2 e (e f + d \sqrt{-f} \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 g^2 (e^2 f + d^2 g)} + \\ & \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^2} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{g^2} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{g^2} \end{aligned}$$

Result (type 4, 1124 leaves):

$$\begin{aligned}
& \frac{1}{4g^2} \left(\frac{2f(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^2}{f + gx^2} + \right. \\
& 2(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n])^2 \operatorname{Log}[f + gx^2] + bn(a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c(d + ex)^n]) \\
& \left. \left(\left(\sqrt{f} \left(2ie(\sqrt{f} + i\sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2i\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + e(\sqrt{f} + i\sqrt{g}x) \operatorname{Log}[f + gx^2] \right) \right) / \left((e\sqrt{f} - id\sqrt{g}) \right. \right. \right. \\
& \left. \left. \left(\sqrt{f} + i\sqrt{g}x \right) - \left(i\sqrt{f} \left(2e(\sqrt{f} - i\sqrt{g}x) \operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + e(i\sqrt{f} + \sqrt{g}x) \operatorname{Log}[f + gx^2] \right) \right) \right) / \right. \\
& \left. \left((e\sqrt{f} + id\sqrt{g})(\sqrt{f} - i\sqrt{g}x) \right) + 4 \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) + \\
& 4 \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \Bigg) + \\
& b^2 n^2 \left(2 \operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2 \operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 4 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& \left(\sqrt{f} \left(\operatorname{Log}[d + ex] \left(i\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + 2e(\sqrt{f} - i\sqrt{g}x) \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + 2e(\sqrt{f} - i\sqrt{g}x) \right. \right. \\
& \left. \left. \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \left((e\sqrt{f} + id\sqrt{g})(\sqrt{f} - i\sqrt{g}x) \right) + 4 \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \\
& \left(\sqrt{f} \left(\operatorname{Log}[d + ex] \left(-i\sqrt{g}(d + ex) \operatorname{Log}[d + ex] + 2e(\sqrt{f} + i\sqrt{g}x) \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) + 2e(\sqrt{f} + i\sqrt{g}x) \operatorname{PolyLog}\left[\right. \right. \\
& \left. \left. 2, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}} \right] \right) \right) / \left((e\sqrt{f} - id\sqrt{g})(\sqrt{f} + i\sqrt{g}x) \right) - 4 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 4 \operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \Bigg)
\end{aligned}$$

Problem 322: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x(a + b \operatorname{Log}[c(d + ex)^n])^2}{(f + gx^2)^2} dx$$

Optimal (type 4, 430 leaves, 13 steps):

$$\frac{e^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 g (e^2 f + d^2 g)} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{2 g (f + g x^2)} -$$

$$\frac{b e (e f + d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f g (e^2 f + d^2 g)} - \frac{b e (e f - d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f g (e^2 f + d^2 g)} -$$

$$\frac{b^2 e (e \sqrt{-f} + d \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 \sqrt{-f} g (e^2 f + d^2 g)} - \frac{b^2 e (e f + d \sqrt{-f} \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f g (e^2 f + d^2 g)}$$

Result (type 4, 544 leaves):

$$\frac{1}{4 g} \left(-\frac{2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} + \left(2 b n (-a + b n \operatorname{Log}[d + e x] - b \operatorname{Log}[c (d + e x)^n]) \left(-2 d e \sqrt{g} (f + g x^2) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + \right. \right. \right.$$

$$\left. \left. \sqrt{f} (2 g (d^2 - e^2 x^2) \operatorname{Log}[d + e x] + e^2 (f + g x^2) \operatorname{Log}[f + g x^2]) \right) \right) / \left(\sqrt{f} (e^2 f + d^2 g) (f + g x^2) \right) + \frac{1}{\sqrt{f}} i b^2 n^2$$

$$\left(\left(-\sqrt{g} (d + e x) \operatorname{Log}[d + e x]^2 + 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) / \right.$$

$$\left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) + \left(\operatorname{Log}[d + e x] \left(\sqrt{g} (d + e x) \operatorname{Log}[d + e x] + 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right.$$

$$\left. \left. 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) / \left((e \sqrt{f} - i d \sqrt{g}) (\sqrt{f} + i \sqrt{g} x) \right) \right)$$

Problem 323: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{x (f + g x^2)^2} dx$$

Optimal (type 4, 814 leaves, 29 steps):

$$\begin{aligned}
& - \frac{e^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 f (e^2 f + d^2 g)} + \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{2 f (f + g x^2)} + \frac{\operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])^2}{f^2} + \\
& \frac{b e (e f + d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^2 (e^2 f + d^2 g)} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^2} + \\
& \frac{b e (e f - d \sqrt{-f} \sqrt{g}) n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f^2 (e^2 f + d^2 g)} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f^2} - \\
& \frac{b^2 e (e \sqrt{-f} + d \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{3/2} (e^2 f + d^2 g)} - \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^2} + \\
& \frac{b^2 e (e f + d \sqrt{-f} \sqrt{g}) n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^2 (e^2 f + d^2 g)} - \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^2} + \\
& \frac{2 b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{f^2} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^2} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^2} - \frac{2 b^2 n^2 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{f^2}
\end{aligned}$$

Result (type 4, 1235 leaves):

$$\begin{aligned}
& \frac{1}{4 f^2} \left(\frac{2 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} + 4 \operatorname{Log}[x] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 - \right. \\
& 2 (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(8 \operatorname{Log}[x] \left(\operatorname{Log}[d + e x] - \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) \right. \\
& \left. \left. \left(\sqrt{f} \left(2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \\
& \left. (\sqrt{f} + i \sqrt{g} x) \right) - \left(i \sqrt{f} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) \right) / \\
& \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 8 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] - 4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) - \\
& 4 \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) + \\
& b^2 n^2 \left(4 \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d + e x]^2 - 2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 4 \operatorname{Log}[d + e x] \right. \\
& \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \left(\sqrt{f} \left(\operatorname{Log}[d + e x] \left(i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + 2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) \right. \right. \\
& \left. \left. + 2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 4 \operatorname{Log}[d + e x] \\
& \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \left(\sqrt{f} \left(\operatorname{Log}[d + e x] \left(-i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + 2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right. \right. \\
& \left. \left. + 2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) (\sqrt{f} + i \sqrt{g} x) \right) + \\
& \left. 8 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] + 4 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 4 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 8 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right] \right) \right)
\end{aligned}$$

Problem 324: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{x^3 (f + g x^2)^2} dx$$

Optimal (type 4, 970 leaves, 36 steps):

$$\begin{aligned}
& \frac{b^2 e^2 n^2 \operatorname{Log}[x]}{d^2 f^2} - \frac{b e n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])}{d^2 f^2 x} + \frac{e^2 g (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 f^2 (e^2 f + d^2 g)} - \\
& \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{2 f^2 x^2} - \frac{g (a + b \operatorname{Log}[c (d + e x)^n])^2}{2 f^2 (f + g x^2)} - \frac{2 g \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])^2}{f^3} - \\
& \frac{b e (e f + d \sqrt{-f} \sqrt{g}) g n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^3 (e^2 f + d^2 g)} + \frac{g (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^3} - \\
& \frac{b e (e f - d \sqrt{-f} \sqrt{g}) g n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f^3 (e^2 f + d^2 g)} + \frac{g (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^3} - \\
& \frac{b e^2 n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[1 - \frac{d}{d + e x}\right]}{d^2 f^2} + \frac{b^2 e^2 n^2 \operatorname{PolyLog}\left[2, \frac{d}{d + e x}\right]}{d^2 f^2} - \frac{b^2 e (e \sqrt{-f} + d \sqrt{g}) g n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2} (e^2 f + d^2 g)} + \\
& \frac{2 b g n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^3} - \frac{b^2 e (e f + d \sqrt{-f} \sqrt{g}) g n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^3 (e^2 f + d^2 g)} + \\
& \frac{2 b g n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^3} - \frac{4 b g n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{f^3} - \\
& \frac{2 b^2 g n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{f^3} - \frac{2 b^2 g n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{f^3} + \frac{4 b^2 g n^2 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{f^3}
\end{aligned}$$

Result (type 4, 1416 leaves):

$$\begin{aligned}
& \frac{1}{4 f^3} \left(-\frac{2 f (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{x^2} - \frac{2 f g (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} - \right. \\
& 8 g \operatorname{Log}[x] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + 4 g (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[f + g x^2] + \\
& \left. b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(-\frac{4 f (d e x + e^2 x^2 \operatorname{Log}[x] + (d^2 - e^2 x^2) \operatorname{Log}[d + e x])}{d^2 x^2} + \right. \right. \\
& \left. \left. \frac{\left(\sqrt{f} g \left(2 e (-i \sqrt{f} + \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 i \sqrt{g} (d + e x) \operatorname{Log}[d + e x] - e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right)}{\left((e \sqrt{f} - i d \sqrt{g}) \right.} \right. \\
& \left. \left. (\sqrt{f} + i \sqrt{g} x) \right) + \left(i \sqrt{f} g \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right)}{\left((e \sqrt{f} + i d \sqrt{g}) \right.} \right. \\
& \left. \left. (\sqrt{f} - i \sqrt{g} x) \right) - 16 g \left(\operatorname{Log}[x] \left(\operatorname{Log}[d + e x] - \operatorname{Log}\left[1 + \frac{e x}{d}\right] \right) - \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& 8g \left(\text{Log}[d+ex] \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& 8g \left(\text{Log}[d+ex] \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& b^2 n^2 \left(\left(ie\sqrt{f}g \left(-\sqrt{g}(d+ex) \text{Log}[d+ex]^2 + 2e \left(ie\sqrt{f} + \sqrt{g}x \right) \text{Log}[d+ex] \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \right. \right. \right. \\
& \quad \left. \left. \left. 2e \left(ie\sqrt{f} + \sqrt{g}x \right) \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \left(\left(e\sqrt{f} + id\sqrt{g} \right) \left(\sqrt{f} - ie\sqrt{g}x \right) \right) - \right. \\
& \quad \left. \left(\sqrt{f}g \left(\text{Log}[d+ex] \left(-ie\sqrt{g}(d+ex) \text{Log}[d+ex] + 2e \left(\sqrt{f} + ie\sqrt{g}x \right) \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) + \right. \right. \\
& \quad \left. \left. 2e \left(\sqrt{f} + ie\sqrt{g}x \right) \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \left(\left(e\sqrt{f} - id\sqrt{g} \right) \left(\sqrt{f} + ie\sqrt{g}x \right) \right) - \frac{1}{d^2 x^2} \right. \\
& 2f \left(2e^2 x^2 \text{Log}\left[-\frac{ex}{d}\right] \left(-1 + \text{Log}[d+ex] \right) + (d+ex) \text{Log}[d+ex] \left(2ex + (d-ex) \text{Log}[d+ex] \right) + 2e^2 x^2 \text{PolyLog}\left[2, 1 + \frac{ex}{d}\right] \right) + \\
& 4g \left(\text{Log}[d+ex]^2 \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2 \text{Log}[d+ex] \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 2 \text{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& 4g \left(\text{Log}[d+ex]^2 \text{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2 \text{Log}[d+ex] \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] - 2 \text{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) - \\
& 8g \left(\text{Log}\left[-\frac{ex}{d}\right] \text{Log}[d+ex]^2 + 2 \text{Log}[d+ex] \text{PolyLog}\left[2, 1 + \frac{ex}{d}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{ex}{d}\right] \right) \Big) \Big) \Big)
\end{aligned}$$

Problem 325: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^4 (a + b \text{Log}[c(d+ex)^n])^2}{(f+gx^2)^2} dx$$

Optimal (type 4, 897 leaves, 36 steps):

$$\begin{aligned}
& -\frac{2abnx}{g^2} + \frac{2b^2n^2x}{g^2} - \frac{2b^2n(d+ex)\text{Log}[c(d+ex)^n]}{eg^2} + \frac{(d+ex)(a+b\text{Log}[c(d+ex)^n])^2}{eg^2} - \frac{f(d+ex)(a+b\text{Log}[c(d+ex)^n])^2}{4(e\sqrt{-f}+d\sqrt{g})g^2(\sqrt{-f}-\sqrt{g}x)} \\
& \frac{f(d+ex)(a+b\text{Log}[c(d+ex)^n])^2}{4(e\sqrt{-f}-d\sqrt{g})g^2(\sqrt{-f}+\sqrt{g}x)} - \frac{befn(a+b\text{Log}[c(d+ex)^n])\text{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g}x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2(e\sqrt{-f}+d\sqrt{g})g^{5/2}} + \frac{3\sqrt{-f}(a+b\text{Log}[c(d+ex)^n])^2\text{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g}x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{4g^{5/2}} \\
& \frac{befn(a+b\text{Log}[c(d+ex)^n])\text{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g}x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(e\sqrt{-f}-d\sqrt{g})g^{5/2}} - \frac{3\sqrt{-f}(a+b\text{Log}[c(d+ex)^n])^2\text{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g}x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{4g^{5/2}} + \\
& \frac{b^2efn^2\text{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(e\sqrt{-f}-d\sqrt{g})g^{5/2}} - \frac{3b\sqrt{-f}n(a+b\text{Log}[c(d+ex)^n])\text{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2g^{5/2}} - \frac{b^2efn^2\text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2(e\sqrt{-f}+d\sqrt{g})g^{5/2}} + \\
& \frac{3b\sqrt{-f}n(a+b\text{Log}[c(d+ex)^n])\text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2g^{5/2}} + \frac{3b^2\sqrt{-f}n^2\text{PolyLog}\left[3, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2g^{5/2}} - \frac{3b^2\sqrt{-f}n^2\text{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2g^{5/2}}
\end{aligned}$$

Result (type 4, 1247 leaves):

$$\begin{aligned}
& \frac{1}{4g^{5/2}} \left(4\sqrt{g} x (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 + \right. \\
& \frac{2f\sqrt{g} x (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2}{f + gx^2} - 6\sqrt{f} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 + \\
& bn (a - bn \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n]) \left(\frac{8\sqrt{g} (d + ex) (-1 + \operatorname{Log}[d + ex])}{e} + \right. \\
& \left. \left(f \left(-2e (\sqrt{f} + i\sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + ie (\sqrt{f} + i\sqrt{g} x) \operatorname{Log}[f + gx^2] \right) \right) / \left((e\sqrt{f} - id\sqrt{g}) \right. \right. \\
& \left. \left. (\sqrt{f} + i\sqrt{g} x) \right) - \left(f \left(2e (\sqrt{f} - i\sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + e (i\sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + gx^2] \right) \right) / \right. \\
& \left. \left((e\sqrt{f} + id\sqrt{g}) (\sqrt{f} - i\sqrt{g} x) \right) - 6ie\sqrt{f} \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& \left. 6ie\sqrt{f} \left(\operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) + \\
& b^2 n^2 \left(\frac{4\sqrt{g} (d + ex) (2 - 2\operatorname{Log}[d + ex] + \operatorname{Log}[d + ex]^2)}{e} - \left(f \left(-\sqrt{g} (d + ex) \operatorname{Log}[d + ex]^2 + \right. \right. \right. \\
& \left. \left. 2e (i\sqrt{f} + \sqrt{g} x) \operatorname{Log}[d + ex] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2e (i\sqrt{f} + \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) / \\
& \left((e\sqrt{f} + id\sqrt{g}) (\sqrt{f} - i\sqrt{g} x) \right) + \left(f \left(\operatorname{Log}[d + ex] \left(\sqrt{g} (d + ex) \operatorname{Log}[d + ex] + 2ie (\sqrt{f} + i\sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right) + \right. \\
& \left. 2ie (\sqrt{f} + i\sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) / \left((e\sqrt{f} - id\sqrt{g}) (\sqrt{f} + i\sqrt{g} x) \right) - \\
& 3ie\sqrt{f} \left(\operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2\operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 2\operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) + \\
& \left. 3ie\sqrt{f} \left(\operatorname{Log}[d + ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2\operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] - 2\operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 326: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 (a + b \operatorname{Log}[c (d + e x)^n])^2}{(f + g x^2)^2} dx$$

Optimal (type 4, 815 leaves, 32 steps):

$$\begin{aligned} & \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 (e \sqrt{-f} + d \sqrt{g}) g (\sqrt{-f} - \sqrt{g} x)} + \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 (e \sqrt{-f} - d \sqrt{g}) g (\sqrt{-f} + \sqrt{g} x)} + \frac{b e n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (e \sqrt{-f} + d \sqrt{g}) g^{3/2}} + \\ & \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 \sqrt{-f} g^{3/2}} - \frac{b e n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (e \sqrt{-f} - d \sqrt{g}) g^{3/2}} - \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 \sqrt{-f} g^{3/2}} - \\ & \frac{b^2 e n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (e \sqrt{-f} - d \sqrt{g}) g^{3/2}} - \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 \sqrt{-f} g^{3/2}} + \frac{b^2 e n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (e \sqrt{-f} + d \sqrt{g}) g^{3/2}} + \\ & \frac{b n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 \sqrt{-f} g^{3/2}} + \frac{b^2 n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 \sqrt{-f} g^{3/2}} - \frac{b^2 n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 \sqrt{-f} g^{3/2}} \end{aligned}$$

Result (type 4, 1149 leaves):

$$\begin{aligned}
& \frac{1}{4g^{3/2}} \left(-\frac{2\sqrt{g}x(a - bn\operatorname{Log}[d+ex] + b\operatorname{Log}[c(d+ex)^n])^2}{f+gx^2} + \frac{2\operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right](a - bn\operatorname{Log}[d+ex] + b\operatorname{Log}[c(d+ex)^n])^2}{\sqrt{f}} + \right. \\
& bn(a - bn\operatorname{Log}[d+ex] + b\operatorname{Log}[c(d+ex)^n]) \left(\frac{2e(\sqrt{f} + i\sqrt{g}x)\operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g}(d+ex)\operatorname{Log}[d+ex] + e(-i\sqrt{f} + \sqrt{g}x)\operatorname{Log}[f+gx^2]}{(e\sqrt{f} - id\sqrt{g})(\sqrt{f} + i\sqrt{g}x)} + \right. \\
& \frac{2e(\sqrt{f} - i\sqrt{g}x)\operatorname{ArcTan}\left[\frac{\sqrt{g}x}{\sqrt{f}}\right] - 2\sqrt{g}(d+ex)\operatorname{Log}[d+ex] + e(i\sqrt{f} + \sqrt{g}x)\operatorname{Log}[f+gx^2]}{(e\sqrt{f} + id\sqrt{g})(\sqrt{f} - i\sqrt{g}x)} + \\
& \left. \frac{2i\left(\operatorname{Log}[d+ex]\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right]\right)}{\sqrt{f}} - \\
& \left. \frac{2i\left(\operatorname{Log}[d+ex]\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right]\right)}{\sqrt{f}} \right) + b^2n^2 \\
& \left(\left(-\sqrt{g}(d+ex)\operatorname{Log}[d+ex]^2 + 2e(i\sqrt{f} + \sqrt{g}x)\operatorname{Log}[d+ex]\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2e(i\sqrt{f} + \sqrt{g}x)\operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) / \right. \\
& \left((e\sqrt{f} + id\sqrt{g})(\sqrt{f} - i\sqrt{g}x) \right) - \left(\operatorname{Log}[d+ex] \left(\sqrt{g}(d+ex)\operatorname{Log}[d+ex] + 2ie(\sqrt{f} + i\sqrt{g}x)\operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) + \right. \\
& \left. 2ie(\sqrt{f} + i\sqrt{g}x)\operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) / \left((e\sqrt{f} - id\sqrt{g})(\sqrt{f} + i\sqrt{g}x) \right) + \frac{1}{\sqrt{f}} \\
& i \left(\operatorname{Log}[d+ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] + 2\operatorname{Log}[d+ex]\operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] - 2\operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{-ie\sqrt{f} + d\sqrt{g}}\right] \right) - \\
& \left. \frac{1}{\sqrt{f}} i \left(\operatorname{Log}[d+ex]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] + 2\operatorname{Log}[d+ex]\operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] - 2\operatorname{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{ie\sqrt{f} + d\sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 327: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b\operatorname{Log}[c(d+ex)^n])^2}{(f+gx^2)^2} dx$$

Optimal (type 4, 821 leaves, 20 steps):

$$\begin{aligned}
& - \frac{(d+ex)(a+b\log[c(d+ex)^n])^2}{4f(e\sqrt{-f}+d\sqrt{g})(\sqrt{-f}-\sqrt{g}x)} - \frac{(d+ex)(a+b\log[c(d+ex)^n])^2}{4f(e\sqrt{-f}-d\sqrt{g})(\sqrt{-f}+\sqrt{g}x)} - \frac{ben(a+b\log[c(d+ex)^n])\log\left[\frac{e(\sqrt{-f}-\sqrt{g}x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2f(e\sqrt{-f}+d\sqrt{g})\sqrt{g}} - \\
& \frac{(a+b\log[c(d+ex)^n])^2\log\left[\frac{e(\sqrt{-f}-\sqrt{g}x)}{e\sqrt{-f}+d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}} - \frac{ben(a+b\log[c(d+ex)^n])\log\left[\frac{e(\sqrt{-f}+\sqrt{g}x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(e(-f)^{3/2}+df\sqrt{g})\sqrt{g}} + \frac{(a+b\log[c(d+ex)^n])^2\log\left[\frac{e(\sqrt{-f}+\sqrt{g}x)}{e\sqrt{-f}-d\sqrt{g}}\right]}{4(-f)^{3/2}\sqrt{g}} - \\
& \frac{b^2e n^2 \text{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(e(-f)^{3/2}+df\sqrt{g})\sqrt{g}} + \frac{bn(a+b\log[c(d+ex)^n])\text{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(-f)^{3/2}\sqrt{g}} - \frac{b^2e n^2 \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2f(e\sqrt{-f}+d\sqrt{g})\sqrt{g}} - \\
& \frac{bn(a+b\log[c(d+ex)^n])\text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2(-f)^{3/2}\sqrt{g}} - \frac{b^2n^2 \text{PolyLog}\left[3, -\frac{\sqrt{g}(d+ex)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2(-f)^{3/2}\sqrt{g}} + \frac{b^2n^2 \text{PolyLog}\left[3, \frac{\sqrt{g}(d+ex)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2(-f)^{3/2}\sqrt{g}}
\end{aligned}$$

Result(type 4, 1162 leaves):

$$\begin{aligned}
& \frac{1}{4 f^{3/2}} \left(\frac{2 \sqrt{f} x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} + \right. \\
& \frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{\sqrt{g}} + \frac{1}{\sqrt{g}} b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \\
& \left. \left(\left(\sqrt{f} \left(-2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \right. \right. \\
& \left. \left. (\sqrt{f} + i \sqrt{g} x) \right) - \left(\sqrt{f} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \right. \\
& \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) + 2 i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \right. \\
& \left. 2 i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) + \\
& \frac{1}{\sqrt{g}} b^2 n^2 \left(- \left(\left(\sqrt{f} \left(-\sqrt{g} (d + e x) \operatorname{Log}[d + e x]^2 + 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \right. \right. \right. \right. \\
& \left. \left. 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) \right) + \\
& \left(\sqrt{f} \left(\operatorname{Log}[d + e x] \left(\sqrt{g} (d + e x) \operatorname{Log}[d + e x] + 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right. \right. \\
& \left. \left. 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) (\sqrt{f} + i \sqrt{g} x) \right) + \\
& i \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) - \\
& i \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right)
\end{aligned}$$

Problem 328: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x)^n])^2}{x^2 (f + g x^2)^2} dx$$

Optimal (type 4, 919 leaves, 35 steps):

$$\begin{aligned} & \frac{2 b e n \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])}{d f^2} - \frac{(d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{d f^2 x} + \frac{g (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 f^2 (e \sqrt{-f} + d \sqrt{g}) (\sqrt{-f} - \sqrt{g} x)} + \\ & \frac{g (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{4 f^2 (e \sqrt{-f} - d \sqrt{g}) (\sqrt{-f} + \sqrt{g} x)} + \frac{b e \sqrt{g} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^2 (e \sqrt{-f} + d \sqrt{g})} - \frac{3 \sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{4 (-f)^{5/2}} + \\ & \frac{b e \sqrt{g} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f (e (-f)^{3/2} + d f \sqrt{g})} + \frac{3 \sqrt{g} (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{4 (-f)^{5/2}} + \\ & \frac{b^2 e \sqrt{g} n^2 \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 f (e (-f)^{3/2} + d f \sqrt{g})} + \frac{3 b \sqrt{g} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2}} + \\ & \frac{b^2 e \sqrt{g} n^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 f^2 (e \sqrt{-f} + d \sqrt{g})} - \frac{3 b \sqrt{g} n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{5/2}} + \\ & \frac{2 b^2 e n^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{d f^2} - \frac{3 b^2 \sqrt{g} n^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{g} (d + e x)}{e \sqrt{-f} - d \sqrt{g}}\right]}{2 (-f)^{5/2}} + \frac{3 b^2 \sqrt{g} n^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{e \sqrt{-f} + d \sqrt{g}}\right]}{2 (-f)^{5/2}} \end{aligned}$$

Result (type 4, 1322 leaves):

$$\begin{aligned}
& \frac{1}{4 f^{5/2}} \left(- \frac{4 \sqrt{f} (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{x} - \right. \\
& \frac{2 \sqrt{f} g x (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2}{f + g x^2} - 6 \sqrt{g} \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n])^2 + \\
& b n (a - b n \operatorname{Log}[d + e x] + b \operatorname{Log}[c (d + e x)^n]) \left(\frac{8 \sqrt{f} (e x \operatorname{Log}[x] - (d + e x) \operatorname{Log}[d + e x])}{d x} - \right. \\
& \left. \left(\sqrt{f} \sqrt{g} \left(-2 e (\sqrt{f} + i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] + 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) \right. \\
& \left. (\sqrt{f} + i \sqrt{g} x) \right) + \left(\sqrt{f} \sqrt{g} \left(2 e (\sqrt{f} - i \sqrt{g} x) \operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] - 2 \sqrt{g} (d + e x) \operatorname{Log}[d + e x] + e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[f + g x^2] \right) \right) / \\
& \left. \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - 6 i \sqrt{g} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right. \\
& \left. 6 i \sqrt{g} \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) + \\
& b^2 n^2 \left(\left(\sqrt{f} \sqrt{g} \left(-\sqrt{g} (d + e x) \operatorname{Log}[d + e x]^2 + 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + \right. \right. \right. \\
& \left. \left. 2 e (i \sqrt{f} + \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} + i d \sqrt{g}) (\sqrt{f} - i \sqrt{g} x) \right) - \\
& \left(\sqrt{f} \sqrt{g} \left(\operatorname{Log}[d + e x] \left(\sqrt{g} (d + e x) \operatorname{Log}[d + e x] + 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) + \right. \right. \\
& \left. \left. 2 i e (\sqrt{f} + i \sqrt{g} x) \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \right) / \left((e \sqrt{f} - i d \sqrt{g}) (\sqrt{f} + i \sqrt{g} x) \right) + \\
& \frac{4 \sqrt{f} \left(2 e x \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d + e x] - (d + e x) \operatorname{Log}[d + e x]^2 + 2 e x \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right] \right)}{d x} - \\
& 3 i \sqrt{g} \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{-i e \sqrt{f} + d \sqrt{g}}\right] \right) + \\
& 3 i \sqrt{g} \left(\operatorname{Log}[d + e x]^2 \operatorname{Log}\left[1 - \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] + 2 \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{g} (d + e x)}{i e \sqrt{f} + d \sqrt{g}}\right] \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 329: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c (a + b x)^n]^3}{d + e x^2} dx$$

Optimal (type 4, 477 leaves, 12 steps):

$$\frac{\text{Log}[c (a + b x)^n]^3 \text{Log}\left[\frac{b(\sqrt{-d} - \sqrt{e} x)}{b\sqrt{-d} + a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{\text{Log}[c (a + b x)^n]^3 \text{Log}\left[\frac{b(\sqrt{-d} + \sqrt{e} x)}{b\sqrt{-d} - a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{3n \text{Log}[c (a + b x)^n]^2 \text{PolyLog}\left[2, -\frac{\sqrt{e}(a + b x)}{b\sqrt{-d} - a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} +$$

$$\frac{3n \text{Log}[c (a + b x)^n]^2 \text{PolyLog}\left[2, \frac{\sqrt{e}(a + b x)}{b\sqrt{-d} + a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} + \frac{3n^2 \text{Log}[c (a + b x)^n] \text{PolyLog}\left[3, -\frac{\sqrt{e}(a + b x)}{b\sqrt{-d} - a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} -$$

$$\frac{3n^2 \text{Log}[c (a + b x)^n] \text{PolyLog}\left[3, \frac{\sqrt{e}(a + b x)}{b\sqrt{-d} + a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} - \frac{3n^3 \text{PolyLog}\left[4, -\frac{\sqrt{e}(a + b x)}{b\sqrt{-d} - a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} + \frac{3n^3 \text{PolyLog}\left[4, \frac{\sqrt{e}(a + b x)}{b\sqrt{-d} + a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}}$$

Result (type 4, 754 leaves):

$$\frac{1}{2\sqrt{d}\sqrt{e}} \left(-2n^3 \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[a + b x]^3 + 6n^2 \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[a + b x]^2 \text{Log}[c (a + b x)^n] -$$

$$6n \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[a + b x] \text{Log}[c (a + b x)^n]^2 + 2 \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[c (a + b x)^n]^3 + i n^3 \text{Log}[a + b x]^3 \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] -$$

$$3 i n^2 \text{Log}[a + b x]^2 \text{Log}[c (a + b x)^n] \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] + 3 i n \text{Log}[a + b x] \text{Log}[c (a + b x)^n]^2 \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] -$$

$$i n^3 \text{Log}[a + b x]^3 \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] + 3 i n^2 \text{Log}[a + b x]^2 \text{Log}[c (a + b x)^n] \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] -$$

$$3 i n \text{Log}[a + b x] \text{Log}[c (a + b x)^n]^2 \text{Log}\left[1 - \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] + 3 i n \text{Log}[c (a + b x)^n]^2 \text{PolyLog}\left[2, \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] -$$

$$3 i n \text{Log}[c (a + b x)^n]^2 \text{PolyLog}\left[2, \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] - 6 i n^2 \text{Log}[c (a + b x)^n] \text{PolyLog}\left[3, \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] +$$

$$6 i n^2 \text{Log}[c (a + b x)^n] \text{PolyLog}\left[3, \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] + 6 i n^3 \text{PolyLog}\left[4, \frac{\sqrt{e}(a + b x)}{-i b \sqrt{d} + a \sqrt{e}}\right] - 6 i n^3 \text{PolyLog}\left[4, \frac{\sqrt{e}(a + b x)}{i b \sqrt{d} + a \sqrt{e}}\right] \right)$$

Problem 330: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c (a + b x)^n]^2}{d + e x^2} dx$$

Optimal (type 4, 347 leaves, 10 steps):

$$\frac{\text{Log}[c (a + b x)^n]^2 \text{Log}\left[\frac{b(\sqrt{-d}-\sqrt{e}x)}{b\sqrt{-d}+a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{\text{Log}[c (a + b x)^n]^2 \text{Log}\left[\frac{b(\sqrt{-d}+\sqrt{e}x)}{b\sqrt{-d}-a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{n \text{Log}[c (a + b x)^n] \text{PolyLog}\left[2, -\frac{\sqrt{e}(a+bx)}{b\sqrt{-d}-a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} +$$

$$\frac{n \text{Log}[c (a + b x)^n] \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{b\sqrt{-d}+a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} + \frac{n^2 \text{PolyLog}\left[3, -\frac{\sqrt{e}(a+bx)}{b\sqrt{-d}-a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}} - \frac{n^2 \text{PolyLog}\left[3, \frac{\sqrt{e}(a+bx)}{b\sqrt{-d}+a\sqrt{e}}\right]}{\sqrt{-d}\sqrt{e}}$$

Result (type 4, 488 leaves):

$$\frac{1}{2\sqrt{d}\sqrt{e}}$$

$$\left(2n^2 \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[a+bx]^2 - 4n \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[a+bx] \text{Log}[c(a+bx)^n] + 2 \text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \text{Log}[c(a+bx)^n]^2 - i n^2 \text{Log}[a+bx]^2 \right.$$

$$\text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{-i b\sqrt{d} + a\sqrt{e}}\right] + 2i n \text{Log}[a+bx] \text{Log}[c(a+bx)^n] \text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{-i b\sqrt{d} + a\sqrt{e}}\right] + i n^2 \text{Log}[a+bx]^2 \text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{i b\sqrt{d} + a\sqrt{e}}\right] -$$

$$2i n \text{Log}[a+bx] \text{Log}[c(a+bx)^n] \text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{i b\sqrt{d} + a\sqrt{e}}\right] + 2i n \text{Log}[c(a+bx)^n] \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{-i b\sqrt{d} + a\sqrt{e}}\right] -$$

$$\left. 2i n \text{Log}[c(a+bx)^n] \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{i b\sqrt{d} + a\sqrt{e}}\right] - 2i n^2 \text{PolyLog}\left[3, \frac{\sqrt{e}(a+bx)}{-i b\sqrt{d} + a\sqrt{e}}\right] + 2i n^2 \text{PolyLog}\left[3, \frac{\sqrt{e}(a+bx)}{i b\sqrt{d} + a\sqrt{e}}\right] \right)$$

Problem 331: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}[c (a + b x)^n]}{d + e x^2} dx$$

Optimal (type 4, 229 leaves, 8 steps):

$$\frac{\text{Log}[c (a + b x)^n] \text{Log}\left[\frac{b(\sqrt{-d}-\sqrt{e}x)}{b\sqrt{-d}+a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{\text{Log}[c (a + b x)^n] \text{Log}\left[\frac{b(\sqrt{-d}+\sqrt{e}x)}{b\sqrt{-d}-a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} - \frac{n \text{PolyLog}\left[2, -\frac{\sqrt{e}(a+bx)}{b\sqrt{-d}-a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} + \frac{n \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{b\sqrt{-d}+a\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}}$$

Result (type 4, 232 leaves):

$$\frac{\text{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \left(-n \text{Log}[a+bx] + \text{Log}\left[c(a+bx)^n\right]\right)}{\sqrt{d}\sqrt{e}} +$$

$$n \left(\frac{i \left(\text{Log}[a+bx] \text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{-ib\sqrt{d}+a\sqrt{e}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{-ib\sqrt{d}+a\sqrt{e}}\right]\right)}{2\sqrt{d}\sqrt{e}} - \frac{i \left(\text{Log}[a+bx] \text{Log}\left[1 - \frac{\sqrt{e}(a+bx)}{ib\sqrt{d}+a\sqrt{e}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{e}(a+bx)}{ib\sqrt{d}+a\sqrt{e}}\right]\right)}{2\sqrt{d}\sqrt{e}} \right)$$

Problem 333: Unable to integrate problem.

$$\int \frac{\text{Log}\left[c - \frac{a(1-c)x^{-m}}{b}\right]}{x(a+bx^m)} dx$$

Optimal (type 4, 27 leaves, 4 steps):

$$\frac{\text{PolyLog}\left[2, \frac{(1-c)(b+ax^{-m})}{b}\right]}{am}$$

Result (type 8, 34 leaves):

$$\int \frac{\text{Log}\left[c - \frac{a(1-c)x^{-m}}{b}\right]}{x(a+bx^m)} dx$$

Problem 334: Unable to integrate problem.

$$\int \frac{\text{Log}\left[\frac{x^{-m}(-a+ac+bcx^m)}{b}\right]}{x(a+bx^m)} dx$$

Optimal (type 4, 27 leaves, 5 steps):

$$\frac{\text{PolyLog}\left[2, \frac{(1-c)(b+ax^{-m})}{b}\right]}{am}$$

Result (type 8, 38 leaves):

$$\int \frac{\text{Log}\left[\frac{x^{-m}(-a+ac+bcx^m)}{b}\right]}{x(a+bx^m)} dx$$

Problem 335: Unable to integrate problem.

$$\int \frac{\text{Log}\left[c \left(a - \frac{(d-acd)x^{-m}}{ce}\right)\right]}{x(d+ex^m)} dx$$

Optimal (type 4, 28 leaves, 4 steps):

$$\frac{\text{PolyLog}\left[2, \frac{(1-ac)(e+dx^{-m})}{e}\right]}{dm}$$

Result (type 8, 40 leaves):

$$\int \frac{\text{Log}\left[c \left(a - \frac{(d-acd)x^{-m}}{ce}\right)\right]}{x(d+ex^m)} dx$$

Problem 336: Unable to integrate problem.

$$\int \frac{\text{Log}\left[\frac{x^{-m}(-d+acd+acex^m)}{e}\right]}{x(d+ex^m)} dx$$

Optimal (type 4, 28 leaves, 5 steps):

$$\frac{\text{PolyLog}\left[2, \frac{(1-ac)(e+dx^{-m})}{e}\right]}{dm}$$

Result (type 8, 40 leaves):

$$\int \frac{\text{Log}\left[\frac{x^{-m}(-d+acd+acex^m)}{e}\right]}{x(d+ex^m)} dx$$

Problem 337: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{2a}{a+bx}\right]}{a^2 - b^2 x^2} dx$$

Optimal (type 4, 24 leaves, 2 steps):

$$\frac{\text{PolyLog}\left[2, 1 - \frac{2a}{a+bx}\right]}{2ab}$$

Result (type 4, 89 leaves):

$$\frac{1}{4 a b} \left(4 \operatorname{ArcTanh} \left[\frac{b x}{a} \right] \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{2 a}{a + b x} \right] \right) - \operatorname{Log} \left[\frac{a}{b} + x \right] \left(\operatorname{Log} [4] + \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[1 - \frac{b x}{a} \right] \right) + 2 \operatorname{PolyLog} \left[2, \frac{a + b x}{2 a} \right] \right)$$

Problem 338: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log} \left[\frac{2 a}{a + b x} \right]}{(a - b x)(a + b x)} dx$$

Optimal (type 4, 24 leaves, 4 steps):

$$\frac{\operatorname{PolyLog} \left[2, 1 - \frac{2 a}{a + b x} \right]}{2 a b}$$

Result (type 4, 89 leaves):

$$\frac{1}{4 a b} \left(4 \operatorname{ArcTanh} \left[\frac{b x}{a} \right] \left(\operatorname{Log} \left[\frac{a}{b} + x \right] + \operatorname{Log} \left[\frac{2 a}{a + b x} \right] \right) - \operatorname{Log} \left[\frac{a}{b} + x \right] \left(\operatorname{Log} [4] + \operatorname{Log} \left[\frac{a}{b} + x \right] - 2 \operatorname{Log} \left[1 - \frac{b x}{a} \right] \right) + 2 \operatorname{PolyLog} \left[2, \frac{a + b x}{2 a} \right] \right)$$

Problem 339: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log} \left[\frac{a(1-c) + b(1+c)x}{a + b x} \right]}{a^2 - b^2 x^2} dx$$

Optimal (type 4, 37 leaves, 1 step):

$$\frac{\operatorname{PolyLog} \left[2, 1 - \frac{a(1-c) + b(1+c)x}{a + b x} \right]}{2 a b}$$

Result (type 4, 259 leaves):

$$\begin{aligned} & \frac{1}{4 a b} \left(4 \operatorname{ArcTanh} \left[\frac{b x}{a} \right] \operatorname{Log} \left[\frac{a}{b} + x \right] - \operatorname{Log} \left[\frac{a}{b} + x \right]^2 - 4 \operatorname{ArcTanh} \left[\frac{b x}{a} \right] \operatorname{Log} \left[\frac{a - a c}{b + b c} + x \right] + 2 \operatorname{Log} \left[\frac{a}{b} + x \right] \operatorname{Log} \left[\frac{a - b x}{2 a} \right] - \right. \\ & \left. 2 \operatorname{Log} \left[\frac{a - a c}{b + b c} + x \right] \operatorname{Log} \left[\frac{(1+c)(a - b x)}{2 a} \right] + 2 \operatorname{Log} \left[\frac{a - a c}{b + b c} + x \right] \operatorname{Log} \left[\frac{(1+c)(a + b x)}{2 a c} \right] + 4 \operatorname{ArcTanh} \left[\frac{b x}{a} \right] \operatorname{Log} \left[\frac{a - a c + b(1+c)x}{a + b x} \right] + \right. \\ & \left. 2 \operatorname{PolyLog} \left[2, \frac{a + b x}{2 a} \right] - 2 \operatorname{PolyLog} \left[2, \frac{a - a c + b(1+c)x}{2 a} \right] + 2 \operatorname{PolyLog} \left[2, -\frac{a - a c + b(1+c)x}{2 a c} \right] \right) \end{aligned}$$

Problem 340: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{a(1-c)+b(1+c)x}{a+bx}\right]}{(a-bx)(a+bx)} dx$$

Optimal (type 4, 27 leaves, 2 steps):

$$\frac{\text{PolyLog}\left[2, \frac{c(a-bx)}{a+bx}\right]}{2ab}$$

Result (type 4, 259 leaves):

$$\begin{aligned} & \frac{1}{4ab} \left(4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{a}{b} + x\right]^2 - 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac}{b+bc} + x\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{a-bx}{2a}\right] - \right. \\ & \left. 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a-bx)}{2a}\right] + 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a+bx)}{2ac}\right] + 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac+b(1+c)x}{a+bx}\right] + \right. \\ & \left. 2 \text{PolyLog}\left[2, \frac{a+bx}{2a}\right] - 2 \text{PolyLog}\left[2, \frac{a-ac+b(1+c)x}{2a}\right] + 2 \text{PolyLog}\left[2, -\frac{a-ac+b(1+c)x}{2ac}\right] \right) \end{aligned}$$

Problem 341: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[1 - \frac{c(a-bx)}{a+bx}\right]}{a^2 - b^2x^2} dx$$

Optimal (type 4, 27 leaves, 1 step):

$$\frac{\text{PolyLog}\left[2, \frac{c(a-bx)}{a+bx}\right]}{2ab}$$

Result (type 4, 259 leaves):

$$\begin{aligned} & \frac{1}{4ab} \left(4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{a}{b} + x\right]^2 - 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac}{b+bc} + x\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{a-bx}{2a}\right] - \right. \\ & \left. 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a-bx)}{2a}\right] + 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a+bx)}{2ac}\right] + 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac+b(1+c)x}{a+bx}\right] + \right. \\ & \left. 2 \text{PolyLog}\left[2, \frac{a+bx}{2a}\right] - 2 \text{PolyLog}\left[2, \frac{a-ac+b(1+c)x}{2a}\right] + 2 \text{PolyLog}\left[2, -\frac{a-ac+b(1+c)x}{2ac}\right] \right) \end{aligned}$$

Problem 342: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[1 - \frac{c(a-bx)}{a+bx}\right]}{(a-bx)(a+bx)} dx$$

Optimal (type 4, 27 leaves, 3 steps):

$$\frac{\text{PolyLog}\left[2, \frac{c(a-bx)}{a+bx}\right]}{2ab}$$

Result (type 4, 259 leaves):

$$\begin{aligned} & \frac{1}{4ab} \left(4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{a}{b} + x\right]^2 - 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac}{b+bc} + x\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{a-bx}{2a}\right] - \right. \\ & \left. 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a-bx)}{2a}\right] + 2 \text{Log}\left[\frac{a-ac}{b+bc} + x\right] \text{Log}\left[\frac{(1+c)(a+bx)}{2ac}\right] + 4 \text{ArcTanh}\left[\frac{bx}{a}\right] \text{Log}\left[\frac{a-ac+b(1+c)x}{a+bx}\right] + \right. \\ & \left. 2 \text{PolyLog}\left[2, \frac{a+bx}{2a}\right] - 2 \text{PolyLog}\left[2, \frac{a-ac+b(1+c)x}{2a}\right] + 2 \text{PolyLog}\left[2, -\frac{a-ac+b(1+c)x}{2ac}\right] \right) \end{aligned}$$

Problem 343: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[c(a+bx)^n]^3}{dx+ex^2} dx$$

Optimal (type 4, 238 leaves, 13 steps):

$$\begin{aligned} & \frac{\text{Log}\left[-\frac{bx}{a}\right] \text{Log}[c(a+bx)^n]^3}{d} - \frac{\text{Log}[c(a+bx)^n]^3 \text{Log}\left[\frac{b(d+ex)}{bd-ae}\right]}{d} - \frac{3n \text{Log}[c(a+bx)^n]^2 \text{PolyLog}\left[2, -\frac{e(a+bx)}{bd-ae}\right]}{d} + \\ & \frac{3n \text{Log}[c(a+bx)^n]^2 \text{PolyLog}\left[2, 1 + \frac{bx}{a}\right]}{d} + \frac{6n^2 \text{Log}[c(a+bx)^n] \text{PolyLog}\left[3, -\frac{e(a+bx)}{bd-ae}\right]}{d} - \\ & \frac{6n^2 \text{Log}[c(a+bx)^n] \text{PolyLog}\left[3, 1 + \frac{bx}{a}\right]}{d} - \frac{6n^3 \text{PolyLog}\left[4, -\frac{e(a+bx)}{bd-ae}\right]}{d} + \frac{6n^3 \text{PolyLog}\left[4, 1 + \frac{bx}{a}\right]}{d} \end{aligned}$$

Result (type 4, 494 leaves):

$$\frac{1}{d} \left(-\text{Log}[x] \left(n \text{Log}[a + b x] - \text{Log}[c (a + b x)^n] \right)^3 + \left(n \text{Log}[a + b x] - \text{Log}[c (a + b x)^n] \right)^3 \text{Log}[d + e x] + 3 n \left(-n \text{Log}[a + b x] + \text{Log}[c (a + b x)^n] \right)^2 \right. \\ \left. \left(\text{Log}[x] \left(\text{Log}[a + b x] - \text{Log}\left[1 + \frac{b x}{a}\right] \right) - \text{Log}[a + b x] \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - \text{PolyLog}\left[2, -\frac{b x}{a}\right] - \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] \right) - \right. \\ \left. 3 n^2 \left(n \text{Log}[a + b x] - \text{Log}[c (a + b x)^n] \right) \left(\text{Log}\left[-\frac{b x}{a}\right] \text{Log}[a + b x]^2 - \text{Log}[a + b x]^2 \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - \right. \right. \\ \left. \left. 2 \text{Log}[a + b x] \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] + 2 \text{Log}[a + b x] \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 2 \text{PolyLog}\left[3, \frac{e (a + b x)}{-b d + a e}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] \right) + \right. \\ \left. n^3 \left(\text{Log}\left[-\frac{b x}{a}\right] \text{Log}[a + b x]^3 - \text{Log}[a + b x]^3 \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - 3 \text{Log}[a + b x]^2 \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] + 3 \text{Log}[a + b x]^2 \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + \right. \right. \\ \left. \left. 6 \text{Log}[a + b x] \text{PolyLog}\left[3, \frac{e (a + b x)}{-b d + a e}\right] - 6 \text{Log}[a + b x] \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] - 6 \text{PolyLog}\left[4, \frac{e (a + b x)}{-b d + a e}\right] + 6 \text{PolyLog}\left[4, 1 + \frac{b x}{a}\right] \right) \right)$$

Problem 369: Result more than twice size of optimal antiderivative.

$$\int \text{Log}[f x^m] (a + b \text{Log}[c (d + e x)^n])^2 dx$$

Optimal (type 4, 309 leaves, 17 steps):

$$2 a b m n x - 4 b^2 m n^2 x + 2 b m n (a - b n) x - 2 a b n x \text{Log}[f x^m] + 2 b^2 n^2 x \text{Log}[f x^m] + \\ \frac{4 b^2 m n (d + e x) \text{Log}[c (d + e x)^n]}{e} + \frac{2 b^2 d m n \text{Log}\left[-\frac{e x}{d}\right] \text{Log}[c (d + e x)^n]}{e} - \frac{2 b^2 n (d + e x) \text{Log}[f x^m] \text{Log}[c (d + e x)^n]}{e} - \\ \frac{m (d + e x) (a + b \text{Log}[c (d + e x)^n])^2}{e} - \frac{d m \text{Log}\left[-\frac{e x}{d}\right] (a + b \text{Log}[c (d + e x)^n])^2}{e} + \frac{(d + e x) \text{Log}[f x^m] (a + b \text{Log}[c (d + e x)^n])^2}{e} + \\ \frac{2 b^2 d m n^2 \text{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e} - \frac{2 b d m n (a + b \text{Log}[c (d + e x)^n]) \text{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e} + \frac{2 b^2 d m n^2 \text{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{e}$$

Result (type 4, 655 leaves):

$$\begin{aligned}
& b^2 n^2 \left(-m \operatorname{Log}[x] + \operatorname{Log}[f x^m] \right) \left(x \operatorname{Log}[d + e x]^2 - 2 e \left(-\frac{x}{e} + \frac{d \operatorname{Log}[d + e x]}{e^2} + \frac{x \operatorname{Log}[d + e x]}{e} - \frac{d \operatorname{Log}[d + e x]^2}{2 e^2} \right) \right) + \\
& 2 b n \left(-m \operatorname{Log}[x] + \operatorname{Log}[f x^m] \right) \left(x \operatorname{Log}[d + e x] - e \left(\frac{x}{e} - \frac{d \operatorname{Log}[d + e x]}{e^2} \right) \right) \left(a + b \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right) \right) + \\
& m x \operatorname{Log}[x] \left(a + b \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right) \right)^2 + x \left(-a^2 m + a^2 \left(-m \operatorname{Log}[x] + \operatorname{Log}[f x^m] \right) - 2 a b m \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right) + \right. \\
& \quad \left. 2 a b \left(-m \operatorname{Log}[x] + \operatorname{Log}[f x^m] \right) \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right) - b^2 m \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right)^2 + \right. \\
& \quad \left. b^2 \left(-m \operatorname{Log}[x] + \operatorname{Log}[f x^m] \right) \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right)^2 \right) + 2 b m n \left(a + b \left(-n \operatorname{Log}[d + e x] + \operatorname{Log}[c (d + e x)^n] \right) \right) \\
& \left(x \operatorname{Log}[x] \operatorname{Log}[d + e x] - \frac{-d - e x + (d + e x) \operatorname{Log}[d + e x]}{e} - e \left(\frac{x (-1 + \operatorname{Log}[x])}{e} - \frac{d \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e x}{d}\right] + \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]\right)}{e^2} \right) \right) \Bigg) + \\
& b^2 m n^2 \left(-x \operatorname{Log}[d + e x]^2 + x \operatorname{Log}[x] \operatorname{Log}[d + e x]^2 + 2 e \left(-\frac{x}{e} + \frac{d \operatorname{Log}[d + e x]}{e^2} + \frac{x \operatorname{Log}[d + e x]}{e} - \frac{d \operatorname{Log}[d + e x]^2}{2 e^2} \right) - \right. \\
& \quad \left. 2 e \left(\frac{x - \frac{d \operatorname{Log}[d + e x]}{e} + x (-1 + \operatorname{Log}[x]) \operatorname{Log}[d + e x] - e \left(\frac{x (-1 + \operatorname{Log}[x])}{e} - \frac{d \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e x}{d}\right] + \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right]\right)}{e^2} \right)}{e} \right) - \right. \\
& \quad \left. \left. \frac{d \left(\frac{1}{2} \left(\operatorname{Log}[x] - \operatorname{Log}\left[-\frac{e x}{d}\right]\right) \operatorname{Log}[d + e x]^2 - \operatorname{Log}[d + e x] \operatorname{PolyLog}\left[2, \frac{d + e x}{d}\right] + \operatorname{PolyLog}\left[3, \frac{d + e x}{d}\right]\right)}{e^2} \right) \right) \Bigg)
\end{aligned}$$

Problem 373: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Log}[f x^m] \left(a + b \operatorname{Log}[c (d + e x)^n] \right)^3 dx$$

Optimal (type 4, 522 leaves, 28 steps):

$$\begin{aligned}
& -12 a b^2 m n^2 x + 18 b^3 m n^3 x - 6 b^2 m n^2 (a - b n) x + 6 a b^2 n^2 x \operatorname{Log}[f x^m] - 6 b^3 n^3 x \operatorname{Log}[f x^m] - \frac{18 b^3 m n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} - \\
& \frac{6 b^3 d m n^2 \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[c (d + e x)^n]}{e} + \frac{6 b^3 n^2 (d + e x) \operatorname{Log}[f x^m] \operatorname{Log}[c (d + e x)^n]}{e} + \frac{6 b m n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} + \\
& \frac{3 b d m n \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} - \frac{3 b n (d + e x) \operatorname{Log}[f x^m] (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} - \frac{m (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e} - \\
& \frac{d m \operatorname{Log}\left[-\frac{e x}{d}\right] (a + b \operatorname{Log}[c (d + e x)^n])^3}{e} + \frac{(d + e x) \operatorname{Log}[f x^m] (a + b \operatorname{Log}[c (d + e x)^n])^3}{e} - \frac{6 b^3 d m n^3 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e} + \\
& \frac{6 b^2 d m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e} - \frac{3 b d m n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e} - \\
& \frac{6 b^3 d m n^3 \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{e} + \frac{6 b^2 d m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, 1 + \frac{e x}{d}\right]}{e} - \frac{6 b^3 d m n^3 \operatorname{PolyLog}\left[4, 1 + \frac{e x}{d}\right]}{e}
\end{aligned}$$

Result (type 4, 1163 leaves):

$$\begin{aligned}
& \frac{1}{e} \left(-b^3 n^3 (d + ex) (m \operatorname{Log}[x] - \operatorname{Log}[fx^m]) (-6 + 6 \operatorname{Log}[d + ex] - 3 \operatorname{Log}[d + ex]^2 + \operatorname{Log}[d + ex]^3) - \right. \\
& 3 b^2 n^2 (m \operatorname{Log}[x] - \operatorname{Log}[fx^m]) (2 ex - 2 (d + ex) \operatorname{Log}[d + ex] + (d + ex) \operatorname{Log}[d + ex]^2) (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n]) - \\
& 3 b e n x (m - \operatorname{Log}[fx^m]) \operatorname{Log}[d + ex] (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 - \\
& 3 b d n (m + m \operatorname{Log}[x] - \operatorname{Log}[fx^m]) \operatorname{Log}[d + ex] (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 + ex (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \\
& (3 b m n + 3 b n (m \operatorname{Log}[x] - \operatorname{Log}[fx^m]) + a (-m \operatorname{Log}[x] + \operatorname{Log}[fx^m]) + b (-m \operatorname{Log}[x] + \operatorname{Log}[fx^m]) (-n \operatorname{Log}[d + ex] + \operatorname{Log}[c (d + ex)^n])) + \\
& a d m (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] \right) - \\
& b d m (n \operatorname{Log}[d + ex] - \operatorname{Log}[c (d + ex)^n]) (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \left(\operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] \right) - \\
& a m (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \left(ex + \operatorname{Log}[x] \left(-ex + d \operatorname{Log}\left[1 + \frac{ex}{d}\right] \right) + d \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] \right) + \\
& 3 b m n (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \left(ex + \operatorname{Log}[x] \left(-ex + d \operatorname{Log}\left[1 + \frac{ex}{d}\right] \right) + d \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] \right) + \\
& b m (n \operatorname{Log}[d + ex] - \operatorname{Log}[c (d + ex)^n]) (a - b n \operatorname{Log}[d + ex] + b \operatorname{Log}[c (d + ex)^n])^2 \left(ex + \operatorname{Log}[x] \left(-ex + d \operatorname{Log}\left[1 + \frac{ex}{d}\right] \right) + d \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] \right) - \\
& 3 b^2 m n^2 (-a + b n \operatorname{Log}[d + ex] - b \operatorname{Log}[c (d + ex)^n]) \left(-6 ex + 2 ex \operatorname{Log}[x] + 4 d \operatorname{Log}[d + ex] + 4 ex \operatorname{Log}[d + ex] - 2 ex \operatorname{Log}[x] \operatorname{Log}[d + ex] - \right. \\
& d \operatorname{Log}[d + ex]^2 - ex \operatorname{Log}[d + ex]^2 + d \operatorname{Log}[x] \operatorname{Log}[d + ex]^2 + ex \operatorname{Log}[x] \operatorname{Log}[d + ex]^2 - d \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d + ex]^2 - \\
& 2 d \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] - 2 d \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] - 2 d \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right] + 2 d \operatorname{PolyLog}\left[3, 1 + \frac{ex}{d}\right] \left. \right) + \\
& b^3 m n^3 \left(6 d + 24 ex - 6 ex \operatorname{Log}[x] - 18 d \operatorname{Log}[d + ex] - 18 ex \operatorname{Log}[d + ex] + 6 ex \operatorname{Log}[x] \operatorname{Log}[d + ex] + 6 d \operatorname{Log}[d + ex]^2 + 6 ex \operatorname{Log}[d + ex]^2 - \right. \\
& 3 d \operatorname{Log}[x] \operatorname{Log}[d + ex]^2 - 3 ex \operatorname{Log}[x] \operatorname{Log}[d + ex]^2 + 3 d \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d + ex]^2 - d \operatorname{Log}[d + ex]^3 - ex \operatorname{Log}[d + ex]^3 + d \operatorname{Log}[x] \operatorname{Log}[d + ex]^3 + \\
& ex \operatorname{Log}[x] \operatorname{Log}[d + ex]^3 - d \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d + ex]^3 + 6 d \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + 6 d \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] - 3 d (-2 + \operatorname{Log}[d + ex]) \\
& \left. \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right] - 6 d \operatorname{PolyLog}\left[3, 1 + \frac{ex}{d}\right] + 6 d \operatorname{Log}[d + ex] \operatorname{PolyLog}\left[3, 1 + \frac{ex}{d}\right] - 6 d \operatorname{PolyLog}\left[4, 1 + \frac{ex}{d}\right] \right) \left. \right)
\end{aligned}$$

Problem 394: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c (d + ex)^n])^2 (f + g \operatorname{Log}[h (i + jx)^m]) dx$$

Optimal (type 4, 649 leaves, 41 steps):

$$\begin{aligned}
& -2 a b f n x + 4 a b g m n x + 2 b^2 f n^2 x - 6 b^2 g m n^2 x - \frac{2 b^2 f n (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} + \frac{4 b^2 g m n (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} + \\
& \frac{d f (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} - \frac{g m (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} - \frac{2 b g i m n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right]}{j} - \\
& \frac{d g m (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right]}{e} + \frac{g i m (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right]}{j} + \frac{2 b^2 g n^2 (i + j x) \operatorname{Log}[h (i + j x)^m]}{j} - \\
& \frac{2 b^2 d g n^2 \operatorname{Log}\left[-\frac{j (d + e x)}{e i - d j}\right] \operatorname{Log}[h (i + j x)^m]}{e} - 2 b g n x (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[h (i + j x)^m] + \\
& \frac{d g (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[h (i + j x)^m]}{e} + x (a + b \operatorname{Log}[c (d + e x)^n])^2 (f + g \operatorname{Log}[h (i + j x)^m]) - \frac{2 b^2 g i m n^2 \operatorname{PolyLog}\left[2, -\frac{j (d + e x)}{e i - d j}\right]}{j} - \\
& \frac{2 b d g m n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j (d + e x)}{e i - d j}\right]}{e} + \frac{2 b g i m n (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j (d + e x)}{e i - d j}\right]}{j} - \\
& \frac{2 b^2 d g m n^2 \operatorname{PolyLog}\left[2, \frac{e (i + j x)}{e i - d j}\right]}{e} + \frac{2 b^2 d g m n^2 \operatorname{PolyLog}\left[3, -\frac{j (d + e x)}{e i - d j}\right]}{e} - \frac{2 b^2 g i m n^2 \operatorname{PolyLog}\left[3, -\frac{j (d + e x)}{e i - d j}\right]}{j}
\end{aligned}$$

Result (type 4, 1405 leaves):

$$\frac{1}{e^j} \left(-2 a b d f j n + 2 a b d g j m n + 2 b^2 d f j n^2 - 4 b^2 d g j m n^2 + a^2 e f j x - a^2 e g j m x - 2 a b e f j n x + 4 a b e g j m n x + 2 b^2 e f j n^2 x - \right. \\
6 b^2 e g j m n^2 x + 2 a b d f j n \operatorname{Log}[d + e x] - 2 a b d g j m n \operatorname{Log}[d + e x] + 2 b^2 d g j m n^2 \operatorname{Log}[d + e x] - b^2 d f j n^2 \operatorname{Log}[d + e x]^2 + \\
b^2 d g j m n^2 \operatorname{Log}[d + e x]^2 - 2 b^2 d f j n \operatorname{Log}[c (d + e x)^n] + 2 b^2 d g j m n \operatorname{Log}[c (d + e x)^n] + 2 a b e f j x \operatorname{Log}[c (d + e x)^n] - \\
2 a b e g j m x \operatorname{Log}[c (d + e x)^n] - 2 b^2 e f j n x \operatorname{Log}[c (d + e x)^n] + 4 b^2 e g j m n x \operatorname{Log}[c (d + e x)^n] + 2 b^2 d f j n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] - \\
2 b^2 d g j m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] + b^2 e f j x \operatorname{Log}[c (d + e x)^n]^2 - b^2 e g j m x \operatorname{Log}[c (d + e x)^n]^2 + a^2 e g i m \operatorname{Log}[i + j x] - \\
2 a b e g i m n \operatorname{Log}[i + j x] + 2 a b d g j m n \operatorname{Log}[i + j x] + 2 b^2 e g i m n^2 \operatorname{Log}[i + j x] - 2 b^2 d g j m n^2 \operatorname{Log}[i + j x] - \\
2 a b e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + 2 b^2 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - 2 b^2 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + \\
b^2 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] + 2 a b e g i m \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 2 b^2 e g i m n \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] + \\
2 b^2 d g j m n \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 2 b^2 e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] + b^2 e g i m \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[i + j x] + \\
2 a b e g i m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] - 2 a b d g j m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] - 2 b^2 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] + \\
2 b^2 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] - b^2 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] + b^2 d g j m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] + \\
2 b^2 e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] - 2 b^2 d g j m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] - \\
2 a b d g j n \operatorname{Log}[h (i + j x)^m] + 2 b^2 d g j n^2 \operatorname{Log}[h (i + j x)^m] + a^2 e g j x \operatorname{Log}[h (i + j x)^m] - 2 a b e g j n x \operatorname{Log}[h (i + j x)^m] + \\
2 b^2 e g j n^2 x \operatorname{Log}[h (i + j x)^m] + 2 a b d g j n \operatorname{Log}[d + e x] \operatorname{Log}[h (i + j x)^m] - b^2 d g j n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[h (i + j x)^m] - \\
2 b^2 d g j n \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[h (i + j x)^m] + 2 a b e g j x \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[h (i + j x)^m] - 2 b^2 e g j n x \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[h (i + j x)^m] + \\
2 b^2 d g j n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[h (i + j x)^m] + b^2 e g j x \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[h (i + j x)^m] + \\
2 b g (e i - d j) m n (a - b n + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, \frac{j (d + e x)}{-e i + d j}\right] + 2 b^2 g (-e i + d j) m n^2 \operatorname{PolyLog}\left[3, \frac{j (d + e x)}{-e i + d j}\right] \Big)$$

Problem 397: Result more than twice size of optimal antiderivative.

$$\int x (a + b \operatorname{Log}[c (d + e x)^n])^3 (f + g \operatorname{Log}[h (i + j x)^m]) dx$$

Optimal (type 4, 2050 leaves, 148 steps):

$$-\frac{6 a b^2 d f n^2 x}{e} + \frac{12 a b^2 d g m n^2 x}{e} + \frac{21 a b^2 g i m n^2 x}{4 j} + \frac{6 b^3 d f n^3 x}{e} - \frac{141 b^3 d g m n^3 x}{8 e} - \frac{45 b^3 g i m n^3 x}{8 j} + \\
\frac{3}{8} b^3 g m n^3 x^2 - \frac{3 b^3 f n^3 (d + e x)^2}{8 e^2} + \frac{3 b^3 g m n^3 (d + e x)^2}{8 e^2} + \frac{3 b^3 d^2 g m n^3 \operatorname{Log}[d + e x]}{8 e^2} - \frac{6 b^3 d f n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e^2} + \\
\frac{12 b^3 d g m n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e^2} + \frac{21 b^3 g i m n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{4 e j} - \frac{3}{8} b^2 g m n^2 x^2 (a + b \operatorname{Log}[c (d + e x)^n]) + \\
\frac{3 b^2 f n^2 (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{4 e^2} - \frac{3 b^2 g m n^2 (d + e x)^2 (a + b \operatorname{Log}[c (d + e x)^n])}{4 e^2} + \frac{3 b d f n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e^2}$$

$$\begin{aligned}
& \frac{15 b d g m n (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^2}{4 e^2} - \frac{9 b g i m n (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^2}{4 e j} - \frac{3 b f n (d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{4 e^2} + \\
& \frac{3 b g m n (d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])^2}{4 e^2} - \frac{d^2 f (a+b \operatorname{Log}[c (d+e x)^n])^3}{2 e^2} + \frac{d g m (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^3}{2 e^2} + \\
& \frac{g i m (d+e x) (a+b \operatorname{Log}[c (d+e x)^n])^3}{2 e j} - \frac{g m (d+e x)^2 (a+b \operatorname{Log}[c (d+e x)^n])^3}{4 e^2} + \frac{3 b^3 g i^2 m n^3 \operatorname{Log}[i+j x]}{8 j^2} - \\
& \frac{3 b^2 g i^2 m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{4 j^2} - \frac{9 b^2 d g i m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{2 e j} - \\
& \frac{9 b d^2 g m n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{4 e^2} + \frac{3 b g i^2 m n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{4 j^2} + \\
& \frac{3 b d g i m n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{2 e j} + \frac{d^2 g m (a+b \operatorname{Log}[c (d+e x)^n])^3 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{2 e^2} - \frac{g i^2 m (a+b \operatorname{Log}[c (d+e x)^n])^3 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]}{2 j^2} - \\
& \frac{3}{8} b^3 g n^3 x^2 \operatorname{Log}[h(i+j x)^m] + \frac{21 b^3 d g n^3 (i+j x) \operatorname{Log}[h(i+j x)^m]}{4 e j} - \frac{21 b^3 d^2 g n^3 \operatorname{Log}\left[-\frac{j(d+e x)}{e i-d j}\right] \operatorname{Log}[h(i+j x)^m]}{4 e^2} - \\
& \frac{9 b^2 d g n^2 x (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}[h(i+j x)^m]}{2 e} + \frac{3}{4} b^2 g n^2 x^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{Log}[h(i+j x)^m] + \\
& \frac{9 b d^2 g n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}[h(i+j x)^m]}{4 e^2} + \frac{3 b d g n x (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}[h(i+j x)^m]}{2 e} - \\
& \frac{3}{4} b g n x^2 (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{Log}[h(i+j x)^m] - \frac{d^2 g (a+b \operatorname{Log}[c (d+e x)^n])^3 \operatorname{Log}[h(i+j x)^m]}{2 e^2} + \\
& \frac{1}{2} x^2 (a+b \operatorname{Log}[c (d+e x)^n])^3 (f+g \operatorname{Log}[h(i+j x)^m]) - \frac{3 b^3 g i^2 m n^3 \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{4 j^2} - \frac{9 b^3 d g i m n^3 \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{2 e j} - \\
& \frac{9 b^2 d^2 g m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{2 e^2} + \frac{3 b^2 g i^2 m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{2 j^2} + \\
& \frac{3 b^2 d g i m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{e j} + \frac{3 b d^2 g m n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{2 e^2} - \\
& \frac{3 b g i^2 m n (a+b \operatorname{Log}[c (d+e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{j(d+e x)}{e i-d j}\right]}{2 j^2} - \frac{21 b^3 d^2 g m n^3 \operatorname{PolyLog}\left[2, \frac{e(i+j x)}{e i-d j}\right]}{4 e^2} + \frac{9 b^3 d^2 g m n^3 \operatorname{PolyLog}\left[3, -\frac{j(d+e x)}{e i-d j}\right]}{2 e^2} - \\
& \frac{3 b^3 g i^2 m n^3 \operatorname{PolyLog}\left[3, -\frac{j(d+e x)}{e i-d j}\right]}{2 j^2} - \frac{3 b^3 d g i m n^3 \operatorname{PolyLog}\left[3, -\frac{j(d+e x)}{e i-d j}\right]}{e j} - \frac{3 b^2 d^2 g m n^2 (a+b \operatorname{Log}[c (d+e x)^n]) \operatorname{PolyLog}\left[3, -\frac{j(d+e x)}{e i-d j}\right]}{e^2} +
\end{aligned}$$

$$\frac{3 b^2 g i^2 m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}[3, -\frac{j(d+e x)}{e i-d j}]}{j^2} + \frac{3 b^3 d^2 g m n^3 \operatorname{PolyLog}[4, -\frac{j(d+e x)}{e i-d j}]}{e^2} - \frac{3 b^3 g i^2 m n^3 \operatorname{PolyLog}[4, -\frac{j(d+e x)}{e i-d j}]}{j^2}$$

Result (type 4, 4971 leaves):

$$\frac{1}{8 e^2 j^2} \left(-12 a^2 b d e g i j m n + 36 a b^2 d e g i j m n^2 + 24 a b^2 d^2 g j^2 m n^2 - 42 b^3 d e g i j m n^3 - 60 b^3 d^2 g j^2 m n^3 + 4 a^3 e^2 g i j m x + 12 a^2 b d e f j^2 n x - \right. \\
18 a^2 b e^2 g i j m n x - 18 a^2 b d e g j^2 m n x - 36 a b^2 d e f j^2 n^2 x + 42 a b^2 e^2 g i j m n^2 x + 84 a b^2 d e g j^2 m n^2 x + 42 b^3 d e f j^2 n^3 x - \\
45 b^3 e^2 g i j m n^3 x - 135 b^3 d e g j^2 m n^3 x + 4 a^3 e^2 f j^2 x^2 - 2 a^3 e^2 g j^2 m x^2 - 6 a^2 b e^2 f j^2 n x^2 + 6 a^2 b e^2 g j^2 m n x^2 + 6 a b^2 e^2 f j^2 n^2 x^2 - \\
9 a b^2 e^2 g j^2 m n^2 x^2 - 3 b^3 e^2 f j^2 n^3 x^2 + 6 b^3 e^2 g j^2 m n^3 x^2 - 12 a^2 b d^2 f j^2 n \operatorname{Log}[d + e x] + 12 a^2 b d e g i j m n \operatorname{Log}[d + e x] + \\
6 a^2 b d^2 g j^2 m n \operatorname{Log}[d + e x] + 36 a b^2 d^2 f j^2 n^2 \operatorname{Log}[d + e x] - 12 a b^2 d e g i j m n^2 \operatorname{Log}[d + e x] - 48 a b^2 d^2 g j^2 m n^2 \operatorname{Log}[d + e x] - \\
42 b^3 d^2 f j^2 n^3 \operatorname{Log}[d + e x] + 6 b^3 d e g i j m n^3 \operatorname{Log}[d + e x] + 69 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d + e x] + 12 a b^2 d^2 f j^2 n^2 \operatorname{Log}[d + e x]^2 - \\
12 a b^2 d e g i j m n^2 \operatorname{Log}[d + e x]^2 - 6 a b^2 d^2 g j^2 m n^2 \operatorname{Log}[d + e x]^2 - 18 b^3 d^2 f j^2 n^3 \operatorname{Log}[d + e x]^2 + 6 b^3 d e g i j m n^3 \operatorname{Log}[d + e x]^2 + \\
24 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d + e x]^2 - 4 b^3 d^2 f j^2 n^3 \operatorname{Log}[d + e x]^3 + 4 b^3 d e g i j m n^3 \operatorname{Log}[d + e x]^3 + 2 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d + e x]^3 - \\
24 a b^2 d e g i j m n \operatorname{Log}[c (d + e x)^n] + 36 b^3 d e g i j m n^2 \operatorname{Log}[c (d + e x)^n] + 24 b^3 d^2 g j^2 m n^2 \operatorname{Log}[c (d + e x)^n] + 12 a^2 b e^2 g i j m x \operatorname{Log}[c (d + e x)^n] + \\
24 a b^2 d e f j^2 n x \operatorname{Log}[c (d + e x)^n] - 36 a b^2 e^2 g i j m n x \operatorname{Log}[c (d + e x)^n] - 36 a b^2 d e g j^2 m n x \operatorname{Log}[c (d + e x)^n] - \\
36 b^3 d e f j^2 n^2 x \operatorname{Log}[c (d + e x)^n] + 42 b^3 e^2 g i j m n^2 x \operatorname{Log}[c (d + e x)^n] + 84 b^3 d e g j^2 m n^2 x \operatorname{Log}[c (d + e x)^n] + \\
12 a^2 b e^2 f j^2 x^2 \operatorname{Log}[c (d + e x)^n] - 6 a^2 b e^2 g j^2 m x^2 \operatorname{Log}[c (d + e x)^n] - 12 a b^2 e^2 f j^2 n x^2 \operatorname{Log}[c (d + e x)^n] + 12 a b^2 e^2 g j^2 m n x^2 \operatorname{Log}[c (d + e x)^n] + \\
6 b^3 e^2 f j^2 n^2 x^2 \operatorname{Log}[c (d + e x)^n] - 9 b^3 e^2 g j^2 m n^2 x^2 \operatorname{Log}[c (d + e x)^n] - 24 a b^2 d^2 f j^2 n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] + \\
24 a b^2 d e g i j m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] + 12 a b^2 d^2 g j^2 m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] + 36 b^3 d^2 f j^2 n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] - \\
12 b^3 d e g i j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] - 48 b^3 d^2 g j^2 m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] + 12 b^3 d^2 f j^2 n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c (d + e x)^n] - \\
12 b^3 d e g i j m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c (d + e x)^n] - 6 b^3 d^2 g j^2 m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c (d + e x)^n] - 12 b^3 d e g i j m n \operatorname{Log}[c (d + e x)^n]^2 + \\
12 a b^2 e^2 g i j m x \operatorname{Log}[c (d + e x)^n]^2 + 12 b^3 d e f j^2 n x \operatorname{Log}[c (d + e x)^n]^2 - 18 b^3 e^2 g i j m n x \operatorname{Log}[c (d + e x)^n]^2 - \\
18 b^3 d e g j^2 m n x \operatorname{Log}[c (d + e x)^n]^2 + 12 a b^2 e^2 f j^2 x^2 \operatorname{Log}[c (d + e x)^n]^2 - 6 a b^2 e^2 g j^2 m x^2 \operatorname{Log}[c (d + e x)^n]^2 - \\
6 b^3 e^2 f j^2 n x^2 \operatorname{Log}[c (d + e x)^n]^2 + 6 b^3 e^2 g j^2 m n x^2 \operatorname{Log}[c (d + e x)^n]^2 - 12 b^3 d^2 f j^2 n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n]^2 + \\
12 b^3 d e g i j m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n]^2 + 6 b^3 d^2 g j^2 m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n]^2 + 4 b^3 e^2 g i j m x \operatorname{Log}[c (d + e x)^n]^3 + \\
4 b^3 e^2 f j^2 x^2 \operatorname{Log}[c (d + e x)^n]^3 - 2 b^3 e^2 g j^2 m x^2 \operatorname{Log}[c (d + e x)^n]^3 - 4 a^3 e^2 g i^2 m \operatorname{Log}[i + j x] + 6 a^2 b e^2 g i^2 m n \operatorname{Log}[i + j x] + \\
12 a^2 b d e g i j m n \operatorname{Log}[i + j x] - 6 a b^2 e^2 g i^2 m n^2 \operatorname{Log}[i + j x] - 36 a b^2 d e g i j m n^2 \operatorname{Log}[i + j x] + 3 b^3 e^2 g i^2 m n^3 \operatorname{Log}[i + j x] + \\
42 b^3 d e g i j m n^3 \operatorname{Log}[i + j x] + 12 a^2 b e^2 g i^2 m n \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - 12 a b^2 e^2 g i^2 m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - \\
24 a b^2 d e g i j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + 6 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + 36 b^3 d e g i j m n^3 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - \\
12 a b^2 e^2 g i^2 m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] + 6 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] + 12 b^3 d e g i j m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] + \\
4 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d + e x]^3 \operatorname{Log}[i + j x] - 12 a^2 b e^2 g i^2 m \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] + 12 a b^2 e^2 g i^2 m n \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] + \\
24 a b^2 d e g i j m n \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 6 b^3 e^2 g i^2 m n^2 \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 36 b^3 d e g i j m n^2 \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] + \\
24 a b^2 e^2 g i^2 m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 12 b^3 e^2 g i^2 m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - \\
24 b^3 d e g i j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - 12 b^3 e^2 g i^2 m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c (d + e x)^n] \operatorname{Log}[i + j x] - \\
12 a b^2 e^2 g i^2 m \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[i + j x] + 6 b^3 e^2 g i^2 m n \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[i + j x] + 12 b^3 d e g i j m n \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[i + j x] + \\
12 b^3 e^2 g i^2 m n \operatorname{Log}[d + e x] \operatorname{Log}[c (d + e x)^n]^2 \operatorname{Log}[i + j x] - 4 b^3 e^2 g i^2 m \operatorname{Log}[c (d + e x)^n]^3 \operatorname{Log}[i + j x] - \\
12 a^2 b e^2 g i^2 m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] + 12 a^2 b d^2 g j^2 m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] + 12 a b^2 e^2 g i^2 m n^2 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e (i + j x)}{e i - d j}\right] +$$

$$\begin{aligned}
& 24 a b^2 d e g i j m n^2 \operatorname{Log}[d+e x] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-36 a b^2 d^2 g j^2 m n^2 \operatorname{Log}[d+e x] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-6 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d+e x] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]- \\
& 36 b^3 d e g i j m n^3 \operatorname{Log}[d+e x] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+42 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d+e x] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+12 a b^2 e^2 g i^2 m n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]- \\
& 12 a b^2 d^2 g j^2 m n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-6 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d+e x]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]- \\
& 12 b^3 d e g i j m n^3 \operatorname{Log}[d+e x]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+18 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d+e x]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-4 b^3 e^2 g i^2 m n^3 \operatorname{Log}[d+e x]^3 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+ \\
& 4 b^3 d^2 g j^2 m n^3 \operatorname{Log}[d+e x]^3 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-24 a b^2 e^2 g i^2 m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+ \\
& 24 a b^2 d^2 g j^2 m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+12 b^3 e^2 g i^2 m n^2 \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+ \\
& 24 b^3 d e g i j m n^2 \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-36 b^3 d^2 g j^2 m n^2 \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+ \\
& 12 b^3 e^2 g i^2 m n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]-12 b^3 d^2 g j^2 m n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]- \\
& 12 b^3 e^2 g i^2 m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+12 b^3 d^2 g j^2 m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right]+ \\
& 12 a^2 b d e g j^2 n x \operatorname{Log}[h(i+j x)^m]-36 a b^2 d e g j^2 n^2 x \operatorname{Log}[h(i+j x)^m]+42 b^3 d e g j^2 n^3 x \operatorname{Log}[h(i+j x)^m]+ \\
& 4 a^3 e^2 g j^2 x^2 \operatorname{Log}[h(i+j x)^m]-6 a^2 b e^2 g j^2 n x^2 \operatorname{Log}[h(i+j x)^m]+6 a b^2 e^2 g j^2 n^2 x^2 \operatorname{Log}[h(i+j x)^m]-3 b^3 e^2 g j^2 n^3 x^2 \operatorname{Log}[h(i+j x)^m]- \\
& 12 a^2 b d^2 g j^2 n \operatorname{Log}[d+e x] \operatorname{Log}[h(i+j x)^m]+36 a b^2 d^2 g j^2 n^2 \operatorname{Log}[d+e x] \operatorname{Log}[h(i+j x)^m]-42 b^3 d^2 g j^2 n^3 \operatorname{Log}[d+e x] \operatorname{Log}[h(i+j x)^m]+ \\
& 12 a b^2 d^2 g j^2 n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[h(i+j x)^m]-18 b^3 d^2 g j^2 n^3 \operatorname{Log}[d+e x]^2 \operatorname{Log}[h(i+j x)^m]-4 b^3 d^2 g j^2 n^3 \operatorname{Log}[d+e x]^3 \operatorname{Log}[h(i+j x)^m]+ \\
& 24 a b^2 d e g j^2 n x \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]-36 b^3 d e g j^2 n^2 x \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]+ \\
& 12 a^2 b e^2 g j^2 x^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]-12 a b^2 e^2 g j^2 n x^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]+ \\
& 6 b^3 e^2 g j^2 n^2 x^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]-24 a b^2 d^2 g j^2 n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]+ \\
& 36 b^3 d^2 g j^2 n^2 \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]+12 b^3 d^2 g j^2 n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m]+ \\
& 12 b^3 d e g j^2 n x \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m]+12 a b^2 e^2 g j^2 x^2 \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m]- \\
& 6 b^3 e^2 g j^2 n x^2 \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m]-12 b^3 d^2 g j^2 n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m]+ \\
& 4 b^3 e^2 g j^2 x^2 \operatorname{Log}[c(d+e x)^n]^3 \operatorname{Log}[h(i+j x)^m]-6 b g(e i-d j) m n\left(2 a^2(e i+d j)-2 a b(e i+3 d j) n+b^2(e i+7 d j) n^2-\right. \\
& \left.2 b(-2 a(e i+d j)+b(e i+3 d j) n) \operatorname{Log}[c(d+e x)^n]+2 b^2(e i+d j) \operatorname{Log}[c(d+e x)^n]^2\right) \operatorname{PolyLog}\left[2, \frac{j(d+e x)}{-e i+d j}\right]+ \\
& 12 b^2 g(e i-d j) m n^2\left(2 a(e i+d j)-b(e i+3 d j) n+2 b(e i+d j) \operatorname{Log}[c(d+e x)^n]\right) \operatorname{PolyLog}\left[3, \frac{j(d+e x)}{-e i+d j}\right]- \\
& 24 b^3 e^2 g i^2 m n^3 \operatorname{PolyLog}\left[4, \frac{j(d+e x)}{-e i+d j}\right]+24 b^3 d^2 g j^2 m n^3 \operatorname{PolyLog}\left[4, \frac{j(d+e x)}{-e i+d j}\right]
\end{aligned}$$

Problem 398: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c (d + e x)^n])^3 (f + g \operatorname{Log}[h (i + j x)^m]) dx$$

Optimal (type 4, 1147 leaves, 64 steps):

$$\begin{aligned} & 6 a b^2 f n^2 x - 18 a b^2 g m n^2 x - 6 b^3 f n^3 x + 24 b^3 g m n^3 x + \frac{6 b^3 f n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} - \frac{18 b^3 g m n^2 (d + e x) \operatorname{Log}[c (d + e x)^n]}{e} - \\ & \frac{3 b f n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} + \frac{6 b g m n (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^2}{e} + \frac{d f (a + b \operatorname{Log}[c (d + e x)^n])^3}{e} - \\ & \frac{g m (d + e x) (a + b \operatorname{Log}[c (d + e x)^n])^3}{e} + \frac{6 b^2 g i m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}\left[\frac{e(i+jx)}{e^{i-dj}}\right]}{j} + \frac{3 b d g m n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(i+jx)}{e^{i-dj}}\right]}{e} - \\ & \frac{3 b g i m n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}\left[\frac{e(i+jx)}{e^{i-dj}}\right]}{j} - \frac{d g m (a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}\left[\frac{e(i+jx)}{e^{i-dj}}\right]}{e} + \frac{g i m (a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}\left[\frac{e(i+jx)}{e^{i-dj}}\right]}{j} - \\ & \frac{6 b^3 g n^3 (i + j x) \operatorname{Log}[h (i + j x)^m]}{j} + \frac{6 b^3 d g n^3 \operatorname{Log}\left[-\frac{j(d+ex)}{e^{i-dj}}\right] \operatorname{Log}[h (i + j x)^m]}{e} + 6 b^2 g n^2 x (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{Log}[h (i + j x)^m] - \\ & \frac{3 b d g n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[h (i + j x)^m]}{e} - 3 b g n x (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{Log}[h (i + j x)^m] + \\ & \frac{d g (a + b \operatorname{Log}[c (d + e x)^n])^3 \operatorname{Log}[h (i + j x)^m]}{e} + x (a + b \operatorname{Log}[c (d + e x)^n])^3 (f + g \operatorname{Log}[h (i + j x)^m]) + \\ & \frac{6 b^3 g i m n^3 \operatorname{PolyLog}\left[2, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} + \frac{6 b^2 d g m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j(d+ex)}{e^{i-dj}}\right]}{e} - \\ & \frac{6 b^2 g i m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[2, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} - \frac{3 b d g m n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{j(d+ex)}{e^{i-dj}}\right]}{e} + \\ & \frac{3 b g i m n (a + b \operatorname{Log}[c (d + e x)^n])^2 \operatorname{PolyLog}\left[2, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} + \frac{6 b^3 d g m n^3 \operatorname{PolyLog}\left[2, \frac{e(i+jx)}{e^{i-dj}}\right]}{e} - \frac{6 b^3 d g m n^3 \operatorname{PolyLog}\left[3, -\frac{j(d+ex)}{e^{i-dj}}\right]}{e} + \\ & \frac{6 b^3 g i m n^3 \operatorname{PolyLog}\left[3, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} + \frac{6 b^2 d g m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, -\frac{j(d+ex)}{e^{i-dj}}\right]}{e} - \\ & \frac{6 b^2 g i m n^2 (a + b \operatorname{Log}[c (d + e x)^n]) \operatorname{PolyLog}\left[3, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} - \frac{6 b^3 d g m n^3 \operatorname{PolyLog}\left[4, -\frac{j(d+ex)}{e^{i-dj}}\right]}{e} + \frac{6 b^3 g i m n^3 \operatorname{PolyLog}\left[4, -\frac{j(d+ex)}{e^{i-dj}}\right]}{j} \end{aligned}$$

Result (type 4, 3326 leaves):

$$\begin{aligned}
& \frac{1}{e^j} \left(-3a^2 b d f j n + 3a^2 b d g j m n + 6a b^2 d f j n^2 - 12a b^2 d g j m n^2 - 6b^3 d f j n^3 + 18b^3 d g j m n^3 + a^3 e f j x - a^3 e g j m x - \right. \\
& 3a^2 b e f j n x + 6a^2 b e g j m n x + 6a b^2 e f j n^2 x - 18a b^2 e g j m n^2 x - 6b^3 e f j n^3 x + 24b^3 e g j m n^3 x + 3a^2 b d f j n \operatorname{Log}[d + e x] - \\
& 3a^2 b d g j m n \operatorname{Log}[d + e x] + 6a b^2 d g j m n^2 \operatorname{Log}[d + e x] - 6b^3 d g j m n^3 \operatorname{Log}[d + e x] - 3a b^2 d f j n^2 \operatorname{Log}[d + e x]^2 + \\
& 3a b^2 d g j m n^2 \operatorname{Log}[d + e x]^2 - 3b^3 d g j m n^3 \operatorname{Log}[d + e x]^2 + b^3 d f j n^3 \operatorname{Log}[d + e x]^3 - b^3 d g j m n^3 \operatorname{Log}[d + e x]^3 - \\
& 6a b^2 d f j n \operatorname{Log}[c(d + e x)^n] + 6a b^2 d g j m n \operatorname{Log}[c(d + e x)^n] + 6b^3 d f j n^2 \operatorname{Log}[c(d + e x)^n] - 12b^3 d g j m n^2 \operatorname{Log}[c(d + e x)^n] + \\
& 3a^2 b e f j x \operatorname{Log}[c(d + e x)^n] - 3a^2 b e g j m x \operatorname{Log}[c(d + e x)^n] - 6a b^2 e f j n x \operatorname{Log}[c(d + e x)^n] + 12a b^2 e g j m n x \operatorname{Log}[c(d + e x)^n] + \\
& 6b^3 e f j n^2 x \operatorname{Log}[c(d + e x)^n] - 18b^3 e g j m n^2 x \operatorname{Log}[c(d + e x)^n] + 6a b^2 d f j n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] - \\
& 6a b^2 d g j m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] + 6b^3 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] - 3b^3 d f j n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c(d + e x)^n] + \\
& 3b^3 d g j m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c(d + e x)^n] - 3b^3 d f j n \operatorname{Log}[c(d + e x)^n]^2 + 3b^3 d g j m n \operatorname{Log}[c(d + e x)^n]^2 + \\
& 3a b^2 e f j x \operatorname{Log}[c(d + e x)^n]^2 - 3a b^2 e g j m x \operatorname{Log}[c(d + e x)^n]^2 - 3b^3 e f j n x \operatorname{Log}[c(d + e x)^n]^2 + 6b^3 e g j m n x \operatorname{Log}[c(d + e x)^n]^2 + \\
& 3b^3 d f j n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n]^2 - 3b^3 d g j m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n]^2 + b^3 e f j x \operatorname{Log}[c(d + e x)^n]^3 - \\
& b^3 e g j m x \operatorname{Log}[c(d + e x)^n]^3 + a^3 e g i m \operatorname{Log}[i + j x] - 3a^2 b e g i m n \operatorname{Log}[i + j x] + 3a^2 b d g j m n \operatorname{Log}[i + j x] + 6a b^2 e g i m n^2 \operatorname{Log}[i + j x] - \\
& 6a b^2 d g j m n^2 \operatorname{Log}[i + j x] - 6b^3 e g i m n^3 \operatorname{Log}[i + j x] + 6b^3 d g j m n^3 \operatorname{Log}[i + j x] - 3a^2 b e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + \\
& 6a b^2 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - 6a b^2 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] - 6b^3 e g i m n^3 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + \\
& 6b^3 d g j m n^3 \operatorname{Log}[d + e x] \operatorname{Log}[i + j x] + 3a b^2 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] - 3b^3 e g i m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] + \\
& 3b^3 d g j m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}[i + j x] - b^3 e g i m n^3 \operatorname{Log}[d + e x]^3 \operatorname{Log}[i + j x] + 3a^2 b e g i m \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] - \\
& 6a b^2 e g i m n \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] + 6a b^2 d g j m n \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] + 6b^3 e g i m n^2 \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] - \\
& 6b^3 d g j m n^2 \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] - 6a b^2 e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] + \\
& 6b^3 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] - 6b^3 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] + \\
& 3b^3 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c(d + e x)^n] \operatorname{Log}[i + j x] + 3a b^2 e g i m \operatorname{Log}[c(d + e x)^n]^2 \operatorname{Log}[i + j x] - \\
& 3b^3 e g i m n \operatorname{Log}[c(d + e x)^n]^2 \operatorname{Log}[i + j x] + 3b^3 d g j m n \operatorname{Log}[c(d + e x)^n]^2 \operatorname{Log}[i + j x] - 3b^3 e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n]^2 \operatorname{Log}[i + j x] + \\
& b^3 e g i m \operatorname{Log}[c(d + e x)^n]^3 \operatorname{Log}[i + j x] + 3a^2 b e g i m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - 3a^2 b d g j m n \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - \\
& 6a b^2 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + 6a b^2 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + 6b^3 e g i m n^3 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - \\
& 6b^3 d g j m n^3 \operatorname{Log}[d + e x] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - 3a b^2 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + 3a b^2 d g j m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + \\
& 3b^3 e g i m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - 3b^3 d g j m n^3 \operatorname{Log}[d + e x]^2 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + b^3 e g i m n^3 \operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - \\
& b^3 d g j m n^3 \operatorname{Log}[d + e x]^3 \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + 6a b^2 e g i m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - \\
& 6a b^2 d g j m n \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - 6b^3 e g i m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] + \\
& 6b^3 d g j m n^2 \operatorname{Log}[d + e x] \operatorname{Log}[c(d + e x)^n] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] - 3b^3 e g i m n^2 \operatorname{Log}[d + e x]^2 \operatorname{Log}[c(d + e x)^n] \operatorname{Log}\left[\frac{e(i + j x)}{e^i - d^j}\right] +
\end{aligned}$$

$$\begin{aligned}
& 3 b^3 d g j m n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right] + 3 b^3 e g i m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right] - \\
& 3 b^3 d g j m n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}\left[\frac{e(i+j x)}{e i-d j}\right] - 3 a^2 b d g j n \operatorname{Log}[h(i+j x)^m] + 6 a b^2 d g j n^2 \operatorname{Log}[h(i+j x)^m] - \\
& 6 b^3 d g j n^3 \operatorname{Log}[h(i+j x)^m] + a^3 e g j x \operatorname{Log}[h(i+j x)^m] - 3 a^2 b e g j n x \operatorname{Log}[h(i+j x)^m] + 6 a b^2 e g j n^2 x \operatorname{Log}[h(i+j x)^m] - \\
& 6 b^3 e g j n^3 x \operatorname{Log}[h(i+j x)^m] + 3 a^2 b d g j n \operatorname{Log}[d+e x] \operatorname{Log}[h(i+j x)^m] - 3 a b^2 d g j n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[h(i+j x)^m] + \\
& b^3 d g j n^3 \operatorname{Log}[d+e x]^3 \operatorname{Log}[h(i+j x)^m] - 6 a b^2 d g j n \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] + 6 b^3 d g j n^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] + \\
& 3 a^2 b e g j x \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] - 6 a b^2 e g j n x \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] + \\
& 6 b^3 e g j n^2 x \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] + 6 a b^2 d g j n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] - \\
& 3 b^3 d g j n^2 \operatorname{Log}[d+e x]^2 \operatorname{Log}[c(d+e x)^n] \operatorname{Log}[h(i+j x)^m] - 3 b^3 d g j n \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m] + \\
& 3 a b^2 e g j x \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m] - 3 b^3 e g j n x \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m] + \\
& 3 b^3 d g j n \operatorname{Log}[d+e x] \operatorname{Log}[c(d+e x)^n]^2 \operatorname{Log}[h(i+j x)^m] + b^3 e g j x \operatorname{Log}[c(d+e x)^n]^3 \operatorname{Log}[h(i+j x)^m] + \\
& 3 b g(e i-d j) m n\left(a^2-2 a b n+2 b^2 n^2+2 b(a-b n) \operatorname{Log}[c(d+e x)^n]+b^2 \operatorname{Log}[c(d+e x)^n]^2\right) \operatorname{PolyLog}\left[2, \frac{j(d+e x)}{-e i+d j}\right] - \\
& 6 b^2 g(e i-d j) m n^2(a-b n+b \operatorname{Log}[c(d+e x)^n]) \operatorname{PolyLog}\left[3, \frac{j(d+e x)}{-e i+d j}\right] + \\
& 6 b^3 e g i m n^3 \operatorname{PolyLog}\left[4, \frac{j(d+e x)}{-e i+d j}\right] - 6 b^3 d g j m n^3 \operatorname{PolyLog}\left[4, \frac{j(d+e x)}{-e i+d j}\right]
\end{aligned}$$

Problem 404: Result more than twice size of optimal antiderivative.

$$\int(a+b \operatorname{Log}[c(d(e+f x)^m)^n])^4 d x$$

Optimal (type 3, 160 leaves, 7 steps):

$$\begin{aligned}
& -24 a b^3 m^3 n^3 x + 24 b^4 m^4 n^4 x - \frac{24 b^4 m^3 n^3(e+f x) \operatorname{Log}[c(d(e+f x)^m)^n]}{f} + \frac{12 b^2 m^2 n^2(e+f x)(a+b \operatorname{Log}[c(d(e+f x)^m)^n])^2}{f} - \\
& \frac{4 b m n(e+f x)(a+b \operatorname{Log}[c(d(e+f x)^m)^n])^3}{f} + \frac{(e+f x)(a+b \operatorname{Log}[c(d(e+f x)^m)^n])^4}{f}
\end{aligned}$$

Result (type 3, 480 leaves):

$$\begin{aligned} & \frac{1}{f} \left(-b^4 e m^4 n^4 \operatorname{Log}[e + f x]^4 + 4 b^3 e m^3 n^3 \operatorname{Log}[e + f x]^3 (a - b m n + b \operatorname{Log}[c (d (e + f x)^m)^n]) - \right. \\ & 6 b^2 e m^2 n^2 \operatorname{Log}[e + f x]^2 (a^2 - 2 a b m n + 2 b^2 m^2 n^2 + 2 b (a - b m n) \operatorname{Log}[c (d (e + f x)^m)^n] + b^2 \operatorname{Log}[c (d (e + f x)^m)^n]^2) + \\ & 4 b e m n \operatorname{Log}[e + f x] (a^3 - 3 a^2 b m n + 6 a b^2 m^2 n^2 - 6 b^3 m^3 n^3 + \\ & 3 b (a^2 - 2 a b m n + 2 b^2 m^2 n^2) \operatorname{Log}[c (d (e + f x)^m)^n] + 3 b^2 (a - b m n) \operatorname{Log}[c (d (e + f x)^m)^n]^2 + b^3 \operatorname{Log}[c (d (e + f x)^m)^n]^3) + \\ & \left. f x (a^4 - 4 a^3 b m n + 12 a^2 b^2 m^2 n^2 - 24 a b^3 m^3 n^3 + 24 b^4 m^4 n^4 + 4 b (a^3 - 3 a^2 b m n + 6 a b^2 m^2 n^2 - 6 b^3 m^3 n^3) \operatorname{Log}[c (d (e + f x)^m)^n] + \right. \\ & \left. 6 b^2 (a^2 - 2 a b m n + 2 b^2 m^2 n^2) \operatorname{Log}[c (d (e + f x)^m)^n]^2 + 4 b^3 (a - b m n) \operatorname{Log}[c (d (e + f x)^m)^n]^3 + b^4 \operatorname{Log}[c (d (e + f x)^m)^n]^4) \right) \end{aligned}$$

Problem 405: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^3 dx$$

Optimal (type 3, 121 leaves, 6 steps):

$$\begin{aligned} & 6 a b^2 m^2 n^2 x - 6 b^3 m^3 n^3 x + \frac{6 b^3 m^2 n^2 (e + f x) \operatorname{Log}[c (d (e + f x)^m)^n]}{f} - \\ & \frac{3 b m n (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^2}{f} + \frac{(e + f x) (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^3}{f} \end{aligned}$$

Result (type 3, 268 leaves):

$$\begin{aligned} & \frac{1}{f} \left(b^3 e m^3 n^3 \operatorname{Log}[e + f x]^3 - 3 b^2 e m^2 n^2 \operatorname{Log}[e + f x]^2 (a - b m n + b \operatorname{Log}[c (d (e + f x)^m)^n]) + \right. \\ & 3 b e m n \operatorname{Log}[e + f x] (a^2 - 2 a b m n + 2 b^2 m^2 n^2 + 2 b (a - b m n) \operatorname{Log}[c (d (e + f x)^m)^n] + b^2 \operatorname{Log}[c (d (e + f x)^m)^n]^2) + f x (a^3 - 3 a^2 b m n + 6 a b^2 m^2 n^2 - \\ & \left. 6 b^3 m^3 n^3 + 3 b (a^2 - 2 a b m n + 2 b^2 m^2 n^2) \operatorname{Log}[c (d (e + f x)^m)^n] + 3 b^2 (a - b m n) \operatorname{Log}[c (d (e + f x)^m)^n]^2 + b^3 \operatorname{Log}[c (d (e + f x)^m)^n]^3) \right) \end{aligned}$$

Problem 411: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{5/2} dx$$

Optimal (type 4, 219 leaves, 8 steps):

$$\begin{aligned} & - \frac{15 b^{5/2} e^{-\frac{a}{b m n}} m^{5/2} n^{5/2} \sqrt{\pi} (e + f x) (c (d (e + f x)^m)^n)^{-\frac{1}{m n}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{\sqrt{b} \sqrt{m} \sqrt{n}}\right]}{8 f} + \\ & \frac{15 b^2 m^2 n^2 (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{4 f} - \frac{5 b m n (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{3/2}}{2 f} + \frac{(e + f x) (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{5/2}}{f} \end{aligned}$$

Result (type 8, 24 leaves):

$$\int (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{5/2} dx$$

Problem 412: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{3/2} dx$$

Optimal (type 4, 176 leaves, 7 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{b m n}} m^{3/2} n^{3/2} \sqrt{\pi} (e + f x) (c (d (e + f x)^m)^n)^{-\frac{1}{m n}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{\sqrt{b} \sqrt{m} \sqrt{n}}\right]}{4 f} - \frac{3 b m n (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{2 f} + \frac{(e + f x) (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{3/2}}{f}$$

Result (type 8, 24 leaves):

$$\int (a + b \operatorname{Log}[c (d (e + f x)^m)^n])^{3/2} dx$$

Problem 413: Attempted integration timed out after 120 seconds.

$$\int \sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]} dx$$

Optimal (type 4, 139 leaves, 6 steps):

$$-\frac{\sqrt{b} e^{-\frac{a}{b m n}} \sqrt{m} \sqrt{n} \sqrt{\pi} (e + f x) (c (d (e + f x)^m)^n)^{-\frac{1}{m n}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{\sqrt{b} \sqrt{m} \sqrt{n}}\right]}{2 f} + \frac{(e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^m)^n]}}{f}$$

Result (type 1, 1 leaves):

???

Problem 432: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{g + h x} dx$$

Optimal (type 4, 123 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{Log}\left[\frac{f(g + h x)}{f g - e h}\right]}{h} + \frac{2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{h(e + f x)}{f g - e h}\right]}{h} - \frac{2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{h(e + f x)}{f g - e h}\right]}{h}$$

Result (type 4, 324 leaves):

$$\begin{aligned} & \frac{1}{h} \left(a^2 \operatorname{Log}[g + hx] - 2abpq \operatorname{Log}[e + fx] \operatorname{Log}[g + hx] + b^2 p^2 q^2 \operatorname{Log}[e + fx]^2 \operatorname{Log}[g + hx] + 2ab \operatorname{Log}[c(d(e + fx)^p)^q] \operatorname{Log}[g + hx] - \right. \\ & \quad \left. 2b^2 pq \operatorname{Log}[e + fx] \operatorname{Log}[c(d(e + fx)^p)^q] \operatorname{Log}[g + hx] + b^2 \operatorname{Log}[c(d(e + fx)^p)^q]^2 \operatorname{Log}[g + hx] + 2abpq \operatorname{Log}[e + fx] \operatorname{Log}\left[\frac{f(g + hx)}{fg - eh}\right] \right) - \\ & \quad b^2 p^2 q^2 \operatorname{Log}[e + fx]^2 \operatorname{Log}\left[\frac{f(g + hx)}{fg - eh}\right] + 2b^2 pq \operatorname{Log}[e + fx] \operatorname{Log}[c(d(e + fx)^p)^q] \operatorname{Log}\left[\frac{f(g + hx)}{fg - eh}\right] + \\ & \quad \left. 2b pq \left(a + b \operatorname{Log}[c(d(e + fx)^p)^q] \right) \operatorname{PolyLog}\left[2, \frac{h(e + fx)}{-fg + eh}\right] - 2b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{h(e + fx)}{-fg + eh}\right] \right) \end{aligned}$$

Problem 437: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c(d(e + fx)^p)^q])^3 dx$$

Optimal (type 3, 121 leaves, 6 steps):

$$\begin{aligned} & 6ab^2 p^2 q^2 x - 6b^3 p^3 q^3 x + \frac{6b^3 p^2 q^2 (e + fx) \operatorname{Log}[c(d(e + fx)^p)^q]}{f} - \\ & \quad \frac{3bpq(e + fx)(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^2}{f} + \frac{(e + fx)(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^3}{f} \end{aligned}$$

Result (type 3, 268 leaves):

$$\begin{aligned} & \frac{1}{f} \left(b^3 e p^3 q^3 \operatorname{Log}[e + fx]^3 - 3b^2 e p^2 q^2 \operatorname{Log}[e + fx]^2 (a - bpq + b \operatorname{Log}[c(d(e + fx)^p)^q]) + \right. \\ & \quad \left. 3bepq \operatorname{Log}[e + fx] (a^2 - 2abpq + 2b^2 p^2 q^2 + 2b(a - bpq) \operatorname{Log}[c(d(e + fx)^p)^q] + b^2 \operatorname{Log}[c(d(e + fx)^p)^q]^2) + fx (a^3 - 3a^2 bpq + 6ab^2 p^2 q^2 - \right. \\ & \quad \left. 6b^3 p^3 q^3 + 3b(a^2 - 2abpq + 2b^2 p^2 q^2) \operatorname{Log}[c(d(e + fx)^p)^q] + 3b^2(a - bpq) \operatorname{Log}[c(d(e + fx)^p)^q]^2 + b^3 \operatorname{Log}[c(d(e + fx)^p)^q]^3 \right) \end{aligned}$$

Problem 438: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^3}{g + hx} dx$$

Optimal (type 4, 177 leaves, 6 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h} - \frac{6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right] + 6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h}$$

Result (type 4, 646 leaves):

$$\frac{1}{h} \left(a^3 \operatorname{Log}[g + h x] - 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + 3 a^2 b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 a b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + b^3 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, \frac{h(e+fx)}{-fg+eh}\right] - 6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, \frac{h(e+fx)}{-fg+eh}\right] + 6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] \right)$$

Problem 439: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{(g + h x)^2} dx$$

Optimal (type 4, 209 leaves, 6 steps):

$$\frac{(e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{(f g - e h) (g + h x)} - \frac{3 b f p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right]}{h (f g - e h)} - \frac{6 b^2 f p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h (f g - e h)} + \frac{6 b^3 f p^3 q^3 \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h (f g - e h)}$$

Result (type 4, 444 leaves):

$$\frac{1}{h(fg - eh)(g + hx)} \left(-3b(fg - eh)pq \operatorname{Log}[e + fx] (a - b p q \operatorname{Log}[e + fx] + b \operatorname{Log}[c(d(e + fx)^p)^q])^2 + \right. \\ \left. 3bfpq(g + hx) \operatorname{Log}[e + fx] (a - b p q \operatorname{Log}[e + fx] + b \operatorname{Log}[c(d(e + fx)^p)^q])^2 - (fg - eh)(a - b p q \operatorname{Log}[e + fx] + b \operatorname{Log}[c(d(e + fx)^p)^q])^3 - \right. \\ \left. 3bfpq(g + hx)(a - b p q \operatorname{Log}[e + fx] + b \operatorname{Log}[c(d(e + fx)^p)^q])^2 \operatorname{Log}[g + hx] + 3b^2 p^2 q^2 (a - b p q \operatorname{Log}[e + fx] + b \operatorname{Log}[c(d(e + fx)^p)^q]) \right. \\ \left. \left(\operatorname{Log}[e + fx] \left(h(e + fx) \operatorname{Log}[e + fx] - 2f(g + hx) \operatorname{Log}\left[\frac{f(g + hx)}{fg - eh}\right] \right) - 2f(g + hx) \operatorname{PolyLog}\left[2, \frac{h(e + fx)}{-fg + eh}\right] \right) + \right. \\ \left. b^3 p^3 q^3 \left(\operatorname{Log}[e + fx]^2 \left(h(e + fx) \operatorname{Log}[e + fx] - 3f(g + hx) \operatorname{Log}\left[\frac{f(g + hx)}{fg - eh}\right] \right) - \right. \right. \\ \left. \left. 6f(g + hx) \operatorname{Log}[e + fx] \operatorname{PolyLog}\left[2, \frac{h(e + fx)}{-fg + eh}\right] + 6f(g + hx) \operatorname{PolyLog}\left[3, \frac{h(e + fx)}{-fg + eh}\right] \right) \right)$$

Problem 441: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Log}[c(d(e + fx)^p)^q])^4 dx$$

Optimal (type 3, 160 leaves, 7 steps):

$$-24ab^3p^3q^3x + 24b^4p^4q^4x - \frac{24b^4p^3q^3(e + fx) \operatorname{Log}[c(d(e + fx)^p)^q]}{f} + \frac{12b^2p^2q^2(e + fx)(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^2}{f} - \\ \frac{4bpq(e + fx)(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^3}{f} + \frac{(e + fx)(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^4}{f}$$

Result (type 3, 480 leaves):

$$\frac{1}{f} \left(-b^4e p^4 q^4 \operatorname{Log}[e + fx]^4 + 4b^3e p^3 q^3 \operatorname{Log}[e + fx]^3 (a - b p q + b \operatorname{Log}[c(d(e + fx)^p)^q]) - \right. \\ \left. 6b^2e p^2 q^2 \operatorname{Log}[e + fx]^2 (a^2 - 2abpq + 2b^2p^2q^2 + 2b(a - b p q) \operatorname{Log}[c(d(e + fx)^p)^q] + b^2 \operatorname{Log}[c(d(e + fx)^p)^q]^2) + \right. \\ \left. 4bepq \operatorname{Log}[e + fx] (a^3 - 3a^2bpq + 6ab^2p^2q^2 - 6b^3p^3q^3 + \right. \\ \left. 3b(a^2 - 2abpq + 2b^2p^2q^2) \operatorname{Log}[c(d(e + fx)^p)^q] + 3b^2(a - b p q) \operatorname{Log}[c(d(e + fx)^p)^q]^2 + b^3 \operatorname{Log}[c(d(e + fx)^p)^q]^3) + \right. \\ \left. fx (a^4 - 4a^3bpq + 12a^2b^2p^2q^2 - 24ab^3p^3q^3 + 24b^4p^4q^4 + 4b(a^3 - 3a^2bpq + 6ab^2p^2q^2 - 6b^3p^3q^3) \operatorname{Log}[c(d(e + fx)^p)^q] + \right. \\ \left. 6b^2(a^2 - 2abpq + 2b^2p^2q^2) \operatorname{Log}[c(d(e + fx)^p)^q]^2 + 4b^3(a - b p q) \operatorname{Log}[c(d(e + fx)^p)^q]^3 + b^4 \operatorname{Log}[c(d(e + fx)^p)^q]^4) \right)$$

Problem 442: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c(d(e + fx)^p)^q])^4}{g + hx} dx$$

Optimal (type 4, 231 leaves, 7 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^4 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right]}{h} + \frac{4 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h} -$$

$$\frac{12 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h} +$$

$$\frac{24 b^3 p^3 q^3 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h} - \frac{24 b^4 p^4 q^4 \operatorname{PolyLog}\left[5, -\frac{h(e+fx)}{fg-eh}\right]}{h}$$

Result (type 4, 1095 leaves):

$$\frac{1}{h} \left(a^4 \operatorname{Log}[g + h x] - 4 a^3 b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 6 a^2 b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - 4 a b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + \right.$$

$$b^4 p^4 q^4 \operatorname{Log}[e + f x]^4 \operatorname{Log}[g + h x] + 4 a^3 b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 12 a^2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] +$$

$$12 a b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 4 b^4 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] +$$

$$6 a^2 b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - 12 a b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] +$$

$$6 b^4 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 4 a b^3 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] -$$

$$4 b^4 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + b^4 \operatorname{Log}[c (d (e + f x)^p)^q]^4 \operatorname{Log}[g + h x] + 4 a^3 b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] -$$

$$6 a^2 b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 4 a b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - b^4 p^4 q^4 \operatorname{Log}[e + f x]^4 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$12 a^2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - 12 a b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$4 b^4 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 12 a b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] -$$

$$6 b^4 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 4 b^4 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$4 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{PolyLog}\left[2, \frac{h(e+fx)}{-fg+eh}\right] - 12 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[3, \frac{h(e+fx)}{-fg+eh}\right] +$$

$$24 a b^3 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] + 24 b^4 p^3 q^3 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] - 24 b^4 p^4 q^4 \operatorname{PolyLog}\left[5, \frac{h(e+fx)}{-fg+eh}\right] \Big)$$

Problem 443: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^4}{(g + h x)^2} dx$$

Optimal (type 4, 274 leaves, 7 steps):

$$\frac{(e+fx)(a+b\log[c(d(e+fx)^p)^q])^4}{(fg-eh)(g+hx)} - \frac{4bfpq(a+b\log[c(d(e+fx)^p)^q])^3 \log\left[\frac{f(g+hx)}{fg-eh}\right]}{h(fg-eh)}$$

$$\frac{12b^2fp^2q^2(a+b\log[c(d(e+fx)^p)^q])^2 \text{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h(fg-eh)} +$$

$$\frac{24b^3fp^3q^3(a+b\log[c(d(e+fx)^p)^q]) \text{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h(fg-eh)} - \frac{24b^4fp^4q^4 \text{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h(fg-eh)}$$

Result (type 4, 1301 leaves):

$$\frac{1}{h(-fg+eh)(g+hx)}$$

$$\left(a^4fg - a^4eh - 4a^3bfgpq \log[e+fx] - 4a^3bfhpqx \log[e+fx] + 6a^2b^2fgp^2q^2 \log[e+fx]^2 + 6a^2b^2fhp^2q^2x \log[e+fx]^2 - \right.$$

$$4a^3b^3fgp^3q^3 \log[e+fx]^3 - 4a^3bfhp^3q^3x \log[e+fx]^3 + b^4fgp^4q^4 \log[e+fx]^4 + b^4fhp^4q^4x \log[e+fx]^4 + 4a^3bfg \log[c(d(e+fx)^p)^q] -$$

$$4a^3beh \log[c(d(e+fx)^p)^q] - 12a^2b^2fgpq \log[e+fx] \log[c(d(e+fx)^p)^q] - 12a^2b^2fhpqx \log[e+fx] \log[c(d(e+fx)^p)^q] +$$

$$12a^3b^3fgp^2q^2 \log[e+fx]^2 \log[c(d(e+fx)^p)^q] + 12a^3bfhp^2q^2x \log[e+fx]^2 \log[c(d(e+fx)^p)^q] -$$

$$4b^4fgp^3q^3 \log[e+fx]^3 \log[c(d(e+fx)^p)^q] - 4b^4fhp^3q^3x \log[e+fx]^3 \log[c(d(e+fx)^p)^q] + 6a^2b^2fg \log[c(d(e+fx)^p)^q]^2 -$$

$$6a^2b^2eh \log[c(d(e+fx)^p)^q]^2 - 12a^3b^3fgpq \log[e+fx] \log[c(d(e+fx)^p)^q]^2 - 12a^3bfhpqx \log[e+fx] \log[c(d(e+fx)^p)^q]^2 +$$

$$6b^4fgp^2q^2 \log[e+fx]^2 \log[c(d(e+fx)^p)^q]^2 + 6b^4fhp^2q^2x \log[e+fx]^2 \log[c(d(e+fx)^p)^q]^2 +$$

$$4a^3b^3fg \log[c(d(e+fx)^p)^q]^3 - 4a^3beh \log[c(d(e+fx)^p)^q]^3 - 4b^4fgpq \log[e+fx] \log[c(d(e+fx)^p)^q]^3 -$$

$$4b^4fhpqx \log[e+fx] \log[c(d(e+fx)^p)^q]^3 + b^4fg \log[c(d(e+fx)^p)^q]^4 - b^4eh \log[c(d(e+fx)^p)^q]^4 +$$

$$4a^3bfgpq \log\left[\frac{f(g+hx)}{fg-eh}\right] + 4a^3bfhpqx \log\left[\frac{f(g+hx)}{fg-eh}\right] + 12a^2b^2fgpq \log[c(d(e+fx)^p)^q] \log\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$12a^2b^2fhpqx \log[c(d(e+fx)^p)^q] \log\left[\frac{f(g+hx)}{fg-eh}\right] + 12a^3bfgpq \log[c(d(e+fx)^p)^q]^2 \log\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$12a^3bfhpqx \log[c(d(e+fx)^p)^q]^2 \log\left[\frac{f(g+hx)}{fg-eh}\right] + 4b^4fgpq \log[c(d(e+fx)^p)^q]^3 \log\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$4b^4fhpqx \log[c(d(e+fx)^p)^q]^3 \log\left[\frac{f(g+hx)}{fg-eh}\right] + 12b^2fp^2q^2(g+hx)(a+b\log[c(d(e+fx)^p)^q])^2 \text{PolyLog}\left[2, \frac{h(e+fx)}{-fg+eh}\right] -$$

$$24b^3fp^3q^3(g+hx)(a+b\log[c(d(e+fx)^p)^q]) \text{PolyLog}\left[3, \frac{h(e+fx)}{-fg+eh}\right] +$$

$$24b^4fp^4q^4 \text{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] + 24b^4fhp^4q^4x \text{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] \Big)$$

Problem 450: Result more than twice size of optimal antiderivative.

$$\int \frac{(g + h x)^2}{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2} dx$$

Optimal (type 4, 326 leaves, 21 steps):

$$\frac{e^{-\frac{a}{b p q}} (f g - e h)^2 (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{b p q}\right]}{b^2 f^3 p^2 q^2} +$$

$$\frac{4 e^{-\frac{2a}{b p q}} h (f g - e h) (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{b p q}\right]}{b^2 f^3 p^2 q^2} +$$

$$\frac{3 e^{-\frac{3a}{b p q}} h^2 (e + f x)^3 (c (d (e + f x)^p)^q)^{-\frac{3}{p q}} \operatorname{ExpIntegralEi}\left[\frac{3 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{b p q}\right]}{b^2 f^3 p^2 q^2} - \frac{(e + f x) (g + h x)^2}{b f p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}$$

Result (type 4, 1310 leaves):

$$\begin{aligned}
& \frac{1}{b^2 f^3 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])} e^{-\frac{3a}{bpq}} (c (d (e + f x)^p)^q)^{-\frac{3}{pq}} \\
& \left(-b e^{\frac{3a}{bpq}} f^2 g^2 p q (c (d (e + f x)^p)^q)^{\frac{3}{pq}} - b e^{\frac{3a}{bpq}} f^3 g^2 p q x (c (d (e + f x)^p)^q)^{\frac{3}{pq}} - 2 b e^{\frac{3a}{bpq}} f^2 g h p q x (c (d (e + f x)^p)^q)^{\frac{3}{pq}} - \right. \\
& 2 b e^{\frac{3a}{bpq}} f^3 g h p q x^2 (c (d (e + f x)^p)^q)^{\frac{3}{pq}} - b e^{\frac{3a}{bpq}} f^2 h^2 p q x^2 (c (d (e + f x)^p)^q)^{\frac{3}{pq}} - b e^{\frac{3a}{bpq}} f^3 h^2 p q x^3 (c (d (e + f x)^p)^q)^{\frac{3}{pq}} + \\
& a e^{\frac{2a}{bpq}} f^2 g^2 (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] - 2 a e^{\frac{2a}{bpq}} f g h (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \\
& \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] + a e^2 e^{\frac{2a}{bpq}} h^2 (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] + \\
& 4 a e^{\frac{a}{bpq}} f g h (e + f x)^2 (c (d (e + f x)^p)^q)^{\frac{1}{pq}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] - 4 a e^{\frac{a}{bpq}} h^2 (e + f x)^2 \\
& (c (d (e + f x)^p)^q)^{\frac{1}{pq}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] + 3 a h^2 (e + f x)^3 \operatorname{ExpIntegralEi}\left[\frac{3 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] + \\
& b e^{\frac{2a}{bpq}} f^2 g^2 (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 2 b e^{\frac{2a}{bpq}} f g h (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& b e^2 e^{\frac{2a}{bpq}} h^2 (e + f x) (c (d (e + f x)^p)^q)^{\frac{2}{pq}} \operatorname{ExpIntegralEi}\left[\frac{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 4 b e^{\frac{a}{bpq}} f g h (e + f x)^2 (c (d (e + f x)^p)^q)^{\frac{1}{pq}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 4 b e^{\frac{a}{bpq}} h^2 (e + f x)^2 (c (d (e + f x)^p)^q)^{\frac{1}{pq}} \operatorname{ExpIntegralEi}\left[\frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& \left. 3 b h^2 (e + f x)^3 \operatorname{ExpIntegralEi}\left[\frac{3 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]}{bpq}\right] \operatorname{Log}[c (d (e + f x)^p)^q] \right)
\end{aligned}$$

Problem 460: Unable to integrate problem.

$$\int (g + h x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]} dx$$

Optimal (type 4, 488 leaves, 18 steps):

$$\begin{aligned}
& - \frac{\sqrt{b} e^{-\frac{a}{b p q}} (f g - e h)^2 \sqrt{p} \sqrt{\pi} \sqrt{q} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{2 f^3} \\
& - \frac{\sqrt{b} e^{-\frac{2 a}{b p q}} h (f g - e h) \sqrt{p} \sqrt{\frac{\pi}{2}} \sqrt{q} (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{2 f^3} \\
& + \frac{\sqrt{b} e^{-\frac{3 a}{b p q}} h^2 \sqrt{p} \sqrt{\frac{\pi}{3}} \sqrt{q} (e + f x)^3 (c (d (e + f x)^p)^q)^{-\frac{3}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{6 f^3} + \frac{(f g - e h)^2 (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{f^3} \\
& + \frac{h (f g - e h) (e + f x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{f^3} + \frac{h^2 (e + f x)^3 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{3 f^3}
\end{aligned}$$

Result (type 8, 32 leaves):

$$\int (g + h x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]} dx$$

Problem 461: Unable to integrate problem.

$$\int (g + h x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]} dx$$

Optimal (type 4, 311 leaves, 13 steps):

$$\begin{aligned}
& - \frac{\sqrt{b} e^{-\frac{a}{b p q}} (f g - e h) \sqrt{p} \sqrt{\pi} \sqrt{q} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{2 f^2} \\
& + \frac{\sqrt{b} e^{-\frac{2 a}{b p q}} h \sqrt{p} \sqrt{\frac{\pi}{2}} \sqrt{q} (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{4 f^2} \\
& + \frac{(f g - e h) (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{f^2} + \frac{h (e + f x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{2 f^2}
\end{aligned}$$

Result (type 8, 30 leaves):

$$\int (g + h x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]} dx$$

Problem 462: Attempted integration timed out after 120 seconds.

$$\int \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]} dx$$

Optimal (type 4, 139 leaves, 6 steps):

$$\frac{\sqrt{b} e^{-\frac{a}{b p q}} \sqrt{p} \sqrt{\pi} \sqrt{q} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{2 f} + \frac{(e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{f}$$

Result (type 1, 1 leaves):

???

Problem 465: Unable to integrate problem.

$$\int (g + h x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Optimal (type 4, 625 leaves, 21 steps):

$$\begin{aligned} & \frac{3 b^{3/2} e^{-\frac{a}{b p q}} (f g - e h)^2 p^{3/2} \sqrt{\pi} q^{3/2} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{4 f^3} + \\ & \frac{3 b^{3/2} e^{-\frac{2a}{b p q}} h (f g - e h) p^{3/2} \sqrt{\frac{\pi}{2}} q^{3/2} (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{8 f^3} + \\ & \frac{b^{3/2} e^{-\frac{3a}{b p q}} h^2 p^{3/2} \sqrt{\frac{\pi}{3}} q^{3/2} (e + f x)^3 (c (d (e + f x)^p)^q)^{-\frac{3}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{12 f^3} - \\ & \frac{3 b (f g - e h)^2 p q (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{2 f^3} - \frac{3 b h (f g - e h) p q (e + f x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{4 f^3} - \\ & \frac{b h^2 p q (e + f x)^3 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{6 f^3} + \frac{(f g - e h)^2 (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{f^3} + \\ & \frac{h (f g - e h) (e + f x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{f^3} + \frac{h^2 (e + f x)^3 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{3 f^3} \end{aligned}$$

Result (type 8, 32 leaves):

$$\int (g + h x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Problem 466: Unable to integrate problem.

$$\int (g + h x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Optimal (type 4, 396 leaves, 15 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{b p q}} (f g - e h) p^{3/2} \sqrt{\pi} q^{3/2} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{4 f^2} +$$

$$\frac{3 b^{3/2} e^{-\frac{2 a}{b p q}} h p^{3/2} \sqrt{\frac{\pi}{2}} q^{3/2} (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{16 f^2} -$$

$$\frac{3 b (f g - e h) p q (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{2 f^2} - \frac{3 b h p q (e + f x)^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{8 f^2} +$$

$$\frac{(f g - e h) (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{f^2} + \frac{h (e + f x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{2 f^2}$$

Result (type 8, 30 leaves):

$$\int (g + h x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Problem 467: Unable to integrate problem.

$$\int (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Optimal (type 4, 176 leaves, 7 steps):

$$\frac{3 b^{3/2} e^{-\frac{a}{b p q}} p^{3/2} \sqrt{\pi} q^{3/2} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{4 f} -$$

$$\frac{3 b p q (e + f x) \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{2 f} + \frac{(e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}}{f}$$

Result (type 8, 24 leaves):

$$\int (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2} dx$$

Problem 470: Result more than twice size of optimal antiderivative.

$$\int \frac{(g + h x)^2}{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}} dx$$

Optimal (type 4, 355 leaves, 15 steps):

$$\frac{e^{-\frac{a}{bpq}} (fg - eh)^2 \sqrt{\pi} (e + fx) (c (d (e + fx)^p)^q)^{-\frac{1}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{\sqrt{b} f^3 \sqrt{p} \sqrt{q}} +$$

$$\frac{e^{-\frac{2a}{bpq}} h (fg - eh) \sqrt{2\pi} (e + fx)^2 (c (d (e + fx)^p)^q)^{-\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{\sqrt{b} f^3 \sqrt{p} \sqrt{q}} +$$

$$\frac{e^{-\frac{3a}{bpq}} h^2 \sqrt{\frac{\pi}{3}} (e + fx)^3 (c (d (e + fx)^p)^q)^{-\frac{3}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{\sqrt{b} f^3 \sqrt{p} \sqrt{q}}$$

Result (type 4, 843 leaves):

$$\frac{1}{3 \sqrt{b} f^3 \sqrt{p} \sqrt{q} \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}} e^{-\frac{3a}{bpq}} \sqrt{\pi} (e + fx) (c (d (e + fx)^p)^q)^{-\frac{3}{pq}}$$

$$\left(3 e^{\frac{2a}{bpq}} fg (fg - 2eh) (c (d (e + fx)^p)^q)^{\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]} + \right.$$

$$\left. h \left(3 \sqrt{2} e^{\frac{a}{bpq}} fg (e + fx) (c (d (e + fx)^p)^q)^{\frac{1}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c (d (e + fx)^p)^q]} + \right.$$

$$\left. \sqrt{b} h \sqrt{p} \sqrt{q} \left(\sqrt{3} e^2 + 2 \sqrt{3} e f x + \sqrt{3} f^2 x^2 - 3 \sqrt{2} e^2 e^{\frac{a}{bpq}} (c (d (e + fx)^p)^q)^{\frac{1}{pq}} - 3 \sqrt{2} e e^{\frac{a}{bpq}} f x (c (d (e + fx)^p)^q)^{\frac{1}{pq}} + \right. \right.$$

$$\left. 3 e^2 e^{\frac{2a}{bpq}} (c (d (e + fx)^p)^q)^{\frac{2}{pq}} - 3 e^2 e^{\frac{2a}{bpq}} (c (d (e + fx)^p)^q)^{\frac{2}{pq}} \operatorname{Erf}\left[\sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}}\right] + 3 \sqrt{2} e e^{\frac{a}{bpq}} (e + fx) \right.$$

$$\left. (c (d (e + fx)^p)^q)^{\frac{1}{pq}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}}\right] - \sqrt{3} e^2 \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}}\right] - 2 \sqrt{3} e f x \right.$$

$$\left. \left. \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}}\right] - \sqrt{3} f^2 x^2 \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}}\right] \right) \sqrt{-\frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{bpq}} \right)$$

Problem 474: Result more than twice size of optimal antiderivative.

$$\int \frac{(g + hx)^2}{(a + b \operatorname{Log}[c(d + fx)^p])^{3/2}} dx$$

Optimal (type 4, 404 leaves, 26 steps):

$$\frac{2 e^{-\frac{a}{bpq}} (fg - eh)^2 \sqrt{\pi} (e + fx) (c(d + fx)^p)^{-\frac{1}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{b^{3/2} f^3 p^{3/2} q^{3/2}} +$$

$$\frac{4 e^{-\frac{2a}{bpq}} h (fg - eh) \sqrt{2\pi} (e + fx)^2 (c(d + fx)^p)^{-\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{b^{3/2} f^3 p^{3/2} q^{3/2}} +$$

$$\frac{2 e^{-\frac{3a}{bpq}} h^2 \sqrt{3\pi} (e + fx)^3 (c(d + fx)^p)^{-\frac{3}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{b^{3/2} f^3 p^{3/2} q^{3/2}} - \frac{2 (e + fx) (g + hx)^2}{b f p q \sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}$$

Result (type 4, 1680 leaves):

$$\frac{1}{b^{3/2} f^3 p^{3/2} q^{3/2} \sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}$$

$$2 e^{-\frac{3a}{bpq}} (c(d + fx)^p)^{-\frac{3}{pq}} \left(-\sqrt{b} e^{\frac{3a}{bpq}} f^2 g^2 \sqrt{p} \sqrt{q} (c(d + fx)^p)^{\frac{3}{pq}} - \sqrt{b} e^{\frac{3a}{bpq}} f^3 g^2 \sqrt{p} \sqrt{q} x (c(d + fx)^p)^{\frac{3}{pq}} - \right.$$

$$2 \sqrt{b} e^{\frac{3a}{bpq}} f^2 g h \sqrt{p} \sqrt{q} x (c(d + fx)^p)^{\frac{3}{pq}} - 2 \sqrt{b} e^{\frac{3a}{bpq}} f^3 g h \sqrt{p} \sqrt{q} x^2 (c(d + fx)^p)^{\frac{3}{pq}} -$$

$$\left. \sqrt{b} e^{\frac{3a}{bpq}} f^2 h^2 \sqrt{p} \sqrt{q} x^2 (c(d + fx)^p)^{\frac{3}{pq}} - \sqrt{b} e^{\frac{3a}{bpq}} f^3 h^2 \sqrt{p} \sqrt{q} x^3 (c(d + fx)^p)^{\frac{3}{pq}} + \right.$$

$$\left. e^{\frac{2a}{bpq}} f^2 g^2 \sqrt{\pi} (e + fx) (c(d + fx)^p)^{\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c(d + fx)^p]} - \right.$$

$$2 e e^{\frac{2a}{bpq}} f g h \sqrt{\pi} (e + fx) (c(d + fx)^p)^{\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c(d + fx)^p]} -$$

$$2 e^2 e^{\frac{2a}{bpq}} h^2 \sqrt{\pi} (e + fx) (c(d + fx)^p)^{\frac{2}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c(d + fx)^p]} +$$

$$\left. 2 e^{\frac{a}{bpq}} f g h \sqrt{2\pi} (e + fx)^2 (c(d + fx)^p)^{\frac{1}{pq}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c(d + fx)^p]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a + b \operatorname{Log}[c(d + fx)^p]} + \right.$$

$$\begin{aligned}
& e e^{\frac{a}{b p q}} h^2 \sqrt{2 \pi} (e+f x)^2 (c(d(e+f x)^p)^q)^{\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right] \sqrt{a+b \operatorname{Log}[c(d(e+f x)^p)^q]} + \\
& \sqrt{b} h^2 \sqrt{p} \sqrt{3 \pi} \sqrt{q} (e+f x)^3 \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}} - 3 \sqrt{b} e e^{\frac{a}{b p q}} h^2 \sqrt{p} \sqrt{2 \pi} \sqrt{q} (e+f x)^2 (c(d(e+f x)^p)^q)^{\frac{1}{p q}} \\
& \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}} + 3 \sqrt{b} e^2 e^{\frac{2 a}{b p q}} h^2 \sqrt{p} \sqrt{\pi} \sqrt{q} (e+f x) (c(d(e+f x)^p)^q)^{\frac{2}{p q}} \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}} - \\
& 3 \sqrt{b} e^2 e^{\frac{2 a}{b p q}} h^2 \sqrt{p} \sqrt{\pi} \sqrt{q} (e+f x) (c(d(e+f x)^p)^q)^{\frac{2}{p q}} \operatorname{Erf}\left[\sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}} + \\
& 3 \sqrt{b} e e^{\frac{a}{b p q}} h^2 \sqrt{p} \sqrt{2 \pi} \sqrt{q} (e+f x)^2 (c(d(e+f x)^p)^q)^{\frac{1}{p q}} \operatorname{Erf}\left[\sqrt{2} \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}} - \\
& \left. \sqrt{b} h^2 \sqrt{p} \sqrt{3 \pi} \sqrt{q} (e+f x)^3 \operatorname{Erf}\left[\sqrt{3} \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}}\right] \sqrt{-\frac{a+b \operatorname{Log}[c(d(e+f x)^p)^q]}{b p q}}\right)
\end{aligned}$$

Problem 478: Result more than twice size of optimal antiderivative.

$$\int \frac{(g+hx)^2}{(a+b \operatorname{Log}[c(d(e+fx)^p)^q])^{5/2}} dx$$

Optimal (type 4, 514 leaves, 42 steps):

$$\begin{aligned}
& \frac{4 e^{-\frac{a}{b p q}} (f g - e h)^2 \sqrt{\pi} (e + f x) (c (d (e + f x)^p)^q)^{-\frac{1}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{3 b^{5/2} f^3 p^{5/2} q^{5/2}} + \\
& \frac{16 e^{-\frac{2a}{b p q}} h (f g - e h) \sqrt{2 \pi} (e + f x)^2 (c (d (e + f x)^p)^q)^{-\frac{2}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{2} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{3 b^{5/2} f^3 p^{5/2} q^{5/2}} + \\
& \frac{4 e^{-\frac{3a}{b p q}} h^2 \sqrt{3 \pi} (e + f x)^3 (c (d (e + f x)^p)^q)^{-\frac{3}{p q}} \operatorname{Erfi}\left[\frac{\sqrt{3} \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}{\sqrt{b} \sqrt{p} \sqrt{q}}\right]}{b^{5/2} f^3 p^{5/2} q^{5/2}} - \frac{2 (e + f x) (g + h x)^2}{3 b f p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^{3/2}} + \\
& \frac{8 (f g - e h) (e + f x) (g + h x)}{3 b^2 f^2 p^2 q^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}} - \frac{4 (e + f x) (g + h x)^2}{b^2 f p^2 q^2 \sqrt{a + b \operatorname{Log}[c (d (e + f x)^p)^q]}}
\end{aligned}$$

Result (type 4, 6490 leaves):

$$\left(4 e^{-\frac{a + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log}[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right)}\right)}{b p q} \right)$$

$$\begin{aligned}
& g^2 \sqrt{\pi} \operatorname{Erfi}\left[\frac{1}{\sqrt{b} \sqrt{p} \sqrt{q}} \left(\sqrt{\left(a + b \left(p q \operatorname{Log}[e + f x] - \operatorname{Log}[d (e + f x)^p] \right) \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) \right)} \right) + \right. \\
& \left. \operatorname{Log}[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right]} \right] \\
& \sqrt{\left(a + b \left(p q \operatorname{Log}[e + f x] - \operatorname{Log}[d (e + f x)^p] \right) \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) \right) +} \\
& \left. \operatorname{Log}[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right]} \right) \Big/ \\
& \left(3 b^{5/2} f p^{5/2} q^{5/2} \sqrt{\left(a + b p q \operatorname{Log}[e + f x] + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \right. \right. \right. \\
& \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log}[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right]} \right) \right) \Big/ +
\end{aligned}$$

$$\left(\frac{a-bq(-p\log[ex]+Log[d(ex)^p])+b\left(-q(-p\log[ex]+Log[d(ex)^p])-\log[d(ex)^p]\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)+Log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right)}{bpq} \right) gh\sqrt{\pi}$$

$$\operatorname{Erfi}\left[\frac{1}{\sqrt{b}\sqrt{p}\sqrt{q}}\left(\sqrt{\left(a+b\left(pq\log[ex]-\log[d(ex)^p]\right)\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)\right)}+\right.$$

$$\left.\left.\left.\left.\log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right]\right)\right)\right]}$$

$$\sqrt{\left(a+b\left(pq\log[ex]-\log[d(ex)^p]\right)\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)\right)}+$$

$$\left.\left.\left.\left.\log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right]\right)\right)\right]}$$

$$\left(b^{5/2}f^2p^{5/2}q^{5/2}\sqrt{\left(a+bpq\log[ex]+bq(-p\log[ex]+Log[d(ex)^p])\right)+b\left(-q(-p\log[ex]+Log[d(ex)^p])\right)}-\right.$$

$$\left.\left.\left.\left.\log[d(ex)^p]\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)\right)+\log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right]\right)\right)}+$$

$$\left(\frac{a-bq(-p\log[ex]+Log[d(ex)^p])+b\left(-q(-p\log[ex]+Log[d(ex)^p])-\log[d(ex)^p]\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)+Log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right)}{bpq} \right) h^2\sqrt{\pi}$$

$$\operatorname{Erfi}\left[\frac{1}{\sqrt{b}\sqrt{p}\sqrt{q}}\left(\sqrt{\left(a+b\left(pq\log[ex]-\log[d(ex)^p]\right)\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)\right)}+\right.$$

$$\left.\left.\left.\left.\log[ce^q(-p\log[ex]+Log[d(ex)^p])](d(ex)^p)^{q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}}\right]\right)\right)\right]}$$

$$\sqrt{\left(a+b\left(pq\log[ex]-\log[d(ex)^p]\right)\left(q-\frac{q(-p\log[ex]+Log[d(ex)^p])}{Log[d(ex)^p]}\right)\right)}+$$

$$\begin{aligned}
& \sqrt{3} \operatorname{Erf}[\sqrt{3}] \sqrt{\left(-\frac{1}{b p q} \left(a + b \left(p q \operatorname{Log}[e + f x] - \operatorname{Log}[d (e + f x)^p]\right) \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \right.} \\
& \quad \left. \left. \left. \left. \left. \left. \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) \right) \right) \right)} \\
& \sqrt{\left(-\frac{1}{b p q} \left(a + b \left(p q \operatorname{Log}[e + f x] - \operatorname{Log}[d (e + f x)^p]\right) \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \right.} \\
& \quad \left. \left. \left. \left. \left. \left. \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) \right) \right) \right)} \\
& \left(b^2 f^3 p^2 q^2 \sqrt{\left(a + b p q \operatorname{Log}[e + f x] + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \right. \right.} \\
& \quad \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) + \\
& \sqrt{\left(a + b p q \operatorname{Log}[e + f x] + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \right. \right.} \\
& \quad \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) \\
& \left(-\left(\left(2 (e + f x) (g + h x)^2\right) / \left(3 b f p q \left(a + b p q \operatorname{Log}[e + f x] + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + \right. \right. \right. \right. \\
& \quad \left. \left. \left. b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left. \left. \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) \right) \right) \right) - (4 (e + f x) (g + h x) (f g + 2 e h + 3 f h x)) / \\
& \left(3 b^2 f^2 p^2 q^2 \left(a + b p q \operatorname{Log}[e + f x] + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \operatorname{Log}[d (e + f x)^p] \right. \right. \right. \\
& \quad \left. \left. \left. \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}\right) + \operatorname{Log}\left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}\right] (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}}\right] \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 489: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (g + h x)^{3/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 dx$$

Optimal (type 4, 635 leaves, 29 steps):

$$\begin{aligned} & \frac{368 b^2 (f g - e h)^2 p^2 q^2 \sqrt{g + h x}}{75 f^2 h} + \frac{128 b^2 (f g - e h) p^2 q^2 (g + h x)^{3/2}}{225 f h} + \frac{16 b^2 p^2 q^2 (g + h x)^{5/2}}{125 h} - \frac{368 b^2 (f g - e h)^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]}{75 f^{5/2} h} \\ & - \frac{8 b^2 (f g - e h)^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]^2}{5 f^{5/2} h} - \frac{8 b (f g - e h)^2 p q \sqrt{g + h x} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{5 f^2 h} \\ & - \frac{8 b (f g - e h) p q (g + h x)^{3/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{15 f h} - \frac{8 b p q (g + h x)^{5/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{25 h} + \\ & \frac{8 b (f g - e h)^{5/2} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{5 f^{5/2} h} + \frac{2 (g + h x)^{5/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{5 h} \\ & - \frac{16 b^2 (f g - e h)^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{5 f^{5/2} h} + \frac{8 b^2 (f g - e h)^{5/2} p^2 q^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{5 f^{5/2} h} \end{aligned}$$

Result (type 5, 2450 leaves):

$$\begin{aligned} & \frac{1}{3 f h \sqrt{1 + \frac{h (e + f x)}{f g - e h}}} 2 b^2 g p^2 q^2 \sqrt{\frac{f g - e h + h (e + f x)}{f}} \left(3 h (e + f x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h (e + f x)}{-f g + e h}\right] - \right. \\ & \left. 3 h (e + f x) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{h (e + f x)}{-f g + e h}\right] \operatorname{Log}[e + f x] - f g \operatorname{Log}[e + f x]^2 + e h \operatorname{Log}[e + f x]^2 + \right. \\ & \left. f g \sqrt{1 + \frac{h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x]^2 - e h \sqrt{1 + \frac{h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x]^2 + h (e + f x) \sqrt{1 + \frac{h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x]^2 \right) - \end{aligned}$$

$$\begin{aligned}
& \frac{1}{15 f^2 h \sqrt{1 + \frac{h(e+fx)}{fg-eh}}} 2 b^2 p^2 q^2 \sqrt{\frac{fg-eh+h(e+fx)}{f}} \left(10 f g h (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] - \right. \\
& 10 e h^2 (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] + \\
& 15 e h^2 (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] - 4 f^2 g^2 \operatorname{Log}[e+fx] + 8 e f g h \operatorname{Log}[e+fx] - \\
& 4 e^2 h^2 \operatorname{Log}[e+fx] + 4 f^2 g^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] - 8 e f g h \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] + \\
& 4 e^2 h^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] + 8 f g h (e+fx) \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] - \\
& 8 e h^2 (e+fx) \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] + 4 h^2 (e+fx)^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx] - \\
& 15 e h^2 (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] \operatorname{Log}[e+fx] - 2 f^2 g^2 \operatorname{Log}[e+fx]^2 - e f g h \operatorname{Log}[e+fx]^2 + \\
& 3 e^2 h^2 \operatorname{Log}[e+fx]^2 + 2 f^2 g^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 + e f g h \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 - \\
& 3 e^2 h^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 - f g h (e+fx) \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 + \\
& 6 e h^2 (e+fx) \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 - 3 h^2 (e+fx)^2 \sqrt{\frac{fg-eh+h(e+fx)}{fg-eh}} \operatorname{Log}[e+fx]^2 + \\
& \left. 10 h (-fg+eh) (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{2}, 1, 1\right\}, \{2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] (1 + \operatorname{Log}[e+fx]) \right) + \frac{1}{9 f h}
\end{aligned}$$

$$\begin{aligned}
& 4 b g p q \left(\frac{6 (f g - e h)^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}} \right]}{\sqrt{f}} - \sqrt{\frac{f g - e h + h (e + f x)}{f}} (h (e + f x) (2 - 3 \operatorname{Log}[e + f x]) + (f g - e h) (8 - 3 \operatorname{Log}[e + f x])) \right) \\
& \left(a + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \right. \right. \\
& \quad \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log} \left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}} \right] \right) \right) - \\
& \frac{1}{225 f^{5/2} h} 4 b p q \left(30 (f g - e h)^{3/2} (2 f g + 3 e h) \operatorname{ArcTanh} \left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}} \right] + \sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} \right. \\
& \quad \left(9 h^2 (e + f x)^2 (2 - 5 \operatorname{Log}[e + f x]) + (f g - e h) (3 e h (-46 + 15 \operatorname{Log}[e + f x]) + 2 f g (-31 + 15 \operatorname{Log}[e + f x])) + \right. \\
& \quad \left. \left. h (e + f x) (f g (16 - 15 \operatorname{Log}[e + f x]) + 6 e h (-11 + 15 \operatorname{Log}[e + f x])) \right) \right) \\
& \left(a + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \right. \right. \\
& \quad \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log} \left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}} \right] \right) \right) + \\
& \sqrt{g + h x} \left(\frac{1}{5 h} 2 g^2 \left(a + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \operatorname{Log}[d (e + f x)^p] \right. \right. \right. \\
& \quad \left. \left. \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log} \left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}} \right] \right) \right)^2 + \\
& \frac{4}{5} g x \left(a + b q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) + b \left(-q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p]) - \operatorname{Log}[d (e + f x)^p] \right. \right. \\
& \quad \left. \left. \left(q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log} \left[c e^{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])} (d (e + f x)^p)^{q - \frac{q (-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p])}{\operatorname{Log}[d (e + f x)^p]}} \right] \right) \right)^2 +
\end{aligned}$$

$$\frac{2}{5} h x^2 \left(a + b q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) + b \left(-q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) - \operatorname{Log}[d (e + f x)^p] \right) \right. \\ \left. \left(q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log}\left[c e^{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)} (d (e + f x)^p)^{q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]}} \right] \right)^2 \right)$$

Problem 490: Result unnecessarily involves higher level functions.

$$\int \sqrt{g + h x} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 dx$$

Optimal (type 4, 547 leaves, 22 steps):

$$\frac{64 b^2 (f g - e h) p^2 q^2 \sqrt{g + h x}}{9 f h} + \frac{16 b^2 p^2 q^2 (g + h x)^{3/2}}{27 h} - \frac{64 b^2 (f g - e h)^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]}{9 f^{3/2} h} - \frac{8 b^2 (f g - e h)^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]^2}{3 f^{3/2} h} \\ - \frac{8 b (f g - e h) p q \sqrt{g + h x} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{3 f h} - \frac{8 b p q (g + h x)^{3/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{9 h} + \\ \frac{8 b (f g - e h)^{3/2} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{3 f^{3/2} h} + \frac{2 (g + h x)^{3/2} (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{3 h} + \\ \frac{16 b^2 (f g - e h)^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{3 f^{3/2} h} + \frac{8 b^2 (f g - e h)^{3/2} p^2 q^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{3 f^{3/2} h}$$

Result (type 5, 365 leaves):

$$\frac{1}{9 h} \left(\frac{1}{f \sqrt{\frac{f(g+hx)}{fg-eh}}} \right.$$

$$3 b^2 p^2 q^2 \sqrt{g+hx} \left(3 h (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] + \operatorname{Log}[e+fx] \left(-3 h (e+fx) \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] + \left(e h + f h x \sqrt{\frac{f(g+hx)}{fg-eh}} + f g \left(-1 + \sqrt{\frac{f(g+hx)}{fg-eh}} \right) \right) \operatorname{Log}[e+fx] \right) \right) -$$

$$\frac{1}{f^{3/2}} 2 b p q \left(6 (fg-eh)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] + \sqrt{f} \sqrt{g+hx} (6 e h - 2 f (4 g + h x) + 3 f (g + h x) \operatorname{Log}[e + f x]) \right)$$

$$\left. \left(-a + b p q \operatorname{Log}[e + f x] - b \operatorname{Log}[c (d (e + f x)^p)^q] \right) + 3 (g + h x)^{3/2} \left(a - b p q \operatorname{Log}[e + f x] + b \operatorname{Log}[c (d (e + f x)^p)^q] \right)^2 \right)$$

Problem 491: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{\sqrt{g + h x}} dx$$

Optimal (type 4, 447 leaves, 16 steps):

$$\begin{aligned}
& \frac{16 b^2 p^2 q^2 \sqrt{g+hx}}{h} - \frac{16 b^2 \sqrt{fg-eh} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right]}{\sqrt{f} h} - \\
& \frac{8 b^2 \sqrt{fg-eh} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right]^2}{\sqrt{f} h} - \frac{8 b p q \sqrt{g+hx} (a+b \operatorname{Log}[c(d(e+fx)^p)^q])}{h} + \\
& \frac{8 b \sqrt{fg-eh} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] (a+b \operatorname{Log}[c(d(e+fx)^p)^q])}{\sqrt{f} h} + \frac{2 \sqrt{g+hx} (a+b \operatorname{Log}[c(d(e+fx)^p)^q])^2}{h} + \\
& \frac{16 b^2 \sqrt{fg-eh} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{\sqrt{f} h} + \frac{8 b^2 \sqrt{fg-eh} p^2 q^2 \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{\sqrt{f} h}
\end{aligned}$$

Result (type 5, 646 leaves):

$$\begin{aligned}
& \frac{1}{f h \sqrt{g+hx}} 2 \left(a^2 f g - 4 a b f g p q + a^2 f h x - 4 a b f h p q x + 4 a b \sqrt{f} \sqrt{fg-eh} p q \sqrt{g+hx} \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] + \right. \\
& b^2 h p^2 q^2 (e+fx) \sqrt{\frac{f(g+hx)}{fg-eh}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, 1, 1, 1\right\}, \{2, 2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] + 4 b^2 f g p^2 q^2 \operatorname{Log}[e+fx] + \\
& 4 b^2 f h p^2 q^2 x \operatorname{Log}[e+fx] - 4 b^2 \sqrt{f} \sqrt{fg-eh} p^2 q^2 \sqrt{g+hx} \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] \operatorname{Log}[e+fx] - \\
& b^2 h p^2 q^2 (e+fx) \sqrt{\frac{f(g+hx)}{fg-eh}} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{2}, 1, 1\right\}, \{2, 2\}, \frac{h(e+fx)}{-fg+eh}\right] \operatorname{Log}[e+fx] - \\
& b^2 f g p^2 q^2 \sqrt{\frac{f(g+hx)}{fg-eh}} \operatorname{Log}[e+fx]^2 + b^2 e h p^2 q^2 \sqrt{\frac{f(g+hx)}{fg-eh}} \operatorname{Log}[e+fx]^2 + 2 a b f g \operatorname{Log}[c(d(e+fx)^p)^q] - \\
& 4 b^2 f g p q \operatorname{Log}[c(d(e+fx)^p)^q] + 2 a b f h x \operatorname{Log}[c(d(e+fx)^p)^q] - 4 b^2 f h p q x \operatorname{Log}[c(d(e+fx)^p)^q] + \\
& \left. 4 b^2 \sqrt{f} \sqrt{fg-eh} p q \sqrt{g+hx} \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] \operatorname{Log}[c(d(e+fx)^p)^q] + b^2 f g \operatorname{Log}[c(d(e+fx)^p)^q]^2 + b^2 f h x \operatorname{Log}[c(d(e+fx)^p)^q]^2 \right)
\end{aligned}$$

Problem 492: Result unnecessarily involves higher level functions.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{(g + h x)^{3/2}} dx$$

Optimal (type 4, 330 leaves, 11 steps):

$$\frac{8 b^2 \sqrt{f} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right]^2}{h \sqrt{fg-eh}} - \frac{8 b \sqrt{f} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{h \sqrt{fg-eh}} - \frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{h \sqrt{g+hx}} - \frac{16 b^2 \sqrt{f} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{h \sqrt{fg-eh}} - \frac{8 b^2 \sqrt{f} p^2 q^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{h \sqrt{fg-eh}}$$

Result (type 5, 356 leaves):

$$\frac{1}{h} \left(\frac{1}{\sqrt{fg-eh} (g+hx)} - 2 b p q \left(2 \sqrt{f} (g+hx) \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] + \sqrt{fg-eh} \sqrt{g+hx} \operatorname{Log}[e + f x] \right) \right. \\ \left. (-a + b p q \operatorname{Log}[e + f x] - b \operatorname{Log}[c (d (e + f x)^p)^q]) - \frac{(a - b p q \operatorname{Log}[e + f x] + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{\sqrt{g+hx}} + \right. \\ \left. \frac{1}{(fg-eh) \sqrt{g+hx}} b^2 p^2 q^2 \left(h (e + f x) \sqrt{\frac{f (g+hx)}{fg-eh}} \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{3}{2}\right\}, \left\{2, 2, 2\right\}, \frac{h (e + f x)}{-fg+eh}\right] + \right. \right. \\ \left. \left. (fg-eh) \operatorname{Log}[e + f x] \left(\left(-1 + \sqrt{\frac{f (g+hx)}{fg-eh}} \right) \operatorname{Log}[e + f x] - 4 \sqrt{\frac{f (g+hx)}{fg-eh}} \operatorname{Log}\left[\frac{1}{2} \left(1 + \sqrt{\frac{f (g+hx)}{fg-eh}} \right) \right] \right) \right) \right)$$

Problem 493: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{(g + h x)^{5/2}} dx$$

Optimal (type 4, 449 leaves, 15 steps):

$$\frac{16 b^2 f^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right]}{3 h (fg-eh)^{3/2}} + \frac{8 b^2 f^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right]^2}{3 h (fg-eh)^{3/2}} + \frac{8 b f p q (a+b \operatorname{Log}[c (d (e+fx)^p)^q])}{3 h (fg-eh) \sqrt{g+hx}} -$$

$$\frac{8 b f^{3/2} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] (a+b \operatorname{Log}[c (d (e+fx)^p)^q])}{3 h (fg-eh)^{3/2}} - \frac{2 (a+b \operatorname{Log}[c (d (e+fx)^p)^q])^2}{3 h (g+hx)^{3/2}} -$$

$$\frac{16 b^2 f^{3/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}\right] \operatorname{Log}\left[\frac{2}{1-\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{3 h (fg-eh)^{3/2}} - \frac{8 b^2 f^{3/2} p^2 q^2 \operatorname{PolyLog}\left[2, 1-\frac{2}{1-\frac{\sqrt{f} \sqrt{g+hx}}{\sqrt{fg-eh}}}\right]}{3 h (fg-eh)^{3/2}}$$

Result (type 5, 1311 leaves):

$$\frac{4 a b f^{3/2} p q \left(-\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}}}{\sqrt{fg-eh}}\right]}{(fg-eh)^{3/2}} + \frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}} (2h(e+fx) - fg(-2 + \operatorname{Log}[e+fx]) + eh(-2 + \operatorname{Log}[e+fx]))}{(fg-eh)(fg+fhx)^2} \right)}{3 h} + \frac{1}{3 h}$$

$$4 b^2 f^{3/2} p q^2 \left(-\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}}}{\sqrt{fg-eh}}\right]}{(fg-eh)^{3/2}} + \frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}} (2h(e+fx) - fg(-2 + \operatorname{Log}[e+fx]) + eh(-2 + \operatorname{Log}[e+fx]))}{(fg-eh)(fg+fhx)^2} \right)$$

$$(-p \operatorname{Log}[e+fx] + \operatorname{Log}[d(e+fx)^p]) + \frac{1}{3 h}$$

$$4 b^2 f^{3/2} p q \left(-\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}}}{\sqrt{fg-eh}}\right]}{(fg-eh)^{3/2}} + \frac{\sqrt{f} \sqrt{\frac{fg-eh+e+fx}{f}} (2h(e+fx) - fg(-2 + \operatorname{Log}[e+fx]) + eh(-2 + \operatorname{Log}[e+fx]))}{(fg-eh)(fg+fhx)^2} \right)$$

$$\left(-q(-p \operatorname{Log}[e+fx] + \operatorname{Log}[d(e+fx)^p]) - \operatorname{Log}[d(e+fx)^p] \left(q - \frac{q(-p \operatorname{Log}[e+fx] + \operatorname{Log}[d(e+fx)^p])}{\operatorname{Log}[d(e+fx)^p]} \right) + \right.$$

$$\left. \operatorname{Log}\left[c e^{q(-p \operatorname{Log}[e+fx] + \operatorname{Log}[d(e+fx)^p])} (d(e+fx)^p)^{q - \frac{q(-p \operatorname{Log}[e+fx] + \operatorname{Log}[d(e+fx)^p])}{\operatorname{Log}[d(e+fx)^p]}} \right] - \right.$$

$$\frac{1}{3 h (g + h x)^{3/2}} 2 \left(a + b q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) + b \left(-q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) - \right. \right. \\ \left. \left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log}\left[c e^{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)} (d (e + f x)^p)^{q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]}} \right] \right) \right)^2 + \\ \frac{1}{3 h (f g - e h)^2 (f g + f h x) \sqrt{\frac{f g - e h + h (e + f x)}{f}}} 2 b^2 f p^2 q^2 \left(3 h (e + f x) (f g + f h x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right. \\ \operatorname{HypergeometricPFQ}\left[\left\{1, 1, 1, \frac{5}{2}\right\}, \{2, 2, 2\}, \frac{h (e + f x)}{-f g + e h}\right] + (f g - e h) \operatorname{Log}[e + f x] \\ \left(4 f g - 4 e h + 4 h (e + f x) - 4 f g \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + 4 e h \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} - 4 h (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} - \right. \\ \left. f g \operatorname{Log}[e + f x] + e h \operatorname{Log}[e + f x] + f g \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x] - e h \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x] + \right. \\ \left. h (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{Log}[e + f x] - 4 (f g - e h) \left(\frac{f g - e h + h (e + f x)}{f g - e h} \right)^{3/2} \operatorname{Log}\left[\frac{1}{2} \left(1 + \sqrt{1 + \frac{h (e + f x)}{f g - e h}} \right) \right] \right) \right)$$

Problem 494: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{(g + h x)^{7/2}} dx$$

Optimal (type 4, 537 leaves, 20 steps):

$$\begin{aligned}
& - \frac{16 b^2 f^2 p^2 q^2}{15 h (f g - e h)^2 \sqrt{g + h x}} + \frac{64 b^2 f^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]}{15 h (f g - e h)^{5/2}} + \frac{8 b^2 f^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]^2}{5 h (f g - e h)^{5/2}} + \frac{8 b f p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{15 h (f g - e h) (g + h x)^{3/2}} \\
& - \frac{8 b f^2 p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{5 h (f g - e h)^2 \sqrt{g + h x}} - \frac{8 b f^{5/2} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{5 h (f g - e h)^{5/2}} \\
& - \frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{5 h (g + h x)^{5/2}} - \frac{16 b^2 f^{5/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{5 h (f g - e h)^{5/2}} - \frac{8 b^2 f^{5/2} p^2 q^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{5 h (f g - e h)^{5/2}}
\end{aligned}$$

Result (type 5, 1349 leaves):

$$\begin{aligned}
& \frac{1}{5 h (f g - e h)^3 (f g + f h x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f}}} \\
& 2 b^2 f^2 p^2 q^2 \left(5 h (e + f x) (f g + f h x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{HypergeometricPFQ}\left[\left\{\{1, 1, 1, \frac{7}{2}\}, \{2, 2, 2\}, \frac{h (e + f x)}{-f g + e h}\right\}\right] - \right. \\
& 5 h (e + f x) (f g + f h x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{HypergeometricPFQ}\left[\left\{\{1, 1, \frac{7}{2}\}, \{2, 2\}, \frac{h (e + f x)}{-f g + e h}\right\}\right] \operatorname{Log}[e + f x] + \\
& (f g - e h) \left(f^2 g^2 \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) - 2 f g h \left(-(e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + e \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) \right) \right) + \\
& h^2 \left(-2 e (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + (e + f x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + e^2 \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) \right) \operatorname{Log}[e + f x]^2 \left. \right) + \frac{1}{15 h} \\
& 4 a b f^{5/2} p q \left(- \frac{6 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{5/2}} + \frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} (2 (f g - e h) (f g + f h x) + 6 (f g + f h x)^2 - 3 (f g - e h)^2 \operatorname{Log}[e + f x])}{(f g - e h)^2 (f g + f h x)^3} \right) +
\end{aligned}$$

$$\frac{1}{15 h}$$

$$4 b^2 f^{5/2} p q^2 \left(-\frac{6 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{5/2}} + \frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} \left(2 (f g - e h) (f g + f h x) + 6 (f g + f h x)^2 - 3 (f g - e h)^2 \operatorname{Log}[e + f x]\right)}{(f g - e h)^2 (f g + f h x)^3} \right)$$

$$\left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) + \frac{1}{15 h}$$

$$4 b^2 f^{5/2} p q \left(-\frac{6 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{5/2}} + \frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} \left(2 (f g - e h) (f g + f h x) + 6 (f g + f h x)^2 - 3 (f g - e h)^2 \operatorname{Log}[e + f x]\right)}{(f g - e h)^2 (f g + f h x)^3} \right)$$

$$\left(-q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) - \operatorname{Log}[d (e + f x)^p] \right) \left(q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]} \right) +$$

$$\operatorname{Log}\left[c e^{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)} \left(d (e + f x)^p \right)^{q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]}} \right] -$$

$$\frac{1}{5 h (g + h x)^{5/2}} 2 \left(a + b q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) + b \left(-q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right) - \right.$$

$$\left. \operatorname{Log}[d (e + f x)^p] \left(q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]} \right) + \operatorname{Log}\left[c e^{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)} \left(d (e + f x)^p \right)^{q - \frac{q \left(-p \operatorname{Log}[e + f x] + \operatorname{Log}[d (e + f x)^p] \right)}{\operatorname{Log}[d (e + f x)^p]}} \right] \right)^2$$

Problem 495: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{(g + h x)^{9/2}} dx$$

Optimal (type 4, 625 leaves, 26 steps):

$$\begin{aligned}
& - \frac{16 b^2 f^2 p^2 q^2}{105 h (f g - e h)^2 (g + h x)^{3/2}} - \frac{128 b^2 f^3 p^2 q^2}{105 h (f g - e h)^3 \sqrt{g + h x}} + \frac{368 b^2 f^{7/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]}{105 h (f g - e h)^{7/2}} + \\
& \frac{8 b^2 f^{7/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right]^2}{7 h (f g - e h)^{7/2}} + \frac{8 b f p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{35 h (f g - e h) (g + h x)^{5/2}} + \frac{8 b f^2 p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{21 h (f g - e h)^2 (g + h x)^{3/2}} + \\
& \frac{8 b f^3 p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{7 h (f g - e h)^3 \sqrt{g + h x}} - \frac{8 b f^{7/2} p q \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{7 h (f g - e h)^{7/2}} - \\
& \frac{2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{7 h (g + h x)^{7/2}} - \frac{16 b^2 f^{7/2} p^2 q^2 \operatorname{ArcTanh}\left[\frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{7 h (f g - e h)^{7/2}} - \frac{8 b^2 f^{7/2} p^2 q^2 \operatorname{PolyLog}\left[2, 1 - \frac{2}{1 - \frac{\sqrt{f} \sqrt{g + h x}}{\sqrt{f g - e h}}}\right]}{7 h (f g - e h)^{7/2}}
\end{aligned}$$

Result (type 5, 1582 leaves):

$$\begin{aligned}
& \frac{1}{7 h (f g - e h)^4 (f g + f h x)^3 \sqrt{\frac{f g - e h + h (e + f x)}{f}}} \\
& 2 b^2 f^3 p^2 q^2 \left(7 h (e + f x) (f g + f h x)^3 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{HypergeometricPFQ}\left[\left\{\{1, 1, 1, \frac{9}{2}\}, \{2, 2, 2\}, \frac{h (e + f x)}{-f g + e h}\right\}\right] - \right. \\
& \left. 7 h (e + f x) (f g + f h x)^3 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \operatorname{HypergeometricPFQ}\left[\left\{\{1, 1, \frac{9}{2}\}, \{2, 2\}, \frac{h (e + f x)}{-f g + e h}\right\}\right] \operatorname{Log}[e + f x] + \right. \\
& \left. (f g - e h) \left(f^3 g^3 \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) - 3 f^2 g^2 h \left(- (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + e \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) \right) \right) \right. \\
& \left. + 3 f g h^2 \left(-2 e (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + (e + f x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + e^2 \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) \right) \right. \\
& \left. + h^3 \left(3 e^2 (e + f x) \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} - 3 e (e + f x)^2 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left((e + f x)^3 \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} - e^3 \left(-1 + \sqrt{\frac{f g - e h + h (e + f x)}{f g - e h}} \right) \right) \right) \text{Log}[e + f x]^2 + \\
& \frac{1}{105 h} 4 a b f^{7/2} p q \left(- \frac{30 \text{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{7/2}} + \frac{1}{(f g - e h)^3 (f g + f h x)^4} \sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} \right. \\
& \left. \left(6 (f g - e h)^2 (f g + f h x) + 10 (f g - e h) (f g + f h x)^2 + 30 (f g + f h x)^3 - 15 (f g - e h)^3 \text{Log}[e + f x] \right) + \right. \\
& \left. \frac{1}{105 h} 4 b^2 f^{7/2} p q^2 \left(- \frac{30 \text{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{7/2}} + \frac{1}{(f g - e h)^3 (f g + f h x)^4} \right. \right. \\
& \left. \left. \sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}} \left(6 (f g - e h)^2 (f g + f h x) + 10 (f g - e h) (f g + f h x)^2 + 30 (f g + f h x)^3 - 15 (f g - e h)^3 \text{Log}[e + f x] \right) \right) \right. \\
& \left. \left(-p \text{Log}[e + f x] + \text{Log}[d (e + f x)^p] \right) + \frac{1}{105 h} 4 b^2 f^{7/2} p q \left(- \frac{30 \text{ArcTanh}\left[\frac{\sqrt{f} \sqrt{\frac{f g - e h + h (e + f x)}{f}}}{\sqrt{f g - e h}}\right]}{(f g - e h)^{7/2}} + \frac{1}{(f g - e h)^3 (f g + f h x)^4} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \sqrt{f} \sqrt{\frac{fg - eh + h(e + fx)}{f}} \left(6(fg - eh)^2 (fg + fhx) + 10(fg - eh)(fg + fhx)^2 + 30(fg + fhx)^3 - 15(fg - eh)^3 \text{Log}[e + fx] \right) \right) \\
& \left(-q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p]) - \text{Log}[d(e + fx)^p] \left(q - \frac{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])}{\text{Log}[d(e + fx)^p]} \right) \right) + \\
& \left. \text{Log}\left[c e^{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])} (d(e + fx)^p)^{q - \frac{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])}{\text{Log}[d(e + fx)^p]}} \right] \right) - \\
& \frac{1}{7h(g + hx)^{7/2}} 2 \left(a + bq(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p]) + b \left(-q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p]) - \right. \right. \\
& \left. \left. \text{Log}[d(e + fx)^p] \left(q - \frac{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])}{\text{Log}[d(e + fx)^p]} \right) \right) + \text{Log}\left[c e^{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])} (d(e + fx)^p)^{q - \frac{q(-p \text{Log}[e + fx] + \text{Log}[d(e + fx)^p])}{\text{Log}[d(e + fx)^p]}} \right] \right) \right)^2
\end{aligned}$$

Problem 518: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \text{Log}\left[c (d(e + fx)^p)^q \right]}{g + hx^2} dx$$

Optimal (type 4, 249 leaves, 9 steps):

$$\begin{aligned}
& \frac{(a + b \text{Log}\left[c (d(e + fx)^p)^q \right]) \text{Log}\left[\frac{f(\sqrt{-g} - \sqrt{h}x)}{f\sqrt{-g} + e\sqrt{h}} \right]}{2\sqrt{-g}\sqrt{h}} - \\
& \frac{(a + b \text{Log}\left[c (d(e + fx)^p)^q \right]) \text{Log}\left[\frac{f(\sqrt{-g} + \sqrt{h}x)}{f\sqrt{-g} - e\sqrt{h}} \right]}{2\sqrt{-g}\sqrt{h}} - \frac{bpq \text{PolyLog}\left[2, -\frac{\sqrt{h}(e+fx)}{f\sqrt{-g} - e\sqrt{h}} \right]}{2\sqrt{-g}\sqrt{h}} + \frac{bpq \text{PolyLog}\left[2, \frac{\sqrt{h}(e+fx)}{f\sqrt{-g} + e\sqrt{h}} \right]}{2\sqrt{-g}\sqrt{h}}
\end{aligned}$$

Result (type 4, 261 leaves):

$$\frac{1}{2\sqrt{g}\sqrt{h}}$$

$$\left(2a \operatorname{ArcTan}\left[\frac{\sqrt{h}x}{\sqrt{g}}\right] - 2bpq \operatorname{ArcTan}\left[\frac{\sqrt{h}x}{\sqrt{g}}\right] \operatorname{Log}[e+fx] + 2b \operatorname{ArcTan}\left[\frac{\sqrt{h}x}{\sqrt{g}}\right] \operatorname{Log}\left[c(d(e+fx)^p)^q\right] + i b p q \operatorname{Log}[e+fx] \operatorname{Log}\left[1 - \frac{\sqrt{h}(e+fx)}{-if\sqrt{g}+e\sqrt{h}}\right] - \right.$$

$$\left. i b p q \operatorname{Log}[e+fx] \operatorname{Log}\left[1 - \frac{\sqrt{h}(e+fx)}{if\sqrt{g}+e\sqrt{h}}\right] + i b p q \operatorname{PolyLog}\left[2, \frac{\sqrt{h}(e+fx)}{-if\sqrt{g}+e\sqrt{h}}\right] - i b p q \operatorname{PolyLog}\left[2, \frac{\sqrt{h}(e+fx)}{if\sqrt{g}+e\sqrt{h}}\right] \right)$$

Problem 519: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}\left[c(d(e+fx)^p)^q\right]}{\sqrt{2+hx^2}} dx$$

Optimal (type 4, 335 leaves, 11 steps):

$$\frac{bpq \operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right]^2}{2\sqrt{h}} - \frac{bpq \operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{\sqrt{2}e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right]}f}{e\sqrt{h}-\sqrt{2f^2+e^2h}}\right]}{\sqrt{h}} - \frac{bpq \operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{\sqrt{2}e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right]}f}{e\sqrt{h}+\sqrt{2f^2+e^2h}}\right]}{\sqrt{h}} +$$

$$\frac{\operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right] (a + b \operatorname{Log}\left[c(d(e+fx)^p)^q\right])}{\sqrt{h}} - \frac{bpq \operatorname{PolyLog}\left[2, -\frac{\sqrt{2}e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right]}f}{e\sqrt{h}-\sqrt{2f^2+e^2h}}\right]}{\sqrt{h}} - \frac{bpq \operatorname{PolyLog}\left[2, -\frac{\sqrt{2}e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h}x}{\sqrt{2}}\right]}f}{e\sqrt{h}+\sqrt{2f^2+e^2h}}\right]}{\sqrt{h}}$$

Result (type 1, 1 leaves):

???

Problem 520: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}\left[c(d(e+fx)^p)^q\right]}{\sqrt{g+hx^2}} dx$$

Optimal (type 4, 515 leaves, 12 steps):

$$\begin{aligned}
& \frac{b \sqrt{g} p q \sqrt{1 + \frac{hx^2}{g}} \operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right]^2}{2 \sqrt{h} \sqrt{g + hx^2}} - \frac{b \sqrt{g} p q \sqrt{1 + \frac{hx^2}{g}} \operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right] \operatorname{Log}\left[1 + \frac{e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right]} f \sqrt{g}}{e \sqrt{h} - \sqrt{f^2 g + e^2 h}}\right]}{\sqrt{h} \sqrt{g + hx^2}} \\
& \frac{b \sqrt{g} p q \sqrt{1 + \frac{hx^2}{g}} \operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right] \operatorname{Log}\left[1 + \frac{e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right]} f \sqrt{g}}{e \sqrt{h} + \sqrt{f^2 g + e^2 h}}\right]}{\sqrt{h} \sqrt{g + hx^2}} + \frac{\sqrt{g} \sqrt{1 + \frac{hx^2}{g}} \operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right] (a + b \operatorname{Log}[c (d (e + fx)^p)^q])}{\sqrt{h} \sqrt{g + hx^2}} \\
& \frac{b \sqrt{g} p q \sqrt{1 + \frac{hx^2}{g}} \operatorname{PolyLog}\left[2, -\frac{e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right]} f \sqrt{g}}{e \sqrt{h} - \sqrt{f^2 g + e^2 h}}\right]}{\sqrt{h} \sqrt{g + hx^2}} - \frac{b \sqrt{g} p q \sqrt{1 + \frac{hx^2}{g}} \operatorname{PolyLog}\left[2, -\frac{e^{\operatorname{ArcSinh}\left[\frac{\sqrt{h} x}{\sqrt{g}}\right]} f \sqrt{g}}{e \sqrt{h} + \sqrt{f^2 g + e^2 h}}\right]}{\sqrt{h} \sqrt{g + hx^2}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 521: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{\sqrt{2 - hx} \sqrt{2 + hx}} dx$$

Optimal (type 4, 287 leaves, 10 steps):

$$\begin{aligned}
& \frac{i b p q \operatorname{ArcSin}\left[\frac{hx}{2}\right]^2}{2 h} - \frac{b p q \operatorname{ArcSin}\left[\frac{hx}{2}\right] \operatorname{Log}\left[1 + \frac{2 e^{i \operatorname{ArcSin}\left[\frac{hx}{2}\right]} f}{i e h - \sqrt{4 f^2 - e^2 h^2}}\right]}{h} - \frac{b p q \operatorname{ArcSin}\left[\frac{hx}{2}\right] \operatorname{Log}\left[1 + \frac{2 e^{i \operatorname{ArcSin}\left[\frac{hx}{2}\right]} f}{i e h + \sqrt{4 f^2 - e^2 h^2}}\right]}{h} + \\
& \frac{\operatorname{ArcSin}\left[\frac{hx}{2}\right] (a + b \operatorname{Log}[c (d (e + fx)^p)^q])}{h} + \frac{i b p q \operatorname{PolyLog}\left[2, -\frac{2 e^{i \operatorname{ArcSin}\left[\frac{hx}{2}\right]} f}{i e h - \sqrt{4 f^2 - e^2 h^2}}\right]}{h} + \frac{i b p q \operatorname{PolyLog}\left[2, -\frac{2 e^{i \operatorname{ArcSin}\left[\frac{hx}{2}\right]} f}{i e h + \sqrt{4 f^2 - e^2 h^2}}\right]}{h}
\end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 522: Attempted integration timed out after 120 seconds.

$$\int \frac{a + b \operatorname{Log}[c (d (e + fx)^p)^q]}{\sqrt{g - hx} \sqrt{g + hx}} dx$$

Optimal (type 4, 519 leaves, 12 steps):

$$\frac{i b g p q \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{ArcSin}\left[\frac{hx}{g}\right]^2}{2 h \sqrt{g - hx} \sqrt{g + hx}} - \frac{b g p q \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{ArcSin}\left[\frac{hx}{g}\right] \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}\left[\frac{hx}{g}\right]} f g}{i e h - \sqrt{f^2 g^2 - e^2 h^2}}\right]}{h \sqrt{g - hx} \sqrt{g + hx}} -$$

$$\frac{b g p q \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{ArcSin}\left[\frac{hx}{g}\right] \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}\left[\frac{hx}{g}\right]} f g}{i e h + \sqrt{f^2 g^2 - e^2 h^2}}\right]}{h \sqrt{g - hx} \sqrt{g + hx}} + \frac{g \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{ArcSin}\left[\frac{hx}{g}\right] (a + b \operatorname{Log}[c (d (e + fx)^p)^q])}{h \sqrt{g - hx} \sqrt{g + hx}} +$$

$$\frac{i b g p q \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}\left[\frac{hx}{g}\right]} f g}{i e h - \sqrt{f^2 g^2 - e^2 h^2}}\right]}{h \sqrt{g - hx} \sqrt{g + hx}} + \frac{i b g p q \sqrt{1 - \frac{h^2 x^2}{g^2}} \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}\left[\frac{hx}{g}\right]} f g}{i e h + \sqrt{f^2 g^2 - e^2 h^2}}\right]}{h \sqrt{g - hx} \sqrt{g + hx}}$$

Result (type 1, 1 leaves):

???

Problem 531: Result more than twice size of optimal antiderivative.

$$\int \frac{(i + j x) (a + b \operatorname{Log}[c (d (e + fx)^p)^q])^2}{g + hx} dx$$

Optimal (type 4, 240 leaves, 11 steps):

$$-\frac{2 a b j p q x}{h} + \frac{2 b^2 j p^2 q^2 x}{h} - \frac{2 b^2 j p q (e + fx) \operatorname{Log}[c (d (e + fx)^p)^q]}{f h} +$$

$$\frac{j (e + fx) (a + b \operatorname{Log}[c (d (e + fx)^p)^q])^2}{f h} + \frac{(h i - g j) (a + b \operatorname{Log}[c (d (e + fx)^p)^q])^2 \operatorname{Log}\left[\frac{f (g + hx)}{f g - e h}\right]}{h^2} +$$

$$\frac{2 b (h i - g j) p q (a + b \operatorname{Log}[c (d (e + fx)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{h (e + fx)}{f g - e h}\right]}{h^2} - \frac{2 b^2 (h i - g j) p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{h (e + fx)}{f g - e h}\right]}{h^2}$$

Result (type 4, 866 leaves):

$$\frac{1}{f h^2} \left(-2 a b e h j p q + 2 b^2 e h j p^2 q^2 + a^2 f h j x - 2 a b f h j p q x + 2 b^2 f h j p^2 q^2 x + 2 a b e h j p q \operatorname{Log}[e + f x] - b^2 e h j p^2 q^2 \operatorname{Log}[e + f x]^2 - \right. \\
2 b^2 e h j p q \operatorname{Log}[c (d (e + f x)^p)^q] + 2 a b f h j x \operatorname{Log}[c (d (e + f x)^p)^q] - 2 b^2 f h j p q x \operatorname{Log}[c (d (e + f x)^p)^q] + \\
2 b^2 e h j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] + b^2 f h j x \operatorname{Log}[c (d (e + f x)^p)^q]^2 + a^2 f h i \operatorname{Log}[g + h x] - a^2 f g j \operatorname{Log}[g + h x] - \\
2 a b f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 2 a b f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + b^2 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - \\
b^2 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] + 2 a b f h i \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 2 a b f g j \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - \\
2 b^2 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 2 b^2 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
b^2 f h i \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - b^2 f g j \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 2 a b f h i p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
2 a b f g j p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - b^2 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + b^2 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
2 b^2 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 2 b^2 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
\left. 2 b f (h i - g j) p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, \frac{h (e + f x)}{-f g + e h}\right] + 2 b^2 f (-h i + g j) p^2 q^2 \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] \right)$$

Problem 532: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{g + h x} dx$$

Optimal (type 4, 123 leaves, 5 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right]}{h} + \frac{2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{h (e + f x)}{f g - e h}\right]}{h} - \frac{2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{h (e + f x)}{f g - e h}\right]}{h}$$

Result (type 4, 324 leaves):

$$\frac{1}{h} \left(a^2 \operatorname{Log}[g + h x] - 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] + 2 a b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - \right. \\
2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
\left. 2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, \frac{h (e + f x)}{-f g + e h}\right] - 2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] \right)$$

Problem 533: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{(g + h x) (i + j x)} dx$$

Optimal (type 4, 288 leaves, 11 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{Log}\left[\frac{f(i+jx)}{fi-ej}\right]}{hi-gj} +$$

$$\frac{2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right] - 2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, -\frac{j(e+fx)}{fi-ej}\right]}{hi-gj} -$$

$$\frac{2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right] - 2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{j(e+fx)}{fi-ej}\right]}{hi-gj} + \frac{2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, -\frac{j(e+fx)}{fi-ej}\right]}{hi-gj}$$

Result (type 4, 652 leaves):

$$\frac{1}{hi-gj} \left(a^2 \operatorname{Log}[g + h x] - 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] + \right.$$

$$2 a b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] +$$

$$b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - a^2 \operatorname{Log}[i + j x] + 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}[i + j x] -$$

$$b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[i + j x] - 2 a b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[i + j x] + 2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[i + j x] -$$

$$b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[i + j x] - 2 a b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f(i+jx)}{fi-ej}\right] + b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f(i+jx)}{fi-ej}\right] -$$

$$2 b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(i+jx)}{fi-ej}\right] + 2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, \frac{h(e+fx)}{-fg+eh}\right] -$$

$$2 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[2, \frac{j(e+fx)}{-fi+ej}\right] - 2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{h(e+fx)}{-fg+eh}\right] + 2 b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{j(e+fx)}{-fi+ej}\right] \Big)$$

Problem 535: Result more than twice size of optimal antiderivative.

$$\int \frac{(i + j x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{g + h x} dx$$

Optimal (type 4, 742 leaves, 24 steps):

$$\begin{aligned}
& \frac{6 a b^2 j (f i - e j) p^2 q^2 x}{f h} + \frac{6 a b^2 j (h i - g j) p^2 q^2 x}{h^2} - \frac{6 b^3 j (f i - e j) p^3 q^3 x}{f h} - \\
& \frac{6 b^3 j (h i - g j) p^3 q^3 x}{h^2} - \frac{3 b^3 j^2 p^3 q^3 (e + f x)^2}{8 f^2 h} + \frac{6 b^3 j (f i - e j) p^2 q^2 (e + f x) \operatorname{Log}[c (d (e + f x)^p)^q]}{f^2 h} + \\
& \frac{6 b^3 j (h i - g j) p^2 q^2 (e + f x) \operatorname{Log}[c (d (e + f x)^p)^q]}{f h^2} + \frac{3 b^2 j^2 p^2 q^2 (e + f x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])}{4 f^2 h} - \\
& \frac{3 b j (f i - e j) p q (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{f^2 h} - \frac{3 b j (h i - g j) p q (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{f h^2} - \\
& \frac{3 b j^2 p q (e + f x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{4 f^2 h} + \frac{j (f i - e j) (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{f^2 h} + \\
& \frac{j (h i - g j) (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{f h^2} + \frac{j^2 (e + f x)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{2 f^2 h} + \\
& \frac{(h i - g j)^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right]}{h^3} + \frac{3 b (h i - g j)^2 p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h^3} - \\
& \frac{6 b^2 (h i - g j)^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h^3} + \frac{6 b^3 (h i - g j)^2 p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h^3}
\end{aligned}$$

Result (type 4, 4146 leaves):

$$\begin{aligned}
& \frac{1}{8 f^2 h^3} \left(-48 a^2 b e f h^2 i j p q + 24 a^2 b e f g h j^2 p q + 96 a b^2 e f h^2 i j p^2 q^2 - 48 a b^2 e f g h j^2 p^2 q^2 - 96 b^3 e f h^2 i j p^3 q^3 + 48 b^3 e f g h j^2 p^3 q^3 + \right. \\
& 16 a^3 f^2 h^2 i j x - 8 a^3 f^2 g h j^2 x - 48 a^2 b f^2 h^2 i j p q x + 24 a^2 b f^2 g h j^2 p q x + 12 a^2 b e f h^2 j^2 p q x + 96 a b^2 f^2 h^2 i j p^2 q^2 x - \\
& 48 a b^2 f^2 g h j^2 p^2 q^2 x - 36 a b^2 e f h^2 j^2 p^2 q^2 x - 96 b^3 f^2 h^2 i j p^3 q^3 x + 48 b^3 f^2 g h j^2 p^3 q^3 x + 42 b^3 e f h^2 j^2 p^3 q^3 x + 4 a^3 f^2 h^2 j^2 x^2 - \\
& 6 a^2 b f^2 h^2 j^2 p q x^2 + 6 a b^2 f^2 h^2 j^2 p^2 q^2 x^2 - 3 b^3 f^2 h^2 j^2 p^3 q^3 x^2 + 48 a^2 b e f h^2 i j p q \operatorname{Log}[e + f x] - 24 a^2 b e f g h j^2 p q \operatorname{Log}[e + f x] - \\
& 12 a^2 b e^2 h^2 j^2 p q \operatorname{Log}[e + f x] + 36 a b^2 e^2 h^2 j^2 p^2 q^2 \operatorname{Log}[e + f x] - 42 b^3 e^2 h^2 j^2 p^3 q^3 \operatorname{Log}[e + f x] - 48 a b^2 e f h^2 i j p^2 q^2 \operatorname{Log}[e + f x]^2 + \\
& 24 a b^2 e f g h j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 + 12 a b^2 e^2 h^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 - 18 b^3 e^2 h^2 j^2 p^3 q^3 \operatorname{Log}[e + f x]^2 + 16 b^3 e f h^2 i j p^3 q^3 \operatorname{Log}[e + f x]^3 - \\
& 8 b^3 e f g h j^2 p^3 q^3 \operatorname{Log}[e + f x]^3 - 4 b^3 e^2 h^2 j^2 p^3 q^3 \operatorname{Log}[e + f x]^3 - 96 a b^2 e f h^2 i j p q \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 48 a b^2 e f g h j^2 p q \operatorname{Log}[c (d (e + f x)^p)^q] + 96 b^3 e f h^2 i j p^2 q^2 \operatorname{Log}[c (d (e + f x)^p)^q] - 48 b^3 e f g h j^2 p^2 q^2 \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 48 a^2 b f^2 h^2 i j x \operatorname{Log}[c (d (e + f x)^p)^q] - 24 a^2 b f^2 g h j^2 x \operatorname{Log}[c (d (e + f x)^p)^q] - 96 a b^2 f^2 h^2 i j p q x \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 48 a b^2 f^2 g h j^2 p q x \operatorname{Log}[c (d (e + f x)^p)^q] + 24 a b^2 e f h^2 j^2 p q x \operatorname{Log}[c (d (e + f x)^p)^q] + 96 b^3 f^2 h^2 i j p^2 q^2 x \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 48 b^3 f^2 g h j^2 p^2 q^2 x \operatorname{Log}[c (d (e + f x)^p)^q] - 36 b^3 e f h^2 j^2 p^2 q^2 x \operatorname{Log}[c (d (e + f x)^p)^q] + 12 a^2 b f^2 h^2 j^2 x^2 \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 12 a b^2 f^2 h^2 j^2 p q x^2 \operatorname{Log}[c (d (e + f x)^p)^q] + 6 b^3 f^2 h^2 j^2 p^2 q^2 x^2 \operatorname{Log}[c (d (e + f x)^p)^q] + 96 a b^2 e f h^2 i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 48 a b^2 e f g h j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] - 24 a b^2 e^2 h^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 36 b^3 e^2 h^2 j^2 p^2 q^2 \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] - 48 b^3 e f h^2 i j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 24 b^3 e f g h j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] + 12 b^3 e^2 h^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] - \\
& 48 b^3 e f h^2 i j p q \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 24 b^3 e f g h j^2 p q \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 48 a b^2 f^2 h^2 i j x \operatorname{Log}[c (d (e + f x)^p)^q]^2 - \\
& 24 a b^2 f^2 g h j^2 x \operatorname{Log}[c (d (e + f x)^p)^q]^2 - 48 b^3 f^2 h^2 i j p q x \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 24 b^3 f^2 g h j^2 p q x \operatorname{Log}[c (d (e + f x)^p)^q]^2 + \\
& 12 b^3 e f h^2 j^2 p q x \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 12 a b^2 f^2 h^2 j^2 x^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 - 6 b^3 f^2 h^2 j^2 p q x^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 +
\end{aligned}$$

$$\begin{aligned}
& 48 b^3 e f h^2 i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 - 24 b^3 e f g h j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 - \\
& 12 b^3 e^2 h^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 16 b^3 f^2 h^2 i j x \operatorname{Log}[c (d (e + f x)^p)^q]^3 - 8 b^3 f^2 g h j^2 x \operatorname{Log}[c (d (e + f x)^p)^q]^3 + \\
& 4 b^3 f^2 h^2 j^2 x^2 \operatorname{Log}[c (d (e + f x)^p)^q]^3 + 8 a^3 f^2 h^2 i^2 \operatorname{Log}[g + h x] - 16 a^3 f^2 g h i j \operatorname{Log}[g + h x] + 8 a^3 f^2 g^2 j^2 \operatorname{Log}[g + h x] - \\
& 24 a^2 b f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 48 a^2 b f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] - 24 a^2 b f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + \\
& 24 a b^2 f^2 h^2 i^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - 48 a b^2 f^2 g h i j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] + 24 a b^2 f^2 g^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - \\
& 8 b^3 f^2 h^2 i^2 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + 16 b^3 f^2 g h i j p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] - 8 b^3 f^2 g^2 j^2 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + \\
& 24 a^2 b f^2 h^2 i^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 48 a^2 b f^2 g h i j \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
& 24 a^2 b f^2 g^2 j^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 48 a b^2 f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
& 96 a b^2 f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 48 a b^2 f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
& 24 b^3 f^2 h^2 i^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 48 b^3 f^2 g h i j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
& 24 b^3 f^2 g^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 24 a b^2 f^2 h^2 i^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - \\
& 48 a b^2 f^2 g h i j \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 24 a b^2 f^2 g^2 j^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - \\
& 24 b^3 f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 48 b^3 f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - \\
& 24 b^3 f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + 8 b^3 f^2 h^2 i^2 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] - \\
& 16 b^3 f^2 g h i j \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + 8 b^3 f^2 g^2 j^2 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + \\
& 24 a^2 b f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 48 a^2 b f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 24 a^2 b f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 24 a b^2 f^2 h^2 i^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 48 a b^2 f^2 g h i j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 24 a b^2 f^2 g^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 8 b^3 f^2 h^2 i^2 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 16 b^3 f^2 g h i j p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 8 b^3 f^2 g^2 j^2 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 48 a b^2 f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 96 a b^2 f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 48 a b^2 f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 24 b^3 f^2 h^2 i^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 48 b^3 f^2 g h i j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 24 b^3 f^2 g^2 j^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 24 b^3 f^2 h^2 i^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 48 b^3 f^2 g h i j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 24 b^3 f^2 g^2 j^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 24 b f^2 (h i - g j)^2 p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, \frac{h (e + f x)}{-f g + e h}\right] -
\end{aligned}$$

$$48 b^2 f^2 (h i - g j)^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] + 48 b^3 f^2 h^2 i^2 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right] -$$

$$96 b^3 f^2 g h i j p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right] + 48 b^3 f^2 g^2 j^2 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right]$$

Problem 536: Result more than twice size of optimal antiderivative.

$$\int \frac{(i + j x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{g + h x} dx$$

Optimal (type 4, 349 leaves, 13 steps):

$$\frac{6 a b^2 j p^2 q^2 x}{h} - \frac{6 b^3 j p^3 q^3 x}{h} + \frac{6 b^3 j p^2 q^2 (e + f x) \operatorname{Log}[c (d (e + f x)^p)^q]}{f h} -$$

$$\frac{3 b j p q (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2}{f h} + \frac{j (e + f x) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{f h} +$$

$$\frac{(h i - g j) (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right]}{h^2} + \frac{3 b (h i - g j) p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{h (e + f x)}{f g - e h}\right]}{h^2} -$$

$$\frac{6 b^2 (h i - g j) p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{h (e + f x)}{f g - e h}\right]}{h^2} + \frac{6 b^3 (h i - g j) p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{h (e + f x)}{f g - e h}\right]}{h^2}$$

Result (type 4, 1806 leaves):

$$\begin{aligned}
& \frac{1}{fh^2} \left(-3a^2 b e h j p q + 6 a b^2 e h j p^2 q^2 - 6 b^3 e h j p^3 q^3 + a^3 f h j x - 3 a^2 b f h j p q x + 6 a b^2 f h j p^2 q^2 x - 6 b^3 f h j p^3 q^3 x + 3 a^2 b e h j p q \operatorname{Log}[e + f x] - \right. \\
& 3 a b^2 e h j p^2 q^2 \operatorname{Log}[e + f x]^2 + b^3 e h j p^3 q^3 \operatorname{Log}[e + f x]^3 - 6 a b^2 e h j p q \operatorname{Log}[c (d (e + f x)^p)^q] + 6 b^3 e h j p^2 q^2 \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 3 a^2 b f h j x \operatorname{Log}[c (d (e + f x)^p)^q] - 6 a b^2 f h j p q x \operatorname{Log}[c (d (e + f x)^p)^q] + 6 b^3 f h j p^2 q^2 x \operatorname{Log}[c (d (e + f x)^p)^q] + \\
& 6 a b^2 e h j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] - 3 b^3 e h j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] - 3 b^3 e h j p q \operatorname{Log}[c (d (e + f x)^p)^q]^2 + \\
& 3 a b^2 f h j x \operatorname{Log}[c (d (e + f x)^p)^q]^2 - 3 b^3 f h j p q x \operatorname{Log}[c (d (e + f x)^p)^q]^2 + 3 b^3 e h j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 + \\
& b^3 f h j x \operatorname{Log}[c (d (e + f x)^p)^q]^3 + a^3 f h i \operatorname{Log}[g + h x] - a^3 f g j \operatorname{Log}[g + h x] - 3 a^2 b f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + \\
& 3 a^2 b f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 3 a b^2 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - 3 a b^2 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - \\
& b^3 f h i p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + b^3 f g j p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + 3 a^2 b f h i \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - \\
& 3 a^2 b f g j \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 6 a b^2 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\
& 6 a b^2 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 b^3 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - \\
& 3 b^3 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 a b^2 f h i \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - \\
& 3 a b^2 f g j \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - 3 b^3 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + \\
& 3 b^3 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + b^3 f h i \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] - \\
& b^3 f g j \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + 3 a^2 b f h i p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 3 a^2 b f g j p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 3 a b^2 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 3 a b^2 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + b^3 f h i p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& b^3 f g j p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 6 a b^2 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 6 a b^2 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - 3 b^3 f h i p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + \\
& 3 b^3 f g j p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 3 b^3 f h i p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\
& 3 b^3 f g j p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 3 b f (h i - g j) p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, \frac{h (e + f x)}{-f g + e h}\right] - \\
& 6 b^2 f (h i - g j) p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] + \\
& 6 b^3 f h i p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right] - 6 b^3 f g j p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right] \Big)
\end{aligned}$$

Problem 537: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{g + h x} dx$$

Optimal (type 4, 177 leaves, 6 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right]}{h} + \frac{3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h} -$$

$$\frac{6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h} + \frac{6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h}$$

Result (type 4, 646 leaves):

$$\frac{1}{h} \left(a^3 \operatorname{Log}[g + h x] - 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - \right.$$

$$b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + 3 a^2 b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] +$$

$$3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 a b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] -$$

$$3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + b^3 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] +$$

$$3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] - 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] +$$

$$3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right] + 3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, \frac{h(e+fx)}{-fg+eh}\right] -$$

$$\left. 6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, \frac{h(e+fx)}{-fg+eh}\right] + 6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h(e+fx)}{-fg+eh}\right] \right)$$

Problem 538: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3}{(g + h x) (i + j x)} dx$$

Optimal (type 4, 410 leaves, 13 steps):

$$\frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f(g+hx)}{fg-eh}\right]}{h i - g j} - \frac{(a + b \operatorname{Log}[c (d (e + f x)^p)^q])^3 \operatorname{Log}\left[\frac{f(i+jx)}{fi-ej}\right]}{h i - g j} +$$

$$\frac{3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{h(e+fx)}{fg-eh}\right]}{h i - g j} - \frac{3 b p q (a + b \operatorname{Log}[c (d (e + f x)^p)^q])^2 \operatorname{PolyLog}\left[2, -\frac{j(e+fx)}{fi-ej}\right]}{h i - g j} -$$

$$\frac{6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{h(e+fx)}{fg-eh}\right]}{h i - g j} + \frac{6 b^2 p^2 q^2 (a + b \operatorname{Log}[c (d (e + f x)^p)^q]) \operatorname{PolyLog}\left[3, -\frac{j(e+fx)}{fi-ej}\right]}{h i - g j} +$$

$$\frac{6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{h(e+fx)}{fg-eh}\right]}{h i - g j} - \frac{6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, -\frac{j(e+fx)}{fi-ej}\right]}{h i - g j}$$

Result (type 4, 1350 leaves):

$$\begin{aligned} & \frac{1}{h i - g j} \left(a^3 \operatorname{Log}[g + h x] - 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}[g + h x] + 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[g + h x] - \right. \\ & b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[g + h x] + 3 a^2 b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] - 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + \\ & 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[g + h x] + 3 a b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] - \\ & 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[g + h x] + b^3 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[g + h x] + 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\ & 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\ & 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] + 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (g + h x)}{f g - e h}\right] - \\ & a^3 \operatorname{Log}[i + j x] + 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}[i + j x] - 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[i + j x] + b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}[i + j x] - \\ & 3 a^2 b \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[i + j x] + 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[i + j x] - \\ & 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}[i + j x] - 3 a b^2 \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[i + j x] + \\ & 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}[i + j x] - b^3 \operatorname{Log}[c (d (e + f x)^p)^q]^3 \operatorname{Log}[i + j x] - 3 a^2 b p q \operatorname{Log}[e + f x] \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] + \\ & 3 a b^2 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] - b^3 p^3 q^3 \operatorname{Log}[e + f x]^3 \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] - 6 a b^2 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] + \\ & 3 b^3 p^2 q^2 \operatorname{Log}[e + f x]^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] - 3 b^3 p q \operatorname{Log}[e + f x] \operatorname{Log}[c (d (e + f x)^p)^q]^2 \operatorname{Log}\left[\frac{f (i + j x)}{f i - e j}\right] + \\ & 3 b p q \left(a + b \operatorname{Log}[c (d (e + f x)^p)^q] \right)^2 \operatorname{PolyLog}\left[2, \frac{h (e + f x)}{-f g + e h}\right] - 3 b p q \left(a + b \operatorname{Log}[c (d (e + f x)^p)^q] \right)^2 \operatorname{PolyLog}\left[2, \frac{j (e + f x)}{-f i + e j}\right] - \\ & 6 a b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] - 6 b^3 p^2 q^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{PolyLog}\left[3, \frac{h (e + f x)}{-f g + e h}\right] + 6 a b^2 p^2 q^2 \operatorname{PolyLog}\left[3, \frac{j (e + f x)}{-f i + e j}\right] + \\ & \left. 6 b^3 p^2 q^2 \operatorname{Log}[c (d (e + f x)^p)^q] \operatorname{PolyLog}\left[3, \frac{j (e + f x)}{-f i + e j}\right] + 6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{h (e + f x)}{-f g + e h}\right] - 6 b^3 p^3 q^3 \operatorname{PolyLog}\left[4, \frac{j (e + f x)}{-f i + e j}\right] \right) \end{aligned}$$

Test results for the 641 problems in "3.4 u (a+b log(c (d+e x^m)^n))^p.m"

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (a + b x^2)^p]^2}{x} dx$$

Optimal (type 4, 72 leaves, 5 steps):

$$\frac{1}{2} \operatorname{Log}\left[-\frac{bx^2}{a}\right] \operatorname{Log}\left[c(a+bx^2)^p\right]^2 + p \operatorname{Log}\left[c(a+bx^2)^p\right] \operatorname{PolyLog}\left[2, 1 + \frac{bx^2}{a}\right] - p^2 \operatorname{PolyLog}\left[3, 1 + \frac{bx^2}{a}\right]$$

Result (type 4, 163 leaves):

$$\begin{aligned} & \operatorname{Log}[x] \left(-p \operatorname{Log}[a+bx^2] + \operatorname{Log}\left[c(a+bx^2)^p\right]\right)^2 + \\ & 2p \left(-p \operatorname{Log}[a+bx^2] + \operatorname{Log}\left[c(a+bx^2)^p\right]\right) \left(\operatorname{Log}[x] \left(\operatorname{Log}[a+bx^2] - \operatorname{Log}\left[1 + \frac{bx^2}{a}\right]\right) - \frac{1}{2} \operatorname{PolyLog}\left[2, -\frac{bx^2}{a}\right]\right) + \\ & \frac{1}{2} p^2 \left(\operatorname{Log}\left[-\frac{bx^2}{a}\right] \operatorname{Log}[a+bx^2]^2 + 2 \operatorname{Log}[a+bx^2] \operatorname{PolyLog}\left[2, 1 + \frac{bx^2}{a}\right] - 2 \operatorname{PolyLog}\left[3, 1 + \frac{bx^2}{a}\right]\right) \end{aligned}$$

Problem 81: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[c(a+bx^2)^p\right]^2}{x^3} dx$$

Optimal (type 4, 80 leaves, 4 steps):

$$\frac{bp \operatorname{Log}\left[-\frac{bx^2}{a}\right] \operatorname{Log}\left[c(a+bx^2)^p\right]}{a} - \frac{(a+bx^2) \operatorname{Log}\left[c(a+bx^2)^p\right]^2}{2ax^2} + \frac{bp^2 \operatorname{PolyLog}\left[2, 1 + \frac{bx^2}{a}\right]}{a}$$

Result (type 4, 446 leaves):

$$\begin{aligned} & -\frac{1}{2ax^2} \left(2p(2bx^2 \operatorname{Log}[x] - (a+bx^2) \operatorname{Log}[a+bx^2]) (p \operatorname{Log}[a+bx^2] - \operatorname{Log}\left[c(a+bx^2)^p\right]) + \right. \\ & a \left(-p \operatorname{Log}[a+bx^2] + \operatorname{Log}\left[c(a+bx^2)^p\right]\right)^2 + p^2 \left(a \operatorname{Log}[a+bx^2]^2 + \right. \\ & bx^2 \left(\operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 + \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + 2 \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[\right. \right. \\ & \left. \left. 1 - \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{b}x}{\sqrt{a}}\right] - 4 \operatorname{Log}[x] \operatorname{Log}[a+bx^2] - 2 \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a+bx^2] - 2 \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a+bx^2] + \right. \\ & \left. \left. 2 \operatorname{Log}[a+bx^2]^2 + 4 \operatorname{PolyLog}\left[2, -\frac{i\sqrt{b}x}{\sqrt{a}}\right] + 4 \operatorname{PolyLog}\left[2, \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right]\right)\right) \end{aligned}$$

Problem 82: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[c(a+bx^2)^p\right]^2}{x^5} dx$$

Optimal (type 4, 129 leaves, 8 steps):

$$\frac{b^2 p^2 \operatorname{Log}[x]}{a^2} - \frac{b p (a + b x^2) \operatorname{Log}[c (a + b x^2)^p]}{2 a^2 x^2} - \frac{\operatorname{Log}[c (a + b x^2)^p]^2}{4 x^4} - \frac{b^2 p \operatorname{Log}[c (a + b x^2)^p] \operatorname{Log}\left[1 - \frac{a}{a + b x^2}\right]}{2 a^2} + \frac{b^2 p^2 \operatorname{PolyLog}\left[2, \frac{a}{a + b x^2}\right]}{2 a^2}$$

Result (type 4, 550 leaves):

$$\begin{aligned} & \frac{1}{4 a^2 x^4} \left(4 b^2 p^2 x^4 \operatorname{Log}[x] + b^2 p^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + b^2 p^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 b^2 p^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right. \\ & 2 b^2 p^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 b^2 p^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 b^2 p^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - \\ & 2 b^2 p^2 x^4 \operatorname{Log}[a + b x^2] - 2 b^2 p^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - 2 b^2 p^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - 2 a b p x^2 \operatorname{Log}[c (a + b x^2)^p] - \\ & 4 b^2 p x^4 \operatorname{Log}[x] \operatorname{Log}[c (a + b x^2)^p] + 2 b^2 p x^4 \operatorname{Log}[a + b x^2] \operatorname{Log}[c (a + b x^2)^p] - a^2 \operatorname{Log}[c (a + b x^2)^p]^2 + 4 b^2 p^2 x^4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + \\ & \left. 4 b^2 p^2 x^4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 b^2 p^2 x^4 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 b^2 p^2 x^4 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \end{aligned}$$

Problem 83: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (a + b x^2)^p]^2}{x^7} dx$$

Optimal (type 4, 193 leaves, 12 steps):

$$\begin{aligned} & -\frac{b^2 p^2}{6 a^2 x^2} - \frac{b^3 p^2 \operatorname{Log}[x]}{a^3} + \frac{b^3 p^2 \operatorname{Log}[a + b x^2]}{6 a^3} - \frac{b p \operatorname{Log}[c (a + b x^2)^p]}{6 a x^4} + \\ & \frac{b^2 p (a + b x^2) \operatorname{Log}[c (a + b x^2)^p]}{3 a^3 x^2} - \frac{\operatorname{Log}[c (a + b x^2)^p]^2}{6 x^6} + \frac{b^3 p \operatorname{Log}[c (a + b x^2)^p] \operatorname{Log}\left[1 - \frac{a}{a + b x^2}\right]}{3 a^3} - \frac{b^3 p^2 \operatorname{PolyLog}\left[2, \frac{a}{a + b x^2}\right]}{3 a^3} \end{aligned}$$

Result (type 4, 583 leaves):

$$\begin{aligned}
& -\frac{1}{6a^3x^6} \left(ab^2p^2x^4 + 6b^3p^2x^6 \operatorname{Log}[x] + b^3p^2x^6 \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 + b^3p^2x^6 \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 + 2b^3p^2x^6 \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + \right. \\
& 2b^3p^2x^6 \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + 4b^3p^2x^6 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 4b^3p^2x^6 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{b}x}{\sqrt{a}}\right] - \\
& 3b^3p^2x^6 \operatorname{Log}[a + bx^2] - 2b^3p^2x^6 \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + bx^2] - 2b^3p^2x^6 \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + bx^2] + a^2bp^2x^2 \operatorname{Log}[c(a + bx^2)^p] - \\
& 2a^2p^2x^4 \operatorname{Log}[c(a + bx^2)^p] - 4b^3px^6 \operatorname{Log}[x] \operatorname{Log}[c(a + bx^2)^p] + 2b^3px^6 \operatorname{Log}[a + bx^2] \operatorname{Log}[c(a + bx^2)^p] + a^3 \operatorname{Log}[c(a + bx^2)^p]^2 + \\
& \left. 4b^3p^2x^6 \operatorname{PolyLog}\left[2, -\frac{i\sqrt{b}x}{\sqrt{a}}\right] + 4b^3p^2x^6 \operatorname{PolyLog}\left[2, \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 2b^3p^2x^6 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + 2b^3p^2x^6 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right] \right)
\end{aligned}$$

Problem 87: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c(a + bx^2)^p]^2}{x^2} dx$$

Optimal (type 4, 190 leaves, 7 steps):

$$\begin{aligned}
& \frac{4i\sqrt{b}p^2 \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right]^2}{\sqrt{a}} + \frac{8\sqrt{b}p^2 \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right] \operatorname{Log}\left[\frac{2\sqrt{a}}{\sqrt{a} + i\sqrt{b}x}\right]}{\sqrt{a}} + \\
& \frac{4\sqrt{b}p \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right] \operatorname{Log}[c(a + bx^2)^p]}{\sqrt{a}} - \frac{\operatorname{Log}[c(a + bx^2)^p]^2}{x} + \frac{4i\sqrt{b}p^2 \operatorname{PolyLog}\left[2, 1 - \frac{2\sqrt{a}}{\sqrt{a} + i\sqrt{b}x}\right]}{\sqrt{a}}
\end{aligned}$$

Result (type 4, 387 leaves):

$$\begin{aligned}
& -\frac{1}{\sqrt{a}x} \left(4\sqrt{b}p^2x \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right] \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] + i\sqrt{b}p^2x \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 + \right. \\
& 4\sqrt{b}p^2x \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right] \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] - i\sqrt{b}p^2x \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right]^2 - 2i\sqrt{b}p^2x \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] + \\
& 2i\sqrt{b}p^2x \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right] - 4\sqrt{b}px \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right] \operatorname{Log}[c(a + bx^2)^p] + \\
& \left. \sqrt{a} \operatorname{Log}[c(a + bx^2)^p]^2 + 2i\sqrt{b}p^2x \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{b}x}{2\sqrt{a}}\right] - 2i\sqrt{b}p^2x \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{b}x}{2\sqrt{a}}\right] \right)
\end{aligned}$$

Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[c (a + b x^2)^p]^3}{x} dx$$

Optimal (type 4, 106 leaves, 6 steps):

$$\frac{1}{2} \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[c (a + b x^2)^p]^3 + \frac{3}{2} p \text{Log}[c (a + b x^2)^p]^2 \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 3 p^2 \text{Log}[c (a + b x^2)^p] \text{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] + 3 p^3 \text{PolyLog}\left[4, 1 + \frac{b x^2}{a}\right]$$

Result (type 4, 279 leaves):

$$\begin{aligned} & \text{Log}[x] \left(-p \text{Log}[a + b x^2] + \text{Log}[c (a + b x^2)^p]\right)^3 + \\ & 3 p \left(-p \text{Log}[a + b x^2] + \text{Log}[c (a + b x^2)^p]\right)^2 \left(\text{Log}[x] \left(\text{Log}[a + b x^2] - \text{Log}\left[1 + \frac{b x^2}{a}\right]\right) - \frac{1}{2} \text{PolyLog}\left[2, -\frac{b x^2}{a}\right]\right) - \\ & \frac{3}{2} p^2 \left(p \text{Log}[a + b x^2] - \text{Log}[c (a + b x^2)^p]\right) \left(\text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[a + b x^2]^2 + 2 \text{Log}[a + b x^2] \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right]\right) + \\ & \frac{1}{2} p^3 \left(\text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[a + b x^2]^3 + 3 \text{Log}[a + b x^2]^2 \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 6 \text{Log}[a + b x^2] \text{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] + 6 \text{PolyLog}\left[4, 1 + \frac{b x^2}{a}\right]\right) \end{aligned}$$

Problem 95: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[c (a + b x^2)^p]^3}{x^3} dx$$

Optimal (type 4, 119 leaves, 6 steps):

$$\frac{3 b p \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[c (a + b x^2)^p]^2}{2 a} - \frac{(a + b x^2) \text{Log}[c (a + b x^2)^p]^3}{2 a x^2} + \frac{3 b p^2 \text{Log}[c (a + b x^2)^p] \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{a} - \frac{3 b p^3 \text{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right]}{a}$$

Result (type 4, 627 leaves):

$$\begin{aligned}
& \frac{1}{2 a x^2} \left(a \left(p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p] \right)^3 + \right. \\
& 6 b p x^2 \operatorname{Log}[x] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 - 3 a p \operatorname{Log}[a + b x^2] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 - \\
& 3 b p x^2 \operatorname{Log}[a + b x^2] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 + 3 p^2 \left(p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p] \right) \left(a \operatorname{Log}[a + b x^2]^2 + \right. \\
& b x^2 \left(\operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 \operatorname{Log}[x] \right. \\
& \left. \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - 4 \operatorname{Log}[x] \operatorname{Log}[a + b x^2] - 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - 2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] + \right. \\
& \left. 2 \operatorname{Log}[a + b x^2]^2 + 4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \left. \right) - \\
& p^3 \left(\operatorname{Log}[a + b x^2]^2 \left(-3 b x^2 \operatorname{Log}\left[-\frac{b x^2}{a}\right] + (a + b x^2) \operatorname{Log}[a + b x^2] \right) - 6 b x^2 \operatorname{Log}[a + b x^2] \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] + 6 b x^2 \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right) \left. \right)
\end{aligned}$$

Problem 96: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (a + b x^2)^p]^3}{x^5} dx$$

Optimal (type 4, 219 leaves, 10 steps):

$$\begin{aligned}
& \frac{3 b^2 p^2 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[c (a + b x^2)^p]}{2 a^2} - \frac{3 b p (a + b x^2) \operatorname{Log}[c (a + b x^2)^p]^2}{4 a^2 x^2} - \frac{\operatorname{Log}[c (a + b x^2)^p]^3}{4 x^4} - \frac{3 b^2 p \operatorname{Log}[c (a + b x^2)^p]^2 \operatorname{Log}\left[1 - \frac{a}{a + b x^2}\right]}{4 a^2} + \\
& \frac{3 b^2 p^2 \operatorname{Log}[c (a + b x^2)^p] \operatorname{PolyLog}\left[2, \frac{a}{a + b x^2}\right]}{2 a^2} + \frac{3 b^2 p^3 \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{2 a^2} + \frac{3 b^2 p^3 \operatorname{PolyLog}\left[3, \frac{a}{a + b x^2}\right]}{2 a^2}
\end{aligned}$$

Result (type 4, 803 leaves):

$$\begin{aligned}
& \frac{1}{4 a^2 x^4} \left(a^2 \left(p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p] \right)^3 - 3 a b p x^2 \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 - \right. \\
& 6 b^2 p x^4 \operatorname{Log}[x] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 - 3 a^2 p \operatorname{Log}[a + b x^2] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 + \\
& \left. 3 b^2 p x^4 \operatorname{Log}[a + b x^2] \left(-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p] \right)^2 + 3 p^2 \left(p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p] \right) \right. \\
& \left(a^2 \operatorname{Log}[a + b x^2]^2 - b x^2 \left(4 b x^2 \operatorname{Log}[x] + b x^2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + b x^2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 b x^2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 b x^2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 b x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 b x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - 2 a \operatorname{Log}[a + b x^2] - 2 b x^2 \operatorname{Log}[a + b x^2] - \right. \right. \\
& \left. \left. 4 b x^2 \operatorname{Log}[x] \operatorname{Log}[a + b x^2] - 2 b x^2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - 2 b x^2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] + 2 b x^2 \operatorname{Log}[a + b x^2]^2 + \right. \right. \\
& \left. \left. 4 b x^2 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 b x^2 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 b x^2 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 b x^2 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \right) + \\
& p^3 \left(\operatorname{Log}[a + b x^2] \left(-3 b^2 x^4 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \left(-2 + \operatorname{Log}[a + b x^2] \right) - (a + b x^2) \operatorname{Log}[a + b x^2] \left(3 b x^2 + (a - b x^2) \operatorname{Log}[a + b x^2] \right) \right) - \right. \\
& \left. 6 b^2 x^4 \left(-1 + \operatorname{Log}[a + b x^2] \right) \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] + 6 b^2 x^4 \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right) \left. \right)
\end{aligned}$$

Problem 97: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (a + b x^2)^p]^3}{x^7} dx$$

Optimal (type 4, 352 leaves, 17 steps):

$$\begin{aligned}
& \frac{b^3 p^3 \operatorname{Log}[x]}{a^3} - \frac{b^2 p^2 (a + b x^2) \operatorname{Log}[c (a + b x^2)^p]}{2 a^3 x^2} - \frac{b^3 p^2 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[c (a + b x^2)^p]}{a^3} - \frac{b p \operatorname{Log}[c (a + b x^2)^p]^2}{4 a x^4} + \\
& \frac{b^2 p (a + b x^2) \operatorname{Log}[c (a + b x^2)^p]^2}{2 a^3 x^2} - \frac{\operatorname{Log}[c (a + b x^2)^p]^3}{6 x^6} - \frac{b^3 p^2 \operatorname{Log}[c (a + b x^2)^p] \operatorname{Log}\left[1 - \frac{a}{a + b x^2}\right]}{2 a^3} + \frac{b^3 p \operatorname{Log}[c (a + b x^2)^p]^2 \operatorname{Log}\left[1 - \frac{a}{a + b x^2}\right]}{2 a^3} + \\
& \frac{b^3 p^3 \operatorname{PolyLog}\left[2, \frac{a}{a + b x^2}\right]}{2 a^3} - \frac{b^3 p^2 \operatorname{Log}[c (a + b x^2)^p] \operatorname{PolyLog}\left[2, \frac{a}{a + b x^2}\right]}{a^3} - \frac{b^3 p^3 \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{a^3} - \frac{b^3 p^3 \operatorname{PolyLog}\left[3, \frac{a}{a + b x^2}\right]}{a^3}
\end{aligned}$$

Result (type 4, 1013 leaves):

$$\frac{1}{12 a^3 x^6} \left(2 a^3 (p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p])^3 - 3 a^2 b p x^2 (-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p])^2 + 6 a b^2 p x^4 (-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p])^2 + \right. \\ \left. 12 b^3 p x^6 \operatorname{Log}[x] (-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p])^2 - 6 a^3 p \operatorname{Log}[a + b x^2] (-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p])^2 - \right. \\ \left. 6 b^3 p x^6 \operatorname{Log}[a + b x^2] (-p \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^p])^2 + 6 p^2 (p \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^p]) \right. \\ \left(a^3 \operatorname{Log}[a + b x^2]^2 + b x^2 \left(a b x^2 + 6 b^2 x^4 \operatorname{Log}[x] + b^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + b^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 b^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right. \right. \\ \left. \left. 2 b^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 b^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 b^2 x^4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] + a^2 \operatorname{Log}[a + b x^2] - \right. \right. \\ \left. \left. 2 a b x^2 \operatorname{Log}[a + b x^2] - 3 b^2 x^4 \operatorname{Log}[a + b x^2] - 4 b^2 x^4 \operatorname{Log}[x] \operatorname{Log}[a + b x^2] - 2 b^2 x^4 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - \right. \right. \\ \left. \left. 2 b^2 x^4 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] + 2 b^2 x^4 \operatorname{Log}[a + b x^2]^2 + 4 b^2 x^4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + \right. \right. \\ \left. \left. 4 b^2 x^4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 b^2 x^4 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 b^2 x^4 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \right) - \\ p^3 \left(-6 b^3 x^6 \operatorname{Log}\left[-\frac{b x^2}{a}\right] + 6 a b^2 x^4 \operatorname{Log}[a + b x^2] + 6 b^3 x^6 \operatorname{Log}[a + b x^2] + 18 b^3 x^6 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[a + b x^2] + 3 a^2 b x^2 \operatorname{Log}[a + b x^2]^2 - \right. \\ \left. 6 a b^2 x^4 \operatorname{Log}[a + b x^2]^2 - 9 b^3 x^6 \operatorname{Log}[a + b x^2]^2 - 6 b^3 x^6 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[a + b x^2]^2 + 2 a^3 \operatorname{Log}[a + b x^2]^3 + \right. \\ \left. \left. 2 b^3 x^6 \operatorname{Log}[a + b x^2]^3 + 6 b^3 x^6 (3 - 2 \operatorname{Log}[a + b x^2]) \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] + 12 b^3 x^6 \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right) \right)$$

Problem 131: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (d + e x^3)^p]^2}{x} dx$$

Optimal (type 4, 77 leaves, 5 steps):

$$\frac{1}{3} \operatorname{Log}\left[-\frac{e x^3}{d}\right] \operatorname{Log}[c (d + e x^3)^p]^2 + \frac{2}{3} p \operatorname{Log}[c (d + e x^3)^p] \operatorname{PolyLog}\left[2, 1 + \frac{e x^3}{d}\right] - \frac{2}{3} p^2 \operatorname{PolyLog}\left[3, 1 + \frac{e x^3}{d}\right]$$

Result (type 4, 2965 leaves):

$$\operatorname{Log}[x] (-p \operatorname{Log}[d + e x^3] + \operatorname{Log}[c (d + e x^3)^p])^2 + \\ 2 p (-p \operatorname{Log}[d + e x^3] + \operatorname{Log}[c (d + e x^3)^p]) \left(\operatorname{Log}[x] \left(\operatorname{Log}[d + e x^3] - \operatorname{Log}\left[1 + \frac{e x^3}{d}\right] \right) - \frac{1}{3} \operatorname{PolyLog}\left[2, -\frac{e x^3}{d}\right] \right) +$$

$$\begin{aligned}
& p^2 \left(\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right]^2 + 2 \text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \right. \\
& \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right]^2 + 2 \text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] + \\
& 2 \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right]^2 + \\
& \left. \text{Log} \left[\frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right]^2 \left(\text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[\frac{i \sqrt{3} d^{1/3}}{(-1)^{1/3} d^{1/3} - e^{1/3} x} \right] - \text{Log} \left[\frac{(-1)^{2/3} (1 + (-1)^{1/3}) e^{1/3} x}{(-1)^{1/3} d^{1/3} - e^{1/3} x} \right] \right) + \right. \\
& \left(\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[-\frac{(-1 + (-1)^{2/3}) d^{1/3}}{d^{1/3} + e^{1/3} x} \right] - \text{Log} \left[\frac{(1 + (-1)^{1/3}) e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{Log} \left[\frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right]^2 + \\
& \left(\text{Log} [2] + \text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[\frac{(1 + (-1)^{1/3}) d^{1/3}}{d^{1/3} + e^{1/3} x} \right] - \text{Log} \left[\frac{(3 - i \sqrt{3}) e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right]^2 + \\
& 2 \left(\text{Log} \left[\frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] - \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[\frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(-\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[\frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[\frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + \\
& \left(\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] - \text{Log} \left[\frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \left(-2 \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \right) + \\
& \left(-\text{Log} \left[\frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \left(-2 \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] \right) + \\
& 2 \left(-\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] + \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \text{Log} \left[1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \\
& \left(\text{Log} \left[-\frac{e^{1/3} x}{d^{1/3}} \right] - \text{Log} \left[-\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) \text{Log} \left[1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \left(-2 \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) + \\
& \left. \text{Log} [x] \left(\text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} [d + e x^3] \right)^2 - \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left(\text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} [d + e x^3] \right) \left(\text{Log} [x] \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \right. \\
& \quad \text{Log} [x] \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} [x] \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} [x] \text{Log} \left[1 + \frac{e^{1/3} x}{d^{1/3}} \right] - \text{Log} [x] \text{Log} \left[1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] - \\
& \quad \left. \text{Log} [x] \text{Log} \left[1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \text{PolyLog} \left[2, -\frac{e^{1/3} x}{d^{1/3}} \right] - \text{PolyLog} \left[2, \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] - \text{PolyLog} \left[2, -\frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) + \\
& 2 \text{Log} \left[\frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] \left(-\text{PolyLog} \left[2, \frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] + \text{PolyLog} \left[2, \frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{-(-1)^{1/3} d^{1/3} + e^{1/3} x} \right] \right) + \\
& 2 \text{Log} \left[\frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \left(\text{PolyLog} \left[2, \frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] - \text{PolyLog} \left[2, \frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) + \\
& 2 \text{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \left(\text{PolyLog} \left[2, \frac{-(-1)^{1/3} d^{1/3} + e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] - \text{PolyLog} \left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) + \\
& 2 \text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \text{PolyLog} \left[2, 1 + \frac{e^{1/3} x}{d^{1/3}} \right] + 2 \left(\text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} \left[\frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{PolyLog} \left[2, 1 + \frac{e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(\text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{PolyLog} \left[2, 1 + \frac{e^{1/3} x}{d^{1/3}} \right] + 2 \text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] \text{PolyLog} \left[2, 1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(\text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] \right) \text{PolyLog} \left[2, 1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(\text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{PolyLog} \left[2, 1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right] + 2 \text{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] \text{PolyLog} \left[2, 1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(\text{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \text{Log} \left[\frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] \right) \text{PolyLog} \left[2, 1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \left(\text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \text{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \right) \text{PolyLog} \left[2, 1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \\
& 2 \text{PolyLog} \left[3, \frac{(-1)^{2/3} \left(\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right)}{-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x} \right] - 2 \text{PolyLog} \left[3, \frac{-(-1)^{1/3} d^{1/3} + e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] - 2 \text{PolyLog} \left[3, \frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] -
\end{aligned}$$

$$2 \operatorname{PolyLog}\left[3, \frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{-(-1)^{1/3} d^{1/3} + e^{1/3} x}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{d^{1/3} + e^{1/3} x}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x}\right] -$$

$$6 \operatorname{PolyLog}\left[3, 1 + \frac{e^{1/3} x}{d^{1/3}}\right] - 6 \operatorname{PolyLog}\left[3, 1 - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}}\right] - 6 \operatorname{PolyLog}\left[3, 1 + \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}}\right]$$

Problem 132: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (d + e x^3)^p]^2}{x^4} dx$$

Optimal (type 4, 86 leaves, 4 steps):

$$\frac{2 e p \operatorname{Log}\left[-\frac{e x^3}{d}\right] \operatorname{Log}[c (d + e x^3)^p]}{3 d} - \frac{(d + e x^3) \operatorname{Log}[c (d + e x^3)^p]^2}{3 d x^3} + \frac{2 e p^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x^3}{d}\right]}{3 d}$$

Result (type 4, 1374 leaves):

$$-\frac{1}{9 d x^3} \left(6 p (3 e x^3 \operatorname{Log}[x] - (d + e x^3) \operatorname{Log}[d + e x^3]) (p \operatorname{Log}[d + e x^3] - \operatorname{Log}[c (d + e x^3)^p]) + 3 d (-p \operatorname{Log}[d + e x^3] + \operatorname{Log}[c (d + e x^3)^p])^2 + \right.$$

$$p^2 \left(3 d \operatorname{Log}[d + e x^3]^2 + e x^3 \left(6 \operatorname{Log}[2]^2 + \operatorname{Log}[6] \operatorname{Log}[64] - 4 \operatorname{Log}[8] \operatorname{Log}[x] - 2 \operatorname{Log}[4096] \operatorname{Log}[x] + 3 \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right]^2 - \right. \right.$$

$$2 \operatorname{Log}[8] \operatorname{Log}\left[\frac{(-1 - i \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right] - \operatorname{Log}[46 656] \operatorname{Log}\left[\frac{(-1 - i \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right] + 3 \operatorname{Log}\left[\frac{(-1 - i \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right]^2 -$$

$$\operatorname{Log}[64] \operatorname{Log}\left[\frac{i (i + \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right] + 3 \operatorname{Log}\left[\frac{i (i + \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right]^2 - 2 \operatorname{Log}[8] \operatorname{Log}\left[\frac{-2 i d^{1/3} + (i + \sqrt{3}) e^{1/3} x}{(-3 i + \sqrt{3}) d^{1/3}}\right] +$$

$$6 \operatorname{Log}\left[\frac{i (i + \sqrt{3}) d^{1/3}}{e^{1/3}} + 2 x\right] \operatorname{Log}\left[\frac{-2 i d^{1/3} + (i + \sqrt{3}) e^{1/3} x}{(-3 i + \sqrt{3}) d^{1/3}}\right] + 6 \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] +$$

$$6 \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[-\frac{-i + \sqrt{3} + \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i - \sqrt{3}}\right] + 18 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e^{1/3} x}{d^{1/3}}\right] - \operatorname{Log}[64] \operatorname{Log}\left[\frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}}\right)}{3 i - \sqrt{3}}\right] +$$

$$\begin{aligned}
& 6 \operatorname{Log}\left[\frac{(-1 - i\sqrt{3})d^{1/3}}{e^{1/3}} + 2x\right] \operatorname{Log}\left[\frac{2i\left(1 + \frac{e^{1/3}x}{d^{1/3}}\right)}{3i - \sqrt{3}}\right] - \operatorname{Log}[64] \operatorname{Log}\left[\frac{2i\left(1 + \frac{e^{1/3}x}{d^{1/3}}\right)}{3i + \sqrt{3}}\right] + 6 \operatorname{Log}\left[\frac{i(i + \sqrt{3})d^{1/3}}{e^{1/3}} + 2x\right] \operatorname{Log}\left[\frac{2i\left(1 + \frac{e^{1/3}x}{d^{1/3}}\right)}{3i + \sqrt{3}}\right] - \\
& \operatorname{Log}[64] \operatorname{Log}\left[3 + i\sqrt{3} - \frac{2i\sqrt{3}e^{1/3}x}{d^{1/3}}\right] + 6 \operatorname{Log}\left[\frac{(-1 - i\sqrt{3})d^{1/3}}{e^{1/3}} + 2x\right] \operatorname{Log}\left[3 + i\sqrt{3} - \frac{2i\sqrt{3}e^{1/3}x}{d^{1/3}}\right] + \\
& 18 \operatorname{Log}[x] \operatorname{Log}\left[2 + \frac{(-1 - i\sqrt{3})e^{1/3}x}{d^{1/3}}\right] + 18 \operatorname{Log}[x] \operatorname{Log}\left[2 + \frac{i(i + \sqrt{3})e^{1/3}x}{d^{1/3}}\right] + \operatorname{Log}[16] \operatorname{Log}[d + ex^3] + \operatorname{Log}[256] \operatorname{Log}[d + ex^3] - \\
& 18 \operatorname{Log}[x] \operatorname{Log}[d + ex^3] - 6 \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}[d + ex^3] - 6 \operatorname{Log}\left[\frac{(-1 - i\sqrt{3})d^{1/3}}{e^{1/3}} + 2x\right] \operatorname{Log}[d + ex^3] - 6 \operatorname{Log}\left[\frac{i(i + \sqrt{3})d^{1/3}}{e^{1/3}} + 2x\right] \\
& \operatorname{Log}[d + ex^3] + 6 \operatorname{Log}[d + ex^3]^2 + 18 \operatorname{PolyLog}\left[2, -\frac{e^{1/3}x}{d^{1/3}}\right] + 18 \operatorname{PolyLog}\left[2, \frac{(1 - i\sqrt{3})e^{1/3}x}{2d^{1/3}}\right] + 18 \operatorname{PolyLog}\left[2, \frac{(1 + i\sqrt{3})e^{1/3}x}{2d^{1/3}}\right] + \\
& 6 \operatorname{PolyLog}\left[2, \frac{-2id^{1/3} + (i + \sqrt{3})e^{1/3}x}{(-3i + \sqrt{3})d^{1/3}}\right] + 6 \operatorname{PolyLog}\left[2, \frac{i + \sqrt{3} - \frac{2ie^{1/3}x}{d^{1/3}}}{3i + \sqrt{3}}\right] + 6 \operatorname{PolyLog}\left[2, -\frac{-i + \sqrt{3} + \frac{2ie^{1/3}x}{d^{1/3}}}{3i - \sqrt{3}}\right] + \\
& 6 \operatorname{PolyLog}\left[2, \frac{2i\left(1 + \frac{e^{1/3}x}{d^{1/3}}\right)}{3i - \sqrt{3}}\right] + 6 \operatorname{PolyLog}\left[2, \frac{2i\left(1 + \frac{e^{1/3}x}{d^{1/3}}\right)}{3i + \sqrt{3}}\right] + 6 \operatorname{PolyLog}\left[2, \frac{1}{6}\left(3 + i\sqrt{3} - \frac{2i\sqrt{3}e^{1/3}x}{d^{1/3}}\right)\right] \Bigg) \Bigg) \Bigg) \Bigg)
\end{aligned}$$

Problem 133: Result unnecessarily involves higher level functions.

$$\int x \operatorname{Log}[c(d + ex^3)^p]^2 dx$$

Optimal (type 4, 1294 leaves, 49 steps):

$$\begin{aligned}
& \frac{9 p^2 x^2}{4} + \frac{3 \sqrt{3} d^{2/3} p^2 \operatorname{ArcTan}\left[\frac{d^{1/3}-2 e^{1/3} x}{\sqrt{3} d^{1/3}}\right]}{2 e^{2/3}} + \frac{3 d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3} x\right]}{2 e^{2/3}} + \frac{d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3} x\right]^2}{2 e^{2/3}} + \frac{d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3} x\right] \operatorname{Log}\left[-\frac{(-1)^{2/3} d^{1/3}+e^{1/3} x}{(1-(-1)^{2/3}) d^{1/3}}\right]}{e^{2/3}} \\
& - \frac{(-1)^{1/3} d^{2/3} p^2 \operatorname{Log}\left[\frac{(-1)^{1/3}\left(d^{1/3}+e^{1/3} x\right)}{(1+(-1)^{1/3}) d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}-(-1)^{1/3} e^{1/3} x\right]}{e^{2/3}} - \frac{(-1)^{1/3} d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}-(-1)^{1/3} e^{1/3} x\right]^2}{2 e^{2/3}} + \\
& - \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{Log}\left[-\frac{(-1)^{2/3}\left(d^{1/3}+e^{1/3} x\right)}{(1-(-1)^{2/3}) d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}+(-1)^{2/3} e^{1/3} x\right]}{e^{2/3}} + \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{Log}\left[\frac{(-1)^{1/3}\left(d^{1/3}-(-1)^{1/3} e^{1/3} x\right)}{(1+(-1)^{1/3}) d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}+(-1)^{2/3} e^{1/3} x\right]}{e^{2/3}} + \\
& - \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}+(-1)^{2/3} e^{1/3} x\right]^2}{2 e^{2/3}} + \frac{d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3} x\right] \operatorname{Log}\left[\frac{(-1)^{1/3}\left(d^{1/3}+(-1)^{2/3} e^{1/3} x\right)}{(1+(-1)^{1/3}) d^{1/3}}\right]}{e^{2/3}} - \\
& - \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{Log}\left[-\frac{(-1)^{2/3}\left(d^{1/3}+e^{1/3} x\right)}{(1-(-1)^{2/3}) d^{1/3}}\right] \operatorname{Log}\left[\frac{d^{1/3}+(-1)^{2/3} e^{1/3} x}{(1-(-1)^{2/3}) d^{1/3}}\right]}{e^{2/3}} - \frac{(-1)^{1/3} d^{2/3} p^2 \operatorname{Log}\left[d^{1/3}-(-1)^{1/3} e^{1/3} x\right] \operatorname{Log}\left[-\frac{(-1)^{2/3}\left(d^{1/3}+(-1)^{2/3} e^{1/3} x\right)}{(1-(-1)^{2/3}) d^{1/3}}\right]}{e^{2/3}} - \\
& + \frac{3 d^{2/3} p^2 \operatorname{Log}\left[d^{2/3}-d^{1/3} e^{1/3} x+e^{2/3} x^2\right]}{4 e^{2/3}} - \frac{3}{2} p x^2 \operatorname{Log}\left[c\left(d+e x^3\right)^p\right] - \frac{d^{2/3} p \operatorname{Log}\left[d^{1/3}+e^{1/3} x\right] \operatorname{Log}\left[c\left(d+e x^3\right)^p\right]}{e^{2/3}} + \\
& - \frac{(-1)^{1/3} d^{2/3} p \operatorname{Log}\left[d^{1/3}-(-1)^{1/3} e^{1/3} x\right] \operatorname{Log}\left[c\left(d+e x^3\right)^p\right]}{e^{2/3}} - \frac{(-1)^{2/3} d^{2/3} p \operatorname{Log}\left[d^{1/3}+(-1)^{2/3} e^{1/3} x\right] \operatorname{Log}\left[c\left(d+e x^3\right)^p\right]}{e^{2/3}} + \\
& + \frac{1}{2} x^2 \operatorname{Log}\left[c\left(d+e x^3\right)^p\right]^2 + \frac{d^{2/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}+e^{1/3} x}{(1+(-1)^{1/3}) d^{1/3}}\right]}{e^{2/3}} - \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{PolyLog}\left[2, -\frac{(-1)^{2/3}\left(d^{1/3}+e^{1/3} x\right)}{(1-(-1)^{2/3}) d^{1/3}}\right]}{e^{2/3}} + \frac{d^{2/3} p^2 \operatorname{PolyLog}\left[2, \frac{2\left(d^{1/3}+e^{1/3} x\right)}{(3-i \sqrt{3}) d^{1/3}}\right]}{e^{2/3}} - \\
& - \frac{(-1)^{1/3} d^{2/3} p^2 \operatorname{PolyLog}\left[2, -\frac{(-1)^{1/3}\left((-1)^{2/3} d^{1/3}+e^{1/3} x\right)}{(1-(-1)^{2/3}) d^{1/3}}\right]}{e^{2/3}} - \frac{(-1)^{1/3} d^{2/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}-(-1)^{1/3} e^{1/3} x}{(1+(-1)^{1/3}) d^{1/3}}\right]}{e^{2/3}} + \frac{(-1)^{2/3} d^{2/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}+(-1)^{2/3} e^{1/3} x}{(1+(-1)^{1/3}) d^{1/3}}\right]}{e^{2/3}}
\end{aligned}$$

Result (type 5, 1227 leaves):

$$\begin{aligned}
& p \left(-\frac{3 e x^5 \operatorname{Hypergeometric2F1}\left[1, \frac{5}{3}, \frac{8}{3}, -\frac{e x^3}{d}\right]}{5 d} + x^2 \operatorname{Log}\left[d+e x^3\right] \right) \left(-p \operatorname{Log}\left[d+e x^3\right] + \operatorname{Log}\left[c\left(d+e x^3\right)^p\right] \right) + \\
& \frac{1}{2} x^2 \left(-p \operatorname{Log}\left[d+e x^3\right] + \operatorname{Log}\left[c\left(d+e x^3\right)^p\right] \right)^2 +
\end{aligned}$$

$$\begin{aligned}
& p^2 \left(\frac{1}{2} x^2 \operatorname{Log}[d + e x^3]^2 - \frac{1}{4 e^{2/3}} \left(6 d^{1/3} e^{1/3} x + 6 (-1)^{2/3} d^{1/3} e^{1/3} x - 6 e^{2/3} x^2 - 3 e^{1/3} x \left(2 (-1)^{1/3} d^{1/3} + e^{1/3} x \right) + 6 e^{2/3} x^2 \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] + \right. \right. \\
& 2 d^{2/3} \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right]^2 + 6 e^{2/3} x^2 \operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] - \frac{6 d^{2/3} \operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right]^2}{\left(1 + (-1)^{1/3}\right)^2} + 6 e^{2/3} x^2 \operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] - \\
& 2 (-1)^{1/3} d^{2/3} \operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right]^2 - 6 d^{2/3} \operatorname{Log}[d^{1/3} + e^{1/3} x] - 6 (-1)^{2/3} d^{2/3} \operatorname{Log}\left[-(-1)^{1/3} d^{1/3} + e^{1/3} x\right] + 6 (-1)^{1/3} d^{2/3} \\
& \left. \operatorname{Log}\left[(-1)^{2/3} d^{1/3} + e^{1/3} x\right] - 2 \left(3 e^{2/3} x^2 + 2 \sqrt{3} d^{2/3} \operatorname{ArcTan}\left[\frac{1 - 2 e^{1/3} x}{d^{1/3}}\right] + 2 d^{2/3} \operatorname{Log}[d^{1/3} + e^{1/3} x] - d^{2/3} \operatorname{Log}[d^{2/3} - d^{1/3} e^{1/3} x + e^{2/3} x^2] \right) \right) \\
& \left(\operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] + \operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] + \operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] - \operatorname{Log}[d + e x^3] \right) + \\
& 4 d^{2/3} \left(\operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{d^{1/3} + e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] \right) - \\
& \frac{12 d^{2/3} \left(\operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{d^{1/3} + e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] \right)}{\left(1 + (-1)^{1/3}\right)^2} - \\
& \frac{12 d^{2/3} \left(\operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x\right)}{\sqrt{3} d^{1/3}}\right] \right)}{\left(1 + (-1)^{1/3}\right)^2} - \\
& 4 (-1)^{1/3} d^{2/3} \left(\operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[-\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x\right)}{\sqrt{3} d^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{\left(1 + (-1)^{1/3}\right) d^{1/3}}\right] \right) + \\
& 4 d^{2/3} \left(\operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}}\right)}{3 i + \sqrt{3}}\right] + \operatorname{PolyLog}\left[2, \frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] \right) -
\end{aligned}$$

$$4 (-1)^{1/3} d^{2/3} \left(\text{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \text{Log} \left[\frac{i + \sqrt{3} - \frac{2i e^{1/3} x}{d^{1/3}}}{3i + \sqrt{3}} \right] + \text{PolyLog} \left[2, \frac{2i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3i + \sqrt{3}} \right] \right)$$

Problem 135: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Log}[c (d + e x^3)^p]^2}{x^2} dx$$

Optimal (type 4, 1137 leaves, 39 steps):

$$\begin{aligned} & \frac{e^{1/3} p^2 \text{Log}[d^{1/3} + e^{1/3} x]^2}{d^{1/3}} + \frac{2 e^{1/3} p^2 \text{Log}[d^{1/3} + e^{1/3} x] \text{Log}\left[-\frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 (-1)^{1/3} e^{1/3} p^2 \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} + e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right] \text{Log}[d^{1/3} - (-1)^{1/3} e^{1/3} x]}{d^{1/3}} \\ & - \frac{(-1)^{1/3} e^{1/3} p^2 \text{Log}[d^{1/3} - (-1)^{1/3} e^{1/3} x]^2}{d^{1/3}} + \frac{2 (-1)^{2/3} e^{1/3} p^2 \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right] \text{Log}[d^{1/3} + (-1)^{2/3} e^{1/3} x]}{d^{1/3}} + \\ & \frac{2 (-1)^{2/3} e^{1/3} p^2 \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} - (-1)^{1/3} e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right] \text{Log}[d^{1/3} + (-1)^{2/3} e^{1/3} x]}{d^{1/3}} + \frac{(-1)^{2/3} e^{1/3} p^2 \text{Log}[d^{1/3} + (-1)^{2/3} e^{1/3} x]^2}{d^{1/3}} + \\ & \frac{2 e^{1/3} p^2 \text{Log}[d^{1/3} + e^{1/3} x] \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} + (-1)^{2/3} e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 (-1)^{2/3} e^{1/3} p^2 \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right] \text{Log}\left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{1/3}} - \\ & \frac{2 (-1)^{1/3} e^{1/3} p^2 \text{Log}[d^{1/3} - (-1)^{1/3} e^{1/3} x] \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + (-1)^{2/3} e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 e^{1/3} p \text{Log}[d^{1/3} + e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{1/3}} + \\ & \frac{2 (-1)^{1/3} e^{1/3} p \text{Log}[d^{1/3} - (-1)^{1/3} e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{1/3}} - \frac{2 (-1)^{2/3} e^{1/3} p \text{Log}[d^{1/3} + (-1)^{2/3} e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{1/3}} - \\ & \frac{\text{Log}[c (d + e x^3)^p]^2}{x} + \frac{2 e^{1/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 (-1)^{2/3} e^{1/3} p^2 \text{PolyLog}\left[2, -\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{1/3}} + \frac{2 e^{1/3} p^2 \text{PolyLog}\left[2, \frac{2 (d^{1/3} + e^{1/3} x)}{(3 - i \sqrt{3}) d^{1/3}}\right]}{d^{1/3}} - \\ & \frac{2 (-1)^{1/3} e^{1/3} p^2 \text{PolyLog}\left[2, -\frac{(-1)^{1/3} ((-1)^{2/3} d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 (-1)^{1/3} e^{1/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{1/3}} - \frac{2 (-1)^{2/3} e^{1/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{1/3}} \end{aligned}$$

Result (type 5, 994 leaves):

$$\begin{aligned}
& 2 p \left(\frac{3 e x^2 \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, 1, \frac{5}{3}, -\frac{e x^3}{d}\right] - \frac{\operatorname{Log}[d + e x^3]}{x}}{2 d} \right) \left(-p \operatorname{Log}[d + e x^3] + \operatorname{Log}[c (d + e x^3)^p] \right) - \\
& \frac{\left(-p \operatorname{Log}[d + e x^3] + \operatorname{Log}[c (d + e x^3)^p] \right)^2}{x} + p^2 \left(-\frac{\operatorname{Log}[d + e x^3]^2}{x} - \right. \\
& \frac{1}{\sqrt{3} d^{1/3}} i e^{1/3} \left(-i \sqrt{3} \operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right]^2 - (-1)^{1/3} (-1 + (-1)^{2/3}) \operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right]^2 + (-1)^{2/3} (1 + (-1)^{1/3}) \operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right]^2 - \right. \\
& \left. (-1)^{5/6} \sqrt{3} (-1 + (-1)^{1/3}) \left(2 \sqrt{3} \operatorname{ArcTan}\left[\frac{1 - \frac{2 e^{1/3} x}{d^{1/3}}}{\sqrt{3}}\right] + 2 \operatorname{Log}[d^{1/3} + e^{1/3} x] - \operatorname{Log}[d^{2/3} - d^{1/3} e^{1/3} x + e^{2/3} x^2] \right) \right) \\
& \left(\operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] + \operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] + \operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] - \operatorname{Log}[d + e x^3] \right) - \\
& 2 i \sqrt{3} \left(\operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] \right) - \\
& 2 (-1)^{1/3} (-1 + (-1)^{2/3}) \left(\operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] \right) - \\
& 2 (-1)^{1/3} (-1 + (-1)^{2/3}) \left(\operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \operatorname{PolyLog}\left[2, -\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}} \right] \right) + \\
& 2 (-1)^{2/3} (1 + (-1)^{1/3}) \left(\operatorname{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[-\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}} \right] + \operatorname{PolyLog}\left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] \right) - \\
& 2 i \sqrt{3} \left(\operatorname{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}}\right] + \operatorname{PolyLog}\left[2, \frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] \right) + \\
& 2 (-1)^{2/3} (1 + (-1)^{1/3}) \left(\operatorname{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \operatorname{Log}\left[\frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] + \operatorname{PolyLog}\left[2, \frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}}\right] \right) \Big) \Big) \Big) \Big)
\end{aligned}$$

Problem 136: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Log}[c (d + e x^3)^p]^2}{x^3} dx$$

Optimal (type 4, 1170 leaves, 39 steps):

$$\begin{aligned} & \frac{e^{2/3} p^2 \text{Log}[-d^{1/3} - e^{1/3} x]^2}{2 d^{2/3}} - \frac{e^{2/3} p^2 \text{Log}[-d^{1/3} - e^{1/3} x] \text{Log}\left[-\frac{(-1)^{2/3} d^{1/3} + e^{1/3} x}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{2/3}} - \frac{(-1)^{2/3} e^{2/3} p^2 \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} + e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right] \text{Log}[-d^{1/3} + (-1)^{1/3} e^{1/3} x]}{d^{2/3}} \\ & \frac{(-1)^{2/3} e^{2/3} p^2 \text{Log}[-d^{1/3} + (-1)^{1/3} e^{1/3} x]^2}{2 d^{2/3}} + \frac{(-1)^{1/3} e^{2/3} p^2 \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right] \text{Log}[-d^{1/3} - (-1)^{2/3} e^{1/3} x]}{d^{2/3}} + \\ & \frac{(-1)^{1/3} e^{2/3} p^2 \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} - (-1)^{1/3} e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right] \text{Log}[-d^{1/3} - (-1)^{2/3} e^{1/3} x]}{d^{2/3}} + \frac{(-1)^{1/3} e^{2/3} p^2 \text{Log}[-d^{1/3} - (-1)^{2/3} e^{1/3} x]^2}{2 d^{2/3}} - \\ & \frac{e^{2/3} p^2 \text{Log}[-d^{1/3} - e^{1/3} x] \text{Log}\left[\frac{(-1)^{1/3} (d^{1/3} + (-1)^{2/3} e^{1/3} x)}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{2/3}} - \frac{(-1)^{1/3} e^{2/3} p^2 \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right] \text{Log}\left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{2/3}} - \\ & \frac{(-1)^{2/3} e^{2/3} p^2 \text{Log}[-d^{1/3} + (-1)^{1/3} e^{1/3} x] \text{Log}\left[-\frac{(-1)^{2/3} (d^{1/3} + (-1)^{2/3} e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{2/3}} + \frac{e^{2/3} p \text{Log}[-d^{1/3} - e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{2/3}} + \\ & \frac{(-1)^{2/3} e^{2/3} p \text{Log}[-d^{1/3} + (-1)^{1/3} e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{2/3}} - \frac{(-1)^{1/3} e^{2/3} p \text{Log}[-d^{1/3} - (-1)^{2/3} e^{1/3} x] \text{Log}[c (d + e x^3)^p]}{d^{2/3}} - \\ & \frac{\text{Log}[c (d + e x^3)^p]^2}{2 x^2} - \frac{e^{2/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{2/3}} - \frac{(-1)^{1/3} e^{2/3} p^2 \text{PolyLog}\left[2, -\frac{(-1)^{2/3} (d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{2/3}} - \frac{e^{2/3} p^2 \text{PolyLog}\left[2, \frac{2 (d^{1/3} + e^{1/3} x)}{(3 - i \sqrt{3}) d^{1/3}}\right]}{d^{2/3}} - \\ & \frac{(-1)^{2/3} e^{2/3} p^2 \text{PolyLog}\left[2, -\frac{(-1)^{1/3} ((-1)^{2/3} d^{1/3} + e^{1/3} x)}{(1 - (-1)^{2/3}) d^{1/3}}\right]}{d^{2/3}} - \frac{(-1)^{2/3} e^{2/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} - (-1)^{1/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{2/3}} + \frac{(-1)^{1/3} e^{2/3} p^2 \text{PolyLog}\left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right]}{d^{2/3}} \end{aligned}$$

Result (type 5, 964 leaves):

$$\begin{aligned}
& p \left(\frac{3 \operatorname{erf} \operatorname{Hypergeometric2F1} \left[\frac{1}{3}, 1, \frac{4}{3}, -\frac{e x^3}{d} \right]}{d} - \frac{\operatorname{Log} [d + e x^3]}{x^2} \right) \left(-p \operatorname{Log} [d + e x^3] + \operatorname{Log} [c (d + e x^3)^p] \right) - \\
& \frac{(-p \operatorname{Log} [d + e x^3] + \operatorname{Log} [c (d + e x^3)^p])^2}{2 x^2} + p^2 \left(-\frac{\operatorname{Log} [d + e x^3]^2}{2 x^2} - \right. \\
& \frac{1}{2 \sqrt{3} d^{2/3}} i e^{2/3} \left(i \sqrt{3} \operatorname{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right]^2 - (-1 + (-1)^{2/3}) \operatorname{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right]^2 - (1 + (-1)^{1/3}) \operatorname{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right]^2 - (-1)^{5/6} \sqrt{3} \right. \\
& \left. (-1 + (-1)^{1/3}) \left(2 \sqrt{3} \operatorname{ArcTan} \left[\frac{1 - \frac{2 e^{1/3} x}{d^{1/3}}}{\sqrt{3}} \right] - 2 \operatorname{Log} [d^{1/3} + e^{1/3} x] + \operatorname{Log} [d^{2/3} - d^{1/3} e^{1/3} x + e^{2/3} x^2] \right) \left(\operatorname{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] + \operatorname{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \right. \\
& \left. \operatorname{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \operatorname{Log} [d + e x^3] \right) + 2 i \sqrt{3} \left(\operatorname{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[\frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] + \operatorname{PolyLog} \left[2, \frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] \right) - \\
& 2 (-1 + (-1)^{2/3}) \left(\operatorname{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[\frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] + \operatorname{PolyLog} \left[2, \frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] \right) - \\
& 2 (-1 + (-1)^{2/3}) \left(\operatorname{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] + \operatorname{PolyLog} \left[2, -\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}} \right] \right) - \\
& 2 (1 + (-1)^{1/3}) \left(\operatorname{Log} \left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[-\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}} \right] + \operatorname{PolyLog} \left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}} \right] \right) + \\
& 2 i \sqrt{3} \left(\operatorname{Log} \left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[\frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}} \right] + \operatorname{PolyLog} \left[2, \frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}} \right] \right) - \\
& 2 (1 + (-1)^{1/3}) \left(\operatorname{Log} \left[\frac{d^{1/3}}{e^{1/3}} + x \right] \operatorname{Log} \left[\frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}} \right] + \operatorname{PolyLog} \left[2, \frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}} \right] \right) \Big) \Big)
\end{aligned}$$

Problem 137: Result unnecessarily involves higher level functions.

$$\int \frac{\operatorname{Log} [c (d + e x^3)^p]^2}{x^5} dx$$

Optimal (type 4, 1328 leaves, 48 steps):

$$\begin{aligned}
& \frac{3\sqrt{3} e^{4/3} p^2 \operatorname{ArcTan}\left[\frac{d^{1/3}-2e^{1/3}x}{\sqrt{3}d^{1/3}}\right]}{2d^{4/3}} - \frac{3e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3}x\right]}{2d^{4/3}} - \frac{e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3}x\right]^2}{4d^{4/3}} - \frac{e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3}x\right] \operatorname{Log}\left[-\frac{(-1)^{2/3}d^{1/3}+e^{1/3}x}{(1-(-1)^{2/3})d^{1/3}}\right]}{2d^{4/3}} + \\
& \frac{(-1)^{1/3} e^{4/3} p^2 \operatorname{Log}\left[\frac{(-1)^{1/3}(d^{1/3}+e^{1/3}x)}{(1+(-1)^{1/3})d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}-(-1)^{1/3}e^{1/3}x\right]}{2d^{4/3}} + \frac{(-1)^{1/3} e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}-(-1)^{1/3}e^{1/3}x\right]^2}{4d^{4/3}} - \\
& \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{Log}\left[-\frac{(-1)^{2/3}(d^{1/3}+e^{1/3}x)}{(1-(-1)^{2/3})d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}+(-1)^{2/3}e^{1/3}x\right]}{2d^{4/3}} - \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{Log}\left[\frac{(-1)^{1/3}(d^{1/3}-(-1)^{1/3}e^{1/3}x)}{(1+(-1)^{1/3})d^{1/3}}\right] \operatorname{Log}\left[d^{1/3}+(-1)^{2/3}e^{1/3}x\right]}{2d^{4/3}} - \\
& \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}+(-1)^{2/3}e^{1/3}x\right]^2}{4d^{4/3}} - \frac{e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}+e^{1/3}x\right] \operatorname{Log}\left[\frac{(-1)^{1/3}(d^{1/3}+(-1)^{2/3}e^{1/3}x)}{(1+(-1)^{1/3})d^{1/3}}\right]}{2d^{4/3}} + \\
& \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{Log}\left[-\frac{(-1)^{2/3}(d^{1/3}+e^{1/3}x)}{(1-(-1)^{2/3})d^{1/3}}\right] \operatorname{Log}\left[\frac{d^{1/3}+(-1)^{2/3}e^{1/3}x}{(1-(-1)^{2/3})d^{1/3}}\right]}{2d^{4/3}} + \frac{(-1)^{1/3} e^{4/3} p^2 \operatorname{Log}\left[d^{1/3}-(-1)^{1/3}e^{1/3}x\right] \operatorname{Log}\left[-\frac{(-1)^{2/3}(d^{1/3}+(-1)^{2/3}e^{1/3}x)}{(1-(-1)^{2/3})d^{1/3}}\right]}{2d^{4/3}} + \\
& \frac{3e^{4/3} p^2 \operatorname{Log}\left[d^{2/3}-d^{1/3}e^{1/3}x+e^{2/3}x^2\right]}{4d^{4/3}} - \frac{3ep \operatorname{Log}\left[c(d+ex^3)^p\right]}{2dx} + \frac{e^{4/3} p \operatorname{Log}\left[d^{1/3}+e^{1/3}x\right] \operatorname{Log}\left[c(d+ex^3)^p\right]}{2d^{4/3}} - \\
& \frac{(-1)^{1/3} e^{4/3} p \operatorname{Log}\left[d^{1/3}-(-1)^{1/3}e^{1/3}x\right] \operatorname{Log}\left[c(d+ex^3)^p\right]}{2d^{4/3}} + \frac{(-1)^{2/3} e^{4/3} p \operatorname{Log}\left[d^{1/3}+(-1)^{2/3}e^{1/3}x\right] \operatorname{Log}\left[c(d+ex^3)^p\right]}{2d^{4/3}} - \\
& \frac{\operatorname{Log}\left[c(d+ex^3)^p\right]^2}{4x^4} - \frac{e^{4/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}+e^{1/3}x}{(1+(-1)^{1/3})d^{1/3}}\right]}{2d^{4/3}} + \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{PolyLog}\left[2, -\frac{(-1)^{2/3}(d^{1/3}+e^{1/3}x)}{(1-(-1)^{2/3})d^{1/3}}\right]}{2d^{4/3}} - \frac{e^{4/3} p^2 \operatorname{PolyLog}\left[2, \frac{2(d^{1/3}+e^{1/3}x)}{(3-i\sqrt{3})d^{1/3}}\right]}{2d^{4/3}} + \\
& \frac{(-1)^{1/3} e^{4/3} p^2 \operatorname{PolyLog}\left[2, -\frac{(-1)^{1/3}((-1)^{2/3}d^{1/3}+e^{1/3}x)}{(1-(-1)^{2/3})d^{1/3}}\right]}{2d^{4/3}} + \frac{(-1)^{1/3} e^{4/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}-(-1)^{1/3}e^{1/3}x}{(1+(-1)^{1/3})d^{1/3}}\right]}{2d^{4/3}} - \frac{(-1)^{2/3} e^{4/3} p^2 \operatorname{PolyLog}\left[2, \frac{d^{1/3}+(-1)^{2/3}e^{1/3}x}{(1+(-1)^{1/3})d^{1/3}}\right]}{2d^{4/3}}
\end{aligned}$$

Result (type 5, 1296 leaves):

$$\begin{aligned}
& \frac{1}{4x^4} \left(\frac{1}{d} 2p \left(3ex^3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{3}, 1, \frac{2}{3}, -\frac{ex^3}{d}\right] + d \operatorname{Log}\left[d+ex^3\right] \right) \left(p \operatorname{Log}\left[d+ex^3\right] - \operatorname{Log}\left[c(d+ex^3)^p\right] \right) - \right. \\
& \left. \left(-p \operatorname{Log}\left[d+ex^3\right] + \operatorname{Log}\left[c(d+ex^3)^p\right] \right)^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& p^2 \left(-\text{Log}[d + e x^3]^2 + \frac{1}{(1 + (-1)^{1/3})^2 d^{4/3}} e x^3 \left(3 (-1)^{1/3} e^{1/3} x \text{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right]^2 + 3 (-1)^{1/3} (-1 + (-1)^{1/3}) e^{1/3} x \text{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right]^2 + \right. \right. \\
& \quad \left. \left. 3 (-1)^{1/3} (-1 + (-1)^{1/3})^2 e^{1/3} x \text{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right]^2 + 6 (1 + (-1)^{1/3})^2 \left(e^{1/3} x \text{Log}[x] - d^{1/3} \text{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] - e^{1/3} x \text{Log}[d^{1/3} + e^{1/3} x] \right) \right) + \right. \\
& \quad \left. 6 (1 + (-1)^{1/3})^2 \left((-1)^{2/3} e^{1/3} x \text{Log}[x] - d^{1/3} \text{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] - (-1)^{2/3} e^{1/3} x \text{Log}\left[-(-1)^{1/3} d^{1/3} + e^{1/3} x\right] \right) - \right. \\
& \quad \left. 6 (1 + (-1)^{1/3})^2 \left((-1)^{1/3} e^{1/3} x \text{Log}[x] + d^{1/3} \text{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] - (-1)^{1/3} e^{1/3} x \text{Log}\left[(-1)^{2/3} d^{1/3} + e^{1/3} x\right] \right) + \right. \\
& \quad \left. \left(1 + (-1)^{1/3} \right)^2 \left(6 d^{1/3} - 2 \sqrt{3} e^{1/3} x \text{ArcTan}\left[\frac{1 - \frac{2 e^{1/3} x}{d^{1/3}}}{\sqrt{3}}\right] - 2 e^{1/3} x \text{Log}[d^{1/3} + e^{1/3} x] + e^{1/3} x \text{Log}[d^{2/3} - d^{1/3} e^{1/3} x + e^{2/3} x^2] \right) \right) \\
& \quad \left(\text{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] + \text{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] + \text{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] - \text{Log}[d + e x^3] \right) + \\
& \quad 6 (-1)^{1/3} e^{1/3} x \left(\text{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[\frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \text{PolyLog}\left[2, \frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] \right) + \\
& \quad 6 (-1)^{1/3} (-1 + (-1)^{1/3}) e^{1/3} x \left(\text{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[\frac{(-1)^{1/3} d^{1/3} - e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \text{PolyLog}\left[2, \frac{d^{1/3} + e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] \right) + \\
& \quad 6 (-1)^{1/3} (-1 + (-1)^{1/3}) e^{1/3} x \left(\text{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[\frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] + \text{PolyLog}\left[2, -\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}}\right] \right) + \\
& \quad 6 (-1)^{1/3} (-1 + (-1)^{1/3})^2 e^{1/3} x \left(\text{Log}\left[-\frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[-\frac{i \left((-1)^{2/3} d^{1/3} + e^{1/3} x \right)}{\sqrt{3} d^{1/3}}\right] + \text{PolyLog}\left[2, \frac{d^{1/3} + (-1)^{2/3} e^{1/3} x}{(1 + (-1)^{1/3}) d^{1/3}}\right] \right) + \\
& \quad 6 (-1)^{1/3} e^{1/3} x \left(\text{Log}\left[\frac{(-1)^{2/3} d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[\frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}}\right] + \text{PolyLog}\left[2, \frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] \right) + \\
& \quad 6 (-1)^{1/3} (-1 + (-1)^{1/3})^2 e^{1/3} x \left(\text{Log}\left[\frac{d^{1/3}}{e^{1/3}} + x\right] \text{Log}\left[\frac{i + \sqrt{3} - \frac{2 i e^{1/3} x}{d^{1/3}}}{3 i + \sqrt{3}}\right] + \text{PolyLog}\left[2, \frac{2 i \left(1 + \frac{e^{1/3} x}{d^{1/3}} \right)}{3 i + \sqrt{3}}\right] \right) \right) \right)
\end{aligned}$$

Problem 169: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[1 + e x^n]}{x} dx$$

Optimal (type 4, 13 leaves, 1 step):

$$\frac{\text{PolyLog}[2, -e x^n]}{n}$$

Result (type 4, 30 leaves):

$$\frac{\text{Log}[-e x^n] \text{Log}[1 + e x^n] + \text{PolyLog}[2, 1 + e x^n]}{n}$$

Problem 174: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[c (d + e x^n)^p]^2}{x} dx$$

Optimal (type 4, 79 leaves, 5 steps):

$$\frac{\text{Log}\left[-\frac{e x^n}{d}\right] \text{Log}[c (d + e x^n)^p]^2}{n} + \frac{2 p \text{Log}[c (d + e x^n)^p] \text{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right]}{n} - \frac{2 p^2 \text{PolyLog}\left[3, 1 + \frac{e x^n}{d}\right]}{n}$$

Result (type 4, 164 leaves):

$$\begin{aligned} & \text{Log}[x] \left(-p \text{Log}[d + e x^n] + \text{Log}[c (d + e x^n)^p]\right)^2 + \\ & 2 p \left(-p \text{Log}[d + e x^n] + \text{Log}[c (d + e x^n)^p]\right) \left(\text{Log}[x] \left(\text{Log}[d + e x^n] - \text{Log}\left[1 + \frac{e x^n}{d}\right]\right) - \frac{\text{PolyLog}\left[2, -\frac{e x^n}{d}\right]}{n}\right) + \\ & \frac{p^2 \left(\text{Log}\left[-\frac{e x^n}{d}\right] \text{Log}[d + e x^n]^2 + 2 \text{Log}[d + e x^n] \text{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{e x^n}{d}\right]\right)}{n} \end{aligned}$$

Problem 175: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[c (d + e x^n)^p]^3}{x} dx$$

Optimal (type 4, 113 leaves, 6 steps):

$$\frac{\text{Log}\left[-\frac{e x^n}{d}\right] \text{Log}[c (d + e x^n)^p]^3}{n} + \frac{3 p \text{Log}[c (d + e x^n)^p]^2 \text{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right]}{n} - \frac{6 p^2 \text{Log}[c (d + e x^n)^p] \text{PolyLog}\left[3, 1 + \frac{e x^n}{d}\right]}{n} + \frac{6 p^3 \text{PolyLog}\left[4, 1 + \frac{e x^n}{d}\right]}{n}$$

Result (type 4, 270 leaves):

$$\frac{1}{n} \left(-n p^3 \operatorname{Log}[x] \operatorname{Log}[d + e x^n]^3 + p^3 \operatorname{Log}\left[-\frac{e x^n}{d}\right] \operatorname{Log}[d + e x^n]^3 + \right. \\ \left. 3 n p^2 \operatorname{Log}[x] \operatorname{Log}[d + e x^n]^2 \operatorname{Log}[c (d + e x^n)^p] - 3 p^2 \operatorname{Log}\left[-\frac{e x^n}{d}\right] \operatorname{Log}[d + e x^n]^2 \operatorname{Log}[c (d + e x^n)^p] - \right. \\ \left. 3 n p \operatorname{Log}[x] \operatorname{Log}[d + e x^n] \operatorname{Log}[c (d + e x^n)^p]^2 + 3 p \operatorname{Log}\left[-\frac{e x^n}{d}\right] \operatorname{Log}[d + e x^n] \operatorname{Log}[c (d + e x^n)^p]^2 + n \operatorname{Log}[x] \operatorname{Log}[c (d + e x^n)^p]^3 + \right. \\ \left. 3 p \operatorname{Log}[c (d + e x^n)^p]^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right] - 6 p^2 \operatorname{Log}[c (d + e x^n)^p] \operatorname{PolyLog}\left[3, 1 + \frac{e x^n}{d}\right] + 6 p^3 \operatorname{PolyLog}\left[4, 1 + \frac{e x^n}{d}\right] \right)$$

Problem 188: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[c (a + b x^2)^p]}{d + e x} dx$$

Optimal (type 4, 201 leaves, 9 steps):

$$-\frac{p \operatorname{Log}\left[\frac{e(\sqrt{-a}-\sqrt{b}x)}{\sqrt{b}d+\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e} - \frac{p \operatorname{Log}\left[-\frac{e(\sqrt{-a}+\sqrt{b}x)}{\sqrt{b}d-\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e} + \\ \frac{\operatorname{Log}[d+ex] \operatorname{Log}[c(a+bx^2)^p]}{e} - \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d-\sqrt{-a}e}\right]}{e} - \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d+\sqrt{-a}e}\right]}{e}$$

Result (type 4, 262 leaves):

$$\frac{1}{e} \left(-p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] - p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] + p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d-i\sqrt{a}e}\right] + \right. \\ \left. p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d+i\sqrt{a}e}\right] + \operatorname{Log}[d+ex] \operatorname{Log}[c(a+bx^2)^p] + p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a}-i\sqrt{b}x)}{i\sqrt{b}d+\sqrt{a}e}\right] + p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a}+i\sqrt{b}x)}{-i\sqrt{b}d+\sqrt{a}e}\right] \right)$$

Problem 206: Result is not expressed in closed-form.

$$\int (d + e x)^m \operatorname{Log}[c (a + b x^3)^p] dx$$

Optimal (type 5, 301 leaves, 6 steps):

$$\frac{b^{1/3} p (d + e x)^{2+m} \operatorname{Hypergeometric2F1}\left[1, 2+m, 3+m, \frac{b^{1/3} (d+e x)}{b^{1/3} d - a^{1/3} e}\right]}{e (b^{1/3} d - a^{1/3} e) (1+m) (2+m)} + \frac{b^{1/3} p (d + e x)^{2+m} \operatorname{Hypergeometric2F1}\left[1, 2+m, 3+m, \frac{b^{1/3} (d+e x)}{b^{1/3} d + (-1)^{1/3} a^{1/3} e}\right]}{e (b^{1/3} d + (-1)^{1/3} a^{1/3} e) (1+m) (2+m)} +$$

$$\frac{b^{1/3} p (d + e x)^{2+m} \operatorname{Hypergeometric2F1}\left[1, 2+m, 3+m, \frac{b^{1/3} (d+e x)}{b^{1/3} d - (-1)^{2/3} a^{1/3} e}\right]}{e (b^{1/3} d - (-1)^{2/3} a^{1/3} e) (1+m) (2+m)} + \frac{(d + e x)^{1+m} \operatorname{Log}[c (a + b x^3)^p]}{e (1+m)}$$

Result (type 7, 399 leaves):

$$\frac{1}{b e m (1+m)^2}$$

$$(d + e x)^m \left(- (b d^3 - a e^3) (1+m) p \operatorname{RootSum}\left[b d^3 - a e^3 - 3 b d^2 \#1 + 3 b d \#1^2 - b \#1^3 \&, \frac{\operatorname{Hypergeometric2F1}\left[-m, -m, 1-m, -\frac{\#1}{d+e x-\#1}\right] \left(\frac{d+e x}{d+e x-\#1}\right)^{-m}}{d^2 - 2 d \#1 + \#1^2}\right] \& \right) +$$

$$b \left(m (d + e x) (-3 p + (1+m) \operatorname{Log}[c (a + b x^3)^p]) + \right.$$

$$2 d^2 (1+m) p \operatorname{RootSum}\left[b d^3 - a e^3 - 3 b d^2 \#1 + 3 b d \#1^2 - b \#1^3 \&, \frac{\operatorname{Hypergeometric2F1}\left[-m, -m, 1-m, -\frac{\#1}{d+e x-\#1}\right] \left(\frac{d+e x}{d+e x-\#1}\right)^{-m} \#1}{d^2 - 2 d \#1 + \#1^2}\right] \& \left. - \right.$$

$$d (1+m) p \operatorname{RootSum}\left[b d^3 - a e^3 - 3 b d^2 \#1 + 3 b d \#1^2 - b \#1^3 \&, \frac{\operatorname{Hypergeometric2F1}\left[-m, -m, 1-m, -\frac{\#1}{d+e x-\#1}\right] \left(\frac{d+e x}{d+e x-\#1}\right)^{-m} \#1^2}{d^2 - 2 d \#1 + \#1^2}\right] \& \left. \right)$$

Problem 207: Result unnecessarily involves imaginary or complex numbers.

$$\int (d + e x)^m \operatorname{Log}[c (a + b x^2)^p] dx$$

Optimal (type 5, 205 leaves, 5 steps):

$$\frac{\sqrt{b} p (d + e x)^{2+m} \operatorname{Hypergeometric2F1}\left[1, 2+m, 3+m, \frac{\sqrt{b} (d+e x)}{\sqrt{b} d - \sqrt{-a} e}\right]}{e (\sqrt{b} d - \sqrt{-a} e) (1+m) (2+m)} +$$

$$\frac{\sqrt{b} p (d + e x)^{2+m} \operatorname{Hypergeometric2F1}\left[1, 2+m, 3+m, \frac{\sqrt{b} (d+e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e (\sqrt{b} d + \sqrt{-a} e) (1+m) (2+m)} + \frac{(d + e x)^{1+m} \operatorname{Log}[c (a + b x^2)^p]}{e (1+m)}$$

Result (type 5, 285 leaves):

$$\frac{1}{\sqrt{b} e m (1+m)^2} (d+ex)^m \left(-(\sqrt{b} d + i \sqrt{a} e) (1+m) p \left(\frac{\sqrt{b} (d+ex)}{e (-i \sqrt{a} + \sqrt{b} x)} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{\sqrt{b} d + i \sqrt{a} e}{i \sqrt{a} e - \sqrt{b} ex} \right] - (\sqrt{b} d - i \sqrt{a} e) (1+m) p \left(\frac{\sqrt{b} (d+ex)}{e (i \sqrt{a} + \sqrt{b} x)} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\sqrt{b} d - i \sqrt{a} e}{i \sqrt{a} e + \sqrt{b} ex} \right] + \sqrt{b} m (d+ex) (-2p + (1+m) \text{Log}[c (a+bx^2)^p]) \right)$$

Problem 210: Result unnecessarily involves imaginary or complex numbers.

$$\int (d+ex)^m \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] dx$$

Optimal (type 5, 257 leaves, 9 steps):

$$\frac{\sqrt{-a} p (d+ex)^{2+m} \text{Hypergeometric2F1} \left[1, 2+m, 3+m, \frac{\sqrt{-a} (d+ex)}{\sqrt{-a} d - \sqrt{b} e} \right]}{e (\sqrt{-a} d - \sqrt{b} e) (1+m) (2+m)} + \frac{\sqrt{-a} p (d+ex)^{2+m} \text{Hypergeometric2F1} \left[1, 2+m, 3+m, \frac{\sqrt{-a} (d+ex)}{\sqrt{-a} d + \sqrt{b} e} \right]}{e (\sqrt{-a} d + \sqrt{b} e) (1+m) (2+m)} - \frac{2p (d+ex)^{2+m} \text{Hypergeometric2F1} \left[1, 2+m, 3+m, 1 + \frac{ex}{d} \right]}{d e (2+3m+m^2)} + \frac{(d+ex)^{1+m} \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right]}{e (1+m)}$$

Result (type 5, 310 leaves):

$$\frac{1}{e m (1+m)} (d+ex)^m \left(2 d p \left(1 + \frac{d}{ex} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{d}{ex} \right] - \frac{(\sqrt{a} d + i \sqrt{b} e) p \left(\frac{\sqrt{a} (d+ex)}{e (-i \sqrt{b} + \sqrt{a} x)} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, \frac{\sqrt{a} d + i \sqrt{b} e}{i \sqrt{b} e - \sqrt{a} ex} \right]}{\sqrt{a}} - \frac{(\sqrt{a} d - i \sqrt{b} e) p \left(\frac{\sqrt{a} (d+ex)}{e (i \sqrt{b} + \sqrt{a} x)} \right)^{-m} \text{Hypergeometric2F1} \left[-m, -m, 1-m, -\frac{\sqrt{a} d - i \sqrt{b} e}{i \sqrt{b} e + \sqrt{a} ex} \right]}{\sqrt{a}} + m (d+ex) \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] \right)$$

Problem 216: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{f + g x} dx$$

Optimal (type 9, 22 leaves, 0 steps):

$$\text{Unintegrable}\left[\frac{\text{Log}[c (d + e x^n)^p]}{f + g x}, x\right]$$

Result (type 1, 1 leaves):

???

Problem 226: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 \text{Log}[c (a + b x^2)^p]}{d + e x} dx$$

Optimal (type 4, 394 leaves, 21 steps):

$$\begin{aligned} & -\frac{2 d^2 p x}{e^3} + \frac{2 a p x}{3 b e} + \frac{d p x^2}{2 e^2} - \frac{2 p x^3}{9 e} + \frac{2 \sqrt{a} d^2 p \text{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{\sqrt{b} e^3} - \frac{2 a^{3/2} p \text{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{3 b^{3/2} e} + \\ & \frac{d^3 p \text{Log}\left[\frac{e(\sqrt{-a}-\sqrt{b} x)}{\sqrt{b} d+\sqrt{-a} e}\right] \text{Log}[d+e x]}{e^4} + \frac{d^3 p \text{Log}\left[-\frac{e(\sqrt{-a}+\sqrt{b} x)}{\sqrt{b} d-\sqrt{-a} e}\right] \text{Log}[d+e x]}{e^4} + \frac{d^2 x \text{Log}[c (a+b x^2)^p]}{e^3} + \frac{x^3 \text{Log}[c (a+b x^2)^p]}{3 e} - \\ & \frac{d (a+b x^2) \text{Log}[c (a+b x^2)^p]}{2 b e^2} - \frac{d^3 \text{Log}[d+e x] \text{Log}[c (a+b x^2)^p]}{e^4} + \frac{d^3 p \text{PolyLog}\left[2, \frac{\sqrt{b} (d+e x)}{\sqrt{b} d-\sqrt{-a} e}\right]}{e^4} + \frac{d^3 p \text{PolyLog}\left[2, \frac{\sqrt{b} (d+e x)}{\sqrt{b} d+\sqrt{-a} e}\right]}{e^4} \end{aligned}$$

Result (type 4, 509 leaves):

$$\begin{aligned}
& -\frac{1}{18e^4} \left(36d^2 e p x - \frac{12ae^3 p x}{b} - 9d^2 e^2 p x^2 + 4e^3 p x^3 + \frac{12a^{3/2} e^3 p \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right]}{b^{3/2}} + \frac{18i\sqrt{a}d^2 e p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right]}{\sqrt{b}} - \frac{18i\sqrt{a}d^2 e p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right]}{\sqrt{b}} \right. \\
& 18d^3 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] - 18d^3 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] + 18d^3 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d - i\sqrt{a}e}\right] + \\
& 18d^3 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d + i\sqrt{a}e}\right] + \frac{9ad^2 e^2 p \operatorname{Log}[a+bx^2]}{b} - 18d^2 ex \operatorname{Log}[c(a+bx^2)^p] + 9d^2 e^2 x^2 \operatorname{Log}[c(a+bx^2)^p] - \\
& \left. 6e^3 x^3 \operatorname{Log}[c(a+bx^2)^p] + 18d^3 \operatorname{Log}[d+ex] \operatorname{Log}[c(a+bx^2)^p] + 18d^3 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} - i\sqrt{b}x)}{i\sqrt{b}d + \sqrt{a}e}\right] + 18d^3 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} + i\sqrt{b}x)}{-i\sqrt{b}d + \sqrt{a}e}\right] \right)
\end{aligned}$$

Problem 227: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 \operatorname{Log}[c(a+bx^2)^p]}{d+ex} dx$$

Optimal (type 4, 313 leaves, 17 steps):

$$\begin{aligned}
& \frac{2dp}{e^2} - \frac{px^2}{2e} - \frac{2\sqrt{a}dp \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right]}{\sqrt{b}e^2} - \frac{d^2 p \operatorname{Log}\left[\frac{e(\sqrt{-a}-\sqrt{b}x)}{\sqrt{b}d+\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e^3} - \frac{d^2 p \operatorname{Log}\left[-\frac{e(\sqrt{-a}+\sqrt{b}x)}{\sqrt{b}d-\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e^3} - \frac{dx \operatorname{Log}[c(a+bx^2)^p]}{e^2} + \\
& \frac{(a+bx^2) \operatorname{Log}[c(a+bx^2)^p]}{2be} + \frac{d^2 \operatorname{Log}[d+ex] \operatorname{Log}[c(a+bx^2)^p]}{e^3} - \frac{d^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d-\sqrt{-a}e}\right]}{e^3} - \frac{d^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d+\sqrt{-a}e}\right]}{e^3}
\end{aligned}$$

Result (type 4, 438 leaves):

$$\begin{aligned}
& \frac{1}{2be^3} \left(4bd e p x - b e^2 p x^2 + 2i\sqrt{a}\sqrt{b}d e p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] - 2i\sqrt{a}\sqrt{b}d e p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] - \right. \\
& 2bd^2 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] - 2bd^2 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] + 2bd^2 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d - i\sqrt{a}e}\right] + \\
& 2bd^2 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d + i\sqrt{a}e}\right] + a e^2 p \operatorname{Log}[a+bx^2] - 2bd ex \operatorname{Log}[c(a+bx^2)^p] + b e^2 x^2 \operatorname{Log}[c(a+bx^2)^p] + \\
& \left. 2bd^2 \operatorname{Log}[d+ex] \operatorname{Log}[c(a+bx^2)^p] + 2bd^2 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} - i\sqrt{b}x)}{i\sqrt{b}d + \sqrt{a}e}\right] + 2bd^2 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} + i\sqrt{b}x)}{-i\sqrt{b}d + \sqrt{a}e}\right] \right)
\end{aligned}$$

Problem 228: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x \operatorname{Log}[c(a + bx^2)^p]}{d + ex} dx$$

Optimal (type 4, 256 leaves, 14 steps):

$$\begin{aligned} & -\frac{2px}{e} + \frac{2\sqrt{a} p \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right]}{\sqrt{b}e} + \frac{d p \operatorname{Log}\left[\frac{e(\sqrt{-a}-\sqrt{b}x)}{\sqrt{b}d+\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e^2} + \frac{d p \operatorname{Log}\left[-\frac{e(\sqrt{-a}+\sqrt{b}x)}{\sqrt{b}d-\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e^2} + \\ & \frac{x \operatorname{Log}[c(a + bx^2)^p]}{e} - \frac{d \operatorname{Log}[d+ex] \operatorname{Log}[c(a + bx^2)^p]}{e^2} + \frac{d p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d-\sqrt{-a}e}\right]}{e^2} + \frac{d p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d+\sqrt{-a}e}\right]}{e^2} \end{aligned}$$

Result (type 4, 357 leaves):

$$\begin{aligned} & -\frac{1}{e^2} \left(2epx + \frac{i\sqrt{a}ep \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right]}{\sqrt{b}} - \frac{i\sqrt{a}ep \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right]}{\sqrt{b}} - d p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] - \right. \\ & \left. d p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+ex] + d p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d-i\sqrt{a}e}\right] + d p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d+i\sqrt{a}e}\right] - \right. \\ & \left. ex \operatorname{Log}[c(a + bx^2)^p] + d \operatorname{Log}[d+ex] \operatorname{Log}[c(a + bx^2)^p] + d p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a}-i\sqrt{b}x)}{i\sqrt{b}d+\sqrt{a}e}\right] + d p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a}+i\sqrt{b}x)}{-i\sqrt{b}d+\sqrt{a}e}\right] \right) \end{aligned}$$

Problem 229: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[c(a + bx^2)^p]}{d + ex} dx$$

Optimal (type 4, 201 leaves, 9 steps):

$$\begin{aligned} & -\frac{p \operatorname{Log}\left[\frac{e(\sqrt{-a}-\sqrt{b}x)}{\sqrt{b}d+\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e} - \frac{p \operatorname{Log}\left[-\frac{e(\sqrt{-a}+\sqrt{b}x)}{\sqrt{b}d-\sqrt{-a}e}\right] \operatorname{Log}[d+ex]}{e} + \\ & \frac{\operatorname{Log}[d+ex] \operatorname{Log}[c(a + bx^2)^p]}{e} - \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d-\sqrt{-a}e}\right]}{e} - \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d+\sqrt{-a}e}\right]}{e} \end{aligned}$$

Result (type 4, 262 leaves):

$$\frac{1}{e} \left(-p \operatorname{Log} \left[-\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} [d + ex] - p \operatorname{Log} \left[\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} [d + ex] + p \operatorname{Log} \left[\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} \left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d - i\sqrt{a}e} \right] + \right. \\ \left. p \operatorname{Log} \left[-\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} \left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d + i\sqrt{a}e} \right] + \operatorname{Log} [d + ex] \operatorname{Log} [c(a + bx^2)^p] + p \operatorname{PolyLog} \left[2, \frac{e(\sqrt{a} - i\sqrt{b}x)}{i\sqrt{b}d + \sqrt{a}e} \right] + p \operatorname{PolyLog} \left[2, \frac{e(\sqrt{a} + i\sqrt{b}x)}{-i\sqrt{b}d + \sqrt{a}e} \right] \right)$$

Problem 230: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log} [c(a + bx^2)^p]}{x(d + ex)} dx$$

Optimal (type 4, 247 leaves, 14 steps):

$$\frac{p \operatorname{Log} \left[\frac{e(\sqrt{-a} - \sqrt{b}x)}{\sqrt{b}d + \sqrt{-a}e} \right] \operatorname{Log} [d + ex]}{d} + \frac{p \operatorname{Log} \left[-\frac{e(\sqrt{-a} + \sqrt{b}x)}{\sqrt{b}d - \sqrt{-a}e} \right] \operatorname{Log} [d + ex]}{d} + \frac{\operatorname{Log} \left[-\frac{bx^2}{a} \right] \operatorname{Log} [c(a + bx^2)^p]}{2d} - \\ \frac{\operatorname{Log} [d + ex] \operatorname{Log} [c(a + bx^2)^p]}{d} + \frac{p \operatorname{PolyLog} \left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d - \sqrt{-a}e} \right]}{d} + \frac{p \operatorname{PolyLog} \left[2, \frac{\sqrt{b}(d+ex)}{\sqrt{b}d + \sqrt{-a}e} \right]}{d} + \frac{p \operatorname{PolyLog} \left[2, 1 + \frac{bx^2}{a} \right]}{2d}$$

Result (type 4, 361 leaves):

$$-\frac{1}{d} \left(p \operatorname{Log} [x] \operatorname{Log} \left[1 - \frac{i\sqrt{b}x}{\sqrt{a}} \right] + p \operatorname{Log} [x] \operatorname{Log} \left[1 + \frac{i\sqrt{b}x}{\sqrt{a}} \right] - p \operatorname{Log} \left[-\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} [d + ex] - p \operatorname{Log} \left[\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} [d + ex] + \right. \\ \left. p \operatorname{Log} \left[\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} \left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d - i\sqrt{a}e} \right] + p \operatorname{Log} \left[-\frac{i\sqrt{a}}{\sqrt{b}} + x \right] \operatorname{Log} \left[\frac{\sqrt{b}(d+ex)}{\sqrt{b}d + i\sqrt{a}e} \right] - \operatorname{Log} [x] \operatorname{Log} [c(a + bx^2)^p] + \operatorname{Log} [d + ex] \operatorname{Log} [c(a + bx^2)^p] + \right. \\ \left. p \operatorname{PolyLog} \left[2, -\frac{i\sqrt{b}x}{\sqrt{a}} \right] + p \operatorname{PolyLog} \left[2, \frac{i\sqrt{b}x}{\sqrt{a}} \right] + p \operatorname{PolyLog} \left[2, \frac{e(\sqrt{a} - i\sqrt{b}x)}{i\sqrt{b}d + \sqrt{a}e} \right] + p \operatorname{PolyLog} \left[2, \frac{e(\sqrt{a} + i\sqrt{b}x)}{-i\sqrt{b}d + \sqrt{a}e} \right] \right)$$

Problem 231: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log} [c(a + bx^2)^p]}{x^2(d + ex)} dx$$

Optimal (type 4, 306 leaves, 16 steps):

$$\frac{2\sqrt{b} p \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{\sqrt{a} d} - \frac{e p \operatorname{Log}\left[\frac{e^{\left(\sqrt{-a}-\sqrt{b} x\right)}}{\sqrt{b} d+\sqrt{-a} e}\right] \operatorname{Log}[d+e x]}{d^2} - \frac{e p \operatorname{Log}\left[-\frac{e^{\left(\sqrt{-a}+\sqrt{b} x\right)}}{\sqrt{b} d-\sqrt{-a} e}\right] \operatorname{Log}[d+e x]}{d^2} -$$

$$\frac{\operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{d x} - \frac{e \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{2 d^2} + \frac{e \operatorname{Log}[d+e x] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{d^2} -$$

$$\frac{e p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+e x)}{\sqrt{b} d-\sqrt{-a} e}\right]}{d^2} - \frac{e p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+e x)}{\sqrt{b} d+\sqrt{-a} e}\right]}{d^2} - \frac{e p \operatorname{PolyLog}\left[2, 1+\frac{b x^2}{a}\right]}{2 d^2}$$

Result (type 4, 417 leaves):

$$\frac{1}{d^2} \left(\frac{2\sqrt{b} d p \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{\sqrt{a}} + e p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{b} x}{\sqrt{a}}\right] + e p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{b} x}{\sqrt{a}}\right] - \right.$$

$$e p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+e x] - e p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d+e x] + e p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+e x)}{\sqrt{b} d - i\sqrt{a} e}\right] +$$

$$e p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d+e x)}{\sqrt{b} d + i\sqrt{a} e}\right] - \frac{d \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{x} - e \operatorname{Log}[x] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right] + e \operatorname{Log}[d+e x] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right] +$$

$$\left. e p \operatorname{PolyLog}\left[2, -\frac{i\sqrt{b} x}{\sqrt{a}}\right] + e p \operatorname{PolyLog}\left[2, \frac{i\sqrt{b} x}{\sqrt{a}}\right] + e p \operatorname{PolyLog}\left[2, \frac{e\left(\sqrt{a}-i\sqrt{b} x\right)}{i\sqrt{b} d+\sqrt{a} e}\right] + e p \operatorname{PolyLog}\left[2, \frac{e\left(\sqrt{a}+i\sqrt{b} x\right)}{-i\sqrt{b} d+\sqrt{a} e}\right] \right)$$

Problem 232: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{x^3(d+e x)} dx$$

Optimal (type 4, 371 leaves, 21 steps):

$$-\frac{2\sqrt{b} e p \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{\sqrt{a} d^2} + \frac{b p \operatorname{Log}[x]}{a d} + \frac{e^2 p \operatorname{Log}\left[\frac{e^{\left(\sqrt{-a}-\sqrt{b} x\right)}}{\sqrt{b} d+\sqrt{-a} e}\right] \operatorname{Log}[d+e x]}{d^3} + \frac{e^2 p \operatorname{Log}\left[-\frac{e^{\left(\sqrt{-a}+\sqrt{b} x\right)}}{\sqrt{b} d-\sqrt{-a} e}\right] \operatorname{Log}[d+e x]}{d^3} -$$

$$\frac{b p \operatorname{Log}\left[a+b x^2\right]}{2 a d} - \frac{\operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{2 d x^2} + \frac{e \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{d^2 x} + \frac{e^2 \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{2 d^3} -$$

$$\frac{e^2 \operatorname{Log}[d+e x] \operatorname{Log}\left[c\left(a+b x^2\right)^p\right]}{d^3} + \frac{e^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+e x)}{\sqrt{b} d-\sqrt{-a} e}\right]}{d^3} + \frac{e^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{b}(d+e x)}{\sqrt{b} d+\sqrt{-a} e}\right]}{d^3} + \frac{e^2 p \operatorname{PolyLog}\left[2, 1+\frac{b x^2}{a}\right]}{2 d^3}$$

Result (type 4, 503 leaves):

$$\begin{aligned}
 & -\frac{1}{2d^3} \left(\frac{4\sqrt{b} d e p \operatorname{ArcTan}\left[\frac{\sqrt{b}x}{\sqrt{a}}\right]}{\sqrt{a}} - \frac{2bd^2 p \operatorname{Log}[x]}{a} + 2e^2 p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 2e^2 p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{b}x}{\sqrt{a}}\right] - \right. \\
 & 2e^2 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d + ex] - 2e^2 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[d + ex] + 2e^2 p \operatorname{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d + ex)}{\sqrt{b}d - i\sqrt{a}e}\right] + \\
 & 2e^2 p \operatorname{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{\sqrt{b}(d + ex)}{\sqrt{b}d + i\sqrt{a}e}\right] + \frac{bd^2 p \operatorname{Log}[a + bx^2]}{a} + \frac{d^2 \operatorname{Log}[c(a + bx^2)^p]}{x^2} - \frac{2de \operatorname{Log}[c(a + bx^2)^p]}{x} - \\
 & 2e^2 \operatorname{Log}[x] \operatorname{Log}[c(a + bx^2)^p] + 2e^2 \operatorname{Log}[d + ex] \operatorname{Log}[c(a + bx^2)^p] + 2e^2 p \operatorname{PolyLog}\left[2, -\frac{i\sqrt{b}x}{\sqrt{a}}\right] + \\
 & \left. 2e^2 p \operatorname{PolyLog}\left[2, \frac{i\sqrt{b}x}{\sqrt{a}}\right] + 2e^2 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} - i\sqrt{b}x)}{i\sqrt{b}d + \sqrt{a}e}\right] + 2e^2 p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{a} + i\sqrt{b}x)}{-i\sqrt{b}d + \sqrt{a}e}\right] \right)
 \end{aligned}$$

Problem 247: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{d + ex} dx$$

Optimal (type 4, 421 leaves, 25 steps):

$$\begin{aligned}
 & \frac{2bp}{3ae} + \frac{2\sqrt{b}d^2 p \operatorname{ArcTan}\left[\frac{\sqrt{a}x}{\sqrt{b}}\right]}{\sqrt{a}e^3} - \frac{2b^{3/2} p \operatorname{ArcTan}\left[\frac{\sqrt{a}x}{\sqrt{b}}\right]}{3a^{3/2}e} + \frac{d^2 x \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{e^3} - \frac{dx^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{2e^2} + \frac{x^3 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{3e} - \\
 & \frac{d^3 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d + ex]}{e^4} - \frac{2d^3 p \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d + ex]}{e^4} + \frac{d^3 p \operatorname{Log}\left[\frac{e(\sqrt{b} - \sqrt{-a}x)}{\sqrt{-a}d + \sqrt{b}e}\right] \operatorname{Log}[d + ex]}{e^4} + \frac{d^3 p \operatorname{Log}\left[-\frac{e(\sqrt{b} + \sqrt{-a}x)}{\sqrt{-a}d - \sqrt{b}e}\right] \operatorname{Log}[d + ex]}{e^4} - \\
 & \frac{bd p \operatorname{Log}[b + ax^2]}{2ae^2} + \frac{d^3 p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d - \sqrt{b}e}\right]}{e^4} + \frac{d^3 p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d + \sqrt{b}e}\right]}{e^4} - \frac{2d^3 p \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right]}{e^4}
 \end{aligned}$$

Result (type 4, 528 leaves):

$$\begin{aligned}
& -\frac{1}{6e^4} \left(-\frac{4be^3px}{a} + \frac{4b^{3/2}e^3p \operatorname{ArcTan}\left[\frac{\sqrt{a}x}{\sqrt{b}}\right]}{a^{3/2}} - 6d^2ex \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] + 3de^2x^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] - \right. \\
& 2e^3x^3 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] + \frac{6i\sqrt{b}d^2ep \operatorname{Log}\left[-\frac{i\sqrt{b}}{\sqrt{a}} + x\right]}{\sqrt{a}} - \frac{6i\sqrt{b}d^2ep \operatorname{Log}\left[\frac{i\sqrt{b}}{\sqrt{a}} + x\right]}{\sqrt{a}} + 6d^3 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d+ex] + \\
& 12d^3p \operatorname{Log}[x] \operatorname{Log}[d+ex] - 6d^3p \operatorname{Log}\left[-\frac{i\sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d+ex] - 6d^3p \operatorname{Log}\left[\frac{i\sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d+ex] + \\
& 6d^3p \operatorname{Log}\left[\frac{i\sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+ex)}{\sqrt{a}d - i\sqrt{b}e}\right] + 6d^3p \operatorname{Log}\left[-\frac{i\sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+ex)}{\sqrt{a}d + i\sqrt{b}e}\right] - 12d^3p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{ex}{d}\right] + \\
& \left. \frac{3bd^2ep \operatorname{Log}[b+ax^2]}{a} - 12d^3p \operatorname{PolyLog}\left[2, -\frac{ex}{d}\right] + 6d^3p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} - i\sqrt{a}x)}{i\sqrt{a}d + \sqrt{b}e}\right] + 6d^3p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} + i\sqrt{a}x)}{-i\sqrt{a}d + \sqrt{b}e}\right] \right)
\end{aligned}$$

Problem 248: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{d+ex} dx$$

Optimal (type 4, 353 leaves, 21 steps):

$$\begin{aligned}
& -\frac{2\sqrt{b}dp \operatorname{ArcTan}\left[\frac{\sqrt{a}x}{\sqrt{b}}\right]}{\sqrt{a}e^2} - \frac{dx \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{e^2} + \frac{x^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{2e} + \frac{d^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d+ex]}{e^3} + \\
& \frac{2d^2p \operatorname{Log}\left[-\frac{ex}{d}\right] \operatorname{Log}[d+ex]}{e^3} - \frac{d^2p \operatorname{Log}\left[\frac{e(\sqrt{b}-\sqrt{-a}x)}{\sqrt{-a}d+\sqrt{b}e}\right] \operatorname{Log}[d+ex]}{e^3} - \frac{d^2p \operatorname{Log}\left[-\frac{e(\sqrt{b}+\sqrt{-a}x)}{\sqrt{-a}d-\sqrt{b}e}\right] \operatorname{Log}[d+ex]}{e^3} + \\
& \frac{bp \operatorname{Log}[b+ax^2]}{2ae} - \frac{d^2p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d-\sqrt{b}e}\right]}{e^3} - \frac{d^2p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d+\sqrt{b}e}\right]}{e^3} + \frac{2d^2p \operatorname{PolyLog}\left[2, 1 + \frac{ex}{d}\right]}{e^3}
\end{aligned}$$

Result (type 4, 470 leaves):

$$\begin{aligned} & \frac{1}{2 a e^3} \left(-2 a d e x \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] + a e^2 x^2 \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] + 2 i \sqrt{a} \sqrt{b} d e p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right] - 2 i \sqrt{a} \sqrt{b} d e p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right] + \right. \\ & 2 a d^2 \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] \operatorname{Log}[d+e x] + 4 a d^2 p \operatorname{Log}[x] \operatorname{Log}[d+e x] - 2 a d^2 p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}[d+e x] - 2 a d^2 p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}[d+e x] + \\ & 2 a d^2 p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d-i \sqrt{b} e}\right] + 2 a d^2 p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d+i \sqrt{b} e}\right] - 4 a d^2 p \operatorname{Log}[x] \operatorname{Log}\left[1+\frac{e x}{d}\right] + \\ & \left. b e^2 p \operatorname{Log}[b+a x^2] - 4 a d^2 p \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right] + 2 a d^2 p \operatorname{PolyLog}\left[2,\frac{e\left(\sqrt{b}-i \sqrt{a} x\right)}{i \sqrt{a} d+\sqrt{b} e}\right] + 2 a d^2 p \operatorname{PolyLog}\left[2,\frac{e\left(\sqrt{b}+i \sqrt{a} x\right)}{-i \sqrt{a} d+\sqrt{b} e}\right] \right) \end{aligned}$$

Problem 249: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]}{d+e x} dx$$

Optimal (type 4, 291 leaves, 18 steps):

$$\begin{aligned} & \frac{2 \sqrt{b} p \operatorname{ArcTan}\left[\frac{\sqrt{a} x}{\sqrt{b}}\right]}{\sqrt{a} e} + \frac{x \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]}{e} - \frac{d \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] \operatorname{Log}[d+e x]}{e^2} - \frac{2 d p \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d+e x]}{e^2} + \frac{d p \operatorname{Log}\left[\frac{e\left(\sqrt{b}-\sqrt{-a} x\right)}{\sqrt{-a} d+\sqrt{b} e}\right] \operatorname{Log}[d+e x]}{e^2} + \\ & \frac{d p \operatorname{Log}\left[-\frac{e\left(\sqrt{b}+\sqrt{-a} x\right)}{\sqrt{-a} d-\sqrt{b} e}\right] \operatorname{Log}[d+e x]}{e^2} + \frac{d p \operatorname{PolyLog}\left[2,\frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d-\sqrt{b} e}\right]}{e^2} + \frac{d p \operatorname{PolyLog}\left[2,\frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d+\sqrt{b} e}\right]}{e^2} - \frac{2 d p \operatorname{PolyLog}\left[2,1+\frac{e x}{d}\right]}{e^2} \end{aligned}$$

Result (type 4, 392 leaves):

$$\begin{aligned} & -\frac{1}{e^2} \left(-e x \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] + \frac{i \sqrt{b} e p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right]}{\sqrt{a}} - \frac{i \sqrt{b} e p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right]}{\sqrt{a}} + \right. \\ & d \operatorname{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] \operatorname{Log}[d+e x] + 2 d p \operatorname{Log}[x] \operatorname{Log}[d+e x] - d p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}[d+e x] - d p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}[d+e x] + \\ & d p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d-i \sqrt{b} e}\right] + d p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}}+x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d+i \sqrt{b} e}\right] - 2 d p \operatorname{Log}[x] \operatorname{Log}\left[1+\frac{e x}{d}\right] - \\ & \left. 2 d p \operatorname{PolyLog}\left[2,-\frac{e x}{d}\right] + d p \operatorname{PolyLog}\left[2,\frac{e\left(\sqrt{b}-i \sqrt{a} x\right)}{i \sqrt{a} d+\sqrt{b} e}\right] + d p \operatorname{PolyLog}\left[2,\frac{e\left(\sqrt{b}+i \sqrt{a} x\right)}{-i \sqrt{a} d+\sqrt{b} e}\right] \right) \end{aligned}$$

Problem 250: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right]}{d + e x} dx$$

Optimal (type 4, 241 leaves, 13 steps):

$$\frac{\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right] \text{Log}[d + e x]}{e} + \frac{2 p \text{Log}\left[-\frac{e x}{d}\right] \text{Log}[d + e x]}{e} - \frac{p \text{Log}\left[\frac{e(\sqrt{b} - \sqrt{-a} x)}{\sqrt{-a} d + \sqrt{b} e}\right] \text{Log}[d + e x]}{e} -$$

$$\frac{p \text{Log}\left[-\frac{e(\sqrt{b} + \sqrt{-a} x)}{\sqrt{-a} d - \sqrt{b} e}\right] \text{Log}[d + e x]}{e} - \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d - \sqrt{b} e}\right]}{e} - \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d + \sqrt{b} e}\right]}{e} + \frac{2 p \text{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{e}$$

Result (type 4, 299 leaves):

$$\frac{1}{e} \left(\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right] \text{Log}[d + e x] + 2 p \text{Log}[x] \text{Log}[d + e x] - p \text{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \text{Log}[d + e x] -$$

$$p \text{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \text{Log}[d + e x] + p \text{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \text{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d - i \sqrt{b} e}\right] + p \text{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \text{Log}\left[\frac{\sqrt{a}(d+e x)}{\sqrt{a} d + i \sqrt{b} e}\right] -$$

$$2 p \text{Log}[x] \text{Log}\left[1 + \frac{e x}{d}\right] - 2 p \text{PolyLog}\left[2, -\frac{e x}{d}\right] + p \text{PolyLog}\left[2, \frac{e(\sqrt{b} - i \sqrt{a} x)}{i \sqrt{a} d + \sqrt{b} e}\right] + p \text{PolyLog}\left[2, \frac{e(\sqrt{b} + i \sqrt{a} x)}{-i \sqrt{a} d + \sqrt{b} e}\right] \right)$$

Problem 251: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right]}{x (d + e x)} dx$$

Optimal (type 4, 287 leaves, 18 steps):

$$-\frac{\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right] \text{Log}\left[-\frac{b}{a x^2}\right]}{2 d} - \frac{\text{Log}\left[c \left(a + \frac{b}{x^2}\right)^p\right] \text{Log}[d + e x]}{d} - \frac{2 p \text{Log}\left[-\frac{e x}{d}\right] \text{Log}[d + e x]}{d} + \frac{p \text{Log}\left[\frac{e(\sqrt{b} - \sqrt{-a} x)}{\sqrt{-a} d + \sqrt{b} e}\right] \text{Log}[d + e x]}{d} +$$

$$\frac{p \text{Log}\left[-\frac{e(\sqrt{b} + \sqrt{-a} x)}{\sqrt{-a} d - \sqrt{b} e}\right] \text{Log}[d + e x]}{d} - \frac{p \text{PolyLog}\left[2, 1 + \frac{b}{a x^2}\right]}{2 d} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d - \sqrt{b} e}\right]}{d} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-a}(d+e x)}{\sqrt{-a} d + \sqrt{b} e}\right]}{d} - \frac{2 p \text{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{d}$$

Result (type 4, 405 leaves):

$$\begin{aligned}
& -\frac{1}{d} \left(-\text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] \text{Log}[x] - p \text{Log}[x]^2 + p \text{Log}[x] \text{Log} \left[1 - \frac{i\sqrt{a}x}{\sqrt{b}} \right] + p \text{Log}[x] \text{Log} \left[1 + \frac{i\sqrt{a}x}{\sqrt{b}} \right] + \right. \\
& \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] \text{Log}[d+ex] + 2p \text{Log}[x] \text{Log}[d+ex] - p \text{Log} \left[-\frac{i\sqrt{b}}{\sqrt{a}} + x \right] \text{Log}[d+ex] - p \text{Log} \left[\frac{i\sqrt{b}}{\sqrt{a}} + x \right] \text{Log}[d+ex] + \\
& p \text{Log} \left[\frac{i\sqrt{b}}{\sqrt{a}} + x \right] \text{Log} \left[\frac{\sqrt{a}(d+ex)}{\sqrt{a}d - i\sqrt{b}e} \right] + p \text{Log} \left[-\frac{i\sqrt{b}}{\sqrt{a}} + x \right] \text{Log} \left[\frac{\sqrt{a}(d+ex)}{\sqrt{a}d + i\sqrt{b}e} \right] - 2p \text{Log}[x] \text{Log} \left[1 + \frac{ex}{d} \right] + p \text{PolyLog} \left[2, -\frac{i\sqrt{a}x}{\sqrt{b}} \right] + \\
& \left. p \text{PolyLog} \left[2, \frac{i\sqrt{a}x}{\sqrt{b}} \right] - 2p \text{PolyLog} \left[2, -\frac{ex}{d} \right] + p \text{PolyLog} \left[2, \frac{e(\sqrt{b} - i\sqrt{a}x)}{i\sqrt{a}d + \sqrt{b}e} \right] + p \text{PolyLog} \left[2, \frac{e(\sqrt{b} + i\sqrt{a}x)}{-i\sqrt{a}d + \sqrt{b}e} \right] \right)
\end{aligned}$$

Problem 252: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right]}{x^2 (d+ex)} dx$$

Optimal (type 4, 357 leaves, 22 steps):

$$\begin{aligned}
& \frac{2p}{dx} + \frac{2\sqrt{a} p \text{ArcTan} \left[\frac{\sqrt{a}x}{\sqrt{b}} \right]}{\sqrt{b}d} - \frac{\text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right]}{dx} + \frac{e \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] \text{Log} \left[-\frac{b}{ax^2} \right]}{2d^2} + \frac{e \text{Log} \left[c \left(a + \frac{b}{x^2} \right)^p \right] \text{Log}[d+ex]}{d^2} + \\
& \frac{2ep \text{Log} \left[-\frac{ex}{d} \right] \text{Log}[d+ex]}{d^2} - \frac{ep \text{Log} \left[\frac{e(\sqrt{b} - \sqrt{-a}x)}{\sqrt{-a}d + \sqrt{b}e} \right] \text{Log}[d+ex]}{d^2} - \frac{ep \text{Log} \left[-\frac{e(\sqrt{b} + \sqrt{-a}x)}{\sqrt{-a}d - \sqrt{b}e} \right] \text{Log}[d+ex]}{d^2} + \\
& \frac{ep \text{PolyLog} \left[2, 1 + \frac{b}{ax^2} \right]}{2d^2} - \frac{ep \text{PolyLog} \left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d - \sqrt{b}e} \right]}{d^2} - \frac{ep \text{PolyLog} \left[2, \frac{\sqrt{-a}(d+ex)}{\sqrt{-a}d + \sqrt{b}e} \right]}{d^2} + \frac{2ep \text{PolyLog} \left[2, 1 + \frac{ex}{d} \right]}{d^2}
\end{aligned}$$

Result (type 4, 472 leaves):

$$\frac{1}{d^2} \left(\frac{2 d p}{x} + \frac{2 \sqrt{a} d p \operatorname{ArcTan}\left[\frac{\sqrt{a} x}{\sqrt{b}}\right]}{\sqrt{b}} - \frac{d \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{x} - e \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[x] - e p \operatorname{Log}[x]^2 + \right.$$

$$e p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{a} x}{\sqrt{b}}\right] + e p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{a} x}{\sqrt{b}}\right] + e \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d + e x] + 2 e p \operatorname{Log}[x] \operatorname{Log}[d + e x] -$$

$$e p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d + e x] - e p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d + e x] + e p \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d + e x)}{\sqrt{a} d - i \sqrt{b} e}\right] +$$

$$e p \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d + e x)}{\sqrt{a} d + i \sqrt{b} e}\right] - 2 e p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e x}{d}\right] + e p \operatorname{PolyLog}\left[2, -\frac{i \sqrt{a} x}{\sqrt{b}}\right] +$$

$$e p \operatorname{PolyLog}\left[2, \frac{i \sqrt{a} x}{\sqrt{b}}\right] - 2 e p \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] + e p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} - i \sqrt{a} x)}{i \sqrt{a} d + \sqrt{b} e}\right] + e p \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} + i \sqrt{a} x)}{-i \sqrt{a} d + \sqrt{b} e}\right] \Bigg)$$

Problem 253: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{x^3 (d + e x)} dx$$

Optimal (type 4, 414 leaves, 25 steps):

$$\frac{p}{2 d x^2} - \frac{2 e p}{d^2 x} - \frac{2 \sqrt{a} e p \operatorname{ArcTan}\left[\frac{\sqrt{a} x}{\sqrt{b}}\right]}{\sqrt{b} d^2} - \frac{\left(a + \frac{b}{x^2}\right) \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{2 b d} + \frac{e \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{d^2 x} - \frac{e^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}\left[-\frac{b}{a x^2}\right]}{2 d^3} -$$

$$\frac{e^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d + e x]}{d^3} - \frac{2 e^2 p \operatorname{Log}\left[-\frac{e x}{d}\right] \operatorname{Log}[d + e x]}{d^3} + \frac{e^2 p \operatorname{Log}\left[\frac{e(\sqrt{b} - \sqrt{-a} x)}{\sqrt{-a} d + \sqrt{b} e}\right] \operatorname{Log}[d + e x]}{d^3} + \frac{e^2 p \operatorname{Log}\left[-\frac{e(\sqrt{b} + \sqrt{-a} x)}{\sqrt{-a} d - \sqrt{b} e}\right] \operatorname{Log}[d + e x]}{d^3} -$$

$$\frac{e^2 p \operatorname{PolyLog}\left[2, 1 + \frac{b}{a x^2}\right]}{2 d^3} + \frac{e^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d + e x)}{\sqrt{-a} d - \sqrt{b} e}\right]}{d^3} + \frac{e^2 p \operatorname{PolyLog}\left[2, \frac{\sqrt{-a}(d + e x)}{\sqrt{-a} d + \sqrt{b} e}\right]}{d^3} - \frac{2 e^2 p \operatorname{PolyLog}\left[2, 1 + \frac{e x}{d}\right]}{d^3}$$

Result (type 4, 643 leaves):

$$\begin{aligned}
& -\frac{1}{2 b d^3 x^2} \left(-b d^2 p + 4 b d e p x + 4 \sqrt{a} \sqrt{b} d e p x^2 \operatorname{ArcTan}\left[\frac{\sqrt{a} x}{\sqrt{b}}\right] + b d^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] - 2 b d e x \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] - 2 a d^2 p x^2 \operatorname{Log}[x] - \right. \\
& 2 b e^2 x^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[x] - 2 b e^2 p x^2 \operatorname{Log}[x]^2 + 2 b e^2 p x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{a} x}{\sqrt{b}}\right] + 2 b e^2 p x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{a} x}{\sqrt{b}}\right] + \\
& 2 b e^2 x^2 \operatorname{Log}\left[c\left(a + \frac{b}{x^2}\right)^p\right] \operatorname{Log}[d + e x] + 4 b e^2 p x^2 \operatorname{Log}[x] \operatorname{Log}[d + e x] - 2 b e^2 p x^2 \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d + e x] - \\
& 2 b e^2 p x^2 \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}[d + e x] + 2 b e^2 p x^2 \operatorname{Log}\left[\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d + e x)}{\sqrt{a} d - i \sqrt{b} e}\right] + 2 b e^2 p x^2 \operatorname{Log}\left[-\frac{i \sqrt{b}}{\sqrt{a}} + x\right] \operatorname{Log}\left[\frac{\sqrt{a}(d + e x)}{\sqrt{a} d + i \sqrt{b} e}\right] - \\
& 4 b e^2 p x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{e x}{d}\right] + a d^2 p x^2 \operatorname{Log}[b + a x^2] + 2 b e^2 p x^2 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{a} x}{\sqrt{b}}\right] + 2 b e^2 p x^2 \operatorname{PolyLog}\left[2, \frac{i \sqrt{a} x}{\sqrt{b}}\right] - \\
& \left. 4 b e^2 p x^2 \operatorname{PolyLog}\left[2, -\frac{e x}{d}\right] + 2 b e^2 p x^2 \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} - i \sqrt{a} x)}{i \sqrt{a} d + \sqrt{b} e}\right] + 2 b e^2 p x^2 \operatorname{PolyLog}\left[2, \frac{e(\sqrt{b} + i \sqrt{a} x)}{-i \sqrt{a} d + \sqrt{b} e}\right] \right)
\end{aligned}$$

Problem 263: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[c(d + e x)^p]}{f + g x^2} dx$$

Optimal (type 4, 229 leaves, 8 steps):

$$\frac{\operatorname{Log}[c(d + e x)^p] \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2\sqrt{-f}\sqrt{g}} - \frac{\operatorname{Log}[c(d + e x)^p] \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2\sqrt{-f}\sqrt{g}} - \frac{p \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d + e x)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2\sqrt{-f}\sqrt{g}} + \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + e x)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2\sqrt{-f}\sqrt{g}}$$

Result (type 4, 232 leaves):

$$\frac{\operatorname{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] (-p \operatorname{Log}[d + e x] + \operatorname{Log}[c(d + e x)^p])}{\sqrt{f}\sqrt{g}} + \\
p \left(\frac{i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + e x)}{-i e\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + e x)}{-i e\sqrt{f} + d\sqrt{g}}\right] \right)}{2\sqrt{f}\sqrt{g}} - \frac{i \left(\operatorname{Log}[d + e x] \operatorname{Log}\left[1 - \frac{\sqrt{g}(d + e x)}{i e\sqrt{f} + d\sqrt{g}}\right] + \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + e x)}{i e\sqrt{f} + d\sqrt{g}}\right] \right)}{2\sqrt{f}\sqrt{g}} \right)$$

Problem 266: Result is not expressed in closed-form.

$$\int \frac{\text{Log}[c (d + e \sqrt{x})^p]}{f + g x^2} dx$$

Optimal (type 4, 541 leaves, 19 steps):

$$\begin{aligned} & - \frac{\text{Log}[c (d + e \sqrt{x})^p] \text{Log}\left[\frac{e^{\left(\sqrt{-\sqrt{-f}} - g^{1/4} \sqrt{x}\right)}}{e^{\sqrt{-\sqrt{-f}}} + d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} + \frac{\text{Log}[c (d + e \sqrt{x})^p] \text{Log}\left[\frac{e^{\left((-f)^{1/4} - g^{1/4} \sqrt{x}\right)}}{e^{(-f)^{1/4}} + d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} \\ & - \frac{\text{Log}[c (d + e \sqrt{x})^p] \text{Log}\left[\frac{e^{\left(\sqrt{-\sqrt{-f}} + g^{1/4} \sqrt{x}\right)}}{e^{\sqrt{-\sqrt{-f}}} - d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} + \frac{\text{Log}[c (d + e \sqrt{x})^p] \text{Log}\left[\frac{e^{\left((-f)^{1/4} + g^{1/4} \sqrt{x}\right)}}{e^{(-f)^{1/4}} - d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} \\ & - \frac{p \text{PolyLog}\left[2, -\frac{g^{1/4} (d + e \sqrt{x})}{e^{\sqrt{-\sqrt{-f}}} - d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} + \frac{p \text{PolyLog}\left[2, -\frac{g^{1/4} (d + e \sqrt{x})}{e^{(-f)^{1/4}} - d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} \\ & - \frac{p \text{PolyLog}\left[2, \frac{g^{1/4} (d + e \sqrt{x})}{e^{\sqrt{-\sqrt{-f}}} + d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} + \frac{p \text{PolyLog}\left[2, \frac{g^{1/4} (d + e \sqrt{x})}{e^{(-f)^{1/4}} + d g^{1/4}}}\right]}{2 \sqrt{-f} \sqrt{g}} \end{aligned}$$

Result (type 7, 227 leaves):

$$\begin{aligned} & \frac{\left(\text{ArcTan}\left[1 - \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right] + \text{ArcTan}\left[1 + \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right]\right) \left(p \text{Log}[d + e \sqrt{x}] - \text{Log}[c (d + e \sqrt{x})^p]\right)}{\sqrt{f} \sqrt{g}} + \frac{1}{4 g} \\ & e^2 p \text{RootSum}\left[e^4 f + d^4 g - 4 d^3 g \#1 + 6 d^2 g \#1^2 - 4 d g \#1^3 + g \#1^4 \&, \frac{-\text{Log}[d + e \sqrt{x}]^2 + 2 \text{Log}[d + e \sqrt{x}] \text{Log}\left[1 - \frac{d + e \sqrt{x}}{\#1}\right] + 2 \text{PolyLog}\left[2, \frac{d + e \sqrt{x}}{\#1}\right]}{d^2 - 2 d \#1 + \#1^2} \&\right] \end{aligned}$$

Problem 267: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}\left[c \left(d + \frac{e}{\sqrt{x}}\right)^p\right]}{f + g x^2} dx$$

Optimal (type 4, 561 leaves, 20 steps):

$$\begin{aligned}
& \frac{\text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] \text{Log}\left[\frac{e\left(g^{1/4} - \frac{\sqrt{-f}}{\sqrt{x}}\right)}{d\sqrt{-f} + e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} - \frac{\text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] \text{Log}\left[-\frac{e\left(g^{1/4} + \frac{\sqrt{-f}}{\sqrt{x}}\right)}{d\sqrt{-f} - e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} + \\
& \frac{\text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] \text{Log}\left[\frac{e\left(g^{1/4} - \frac{(-f)^{1/4}}{\sqrt{x}}\right)}{d(-f)^{1/4} + e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} + \frac{\text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] \text{Log}\left[-\frac{e\left(g^{1/4} + \frac{(-f)^{1/4}}{\sqrt{x}}\right)}{d(-f)^{1/4} - e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} - \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f}\left(d + \frac{e}{\sqrt{x}}\right)}{d\sqrt{-f} - e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} + \\
& \frac{p \text{PolyLog}\left[2, \frac{(-f)^{1/4}\left(d + \frac{e}{\sqrt{x}}\right)}{d(-f)^{1/4} - e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} - \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f}\left(d + \frac{e}{\sqrt{x}}\right)}{d\sqrt{-f} + e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}} + \frac{p \text{PolyLog}\left[2, \frac{(-f)^{1/4}\left(d + \frac{e}{\sqrt{x}}\right)}{d(-f)^{1/4} + e g^{1/4}}\right]}{2\sqrt{-f}\sqrt{g}}
\end{aligned}$$

Result (type 4, 895 leaves):

$$\begin{aligned}
& \frac{1}{4\sqrt{f}\sqrt{g}} \left(4 p \text{ArcTan}\left[1 - \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}\left[d + \frac{e}{\sqrt{x}}\right] + 4 p \text{ArcTan}\left[1 + \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}\left[d + \frac{e}{\sqrt{x}}\right] + \right. \\
& 4 p \text{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] \text{Log}\left[d + \frac{e}{\sqrt{x}}\right] - 4 \text{ArcTan}\left[1 - \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] - 4 \text{ArcTan}\left[1 + \frac{\sqrt{2} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^p\right] - \\
& 4 p \text{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] \text{Log}\left[\frac{e}{d} + \sqrt{x}\right] - 2 i p \text{Log}\left[1 + \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{1/4} d f^{1/4} - e g^{1/4}}\right] \text{Log}\left[\frac{e}{d} + \sqrt{x}\right] + 2 i p \text{Log}\left[1 + \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{3/4} d f^{1/4} - e g^{1/4}}\right] \text{Log}\left[\frac{e}{d} + \sqrt{x}\right] - \\
& 2 i p \text{Log}\left[1 - \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{1/4} d f^{1/4} + e g^{1/4}}\right] \text{Log}\left[\frac{e}{d} + \sqrt{x}\right] + 2 i p \text{Log}\left[1 - \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{3/4} d f^{1/4} + e g^{1/4}}\right] \text{Log}\left[\frac{e}{d} + \sqrt{x}\right] + 2 p \text{ArcTan}\left[\frac{\sqrt{g} x}{\sqrt{f}}\right] \text{Log}[x] - \\
& i p \text{Log}\left[1 - \frac{(-1)^{1/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}[x] - i p \text{Log}\left[1 + \frac{(-1)^{1/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}[x] + i p \text{Log}\left[1 - \frac{(-1)^{3/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}[x] + \\
& i p \text{Log}\left[1 + \frac{(-1)^{3/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \text{Log}[x] - 2 i p \text{PolyLog}\left[2, -\frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{1/4} d f^{1/4} - e g^{1/4}}\right] + 2 i p \text{PolyLog}\left[2, -\frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{3/4} d f^{1/4} - e g^{1/4}}\right] - \\
& 2 i p \text{PolyLog}\left[2, \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{1/4} d f^{1/4} + e g^{1/4}}\right] + 2 i p \text{PolyLog}\left[2, \frac{g^{1/4}(e + d\sqrt{x})}{(-1)^{3/4} d f^{1/4} + e g^{1/4}}\right] - 2 i p \text{PolyLog}\left[2, -\frac{(-1)^{1/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] - \\
& \left. 2 i p \text{PolyLog}\left[2, \frac{(-1)^{1/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] + 2 i p \text{PolyLog}\left[2, -\frac{(-1)^{3/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] + 2 i p \text{PolyLog}\left[2, \frac{(-1)^{3/4} g^{1/4} \sqrt{x}}{f^{1/4}}\right] \right)
\end{aligned}$$

Problem 274: Result more than twice size of optimal antiderivative.

$$\int (f + g x^2) \operatorname{Log}[c (d + e x^2)^p] dx$$

Optimal (type 4, 548 leaves, 30 steps):

$$\begin{aligned} & 8 f p^2 x - \frac{32 d g p^2 x}{9 e} + \frac{8}{27} g p^2 x^3 - \frac{8 \sqrt{d} f p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}} + \frac{32 d^{3/2} g p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{9 e^{3/2}} + \frac{4 i \sqrt{d} f p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{\sqrt{e}} - \frac{4 i d^{3/2} g p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]^2}{3 e^{3/2}} + \\ & \frac{8 \sqrt{d} f p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} + i \sqrt{e} x}\right]}{\sqrt{e}} - \frac{8 d^{3/2} g p^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2 \sqrt{d}}{\sqrt{d} + i \sqrt{e} x}\right]}{3 e^{3/2}} - 4 f p x \operatorname{Log}[c (d + e x^2)^p] + \frac{4 d g p x \operatorname{Log}[c (d + e x^2)^p]}{3 e} - \\ & \frac{4}{9} g p x^3 \operatorname{Log}[c (d + e x^2)^p] + \frac{4 \sqrt{d} f p \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c (d + e x^2)^p]}{\sqrt{e}} - \frac{4 d^{3/2} g p \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[c (d + e x^2)^p]}{3 e^{3/2}} + \\ & f x \operatorname{Log}[c (d + e x^2)^p]^2 + \frac{1}{3} g x^3 \operatorname{Log}[c (d + e x^2)^p]^2 + \frac{4 i \sqrt{d} f p^2 \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} + i \sqrt{e} x}\right]}{\sqrt{e}} - \frac{4 i d^{3/2} g p^2 \operatorname{PolyLog}\left[2, 1 - \frac{2 \sqrt{d}}{\sqrt{d} + i \sqrt{e} x}\right]}{3 e^{3/2}} \end{aligned}$$

Result (type 4, 1125 leaves):

$$\begin{aligned}
& 2 f p \left(-2 e \left(\frac{x}{e} - \frac{\sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{e^{3/2}} \right) + x \operatorname{Log}[d + e x^2] \right) \left(-p \operatorname{Log}[d + e x^2] + \operatorname{Log}[c (d + e x^2)^p] \right) + \\
& 2 g p \left(-\frac{2}{3} e \left(-\frac{d x}{e^2} + \frac{x^3}{3 e} + \frac{d^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{e^{5/2}} \right) + \frac{1}{3} x^3 \operatorname{Log}[d + e x^2] \right) \left(-p \operatorname{Log}[d + e x^2] + \operatorname{Log}[c (d + e x^2)^p] \right) + \\
& f x \left(-p \operatorname{Log}[d + e x^2] + \operatorname{Log}[c (d + e x^2)^p] \right)^2 + \frac{1}{3} g x^3 \left(-p \operatorname{Log}[d + e x^2] + \operatorname{Log}[c (d + e x^2)^p] \right)^2 + \\
& f p^2 \left(x \operatorname{Log}[d + e x^2]^2 - \frac{1}{\sqrt{e}} \left(-8 \sqrt{e} x - 4 i \sqrt{d} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] + 4 \sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] + \right. \right. \\
& \quad \left. \left. i \sqrt{d} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right]^2 + 4 i \sqrt{d} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] + 4 \sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] - i \sqrt{d} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right]^2 - \right. \right. \\
& \quad \left. \left. 2 i \sqrt{d} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] + 2 i \sqrt{d} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] + 4 \sqrt{e} x \operatorname{Log}[d + e x^2] - \right. \right. \\
& \quad \left. \left. 4 \sqrt{d} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[d + e x^2] + 2 i \sqrt{d} \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] - 2 i \sqrt{d} \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] \right) \right) + \\
& g p^2 \left(\frac{1}{3} x^3 \operatorname{Log}[d + e x^2]^2 - \frac{1}{27 e^{3/2}} \left(96 d \sqrt{e} x - 8 e^{3/2} x^3 - 24 d^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 36 i d^{3/2} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] - \right. \right. \\
& \quad \left. \left. 36 d^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] - 9 i d^{3/2} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right]^2 - 36 i d^{3/2} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] - 36 d^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] + \right. \right. \\
& \quad \left. \left. 9 i d^{3/2} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right]^2 + 18 i d^{3/2} \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] - 18 i d^{3/2} \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] - 36 d \sqrt{e} x \operatorname{Log}[d + e x^2] + \right. \right. \\
& \quad \left. \left. 12 e^{3/2} x^3 \operatorname{Log}[d + e x^2] + 36 d^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] \operatorname{Log}[d + e x^2] - 18 i d^{3/2} \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] + 18 i d^{3/2} \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{e} x}{2 \sqrt{d}}\right] \right) \right)
\end{aligned}$$

Problem 341: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (d + e x^2)^p]}{x (f + g x^2)} dx$$

Optimal (type 4, 119 leaves, 8 steps):

$$\frac{\operatorname{Log}\left[-\frac{e x^2}{d}\right] \operatorname{Log}[c (d + e x^2)^p]}{2 f} - \frac{\operatorname{Log}[c (d + e x^2)^p] \operatorname{Log}\left[\frac{e (f + g x^2)}{e f - d g}\right]}{2 f} - \frac{p \operatorname{PolyLog}\left[2, -\frac{g (d + e x^2)}{e f - d g}\right]}{2 f} + \frac{p \operatorname{PolyLog}\left[2, 1 + \frac{e x^2}{d}\right]}{2 f}$$

Result (type 4, 663 leaves):

$$\begin{aligned}
 & -\frac{1}{2f} \left(2p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i\sqrt{g}x)}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}}\right] + \right. \\
 & p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i\sqrt{g}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i\sqrt{g}x)}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}}\right] + p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i\sqrt{g}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] \left. - \right. \\
 & 2 \operatorname{Log}[x] \operatorname{Log}[c(d + ex^2)^p] - p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + gx^2] - p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + gx^2] + \\
 & \operatorname{Log}[c(d + ex^2)^p] \operatorname{Log}[f + gx^2] + 2p \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2p \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} - i\sqrt{e}x)}{-\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + \\
 & \left. p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} - i\sqrt{e}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} + i\sqrt{e}x)}{-\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} + i\sqrt{e}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] \right)
 \end{aligned}$$

Problem 342: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c(d + ex^2)^p]}{x^3(f + gx^2)} dx$$

Optimal (type 4, 176 leaves, 12 steps):

$$\begin{aligned}
 & \frac{ep \operatorname{Log}[x]}{df} - \frac{ep \operatorname{Log}[d + ex^2]}{2df} - \frac{\operatorname{Log}[c(d + ex^2)^p]}{2fx^2} - \frac{g \operatorname{Log}\left[-\frac{ex^2}{d}\right] \operatorname{Log}[c(d + ex^2)^p]}{2f^2} + \\
 & \frac{g \operatorname{Log}[c(d + ex^2)^p] \operatorname{Log}\left[\frac{e(f + gx^2)}{ef - dg}\right]}{2f^2} + \frac{gp \operatorname{PolyLog}\left[2, -\frac{g(d + ex^2)}{ef - dg}\right]}{2f^2} - \frac{gp \operatorname{PolyLog}\left[2, 1 + \frac{ex^2}{d}\right]}{2f^2}
 \end{aligned}$$

Result (type 4, 791 leaves):

$$\frac{1}{2 d f^2 x^2} \left(2 e f p x^2 \operatorname{Log}[x] + 2 d g p x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 d g p x^2 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + d g p x^2 \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e} (\sqrt{f} - i \sqrt{g} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + \right. \\ \left. d g p x^2 \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e} (\sqrt{f} - i \sqrt{g} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + d g p x^2 \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e} (\sqrt{f} + i \sqrt{g} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + \right. \\ \left. d g p x^2 \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e} (\sqrt{f} + i \sqrt{g} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] - e f p x^2 \operatorname{Log}[d + e x^2] - d f \operatorname{Log}[c (d + e x^2)^p] - 2 d g x^2 \operatorname{Log}[x] \operatorname{Log}[c (d + e x^2)^p] - \right. \\ \left. d g p x^2 \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + g x^2] - d g p x^2 \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + g x^2] + d g x^2 \operatorname{Log}[c (d + e x^2)^p] \operatorname{Log}[f + g x^2] + \right. \\ \left. 2 d g p x^2 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 2 d g p x^2 \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] + d g p x^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (\sqrt{d} - i \sqrt{e} x)}{-\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + \right. \\ \left. d g p x^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (\sqrt{d} - i \sqrt{e} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + d g p x^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (\sqrt{d} + i \sqrt{e} x)}{-\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + d g p x^2 \operatorname{PolyLog}\left[2, \frac{\sqrt{g} (\sqrt{d} + i \sqrt{e} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] \right)$$

Problem 351: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c (d + e x^2)^p]}{x (f + g x^2)^2} dx$$

Optimal (type 4, 201 leaves, 12 steps):

$$-\frac{e p \operatorname{Log}[d + e x^2]}{2 f (e f - d g)} + \frac{\operatorname{Log}[c (d + e x^2)^p]}{2 f (f + g x^2)} + \frac{\operatorname{Log}\left[-\frac{e x^2}{d}\right] \operatorname{Log}[c (d + e x^2)^p]}{2 f^2} + \\ \frac{e p \operatorname{Log}[f + g x^2]}{2 f (e f - d g)} - \frac{\operatorname{Log}[c (d + e x^2)^p] \operatorname{Log}\left[\frac{e (f + g x^2)}{e f - d g}\right]}{2 f^2} - \frac{p \operatorname{PolyLog}\left[2, -\frac{g (d + e x^2)}{e f - d g}\right]}{2 f^2} + \frac{p \operatorname{PolyLog}\left[2, 1 + \frac{e x^2}{d}\right]}{2 f^2}$$

Result (type 4, 1124 leaves):

$$\begin{aligned}
& -\frac{1}{4f^2} \\
& \left(\frac{i\sqrt{f} p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{-i\sqrt{f} + \sqrt{g}x} - \frac{i\sqrt{f} p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{i\sqrt{f} + \sqrt{g}x} + \frac{2fp \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{f + gx^2} + \frac{i\sqrt{f} p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{-i\sqrt{f} + \sqrt{g}x} - \frac{i\sqrt{f} p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{i\sqrt{f} + \sqrt{g}x} + \frac{2fp \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]}{f + gx^2} + \right. \\
& 4p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 4p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i\sqrt{g}x)}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}}\right] + 2p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \\
& \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i\sqrt{g}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + 2p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i\sqrt{g}x)}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}}\right] + 2p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i\sqrt{g}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + \\
& \frac{\sqrt{e}\sqrt{f} p \operatorname{Log}[d + ex^2]}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}} + \frac{\sqrt{e}\sqrt{f} p \operatorname{Log}[d + ex^2]}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}} - \frac{2f \operatorname{Log}[c(d + ex^2)^p]}{f + gx^2} - 4 \operatorname{Log}[x] \operatorname{Log}[c(d + ex^2)^p] - \\
& \frac{\sqrt{e}\sqrt{f} p \operatorname{Log}[f + gx^2]}{\sqrt{e}\sqrt{f} - \sqrt{d}\sqrt{g}} - \frac{\sqrt{e}\sqrt{f} p \operatorname{Log}[f + gx^2]}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}} - 2p \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + gx^2] - 2p \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + gx^2] + \\
& 2 \operatorname{Log}[c(d + ex^2)^p] \operatorname{Log}[f + gx^2] + 4p \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 4p \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} - i\sqrt{e}x)}{-\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + \\
& \left. 2p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} - i\sqrt{e}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + 2p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} + i\sqrt{e}x)}{-\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] + 2p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} + i\sqrt{e}x)}{\sqrt{e}\sqrt{f} + \sqrt{d}\sqrt{g}}\right] \right)
\end{aligned}$$

Problem 352: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c(d + ex^2)^p]}{x^3(f + gx^2)^2} dx$$

Optimal (type 4, 251 leaves, 16 steps):

$$\begin{aligned}
& \frac{ep \operatorname{Log}[x]}{df^2} - \frac{ep \operatorname{Log}[d + ex^2]}{2df^2} + \frac{egp \operatorname{Log}[d + ex^2]}{2f^2(ef - dg)} - \frac{\operatorname{Log}[c(d + ex^2)^p]}{2f^2x^2} - \frac{g \operatorname{Log}[c(d + ex^2)^p]}{2f^2(f + gx^2)} - \frac{g \operatorname{Log}\left[-\frac{ex^2}{d}\right] \operatorname{Log}[c(d + ex^2)^p]}{f^3} \\
& \frac{egp \operatorname{Log}[f + gx^2]}{2f^2(ef - dg)} + \frac{g \operatorname{Log}[c(d + ex^2)^p] \operatorname{Log}\left[\frac{e(f + gx^2)}{ef - dg}\right]}{f^3} + \frac{gp \operatorname{PolyLog}\left[2, -\frac{g(d + ex^2)}{ef - dg}\right]}{f^3} - \frac{gp \operatorname{PolyLog}\left[2, 1 + \frac{ex^2}{d}\right]}{f^3}
\end{aligned}$$

Result (type 4, 1197 leaves):

$$\begin{aligned}
& \frac{1}{4 f^3} \left(\frac{4 e f p \operatorname{Log}[x]}{d} + \frac{i \sqrt{f} g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{-i \sqrt{f} + \sqrt{g} x} - \frac{i \sqrt{f} g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{i \sqrt{f} + \sqrt{g} x} + \frac{2 f g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{f + g x^2} + \right. \\
& \frac{i \sqrt{f} g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{-i \sqrt{f} + \sqrt{g} x} - \frac{i \sqrt{f} g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{i \sqrt{f} + \sqrt{g} x} + \frac{2 f g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right]}{f + g x^2} + 8 g p \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{e} x}{\sqrt{d}}\right] + \\
& 8 g p \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i \sqrt{g} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + 4 g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} - i \sqrt{g} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + \\
& 4 g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i \sqrt{g} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + 4 g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e}(\sqrt{f} + i \sqrt{g} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] - \frac{2 e f p \operatorname{Log}[d + e x^2]}{d} + \\
& \frac{\sqrt{e} \sqrt{f} g p \operatorname{Log}[d + e x^2]}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}} + \frac{\sqrt{e} \sqrt{f} g p \operatorname{Log}[d + e x^2]}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}} - \frac{2 f \operatorname{Log}[c(d + e x^2)^p]}{x^2} - \frac{2 f g \operatorname{Log}[c(d + e x^2)^p]}{f + g x^2} - 8 g \operatorname{Log}[x] \operatorname{Log}[c(d + e x^2)^p] - \\
& \frac{\sqrt{e} \sqrt{f} g p \operatorname{Log}[f + g x^2]}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}} - \frac{\sqrt{e} \sqrt{f} g p \operatorname{Log}[f + g x^2]}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}} - 4 g p \operatorname{Log}\left[-\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + g x^2] - 4 g p \operatorname{Log}\left[\frac{i \sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}[f + g x^2] + \\
& 4 g \operatorname{Log}[c(d + e x^2)^p] \operatorname{Log}[f + g x^2] + 8 g p \operatorname{PolyLog}\left[2, -\frac{i \sqrt{e} x}{\sqrt{d}}\right] + 8 g p \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} x}{\sqrt{d}}\right] + 4 g p \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(\sqrt{d} - i \sqrt{e} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + \\
& \left. 4 g p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} - i \sqrt{e} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] + 4 g p \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(\sqrt{d} + i \sqrt{e} x)}{\sqrt{e} \sqrt{f} - \sqrt{d} \sqrt{g}}\right] + 4 g p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(\sqrt{d} + i \sqrt{e} x)}{\sqrt{e} \sqrt{f} + \sqrt{d} \sqrt{g}}\right] \right)
\end{aligned}$$

Problem 359: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[d + e x^2]}{1 - x^2} dx$$

Optimal (type 4, 217 leaves, 11 steps):

$$\begin{aligned}
& 2 \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2}{1+x}\right] - \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2(\sqrt{-d} - \sqrt{e} x)}{(\sqrt{-d} - \sqrt{e})(1+x)}\right] - \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2(\sqrt{-d} + \sqrt{e} x)}{(\sqrt{-d} + \sqrt{e})(1+x)}\right] + \\
& \operatorname{ArcTanh}[x] \operatorname{Log}[d + e x^2] - \operatorname{PolyLog}\left[2, 1 - \frac{2}{1+x}\right] + \frac{1}{2} \operatorname{PolyLog}\left[2, 1 - \frac{2(\sqrt{-d} - \sqrt{e} x)}{(\sqrt{-d} - \sqrt{e})(1+x)}\right] + \frac{1}{2} \operatorname{PolyLog}\left[2, 1 - \frac{2(\sqrt{-d} + \sqrt{e} x)}{(\sqrt{-d} + \sqrt{e})(1+x)}\right]
\end{aligned}$$

Result (type 4, 468 leaves):

$$\frac{1}{2} \left(\text{Log}[1-x] \text{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}}+x\right] - \text{Log}\left[\frac{\sqrt{e}(-1+x)}{i\sqrt{d}-\sqrt{e}}\right] \text{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}}+x\right] - \text{Log}[1+x] \text{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}}+x\right] + \right. \\ \left. \text{Log}\left[-\frac{i\sqrt{e}(1+x)}{\sqrt{d}-i\sqrt{e}}\right] \text{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}}+x\right] + \text{Log}[1-x] \text{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}}+x\right] - \text{Log}\left[\frac{\sqrt{e}(-1+x)}{-i\sqrt{d}-\sqrt{e}}\right] \text{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}}+x\right] - \right. \\ \left. \text{Log}[1+x] \text{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}}+x\right] + \text{Log}\left[\frac{i\sqrt{e}(1+x)}{\sqrt{d}+i\sqrt{e}}\right] \text{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}}+x\right] - \text{Log}[1-x] \text{Log}[d+ex^2] + \text{Log}[1+x] \text{Log}[d+ex^2] - \right. \\ \left. \text{PolyLog}\left[2, \frac{\sqrt{d}-i\sqrt{e}x}{\sqrt{d}-i\sqrt{e}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{d}-i\sqrt{e}x}{\sqrt{d}+i\sqrt{e}}\right] + \text{PolyLog}\left[2, \frac{\sqrt{d}+i\sqrt{e}x}{\sqrt{d}-i\sqrt{e}}\right] - \text{PolyLog}\left[2, \frac{\sqrt{d}+i\sqrt{e}x}{\sqrt{d}+i\sqrt{e}}\right] \right)$$

Problem 370: Unable to integrate problem.

$$\int \frac{\text{Log}[c(d+ex^n)^p]}{x(f+gx^{2n})} dx$$

Optimal (type 4, 266 leaves, 13 steps):

$$\frac{\text{Log}\left[-\frac{ex^n}{d}\right] \text{Log}[c(d+ex^n)^p]}{fn} - \frac{\text{Log}[c(d+ex^n)^p] \text{Log}\left[\frac{e(\sqrt{-f}-\sqrt{g}x^n)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2fn} - \\ \frac{\text{Log}[c(d+ex^n)^p] \text{Log}\left[\frac{e(\sqrt{-f}+\sqrt{g}x^n)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2fn} - \frac{p \text{PolyLog}\left[2, -\frac{\sqrt{g}(d+ex^n)}{e\sqrt{-f}-d\sqrt{g}}\right]}{2fn} - \frac{p \text{PolyLog}\left[2, \frac{\sqrt{g}(d+ex^n)}{e\sqrt{-f}+d\sqrt{g}}\right]}{2fn} + \frac{p \text{PolyLog}\left[2, 1+\frac{ex^n}{d}\right]}{fn}$$

Result (type 8, 29 leaves):

$$\int \frac{\text{Log}[c(d+ex^n)^p]}{x(f+gx^{2n})} dx$$

Problem 371: Unable to integrate problem.

$$\int \frac{\text{Log}[c(d+ex^n)^p]}{x(f+gx^n)} dx$$

Optimal (type 4, 121 leaves, 8 steps):

$$\frac{\text{Log}\left[-\frac{ex^n}{d}\right] \text{Log}[c(d+ex^n)^p]}{fn} - \frac{\text{Log}[c(d+ex^n)^p] \text{Log}\left[\frac{e(f+gx^n)}{ef-dg}\right]}{fn} - \frac{p \text{PolyLog}\left[2, -\frac{g(d+ex^n)}{ef-dg}\right]}{fn} + \frac{p \text{PolyLog}\left[2, 1+\frac{ex^n}{d}\right]}{fn}$$

Result (type 8, 27 leaves):

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^n)} dx$$

Problem 372: Unable to integrate problem.

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-n})} dx$$

Optimal (type 4, 70 leaves, 5 steps):

$$\frac{\text{Log}[c (d + e x^n)^p] \text{Log}\left[-\frac{e(g+fx^n)}{df-eg}\right]}{fn} + \frac{p \text{PolyLog}\left[2, \frac{f(d+ex^n)}{df-eg}\right]}{fn}$$

Result (type 8, 29 leaves):

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-n})} dx$$

Problem 373: Unable to integrate problem.

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-2n})} dx$$

Optimal (type 4, 221 leaves, 9 steps):

$$\frac{\text{Log}[c (d + e x^n)^p] \text{Log}\left[\frac{e(\sqrt{g}-\sqrt{-f}x^n)}{d\sqrt{-f}+e\sqrt{g}}\right]}{2fn} + \frac{\text{Log}[c (d + e x^n)^p] \text{Log}\left[-\frac{e(\sqrt{g}+\sqrt{-f}x^n)}{d\sqrt{-f}-e\sqrt{g}}\right]}{2fn} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f}(d+ex^n)}{d\sqrt{-f}-e\sqrt{g}}\right]}{2fn} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f}(d+ex^n)}{d\sqrt{-f}+e\sqrt{g}}\right]}{2fn}$$

Result (type 8, 29 leaves):

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-2n})} dx$$

Problem 374: Unable to integrate problem.

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{2n})^2} dx$$

Optimal (type 4, 419 leaves, 19 steps):

$$\begin{aligned}
& - \frac{d e \sqrt{g} p \operatorname{ArcTan}\left[\frac{\sqrt{g} x^n}{\sqrt{f}}\right]}{2 f^{3/2} (e^2 f + d^2 g) n} - \frac{e^2 p \operatorname{Log}[d + e x^n]}{2 f (e^2 f + d^2 g) n} + \frac{\operatorname{Log}[c (d + e x^n)^p]}{2 f n (f + g x^{2n})} + \frac{\operatorname{Log}\left[-\frac{e x^n}{d}\right] \operatorname{Log}[c (d + e x^n)^p]}{f^2 n} - \frac{\operatorname{Log}[c (d + e x^n)^p] \operatorname{Log}\left[\frac{e(\sqrt{-f} - \sqrt{g} x^n)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 f^2 n} \\
& \frac{\operatorname{Log}[c (d + e x^n)^p] \operatorname{Log}\left[\frac{e(\sqrt{-f} + \sqrt{g} x^n)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 f^2 n} + \frac{e^2 p \operatorname{Log}[f + g x^{2n}]}{4 f (e^2 f + d^2 g) n} - \frac{p \operatorname{PolyLog}\left[2, -\frac{\sqrt{g}(d + e x^n)}{e\sqrt{-f} - d\sqrt{g}}\right]}{2 f^2 n} - \frac{p \operatorname{PolyLog}\left[2, \frac{\sqrt{g}(d + e x^n)}{e\sqrt{-f} + d\sqrt{g}}\right]}{2 f^2 n} + \frac{p \operatorname{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right]}{f^2 n}
\end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{\operatorname{Log}[c (d + e x^n)^p]}{x (f + g x^{2n})^2} dx$$

Problem 375: Unable to integrate problem.

$$\int \frac{\operatorname{Log}[c (d + e x^n)^p]}{x (f + g x^n)^2} dx$$

Optimal (type 4, 204 leaves, 12 steps):

$$\begin{aligned}
& - \frac{e p \operatorname{Log}[d + e x^n]}{f (e f - d g) n} + \frac{\operatorname{Log}[c (d + e x^n)^p]}{f n (f + g x^n)} + \frac{\operatorname{Log}\left[-\frac{e x^n}{d}\right] \operatorname{Log}[c (d + e x^n)^p]}{f^2 n} + \\
& \frac{e p \operatorname{Log}[f + g x^n]}{f (e f - d g) n} - \frac{\operatorname{Log}[c (d + e x^n)^p] \operatorname{Log}\left[\frac{e(f + g x^n)}{e f - d g}\right]}{f^2 n} - \frac{p \operatorname{PolyLog}\left[2, -\frac{g(d + e x^n)}{e f - d g}\right]}{f^2 n} + \frac{p \operatorname{PolyLog}\left[2, 1 + \frac{e x^n}{d}\right]}{f^2 n}
\end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{\operatorname{Log}[c (d + e x^n)^p]}{x (f + g x^n)^2} dx$$

Problem 376: Unable to integrate problem.

$$\int \frac{\operatorname{Log}[c (d + e x^n)^p]}{x (f + g x^{-n})^2} dx$$

Optimal (type 4, 156 leaves, 10 steps):

$$\frac{e g p \operatorname{Log}[d + e x^n]}{f^2 (d f - e g) n} + \frac{g \operatorname{Log}[c (d + e x^n)^p]}{f^2 n (g + f x^n)} - \frac{e g p \operatorname{Log}[g + f x^n]}{f^2 (d f - e g) n} + \frac{\operatorname{Log}[c (d + e x^n)^p] \operatorname{Log}\left[-\frac{e(g + f x^n)}{d f - e g}\right]}{f^2 n} + \frac{p \operatorname{PolyLog}\left[2, \frac{f(d + e x^n)}{d f - e g}\right]}{f^2 n}$$

Result (type 8, 29 leaves):

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-n})^2} dx$$

Problem 377: Unable to integrate problem.

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-2n})^2} dx$$

Optimal (type 4, 377 leaves, 17 steps):

$$\begin{aligned} & - \frac{d e \sqrt{g} p \text{ArcTan}\left[\frac{\sqrt{f} x^n}{\sqrt{g}}\right]}{2 f^{3/2} (d^2 f + e^2 g) n} - \frac{e^2 g p \text{Log}[d + e x^n]}{2 f^2 (d^2 f + e^2 g) n} + \frac{g \text{Log}[c (d + e x^n)^p]}{2 f^2 n (g + f x^{2n})} + \frac{\text{Log}[c (d + e x^n)^p] \text{Log}\left[\frac{e (\sqrt{g} - \sqrt{-f} x^n)}{d \sqrt{-f} + e \sqrt{g}}\right]}{2 f^2 n} + \\ & \frac{\text{Log}[c (d + e x^n)^p] \text{Log}\left[-\frac{e (\sqrt{g} + \sqrt{-f} x^n)}{d \sqrt{-f} - e \sqrt{g}}\right]}{2 f^2 n} + \frac{e^2 g p \text{Log}[g + f x^{2n}]}{4 f^2 (d^2 f + e^2 g) n} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f} (d + e x^n)}{d \sqrt{-f} - e \sqrt{g}}\right]}{2 f^2 n} + \frac{p \text{PolyLog}\left[2, \frac{\sqrt{-f} (d + e x^n)}{d \sqrt{-f} + e \sqrt{g}}\right]}{2 f^2 n} \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{\text{Log}[c (d + e x^n)^p]}{x (f + g x^{-2n})^2} dx$$

Problem 380: Unable to integrate problem.

$$\int \frac{\text{Log}[c (d + e x^{-n})]}{x (c e - (1 - c d) x^n)} dx$$

Optimal (type 4, 26 leaves, 4 steps):

$$\frac{\text{PolyLog}\left[2, 1 - c (d + e x^{-n})\right]}{c e n}$$

Result (type 8, 35 leaves):

$$\int \frac{\text{Log}[c (d + e x^{-n})]}{x (c e - (1 - c d) x^n)} dx$$

Problem 392: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[x^{-n} (a + x^n)]}{x} dx$$

Optimal (type 4, 14 leaves, 2 steps):

$$\frac{\text{PolyLog}[2, -a x^{-n}]}{n}$$

Result (type 4, 51 leaves):

$$\frac{1}{2} \text{Log}[x] \left(n \text{Log}[x] + 2 \text{Log}[1 + a x^{-n}] - 2 \text{Log}\left[\frac{a + x^n}{a}\right] \right) - \frac{\text{PolyLog}[2, -\frac{x^n}{a}]}{n}$$

Problem 397: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}\left[\frac{a+bx^2}{x^2}\right]}{c+dx} dx$$

Optimal (type 4, 227 leaves, 14 steps):

$$\frac{\text{Log}\left[b + \frac{a}{x^2}\right] \text{Log}[c+dx]}{d} + \frac{2 \text{Log}\left[-\frac{dx}{c}\right] \text{Log}[c+dx]}{d} - \frac{\text{Log}\left[\frac{d(\sqrt{-a}-\sqrt{b}x)}{\sqrt{b}c+\sqrt{-a}d}\right] \text{Log}[c+dx]}{d} -$$

$$\frac{\text{Log}\left[-\frac{d(\sqrt{-a}+\sqrt{b}x)}{\sqrt{b}c-\sqrt{-a}d}\right] \text{Log}[c+dx]}{d} - \frac{\text{PolyLog}\left[2, \frac{\sqrt{b}(c+dx)}{\sqrt{b}c-\sqrt{-a}d}\right]}{d} - \frac{\text{PolyLog}\left[2, \frac{\sqrt{b}(c+dx)}{\sqrt{b}c+\sqrt{-a}d}\right]}{d} + \frac{2 \text{PolyLog}\left[2, 1 + \frac{dx}{c}\right]}{d}$$

Result (type 4, 284 leaves):

$$\frac{1}{d} \left(\text{Log}\left[b + \frac{a}{x^2}\right] \text{Log}[c+dx] + 2 \text{Log}[x] \text{Log}[c+dx] - \text{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \text{Log}[c+dx] -$$

$$\text{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \text{Log}[c+dx] + \text{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \text{Log}\left[\frac{\sqrt{b}(c+dx)}{\sqrt{b}c-i\sqrt{a}d}\right] + \text{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \text{Log}\left[\frac{\sqrt{b}(c+dx)}{\sqrt{b}c+i\sqrt{a}d}\right] -$$

$$2 \text{Log}[x] \text{Log}\left[1 + \frac{dx}{c}\right] - 2 \text{PolyLog}\left[2, -\frac{dx}{c}\right] + \text{PolyLog}\left[2, \frac{d(\sqrt{a}-i\sqrt{b}x)}{i\sqrt{b}c+\sqrt{a}d}\right] + \text{PolyLog}\left[2, \frac{d(\sqrt{a}+i\sqrt{b}x)}{-i\sqrt{b}c+\sqrt{a}d}\right] \right)$$

Problem 411: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \text{Log}[c(d + e\sqrt{x})^n])^2}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^2 \operatorname{Log} \left[-\frac{e \sqrt{x}}{d} \right] + 4 b n \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right) \operatorname{PolyLog} \left[2, 1 + \frac{e \sqrt{x}}{d} \right] - 4 b^2 n^2 \operatorname{PolyLog} \left[3, 1 + \frac{e \sqrt{x}}{d} \right]$$

Result (type 4, 195 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log} \left[d + e \sqrt{x} \right] + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^2 \operatorname{Log} [x] + \\ & 2 b n \left(a - b n \operatorname{Log} \left[d + e \sqrt{x} \right] + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right) \left(\left(\operatorname{Log} \left[d + e \sqrt{x} \right] - \operatorname{Log} \left[1 + \frac{e \sqrt{x}}{d} \right] \right) \operatorname{Log} [x] - 2 \operatorname{PolyLog} \left[2, -\frac{e \sqrt{x}}{d} \right] \right) + \\ & 2 b^2 n^2 \left(\operatorname{Log} \left[d + e \sqrt{x} \right]^2 \operatorname{Log} \left[-\frac{e \sqrt{x}}{d} \right] + 2 \operatorname{Log} \left[d + e \sqrt{x} \right] \operatorname{PolyLog} \left[2, 1 + \frac{e \sqrt{x}}{d} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{e \sqrt{x}}{d} \right] \right) \end{aligned}$$

Problem 418: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^3}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\begin{aligned} & 2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^3 \operatorname{Log} \left[-\frac{e \sqrt{x}}{d} \right] + 6 b n \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^2 \operatorname{PolyLog} \left[2, 1 + \frac{e \sqrt{x}}{d} \right] - \\ & 12 b^2 n^2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right) \operatorname{PolyLog} \left[3, 1 + \frac{e \sqrt{x}}{d} \right] + 12 b^3 n^3 \operatorname{PolyLog} \left[4, 1 + \frac{e \sqrt{x}}{d} \right] \end{aligned}$$

Result (type 4, 333 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log} \left[d + e \sqrt{x} \right] + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^3 \operatorname{Log} [x] + \\ & 3 b n \left(a - b n \operatorname{Log} \left[d + e \sqrt{x} \right] + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right)^2 \left(\left(\operatorname{Log} \left[d + e \sqrt{x} \right] - \operatorname{Log} \left[1 + \frac{e \sqrt{x}}{d} \right] \right) \operatorname{Log} [x] - 2 \operatorname{PolyLog} \left[2, -\frac{e \sqrt{x}}{d} \right] \right) + \\ & 6 b^2 n^2 \left(a - b n \operatorname{Log} \left[d + e \sqrt{x} \right] + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^n \right] \right) \\ & \left(\operatorname{Log} \left[d + e \sqrt{x} \right]^2 \operatorname{Log} \left[-\frac{e \sqrt{x}}{d} \right] + 2 \operatorname{Log} \left[d + e \sqrt{x} \right] \operatorname{PolyLog} \left[2, 1 + \frac{e \sqrt{x}}{d} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{e \sqrt{x}}{d} \right] \right) + 2 b^3 n^3 \\ & \left(\operatorname{Log} \left[d + e \sqrt{x} \right]^3 \operatorname{Log} \left[-\frac{e \sqrt{x}}{d} \right] + 3 \operatorname{Log} \left[d + e \sqrt{x} \right]^2 \operatorname{PolyLog} \left[2, 1 + \frac{e \sqrt{x}}{d} \right] - 6 \operatorname{Log} \left[d + e \sqrt{x} \right] \operatorname{PolyLog} \left[3, 1 + \frac{e \sqrt{x}}{d} \right] + 6 \operatorname{PolyLog} \left[4, 1 + \frac{e \sqrt{x}}{d} \right] \right) \end{aligned}$$

Problem 419: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + e \sqrt{x})^n])^3}{x^2} dx$$

Optimal (type 4, 263 leaves, 10 steps):

$$\begin{aligned} & \frac{3 b e n (d + e \sqrt{x}) (a + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2}{d^2 \sqrt{x}} - \frac{3 b e^2 n \operatorname{Log}\left[1 - \frac{d}{d + e \sqrt{x}}\right] (a + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2}{d^2} \\ & \frac{(a + b \operatorname{Log}[c (d + e \sqrt{x})^n])^3}{x} + \frac{6 b^2 e^2 n^2 (a + b \operatorname{Log}[c (d + e \sqrt{x})^n]) \operatorname{Log}\left[-\frac{e \sqrt{x}}{d}\right]}{d^2} + \\ & \frac{6 b^2 e^2 n^2 (a + b \operatorname{Log}[c (d + e \sqrt{x})^n]) \operatorname{PolyLog}\left[2, \frac{d}{d + e \sqrt{x}}\right]}{d^2} + \frac{6 b^3 e^2 n^3 \operatorname{PolyLog}\left[2, 1 + \frac{e \sqrt{x}}{d}\right]}{d^2} + \frac{6 b^3 e^2 n^3 \operatorname{PolyLog}\left[3, \frac{d}{d + e \sqrt{x}}\right]}{d^2} \end{aligned}$$

Result (type 4, 536 leaves):

$$\begin{aligned} & \frac{1}{d^2 x} \left(-3 b d e n \sqrt{x} (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2 - \right. \\ & 3 b d^2 n \operatorname{Log}[d + e \sqrt{x}] (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2 + 3 b e^2 n x \operatorname{Log}[d + e \sqrt{x}] (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2 - \\ & d^2 (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n])^3 - \frac{3}{2} b e^2 n x (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n])^2 \operatorname{Log}[x] + \\ & 3 b^2 n^2 (a - b n \operatorname{Log}[d + e \sqrt{x}] + b \operatorname{Log}[c (d + e \sqrt{x})^n]) \left((d + e \sqrt{x}) \operatorname{Log}[d + e \sqrt{x}] (-2 e \sqrt{x} + (-d + e \sqrt{x}) \operatorname{Log}[d + e \sqrt{x}]) - \right. \\ & \left. 2 e^2 x (-1 + \operatorname{Log}[d + e \sqrt{x}]) \operatorname{Log}\left[-\frac{e \sqrt{x}}{d}\right] - 2 e^2 x \operatorname{PolyLog}\left[2, 1 + \frac{e \sqrt{x}}{d}\right] \right) + \\ & b^3 n^3 \left((d + e \sqrt{x}) \operatorname{Log}[d + e \sqrt{x}]^2 (-3 e \sqrt{x} + (-d + e \sqrt{x}) \operatorname{Log}[d + e \sqrt{x}]) - 3 e^2 x (-2 + \operatorname{Log}[d + e \sqrt{x}]) \operatorname{Log}[d + e \sqrt{x}] \operatorname{Log}\left[-\frac{e \sqrt{x}}{d}\right] - \right. \\ & \left. \left. 6 e^2 x (-1 + \operatorname{Log}[d + e \sqrt{x}]) \operatorname{PolyLog}\left[2, 1 + \frac{e \sqrt{x}}{d}\right] + 6 e^2 x \operatorname{PolyLog}\left[3, 1 + \frac{e \sqrt{x}}{d}\right] \right) \right) \end{aligned}$$

Problem 432: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + \frac{e}{\sqrt{x}})^n])^2}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$-2 \left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^2 \operatorname{Log} \left[-\frac{e}{d\sqrt{x}} \right] - 4 b n \left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right) \operatorname{PolyLog} \left[2, 1 + \frac{e}{d\sqrt{x}} \right] + 4 b^2 n^2 \operatorname{PolyLog} \left[3, 1 + \frac{e}{d\sqrt{x}} \right]$$

Result (type 4, 386 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^2 \operatorname{Log}[x] + \\ & 2 b n \left(a - b n \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right) \left(\left(\operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] - \operatorname{Log} \left[1 + \frac{e}{d\sqrt{x}} \right] \right) \operatorname{Log}[x] + 2 \operatorname{PolyLog} \left[2, -\frac{e}{d\sqrt{x}} \right] \right) + \\ & \frac{1}{12} b^2 n^2 \left(24 \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right]^2 \operatorname{Log} \left[-\frac{d\sqrt{x}}{e} \right] + 12 \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right]^2 \operatorname{Log}[x] - 12 \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right]^2 \operatorname{Log}[x] - 24 \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] \operatorname{Log} \left[1 + \frac{d\sqrt{x}}{e} \right] \operatorname{Log}[x] + \right. \\ & \left. 24 \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \operatorname{Log} \left[1 + \frac{d\sqrt{x}}{e} \right] \operatorname{Log}[x] + 6 \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] \operatorname{Log}[x]^2 - 6 \operatorname{Log} \left[1 + \frac{d\sqrt{x}}{e} \right] \operatorname{Log}[x]^2 + \operatorname{Log}[x]^3 + 48 \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \right. \\ & \left. \operatorname{PolyLog} \left[2, 1 + \frac{d\sqrt{x}}{e} \right] - 48 \left(\operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] - \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \right) \operatorname{PolyLog} \left[2, -\frac{d\sqrt{x}}{e} \right] - 48 \operatorname{PolyLog} \left[3, 1 + \frac{d\sqrt{x}}{e} \right] - 48 \operatorname{PolyLog} \left[3, -\frac{d\sqrt{x}}{e} \right] \right) \end{aligned}$$

Problem 438: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^3}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\begin{aligned} & -2 \left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^3 \operatorname{Log} \left[-\frac{e}{d\sqrt{x}} \right] - 6 b n \left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^2 \operatorname{PolyLog} \left[2, 1 + \frac{e}{d\sqrt{x}} \right] + \\ & 12 b^2 n^2 \left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right) \operatorname{PolyLog} \left[3, 1 + \frac{e}{d\sqrt{x}} \right] - 12 b^3 n^3 \operatorname{PolyLog} \left[4, 1 + \frac{e}{d\sqrt{x}} \right] \end{aligned}$$

Result (type 4, 532 leaves):

$$\begin{aligned}
& \left(a - b n \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^3 \operatorname{Log}[x] + \\
& 3 b n \left(a - b n \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^2 \left(\left(\operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] - \operatorname{Log} \left[1 + \frac{e}{d \sqrt{x}} \right] \right) \operatorname{Log}[x] + 2 \operatorname{PolyLog} \left[2, -\frac{e}{d \sqrt{x}} \right] \right) + \\
& 6 b^2 n^2 \left(a - b n \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] + b \operatorname{Log} \left[c \left(d + \frac{e}{\sqrt{x}} \right)^n \right] \right) \\
& \left(\operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right]^2 \operatorname{Log} \left[-\frac{d \sqrt{x}}{e} \right] + \frac{1}{2} \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right]^2 \operatorname{Log}[x] - \frac{1}{2} \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right]^2 \operatorname{Log}[x] - \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] \operatorname{Log} \left[1 + \frac{d \sqrt{x}}{e} \right] \operatorname{Log}[x] + \right. \\
& \left. \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \operatorname{Log} \left[1 + \frac{d \sqrt{x}}{e} \right] \operatorname{Log}[x] + \frac{1}{4} \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] \operatorname{Log}[x]^2 - \frac{1}{4} \operatorname{Log} \left[1 + \frac{d \sqrt{x}}{e} \right] \operatorname{Log}[x]^2 + \frac{\operatorname{Log}[x]^3}{24} + 2 \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \operatorname{PolyLog} \left[2, 1 + \frac{d \sqrt{x}}{e} \right] - \right. \\
& \left. 2 \left(\operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] - \operatorname{Log} \left[\frac{e}{d} + \sqrt{x} \right] \right) \operatorname{PolyLog} \left[2, -\frac{d \sqrt{x}}{e} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{d \sqrt{x}}{e} \right] - 2 \operatorname{PolyLog} \left[3, -\frac{d \sqrt{x}}{e} \right] \right) - \\
& 2 b^3 n^3 \left(\operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right]^3 \operatorname{Log} \left[-\frac{e}{d \sqrt{x}} \right] + 3 \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right]^2 \operatorname{PolyLog} \left[2, 1 + \frac{e}{d \sqrt{x}} \right] - 6 \operatorname{Log} \left[d + \frac{e}{\sqrt{x}} \right] \operatorname{PolyLog} \left[3, 1 + \frac{e}{d \sqrt{x}} \right] + 6 \operatorname{PolyLog} \left[4, 1 + \frac{e}{d \sqrt{x}} \right] \right)
\end{aligned}$$

Problem 453: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x^{1/3})^n])^2}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$3 (a + b \operatorname{Log}[c (d + e x^{1/3})^n])^2 \operatorname{Log} \left[-\frac{e x^{1/3}}{d} \right] + 6 b n (a + b \operatorname{Log}[c (d + e x^{1/3})^n]) \operatorname{PolyLog} \left[2, 1 + \frac{e x^{1/3}}{d} \right] - 6 b^2 n^2 \operatorname{PolyLog} \left[3, 1 + \frac{e x^{1/3}}{d} \right]$$

Result (type 4, 195 leaves):

$$\begin{aligned}
& (a - b n \operatorname{Log}[d + e x^{1/3}] + b \operatorname{Log}[c (d + e x^{1/3})^n])^2 \operatorname{Log}[x] + \\
& 2 b n (a - b n \operatorname{Log}[d + e x^{1/3}] + b \operatorname{Log}[c (d + e x^{1/3})^n]) \left(\left(\operatorname{Log}[d + e x^{1/3}] - \operatorname{Log} \left[1 + \frac{e x^{1/3}}{d} \right] \right) \operatorname{Log}[x] - 3 \operatorname{PolyLog} \left[2, -\frac{e x^{1/3}}{d} \right] \right) + \\
& 3 b^2 n^2 \left(\operatorname{Log}[d + e x^{1/3}]^2 \operatorname{Log} \left[-\frac{e x^{1/3}}{d} \right] + 2 \operatorname{Log}[d + e x^{1/3}] \operatorname{PolyLog} \left[2, 1 + \frac{e x^{1/3}}{d} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{e x^{1/3}}{d} \right] \right)
\end{aligned}$$

Problem 460: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log}[c (d + e x^{1/3})^n])^3}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$3 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^n \right] \right)^3 \operatorname{Log} \left[-\frac{e x^{1/3}}{d} \right] + 9 b n \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^n \right] \right)^2 \operatorname{PolyLog} \left[2, 1 + \frac{e x^{1/3}}{d} \right] - 18 b^2 n^2 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^n \right] \right) \operatorname{PolyLog} \left[3, 1 + \frac{e x^{1/3}}{d} \right] + 18 b^3 n^3 \operatorname{PolyLog} \left[4, 1 + \frac{e x^{1/3}}{d} \right]$$

Result (type 4, 333 leaves):

$$\begin{aligned} & (a - b n \operatorname{Log} [d + e x^{1/3}] + b \operatorname{Log} [c (d + e x^{1/3})^n])^3 \operatorname{Log} [x] + \\ & 3 b n \left(a - b n \operatorname{Log} [d + e x^{1/3}] + b \operatorname{Log} [c (d + e x^{1/3})^n] \right)^2 \left(\left(\operatorname{Log} [d + e x^{1/3}] - \operatorname{Log} \left[1 + \frac{e x^{1/3}}{d} \right] \right) \operatorname{Log} [x] - 3 \operatorname{PolyLog} \left[2, -\frac{e x^{1/3}}{d} \right] \right) + \\ & 9 b^2 n^2 \left(a - b n \operatorname{Log} [d + e x^{1/3}] + b \operatorname{Log} [c (d + e x^{1/3})^n] \right) \\ & \left(\operatorname{Log} [d + e x^{1/3}]^2 \operatorname{Log} \left[-\frac{e x^{1/3}}{d} \right] + 2 \operatorname{Log} [d + e x^{1/3}] \operatorname{PolyLog} \left[2, 1 + \frac{e x^{1/3}}{d} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{e x^{1/3}}{d} \right] \right) + \\ & 3 b^3 n^3 \left(\operatorname{Log} [d + e x^{1/3}]^3 \operatorname{Log} \left[-\frac{e x^{1/3}}{d} \right] + 3 \operatorname{Log} [d + e x^{1/3}]^2 \operatorname{PolyLog} \left[2, 1 + \frac{e x^{1/3}}{d} \right] - 6 \operatorname{Log} [d + e x^{1/3}] \operatorname{PolyLog} \left[3, 1 + \frac{e x^{1/3}}{d} \right] + 6 \operatorname{PolyLog} \left[4, 1 + \frac{e x^{1/3}}{d} \right] \right) \end{aligned}$$

Problem 473: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log} [c (d + e x^{2/3})^n])^2}{x} dx$$

Optimal (type 4, 95 leaves, 5 steps):

$$\frac{3}{2} \left(a + b \operatorname{Log} [c (d + e x^{2/3})^n] \right)^2 \operatorname{Log} \left[-\frac{e x^{2/3}}{d} \right] + 3 b n \left(a + b \operatorname{Log} [c (d + e x^{2/3})^n] \right) \operatorname{PolyLog} \left[2, 1 + \frac{e x^{2/3}}{d} \right] - 3 b^2 n^2 \operatorname{PolyLog} \left[3, 1 + \frac{e x^{2/3}}{d} \right]$$

Result (type 4, 199 leaves):

$$\begin{aligned} & (a - b n \operatorname{Log} [d + e x^{2/3}] + b \operatorname{Log} [c (d + e x^{2/3})^n])^2 \operatorname{Log} [x] + \\ & 2 b n \left(a - b n \operatorname{Log} [d + e x^{2/3}] + b \operatorname{Log} [c (d + e x^{2/3})^n] \right) \left(\left(\operatorname{Log} [d + e x^{2/3}] - \operatorname{Log} \left[1 + \frac{e x^{2/3}}{d} \right] \right) \operatorname{Log} [x] - \frac{3}{2} \operatorname{PolyLog} \left[2, -\frac{e x^{2/3}}{d} \right] \right) + \\ & \frac{3}{2} b^2 n^2 \left(\operatorname{Log} [d + e x^{2/3}]^2 \operatorname{Log} \left[-\frac{e x^{2/3}}{d} \right] + 2 \operatorname{Log} [d + e x^{2/3}] \operatorname{PolyLog} \left[2, 1 + \frac{e x^{2/3}}{d} \right] - 2 \operatorname{PolyLog} \left[3, 1 + \frac{e x^{2/3}}{d} \right] \right) \end{aligned}$$

Problem 483: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{Log} [c (d + e x^{2/3})^n])^3}{x} dx$$

Optimal (type 4, 139 leaves, 6 steps):

$$\frac{3}{2} (a + b \operatorname{Log}[c (d + e x^{2/3})^n])^3 \operatorname{Log}\left[-\frac{e x^{2/3}}{d}\right] + \frac{9}{2} b n (a + b \operatorname{Log}[c (d + e x^{2/3})^n])^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x^{2/3}}{d}\right] - 9 b^2 n^2 (a + b \operatorname{Log}[c (d + e x^{2/3})^n]) \operatorname{PolyLog}\left[3, 1 + \frac{e x^{2/3}}{d}\right] + 9 b^3 n^3 \operatorname{PolyLog}\left[4, 1 + \frac{e x^{2/3}}{d}\right]$$

Result (type 4, 339 leaves):

$$\begin{aligned} & (a - b n \operatorname{Log}[d + e x^{2/3}] + b \operatorname{Log}[c (d + e x^{2/3})^n])^3 \operatorname{Log}[x] + \\ & 3 b n (a - b n \operatorname{Log}[d + e x^{2/3}] + b \operatorname{Log}[c (d + e x^{2/3})^n])^2 \left(\left(\operatorname{Log}[d + e x^{2/3}] - \operatorname{Log}\left[1 + \frac{e x^{2/3}}{d}\right] \right) \operatorname{Log}[x] - \frac{3}{2} \operatorname{PolyLog}\left[2, -\frac{e x^{2/3}}{d}\right] \right) + \\ & \frac{9}{2} b^2 n^2 (a - b n \operatorname{Log}[d + e x^{2/3}] + b \operatorname{Log}[c (d + e x^{2/3})^n]) \\ & \left(\operatorname{Log}[d + e x^{2/3}]^2 \operatorname{Log}\left[-\frac{e x^{2/3}}{d}\right] + 2 \operatorname{Log}[d + e x^{2/3}] \operatorname{PolyLog}\left[2, 1 + \frac{e x^{2/3}}{d}\right] - 2 \operatorname{PolyLog}\left[3, 1 + \frac{e x^{2/3}}{d}\right] \right) + \frac{3}{2} b^3 n^3 \\ & \left(\operatorname{Log}[d + e x^{2/3}]^3 \operatorname{Log}\left[-\frac{e x^{2/3}}{d}\right] + 3 \operatorname{Log}[d + e x^{2/3}]^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x^{2/3}}{d}\right] - 6 \operatorname{Log}[d + e x^{2/3}] \operatorname{PolyLog}\left[3, 1 + \frac{e x^{2/3}}{d}\right] + 6 \operatorname{PolyLog}\left[4, 1 + \frac{e x^{2/3}}{d}\right] \right) \end{aligned}$$

Problem 500: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^2}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$-3 \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^2 \operatorname{Log}\left[-\frac{e}{d x^{1/3}}\right] - 6 b n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right) \operatorname{PolyLog}\left[2, 1 + \frac{e}{d x^{1/3}}\right] + 6 b^2 n^2 \operatorname{PolyLog}\left[3, 1 + \frac{e}{d x^{1/3}}\right]$$

Result (type 4, 389 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^2 \operatorname{Log}[x] + \\ & 2 b n \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right) \left(\left(\operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] - \operatorname{Log}\left[1 + \frac{e}{d x^{1/3}}\right] \right) \operatorname{Log}[x] + 3 \operatorname{PolyLog}\left[2, -\frac{e}{d x^{1/3}}\right] \right) + \\ & 3 b^2 n^2 \left(2 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 + \frac{d x^{1/3}}{e}\right] - 2 \left(\operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] - \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right] \right) \operatorname{PolyLog}\left[2, -\frac{d x^{1/3}}{e}\right] + \frac{1}{81} \left(81 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right]^2 \operatorname{Log}\left[-\frac{d x^{1/3}}{e}\right] + \right. \right. \\ & \quad \left. \left. 27 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right]^2 \operatorname{Log}[x] - 27 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right]^2 \operatorname{Log}[x] - 54 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x] + 54 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right] \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x] + \right. \right. \\ & \quad \left. \left. 9 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] \operatorname{Log}[x]^2 - 9 \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x]^2 + \operatorname{Log}[x]^3 - 162 \operatorname{PolyLog}\left[3, 1 + \frac{d x^{1/3}}{e}\right] - 162 \operatorname{PolyLog}\left[3, -\frac{d x^{1/3}}{e}\right] \right) \right) \end{aligned}$$

Problem 505: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^3}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$-3 \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^3 \operatorname{Log}\left[-\frac{e}{d x^{1/3}}\right] - 9 b n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d x^{1/3}}\right] + 18 b^2 n^2 \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right) \operatorname{PolyLog}\left[3, 1 + \frac{e}{d x^{1/3}}\right] - 18 b^3 n^3 \operatorname{PolyLog}\left[4, 1 + \frac{e}{d x^{1/3}}\right]$$

Result (type 4, 527 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^3 \operatorname{Log}[x] + \\ & 3 b n \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^2 \left(\left(\operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] - \operatorname{Log}\left[1 + \frac{e}{d x^{1/3}}\right]\right) \operatorname{Log}[x] + 3 \operatorname{PolyLog}\left[2, -\frac{e}{d x^{1/3}}\right]\right) + \\ & 9 b^2 n^2 \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right) \left(2 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 + \frac{d x^{1/3}}{e}\right] - 2 \left(\operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] - \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right]\right) \operatorname{PolyLog}\left[2, -\frac{d x^{1/3}}{e}\right] + \frac{1}{81} \left(81 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right]^2 \operatorname{Log}\left[-\frac{d x^{1/3}}{e}\right] + \right. \right. \\ & \quad \left. \left. 27 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right]^2 \operatorname{Log}[x] - 27 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right]^2 \operatorname{Log}[x] - 54 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x] + 54 \operatorname{Log}\left[\frac{e}{d} + x^{1/3}\right] \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x] + \right. \right. \\ & \quad \left. \left. 9 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] \operatorname{Log}[x]^2 - 9 \operatorname{Log}\left[1 + \frac{d x^{1/3}}{e}\right] \operatorname{Log}[x]^2 + \operatorname{Log}[x]^3 - 162 \operatorname{PolyLog}\left[3, 1 + \frac{d x^{1/3}}{e}\right] - 162 \operatorname{PolyLog}\left[3, -\frac{d x^{1/3}}{e}\right]\right)\right) - \\ & 3 b^3 n^3 \left(\operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right]^3 \operatorname{Log}\left[-\frac{e}{d x^{1/3}}\right] + 3 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right]^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d x^{1/3}}\right] - 6 \operatorname{Log}\left[d + \frac{e}{x^{1/3}}\right] \operatorname{PolyLog}\left[3, 1 + \frac{e}{d x^{1/3}}\right] + 6 \operatorname{PolyLog}\left[4, 1 + \frac{e}{d x^{1/3}}\right]\right) \end{aligned}$$

Problem 518: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2}{x} dx$$

Optimal (type 4, 95 leaves, 5 steps):

$$-\frac{3}{2} \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2 \operatorname{Log}\left[-\frac{e}{d x^{2/3}}\right] - 3 b n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right) \operatorname{PolyLog}\left[2, 1 + \frac{e}{d x^{2/3}}\right] + 3 b^2 n^2 \operatorname{PolyLog}\left[3, 1 + \frac{e}{d x^{2/3}}\right]$$

Result (type 4, 1701 leaves):

$$\begin{aligned}
& \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right] \right)^2 \operatorname{Log}[x] + \\
& 2 b n \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right] \right) \left(\left(\operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - \operatorname{Log}\left[1 + \frac{e}{d x^{2/3}}\right] \right) \operatorname{Log}[x] + \frac{3}{2} \operatorname{PolyLog}\left[2, -\frac{e}{d x^{2/3}}\right] \right) + \\
& 3 b^2 n^2 \left(\operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \right. \\
& \left. \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \left(-2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) \left(\operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) + \right. \\
& \left. \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \left(-\operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) + \right. \\
& \left. \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right]^2 \left(\operatorname{Log}\left[\frac{2 \sqrt{e}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] + \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \operatorname{Log}\left[\frac{2 x^{1/3}}{-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}}\right] \right) + \right. \\
& \left. \frac{1}{3} \left(-\operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \frac{2 \operatorname{Log}[x]}{3} \right)^2 \operatorname{Log}[x] + \frac{4 \operatorname{Log}[x]^3}{81} + \right. \\
& \left. 2 \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \left(-\operatorname{PolyLog}\left[2, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{i \sqrt{e} - \sqrt{d} x^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{-i \sqrt{e} + \sqrt{d} x^{1/3}}\right] \right) + \right. \\
& \left. 2 \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \left(\operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \right) \operatorname{PolyLog}\left[2, 1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \right. \\
& \left. 2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \left(\operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \right) \operatorname{PolyLog}\left[2, 1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \right. \\
& \left. 2 \left(\operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \frac{2 \operatorname{Log}[x]}{3} \right) \right. \\
& \left(\frac{1}{9} \left(3 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + 3 \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - 3 \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - 3 \operatorname{Log}\left[1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \operatorname{Log}[x] \right) \operatorname{Log}[x] - \operatorname{PolyLog}\left[2, -\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \right. \\
& \left. \operatorname{PolyLog}\left[2, \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) + 2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{i \sqrt{e} - \sqrt{d} x^{1/3}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{-i \sqrt{e} + \sqrt{d} x^{1/3}}\right] - 4 \operatorname{PolyLog}\left[3, 1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \\
& \left. 4 \operatorname{PolyLog}\left[3, 1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \frac{2}{9} \left(\left(\operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) \operatorname{Log}[x]^2 + \left(\operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \operatorname{Log}\left[1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) \operatorname{Log}[x]^2 - \right.
\end{aligned}$$

$$6 \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] - 6 \operatorname{Log}[x] \operatorname{PolyLog}\left[2, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 18 \operatorname{PolyLog}\left[3, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 18 \operatorname{PolyLog}\left[3, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \Bigg)$$

Problem 523: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2}{x^2} dx$$

Optimal (type 4, 361 leaves, 19 steps):

$$\begin{aligned} & -\frac{8 b^2 n^2}{9 x} + \frac{32 b^2 d n^2}{3 e x^{1/3}} + \frac{32 b^2 d^{3/2} n^2 \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right]}{3 e^{3/2}} + \frac{4 i b^2 d^{3/2} n^2 \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right]^2}{e^{3/2}} - \\ & \frac{8 b^2 d^{3/2} n^2 \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}\left[2 - \frac{2\sqrt{e}}{\sqrt{e} - i\sqrt{d} x^{1/3}}\right]}{e^{3/2}} + \frac{4 b n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)}{3 x} - \frac{4 b d n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)}{e x^{1/3}} - \\ & \frac{4 b d^{3/2} n \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)}{e^{3/2}} - \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2}{x} + \frac{4 i b^2 d^{3/2} n^2 \operatorname{PolyLog}\left[2, -1 + \frac{2\sqrt{e}}{\sqrt{e} - i\sqrt{d} x^{1/3}}\right]}{e^{3/2}} \end{aligned}$$

Result (type 4, 797 leaves):

$$\begin{aligned} & \frac{1}{9 e^{3/2} x} \left(6 b n \left(-6 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \sqrt{e} \left(2 e - 6 d x^{2/3} - 3 e \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right]\right) \right) \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right] \right) - \right. \\ & 9 e^{3/2} \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right] \right)^2 + b^2 n^2 \left(-8 e^{3/2} + 96 d \sqrt{e} x^{2/3} + 96 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 12 e^{3/2} \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - \right. \\ & 36 d \sqrt{e} x^{2/3} \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - 36 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - 9 e^{3/2} \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right]^2 + 36 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}\left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \\ & 9 i d^{3/2} x \operatorname{Log}\left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 + 36 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}\left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - 9 i d^{3/2} x \operatorname{Log}\left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 - \\ & 18 i d^{3/2} x \operatorname{Log}\left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{d} x^{1/3}}{2\sqrt{e}}\right] + 18 i d^{3/2} x \operatorname{Log}\left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{d} x^{1/3}}{2\sqrt{e}}\right] - 24 d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}[x] + \\ & 12 i d^{3/2} x \operatorname{Log}\left[1 - \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}[x] - 12 i d^{3/2} x \operatorname{Log}\left[1 + \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \operatorname{Log}[x] + 18 i d^{3/2} x \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{d} x^{1/3}}{2\sqrt{e}}\right] - \\ & \left. \left. 18 i d^{3/2} x \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{d} x^{1/3}}{2\sqrt{e}}\right] - 36 i d^{3/2} x \operatorname{PolyLog}\left[2, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 36 i d^{3/2} x \operatorname{PolyLog}\left[2, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}}\right] \right) \right) \end{aligned}$$

Problem 526: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^3}{x} dx$$

Optimal (type 4, 139 leaves, 6 steps):

$$-\frac{3}{2} \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^3 \operatorname{Log}\left[-\frac{e}{d x^{2/3}}\right] - \frac{9}{2} b n \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d x^{2/3}}\right] + 9 b^2 n^2 \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right) \operatorname{PolyLog}\left[3, 1 + \frac{e}{d x^{2/3}}\right] - 9 b^3 n^3 \operatorname{PolyLog}\left[4, 1 + \frac{e}{d x^{2/3}}\right]$$

Result (type 4, 1841 leaves):

$$\begin{aligned} & \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^3 \operatorname{Log}[x] + \\ & 3 b n \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2 \left(\left(\operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] - \operatorname{Log}\left[1 + \frac{e}{d x^{2/3}}\right]\right) \operatorname{Log}[x] + \frac{3}{2} \operatorname{PolyLog}\left[2, -\frac{e}{d x^{2/3}}\right]\right) + 9 b^2 n^2 \\ & \left(a - b n \operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right) \left(\operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \right. \\ & \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \left(-2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right]\right) \left(\operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right]\right) + \\ & \left. \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right]^2 \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \operatorname{Log}\left[1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] \left(-\operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \operatorname{Log}\left[\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right]\right) + \right. \\ & \left. \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right]^2 \left(\operatorname{Log}\left[\frac{2 \sqrt{e}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] + \operatorname{Log}\left[-\frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] - \operatorname{Log}\left[\frac{2 x^{1/3}}{-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}}\right]\right) + \right. \\ & \left. \frac{1}{3} \left(-\operatorname{Log}\left[d + \frac{e}{x^{2/3}}\right] + \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \frac{2 \operatorname{Log}[x]}{3}\right)^2 \operatorname{Log}[x] + \frac{4 \operatorname{Log}[x]^3}{81} + \right. \\ & 2 \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right] \left(-\operatorname{PolyLog}\left[2, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{i \sqrt{e} - \sqrt{d} x^{1/3}}\right] + \operatorname{PolyLog}\left[2, \frac{i \sqrt{e} + \sqrt{d} x^{1/3}}{-i \sqrt{e} + \sqrt{d} x^{1/3}}\right]\right) + \\ & 2 \operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \left(\operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] + \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right]\right) \operatorname{PolyLog}\left[2, 1 - \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \\ & 2 \operatorname{Log}\left[-\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] \operatorname{PolyLog}\left[2, 1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + 2 \left(\operatorname{Log}\left[\frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3}\right] - \operatorname{Log}\left[\frac{\sqrt{e} - i \sqrt{d} x^{1/3}}{\sqrt{e} + i \sqrt{d} x^{1/3}}\right]\right) \operatorname{PolyLog}\left[2, 1 + \frac{i \sqrt{d} x^{1/3}}{\sqrt{e}}\right] + \end{aligned}$$

$$\begin{aligned}
& 2 \left(\operatorname{Log} \left[d + \frac{e}{x^{2/3}} \right] - \operatorname{Log} \left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - \operatorname{Log} \left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] + \frac{2 \operatorname{Log}[x]}{3} \right) \\
& \left(\frac{1}{9} \left(3 \operatorname{Log} \left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] + 3 \operatorname{Log} \left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - 3 \operatorname{Log} \left[1 - \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - 3 \operatorname{Log} \left[1 + \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - \operatorname{Log}[x] \right) \operatorname{Log}[x] - \operatorname{PolyLog} \left[2, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - \right. \\
& \quad \left. \operatorname{PolyLog} \left[2, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] \right) + 2 \operatorname{PolyLog} \left[3, \frac{i\sqrt{e} + \sqrt{d} x^{1/3}}{i\sqrt{e} - \sqrt{d} x^{1/3}} \right] - 2 \operatorname{PolyLog} \left[3, \frac{i\sqrt{e} + \sqrt{d} x^{1/3}}{-i\sqrt{e} + \sqrt{d} x^{1/3}} \right] - 4 \operatorname{PolyLog} \left[3, 1 - \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - \\
& 4 \operatorname{PolyLog} \left[3, 1 + \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - \frac{2}{9} \left(\left(\operatorname{Log} \left[\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - \operatorname{Log} \left[1 - \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] \right) \operatorname{Log}[x]^2 + \left(\operatorname{Log} \left[-\frac{i\sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - \operatorname{Log} \left[1 + \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] \right) \operatorname{Log}[x]^2 - \right. \\
& \quad \left. 6 \operatorname{Log}[x] \operatorname{PolyLog} \left[2, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] - 6 \operatorname{Log}[x] \operatorname{PolyLog} \left[2, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] + 18 \operatorname{PolyLog} \left[3, -\frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] + 18 \operatorname{PolyLog} \left[3, \frac{i\sqrt{d} x^{1/3}}{\sqrt{e}} \right] \right) \left. \right) - \\
& \frac{3}{2} b^3 n^3 \left(\operatorname{Log} \left[d + \frac{e}{x^{2/3}} \right]^3 \operatorname{Log} \left[-\frac{e}{d x^{2/3}} \right] + 3 \operatorname{Log} \left[d + \frac{e}{x^{2/3}} \right]^2 \operatorname{PolyLog} \left[2, 1 + \frac{e}{d x^{2/3}} \right] - 6 \operatorname{Log} \left[d + \frac{e}{x^{2/3}} \right] \operatorname{PolyLog} \left[3, 1 + \frac{e}{d x^{2/3}} \right] + 6 \operatorname{PolyLog} \left[4, 1 + \frac{e}{d x^{2/3}} \right] \right)
\end{aligned}$$

Problem 538: Unable to integrate problem.

$$\int x^3 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 907 leaves, 27 steps):

$$\begin{aligned}
& \frac{2^{-2(1+p)} e^{-\frac{4a}{b}} \text{Gamma}\left[1+p, -\frac{4(a+b \text{Log}[c(d+e\sqrt{x})^2])}{b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p}}{c^4 e^8} - \frac{1}{e^8 (c(d+e\sqrt{x})^2)^{7/2}} \\
& 2^{1+p} \times 7^{-p} d e^{-\frac{7a}{2b}} (d+e\sqrt{x})^7 \text{Gamma}\left[1+p, -\frac{7(a+b \text{Log}[c(d+e\sqrt{x})^2])}{2b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p} + \\
& \frac{7 \times 3^{-p} d^2 e^{-\frac{3a}{b}} \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e\sqrt{x})^2])}{b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p}}{c^3 e^8} - \frac{1}{e^8 (c(d+e\sqrt{x})^2)^{5/2}} \\
& 7 \times 2^{1+p} \times 5^{-p} d^3 e^{-\frac{5a}{2b}} (d+e\sqrt{x})^5 \text{Gamma}\left[1+p, -\frac{5(a+b \text{Log}[c(d+e\sqrt{x})^2])}{2b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p} + \\
& \frac{35 \times 2^{-1-p} d^4 e^{-\frac{2a}{b}} \text{Gamma}\left[1+p, -\frac{2(a+b \text{Log}[c(d+e\sqrt{x})^2])}{b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p}}{c^2 e^8} - \frac{1}{e^8 (c(d+e\sqrt{x})^2)^{3/2}} \\
& 7 \times 2^{1+p} \times 3^{-p} d^5 e^{-\frac{3a}{2b}} (d+e\sqrt{x})^3 \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e\sqrt{x})^2])}{2b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p} + \\
& \frac{7 d^6 e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p}}{c e^8} - \frac{1}{e^8 \sqrt{c(d+e\sqrt{x})^2}} \\
& 2^{1+p} d^7 e^{-\frac{a}{2b}} (d+e\sqrt{x}) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{2b}\right] (a+b \text{Log}[c(d+e\sqrt{x})^2])^p \left(-\frac{a+b \text{Log}[c(d+e\sqrt{x})^2]}{b}\right)^{-p}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int x^3 (a+b \text{Log}[c(d+e\sqrt{x})^2])^p dx$$

Problem 539: Unable to integrate problem.

$$\int x^2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 677 leaves, 21 steps):

$$\frac{3^{-1-p} e^{-\frac{3a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{3 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}}{c^3 e^6} - \frac{1}{e^6 \left(c \left(d + e \sqrt{x} \right)^2 \right)^{5/2}}$$

$$2^{1+p} \times 5^{-p} d e^{-\frac{5a}{2b}} \left(d + e \sqrt{x} \right)^5 \operatorname{Gamma} \left[1 + p, -\frac{5 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{2b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{5 \times 2^{-p} d^2 e^{-\frac{2a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}}{c^2 e^6} - \frac{1}{e^6 \left(c \left(d + e \sqrt{x} \right)^2 \right)^{3/2}}$$

$$5 \times 2^{2+p} \times 3^{-1-p} d^3 e^{-\frac{3a}{2b}} \left(d + e \sqrt{x} \right)^3 \operatorname{Gamma} \left[1 + p, -\frac{3 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{2b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{5 d^4 e^{-\frac{a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}}{c e^6} - \frac{1}{e^6 \sqrt{c \left(d + e \sqrt{x} \right)^2}}$$

$$2^{1+p} d^5 e^{-\frac{a}{2b}} \left(d + e \sqrt{x} \right) \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{2b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 26 leaves):

$$\int x^2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Problem 540: Unable to integrate problem.

$$\int x \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 445 leaves, 15 steps):

$$\frac{2^{-1+p} e^{-\frac{2a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{2 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}}{c^2 e^4} - \frac{1}{e^4 \left(c \left(d + e \sqrt{x} \right)^2 \right)^{3/2}}$$

$$2^{1+p} \times 3^{-p} d e^{-\frac{3a}{2b}} \left(d + e \sqrt{x} \right)^3 \operatorname{Gamma} \left[1 + p, -\frac{3 \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)}{2b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{3 d^2 e^{-\frac{a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}}{c e^4} - \frac{1}{e^4 \sqrt{c \left(d + e \sqrt{x} \right)^2}}$$

$$2^{1+p} d^3 e^{-\frac{3a}{2b}} \left(d + e \sqrt{x} \right) \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{2b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 24 leaves):

$$\int x \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Problem 541: Unable to integrate problem.

$$\int \left(a + b \operatorname{Log} \left[c \left(d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\frac{e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]}{b}\right] \left(a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]}{b}\right)^{-p}}{c e^2} - \frac{1}{e^2 \sqrt{c\left(d+e\sqrt{x}\right)^2}}$$

$$2^{1+p} d e^{-\frac{a}{2b}} \left(d+e\sqrt{x}\right) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]}{2b}\right] \left(a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]}{b}\right)^{-p}$$

Result (type 8, 22 leaves):

$$\int \left(a+b \text{Log}\left[c\left(d+e\sqrt{x}\right)^2\right]\right)^p dx$$

Problem 553: Unable to integrate problem.

$$\int \frac{\left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^2} dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\frac{e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c e^2} +$$

$$\frac{2^{1+p} d e^{-\frac{a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{2b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{e^2 \sqrt{c\left(d+\frac{e}{\sqrt{x}}\right)^2}}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^2} dx$$

Problem 554: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^4} dx$$

Optimal (type 4, 676 leaves, 21 steps):

$$\begin{aligned} & - \frac{3^{-1-p} e^{-\frac{3a}{b}} \operatorname{Gamma}\left[1+p, -\frac{3\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^3 e^6} + \frac{1}{e^6 \left(c \left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{5/2}} \\ & 2^{1+p} \times 5^{-p} d e^{-\frac{5a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right)^5 \operatorname{Gamma}\left[1+p, -\frac{5\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p} - \\ & \frac{5 \times 2^{-p} d^2 e^{-\frac{2a}{b}} \operatorname{Gamma}\left[1+p, -\frac{2\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^2 e^6} + \frac{1}{e^6 \left(c \left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{3/2}} \\ & 5 \times 2^{2+p} \times 3^{-1-p} d^3 e^{-\frac{3a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right)^3 \operatorname{Gamma}\left[1+p, -\frac{3\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p} - \\ & \frac{5 d^4 e^{-\frac{a}{b}} \operatorname{Gamma}\left[1+p, -\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c e^6} + \\ & \frac{2^{1+p} d^5 e^{-\frac{a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right) \operatorname{Gamma}\left[1+p, -\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{e^6 \sqrt{c \left(d+\frac{e}{\sqrt{x}}\right)^2}} \end{aligned}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^4} dx$$

Problem 555: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^6} dx$$

Optimal (type 4, 1141 leaves, 33 steps):

$$\frac{5^{-1-p} e^{-\frac{5a}{b}} \operatorname{Gamma}\left[1+p, -\frac{5\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^5 e^{10}} + \frac{1}{e^{10} \left(c \left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{9/2}}$$

$$2^{1+p} \times 9^{-p} d e^{-\frac{9a}{2b}} \left(d + \frac{e}{\sqrt{x}}\right)^9 \operatorname{Gamma}\left[1+p, -\frac{9\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p} -$$

$$\frac{9 \times 4^{-p} d^2 e^{-\frac{4a}{b}} \operatorname{Gamma}\left[1+p, -\frac{4\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^4 e^{10}} + \frac{1}{e^{10} \left(c \left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{7/2}}$$

$$3 \times 2^{3+p} \times 7^{-p} d^3 e^{-\frac{7a}{2b}} \left(d + \frac{e}{\sqrt{x}}\right)^7 \operatorname{Gamma}\left[1+p, -\frac{7\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p} -$$

$$\frac{14 \times 3^{1-p} d^4 e^{-\frac{3a}{b}} \operatorname{Gamma}\left[1+p, -\frac{3\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^3 e^{10}} + \frac{1}{e^{10} \left(c \left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{5/2}}$$

$$63 \times 2^{2+p} \times 5^{-1-p} d^5 e^{-\frac{5a}{2b}} \left(d + \frac{e}{\sqrt{x}}\right)^5 \operatorname{Gamma}\left[1+p, -\frac{5\left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \operatorname{Log}\left[c \left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p} -$$

$$\begin{aligned}
& \frac{21 \times 2^{1-p} d^6 e^{-\frac{2a}{b}} \text{Gamma}\left[1+p, -\frac{2\left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^2 e^{10}} + \frac{1}{e^{10} \left(c\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{3/2}} \\
& \frac{2^{3+p} \times 3^{1-p} d^7 e^{-\frac{3a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right)^3 \text{Gamma}\left[1+p, -\frac{3\left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c^2 e^{10}} - \\
& \frac{9 d^8 e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{c e^{10}} + \\
& \frac{2^{1+p} d^9 e^{-\frac{a}{2b}} \left(d+\frac{e}{\sqrt{x}}\right) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{2b}\right] \left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right)^{-p}}{e^{10} \sqrt{c\left(d+\frac{e}{\sqrt{x}}\right)^2}}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a+b \text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^6} dx$$

Problem 562: Unable to integrate problem.

$$\int x^3 \left(a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]\right)^p dx$$

Optimal (type 4, 1363 leaves, 39 steps):

$$\begin{aligned}
& \frac{2^{-2-p} \times 3^{-p} e^{-\frac{6a}{b}} \text{Gamma}\left[1+p, -\frac{6\left(a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]\right)}{b}\right] \left(a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]}{b}\right)^{-p}}{c^6 e^{12}} - \frac{1}{e^{12} \left(c\left(d+e x^{1/3}\right)^2\right)^{11/2}} \\
& 3 \left(\frac{2}{11}\right)^p d e^{-\frac{11a}{2b}} \left(d+e x^{1/3}\right)^{11} \text{Gamma}\left[1+p, -\frac{11\left(a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c\left(d+e x^{1/3}\right)^2\right]}{b}\right)^{-p} +
\end{aligned}$$

$$\begin{aligned}
& \frac{33 \times 5^{-p} d^2 e^{-\frac{5a}{b}} \text{Gamma}\left[1+p, -\frac{5(a+b \text{Log}[c(d+e x^{1/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p}}{2 c^5 e^{12}} - \frac{1}{e^{12} (c(d+e x^{1/3})^2)^{9/2}} \\
& 55 \left(\frac{2}{9}\right)^p d^3 e^{-\frac{9a}{2b}} (d+e x^{1/3})^9 \text{Gamma}\left[1+p, -\frac{9(a+b \text{Log}[c(d+e x^{1/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} + \frac{1}{c^4 e^{12}} 495 \times \\
& 2^{-2(1+p)} d^4 e^{-\frac{4a}{b}} \text{Gamma}\left[1+p, -\frac{4(a+b \text{Log}[c(d+e x^{1/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} - \frac{1}{e^{12} (c(d+e x^{1/3})^2)^{7/2}} \\
& 99 \times 2^{1+p} \times 7^{-p} d^5 e^{-\frac{7a}{2b}} (d+e x^{1/3})^7 \text{Gamma}\left[1+p, -\frac{7(a+b \text{Log}[c(d+e x^{1/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} + \\
& \frac{77 \times 3^{1-p} d^6 e^{-\frac{3a}{b}} \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e x^{1/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p}}{c^3 e^{12}} - \frac{1}{e^{12} (c(d+e x^{1/3})^2)^{5/2}} \\
& 99 \times 2^{1+p} \times 5^{-p} d^7 e^{-\frac{5a}{2b}} (d+e x^{1/3})^5 \text{Gamma}\left[1+p, -\frac{5(a+b \text{Log}[c(d+e x^{1/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} + \frac{1}{c^2 e^{12}} \\
& 495 \times 2^{-2-p} d^8 e^{-\frac{2a}{b}} \text{Gamma}\left[1+p, -\frac{2(a+b \text{Log}[c(d+e x^{1/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} - \frac{1}{e^{12} (c(d+e x^{1/3})^2)^{3/2}} \\
& 55 \left(\frac{2}{3}\right)^p d^9 e^{-\frac{3a}{2b}} (d+e x^{1/3})^3 \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e x^{1/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p} + \\
& \frac{33 d^{10} e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p}}{2 c e^{12}} - \frac{1}{e^{12} \sqrt{c(d+e x^{1/3})^2}} \\
& 3 \times 2^p d^{11} e^{-\frac{a}{2b}} (d+e x^{1/3}) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{2b}\right] (a+b \text{Log}[c(d+e x^{1/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{1/3})^2]}{b}\right)^{-p}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int x^3 (a+b \text{Log}[c(d+e x^{1/3})^2])^p dx$$

Problem 563: Unable to integrate problem.

$$\int x^2 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 1035 leaves, 30 steps):

$$\begin{aligned}
& \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{9/2}} \\
& \frac{2^p \times 3^{-1-2p} e^{-\frac{9a}{2b}} \left(d + e x^{1/3} \right)^9 \text{Gamma} \left[1 + p, -\frac{9 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^4 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{7/2}} \\
& \frac{3 \times 4^{-p} d e^{-\frac{4a}{b}} \text{Gamma} \left[1 + p, -\frac{4 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^3 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{5/2}} \\
& \frac{3 \times 2^{2+p} \times 7^{-p} d^2 e^{-\frac{7a}{2b}} \left(d + e x^{1/3} \right)^7 \text{Gamma} \left[1 + p, -\frac{7 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^3 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{5/2}} \\
& \frac{28 \times 3^{-p} d^3 e^{-\frac{3a}{b}} \text{Gamma} \left[1 + p, -\frac{3 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^3 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{5/2}} \\
& \frac{21 \times 2^{1+p} \times 5^{-p} d^4 e^{-\frac{5a}{2b}} \left(d + e x^{1/3} \right)^5 \text{Gamma} \left[1 + p, -\frac{5 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^2 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{3/2}} \\
& \frac{21 \times 2^{1-p} d^5 e^{-\frac{2a}{b}} \text{Gamma} \left[1 + p, -\frac{2 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^2 e^9} + \frac{1}{e^9 \left(c \left(d + e x^{1/3} \right)^2 \right)^{3/2}} \\
& \frac{7 \times 2^{2+p} \times 3^{-p} d^6 e^{-\frac{3a}{2b}} \left(d + e x^{1/3} \right)^3 \text{Gamma} \left[1 + p, -\frac{3 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c e^9} + \frac{1}{e^9 \sqrt{c \left(d + e x^{1/3} \right)^2}} \\
& \frac{12 d^7 e^{-\frac{a}{b}} \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c e^9} + \frac{1}{e^9 \sqrt{c \left(d + e x^{1/3} \right)^2}} \\
& \frac{3 \times 2^p d^8 e^{-\frac{a}{2b}} \left(d + e x^{1/3} \right) \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c e^9} + \frac{1}{e^9 \sqrt{c \left(d + e x^{1/3} \right)^2}}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int x^2 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Problem 564: Unable to integrate problem.

$$\int x \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 673 leaves, 21 steps):

$$\frac{3^{-p} e^{-\frac{3a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{3 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{2 c^3 e^6} - \frac{1}{e^6 \left(c \left(d + e x^{1/3} \right)^2 \right)^{5/2}}$$

$$+ 3 \left(\frac{2}{5} \right)^p d e^{-\frac{5a}{2b}} \left(d + e x^{1/3} \right)^5 \operatorname{Gamma} \left[1 + p, -\frac{5 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2 b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{15 \times 2^{-1-p} d^2 e^{-\frac{2a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{2 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c^2 e^6} - \frac{1}{e^6 \left(c \left(d + e x^{1/3} \right)^2 \right)^{3/2}}$$

$$+ 5 \times 2^{1+p} \times 3^{-p} d^3 e^{-\frac{3a}{2b}} \left(d + e x^{1/3} \right)^3 \operatorname{Gamma} \left[1 + p, -\frac{3 \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2 b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{15 d^4 e^{-\frac{a}{b}} \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{2 c e^6} - \frac{1}{e^6 \sqrt{c \left(d + e x^{1/3} \right)^2}}$$

$$+ 3 \times 2^p d^5 e^{-\frac{a}{2b}} \left(d + e x^{1/3} \right) \operatorname{Gamma} \left[1 + p, -\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{2 b} \right] \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 24 leaves):

$$\int x \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Problem 565: Unable to integrate problem.

$$\int \left(a + b \operatorname{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 338 leaves, 12 steps):

$$\frac{1}{e^3 \left(c \left(d + e x^{1/3} \right)^2 \right)^{3/2}}$$

$$\left(\frac{2}{3} \right)^p e^{-\frac{3a}{2b}} \left(d + e x^{1/3} \right)^3 \text{Gamma} \left[1 + p, -\frac{3 \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p} -$$

$$\frac{3 d e^{-\frac{a}{b}} \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}}{c e^3} + \frac{1}{e^3 \sqrt{c \left(d + e x^{1/3} \right)^2}}$$

$$3 \times 2^p d^2 e^{-\frac{a}{2b}} \left(d + e x^{1/3} \right) \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 22 leaves):

$$\int \left(a + b \text{Log} \left[c \left(d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Problem 575: Unable to integrate problem.

$$\int x^3 \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 675 leaves, 21 steps):

$$\begin{aligned}
& \frac{3^{-p} e^{-\frac{3a}{b}} \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e x^{2/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p}}{4 c^3 e^6} - \frac{1}{e^6 (c(d+e x^{2/3})^2)^{5/2}} \\
& 3 \times 2^{-1+p} \times 5^{-p} d e^{-\frac{5a}{2b}} (d+e x^{2/3})^5 \text{Gamma}\left[1+p, -\frac{5(a+b \text{Log}[c(d+e x^{2/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p} + \\
& \frac{15 \times 2^{-2+p} d^2 e^{-\frac{2a}{b}} \text{Gamma}\left[1+p, -\frac{2(a+b \text{Log}[c(d+e x^{2/3})^2])}{b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p}}{c^2 e^6} - \frac{1}{e^6 (c(d+e x^{2/3})^2)^{3/2}} \\
& 5 \left(\frac{2}{3}\right)^p d^3 e^{-\frac{3a}{2b}} (d+e x^{2/3})^3 \text{Gamma}\left[1+p, -\frac{3(a+b \text{Log}[c(d+e x^{2/3})^2])}{2b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p} + \\
& \frac{15 d^4 e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p}}{4 c e^6} - \frac{1}{e^6 \sqrt{c(d+e x^{2/3})^2}} \\
& 3 \times 2^{-1+p} d^5 e^{-\frac{a}{2b}} (d+e x^{2/3}) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{2b}\right] (a+b \text{Log}[c(d+e x^{2/3})^2])^p \left(-\frac{a+b \text{Log}[c(d+e x^{2/3})^2]}{b}\right)^{-p}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int x^3 (a+b \text{Log}[c(d+e x^{2/3})^2])^p dx$$

Problem 576: Unable to integrate problem.

$$\int x (a+b \text{Log}[c(d+e x^{2/3})^2])^p dx$$

Optimal (type 4, 347 leaves, 12 steps):

$$\frac{1}{e^3 \left(c \left(d + e x^{2/3} \right)^2 \right)^{3/2}}$$

$$2^{-1+p} \times 3^{-p} e^{-\frac{3a}{2b}} \left(d + e x^{2/3} \right)^3 \text{Gamma} \left[1 + p, -\frac{3 \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right]}{b} \right)^{-p} -$$

$$\frac{3 d e^{-\frac{a}{b}} \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right]}{b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right]}{b} \right)^{-p}}{2 c e^3} + \frac{1}{e^3 \sqrt{c \left(d + e x^{2/3} \right)^2}}$$

$$3 \times 2^{-1+p} d^2 e^{-\frac{a}{2b}} \left(d + e x^{2/3} \right) \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right]}{2b} \right] \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 24 leaves):

$$\int x \left(a + b \text{Log} \left[c \left(d + e x^{2/3} \right)^2 \right] \right)^p dx$$

Problem 591: Unable to integrate problem.

$$\int \frac{\left(a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p}{x^2} dx$$

Optimal (type 4, 339 leaves, 12 steps):

$$-\frac{1}{e^3 \left(c \left(d + \frac{e}{x^{1/3}} \right)^2 \right)^{3/2}} \left(\frac{2}{3} \right)^p e^{-\frac{3a}{2b}} \left(d + \frac{e}{x^{1/3}} \right)^3 \text{Gamma} \left[1 + p, -\frac{3 \left(a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)}{2b} \right] \left(a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right]}{b} \right)^{-p} +$$

$$\frac{3 d e^{-\frac{a}{b}} \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right]}{b} \right] \left(a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right]}{b} \right)^{-p}}{c e^3} - \frac{1}{e^3 \sqrt{c \left(d + \frac{e}{x^{1/3}} \right)^2}}$$

$$3 \times 2^p d^2 e^{-\frac{a}{2b}} \left(d + \frac{e}{x^{1/3}} \right) \text{Gamma} \left[1 + p, -\frac{a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right]}{2b} \right] \left(a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p \left(-\frac{a + b \text{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right]}{b} \right)^{-p}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^2} dx$$

Problem 592: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^3} dx$$

Optimal (type 4, 673 leaves, 21 steps):

$$\begin{aligned} & - \frac{3^{-p} e^{-\frac{3a}{b}} \operatorname{Gamma}\left[1 + p, -\frac{3\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{2 c^3 e^6} + \frac{1}{e^6 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{5/2}} \\ & 3 \left(\frac{2}{5}\right)^p d e^{-\frac{5a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^5 \operatorname{Gamma}\left[1 + p, -\frac{5\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} - \\ & \frac{15 \times 2^{-1-p} d^2 e^{-\frac{2a}{b}} \operatorname{Gamma}\left[1 + p, -\frac{2\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{c^2 e^6} + \frac{1}{e^6 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{3/2}} \\ & 5 \times 2^{1+p} \times 3^{-p} d^3 e^{-\frac{3a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^3 \operatorname{Gamma}\left[1 + p, -\frac{3\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} - \\ & \frac{15 d^4 e^{-\frac{a}{b}} \operatorname{Gamma}\left[1 + p, -\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{2 c e^6} + \frac{1}{e^6 \sqrt{c \left(d + \frac{e}{x^{1/3}}\right)^2}} \\ & 3 \times 2^p d^5 e^{-\frac{a}{2b}} \left(d + \frac{e}{x^{1/3}}\right) \operatorname{Gamma}\left[1 + p, -\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{2b}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} \end{aligned}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p}{x^3} dx$$

Problem 593: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{Log} \left[c \left(d + \frac{e}{x^{1/3}} \right)^2 \right] \right)^p}{x^4} dx$$

Optimal (type 4, 1036 leaves, 30 steps):

$$\begin{aligned}
& - \frac{1}{e^9 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{9/2}} 2^p \times 3^{-1-2p} e^{-\frac{9a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^9 \text{Gamma}\left[1+p, -\frac{9\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} + \\
& \frac{3 \times 4^{-p} d e^{-\frac{4a}{b}} \text{Gamma}\left[1+p, -\frac{4\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{c^4 e^9} - \frac{1}{e^9 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{7/2}} \\
& 3 \times 2^{2+p} \times 7^{-p} d^2 e^{-\frac{7a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^7 \text{Gamma}\left[1+p, -\frac{7\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} + \\
& \frac{28 \times 3^{-p} d^3 e^{-\frac{3a}{b}} \text{Gamma}\left[1+p, -\frac{3\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{c^3 e^9} - \frac{1}{e^9 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{5/2}} \\
& 21 \times 2^{1+p} \times 5^{-p} d^4 e^{-\frac{5a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^5 \text{Gamma}\left[1+p, -\frac{5\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} + \\
& \frac{21 \times 2^{1-p} d^5 e^{-\frac{2a}{b}} \text{Gamma}\left[1+p, -\frac{2\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{c^2 e^9} - \frac{1}{e^9 \left(c \left(d + \frac{e}{x^{1/3}}\right)^2\right)^{3/2}} \\
& 7 \times 2^{2+p} \times 3^{-p} d^6 e^{-\frac{3a}{2b}} \left(d + \frac{e}{x^{1/3}}\right)^3 \text{Gamma}\left[1+p, -\frac{3\left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)}{2b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} + \\
& \frac{12 d^7 e^{-\frac{a}{b}} \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}}{c e^9} - \frac{1}{e^9 \sqrt{c \left(d + \frac{e}{x^{1/3}}\right)^2}} \\
& 3 \times 2^p d^8 e^{-\frac{a}{2b}} \left(d + \frac{e}{x^{1/3}}\right) \text{Gamma}\left[1+p, -\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{2b}\right] \left(a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b \text{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}
\end{aligned}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^4} dx$$

Problem 619: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[f x^p] \operatorname{Log}[1 + e x^m]}{x} dx$$

Optimal (type 4, 33 leaves, 2 steps):

$$-\frac{\operatorname{Log}[f x^p] \operatorname{PolyLog}[2, -e x^m]}{m} + \frac{p \operatorname{PolyLog}[3, -e x^m]}{m^2}$$

Result (type 4, 160 leaves):

$$\frac{1}{6 m^2} \left(-m^3 p \operatorname{Log}[x]^3 - 3 m^2 p \operatorname{Log}[x]^2 \operatorname{Log}\left[\frac{e + x^{-m}}{e}\right] + 3 m^2 p \operatorname{Log}[x]^2 \operatorname{Log}[1 + e x^m] - 6 m p \operatorname{Log}[x] \operatorname{Log}[-e x^m] \operatorname{Log}[1 + e x^m] + \right. \\ \left. 6 m \operatorname{Log}[-e x^m] \operatorname{Log}[f x^p] \operatorname{Log}[1 + e x^m] + 6 m p \operatorname{Log}[x] \operatorname{PolyLog}[2, -\frac{x^{-m}}{e}] + 6 m (-p \operatorname{Log}[x] + \operatorname{Log}[f x^p]) \operatorname{PolyLog}[2, 1 + e x^m] + 6 p \operatorname{PolyLog}[3, -\frac{x^{-m}}{e}] \right)$$

Problem 620: Result more than twice size of optimal antiderivative.

$$\int \frac{x^{-1+m} \operatorname{Log}[f x^p]^2}{d + e x^m} dx$$

Optimal (type 4, 75 leaves, 3 steps):

$$\frac{\operatorname{Log}[f x^p]^2 \operatorname{Log}\left[1 + \frac{e x^m}{d}\right]}{e m} + \frac{2 p \operatorname{Log}[f x^p] \operatorname{PolyLog}[2, -\frac{e x^m}{d}]}{e m^2} - \frac{2 p^2 \operatorname{PolyLog}[3, -\frac{e x^m}{d}]}{e m^3}$$

Result (type 4, 210 leaves):

$$\frac{1}{3 e m^3} \left(m^3 p^2 \operatorname{Log}[x]^3 + 3 m^2 p^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{d x^{-m}}{e}\right] - 3 m^2 p^2 \operatorname{Log}[x]^2 \operatorname{Log}[d + e x^m] + \right. \\ \left. 6 m p^2 \operatorname{Log}[x] \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[d + e x^m] - 6 m p \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[f x^p] \operatorname{Log}[d + e x^m] + 3 m^2 \operatorname{Log}[f x^p]^2 \operatorname{Log}[d + e x^m] - \right. \\ \left. 6 m p^2 \operatorname{Log}[x] \operatorname{PolyLog}[2, -\frac{d x^{-m}}{e}] + 6 m p (p \operatorname{Log}[x] - \operatorname{Log}[f x^p]) \operatorname{PolyLog}[2, 1 + \frac{e x^m}{d}] - 6 p^2 \operatorname{PolyLog}[3, -\frac{d x^{-m}}{e}] \right)$$

Problem 621: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[f x^p]^3 (a + b \operatorname{Log}[c (d + e x^m)^n])}{x} dx$$

Optimal (type 4, 161 leaves, 6 steps):

$$\frac{\text{Log}[f x^p]^4 (a + b \text{Log}[c (d + e x^m)^n])}{4 p} - \frac{b n \text{Log}[f x^p]^4 \text{Log}\left[1 + \frac{e x^m}{d}\right]}{4 p} - \frac{b n \text{Log}[f x^p]^3 \text{PolyLog}\left[2, -\frac{e x^m}{d}\right]}{m} +$$

$$\frac{3 b n p \text{Log}[f x^p]^2 \text{PolyLog}\left[3, -\frac{e x^m}{d}\right]}{m^2} - \frac{6 b n p^2 \text{Log}[f x^p] \text{PolyLog}\left[4, -\frac{e x^m}{d}\right]}{m^3} + \frac{6 b n p^3 \text{PolyLog}\left[5, -\frac{e x^m}{d}\right]}{m^4}$$

Result (type 4, 659 leaves):

$$-\frac{3}{10} b m n p^3 \text{Log}[x]^5 + \frac{3}{4} b m n p^2 \text{Log}[x]^4 \text{Log}[f x^p] - \frac{1}{2} b m n p \text{Log}[x]^3 \text{Log}[f x^p]^2 + \frac{a \text{Log}[f x^p]^4}{4 p} -$$

$$\frac{3}{4} b n p^3 \text{Log}[x]^4 \text{Log}\left[1 + \frac{d x^{-m}}{e}\right] + 2 b n p^2 \text{Log}[x]^3 \text{Log}[f x^p] \text{Log}\left[1 + \frac{d x^{-m}}{e}\right] - \frac{3}{2} b n p \text{Log}[x]^2 \text{Log}[f x^p]^2 \text{Log}\left[1 + \frac{d x^{-m}}{e}\right] +$$

$$b n p^3 \text{Log}[x]^4 \text{Log}[d + e x^m] - \frac{b n p^3 \text{Log}[x]^3 \text{Log}\left[-\frac{e x^m}{d}\right] \text{Log}[d + e x^m]}{m} - 3 b n p^2 \text{Log}[x]^3 \text{Log}[f x^p] \text{Log}[d + e x^m] +$$

$$\frac{3 b n p^2 \text{Log}[x]^2 \text{Log}\left[-\frac{e x^m}{d}\right] \text{Log}[f x^p] \text{Log}[d + e x^m]}{m} + 3 b n p \text{Log}[x]^2 \text{Log}[f x^p]^2 \text{Log}[d + e x^m] - \frac{3 b n p \text{Log}[x] \text{Log}\left[-\frac{e x^m}{d}\right] \text{Log}[f x^p]^2 \text{Log}[d + e x^m]}{m} -$$

$$b n \text{Log}[x] \text{Log}[f x^p]^3 \text{Log}[d + e x^m] + \frac{b n \text{Log}\left[-\frac{e x^m}{d}\right] \text{Log}[f x^p]^3 \text{Log}[d + e x^m]}{m} - \frac{1}{4} b p^3 \text{Log}[x]^4 \text{Log}[c (d + e x^m)^n] +$$

$$b p^2 \text{Log}[x]^3 \text{Log}[f x^p] \text{Log}[c (d + e x^m)^n] - \frac{3}{2} b p \text{Log}[x]^2 \text{Log}[f x^p]^2 \text{Log}[c (d + e x^m)^n] + b \text{Log}[x] \text{Log}[f x^p]^3 \text{Log}[c (d + e x^m)^n] +$$

$$\frac{b n p \text{Log}[x] (p^2 \text{Log}[x]^2 - 3 p \text{Log}[x] \text{Log}[f x^p] + 3 \text{Log}[f x^p]^2) \text{PolyLog}\left[2, -\frac{d x^{-m}}{e}\right]}{m} - \frac{b n (p \text{Log}[x] - \text{Log}[f x^p])^3 \text{PolyLog}\left[2, 1 + \frac{e x^m}{d}\right]}{m} +$$

$$\frac{3 b n p \text{Log}[f x^p]^2 \text{PolyLog}\left[3, -\frac{d x^{-m}}{e}\right]}{m^2} + \frac{6 b n p^2 \text{Log}[f x^p] \text{PolyLog}\left[4, -\frac{d x^{-m}}{e}\right]}{m^3} + \frac{6 b n p^3 \text{PolyLog}\left[5, -\frac{d x^{-m}}{e}\right]}{m^4}$$

Problem 622: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[f x^p]^2 (a + b \text{Log}[c (d + e x^m)^n])}{x} dx$$

Optimal (type 4, 132 leaves, 5 steps):

$$\frac{\text{Log}[f x^p]^3 (a + b \text{Log}[c (d + e x^m)^n])}{3 p} - \frac{b n \text{Log}[f x^p]^3 \text{Log}\left[1 + \frac{e x^m}{d}\right]}{3 p} -$$

$$\frac{b n \text{Log}[f x^p]^2 \text{PolyLog}\left[2, -\frac{e x^m}{d}\right]}{m} + \frac{2 b n p \text{Log}[f x^p] \text{PolyLog}\left[3, -\frac{e x^m}{d}\right]}{m^2} - \frac{2 b n p^2 \text{PolyLog}\left[4, -\frac{e x^m}{d}\right]}{m^3}$$

Result (type 4, 456 leaves):

$$\begin{aligned} & \frac{1}{4} b m n p^2 \operatorname{Log}[x]^4 - \frac{1}{3} b m n p \operatorname{Log}[x]^3 \operatorname{Log}[f x^p] + \frac{a \operatorname{Log}[f x^p]^3}{3 p} + \frac{2}{3} b n p^2 \operatorname{Log}[x]^3 \operatorname{Log}\left[1 + \frac{d x^{-m}}{e}\right] - \\ & b n p \operatorname{Log}[x]^2 \operatorname{Log}[f x^p] \operatorname{Log}\left[1 + \frac{d x^{-m}}{e}\right] - b n p^2 \operatorname{Log}[x]^3 \operatorname{Log}[d + e x^m] + \frac{b n p^2 \operatorname{Log}[x]^2 \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[d + e x^m]}{m} + \\ & 2 b n p \operatorname{Log}[x]^2 \operatorname{Log}[f x^p] \operatorname{Log}[d + e x^m] - \frac{2 b n p \operatorname{Log}[x] \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[f x^p] \operatorname{Log}[d + e x^m]}{m} - b n \operatorname{Log}[x] \operatorname{Log}[f x^p]^2 \operatorname{Log}[d + e x^m] + \\ & \frac{b n \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[f x^p]^2 \operatorname{Log}[d + e x^m]}{m} + \frac{1}{3} b p^2 \operatorname{Log}[x]^3 \operatorname{Log}[c (d + e x^m)^n] - b p \operatorname{Log}[x]^2 \operatorname{Log}[f x^p] \operatorname{Log}[c (d + e x^m)^n] + \\ & b \operatorname{Log}[x] \operatorname{Log}[f x^p]^2 \operatorname{Log}[c (d + e x^m)^n] - \frac{b n p \operatorname{Log}[x] (p \operatorname{Log}[x] - 2 \operatorname{Log}[f x^p]) \operatorname{PolyLog}\left[2, -\frac{d x^{-m}}{e}\right]}{m} + \\ & \frac{b n (-p \operatorname{Log}[x] + \operatorname{Log}[f x^p])^2 \operatorname{PolyLog}\left[2, 1 + \frac{e x^m}{d}\right]}{m} + \frac{2 b n p \operatorname{Log}[f x^p] \operatorname{PolyLog}\left[3, -\frac{d x^{-m}}{e}\right]}{m^2} + \frac{2 b n p^2 \operatorname{PolyLog}\left[4, -\frac{d x^{-m}}{e}\right]}{m^3} \end{aligned}$$

Problem 623: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[f x^p] (a + b \operatorname{Log}[c (d + e x^m)^n])}{x} dx$$

Optimal (type 4, 102 leaves, 4 steps):

$$\frac{\operatorname{Log}[f x^p]^2 (a + b \operatorname{Log}[c (d + e x^m)^n])}{2 p} - \frac{b n \operatorname{Log}[f x^p]^2 \operatorname{Log}\left[1 + \frac{e x^m}{d}\right]}{2 p} - \frac{b n \operatorname{Log}[f x^p] \operatorname{PolyLog}\left[2, -\frac{e x^m}{d}\right]}{m} + \frac{b n p \operatorname{PolyLog}\left[3, -\frac{e x^m}{d}\right]}{m^2}$$

Result (type 4, 265 leaves):

$$\begin{aligned} & -\frac{1}{6} b m n p \operatorname{Log}[x]^3 + \frac{a \operatorname{Log}[f x^p]^2}{2 p} - \frac{1}{2} b n p \operatorname{Log}[x]^2 \operatorname{Log}\left[1 + \frac{d x^{-m}}{e}\right] + b n p \operatorname{Log}[x]^2 \operatorname{Log}[d + e x^m] - \frac{b n p \operatorname{Log}[x] \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[d + e x^m]}{m} - \\ & b n \operatorname{Log}[x] \operatorname{Log}[f x^p] \operatorname{Log}[d + e x^m] + \frac{b n \operatorname{Log}\left[-\frac{e x^m}{d}\right] \operatorname{Log}[f x^p] \operatorname{Log}[d + e x^m]}{m} - \frac{1}{2} b p \operatorname{Log}[x]^2 \operatorname{Log}[c (d + e x^m)^n] + \\ & b \operatorname{Log}[x] \operatorname{Log}[f x^p] \operatorname{Log}[c (d + e x^m)^n] + \frac{b n p \operatorname{Log}[x] \operatorname{PolyLog}\left[2, -\frac{d x^{-m}}{e}\right]}{m} - \frac{b n (p \operatorname{Log}[x] - \operatorname{Log}[f x^p]) \operatorname{PolyLog}\left[2, 1 + \frac{e x^m}{d}\right]}{m} + \frac{b n p \operatorname{PolyLog}\left[3, -\frac{d x^{-m}}{e}\right]}{m^2} \end{aligned}$$

Problem 628: Unable to integrate problem.

$$\int \operatorname{Log}[c (d + e (f + g x)^p)^q] dx$$

Optimal (type 5, 76 leaves, 3 steps):

$$-\frac{e p q (f+g x)^{1+p} \operatorname{Hypergeometric2F1}\left[1, 1+\frac{1}{p}, 2+\frac{1}{p}, -\frac{e(f+g x)^p}{d}\right]}{d g (1+p)} + \frac{(f+g x) \operatorname{Log}\left[c(d+e(f+g x)^p)^q\right]}{g}$$

Result (type 8, 18 leaves):

$$\int \operatorname{Log}\left[c(d+e(f+g x)^p)^q\right] dx$$

Problem 636: Result more than twice size of optimal antiderivative.

$$\int \left(a + b \operatorname{Log}\left[c\left(d + \frac{e}{f+g x}\right)^p\right]\right)^4 dx$$

Optimal (type 4, 221 leaves, 8 steps):

$$\begin{aligned} & -\frac{4 b e p \operatorname{Log}\left[-\frac{e}{d(f+g x)}\right] \left(a + b \operatorname{Log}\left[c\left(d + \frac{e}{f+g x}\right)^p\right]\right)^3}{d g} + \\ & \frac{(e+d(f+g x)) \left(a + b \operatorname{Log}\left[c\left(d + \frac{e}{f+g x}\right)^p\right]\right)^4}{d g} - \frac{12 b^2 e p^2 \left(a + b \operatorname{Log}\left[c\left(d + \frac{e}{f+g x}\right)^p\right]\right)^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d(f+g x)}\right]}{d g} + \\ & \frac{24 b^3 e p^3 \left(a + b \operatorname{Log}\left[c\left(d + \frac{e}{f+g x}\right)^p\right]\right) \operatorname{PolyLog}\left[3, 1 + \frac{e}{d(f+g x)}\right]}{d g} - \frac{24 b^4 e p^4 \operatorname{PolyLog}\left[4, 1 + \frac{e}{d(f+g x)}\right]}{d g} \end{aligned}$$

Result (type 4, 732 leaves):

$$\begin{aligned}
& \frac{1}{d g} \left(-4 b p \left(d f \operatorname{Log}[f+g x] - (e+d f) \operatorname{Log}[e+d f+d g x] - d g x \operatorname{Log}\left[\frac{e+d f+d g x}{f+g x}\right] \right) \left(a - b p \operatorname{Log}\left[d + \frac{e}{f+g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x}\right)^p\right] \right)^3 + \right. \\
& d g x \left(a - b p \operatorname{Log}\left[d + \frac{e}{f+g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x}\right)^p\right] \right)^4 + \\
& 6 b^2 p^2 \left(a - b p \operatorname{Log}\left[d + \frac{e}{f+g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x}\right)^p\right] \right)^2 \left(d f \operatorname{Log}\left[\frac{f}{g} + x\right]^2 + (e+d f) \operatorname{Log}\left[\frac{e+d f+d g x}{d g}\right]^2 + d g x \operatorname{Log}\left[\frac{e+d f+d g x}{f+g x}\right]^2 - \right. \\
& 2 (d f \operatorname{Log}[f+g x] - (e+d f) \operatorname{Log}[e+d f+d g x]) \left(\operatorname{Log}\left[\frac{f}{g} + x\right] - \operatorname{Log}\left[\frac{e+d f+d g x}{d g}\right] + \operatorname{Log}\left[\frac{e+d f+d g x}{f+g x}\right] \right) - 2 (e+d f) \\
& \left. \left(\operatorname{Log}\left[\frac{f}{g} + x\right] \operatorname{Log}\left[\frac{e+d f+d g x}{e}\right] + \operatorname{PolyLog}\left[2, -\frac{d(f+g x)}{e}\right] \right) - 2 d f \left(\operatorname{Log}\left[-\frac{d(f+g x)}{e}\right] \operatorname{Log}\left[\frac{e+d f+d g x}{d g}\right] + \operatorname{PolyLog}\left[2, \frac{e+d f+d g x}{e}\right] \right) \right) + \\
& 4 b^3 p^3 \left(a - b p \operatorname{Log}\left[d + \frac{e}{f+g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x}\right)^p\right] \right) \left(\operatorname{Log}\left[d + \frac{e}{f+g x}\right]^2 \left(-3 e \operatorname{Log}\left[-\frac{e}{d f+d g x}\right] + (e+d f+d g x) \operatorname{Log}\left[d + \frac{e}{f+g x}\right] \right) - \right. \\
& 6 e \operatorname{Log}\left[d + \frac{e}{f+g x}\right] \operatorname{PolyLog}\left[2, 1 + \frac{e}{d f+d g x}\right] + 6 e \operatorname{PolyLog}\left[3, 1 + \frac{e}{d f+d g x}\right] \left. \right) - \\
& b^4 p^4 \left(4 e \operatorname{Log}\left[-\frac{e}{d f+d g x}\right] \operatorname{Log}\left[d + \frac{e}{f+g x}\right]^3 - e \operatorname{Log}\left[d + \frac{e}{f+g x}\right]^4 - d (f+g x) \operatorname{Log}\left[d + \frac{e}{f+g x}\right]^4 + \right. \\
& \left. 12 e \operatorname{Log}\left[d + \frac{e}{f+g x}\right]^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d f+d g x}\right] - 24 e \operatorname{Log}\left[d + \frac{e}{f+g x}\right] \operatorname{PolyLog}\left[3, 1 + \frac{e}{d f+d g x}\right] + 24 e \operatorname{PolyLog}\left[4, 1 + \frac{e}{d f+d g x}\right] \right) \left. \right)
\end{aligned}$$

Problem 637: Result more than twice size of optimal antiderivative.

$$\int \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x} \right)^p \right] \right)^3 dx$$

Optimal (type 4, 168 leaves, 7 steps):

$$\begin{aligned}
& - \frac{3 b e p \operatorname{Log}\left[-\frac{e}{d(f+g x)}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x} \right)^p \right] \right)^2}{d g} + \frac{(e+d(f+g x)) \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x} \right)^p \right] \right)^3}{d g} - \\
& \frac{6 b^2 e p^2 \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f+g x} \right)^p \right] \right) \operatorname{PolyLog}\left[2, 1 + \frac{e}{d(f+g x)}\right]}{d g} + \frac{6 b^3 e p^3 \operatorname{PolyLog}\left[3, 1 + \frac{e}{d(f+g x)}\right]}{d g}
\end{aligned}$$

Result (type 4, 441 leaves):

$$\frac{1}{dg} \left(3 b d p (f + g x) \operatorname{Log}\left[d + \frac{e}{f + g x}\right] \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^2 + d (f + g x) \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^3 + 3 b e p \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^2 \operatorname{Log}[e + d (f + g x)] + 3 b^2 p^2 \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right) \left(d (f + g x) \operatorname{Log}\left[d + \frac{e}{f + g x}\right]^2 + e \left(\operatorname{Log}\left[\frac{e}{d} + f + g x\right]^2 + 2 \left(\operatorname{Log}[f + g x] - \operatorname{Log}\left[\frac{e}{d} + f + g x\right] + \operatorname{Log}\left[d + \frac{e}{f + g x}\right] \right) \operatorname{Log}[e + d (f + g x)] - 2 \left(\operatorname{Log}[f + g x] \operatorname{Log}\left[1 + \frac{d (f + g x)}{e}\right] + \operatorname{PolyLog}\left[2, -\frac{d (f + g x)}{e}\right] \right) \right) \right) + b^3 p^3 \left(\operatorname{Log}\left[d + \frac{e}{f + g x}\right]^2 \left(-3 e \operatorname{Log}\left[-\frac{e}{d f + d g x}\right] + (e + d f + d g x) \operatorname{Log}\left[d + \frac{e}{f + g x}\right] \right) - 6 e \operatorname{Log}\left[d + \frac{e}{f + g x}\right] \operatorname{PolyLog}\left[2, 1 + \frac{e}{d f + d g x}\right] + 6 e \operatorname{PolyLog}\left[3, 1 + \frac{e}{d f + d g x}\right] \right)$$

Problem 638: Result more than twice size of optimal antiderivative.

$$\int \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^2 dx$$

Optimal (type 4, 115 leaves, 5 steps):

$$-\frac{2 b e p \operatorname{Log}\left[-\frac{e}{d (f + g x)}\right] \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)}{d g} + \frac{(e + d (f + g x)) \left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^2}{d g} - \frac{2 b^2 e p^2 \operatorname{PolyLog}\left[2, 1 + \frac{e}{d (f + g x)}\right]}{d g}$$

Result (type 4, 250 leaves):

$$\frac{1}{d g} \left(d (f + g x) \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right)^2 + 2 b p \left(a - b p \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + b \operatorname{Log}\left[c \left(d + \frac{e}{f + g x}\right)^p\right] \right) \left(d (f + g x) \operatorname{Log}\left[d + \frac{e}{f + g x}\right] + e \operatorname{Log}[e + d (f + g x)] \right) + b^2 p^2 \left(d (f + g x) \operatorname{Log}\left[d + \frac{e}{f + g x}\right]^2 + e \left(\operatorname{Log}\left[\frac{e}{d} + f + g x\right]^2 + 2 \left(\operatorname{Log}[f + g x] - \operatorname{Log}\left[\frac{e}{d} + f + g x\right] + \operatorname{Log}\left[d + \frac{e}{f + g x}\right] \right) \operatorname{Log}[e + d (f + g x)] - 2 \left(\operatorname{Log}[f + g x] \operatorname{Log}\left[1 + \frac{d (f + g x)}{e}\right] + \operatorname{PolyLog}\left[2, -\frac{d (f + g x)}{e}\right] \right) \right) \right)$$

Test results for the 314 problems in "3.5 Logarithm functions.m"

Problem 39: Attempted integration timed out after 120 seconds.

$$\int \frac{n q - \text{Log}[c x^n]}{(a x + b \text{Log}[c x^n]^q)^2} dx$$

Optimal (type 9, 60 leaves, 1 step):

$$-\frac{n(1-q) \text{CannotIntegrate}\left[\frac{1}{x(a x + b \text{Log}[c x^n]^q)}, x\right]}{a} + \frac{\text{Log}[c x^n]}{a(a x + b \text{Log}[c x^n]^q)}$$

Result (type 1, 1 leaves):

???

Problem 40: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{2x\left(d\sqrt{-\frac{e}{d}}+ex\right)}{d+ex^2}\right]}{d+ex^2} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$-\frac{\sqrt{-\frac{e}{d}} \text{PolyLog}\left[2, 1 - \frac{2x\left(d\sqrt{-\frac{e}{d}}+ex\right)}{d+ex^2}\right]}{2e}$$

Result (type 4, 686 leaves):

$$\frac{1}{4\sqrt{d}\sqrt{e}}$$

$$\left(-4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 - \right.$$

$$4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] - 2i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] -$$

$$2i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{Log}\left[-\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] \operatorname{Log}\left[\frac{\sqrt{d}\sqrt{e} - iex}{\sqrt{d}\sqrt{e} + id\sqrt{-\frac{e}{d}}}\right] - 2i \operatorname{Log}\left[-\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] \operatorname{Log}\left[\frac{\sqrt{d}\sqrt{e} + iex}{\sqrt{d}\sqrt{e} - id\sqrt{-\frac{e}{d}}}\right] +$$

$$4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2x\left(d\sqrt{-\frac{e}{d}} + ex\right)}{d + ex^2}\right] - 2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] -$$

$$2i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{d\sqrt{-\frac{e}{d}} + ex}{-i\sqrt{d}\sqrt{e} + d\sqrt{-\frac{e}{d}}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{d\sqrt{-\frac{e}{d}} + ex}{i\sqrt{d}\sqrt{e} + d\sqrt{-\frac{e}{d}}}\right] \left. \right)$$

Problem 41: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[-\frac{2x\left(d\sqrt{-\frac{e}{d}} - ex\right)}{d + ex^2}\right]}{d + ex^2} dx$$

Optimal (type 4, 50 leaves, 1 step):

$$\frac{\sqrt{-\frac{e}{d}} \operatorname{PolyLog}\left[2, 1 + \frac{2x\left(d\sqrt{-\frac{e}{d}} - ex\right)}{d + ex^2}\right]}{2e}$$

Result (type 4, 674 leaves):

$$\frac{1}{4\sqrt{d}\sqrt{e}}$$

$$\left(\begin{aligned} & -4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 - \\ & 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] - 2i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - \\ & 2i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 2i \operatorname{Log}\left[\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] \operatorname{Log}\left[\frac{-i\sqrt{d}\sqrt{e} + ex}{-i\sqrt{d}\sqrt{e} + d\sqrt{-\frac{e}{d}}}\right] + 2i \operatorname{Log}\left[\frac{1}{\sqrt{-\frac{e}{d}}} + x\right] \operatorname{Log}\left[\frac{\sqrt{e} - \frac{ix}{\sqrt{d}}}{\sqrt{e} - i\sqrt{d}\sqrt{-\frac{e}{d}}}\right] + \\ & 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2ex\left(\frac{1}{\sqrt{-\frac{e}{d}}} + x\right)}{d + ex^2}\right] - 2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + \\ & 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{e}\left(\frac{1}{\sqrt{-\frac{e}{d}}} + x\right)}{-i\sqrt{d} + \frac{\sqrt{e}}{\sqrt{-\frac{e}{d}}}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{e}\left(\frac{1}{\sqrt{-\frac{e}{d}}} + x\right)}{i\sqrt{d} + \frac{\sqrt{e}}{\sqrt{-\frac{e}{d}}}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] \end{aligned} \right)$$

Problem 42: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{2x\left(\frac{d\sqrt{e}}{\sqrt{-d}} + ex\right)}{d + ex^2}\right]}{d + ex^2} dx$$

Optimal (type 4, 53 leaves, 1 step):

$$\frac{\text{PolyLog}\left[2, 1 + \frac{2\sqrt{e}x(\sqrt{-d}-\sqrt{e}x)}{d+ex^2}\right]}{2\sqrt{-d}\sqrt{e}}$$

Result (type 4, 654 leaves):

$$\begin{aligned} & \frac{1}{4\sqrt{d}\sqrt{e}} \left(-4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] - 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{\sqrt{-d}}{\sqrt{e}} + x\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + \right. \\ & 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 - 2i \operatorname{Log}\left[-\frac{\sqrt{-d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{-i\sqrt{d} + \sqrt{e}x}{\sqrt{-d} - i\sqrt{d}}\right] + 2i \operatorname{Log}\left[-\frac{\sqrt{-d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{i\sqrt{d} + \sqrt{e}x}{\sqrt{-d} + i\sqrt{d}}\right] - \\ & 2i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - \\ & 2i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2(-\sqrt{-d}\sqrt{e}x + ex^2)}{d+ex^2}\right] - 2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] - \\ & \left. 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{-d} - \sqrt{e}x}{\sqrt{-d} - i\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{-d} - \sqrt{e}x}{\sqrt{-d} + i\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] \right) \end{aligned}$$

Problem 43: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[-\frac{2x\left(\frac{d\sqrt{e}}{\sqrt{-d}} - ex\right)}{d+ex^2}\right]}{d+ex^2} dx$$

Optimal (type 4, 52 leaves, 1 step):

$$\frac{\text{PolyLog}\left[2, 1 - \frac{2\sqrt{e}x(\sqrt{-d}+\sqrt{e}x)}{d+ex^2}\right]}{2\sqrt{-d}\sqrt{e}}$$

Result (type 4, 651 leaves):

$$\begin{aligned}
& \frac{1}{4\sqrt{d}\sqrt{e}} \left(-4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] - 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{\sqrt{-d}}{\sqrt{e}} + x\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + \right. \\
& 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 - 2i \operatorname{Log}\left[\frac{\sqrt{-d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{i(\sqrt{d} + i\sqrt{e}x)}{\sqrt{-d} + i\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{\sqrt{-d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[-\frac{i\sqrt{d} + \sqrt{e}x}{\sqrt{-d} - i\sqrt{d}}\right] - \\
& 2i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - \\
& 2i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2(\sqrt{-d}\sqrt{e}x + ex^2)}{d + ex^2}\right] - 2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + \\
& \left. 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{-d} + \sqrt{e}x}{\sqrt{-d} - i\sqrt{d}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{\sqrt{-d} + \sqrt{e}x}{\sqrt{-d} + i\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] \right)
\end{aligned}$$

Problem 44: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{2x(\sqrt{d}\sqrt{-e} + ex)}{d + ex^2}\right]}{d + ex^2} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{\operatorname{PolyLog}\left[2, 1 - \frac{2x(\sqrt{d}\sqrt{-e} + ex)}{d + ex^2}\right]}{2\sqrt{d}\sqrt{-e}}$$

Result (type 4, 701 leaves):

$$\frac{1}{4\sqrt{d}\sqrt{e}}$$

$$\left(-4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 - \right.$$

$$4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{\sqrt{d}e}{(-e)^{3/2}} + x\right] + 2i \operatorname{Log}\left[\frac{\sqrt{d}e}{(-e)^{3/2}} + x\right] \operatorname{Log}\left[\frac{\sqrt{-e}(\sqrt{d} - i\sqrt{e}x)}{\sqrt{d}(\sqrt{-e} - i\sqrt{e})}\right] - 2i \operatorname{Log}\left[\frac{\sqrt{d}e}{(-e)^{3/2}} + x\right] \operatorname{Log}\left[\frac{\sqrt{-e}(\sqrt{d} + i\sqrt{e}x)}{\sqrt{d}(\sqrt{-e} + i\sqrt{e})}\right] -$$

$$2i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 2i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] +$$

$$4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2x(\sqrt{d}\sqrt{-e} + ex)}{d + ex^2}\right] - 2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}(-\sqrt{d} + \sqrt{-e}x)}{\sqrt{d}(\sqrt{-e} - i\sqrt{e})}\right] -$$

$$2i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}(-\sqrt{d} + \sqrt{-e}x)}{\sqrt{d}(\sqrt{-e} + i\sqrt{e})}\right] + 2i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] - 2i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] \Big)$$

Problem 45: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[-\frac{2x(\sqrt{d}\sqrt{-e} - ex)}{d + ex^2}\right]}{d + ex^2} dx$$

Optimal (type 4, 50 leaves, 1 step):

$$-\frac{\operatorname{PolyLog}\left[2, 1 + \frac{2x(\sqrt{d}\sqrt{-e} - ex)}{d + ex^2}\right]}{2\sqrt{d}\sqrt{-e}}$$

Result (type 4, 695 leaves):

$$\begin{aligned}
& \frac{1}{4\sqrt{d}\sqrt{e}} \left(-4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[x] - 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{\sqrt{d}}{\sqrt{-e}} + x\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] + \right. \\
& i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] - i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right]^2 + 2 i \operatorname{Log}\left[\frac{\sqrt{d}}{\sqrt{-e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{-e}(\sqrt{d} - i\sqrt{e}x)}{\sqrt{d}(\sqrt{-e} + i\sqrt{e})}\right] - \\
& 2 i \operatorname{Log}\left[\frac{\sqrt{d}}{\sqrt{-e}} + x\right] \operatorname{Log}\left[\frac{\sqrt{-e}(\sqrt{d} + i\sqrt{e}x)}{\sqrt{d}(\sqrt{-e} - i\sqrt{e})}\right] - 2 i \operatorname{Log}\left[-\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + 2 i \operatorname{Log}\left[\frac{i\sqrt{d}}{\sqrt{e}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] + \\
& 2 i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 2 i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i\sqrt{e}x}{\sqrt{d}}\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{2x(-\sqrt{d}\sqrt{-e} + ex)}{d + ex^2}\right] - \\
& 2 i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}x}{\sqrt{d}}\right] + 2 i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}x}{\sqrt{d}}\right] - 2 i \operatorname{PolyLog}\left[2, -\frac{i\sqrt{e}(\sqrt{d} + \sqrt{-e}x)}{\sqrt{d}(\sqrt{-e} - i\sqrt{e})}\right] + \\
& \left. 2 i \operatorname{PolyLog}\left[2, \frac{i\sqrt{e}(\sqrt{d} + \sqrt{-e}x)}{\sqrt{d}(\sqrt{-e} + i\sqrt{e})}\right] + 2 i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i\sqrt{e}x}{2\sqrt{d}}\right] - 2 i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i\sqrt{e}x}{2\sqrt{d}}\right] \right)
\end{aligned}$$

Problem 93: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[d(a + bx + cx^2)^n]}{ae + bex + cex^2} dx$$

Optimal (type 4, 258 leaves, 8 steps):

$$\begin{aligned}
& \frac{2n \operatorname{ArcTanh}\left[\frac{b+2cx}{\sqrt{b^2-4ac}}\right]^2 - 4n \operatorname{ArcTanh}\left[\frac{b+2cx}{\sqrt{b^2-4ac}}\right] \operatorname{Log}\left[\frac{2}{1 - \frac{b}{\sqrt{b^2-4ac}} - \frac{2cx}{\sqrt{b^2-4ac}}}\right]}{\sqrt{b^2-4ac}e} - \frac{2n \operatorname{PolyLog}\left[2, -\frac{1 + \frac{b}{\sqrt{b^2-4ac}} + \frac{2cx}{\sqrt{b^2-4ac}}}{1 - \frac{b}{\sqrt{b^2-4ac}} - \frac{2cx}{\sqrt{b^2-4ac}}}\right]}{\sqrt{b^2-4ac}e}
\end{aligned}$$

Result (type 4, 555 leaves):

$$\begin{aligned}
& - \frac{1}{2\sqrt{-(b^2-4ac)^2}e} \left(4\sqrt{b^2-4ac} \operatorname{nArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] - \right. \\
& \quad \left. \sqrt{-b^2+4ac} \operatorname{nLog}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right]^2 + 4\sqrt{b^2-4ac} \operatorname{nArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] - \right. \\
& \quad \left. 2\sqrt{-b^2+4ac} \operatorname{nLog}\left[\frac{-b+\sqrt{b^2-4ac}-2cx}{2\sqrt{b^2-4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] + \sqrt{-b^2+4ac} \operatorname{nLog}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right]^2 + \right. \\
& \quad \left. 2\sqrt{-b^2+4ac} \operatorname{nLog}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2\sqrt{b^2-4ac}}\right] - 4\sqrt{b^2-4ac} \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}[d(a+x(b+cx))^n] + \right. \\
& \quad \left. 2\sqrt{-b^2+4ac} \operatorname{nPolyLog}\left[2, \frac{-b+\sqrt{b^2-4ac}-2cx}{2\sqrt{b^2-4ac}}\right] - 2\sqrt{-b^2+4ac} \operatorname{nPolyLog}\left[2, \frac{b+\sqrt{b^2-4ac}+2cx}{2\sqrt{b^2-4ac}}\right] \right)
\end{aligned}$$

Problem 94: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[g(a+bx+cx^2)^n]}{d+ex^2} dx$$

Optimal (type 4, 762 leaves, 20 steps):

$$\begin{aligned}
& \frac{\operatorname{nLog}\left[\frac{\sqrt{e}(b-\sqrt{b^2-4ac}+2cx)}{2c\sqrt{-d}+(b-\sqrt{b^2-4ac})\sqrt{e}}\right] \operatorname{Log}[\sqrt{-d}-\sqrt{e}x]}{2\sqrt{-d}\sqrt{e}} - \frac{\operatorname{nLog}\left[\frac{\sqrt{e}(b+\sqrt{b^2-4ac}+2cx)}{2c\sqrt{-d}+(b+\sqrt{b^2-4ac})\sqrt{e}}\right] \operatorname{Log}[\sqrt{-d}-\sqrt{e}x]}{2\sqrt{-d}\sqrt{e}} + \\
& \frac{\operatorname{nLog}\left[-\frac{\sqrt{e}(b-\sqrt{b^2-4ac}+2cx)}{2c\sqrt{-d}-(b-\sqrt{b^2-4ac})\sqrt{e}}\right] \operatorname{Log}[\sqrt{-d}+\sqrt{e}x]}{2\sqrt{-d}\sqrt{e}} + \frac{\operatorname{nLog}\left[-\frac{\sqrt{e}(b+\sqrt{b^2-4ac}+2cx)}{2c\sqrt{-d}-(b+\sqrt{b^2-4ac})\sqrt{e}}\right] \operatorname{Log}[\sqrt{-d}+\sqrt{e}x]}{2\sqrt{-d}\sqrt{e}} + \\
& \frac{\operatorname{Log}[\sqrt{-d}-\sqrt{e}x] \operatorname{Log}[g(a+bx+cx^2)^n]}{2\sqrt{-d}\sqrt{e}} - \frac{\operatorname{Log}[\sqrt{-d}+\sqrt{e}x] \operatorname{Log}[g(a+bx+cx^2)^n]}{2\sqrt{-d}\sqrt{e}} - \frac{\operatorname{nPolyLog}\left[2, \frac{2c(\sqrt{-d}-\sqrt{e}x)}{2c\sqrt{-d}+(b-\sqrt{b^2-4ac})\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} \\
& \frac{\operatorname{nPolyLog}\left[2, \frac{2c(\sqrt{-d}-\sqrt{e}x)}{2c\sqrt{-d}+(b+\sqrt{b^2-4ac})\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} + \frac{\operatorname{nPolyLog}\left[2, \frac{2c(\sqrt{-d}+\sqrt{e}x)}{2c\sqrt{-d}-(b-\sqrt{b^2-4ac})\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}} + \frac{\operatorname{nPolyLog}\left[2, \frac{2c(\sqrt{-d}+\sqrt{e}x)}{2c\sqrt{-d}-(b+\sqrt{b^2-4ac})\sqrt{e}}\right]}{2\sqrt{-d}\sqrt{e}}
\end{aligned}$$

Result (type 4, 736 leaves):

$$\begin{aligned}
& - \frac{1}{2\sqrt{d}\sqrt{e}} \left(2n \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{b - \sqrt{b^2 - 4ac}}{2c} + x\right] + \right. \\
& 2n \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}\left[\frac{b + \sqrt{b^2 - 4ac} + 2cx}{2c}\right] - i n \operatorname{Log}\left[\frac{b - \sqrt{b^2 - 4ac}}{2c} + x\right] \operatorname{Log}\left[\frac{2c(\sqrt{d} - i\sqrt{e}x)}{2c\sqrt{d} - i(-b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] - \\
& i n \operatorname{Log}\left[\frac{b + \sqrt{b^2 - 4ac} + 2cx}{2c}\right] \operatorname{Log}\left[\frac{2c(\sqrt{d} - i\sqrt{e}x)}{2c\sqrt{d} + i(b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] + i n \operatorname{Log}\left[\frac{b - \sqrt{b^2 - 4ac}}{2c} + x\right] \operatorname{Log}\left[\frac{2c(\sqrt{d} + i\sqrt{e}x)}{2c\sqrt{d} + i(-b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] + \\
& i n \operatorname{Log}\left[\frac{b + \sqrt{b^2 - 4ac} + 2cx}{2c}\right] \operatorname{Log}\left[\frac{2c(\sqrt{d} + i\sqrt{e}x)}{2c\sqrt{d} - i(b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] - 2 \operatorname{ArcTan}\left[\frac{\sqrt{e}x}{\sqrt{d}}\right] \operatorname{Log}[g(a + x(b + cx))^n] + \\
& i n \operatorname{PolyLog}\left[2, \frac{\sqrt{e}(-b + \sqrt{b^2 - 4ac} - 2cx)}{-2ic\sqrt{d} + (-b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] - i n \operatorname{PolyLog}\left[2, \frac{\sqrt{e}(-b + \sqrt{b^2 - 4ac} - 2cx)}{2ic\sqrt{d} + (-b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] - \\
& \left. i n \operatorname{PolyLog}\left[2, \frac{\sqrt{e}(b + \sqrt{b^2 - 4ac} + 2cx)}{-2ic\sqrt{d} + (b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] + i n \operatorname{PolyLog}\left[2, \frac{\sqrt{e}(b + \sqrt{b^2 - 4ac} + 2cx)}{2ic\sqrt{d} + (b + \sqrt{b^2 - 4ac})\sqrt{e}}\right] \right)
\end{aligned}$$

Problem 97: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Log}[d(a + bx + cx^2)^n]^2 dx$$

Optimal (type 4, 587 leaves, 27 steps):

$$\begin{aligned}
& 8 n^2 x - \frac{4 \sqrt{b^2 - 4 a c} n^2 \operatorname{ArcTanh}\left[\frac{b+2 c x}{\sqrt{b^2 - 4 a c}}\right]}{c} - \frac{(b - \sqrt{b^2 - 4 a c}) n^2 \operatorname{Log}[b - \sqrt{b^2 - 4 a c} + 2 c x]^2}{2 c} - \\
& \frac{(b + \sqrt{b^2 - 4 a c}) n^2 \operatorname{Log}\left[-\frac{b - \sqrt{b^2 - 4 a c} + 2 c x}{2 \sqrt{b^2 - 4 a c}}\right] \operatorname{Log}[b + \sqrt{b^2 - 4 a c} + 2 c x]}{c} - \frac{(b + \sqrt{b^2 - 4 a c}) n^2 \operatorname{Log}[b + \sqrt{b^2 - 4 a c} + 2 c x]^2}{2 c} - \\
& \frac{(b - \sqrt{b^2 - 4 a c}) n^2 \operatorname{Log}[b - \sqrt{b^2 - 4 a c} + 2 c x] \operatorname{Log}\left[\frac{b + \sqrt{b^2 - 4 a c} + 2 c x}{2 \sqrt{b^2 - 4 a c}}\right]}{c} - \frac{2 b n^2 \operatorname{Log}[a + b x + c x^2]}{c} - 4 n x \operatorname{Log}[d (a + b x + c x^2)^n] + \\
& \frac{(b - \sqrt{b^2 - 4 a c}) n \operatorname{Log}[b - \sqrt{b^2 - 4 a c} + 2 c x] \operatorname{Log}[d (a + b x + c x^2)^n]}{c} + \frac{(b + \sqrt{b^2 - 4 a c}) n \operatorname{Log}[b + \sqrt{b^2 - 4 a c} + 2 c x] \operatorname{Log}[d (a + b x + c x^2)^n]}{c} + \\
& x \operatorname{Log}[d (a + b x + c x^2)^n]^2 - \frac{(b - \sqrt{b^2 - 4 a c}) n^2 \operatorname{PolyLog}\left[2, -\frac{b - \sqrt{b^2 - 4 a c} + 2 c x}{2 \sqrt{b^2 - 4 a c}}\right]}{c} - \frac{(b + \sqrt{b^2 - 4 a c}) n^2 \operatorname{PolyLog}\left[2, \frac{b + \sqrt{b^2 - 4 a c} + 2 c x}{2 \sqrt{b^2 - 4 a c}}\right]}{c}
\end{aligned}$$

Result (type 4, 1447 leaves):

$$\begin{aligned}
& \frac{1}{2c\sqrt{-b^2+4ac}} \\
& \left(8b\sqrt{-b^2+4ac}n^2 + 16c\sqrt{-b^2+4ac}n^2x + 4\sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] - 4b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] + \right. \\
& 4b^2n^2 \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] - 16acn^2 \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] - \\
& \sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right]^2 + b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right]^2 - 4\sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] - \\
& 4b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] + 4b^2n^2 \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] - \\
& 16acn^2 \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] - 2\sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{-b+\sqrt{b^2-4ac}-2cx}{2\sqrt{b^2-4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] + \\
& 2b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{-b+\sqrt{b^2-4ac}-2cx}{2\sqrt{b^2-4ac}}\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] + \sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right]^2 + \\
& b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right]^2 + 2\sqrt{-(b^2-4ac)^2}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2\sqrt{b^2-4ac}}\right] + \\
& 2b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2\sqrt{b^2-4ac}}\right] - 2b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b-\sqrt{b^2-4ac}}{2c}+x\right] \operatorname{Log}[a+x(b+cx)] - \\
& 2b\sqrt{-b^2+4ac}n^2 \operatorname{Log}\left[\frac{b+\sqrt{b^2-4ac}+2cx}{2c}\right] \operatorname{Log}[a+x(b+cx)] - 8c\sqrt{-b^2+4ac}nx \operatorname{Log}[d(a+x(b+cx))^n] - \\
& 4b^2n \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}[d(a+x(b+cx))^n] + 16acn \operatorname{ArcTan}\left[\frac{b+2cx}{\sqrt{-b^2+4ac}}\right] \operatorname{Log}[d(a+x(b+cx))^n] + \\
& 2b\sqrt{-b^2+4ac}n \operatorname{Log}[a+x(b+cx)] \operatorname{Log}[d(a+x(b+cx))^n] + 2c\sqrt{-b^2+4ac}x \operatorname{Log}[d(a+x(b+cx))^n]^2 + \\
& 2\left(\sqrt{-(b^2-4ac)^2} + b\sqrt{-b^2+4ac}\right)n^2 \operatorname{PolyLog}\left[2, \frac{-b+\sqrt{b^2-4ac}-2cx}{2\sqrt{b^2-4ac}}\right] - \\
& 2\left(\sqrt{-(b^2-4ac)^2} - b\sqrt{-b^2+4ac}\right)n^2 \operatorname{PolyLog}\left[2, \frac{b+\sqrt{b^2-4ac}+2cx}{2\sqrt{b^2-4ac}}\right] \Big)
\end{aligned}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[-1+x+x^2]^2}{x^3} dx$$

Optimal (type 4, 443 leaves, 34 steps):

$$\begin{aligned} & \text{Log}[x] - \frac{1}{2} (1 + \sqrt{5}) \text{Log}[1 - \sqrt{5} + 2x] + 3 \text{Log}\left[\frac{1}{2} (-1 + \sqrt{5})\right] \text{Log}[1 - \sqrt{5} + 2x] - \frac{1}{4} (3 + \sqrt{5}) \text{Log}[1 - \sqrt{5} + 2x]^2 - \\ & \frac{1}{2} (1 - \sqrt{5}) \text{Log}[1 + \sqrt{5} + 2x] - \frac{1}{2} (3 - \sqrt{5}) \text{Log}\left[-\frac{1 - \sqrt{5} + 2x}{2\sqrt{5}}\right] \text{Log}[1 + \sqrt{5} + 2x] - \frac{1}{4} (3 - \sqrt{5}) \text{Log}[1 + \sqrt{5} + 2x]^2 - \\ & \frac{1}{2} (3 + \sqrt{5}) \text{Log}[1 - \sqrt{5} + 2x] \text{Log}\left[\frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] + 3 \text{Log}[x] \text{Log}\left[1 + \frac{2x}{1 + \sqrt{5}}\right] + \frac{\text{Log}[-1 + x + x^2]}{x} - 3 \text{Log}[x] \text{Log}[-1 + x + x^2] + \\ & \frac{1}{2} (3 + \sqrt{5}) \text{Log}[1 - \sqrt{5} + 2x] \text{Log}[-1 + x + x^2] + \frac{1}{2} (3 - \sqrt{5}) \text{Log}[1 + \sqrt{5} + 2x] \text{Log}[-1 + x + x^2] - \frac{\text{Log}[-1 + x + x^2]^2}{2x^2} + \\ & 3 \text{PolyLog}\left[2, -\frac{2x}{1 + \sqrt{5}}\right] - \frac{1}{2} (3 + \sqrt{5}) \text{PolyLog}\left[2, -\frac{1 - \sqrt{5} + 2x}{2\sqrt{5}}\right] - \frac{1}{2} (3 - \sqrt{5}) \text{PolyLog}\left[2, \frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] - 3 \text{PolyLog}\left[2, 1 + \frac{2x}{1 - \sqrt{5}}\right] \end{aligned}$$

Result (type 4, 955 leaves):

$$\begin{aligned}
& \frac{1}{20} \left(-10 \operatorname{Log}[-1 + \sqrt{5} - 2x] - 10\sqrt{5} \operatorname{Log}[-1 + \sqrt{5} - 2x] + 20 \operatorname{Log}[x] + 2\sqrt{5} \operatorname{Log}[100] \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] - \right. \\
& 30 \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] - 10\sqrt{5} \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] + 60 \operatorname{Log}[x] \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] - \\
& 60 \operatorname{Log}\left[\frac{2x}{-1 + \sqrt{5}}\right] \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] + 15 \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right]^2 + 5\sqrt{5} \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right]^2 + \sqrt{5} \operatorname{Log}[8] \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] - \\
& 30 \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] - 10\sqrt{5} \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] + \\
& 15 \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right]^2 - 2\sqrt{5} \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right]^2 - 10 \operatorname{Log}[1 + \sqrt{5} + 2x] + 10\sqrt{5} \operatorname{Log}[1 + \sqrt{5} + 2x] - \\
& 30 \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] \operatorname{Log}[1 + \sqrt{5} + 2x] + 10\sqrt{5} \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] \operatorname{Log}[1 + \sqrt{5} + 2x] - 30 \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] \operatorname{Log}[1 + \sqrt{5} + 2x] + \\
& 7\sqrt{5} \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] \operatorname{Log}[1 + \sqrt{5} + 2x] + 30 \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] \operatorname{Log}\left[\frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] - 6\sqrt{5} \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] \operatorname{Log}\left[\frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] + \\
& 30 \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] \operatorname{Log}\left[\frac{1}{10}(5 - \sqrt{5} - 2\sqrt{5}x)\right] + 10\sqrt{5} \operatorname{Log}\left[\frac{1}{2}(1 + \sqrt{5}) + x\right] \operatorname{Log}\left[\frac{1}{10}(5 - \sqrt{5} - 2\sqrt{5}x)\right] - \\
& 4\sqrt{5} \operatorname{Log}\left[\frac{1}{2} - \frac{\sqrt{5}}{2} + x\right] \operatorname{Log}[5 + \sqrt{5} + 2\sqrt{5}x] + 60 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{2x}{1 + \sqrt{5}}\right] + \frac{20 \operatorname{Log}[-1 + x + x^2]}{x} + 30 \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}[-1 + x + x^2] + \\
& 10\sqrt{5} \operatorname{Log}[-1 + \sqrt{5} - 2x] \operatorname{Log}[-1 + x + x^2] - 60 \operatorname{Log}[x] \operatorname{Log}[-1 + x + x^2] + 30 \operatorname{Log}[1 + \sqrt{5} + 2x] \operatorname{Log}[-1 + x + x^2] - \\
& 10\sqrt{5} \operatorname{Log}[1 + \sqrt{5} + 2x] \operatorname{Log}[-1 + x + x^2] - \frac{10 \operatorname{Log}[-1 + x + x^2]^2}{x^2} - 10(-3 + \sqrt{5}) \operatorname{PolyLog}\left[2, \frac{-1 + \sqrt{5} - 2x}{2\sqrt{5}}\right] - \\
& \left. 60 \operatorname{PolyLog}\left[2, \frac{-1 + \sqrt{5} - 2x}{-1 + \sqrt{5}}\right] + 60 \operatorname{PolyLog}\left[2, -\frac{2x}{1 + \sqrt{5}}\right] + 30 \operatorname{PolyLog}\left[2, \frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] + 10\sqrt{5} \operatorname{PolyLog}\left[2, \frac{1 + \sqrt{5} + 2x}{2\sqrt{5}}\right] \right)
\end{aligned}$$

Problem 108: Result unnecessarily involves imaginary or complex numbers.

$$\int x^{3/2} \operatorname{Log}[-1 + 4x + 4\sqrt{(-1+x)x}] dx$$

Optimal (type 3, 187 leaves, 15 steps):

$$\begin{aligned}
& -\frac{\sqrt{x}}{160} + \frac{x^{3/2}}{60} - \frac{2x^{5/2}}{25} - \frac{17\sqrt{-x+x^2}}{32\sqrt{x}} - \frac{71(-x+x^2)^{3/2}}{300x^{3/2}} - \frac{2(-x+x^2)^{3/2}}{25\sqrt{x}} - \\
& \frac{\sqrt{-x+x^2} \operatorname{ArcTan}\left[\frac{2}{3}\sqrt{2}\sqrt{-1+x}\right]}{320\sqrt{2}\sqrt{-1+x}\sqrt{x}} + \frac{\operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right]}{320\sqrt{2}} + \frac{2}{5}x^{5/2} \operatorname{Log}[-1 + 4x + 4\sqrt{-x+x^2}]
\end{aligned}$$

Result (type 3, 232 leaves):

$$\frac{1}{38400} \left(-240 \sqrt{x} + 640 x^{3/2} - 3072 x^{5/2} - \frac{11312 \sqrt{(-1+x)x}}{\sqrt{x}} - 6016 \sqrt{x} \sqrt{(-1+x)x} - 3072 x^{3/2} \sqrt{(-1+x)x} + 60 \sqrt{2} \operatorname{ArcTan}[2 \sqrt{2} \sqrt{x}] - \right.$$

$$60 \sqrt{2} \operatorname{ArcTan}\left[\frac{2 \sqrt{2} \sqrt{(-1+x)x}}{3 \sqrt{x}}\right] - 30 i \sqrt{2} \operatorname{Log}[4(1+8x)^2] + 15 i \sqrt{2} \operatorname{Log}[(1+8x)(1-10x-6\sqrt{(-1+x)x})] +$$

$$\left. 15360 x^{5/2} \operatorname{Log}[-1+4x+4\sqrt{(-1+x)x}] + 15 i \sqrt{2} \operatorname{Log}[(1+8x)(1-10x+6\sqrt{(-1+x)x})] \right)$$

Problem 109: Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{x} \operatorname{Log}[-1+4x+4\sqrt{(-1+x)x}] dx$$

Optimal (type 3, 158 leaves, 13 steps):

$$\frac{\sqrt{x}}{12} - \frac{2x^{3/2}}{9} - \frac{11\sqrt{-x+x^2}}{12\sqrt{x}} - \frac{2(-x+x^2)^{3/2}}{9x^{3/2}} + \frac{\sqrt{-x+x^2} \operatorname{ArcTan}\left[\frac{2}{3}\sqrt{2}\sqrt{-1+x}\right]}{24\sqrt{2}\sqrt{-1+x}\sqrt{x}} - \frac{\operatorname{ArcTan}[2\sqrt{2}\sqrt{x}]}{24\sqrt{2}} + \frac{2}{3}x^{3/2} \operatorname{Log}[-1+4x+4\sqrt{-x+x^2}]$$

Result (type 3, 209 leaves):

$$\frac{1}{576} \left(48 \sqrt{x} - 128 x^{3/2} - \frac{400 \sqrt{(-1+x)x}}{\sqrt{x}} - 128 \sqrt{x} \sqrt{(-1+x)x} - 12 \sqrt{2} \operatorname{ArcTan}[2 \sqrt{2} \sqrt{x}] + \right.$$

$$12 \sqrt{2} \operatorname{ArcTan}\left[\frac{2 \sqrt{2} \sqrt{(-1+x)x}}{3 \sqrt{x}}\right] + 6 i \sqrt{2} \operatorname{Log}[4(1+8x)^2] - 3 i \sqrt{2} \operatorname{Log}[(1+8x)(1-10x-6\sqrt{(-1+x)x})] +$$

$$\left. 384 x^{3/2} \operatorname{Log}[-1+4x+4\sqrt{(-1+x)x}] - 3 i \sqrt{2} \operatorname{Log}[(1+8x)(1-10x+6\sqrt{(-1+x)x})] \right)$$

Problem 110: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}[-1+4x+4\sqrt{(-1+x)x}]}{\sqrt{x}} dx$$

Optimal (type 3, 118 leaves, 12 steps):

$$-2\sqrt{x} - \frac{2\sqrt{-x+x^2}}{\sqrt{x}} - \frac{\sqrt{-x+x^2} \operatorname{ArcTan}\left[\frac{2}{3}\sqrt{2}\sqrt{-1+x}\right]}{\sqrt{2}\sqrt{-1+x}\sqrt{x}} + \frac{\operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right]}{\sqrt{2}} + 2\sqrt{x} \operatorname{Log}\left[-1+4x+4\sqrt{-x+x^2}\right]$$

Result (type 3, 186 leaves):

$$\frac{1}{8} \left(-16\sqrt{x} - \frac{16\sqrt{(-1+x)x}}{\sqrt{x}} + 4\sqrt{2} \operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right] - 4\sqrt{2} \operatorname{ArcTan}\left[\frac{2\sqrt{2}\sqrt{(-1+x)x}}{3\sqrt{x}}\right] - 2i\sqrt{2} \operatorname{Log}\left[4(1+8x)^2\right] + \right. \\ \left. i\sqrt{2} \operatorname{Log}\left[(1+8x)\left(1-10x-6\sqrt{(-1+x)x}\right)\right] + 16\sqrt{x} \operatorname{Log}\left[-1+4x+4\sqrt{(-1+x)x}\right] + i\sqrt{2} \operatorname{Log}\left[(1+8x)\left(1-10x+6\sqrt{(-1+x)x}\right)\right] \right)$$

Problem 111: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}\left[-1+4x+4\sqrt{(-1+x)x}\right]}{x^{3/2}} dx$$

Optimal (type 3, 114 leaves, 15 steps):

$$-\frac{4\sqrt{2}\sqrt{-x+x^2} \operatorname{ArcTan}\left[\frac{2}{3}\sqrt{2}\sqrt{-1+x}\right]}{\sqrt{-1+x}\sqrt{x}} + 4\sqrt{2} \operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right] - 8 \operatorname{ArcTan}\left[\frac{\sqrt{x}}{\sqrt{-x+x^2}}\right] - \frac{2 \operatorname{Log}\left[-1+4x+4\sqrt{-x+x^2}\right]}{\sqrt{x}}$$

Result (type 3, 177 leaves):

$$4\sqrt{2} \operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right] + 8 \operatorname{ArcTan}\left[\frac{\sqrt{(-1+x)x}}{\sqrt{x}}\right] - 4\sqrt{2} \operatorname{ArcTan}\left[\frac{2\sqrt{2}\sqrt{(-1+x)x}}{3\sqrt{x}}\right] - 2i\sqrt{2} \operatorname{Log}\left[4(1+8x)^2\right] + \\ i\sqrt{2} \operatorname{Log}\left[(1+8x)\left(1-10x-6\sqrt{(-1+x)x}\right)\right] - \frac{2 \operatorname{Log}\left[-1+4x+4\sqrt{(-1+x)x}\right]}{\sqrt{x}} + i\sqrt{2} \operatorname{Log}\left[(1+8x)\left(1-10x+6\sqrt{(-1+x)x}\right)\right]$$

Problem 112: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Log}\left[-1+4x+4\sqrt{(-1+x)x}\right]}{x^{5/2}} dx$$

Optimal (type 3, 151 leaves, 18 steps):

$$-\frac{16}{3\sqrt{x}} + \frac{4\sqrt{-x+x^2}}{3x^{3/2}} + \frac{32\sqrt{2}\sqrt{-x+x^2}\operatorname{ArcTan}\left[\frac{2}{3}\sqrt{2}\sqrt{-1+x}\right]}{3\sqrt{-1+x}\sqrt{x}} -$$

$$\frac{32}{3}\sqrt{2}\operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right] + \frac{44}{3}\operatorname{ArcTan}\left[\frac{\sqrt{x}}{\sqrt{-x+x^2}}\right] - \frac{2\operatorname{Log}\left[-1+4x+4\sqrt{-x+x^2}\right]}{3x^{3/2}}$$

Result (type 3, 204 leaves):

$$\frac{2}{3}\left(-\frac{8}{\sqrt{x}} + \frac{2\sqrt{(-1+x)x}}{x^{3/2}} - 16\sqrt{2}\operatorname{ArcTan}\left[2\sqrt{2}\sqrt{x}\right] - 22\operatorname{ArcTan}\left[\frac{\sqrt{(-1+x)x}}{\sqrt{x}}\right] + 16\sqrt{2}\operatorname{ArcTan}\left[\frac{2\sqrt{2}\sqrt{(-1+x)x}}{3\sqrt{x}}\right] + 8i\sqrt{2}\operatorname{Log}\left[4(1+8x)^2\right] -\right.$$

$$\left.4i\sqrt{2}\operatorname{Log}\left[(1+8x)\left(1-10x-6\sqrt{(-1+x)x}\right)\right] - \frac{\operatorname{Log}\left[-1+4x+4\sqrt{(-1+x)x}\right]}{x^{3/2}} - 4i\sqrt{2}\operatorname{Log}\left[(1+8x)\left(1-10x+6\sqrt{(-1+x)x}\right)\right]\right)$$

Problem 118: Unable to integrate problem.

$$\int x^3 \operatorname{Log}\left[1 + e^{(f^c (a+bx))^n}\right] dx$$

Optimal (type 4, 132 leaves, 5 steps):

$$-\frac{x^3 \operatorname{PolyLog}\left[2, -e^{(f^c (a+bx))^n}\right]}{bcn \operatorname{Log}[f]} + \frac{3x^2 \operatorname{PolyLog}\left[3, -e^{(f^c (a+bx))^n}\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2} - \frac{6x \operatorname{PolyLog}\left[4, -e^{(f^c (a+bx))^n}\right]}{b^3 c^3 n^3 \operatorname{Log}[f]^3} + \frac{6 \operatorname{PolyLog}\left[5, -e^{(f^c (a+bx))^n}\right]}{b^4 c^4 n^4 \operatorname{Log}[f]^4}$$

Result (type 8, 22 leaves):

$$\int x^3 \operatorname{Log}\left[1 + e^{(f^c (a+bx))^n}\right] dx$$

Problem 119: Unable to integrate problem.

$$\int x^2 \operatorname{Log}\left[1 + e^{(f^c (a+bx))^n}\right] dx$$

Optimal (type 4, 98 leaves, 4 steps):

$$-\frac{x^2 \operatorname{PolyLog}\left[2, -e^{(f^c (a+bx))^n}\right]}{bcn \operatorname{Log}[f]} + \frac{2x \operatorname{PolyLog}\left[3, -e^{(f^c (a+bx))^n}\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2} - \frac{2 \operatorname{PolyLog}\left[4, -e^{(f^c (a+bx))^n}\right]}{b^3 c^3 n^3 \operatorname{Log}[f]^3}$$

Result (type 8, 22 leaves):

$$\int x^2 \operatorname{Log}\left[1 + e^{(f^c (a+bx))^n}\right] dx$$

Problem 120: Unable to integrate problem.

$$\int x \operatorname{Log}\left[1 + e\left(f^{c(a+bx)}\right)^n\right] dx$$

Optimal (type 4, 63 leaves, 3 steps):

$$-\frac{x \operatorname{PolyLog}\left[2, -e\left(f^{c(a+bx)}\right)^n\right]}{b c n \operatorname{Log}[f]} + \frac{\operatorname{PolyLog}\left[3, -e\left(f^{c(a+bx)}\right)^n\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2}$$

Result (type 8, 20 leaves):

$$\int x \operatorname{Log}\left[1 + e\left(f^{c(a+bx)}\right)^n\right] dx$$

Problem 121: Attempted integration timed out after 120 seconds.

$$\int \operatorname{Log}\left[1 + e\left(f^{c(a+bx)}\right)^n\right] dx$$

Optimal (type 4, 31 leaves, 2 steps):

$$-\frac{\operatorname{PolyLog}\left[2, -e\left(f^{c(a+bx)}\right)^n\right]}{b c n \operatorname{Log}[f]}$$

Result (type 1, 1 leaves):

???

Problem 123: Unable to integrate problem.

$$\int x^3 \operatorname{Log}\left[d + e\left(f^{c(a+bx)}\right)^n\right] dx$$

Optimal (type 4, 193 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{4} x^4 \operatorname{Log}\left[d + e\left(f^{c(a+bx)}\right)^n\right] - \frac{1}{4} x^4 \operatorname{Log}\left[1 + \frac{e\left(f^{c(a+bx)}\right)^n}{d}\right] - \frac{x^3 \operatorname{PolyLog}\left[2, -\frac{e\left(f^{c(a+bx)}\right)^n}{d}\right]}{b c n \operatorname{Log}[f]} + \\ & \frac{3 x^2 \operatorname{PolyLog}\left[3, -\frac{e\left(f^{c(a+bx)}\right)^n}{d}\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2} - \frac{6 x \operatorname{PolyLog}\left[4, -\frac{e\left(f^{c(a+bx)}\right)^n}{d}\right]}{b^3 c^3 n^3 \operatorname{Log}[f]^3} + \frac{6 \operatorname{PolyLog}\left[5, -\frac{e\left(f^{c(a+bx)}\right)^n}{d}\right]}{b^4 c^4 n^4 \operatorname{Log}[f]^4} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^3 \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Problem 124: Unable to integrate problem.

$$\int x^2 \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Optimal (type 4, 156 leaves, 5 steps):

$$\frac{1}{3} x^3 \operatorname{Log}[d + e (f^{c(a+bx)})^n] - \frac{1}{3} x^3 \operatorname{Log}\left[1 + \frac{e (f^{c(a+bx)})^n}{d}\right] - \frac{x^2 \operatorname{PolyLog}\left[2, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b c n \operatorname{Log}[f]} + \frac{2 x \operatorname{PolyLog}\left[3, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2} - \frac{2 \operatorname{PolyLog}\left[4, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b^3 c^3 n^3 \operatorname{Log}[f]^3}$$

Result (type 8, 22 leaves):

$$\int x^2 \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Problem 125: Unable to integrate problem.

$$\int x \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Optimal (type 4, 118 leaves, 4 steps):

$$\frac{1}{2} x^2 \operatorname{Log}[d + e (f^{c(a+bx)})^n] - \frac{1}{2} x^2 \operatorname{Log}\left[1 + \frac{e (f^{c(a+bx)})^n}{d}\right] - \frac{x \operatorname{PolyLog}\left[2, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b c n \operatorname{Log}[f]} + \frac{\operatorname{PolyLog}\left[3, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b^2 c^2 n^2 \operatorname{Log}[f]^2}$$

Result (type 8, 20 leaves):

$$\int x \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Problem 126: Attempted integration timed out after 120 seconds.

$$\int \operatorname{Log}[d + e (f^{c(a+bx)})^n] dx$$

Optimal (type 4, 75 leaves, 4 steps):

$$x \operatorname{Log}[d + e (f^{c(a+bx)})^n] - x \operatorname{Log}\left[1 + \frac{e (f^{c(a+bx)})^n}{d}\right] - \frac{\operatorname{PolyLog}\left[2, -\frac{e (f^{c(a+bx)})^n}{d}\right]}{b c n \operatorname{Log}[f]}$$

Result (type 1, 1 leaves):

???

Problem 128: Attempted integration timed out after 120 seconds.

$$\int \text{Log}[b (F^{e(c+dx)})^n + \pi] dx$$

Optimal (type 4, 39 leaves, 3 steps):

$$x \text{Log}[\pi] - \frac{\text{PolyLog}\left[2, -\frac{b(F^{e(c+dx)})^n}{\pi}\right]}{d e n \text{Log}[F]}$$

Result (type 1, 1 leaves):

???

Problem 131: Result more than twice size of optimal antiderivative.

$$\int \frac{(1 + \text{Log}[x])^5}{x} dx$$

Optimal (type 3, 10 leaves, 2 steps):

$$\frac{1}{6} (1 + \text{Log}[x])^6$$

Result (type 3, 39 leaves):

$$\text{Log}[x] + \frac{5 \text{Log}[x]^2}{2} + \frac{10 \text{Log}[x]^3}{3} + \frac{5 \text{Log}[x]^4}{2} + \text{Log}[x]^5 + \frac{\text{Log}[x]^6}{6}$$

Problem 134: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{x \sqrt{-3 + \text{Log}[x]^2}} dx$$

Optimal (type 3, 14 leaves, 3 steps):

$$\text{ArcTanh}\left[\frac{\text{Log}[x]}{\sqrt{-3 + \text{Log}[x]^2}}\right]$$

Result (type 3, 42 leaves):

$$-\frac{1}{2} \operatorname{Log}\left[1 - \frac{\operatorname{Log}[x]}{\sqrt{-3 + \operatorname{Log}[x]^2}}\right] + \frac{1}{2} \operatorname{Log}\left[1 + \frac{\operatorname{Log}[x]}{\sqrt{-3 + \operatorname{Log}[x]^2}}\right]$$

Problem 189: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[x] \operatorname{Log}[\operatorname{Cos}[x]] \, dx$$

Optimal (type 3, 14 leaves, 4 steps):

$$\operatorname{ArcTanh}[\operatorname{Sin}[x]] - \operatorname{Sin}[x] + \operatorname{Log}[\operatorname{Cos}[x]] \operatorname{Sin}[x]$$

Result (type 3, 43 leaves):

$$-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{x}{2}\right] - \operatorname{Sin}\left[\frac{x}{2}\right]\right] + \operatorname{Log}\left[\operatorname{Cos}\left[\frac{x}{2}\right] + \operatorname{Sin}\left[\frac{x}{2}\right]\right] - \operatorname{Sin}[x] + \operatorname{Log}[\operatorname{Cos}[x]] \operatorname{Sin}[x]$$

Problem 277: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}[c(1+x^2)^n]}{1+x^2} \, dx$$

Optimal (type 4, 60 leaves, 5 steps):

$$i n \operatorname{ArcTan}[x]^2 + 2 n \operatorname{ArcTan}[x] \operatorname{Log}\left[\frac{2}{1+i x}\right] + \operatorname{ArcTan}[x] \operatorname{Log}[c(1+x^2)^n] + i n \operatorname{PolyLog}\left[2, 1 - \frac{2}{1+i x}\right]$$

Result (type 4, 149 leaves):

$$\frac{1}{4} \left(-4 n \operatorname{ArcTan}[x] \operatorname{Log}[-i+x] - i n \operatorname{Log}[-i+x]^2 + 2 i n \operatorname{Log}[-i+x] \operatorname{Log}\left[-\frac{1}{2} i (i+x)\right] - 4 n \operatorname{ArcTan}[x] \operatorname{Log}[i+x] - \right. \\ \left. 2 i n \operatorname{Log}\left[\frac{1}{2} (1+i x)\right] \operatorname{Log}[i+x] + i n \operatorname{Log}[i+x]^2 + 4 \operatorname{ArcTan}[x] \operatorname{Log}[c(1+x^2)^n] + 2 i n \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i x}{2}\right] - 2 i n \operatorname{PolyLog}\left[2, -\frac{1}{2} i (i+x)\right] \right)$$

Problem 278: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{-x^2}{1+x^2}\right]}{1+x^2} \, dx$$

Optimal (type 4, 61 leaves, 5 steps):

$$i \operatorname{ArcTan}[x]^2 - 2 \operatorname{ArcTan}[x] \operatorname{Log}\left[2 - \frac{2}{1-i x}\right] + \operatorname{ArcTan}[x] \operatorname{Log}\left[\frac{x^2}{1+x^2}\right] + i \operatorname{PolyLog}\left[2, -1 + \frac{2}{1-i x}\right]$$

Result (type 4, 182 leaves):

$$\frac{1}{4} \left(i \operatorname{Log}[-i + x]^2 - i \operatorname{Log}[i + x]^2 + 4 \operatorname{ArcTan}[x] \left(-2 \operatorname{Log}[x] + \operatorname{Log}[-i + x] + \operatorname{Log}[i + x] + \operatorname{Log}\left[\frac{x^2}{1 + x^2}\right] \right) - \right. \\ \left. 2 i \left(\operatorname{Log}[-i + x] \operatorname{Log}\left[-\frac{1}{2} i (i + x)\right] + \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i x}{2}\right] \right) - 4 i \left(\operatorname{Log}[1 + i x] \operatorname{Log}[x] + \operatorname{PolyLog}\left[2, -i x\right] \right) + \right. \\ \left. 4 i \left(\operatorname{Log}[1 - i x] \operatorname{Log}[x] + \operatorname{PolyLog}\left[2, i x\right] \right) + 2 i \left(\operatorname{Log}\left[\frac{1}{2} (1 + i x)\right] \operatorname{Log}[i + x] + \operatorname{PolyLog}\left[2, -\frac{1}{2} i (i + x)\right] \right) \right)$$

Problem 279: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[\frac{c x^2}{a + b x^2}\right]}{a + b x^2} dx$$

Optimal (type 4, 165 leaves, 5 steps):

$$\frac{i \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right]^2}{\sqrt{a} \sqrt{b}} + \frac{\operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}\left[\frac{c x^2}{a + b x^2}\right]}{\sqrt{a} \sqrt{b}} - \frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}\left[2 - \frac{2\sqrt{a}}{\sqrt{a} - i\sqrt{b} x}\right]}{\sqrt{a} \sqrt{b}} + \frac{i \operatorname{PolyLog}\left[2, -1 + \frac{2\sqrt{a}}{\sqrt{a} - i\sqrt{b} x}\right]}{\sqrt{a} \sqrt{b}}$$

Result (type 4, 402 leaves):

$$\frac{1}{4 \sqrt{a} \sqrt{b}} \left(-8 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}[x] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] + \right. \\ \left. i \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 4 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] - i \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 - 2 i \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right. \\ \left. 2 i \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 i \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] - 4 i \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{a}}\right] \operatorname{Log}\left[\frac{c x^2}{a + b x^2}\right] - \right. \\ \left. 4 i \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 i \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 i \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] - 2 i \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right)$$

Problem 280: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[1 + \frac{i \sqrt{1 - a x}}{\sqrt{1 + a x}}\right]}{1 - a^2 x^2} dx$$

Optimal (type 4, 29 leaves, 1 step):

$$\frac{\operatorname{PolyLog}\left[2, -\frac{i \sqrt{1 - a x}}{\sqrt{1 + a x}}\right]}{a}$$

Result (type 4, 134 leaves):

$$\frac{1}{4a} \left(4 \operatorname{ArcTanh}[ax] \operatorname{Log}\left[1 + \frac{i\sqrt{1-ax}}{\sqrt{1+ax}}\right] + \operatorname{PolyLog}\left[2, -e^{-2\operatorname{ArcTanh}[ax]}\right] - 2 \left(\operatorname{ArcTanh}[ax] \left(\operatorname{Log}\left[1 + e^{-2\operatorname{ArcTanh}[ax]}\right] - \operatorname{Log}\left[1 - i e^{-\operatorname{ArcTanh}[ax]}\right] + \operatorname{Log}\left[1 + i e^{-\operatorname{ArcTanh}[ax]}\right] \right) - \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcTanh}[ax]}\right] + \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcTanh}[ax]}\right] \right) \right)$$

Problem 281: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Log}\left[1 - \frac{i\sqrt{1-ax}}{\sqrt{1+ax}}\right]}{1 - a^2 x^2} dx$$

Optimal (type 4, 29 leaves, 1 step):

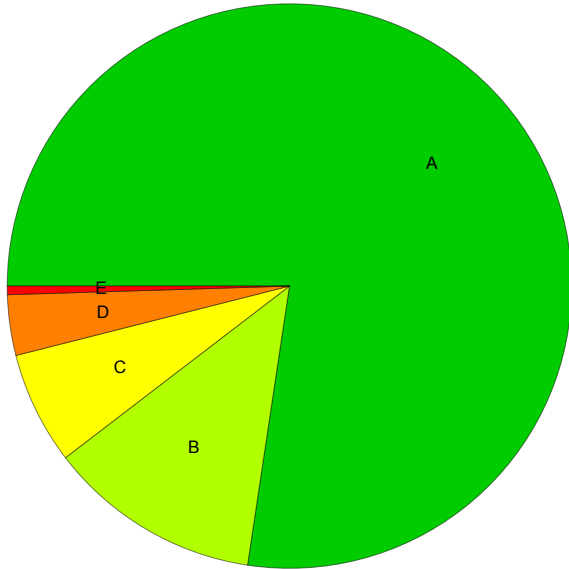
$$\frac{\operatorname{PolyLog}\left[2, \frac{i\sqrt{1-ax}}{\sqrt{1+ax}}\right]}{a}$$

Result (type 4, 134 leaves):

$$\frac{1}{4a} \left(4 \operatorname{ArcTanh}[ax] \operatorname{Log}\left[1 - \frac{i\sqrt{1-ax}}{\sqrt{1+ax}}\right] + \operatorname{PolyLog}\left[2, -e^{-2\operatorname{ArcTanh}[ax]}\right] - 2 \left(\operatorname{ArcTanh}[ax] \left(\operatorname{Log}\left[1 + e^{-2\operatorname{ArcTanh}[ax]}\right] + \operatorname{Log}\left[1 - i e^{-\operatorname{ArcTanh}[ax]}\right] - \operatorname{Log}\left[1 + i e^{-\operatorname{ArcTanh}[ax]}\right] \right) + \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcTanh}[ax]}\right] - \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcTanh}[ax]}\right] \right) \right)$$

Summary of Integration Test Results

3085 integration problems



A - 2387 optimal antiderivatives

B - 377 more than twice size of optimal antiderivatives

C - 199 unnecessarily complex antiderivatives

D - 107 unable to integrate problems

E - 15 integration timeouts